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3 Comparative study of in situ N₂ rotational Raman spectroscopy 4 methods for probing energy thermalisation processes during 5 spin-exchange optical pumping

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11 **Abstract** Spin-exchange optical pumping (SEOP) has
12 been widely used to produce enhancements in nuclear spin
13 polarisation for hyperpolarised noble gases. However, some
14 key fundamental physical processes underlying SEOP
15 remain poorly understood, particularly in regards to how
16 pump laser energy absorbed during SEOP is thermalised,
17 distributed, and dissipated. This study uses in situ ultra-low
18 frequency Raman spectroscopy to probe rotational temper-
19 atures of nitrogen buffer gas during optical pumping under
20 conditions of high resonant laser flux and binary Xe/N₂ gas
21 mixtures. We compare two methods of collecting the Raman
22 scattering signal from the SEOP cell: a conventional
23 orthogonal arrangement combining intrinsic spatial filtering
24 with the utilisation of the internal baffles of the Raman
25 spectrometer, eliminating probe laser light and Rayleigh
26 scattering, versus a new in-line modular design that uses
27 ultra-narrowband notch filters to remove such unwanted
28 contributions. We report a ~23-fold improvement in

detection sensitivity using the in-line module, which leads to 29
faster data acquisition and more accurate real-time moni- 30
toring of energy transport processes during optical pumping. 31
The utility of this approach is demonstrated via measure- 32
ments of the local internal gas temperature (which can 33
greatly exceed the externally measured temperature) as a 34
function of incident laser power and position within the cell. 35
36

1 Introduction 37

Conventional nuclear magnetic resonance (NMR) spec- 38
troscopy and imaging (MRI) suffer from inherently low 39
detection sensitivity; even in the highest available magnetic 40
fields, the equilibrium nuclear spin polarisation is very low 41
(~10⁻⁴–10⁻⁶). In an effort to combat this sensitivity issue, 42
the increased nuclear spin polarisation of hyperpolarised 43
(HP) noble gases (e.g. ³He, ¹²⁹Xe, and ⁸³Kr) has attracted 44

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attention for many diverse MR applications [1], including biomedical MRI of human lung space [2–4], probing porous materials and surfaces [5], and studying host–guest interactions of molecules [6–9]. ^3He has a higher gyromagnetic ratio, but ^{129}Xe is attractive due to its far wider chemical shift range making it a sensitive MR probe [1], as well as greater physiological solubility and lipophilicity [1]. Additionally, ^{129}Xe is naturally abundant, and due to the worldwide ^3He shortage [10], there exists an emerging market for HP ^{129}Xe technology.

HP ^{129}Xe is produced via spin-exchange optical pumping (SEOP) [11], a two-step process by which the angular momentum from circularly polarised laser light is absorbed by the electronic spins of an alkali metal vapour (e.g. Rb or Cs [12]), and then transferred to the nuclear spins of ^{129}Xe via collisions. Our previous work studying HP ^{129}Xe production at elevated Xe densities and high resonant laser flux [12–14] has led to improvements in Xe polarisation (P_{Xe}), culminating in the recent design of ‘open-source’ clinical xenon polarisers capable of producing HP ^{129}Xe with P_{Xe} values approaching unity, despite the use of Xe-rich gas mixtures [15, 16].

