Connecting Subspace Learning and Extreme Learning Machine in Speech Emotion Recognition

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Abstract-Speech Emotion Recognition (SER) is a powerful tool for endowing computers with the capacity to process information about the affective states of users in human-machine interactions. Recent research has shown the effectiveness of graph embedding based subspace learning and extreme learning machine applied to SER, but there are still various drawbacks in these two techniques that limit their application. Regarding subspace learning, the change from linearity to nonlinearity is usually achieved through kernelisation, while extreme learning machines only take label information into consideration at the output layer. In order to overcome these drawbacks, this paper leverages extreme learning machine for dimensionality reduction and proposes a novel framework to combine spectral regression based subspace learning and extreme learning machine. The proposed framework contains three stages - data mapping, graph decomposition, and regression. At the data mapping stage, various mapping strategies provide different views of the samples. At the graph decomposition stage, specifically designed embedding graphs provide a possibility to better represent the structure of data, through generating virtual coordinates. Finally, at the regression stage, dimension-reduced mappings are achieved by connecting the virtual coordinates and data mapping. Using this framework, we propose several novel dimensionality reduction algorithms, apply them to SER tasks, and compare their performance to relevant state-of-the-art methods. Our results on several paralinguistic corpora show that our proposed techniques lead to significant improvements.

Index Terms—Speech emotion recognition, extreme learning machine, subspace learning, graph embedding, spectral regression.

I. INTRODUCTION

N many Machine Learning problems, particularly those involving real world applications, researchers have to deal with high or very high dimensional data, particularly in the

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context of 'Big Data' analytics [1]. Unfortunately, due to computational constraints, dealing with such large feature spaces can be impractical (if not impossible). Therefore, it is essential to explore alternative representations (i.e., lower dimensionality) that are computationally manageable whilst maintaining the relevant information about the original feature spaces. This need is apparent in many human-computer interaction tasks such as Speech Emotion Recognition (SER), which aims to detect emotional information conveyed by the human voice [2]–[5], but many of the typically used acoustic features contain information that may not be relevant for emotion recognition [6], [7]. Thus SER requires new methods for obtaining factors specifically related to emotional representation from large feature spaces [6], [8].

Motivated by this need, in recent years a multitude of techniques for dimensionality reduction have been proposed, and subspace learning has become a central topic in machine learning. Prominent algorithms in the field of pattern recognition are Graph Embedding (GE; [9], [10]) and Spectral Regression (SR; [11]–[13]). These two classes of algorithms include popular dimensionality reduction techniques, such as, Principal Component Analysis (PCA), Fisher Discriminant Analysis (FDA), Linear Discriminant Projections (LDP) [14], Locality Preserving Projections (LPP; [15]), Locally Discriminant Embedding (LDE; [16]), and Graph-based Fisher Analysis (GbFA; [17]), all of which can be seen as particular cases (i.e., graph structures) of a general GE framework [9], [10], [17]. At their core, both GE and SR utilise embedding graphs to calculate projections for optimal subspaces. However, GE computes these projections directly, whilst SR makes use of regression on spectral coordinates to calculate the projections with the goal of achieving computational efficiency and better performance [12], [13], [18], [19]. The linear and kernelised forms of GE and SR are known as Linear GE (LGE), Kernel GE (KGE) [10], Linear SR (LSR; [11], [13]) and Kernel SR (KSR; [20]), respectively.

A. Extreme Learning Machines

Recently, Extreme Learning Machines (ELMs) have been introduced as an alternative approach [21]–[26] for emotion recognition tasks [27], [28]. ELMs' working principles are similar to those of Single-hidden Layer Feedforward Neural Networks (SLFNs; [21], [24]). However, from an optimisation perspective, the calculation of the weights to the output layer in ELM is related to Support Vector Machines (SVMs), Least Square Support Vector Machines (LSSVM; [23], [25]), and Ridge Regression (RR; [29]–[31]). Compared to SLFNs, a

major advantage of ELMs is to generate the input to hidden layer weights directly without training, as well as adopting RR for hidden to output layer weights in order to increase computational speed [23], [25]. Motivated by the appealing characteristics of ELM and SR, various attempts have been made to apply ELM methods to subspace learning. For example, [30], [31] computed a low-dimensional space directly using spectral regression, while *Huang et al.* [32] and *Iosifidis et al.* [33] improved the optimisation procedures of ELMs by adding additional terms for regression.

In spite of the clear benefits of GE, SR, and ELM, there are evident *limitations* associated with the application of these methods in subspace learning. First, the nonlinear extension in GE and SR relies on kernelisation [10], [20], which in essence maps the original feature space to a new space represented by training samples. This process may lead to decreased performance when the training data maps the original features to a poorly represented space. Second, with respect to ELM, the calculation of the decision values at the output layer depends exclusively on the labels [21], [23], whereas the unsupervised relationship between training samples (addressed by most GE based methods, e.g., neighbouring information) is simply ignored. This leads to a limitation related to correctly representing the structure of data according to GE related methods [10], [15]–[17].

B. Overview of this paper

Inspired by previous work showing that ELM can be adapted for subspace learning by employing different optimisation structures [23], [25], [30]–[33], in this paper we propose a novel framework – *Generalised Spectral Regression* (GSR) – that exploits the relationships between ELM and subspace learning to overcome the above mentioned drawbacks associated with both methods.

We use this framework to design several embedding graphs for SER tasks at the stage of graph decomposition, which takes both of neighbouring and supervised information from training samples into consideration [16], [17], in order to construct suitable graph structures representing the inherent properties of the data. We argue that this makes the system more robust and effective by providing additional unsupervised information. Then, the proposed methods are evaluated and compared to other state-of-the-art methods in multiple SER tasks. The main contributions of this paper are:

- A new framework (GSR) for dimensionality reduction combining ELM and subspace learning;
- A set of novel feature reduction algorithms specifically developed to improve the performance of SER systems;
- A demonstration of the effectiveness of the proposed framework and methods in the context of SER, including a thorough comparison with existent methods.

The remainder of this paper is organised as follows. In Section II, we review the essential background for this work, including the notation used, and the basic principles of ELM, GE frameworks, and SR. In Section III, the proposed GSR framework is presented in detail, and the different GSR strategies developed are described in Section IV. Then, in

Section V, we introduce the experimental methodology, and in Section VI we evaluate the performance of the algorithms on multiple SER corpora. Finally, in Section VII we discuss our work, and propose future research directions.

II. BACKGROUND

In this section, we introduce the basic concepts, variables, and notations used throughout this article.

Let $X = [x_1, x_2, \ldots, x_N] \in \mathbb{R}^{n \times N}$ and $Y = [y_1, y_2, \ldots, y_N] \in \mathbb{R}^{d \times N}$ be sets of N labelled training samples in the original feature space with dimensionality n and the lower-dimensional feature space with the dimensionality d, respectively. Each column of $\phi(X) = [\phi(x_1), \phi(x_2), \ldots, \phi(x_N)]$ is the *Reproducing Kernel Hilbert Space* (RKHS) of the corresponding column in X. The Gram matrix K is defined as $\phi^T(X)\phi(X)$. It is assumed that all samples (training and test) in the original and reduced dimensionalities can be represented by column vectors $x \in \mathbb{R}^{n \times 1}$ and $y \in \mathbb{R}^{d \times 1}$, respectively. The RKHS of x is defined as $\phi(x)$. For sample x, its kernelised coordinate is $K_x = \phi^T(X)\phi(x)$.

Each column of the label matrix $S = [s_1, s_2, \ldots, s_N] = [\widehat{s}_1, \widehat{s}_2, \ldots, \widehat{s}_c]^T \in \Re^{c \times N}$ represents the labelling information of each training sample, where c is the number of classes. $S_{ij} = 1$ when sample j belongs to class i, otherwise $S_{ij} = 0$, where $i = 1, 2, \ldots, c$ and $j = 1, 2, \ldots, N$. $I \in \Re^{N \times N}$ is the identity matrix. Every element of $e \in \Re^{N \times 1}$ is equal to 1.

