Decay spectroscopy of 160 Sm: the lightest four-quasiparticle K isomer

Z. Patel^{a,b,*}, Zs. Podolyák^a, P. M. Walker^a, P. H. Regan^{a,c}, P.-A. Söderström^b, H. Watanabe^{b,d,e}, E. Ideguchi^{f,g},
G. S. Simpson^h, S. Nishimura^b, F. Browne^{b,j}, P. Doornenbal^b, G. Lorusso^{b,c}, S. Rice^{a,b}, L. Sinclair^{b,k}, T. Sumikama^l,
J. Wu^{b,i}, Z. Y. Xu^m, N. Aoi^{f,g}, H. Baba^b, F. L. Bello Garroteⁿ, G. Benzoni^o, R. Daido^g, Zs. Dombrádi^v, Y. Fang^g,
N. Fukuda^b, G. Gey^h, S. Go^p, A. Gottardo^q, N. Inabe^b, T. Isobe^b, D. Kameda^b, K. Kobayashi^r, M. Kobayashi^p,
T. Komatsubara^{s,t}, I. Kojouharov^u, T. Kubo^b, N. Kurz^u, I. Kuti^v, Z. Li^w, H. L. Liu^x, M. Matsushita^p, S. Michimasa^p,
C.-B. Moon^y, H. Nishibata^g, I. Nishizuka^l, A. Odahara^g, E. Şahinⁿ, H. Sakurai^{b,m}, H. Schaffner^u, H. Suzuki^b,
H. Takeda^b, M. Tanaka^g, J. Taprogge^{z,aa}, Zs. Vajta^v, F. R. Xuⁱ, A. Yagi^g, R. Yokoyama^p

^aDepartment of Physics, University of Surrey, Guildford, GU2 7XH, UK

^bRIKEN Nishina Center, 2-1 Hirosawa, Wako-shi, Saitama 351-0198, Japan

 $^cNational\ Physical\ Laboratory,\ Teddington,\ Middlesex,\ TW11\ 0LW,\ UK$

^dInternational Research Center for Nuclei and Particles in the Cosmos, Beihang University, Beijing 100191, China

^eSchool of Physics and Nuclear Energy Engineering, Beihang University, Beijing 100191, China

^fResearch Center for Nuclear Physics (RCNP), Osaka University, Ibaraki, Osaka 567-0047, Japan

^gDepartment of Physics, Osaka University, Machikaneyama-machi 1-1, Osaka 560-0043 Toyonaka, Japan

^hLPSC, Université Joseph Fourier Grenoble 1, CNRS/IN2P3, Institut National Polytechnique de Grenoble, F-38026 Grenoble Cedex, France

ⁱSchool of Physics and State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, China

^jSchool of Computing, Engineering and Mathematics, University of Brighton, Brighton, BN2 4JG, United Kingdom

^kDepartment of Physics, University of York, Heslington, York, YO10 5DD, United Kingdom

¹Department of Physics, Tohoku University, Aoba, Sendai, Miyagi 980-8578, Japan

^mDepartment of Physics, University of Tokyo, Hongo, Bunkyo-ku, Tokyo 113-0033, Japan

ⁿDepartment of Physics, University of Oslo, Oslo, Norway

^oINFN Sezione di Milano, I-20133 Milano, Italy

^pCenter for Nuclear Study (CNS), University of Tokyo, Wako, Saitama 351-0198, Japan

^qInstituto Nazionale di Fisica Nucleare, Laboratori Nazionali di Legnaro, I-35020 Legnaro, Italy

^rDepartment of Physics, Rikkyo University, 3-34-1 Nishi-Ikebukuro, Toshima-ku, Tokyo 171-8501, Japan

^sResearch Facility Center for Pure and Applied Science, University of Tsukuba, Ibaraki 305-8577, Japan

^tRare Isotope Science Project, Institute for Basic Science, Daejeon 305-811, Korea

^uGSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

^vInstitute for Nuclear Research, Hungarian Academy of Sciences, P. O. Box 51, Debrecen, H-4001, Hungary

^wSchool of Physics, Peking University, Beijing 100871, China

^xDepartment of Applied Physics, School of Science, Xi'an Jiaotong University, Xi'an 710049, China ^yHoseo University, Asan, Chungnam 336-795, Korea

^zInstituto de Estructura de la Materia, CSIC, E-28006 Madrid, Spain

^{aa}Departamento de Física Teórica, Universidad Autónoma de Madrid, E-28049 Madrid, Spain

Abstract

The decay of a new four-quasiparticle isomeric state in ¹⁶⁰Sm has been observed using γ -ray spectroscopy at the RIBF, RIKEN. The four-quasiparticle state is assigned a $2\pi \otimes 2\nu \pi \frac{5}{2}^{-}[532], \pi \frac{5}{2}^{+}[413], \nu \frac{5}{2}^{-}[523], \nu \frac{7}{2}^{+}[633]$ configuration. The half-life of this (11⁺) state is measured to be 1.8(4) μ s. The (11⁺) isomer decays into a rotational band structure, based on a (6⁻) $\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{7}{2}^{+}[633]$ bandhead, consistent with the $g_K - g_R$ values. This decays to a (5⁻) two-proton quasiparticle state, which in turn decays to the ground state band. Potential energy surface and blocked-BCS calculations were performed in the deformed midshell region around ¹⁶⁰Sm. They reveal a significant influence from β_6 deformation and that ¹⁶⁰Sm is the best candidate for the lightest four-quasiparticle K isomer to exist in this region. The relationship between reduced hindrance and isomer excitation energy for E1 transitions from multiquasiparticle states is considered with the new data from ¹⁶⁰Sm. The E1 data are found to agree with the existing relationship for E2 transitions.