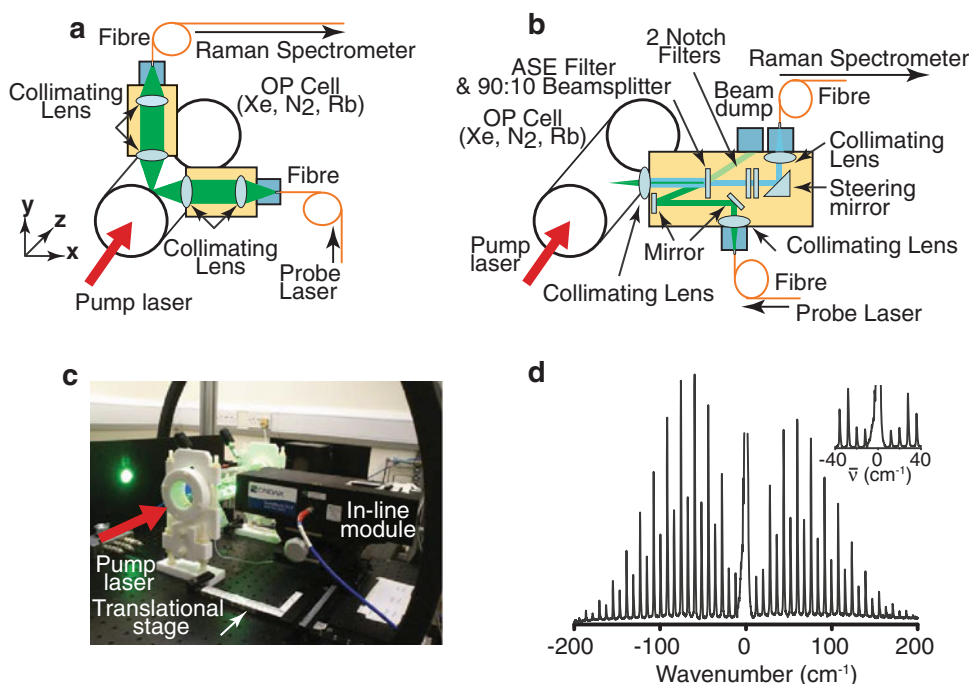
Despite decades of study, some aspects of SEOP remain poorly understood, particularly under the demanding conditions of high resonant laser flux and Xe densities. One such facet concerns the transport of energy within the SEOP chamber (or ‘OP cell’). Nitrogen is often added as a buffer gas to quench fluorescent re-emission (and other undesirable energetic processes [17]) from electronically excited alkali metal atoms via radiationless, two-body (Rb/ N_2) collisions. However, these processes result in the accumulation of large amounts of energy in the ro-vibrational manifold of the N_2 buffer gas. In turn, this energy may be thermally distributed to other species throughout the cell in a heterogeneous fashion (with implications for various aspects of the SEOP process), and eventually dissipated to the cell walls and surroundings. Previous work by Walter et al. [18] explored the rotational and vibrational temperatures of N_2 in OP cells via Raman spectroscopy, performed with an orthogonal arrangement for excitation and collection, and subsequent fitting of the recorded Raman intensities to a Boltzmann model. N_2 rotational temperatures of up to ~ 200 °C above the apparent temperature for the exterior surface of the OP cell were reported for SEOP under relatively modest conditions, e.g. ≤ 15 W of ~ 2 nm full-width half maximum (FWHM) laser light with a $^4\text{He}/\text{N}_2$ gas mixture [18]. Walter et al. concluded that probing the outer surface temperature of the OP cell was often a poor indicator of the actual internal gas temperature compared to Raman measurements, given that the N_2 rotational temperature, T_{N_2} , should quickly equilibrate with the translational temperature of N_2 and the other gas species in the cell. We have recently extended such work to the study of Rb/Xe SEOP with high resonant laser flux and high Xe densities [19, 20], and observed much

larger temperature differences between the external and internal measurements. Other studies to examine energy transport in optical pumping include work performed by Parnell et al. [21] using diffusion sensitised gradients to measure laser heating, as well as numerical simulations of the production of HP ^{129}Xe by Fink et al. [22]. To further the study of energy transport during SEOP, here we introduce a new method for recording the Stokes/anti-Stokes rotational Raman lines used to determine the local internal gas temperature during optical pumping. We compare this method, a fibre-coupled ‘in-line’ module with ultra-narrow-band notch filters, with our previous home-built orthogonal arrangement [19, 20] for collecting Raman data during SEOP. The utility of the ~ 23 -fold sensitivity improvement provided by the in-line module is demonstrated with measurements of the internal gas temperature elevation as a function of position and incident laser power, including a comparison of the effects of using frequency-narrowed compared to broadband lasers for SEOP.