A. Extreme Learning Machines

ELM [21]–[24] assumes that L is the number of hidden neurons. $H = [h_1, h_2, \ldots, h_N] \in \Re^{L \times N}$ represents the outputs of the hidden neurons pertaining to the sets of N training samples, with each column representing one training sample in the feature space generated by the input nodes. The label coordinate matrix of extreme learning is $T = 2S^T - ee_c^T$, where each element of $e_c \in \Re^{c \times 1}$ is equal to 1. The hidden neurons' parameters are selected randomly [24], and the activation functions of these hidden neurons can be sigmoidal, hard limit or Gaussian (for more details please refer to [21]–[25]). The typical optimisation function of extreme learning is represented as

$$\min_{\beta} \left(\parallel \beta \parallel_F^2 + C \parallel H^T \beta - T \parallel_F^2 \right), \tag{1}$$

where, $\beta \in \Re^{L \times c}$ represents the matrix of output weights, and C>0 is a constant value controlling the relation between the Frobenius norm of the coefficients β and the linear regression term. The optimal value of β is determined by RR:

$$\beta^* = (\frac{I_L}{C} + HH^T)^{-1}HT,$$
 (2)

where I_L is the identity matrix with the dimensionality of L. In order to reduce the computational cost, we obtain the optimal β as

$$\beta^* = \begin{cases} (\frac{I_L}{C} + HH^T)^{-1}HT, & L < N, \\ H(\frac{I}{C} + H^TH)^{-1}T, & L \ge N. \end{cases}$$
(3)

B. Graph Embedding Frameworks

GE frameworks [10] aim to find optimal embedding graphs in tandem with data mapping types and optimisation forms, to unveil the internal structure of a given data set. The optimisation forms of GE frameworks with penalty and scaling constraints are shown, respectively, in Eqs. (4) and (5):

$$\min \sum_{i,j=1}^{N} \parallel y_i - y_j \parallel^2 W_{ij}^{(I)} \quad s.t. \sum_{i,j=1}^{N} \parallel y_i - y_j \parallel^2 W_{ij}^{(P)} = \mu, \quad (4)$$

$$\min \sum_{i,j=1}^{N} \| y_i - y_j \|^2 W_{ij}^{(I)} \quad s.t. \sum_{i=1}^{N} y_i^2 D_{ii} = \mu,$$
 (5)

where $W^{(I)} \in \Re^{N \times N}$ and $W^{(P)} \in \Re^{N \times N}$ are the adjacency matrices of the intrinsic graph and the penalty graph. D is a diagonal matrix to control weights of samples, and μ is a positive constant value. With one mapping direction $a \in \Re^{n \times 1}$ for sample $i, y_i = a^T x_i$. For the training set with multiple mapping directions $A = [a_1, a_2, \ldots, a_d] \in \Re^{n \times d}, \ Y = A^T X$. The kernelised form of Y can be written as $Y = A_K^T \phi^T(X) \phi(X) = A_K^T K$, where $A_K = [a_{K1}, a_{K2}, \ldots, a_{Kd}] \in \Re^{N \times d}$ is the kernelised mapping. We reformulate the optimisation function (Eq. (4)) to obtain the optimal one-dimensional new features of N samples

$$z^* = \operatorname{argmin}_{z} \quad \frac{zL^{(I)}z^T}{zL^{(P)}z^T},\tag{6}$$

where $z\in\Re^{1\times N}$. $L^{(I)}=D^{(I)}-W^{(I)}$, with each element of the diagonal degree matrix $D^{(I)}\in\Re^{N\times N}$ as $D^{(I)}_{ii}=\sum_{j=1}^{N}W^{(I)}_{ij}$, where $i=1,2,\ldots,N$. Similarly, $L^{(P)}=D^{(P)}-W^{(P)}$ and the diagonal matrix $D^{(P)}\in\Re^{N\times N}$ contains elements $D^{(P)}_{ii}=\sum_{j=1}^{N}W^{(P)}_{ij}$. The mapping coefficients connecting training and test data

The mapping coefficients connecting training and test data can be obtained by reformulating z directly in Eq. 6 and solving the *Generalised Eigenvalue Problem* (GEP; [10], [15]).

For **FDA**, given that $N \geq c$, the adjacency matrices of intrinsic and penalty graphs are represented as $W^{(I)} = W_{FDA}^{(I)} = S^T(SS^T)^{-1}S = \sum_{l=1}^c (\widehat{s}_l^T e)^{-1}\widehat{s}_l\widehat{s}_l^T$ and $W^{(P)} = W_{FDA}^{(P)} = \frac{1}{N}ee^T$. Similarly for **LDP**, $W^{(I)} = W_{LDP}^{(I)} = S^TS$ and $W^{(P)} = W_{LDP}^{(P)} = ee^T - S^TS$.

C. Spectral Regression

SR [13], [18], [19] is a two-stage process developed to solve GE problems efficiently that divides the GE solution into spectral graph learning and regression. By setting the new dimensionality of the feature space as one, according to Eq. (6), we can draw a new, optimal one-dimensional feature vector of training samples, written as z^* .

In the linear case, assuming $z=a^TX$, the optimal linear mapping vector a^* can be obtained by a least-square form. However, the least-square solution is often not satisfactory, when the dimensionality of features n is higher than the number of training samples N. Thus we obtain the optimal a as

$$a^* = \operatorname{argmin}_a \left(\parallel a \parallel^2 + C \parallel X^T a - z^{*T} \parallel^2 \right). \tag{7}$$

It has been shown in [18] that when $\frac{1}{C}$ decreases to zero, a^* turns to be the optimal solution for the LS Regression. Eq. (7) also can be solved by RR. In the kernelised form of SR

(i.e., KSR), the optimisation method is changed to obtain the optimal kernelised mapping as

$$a_K^* = \underset{a_K}{\operatorname{argmin}} \left(\parallel a_K \parallel^2 + C \parallel K a_K - z^{*T} \parallel^2 \right). \tag{8}$$

III. PROPOSED FRAMEWORK

In this section, we describe the proposed GSR framework which consists of three stages: 1) data mapping; 2) graph decomposition; and 3) regression. At the first stage, the features of a give sample are projected into a new feature space, and we show that kernel and linear forms in subspace learning [34] follow similar rules as the input-hidden layer procedures in ELMs. By including the data mappings adopted in LSR, KSR, and ELM, different types of data mapping can be employed to generate relevant underlying subspaces. At the **second** stage, we make use of embedding graphs [10] to automatically generate virtual feature vectors for each training sample [35]. This process creates corresponding coordinates of the embedding graphs, which reflect the relationship between each pair of training samples. The goal is to enhance the performance on the target task by better depicting the salient structure in feature space of the data set. Finally, at the third stage, in order to construct a connection between the mapping data and the virtual feature vectors, the subspace mapping matrix is learnt by fitting the new feature space to virtual coordinates employing different regression algorithms.

A. Data Mapping

By representing the data mapping of sample x as f(x), we draw the mapping $x \to f(x)$ for the cases of kernelisation and ELM. Note that for the linear case, the mapping is written as $x \to x$ directly.

Data mapping in kernelisation

In the linear domain, the lower-dimensional features of N training samples are $Y = A^T X$, assuming that $A = \phi(X)A_K + \phi_\perp(X)A_K'$, where the columns of $\phi_\perp(X)$ represent the basis of the null space of $\{\phi(x_1), \phi(x_2), \ldots, \phi(x_N)\}$, and A_K' contains their linear coefficients. Then $Y = A_K^T K$, where X is transformed into its RKHS $\phi(X)$.

According to the equation $Y = A_K^T K$, kernel tricks essentially employ a type of data mapping, which maps the original feature space into a new space created from multiple views of all the training samples. The dimensionality of the linear feature mappings in the dimensionality reduction process also changes to fit the dimensionality of the new space.

Further, on the assumption that $\phi_{\perp}^T(X)\phi(x)=0$, the data mapping in kernelisation for sample x is drawn as

$$x \to f(x) = \phi^T(X)\phi(x) = \mathbf{k}_x,$$
 (9)

where the column vector $\mathbf{k}_x \in \Re^{N \times 1}$. It can thus be concluded from Eq. (9) that the newly generated features of sample x are written in the form of

$$\mathbf{k}_{x} = [\phi^{T}(x_{1})\phi(x), \phi^{T}(x_{2})\phi(x), \dots, \phi^{T}(x_{N})\phi(x)]^{T}.$$
 (10)

Anchor points

In typical kernelisation methods, kernel tricks only present a fixed set of bases in nonlinearisation. Moreover, $\phi_{\perp}^T(X)\phi(x)=0$ does not always hold when x is excluded

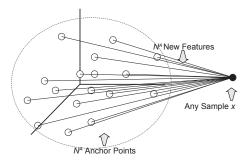


Fig. 1: Generation of N^A new features by N^A anchor points for a certain sample x when the dimensionality of the original feature space is n=3.

from the columns of X. Hence, it is feasible to solve the problems through changing the columns of $\phi(X)$.

We define a set of N^A anchor points $X^A = [x_1^A, x_2^A, \dots, x_{N^A}^A]$ to replace X, where usually $N^A > N$ and $x_i^A \in \Re^{n \times 1}$ with $i = 1, 2, \dots, N^A$. This leads to a set of vectors $\left\{\phi(x_1^A), \phi(x_2^A), \dots, \phi(x_{N^A}^A)\right\}$ in RKHS, as

$$\phi(X^A) = [\phi(x_1^A), \phi(x_2^A), \dots, \phi(x_{N^A}^A)]. \tag{11}$$

We assume that the basis of $\{\phi(x_1^A), \phi(x_2^A), \dots, \phi(x_{N^A}^A)\}$ is able to span the space of $\{\phi(x_1), \phi(x_2), \dots, \phi(x_N)\}$, and $\phi_{\perp}^T(X^A)\phi(x)=0$. Therefore, the new features generated by the anchor points are

$$\mathbf{k}_x^A = \phi^T(X^A)\phi(x). \tag{12}$$

Fig. 1 illustrates the generation of new features when anchor points are provided. For a given sample x, its new features can be generated by N^A views of N^A anchor points with the same dimensionality.

Data mapping in ELM

For ELM, the number of anchor points N^A is exactly equal to the number of hidden neurons L. Assuming that the coordinates of the anchor points are the columns of $\Psi = [\psi_1, \psi_2, \dots, \psi_L] \in \Re^{n \times L}$, the data mapping of ELM is

$$x \to f(x) = g(\phi^T(\Psi)\phi(x)) = h_x, \tag{13}$$

where $h_x \in \Re^{L \times 1}$ is the *L*-dimensional feature vector in the newly generated space. $g(\cdot)$ represents a certain mapping since the output of the activation function is not always nonnegative.

For sample x in ELM, the implicit inner product $\phi^T(\Psi)\phi(x)$ can be represented as an explicit new feature vector h_x . The explicit mapping depends on random anchor points in ELM [21]–[24]. The theory of ELM also indicates that it is possible to select the parameters randomly in the mapping forms. Consequently, the original anchor points and the model parameters can be chosen as random values.

B. Graph Decomposition

We define the embedding graphs as $G^{(I)}$ and $G^{(P)}$. The former represents intrinsic information, whereas the latter represents penalty properties. With this notation, the optimal virtual one-dimensional coordinates are drawn as

$$z^* = \underset{z}{\operatorname{argmin}} \text{ or } \underset{z}{\operatorname{argmax}} \frac{zG^{(I)}z^T}{zG^{(P)}z^T}, \tag{14}$$

where the selection of minimisation and maximisation, as well as the elements in graphs $G^{(I)}$ and $G^{(P)}$, depends on practical requirements as in [10], [15], [36], [37]. This optimisation process can be adapted to solve the GEP

$$G^{(I)}z^T = \lambda G^{(P)}z^T,\tag{15}$$

where λ is the eigenvalue of the GEP. $G^{(I)}$ and $G^{(P)}$ are the matrices of the intrinsic and penalty graphs, without considering the trivial eigenvectors.

For multiple locally optimal zs in constructing the optimal subspace, we define the zs as the 'virtual coordinates' of training samples. Thus, we get $z_i \in \Re^{1 \times N}$, where $i=1,2,\ldots,d$, and

$$[z_1^T, z_2^T, \dots, z_d^T]^T = Z \in \Re^{d \times N},$$
 (16)

which leads to the optimal Z, namely Z^* , by

$$Z^* = \underset{Z}{\operatorname{argmin}} \text{ or } \underset{Z}{\operatorname{argmax}} \quad \frac{tr\left(ZG^{(I)}Z^T\right)}{tr\left(ZG^{(P)}Z^T\right)}, \tag{17}$$

which is a *trace-ratio* problem and it can be solved either by iterative procedures with the orthonormalisation assumption [38], or by the the approximate *ratio-trace* form

$$Z^* = \underset{Z}{\operatorname{argmin}} \ or \ \operatorname{argmax} \quad tr \left(\ [ZG^{(P)}Z^T]^{-1}[ZG^{(I)}Z^T] \ \right), \quad (18)$$

when $ZG^{(P)}Z^T$ is invertible. This results in solving the GEP of Eq. (15), resorting to the Lagrangian method using *Singular Value Decomposition* (SVD). Theorem 1 shows the effectiveness on using the GEP to solve the optimisation, which can be proved by pre-multiplying z on both sides of Eq. (15).

Theorem 1 The nontrivial eigenvectors corresponding to minimal / maximal eigenvalues in Eq. (15) are the optimal solutions of Eq. (14).

It should be noticed that the newly generated coordinates can be processed before the stage of regression (as in ELM and SR). The processing is defined as

$$Z \to \widetilde{Z} = [\widetilde{z}_1^T, \widetilde{z}_2^T, \dots, \widetilde{z}_d^T]^T,$$
 (19)

with each row corresponding to the respective row in Z. It is also feasible to employ normalisation or orthonormalisation using their corresponding constraints on each column of Z at this stage [39], [40].

Graph decomposition in SR and ELM

In the context of SR, the work presented in [20] shows that the graph-decomposition solution is straightforward to obtain by solving Eq. (17), with $\widetilde{Z}=Z$. According to previous work on ELM [21], [23], [25] and SR [11], [13], [18], [20], $S^T(SS^T)^{-1}S$ and I can be used as the embedding graphs. The lth virtual set of coordinates $z_l^T = \widehat{s}_l$, where the elements of \widehat{s}_l corresponding to the lth class are equal to 1, and all the other elements are equal to 0, with $l=1,2,\ldots c$. This solution is presented in Theorem 2, and the proof is shown in Appendix A. For ELM, d is fixed as c, whilst for the SRs (in [11], [13], [18], [20]) d is equal to c-1.

Theorem 2 For SR (in [11], [13], [18], [20]) and ELM, one selection of the embedding graphs is: $G^{(I)} = W_{FDA}^{(I)} = S^T(SS^T)^{-1}S$ and a scaling diagonal matrix $G^{(P)} = I$.

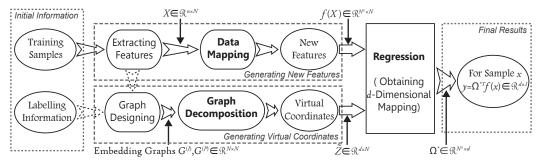


Fig. 2: Schematic diagram of the proposed GSR framework. The features of training samples X are utilised in data mapping and sometimes in graph design. Given the set of new features and a set of virtual coordinates, we can predict y for sample x in the regression process.