2 Methods

In order to record a sufficiently complete rotational Raman spectrum, it is necessary to suppress the scattered ‘probe’ laser signal well enough to resolve the much weaker Raman lines that may be only a few 10 s of cm^{-1} away. Therefore, to observe such ultra-low frequency rotational Raman spectra, we have employed two contrasting assemblies. The first (Fig. 1a) has already been discussed in Refs. [19, 20] and has demonstrated our initial results using Raman spectroscopy to probe T_{N_2} during SEOP. Briefly, the probe laser source (Coherent ‘Verdi’, 5 W, 532 nm) is fibre-coupled to a modular optical lens assembly near the OP cell, collimated, and then focused to a sub-millimetre point within the OP cell (along the x -axis) using a planoconvex lens; the Raman scattering is collected at a 90° angle to the laser source (i.e. along the y -axis), focused onto a $50\text{-}\mu\text{m}$ fibre, and fibre-coupled to the Raman spectrometer. Laser and Rayleigh scattering are spatially filtered using the internal baffles of the Raman spectrometer. Our new approach uses an in-line (confocal) module (Fig. 1b, c) for excitation and detection of the Raman transitions along the same optical path (i.e. x -axis), custom-designed for our application in collaboration with Ondax Incorporated (XLF-C). The same 532 nm laser was used as the probe for the Raman system and was subsequently fibre-coupled into a double 1-m Horiba Jobin–Yvon U1000 Raman Spectrometer with an Andor Newton thermoelectrically cooled electron-multiplying CCD. The in-line module contains two SureBlockTM ultra-narrow-band notch filters, which allow both Stokes and anti-Stokes lines to be viewed simultaneously and increase the system’s capacity to resolve ultra-low frequency Raman lines, as

Fig. 1 Schematic of (a) orthogonal set-up (previously reported in Refs. [19, 20]) and (b) in-line module for excitation and detection for in situ Raman spectroscopy. c Corresponding photograph of the in-line module. The inline module is mounted onto a translational stage to allow three-dimensional mapping of T_{N_2} within the cell. d Typical background-corrected rotational Raman spectrum from N_2 gas within OP cell showing the full ranges of Stokes and anti-Stokes scattering frequencies centred around (and plotted as a difference in frequency from) the 532 nm (Rayleigh scattered) probe laser line. The inset shows a close-up of the ultra-low frequency region that is spectrally resolvable using the in-line apparatus



148 well as one NoiseBlock™ ultra-narrow-band beamsplitter
 149 filter that improves the spectrum of the incoming probe
 150 beam by reducing any laser sidebands, spontaneous laser
 151 diode emissions, or fibre-induced fluorescence. The
 152 NoiseBlock filter also acts as a spectrally sensitive 90:10
 153 beamsplitter that transmits collected Raman signals and
 154 reduces Rayleigh scattered light by an order of magnitude.
 155 This system is capable of being easily translated to allow
 156 three-dimensional temperature mapping of the OP cell.

157 The OP cell under investigation is a 2.5 cm diameter,
 158 15 cm long Pyrex glass cylinder coated with SurfaSil™ sili-
 159 conising agent and filled with Rb (~500 mg), Xe (100 torr),
 160 and N₂ (1,900 torr), Fig. 1. The OP cell is heated by a 400-W
 161 heat pipe and controlled by a CAL 9,500 temperature con-
 162 troller, with corresponding Pt100 sensors on the oven inlet and
 163 outlet. Raman temperature data were acquired in three-second
 164 acquisitions to ensure nearly ‘real-time’ information. For
 165 demonstration, experiments involving the in-line module and
 166 two ‘pump’ (SEOP) lasers with similar overall laser output
 167 powers were compared: broadband (QPC Brightlase Ultra-
 168 100; ~2.13 nm FWHM) and frequency-narrowed (QPC
 169 Brightlock Ultra-100; ~0.26 nm FWHM).

170 Raman data were analysed by first applying a baseline
 171 correction to the spectra, then fitting each peak to a
 172 Gaussian line shape and obtaining peak heights, $S(J)$, for
 173 six of the Stokes lines ($J = 4, 6, 8, 10, 12$). These values
 174 were then linearly fit using $J(J + 1)$ versus $\ln [S(J)$
 175 $2(2J + 3)] / (3(J + 1)(J + 2))$, according to the equations
 176 discussed by Hickman et al. [23]. This process results in a
 177 line with a slope equal to Bhc/kT , from which the rotational
 178 temperature, T , of the system can be computed using the

rotational constant for N₂ ($B \approx 2 \text{ cm}^{-1}$), Planck’s con-
 179 stant (h), the speed of light (c), and Boltzmann’s constant
 180 (k). The error bars of the calculated temperature data points
 181 reflect the fit error of these plots.
 182

3 Results and discussion

183
 184 When utilising the orthogonal arrangement [19, 20] (Fig. 1a),
 185 contributions from Rayleigh scattering and the probe laser are
 186 minimised by exciting and detecting along different axes
 187 (x and y , respectively), as well as spatially filtered by the
 188 internal baffles of the Raman spectrometer. However, sub-
 189 mm³ accuracy is needed for aligning the focal points of the
 190 excitation and receive optics; this critical alignment is tedious
 191 to set up and prone to drift over time. In contrast, the in-line
 192 module uses two ultra-narrow-band notch filters, with an
 193 optical density greater than 4 and FWHM of 0.35 nm for each
 194 filter, to allow transmission of the Raman light while dra-
 195 matically reducing the infiltration of laser light and Raleigh
 196 scattering into the Raman spectrometer. The application of
 197 these filters enables ultra-low frequency Stokes and anti-
 198 Stokes Raman scattering [24] peaks to be resolved as close as
 199 10 cm⁻¹ from the probe laser line (Fig. 1d).