C. Regression

Note that $\omega \in \Re^{N^A \times 1}$ is the mapping direction for dimensionality reduction on samples, and ω_i^* is its optimal value corresponding to the virtual coordinate vector \widetilde{z}_i . As in elastic nets [11], [41], the unified regression form of GSR is defined to calculate

$$\omega_{i}^{*} = \operatorname{argmin}_{\omega} \left(\| f^{T}(X)\omega - \widetilde{z}_{i}^{T} \|^{2} + \gamma_{1} \| \omega \|_{1} + \gamma_{2} \| \omega \|^{2} \right), \quad (20)$$

where $f(X) = [f(x_1), f(x_2), \ldots, f(x_N)]$ is the mapping set of training samples X. $i = 1, 2, \ldots, d$ represents the ith dimension of the virtual coordinates generated at the stage of graph decomposition. $\gamma_1, \gamma_2 \ge 0$ are the constant weights for the l1-norm and l2-norm minimisation terms.

Regarding the choices of parameters γ_1 and γ_2 , if $\gamma_1=\gamma_2=0$, Eq. (20) becomes an LS Regression problem. When $\gamma_1=0$ and $\gamma_2>0$, this equation changes into an RR problem, whilst if $\gamma_1>0$ and $\gamma_2=0$ it becomes a *Least absolute shrinkage and selection operator* (Lasso) problem [42]. These forms are minimised with various norms on the basis of SR.

Finally, $\Omega = [\omega_1, \omega_2, \dots, \omega_d]$ represents the dimensionality-reduced mapping matrix.

Regression in SR and ELM

In [11] (Unified Sparse Subspace Learning framework (US-SL)), $\gamma_1 > 0$ and $\gamma_2 = 0$. Eq. (20) can be solved by the Least Angle Regression (LARS) algorithm [11]. In previous SR [13], [18], [20], [35] and ELM [21], [23], [25] research, these parameters were set as $\gamma_2 > 0$ and $\gamma_1 = 0$, and consequently the solution can be written in the form of a column vector:

$$\omega_i^* = \left(\frac{I_{NA}}{\gamma_2} + f(X)f^T(X)\right)^{-1} f(X)\tilde{z}_i^T, \tag{21}$$

where I_{N^A} is the N^A -dimensional identity matrix, and z_i is equal to \widehat{s}_i^T , where $i=1,2,\ldots,c$.

However, for ELM, the decision procedure is similar to what has been frequently employed in neural networks. Instead of directly using nearest-neighbour classifiers, ELM implicitly assumes that for each training sample x_j , the regression $f^T(x_j)\alpha_i^*=(\widetilde{z}_i)_j$ always holds for $j=1,2,\ldots,N$. With this assumption, the decision process in ELM is equivalent to that of a nearest-neighbour classifier.

D. Generalised Spectral Regression Framework

In this section, we present the complete GSR framework, and demonstrate that several existing methods are particular instances of this framework.

As illustrated in Fig. 2, given the originally extracted features from N training samples X and a given sample x, we can obtain the data mapping f(X) and f(x) for samples X and x, respectively, as described in Section III-A. When designing embedding graphs, both X and their corresponding labels can be employed to construct suitable embedding graphs. The designed embedding graphs are utilised to generate virtual coordinates by solving the GEP in graph decomposition, as described in Section III-B. At the regression stage (see Section III-C), the linear d-dimensional mapping matrix Ω^* is obtained according to Eq. (20), and from it we derive the low-dimensional feature vector $y = \Omega^{*T} f(x)$ for sample x.

Table I shows how the proposed GSR can be parameterised to include LSR, KSR, and ELM, through regulating the data mapping form $f(\cdot)$, the number of anchor points N^A , the transformation from Z to \widetilde{Z} , as well as the regression parameters $\gamma_1, \gamma_2 \geq 0$ (where $i, j = 1, 2, \ldots, d$). Note that, for the methods shown in Table I, we set the optimisation types in graph decomposition of Eq. (14) to maximum. The description of the remaining variables shown in Table I can be found in Section II.

IV. GSR APPLIED TO SPEECH EMOTION RECOGNITION

SER focuses on exploring relevant features and algorithms to infer the emotional state of speakers from paralinguistic information, i.e., the nonverbal aspects of speech (including speech prosody, voice quality, and other quantities estimated directly from the acoustic signal). In a typical framework, a set of (relevant) acoustic descriptors is extracted from spoken utterances, which are then used as features in estimating speakers' emotional states using machine learning methods.

System setup

At the stage of **data mapping**, the anchor points can be random coordinates or training samples. Considering the different data mapping methods, we define three GSRs as: *Random-anchor-points GSR* (RGSR), *Training-sample-anchor-points GSR* (TGSR), and *Linear GSR* (LGSR). In RGSR, the anchor points are randomly chosen (as in ELM), while TGSR utilises

 $\begin{array}{|c|c|c|c|c|c|c|c|c|}\hline \text{Stages} & \text{Data Mapping} & Graph Decomposition} \\ Parameters & f(x) & N^A & G^{(I)} & G^{(P)} & Z \rightarrow \widetilde{Z} & \gamma_1 & \gamma_2 \\ \hline LSR [13], [18] & x \rightarrow x & n \\ LSR (USSL) [11] & x \rightarrow x & n \\ KSR [20] & x \rightarrow \mathbf{k}_x & N & S^T (SS^T)^{-1}S & I & \widetilde{Z}e = \mathbf{0}_{d \times 1}, \widetilde{z}_i \widetilde{z}_j^T = 0 & \gamma_1 \neq 0 & \gamma_2 \neq 0 \\ KSR [35] * & x \rightarrow x & n & \left[S^T (SS^T)^{-1}S & \mathbf{0} & (i,j=1,2,\ldots d) & \gamma_1 = 0 & \gamma_2 \neq 0 \\ \hline LSR [35] * & x \rightarrow x & n & \left[S^T (SS^T)^{-1}S & \mathbf{0} & \widetilde{J}_{N \times \bar{N}} & \widetilde{J}_{N \times$

TABLE I: The parameters $(f(\cdot), N^A, G^{(I)}, G^{(P)}, \widetilde{Z}, \gamma_1, \gamma_2)$ of frequently used SRs and ELMs in the GSR framework.

* $\bar{N} = N + N_{UL}$: the total number of training samples with N_{UL} unlabelled ones. $L^{(0)}$: Laplacian matrix of $W^{(0)}$, with $W^{(0)}_{ij}$ obeying that, when x_i and x_j (i, j = 1, 2, ..., N) are labelled, $W^{(0)}_{ij} = 1$ if the labels are same, while $W^{(0)}_{ij} = 0$ if the labels are different; otherwise, $W^{(0)}$ is the k-nearest neighbours adjacency matrix.

training samples as the anchor points (as in KSR). Linear GSR (LGSR) represents the data mapping $x \to x$ as in LSR.

At the stage of graph decomposition, several pairs of embedding graphs are proposed in the GSR framework, since the embedding graphs of ELM are only related to labelling information. As shown in Fig. 2, together with labelling information, features extracted from training samples are also available for graph design. This leads to the creation of knearest neighbour graphs or some other distance-based representations. It should be noticed that we only consider the fully supervised case, where each training sample is labelled by a single emotional class. The embedding graphs ($G^{(I)}$ and $G^{(P)}$) are obtained using pre-existent GE based algorithms – FDA [6], [10], LDP [14], LDE [16], GbFA [17], and Locally Penalised Discriminant Analysis (LPDA; [8]). The description of the FDA and LDP embedding graphs can be found in [6], [10], [14] (also introduced in Section II-B). The embedding graphs of LDE and GbFA are shown mathematically in Eqs. (22) and (23).

For LDE,

$$\begin{cases} W^{(I)} = W_{LDE}^{(I)} = S^T S \odot W_{k_1 NN}, \\ W^{(P)} = W_{LDE}^{(P)} = (ee^T - S^T S) \odot W_{k_2 NN}, \end{cases}$$
(22)

where the operator ' \odot ' represents the element-wise product between two matrices. W_{k_1NN} and W_{k_2NN} are k_1 - and k_2 -nearest neighbour adjacency matrices of training samples, where the elements $(W_{k_1NN})_{ij}=1$ or $e^{-\frac{\|x_i-x_j\|^2}{t}}$, when x_i is among k_1 -nearest neighbours of x_j or vice versa, with $i,j=1,2,\ldots,N$ and the constant value t>0. Otherwise, $(W_{k_1NN})_{ij}=0$. W_{k_2NN} uses k_2 -nearest neighbours, similar as in W_{k_1NN} .

For GbFA,

$$\begin{cases} W^{(I)} = W_{GbFA}^{(I)} = S^{T}S \odot W_{Gram}, \\ W^{(P)} = W_{GbFA}^{(P)} = (ee^{T} - S^{T}S) \odot W_{Gram}, \end{cases}$$
(23)

where $(W_{Gram})_{ij} = e^{-\frac{\|x_i - x_j\|^2}{t}}$. Thus, nearest neighbour truncation is considered in GbFA.

The embedding graphs for LPDA [8] are given in Eq. (24). The intrinsic embedding graph of LPDA is designed as FDA, so as to remove the impact from the relatively inaccurate neighbouring information in SER. The penalty graph of LPDA

aims to penalise neighbouring between-class sample pairs, similar as in LDE and GbFA.

For LPDA,

$$\begin{cases} W^{(I)} = W_{LPDA}^{(I)} = W_{FDA}^{(I)} = S^T (SS^T)^{-1} S, \\ W^{(P)} = W_{LPDA}^{(P)} = \frac{1}{N} e e^T + \delta_0 W_{LDE}^{(P)}, \end{cases}$$
(24)

where the constant value $\delta_0 > 0$ controls the relation between scattering (as in PCA) and the labelling penalty of training samples. It is equivalent to FDA when δ_0 deceases to zero.

In accordance with GE frameworks, we use the Laplacian matrices $L^{(I)}$ and $L^{(P)}$ of $W^{(I)}$ and $W^{(P)}$ (respectively) in graph decomposition. This implies setting the optimisation type to minimum for Eq. (14). In order to avoid the theoretically minimal zero value of the term $zG^{(I)}z^T$ for the intrinsic graphs, we add a term δI with a small value $\delta>0$ in $G^{(I)}$. This leads to $G^{(I)}=\delta I+L^{(I)}$ and $G^{(P)}=L^{(P)}$. We only list each $W^{(I)}$ and $W^{(P)}$, for $G^{(I)}$ and $G^{(P)}$ (respectively) in Eq. (22), (23), and (24). The virtual coordinates relate to the eigenvectors corresponding to minimal eigenvalues [10], [15].

At the **regression** stage, we keep the form of RR employed in the SRs in [13], [18], [20], [35] and the ELMs in [21], [23]–[25]. This leads to the parameter settings as $\gamma_1=0$ and $\gamma_2\neq 0$ in the regression of Eq. (20). The solution of the regression problem can be determined by Eq. (3) or the previously proposed LSQR method [13], [18], [35].

The proposed GSRs described above aim at obtaining multiple linear mapping directions reflecting emotional dimensions. However, general feature sets used in SER often include features that are relevant to other linguistic and paralinguistic application, e.g., *Automatic Speech Recognition* (ASR) or *Speaker Identification* (SI) [6]. Since the feature sets contain information that may not be relevant to SER, all the embedding graphs in the proposed methods include supervised information, considering that the target labels play a crucial role in determining the relevant features for the SER task. The new features are used in the procedure of classification or decision making.

Computational complexity

The computational complexity of the proposed methods primarily depends on graph decomposition and regression:

• Graph decomposition: The conventional GEP solution using SVD requires the complexity $O(N^3)$; when using the fast Monte Carlo algorithm [48], the complexity is

TABLE II: Description of the emotional corpora GEMEP, ABC, VAM, and eNTERFACE for the audio sections.

Corpus	Language	Sampling Rate (kHz)	# Classes	# Speakers	# Samples	Means of Training
GEMEP [43]	French	44.1	18 (here 12)*	10 (5 female)	1 260 (here 1 080)	Training-Testing
ABC [44]	German	16	6	8 (4 female)	430	2-fold CV
VAM [45]	German	16	4	47 (36 female)	946	5-fold CV
eNTERFACE [46]	English	16	6	42 (here 40, 8 female)**	1 277 (here 1 200)	2-fold CV

^{*} We choose 12 classes according to the set in the INTERSPEECH 2013 Computational Paralinguistics Challenge [47].

 $O(r^2N)$, where r is the predefined approximate rank in solving SVD.

• Regression: When directly solving RR, the maximal complexity is $O((\min(N,L))^3 + \min(N,L)LN + \min(N,L)Nd)$ for random data mapping, and is $O(2N^3 + N^2d)$ for kernelisation; when using LSQR, the complexity turns to be $O(NLDl_0)$ for random data mapping, while $O(N^2Dl_0)$ for kernelisation, where l_0 is the iteration number in LSQR.

V. EXPERIMENTAL METHODOLOGY

A. Selected Corpora

In our experiments, we use four corpora that are commonly used in SER tasks. Each corpus is described in the next paragraphs, and Table II summarises the key information.

GEMEP: The *GEneva Multimodal Emotion Portrayals* (GEMEP; [43], [47]) is a database of audio and video recordings featuring 10 actors portraying 18 affective states. In this work we use 12 of these states or classes – *amusement*, *pride*, *joy*, *relief*, *interest*, *pleasure*, *hot anger*, *panic fear*, *despair*, *irritation*, *anxiety*, *sadness*, as in [47]. The number of samples per class is 90. The full database was divided into training and test sets, with 648 (6 speakers; 3 female) and 432 (4 speakers; 2 female), respectively.

ABC: The Airplane Behavior Corpus (ABC; [44], [49]) contains speech recordings labelled in six emotions: aggressive, cheerful, intoxicated, nervous, neutral, tired. The numbers of samples in each emotional class are 95, 105, 33, 93, 79, 25, respectively, leading to a total number of 430 samples. The samples were obtained from 8 speakers (4 female). For our experiments, the full corpus was divided into two folds, each including the recordings of 4 speakers (2 female). Then, one fold is for training while the other for testing, and vice versa, which is equivalent to a 2-fold CV (Cross-Validation).

VAM: The "Vera am Mittag" German audio-visual emotional speech database (VAM; [45], [49]) includes 12 hours of spontaneous and very emotional audio-visual recordings of the German TV show "Vera am Mittag". The corpus includes natural speech utterances in four emotions: happy / excited, angry / anxious, sad / bored, and relaxed / serene, which are here referred to as q1 (21 instances), q2 (50 instances), q3 (451 instances), and q4 (424 instances), respectively, based on quadrants in the arousal/valence plane. The corpus includes recordings from a total of 47 different speakers (36 female). For the purposes of our work, the corpus was divided into 5 (speaker-independent) folds. In order to also balance for gender, the first fold contains the samples from 11 speakers, while all other folds contain the recordings of 9 speakers.

eNTERFACE: The *eNTERFACE'05* (eNTERFACE; [46], [49]) database contains speech utterances recorded in office environment expressing six basic emotions (*happiness*, *sadness*, *surprise*, *anger*, *disgust*, *fear*) as defined by Ekman et al. [50]. There are a total of 42 different speakers (8 female) in the database. In our work, we employed the samples from 40 speakers (8 female), and 200 samples per emotion category. Half of the samples were used for training while the rest were used for test (and vice versa; 2-fold CV).