200 Examples of typical rotational Raman spectra acquired
 201 with the conventional ‘orthogonal’ and ‘in-line’ set-ups are
 202 shown in Fig. 2a, b, respectively. The spectra, obtained
 203 under identical conditions from a cell containing 100 torr
 204 Xe/1,900 torr N₂, were each acquired over 15 s at room
 205 temperature (in the absence of pump laser irradiation). The
 206 in-line module was found to provide ~23-fold improved

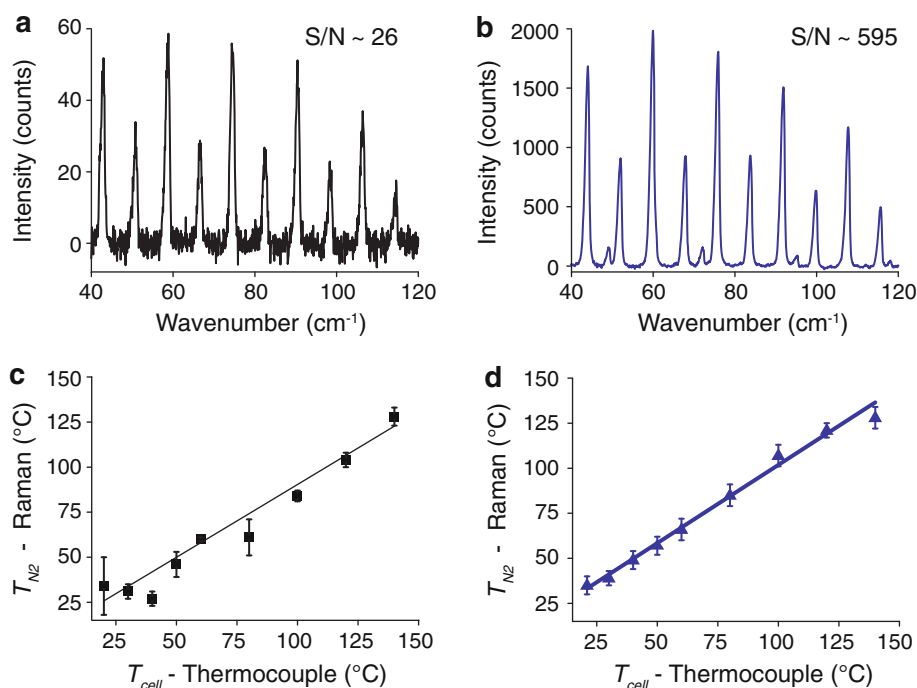


Fig. 2 Comparison of typical rotational Raman spectra from N₂ gas at 24 °C using either the ‘orthogonal’ detection system (a) or the ‘in-line’ module (b). Spectra were obtained under identical conditions (OP cell containing 100 torr Xe/1,900 torr N₂, 15 s acquisition time, no pump laser illumination), and indicate a SNR improvement of ~23-fold when using the in-line apparatus. Corresponding

temperature calibration plots obtained using the ‘orthogonal’ and ‘in-line’ set-ups are shown, respectively, in c and d with R-square values of 0.94 and 0.99. Oxygen peaks appearing in b are due to contributions from atmospheric O₂ in the optical path (but outside of the SEOP cell); the contributions from atmospheric N₂ and O₂ were found to be negligible in determining T_{N₂} under present conditions

207 SNR, which translates directly into more precise temper- 232
 208 ature measurements, as indicated by the corresponding 233
 209 temperature calibration plots (Fig. 2c, d). One complica- 234
 210 tion of the in-line module is the contribution of signals 235
 211 arising from Raman scattering from atmospheric N₂ and O₂ 236
 212 along the optics path outside of the SEOP cell, as mani- 237
 213 fested by the appearance of the small O₂ peaks in Fig. 2b 238
 214 (note that the molar scattering intensity of O₂ is roughly 239
 215 twice that of N₂ [25]). Removal of these unwanted contri- 240
 216 butions was attempted by collecting background spectra 241
 217 using an evacuated OP cell. However, slight spectral drifts 242
 218 caused the subtraction of these peaks to lead to non-real- 243
 219 istic difference spectra resulting in poorer fits to the 244
 220 Boltzmann model, and hence, more imprecise temperature 245
 221 measurements compared to results obtained simply by fit- 246
 222 ting the spectra without subtraction. In any case, when 247
 223 combined with CCD detection (as opposed to using a 248
 224 photomultiplier tube to collect the Raman-scattered pho- 249
 225 tons), the in-line module provides an improvement in SNR 250
 226 compared to the previous orthogonal set-up used by Walter
 227 et al. [18], according to calculations considering the
 228 acquisition time for a given spectral window of equivalent
 229 gas loading and the corresponding spectral SNR obtained.

230 Once optimised and calibrated, the in-line module was
 231 used to demonstrate the in situ measurement of the gas mix

temperature inside cells during Rb/¹²⁹Xe spin-exchange 232
 optical pumping. For example, we evaluated the effects of 233
 pump laser-induced cell heating by comparing the spatial 234
 profile (along the *x*-axis) of T_{N₂} (Fig. 3a) using both fre- 235
 quency-narrowed (Fig. 3c) and broadband (Fig. 3d) laser 236
 diode arrays, both operating at 60 W, after only 5 min of 237
 optical pumping. N₂ rotational Raman spectra were mea- 238
 sured transversely as a function of position across the cell 239
 (~21 mm behind the front window) at 1 mm intervals, 240
 perpendicular to the main pump laser beam (Fig. 3b); these 241
 spectra were then converted to temperatures as described 242
 above. Illumination by the broadband pump laser resulted 243
 in internal gas temperatures (as manifested by T_{N₂} values) 244
 that were ~40 °C in excess of T_{cell}, and the temperature 245
 (measured via thermocouple) from the forced air oven used 246
 to externally heat the OP cell. On the other hand, the 247
 dramatically increased resonant energy emitted by the 248
 frequency-narrowed laser gave rise to T_{N₂} values that were 249
 ~200 °C elevated relative to T_{cell}.¹ Figure 3 also 250

¹ The much larger differences between internal (gas) and external (wall/oven) temperatures measured in ref [19] likely reflect the much longer optical pumping times for those experiments (allowing more thermal energy to accumulate within the cell), as well as any gas mixture-dependent effects.

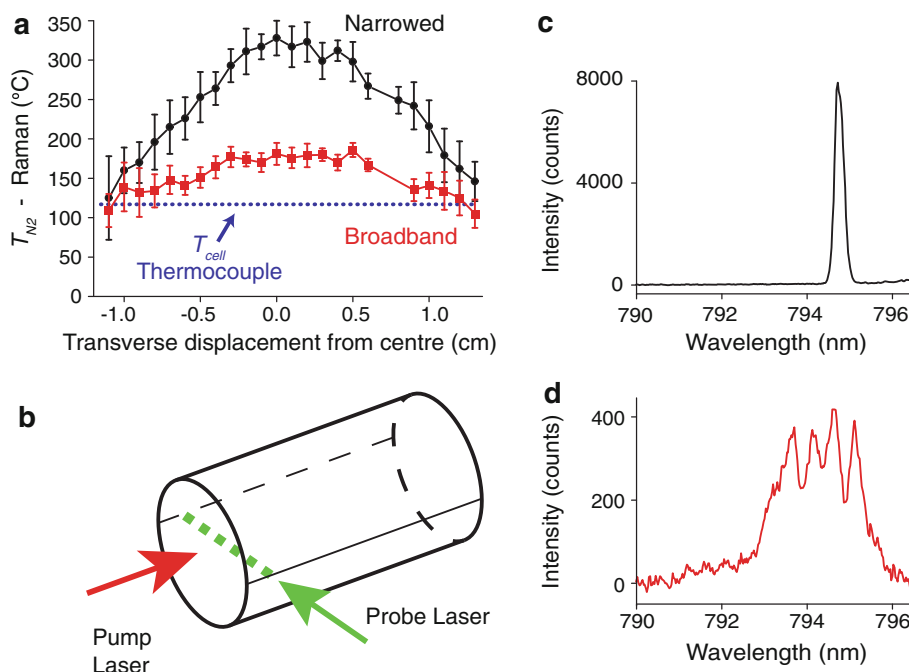


Fig. 3 a Plots showing the spatial variation of the steady-state values of T_{N_2} during SEOP, as induced by the ‘pump’ LDAs [acquired after 5 min of illumination by either a 60 W broadband (red squares) or 60 W VHG-narrowed LDA [14] (black circles)]. Plots are compared to the temperature of the external glass wall near the front of the cell, as measured with a thermocouple (dotted line); T_{cell} values were 110 and 150 °C near the front and back of the cell, respectively (lines are