B. Features

For our experiments we adopt the official feature set of the *INTERSPEECH 2013 Computational Paralinguistics Challenge* (ComParE; [47]), which includes 6 373 static features of functionals of 65 *Low-Level Descriptor* (LLD) contours (a thorough description of the feature set is given in [51]). All features were extracted with *openSMILE* (version 2.0; [52]), a framework for extracting general-purpose acoustic and prosodic features, which has been successfully applied in a variety of SER and other paralinguistic tasks.

C. Preprocessing

As discussed in Section IV, at the stage of **data mapping**, the anchor points are chosen as training samples for TGSR (KSR), or as random points for the RGSR (ELM) case. The number of anchor points for the TGSR based methods is N, while the number of anchor points L for RGSR based methods is set to 500, 1000, 3500, 5000, and 10000. In accordance with the min-max normalisation of the training samples in TGSR, we set each attribute of the random anchor points in RGSR ranging between 0 and 1. In addition, the random anchor points are the same for each method when the number of the points is fixed. The random choices of anchor points are repeated 10 times in our experiments. For each experiment, we only consider the best accuracies among the dimensions no larger than 100.

Similar as in existing SR and ELM approaches, the data mapping employs the popular *Gaussian Kernel* form. For sample x, the generated new features, represented as k_x and k_x for TGSR and RGSR respectively, are given as

$$\begin{cases} k_{x} = \left[e^{-\frac{\|x-x_{1}\|^{2}}{t_{0}}}, e^{-\frac{\|x-x_{2}\|^{2}}{t_{0}}}, \dots, e^{-\frac{\|x-x_{N}\|^{2}}{t_{0}}}\right]^{T}, \\ h_{x} = \left[e^{-\frac{\|x-\psi_{1}\|^{2}}{t_{0}}}, e^{-\frac{\|x-\psi_{2}\|^{2}}{t_{0}}}, \dots, e^{-\frac{\|x-\psi_{L}\|^{2}}{t_{0}}}\right]^{T}, \end{cases}$$
(25)

where also for fair comparison, the scaling parameter t_0 is set as n (no random selection).

^{**} In order to make the two folds balance, we keep the samples from 40 speakers (each one contains 30 samples) in the experiments.

TABLE III: UAs (%) including the means and standard deviations in the ten-time repeating experiments on the GEMEP, ABC, VAM, and eNTERFACE corpora, respectively.

L	Methods	GEMEP	ABC	VAM	eNTERFACE
	ELM	35.5 ± 1.5	43.5 ± 1.5	37.9 ± 0.4	51.8 ± 1.4
	RGSR-FDA	35.0 ± 2.1	42.9 ± 1.1	38.5 ± 1.3	48.5 ± 1.2
L = 500	RGSR-LDP	35.3 ± 2.2	43.1 ± 1.4	38.5 ± 1.0	48.9 ± 1.1
L = 500	RGSR-LDE	35.9 ± 1.6	43.3 ± 1.3	36.6 ± 0.8	49.8 ± 0.5
	RGSR-GbFA	35.6 ± 1.8	42.8 ± 1.2	38.2 ± 1.2	50.8 ± 1.2
	RGSR-LPDA	35.7 ± 1.9	44.3 ± 1.3	39.2 ± 1.8	49.0 ± 1.3
	ELM	37.9 ± 1.1	43.9 ± 0.9	38.2 ± 0.4	53.9 ± 1.0
	RGSR-FDA	36.9 ± 1.5	43.9 ± 1.2	39.0 ± 1.0	52.0 ± 1.0
L = 1000	RGSR-LDP	36.8 ± 1.6	44.8 ± 1.2	38.6 ± 0.9	52.5 ± 1.1
L = 1000	RGSR-LDE	38.1 ± 1.1	44.8 ± 1.0	37.0 ± 0.9	53.3 ± 0.6
	RGSR-GbFA	38.1 ± 1.7	44.2 ± 0.9	39.1 ± 1.5	54.3 ± 1.0
	RGSR-LPDA	38.4 ± 1.3	46.3 ± 1.1	39.2 ± 1.5	52.3 ± 0.9
	ELM	38.9 ± 0.7	43.9 ± 1.0	37.2 ± 0.4	56.2 ± 1.0
	RGSR-FDA	39.2 ± 0.8	44.8 ± 1.2	38.9 ± 1.3	56.0 ± 0.9
L = 3500	RGSR-LDP	39.4 ± 0.7	45.3 ± 1.1	38.3 ± 1.1	56.0 ± 0.9
L = 3300	RGSR-LDE	40.8 ± 1.1	46.0 ± 0.6	36.5 ± 0.3	58.6 ± 0.9
	RGSR-GbFA	40.5 ± 0.8	45.0 ± 1.2	38.5 ± 0.9	59.0 ± 0.8
	RGSR-LPDA	41.0 ± 1.0	47.8 ± 1.0	38.8 ± 1.4	56.7 ± 0.7
	ELM	38.2 ± 0.9	43.3 ± 1.5	36.8 ± 0.3	56.6 ± 0.6
	RGSR-FDA	39.0 ± 0.8	45.0 ± 1.2	38.7 ± 0.6	56.7 ± 0.8
L = 5000	RGSR-LDP	39.0 ± 1.0	44.9 ± 1.2	37.5 ± 0.4	56.6 ± 1.0
L = 5000	RGSR-LDE	40.5 ± 0.7	46.2 ± 1.0	36.6 ± 0.3	59.4 ± 0.8
	RGSR-GbFA	39.9 ± 0.6	44.8 ± 1.1	38.2 ± 0.8	59.5 ± 1.0
	RGSR-LPDA	40.0 ± 0.7	48.0 ± 1.0	38.0 ± 0.8	57.3 ± 0.8
	ELM	36.5 ± 1.0	42.9 ± 1.0	36.1 ± 0.3	56.4 ± 0.7
	RGSR-FDA	38.2 ± 0.9	44.4 ± 0.5	38.5 ± 1.0	56.4 ± 0.7
L = 10000	RGSR-LDP	38.1 ± 1.0	44.2 ± 1.0	37.1 ± 0.4	56.5 ± 0.8
L = 10000	RGSR-LDE	39.8 ± 0.6	46.0 ± 0.6	36.3 ± 0.3	59.8 ± 0.3
	RGSR-GbFA	39.0 ± 0.5	44.6 ± 0.7	38.4 ± 0.6	$\boldsymbol{60.2 \pm 0.8}$
	RGSR-LPDA	38.8 ± 0.4	47.0 ± 0.6	37.3 ± 0.4	57.3 ± 0.6

At the stage of **graph decomposition**, the embedding graphs, including LDE, GbFA, and LPDA, as well as FDA and LDP, are used as terms of comparison in our experiments (an introduction to these graph types is given in Sections II-B and IV). The k_1 and k_2 parameters in Eq. (22) for LDE are both set to 30, and the strategy with $(W_{k_1NN})_{ij}=1$ is adopted. The t parameter in Eq. (23) is chosen as n for GbFA. For LPDA, δ_0 is set to 10^{-4} in Eq. (24).

At the **regression** stage, the weights of γ_1 and γ_2 in Eq. (20) are set to $\gamma_1=0$ and $\gamma_2=10^{-3}$, respectively, and δ is set to 10^{-6} . At the decision level, a k Nearest Neighbour classifier (kNN) is adopted in order to better evaluate the performance compared to other classifiers with complex structures. Thus, kNN can be seen as the baseline. We set k=1 in the experiments.

VI. RESULTS

A. RGSR vs. ELM

This section shows a comparison between our proposed method RGSR and its counterpart ELM. As mentioned above, on the one hand, both ELM and RGSR adopt the same random anchor points at the data mapping stage. On the other hand, it is possible for RGSR to use different embedding graphs for graph decomposition, whereas ELM only employs the fixed embedding graphs as shown in Table I. Hence, in this article, we first conduct a series of experiments with ELM and RGSR on multiple speech emotion corpora using the same sets of random anchor points for all tests. The RGSR algorithms using FDA, LDP, LDE, GbFA, and LPDA embedding graphs

are denoted as RGSR-{FDA, LDP, LDE, GbFA, LPDA}, respectively.