meant to guide the eye). Values for T_{N_2} (three-second integration time) were measured in 1-mm increments by translating the focused spot horizontally across the cross-section of the cell, transverse to the pump beam (b). The spectral profiles of the VHG-narrowed and broadband LDAs are shown, respectively, in c and d; FWHM = 0.26 and 2.13 nm

251 showcases the ability of the in-line module to spatially
 252 translate to collect data from different regions of the OP
 253 cell.

254 We also used the frequency-narrowed laser to examine
 255 the relationship between illuminated laser powers and ΔT_{N_2}
 256 ($T_{N_2} - T_{cell}$) for various external oven cell temperatures,
 257 Fig. 4. We found a quasi-linear dependence of ΔT_{N_2} on
 258 emitted laser power for each oven temperature setting, with
 259 the largest increase in ΔT_{N_2} observed at the highest laser
 260 powers and T_{cell} . The fact that the slope of the lines rises
 261 with T_{cell} is likely explained by concomitant increases in Rb
 262 density [26]; the increased concentration of gaseous
 263 absorbers of the incident laser light will drive up the energy
 264 deposition rate into the N_2 ro-vibrational degrees of free-
 265 dom. Moreover, the absorber concentration will also
 266 increase as P_{Rb} suffers from poorer cell illumination [13];
 267 these effects can be rapidly compounded as macroscopic
 268 heating from the laser absorption drives more Rb atoms into
 269 the vapour phase, increasing the optical density of the cell,
 270 which then further increases the laser absorption, thereby
 271 fuelling the ‘Rb runaway’ positive feedback loop [14, 27].
 272 On the other hand, it appears that SEOP performed at lower
 273 T_{cell} values gives rise to relatively stable T_{N_2} behaviour,
 274 Fig. 4, as many of the available photons are not absorbed, as
 275 monitored by the laser power meter behind the cell.

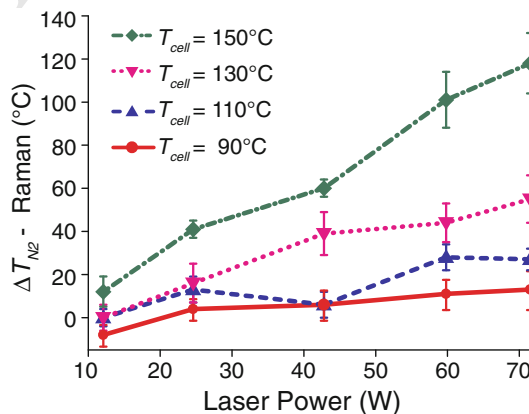


Fig. 4 The temperature difference between T_{N_2} and T_{cell} (ΔT_{N_2}) measured in the middle of the OP cell after 2-min pump laser illumination, plotted as a function of pump laser power for T_{cell} values ranging from 90–150 °C

4 Summary

276
 277 We have implemented a new in-line Raman module for
 278 rapidly measuring local internal gas temperatures during
 279 SEOP. This apparatus, which obtains N_2 rotational tem-
 280 peratures by probing the ultra-low frequency Stokes/anti-
 281 Stokes Raman lines, was shown to provide improvements

Author Proof

282 in detection sensitivity (SNR increase ~ 23 -fold, with
 283 corresponding gains in spatiotemporal resolution), accu-
 284 racy and precision in determining T_{N2} values, and ease of
 285 use compared to our previous orthogonal arrangement. The
 286 utility of the in-line approach was demonstrated by
 287 exploring the effects of laser heating during SEOP as a
 288 function of pump laser power, linewidth, and position
 289 within the OP cell. Future experiments will use this in-line
 290 module to dynamically probe T_{N2} for a variety of SEOP
 291 parameters, most notably at elevated resonant pump laser
 292 powers and as a function of gas mixture, where the benefits
 293 of greater understanding of energy transport and ther-
 294 malisation processes during SEOP can be directly trans-
 295 lated to improved designs and practices for next-generation
 296 clinical polarisers for ^{129}Xe , as well as other noble gas
 297 isotopes.

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