In Table III, we show the classification results for the various corpora and different numbers of anchor points ($L \in$ $\{500, 1000, 3500, 5000, 10000\}$) on the four corpora. Experiments were run 10 times in order to obtain a distribution of *Unweighted Accuracies* (UAs; indicated as percentages) as the performance measure. As shown in Table III, RGSR-{LDE, GbFA, LPDA} always achieve better performance than ELM on the four chosen databases. For example, the proposed RGSR-LPDA get a UA of 48.0% on the ABC database, representing a 4.1% relative improvement over the ELM system. Note that, RGSR-LPDA performs better than RGSR-LDE, and RGSR-GbFA on GEMEP, ABC, and VAM, except the six-class emotion recognition task on the eNTERFACE corpus. This reflects that the proposed GRSR with LPDA embedding graphs (i.e., GRSR-LPDA) is more robust across different emotional corpora.

TABLE IV: Factors and the categories (marked as Categ.) of each factor in the three-way ANOVA.

Factors	# Categ.	Categ.
Method	6	ELM, RGSR-{FDA, LDP, LDE, GbFA, LPDA}
L	5	500, 1000, 3500, 5000, 10000
Database	4	GEMEP, ABC, VAM, eNTERFACE

In order to verify whether there are statistically significant differences between the performance obtained for each method and number of anchor points, we conducted a three-way *Analysis of Variance* (ANOVA) (factors shown in Table IV)

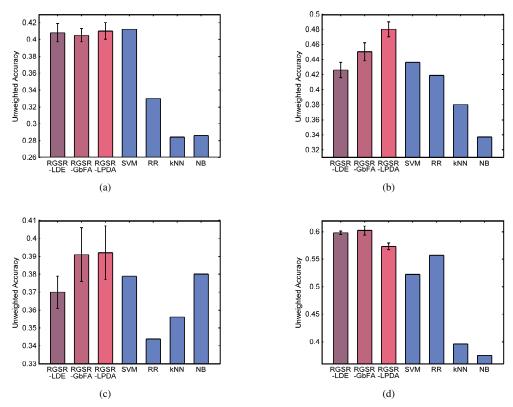


Fig. 3: Column charts of the UAs for our proposed (red) RGSR-{LDE, GbFA, and LPDA }, and other conventional methods (blue) including SVM, RR [29], kNN, and Naive Bayes (NB), on the corpora of (a) GEMEP, (b) ABC, (c) VAM, and (d) eNTERFACE.

TABLE V: Pairwise comparisons (Mean Difference and Significance) of UAs between ELM and RGSRs across the four corpora.

Method1	Method2	Mean Difference (Method1-Method2)	Significance
	RGSR-FDA	-0.003	p > 0.05
	RGSR-LDP	-0.003	p > 0.05
ELM	RGSR-LDE	-0.010	p < 0.0001*
	RGSR-GbFA	-0.012	p < 0.0001*
	RGSR-LPDA	-0.013	p < 0.0001*

and analysed the main effects. The results reveal significant main effects of Method (F(5,1167)=19.068,p<0.0001) and L (F(4,1167)=151.327,p<0.0001). This indicates that the factors of Method and the number of anchor points L have a statistically significant influence on the accuracies for recognising speech emotion. We conducted a post-hoc analysis on the factors to determine the direction of the various effects using Tukey's Honest Significant Difference (Tukey's HSD) test. In respect of Method (see Table V), the RGSR-{LDE, GbFA, LPDA} methods result in significantly better performance when compared to the ELM model across the four corpora (p<0.0001), implying that the proposed RGSR algorithms considerably benefit from the graph decomposition.

B. RGSR vs. Conventional Algorithms

Having shown that RGSR algorithms yield better performance than ELMs on the four different corpora, we now focus on the performance comparison between our proposed methods and state-of-the-art supervised learning algorithms that are typically used to build speech emotion recognition systems. To this end, we compared the performance of RGSR-{LDE, GbFA, LPDA} with standard supervised learning methods, including SVM, *Generalised RR* (noted as RR; [29]), kNN, and *Naive Bayes* (NB). For the SVM tests, we used a 'one-against-one' strategy and the *Sequential Minimal Optimisation* (SMO) for training using a penalty constant C = 0.001. For the RR tests, the weight of the l2 norm was set as 0.001 (in accordance with the RGSRs), and to achieve a fair comparison, we employed a 1-nearest neighbour classifier (the same used for RGSRs).

The results are depicted in Fig. 3 for each corpus studied: a) GEMEP, b) ABC, c) VAM, and d) eNTERFACE). A one-tailed *z-test* [53] was also conducted to determine the significance of the best algorithm's UA performance (from the 10-time RGSR experiments). As observed, our proposed RGSR-{LDE, GbFA, LPDA} achieve better performance when compared to other conventional methods (e. g., SVM and RR). For example, the average UAs obtained using the RGSR and SVM methods are similar on the GEMEP database, but the RGSR method is significantly (p < 0.05) better than the kNN, NB, SVM, and

%UA	Corpus	GEMEP	ABC	VAM	eNTERFACE
	PCA	30.5	40.8	36.1	39.7
	LPP [15]	20.6	32.5	34.0	35.3
	LDA	34.6	43.9	34.7	55.2
Linear SL	LDP [14]	33.7	41.6	35.2	55.1
	LDE [16]	36.5	47.0	35.8	58.7
	GbFA [17]	34.3	41.6	35.3	58.6
	LPDA [8]	37.1	46.4	35.3	56.0
Kernel SL	Kernel LDE [16]	37.0	46.2	34.1	59.2
	Kernel GbFA [17]	34.9	44.5	35.2	57.5
	Kernel LPDA [8]	37.1	46.4	35.2	56.3
Linear SR	l2-norm LSR [13], [18]	32.2	40.8	34.0	55.1
Linear SK	l1-norm LSR [11]	32.7	38.5	34.7	50.8
Kernel SR	l2-norm KSR [20]	37.8	43.6	37.3	55.1
	l1-norm KSR	37.1	42.0	36.4	49.6
	RGSR-LDE	40.8 ± 1.1	46.2 ± 1.0	37.0 ± 0.9	59.8 ± 0.3
Our Methods	RGSR-GbFA	40.5 ± 0.8	45.0 ± 1.2	39.1 ± 1.5	60.2 ± 0.8

 41.0 ± 1.0

TABLE VI: UAs (%) obtained by Subspace Learning (SL) methods (including Linear SL, and Kernel SL), and existing Spectral Regression (SR) methods (including Linear SR (LSR) and Kernel SR (KSR)), and our proposed RGSR methods, including RGSR-{LDE, GbFA, LPDA} on the four speech emotion corpora.

RR methods on the remaining databases.

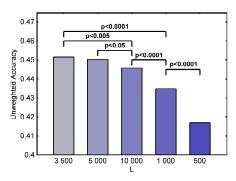
We also compared the RGSRs with GMKDA [54] method on the GEMEP corpus. GMKDA yielded a UA of 42.5%, while the best UA performance of RGSR-LPDA is 43.3%. In addition, the proposed GMKDA requires a much higher iterative computational complexity than the GSR algorithms.

RGSR-LPDA

C. RGSR vs. Conventional Subspace Learning Methods and Spectral Regression

Next, we systematically compared our proposed method with conventional subspace learning and existing SR methods. Specifically, the conventional linear subspace learning methods PCA, LPP [15], LDA, LDE [16] were considered. The recently proposed linear subspace learning methods, LDP [14], GbFA [17], and LPDA [8], were also used for comparison purposes. Furthermore, we tested three kernel subspace learning methods [10] using LDE, GbFA, and LPDA embedding graphs respectively. The SR methods tested were LSR [13], [18] (with l2-norm), LSR [11] (with l1-norm), KSR [20] (with l2-norm), and KSR (with l1-norm). As shown in Table I, the γ_2 s in l2-norm LSR and KSR were set to 0.001, while the γ_1 s in l1-norm LSR and KSR were set to 0.1. Note that the LSR in [35] was used in semisupervised learning. The experimental results on the four corpora are shown in Table VI.

As it can be observed, the proposed RGSR subspace learning framework always reaches the best results on the four emotional corpora. More specifically, RGSR-LPDA achieves the average UAs of 41.0%, 48.0%, and 39.2% on GEMEP, ABC, and VAM, respectively. RGSR-GbFA achieves the average UA of 60.2% on the eNTERFACE corpus. The one-tailed *z-tests* reveal that our proposed RGSR method significantly outperforms the widely used subspace learning methods, PCA and LDA, and the adopted linear spectral regression methods, *l*1-norm LSR and *l*2-norm LSR. Further, RGSR consistently surpasses the performance of other kernel subspace learning and kernel spectral regression methods on the four speech emotion recognition benchmarks by a large margin. These



 39.2 ± 1.5

 57.3 ± 0.6

Fig. 4: The column bar chart of the averaging UAs across the four corpora when using different number of anchor points Ls, with the corresponding significance level between Ls.

results suggest that our proposed RGSR is an efficient method for supervised dimensionality reduction in SER.

D. Influence of Anchor Points

 48.0 ± 1.0

As discussed above (cf. Section III), one major advantage of our proposed method over previous spectral regression counterparts is that anchor points are randomly generated, leading to the new features in RKHS. Here, we investigate the influence of anchor points.

Following the three-way ANOVA analysis conducted in Section VI-A, we first look into the effect of the number of anchor points L on our proposed method. The results are depicted in Table VII and Fig. 4. As shown in Table VII, ' $L=3\,500$ ' and ' $L=5\,000$ ' lead to a significantly better performance than 'L=500', ' $L=1\,000$ ', and ' $L=10\,000$ ' (p<0.05). Furthermore, as can be seen in Fig. 4, the tests using more than $3\,500$ anchor points yield significant performance improvements when compared with the ones using a lower number of anchor points (p<0.0001). This indicates that the number of anchor points plays a significant role in our proposed algorithm. Further, our proposed method

TABLE VII: Pairwise comparisons (Mean Difference and Significance) of UAs for the RGSRs between the number of anchor points $L=3\,500,\,L=5\,000,\,$ and the other Ls across the four corpora.

L1	L2	Mean Difference (L1-L2)	Significance
L = 3500	L = 500 L = 1000 L = 10000	0.035 0.017 0.006	p < 0.0001* p < 0.0001* p < 0.005*
L = 5000	L = 500 L = 1000 L = 10000	0.033 0.016 0.005	$\begin{array}{c} p < 0.0001^* \\ p < 0.0001^* \\ p < 0.05^* \end{array}$

TABLE VIII: UAs obtained by Linear GSR (LGSR; without using anchor points), TGSR (with anchor points from training samples), and the RGSR (with random anchor points), with the embedding graphs LDE, GbFA, and LPDA. 'EG' stands for the corresponding embedding graphs on the four corpora.

EG	Methods	GEMEP	ABC	VAM	eNTERFACE
	LGSR-	36.2	46.6	34.7	59.0
LDE	TGSR-	38.0	47.5	38.2	57.8
	RGSR-	42.8	47.5	38.9	60.3
	LGSR-	35.1	43.2	35.5	58.2
GbFA	TGSR-	40.3	46.8	40.1	59.1
	RGSR-	41.7	46.0	42.5	61.3
	LGSR-	36.4	47.3	35.1	55.7
LPDA	TGSR-	40.3	48.3	41.3	58.2
	RGSR-	43.3	49.4	42.3	58.7

highly benefits from a large number of anchor points, yet, too many anchor points may degenerate the performance.

Now, we show the importance of randomly generated anchor points in our introduced GSR framework. We compare our proposed RGSR relying on random anchor points with the corresponding GSR methods using training sample anchor points, which are referred as to TGSR. Linear GSR (i. e., the data mapping $x \to x$) methods, which do not need the help of anchor points, are also reported. Table VIII shows the highest UAs yielded by these various methods. Note that the UAs of RGSRs correspond to the best performance of RGSR-{LDE, GbFA, LPDA}, respectively.

As seen in Table VIII, the GSR algorithms using anchor points (i. e., RGSR and TGSR) outperform the linear GSR. Furthermore, the proposed RGSR algorithms often achieve the best performance on the four speech emotion databases, which demonstrates the importance of random anchor points.

VII. CONCLUSIONS AND OUTLOOK

In this article, we proposed the *Generalised Spectral Regression* framework that exploits the combination of Extreme Leaning Machines (ELMs) and subspace learning to overcome the drawbacks of ELM and Graph Embedding (GE) based spectral regression. The GSR framework consists of three stages, namely *data mapping*, *graph decomposition*, and *regression*. In *data mapping*, samples with original features are mapped into new spaces by using anchor points. In *graph decomposition*, designed embedding graphs reflecting the intrinsic structure of data are decomposed to obtain virtual coordinates. In *regression*, combining the virtual coordinates

and data mapping, dimension-reduced mappings are calculated employing different regression types.

Using the GSR framework, we designed multiple embedding graphs to specifically represent the relations between data in the application of *Speech Emotion Recognition* (S-ER). Extensive experiments on four speech emotional corpora demonstrate the effectiveness and practicality of the proposed approaches when compared with related existing methods including ELM and subspace learning approaches.

Despite the excellent results using our proposed approach, there are various aspects on which this work could be improved. In *data mapping*, optimising the selections of anchor points or data mapping types is a meaningful research direction, since there exist significant differences in performance in the experiments. In the *graph decomposition* phase, it still remains unknown which type of embedding graphs can be more beneficial for SER tasks. Exploring more specific embedding graphs may further improve the system performance. In the *regression* stage, we only considered *Least-Square Regression* with *l*2-norm minimisation. Other approaches such as deep learning could also be explored in future work.

APPENDIX A PROOF OF THEOREM 2

According to Section II-A, we change the z^T in both the left and the right parts of Eq. (15) into \hat{s}_l , where the label $l = 1, 2, \ldots, c$. It can be proved that

$$G^{(I)}\widehat{s}_{l} = S^{T}(SS^{T})^{-1}(S\widehat{s}_{l}) = I_{N}\widehat{s}_{l}.$$
 (26)

With the left part of Eq. (15) equal to $\lambda I_N \hat{s}_l$, $\lambda = 1$ can be drawn. According to the SVD of

$$W_{FDA}^{(I)} = S^T (SS^T)^{-1} S = U \Lambda U^T,$$
 (27)

where $U^TU = I$, $\Lambda = diag(\lambda_1, \lambda_2, \dots, \lambda_N)$, and $\lambda_1 \ge \lambda_2 \ge \dots \ge \lambda_N$. Accordingly, the c eigenvalues $\lambda_1 = \lambda_2 = \dots = \lambda_c = 1$, while the others are equal to zero.

Thus, $\lambda=1$ are the c largest eigenvalues, which are corresponding to the maximal values of $zG^{(I)}z^T$. This is equivalent to solving

$$\max \left(zG^{(I)}z^T \right) \Rightarrow \min \left(zL^{(I)}z^T \right),$$
 (28)

where $L^{(I)}$ is the Laplacian matrix of $S^T(SS^T)^{-1}S$.

The transformation for virtual coordinates is then changed into $2\hat{s}_l - e$. Therefore, Theorem 2 is proved.

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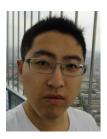
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