The existence of nuclear metastable, or isomeric, states with half-lives of nanoseconds or longer provides a useful tool, enabling spectroscopic investigation of intrinsic and collective states within a nucleus that might otherwise be difficult to observe. In combination with projectile fragmentation and fission reactions, isomers can give unique access to the high-spin excited-state structure of neutronrich nuclei, but only if suitable high-spin isomers exist. Therefore, understanding the formation and stability of multi-quasiparticle isomers is a key part of fully exploiting the new generation of radioactive-beam facilities.

*Corresponding author Email address: z.patel@surrey.ac.uk (Z. Patel)

Preprint submitted to Nuclear Physics B

The projection of the angular momentum of a nucleus on its symmetry axis is known as the K quantum number. K isometrism arises from axially symmetric deformation in the nucleus, enabling the nucleus to be 'trapped' in an aligned spin orientation relative to its symmetry axis [1]. K-isomeric states appear systematically in neutronrich nuclei with A > 150 which typically have deformed prolate shapes. The nucleus is isomeric when the transition to a lower energy state with a different K value is inhibited by the $\Delta K \leq \lambda$ selection rule, where λ is the multipole order of the transition. These transitions are able to proceed through symmetry-breaking processes, where the hindrance factor is strongly correlated with the degree of forbiddenness, $\nu = \Delta K - \lambda$. The partial half-life of the isomeric state relative to the single-particle Weisskopf estimate is known as the reduced hindrance of a transition, expressed as $f_{\nu} = (T_{1/2}^{\gamma}/T_{1/2}^{W})^{1/\nu}$ [1].

K isomers may arise from the breaking of one or more coupled nucleon pairs to form multiquasiparticle (multiqp) states. The excitation energy and other properties of these states depend strongly on the number of proton and neutron states involved [2]. Prior to this work, ¹⁶⁴Er (Z = 68, N = 96) was the lightest nucleus with a known four-qp K isomeric state [3]. Many two-qp isomeric states have been discovered in nuclei lighter than ¹⁶⁴Er, for example, in ^{156,158,160,164}Sm (Z = 62) [4–7], ^{152,154,156}Nd (Z = 60) [6, 8–11], and ¹⁶⁶Gd (Z = 64) [7], but none \geq four-qp. Increasingly more neutron-rich isotopes must be populated to further probe this region. The radioactive isotope beam factory, RIBF, at RIKEN has more recently enabled population of these nuclei using high uranium beam intensities.

Nuclei around ¹⁶⁰Sm were populated by in-flight fission of a 345 A·MeV ²³⁸U beam incident on a 4 mm thick ⁹Be target at the RIBF. The beam intensity at the target was 10 particle-nA on average. The secondary radioactive isotope beam containing the nuclei of interest was passed through the BigRIPS and ZeroDegree spectrometers: a two-stage achromatic separation system that separates and identifies the beam species on an ion by ion basis, using time-of-flight, magnetic rigidity and energy loss (TOF-B ρ - Δ E) [12, 13].

Delayed γ rays were detected from the isomeric decay of the tagged ions using EURICA (Euroball-RIKEN Cluster Array) [14–16]: 84 HPGe crystals arranged in a 4π configuration around a copper passive stopper. The absolute efficiency of the array was 16.6% at 100 keV and 7.6% at 1 MeV. A 100 μ s time coincidence window was used to correlate ion implantation to γ -ray detection.

Delayed γ rays from the isomeric decay of ¹⁶⁰Sm are shown in Fig. 1. All labelled peaks have been identified and placed in the level scheme. A previous experiment by Simpson *et al.* [6] had identified a (5⁻) two-qp isomer that decays via 878 and 1128 keV transitions to the 6⁺ and 4⁺ states in the ground state band respectively. In addition to these transitions, γ rays from the decay of a



Figure 1: Energy spectrum of delayed γ rays from ¹⁶⁰Sm observed 0.5 to 2.5 μ s following implantation. All labelled γ rays have been placed in the level scheme. Those marked with filled circles are the 123, 149, and 316 keV γ rays that were unable to be placed in the level scheme. Inset: The exponential decay curve from the fourquasiparticle isomeric decay of ¹⁶⁰Sm, obtained from the 432 and 641 keV γ rays.

four-qp isomer are now observed in the current work. In particular a strongly-coupled rotational band structure is newly identified. These new γ rays have been added to the ¹⁶⁰Sm level scheme, presented in Fig. 2.

The level scheme was deduced from γ - γ coincidence analysis. The new γ rays with the highest energy (432 and 641 keV) were determined to depopulate the isomeric state directly. The 2⁺ \rightarrow 0⁺ 71 keV γ ray cannot be observed in Fig. 1 due to a strongly competing electron conversion process, but has been observed in coincident spectra. In addition to the γ rays placed in the ¹⁶⁰Sm level scheme, weak γ rays at 123, 149, and 316 keV are also observed in Fig. 1, but were unable to be placed due to low statistics in the coincident spectra.

The spin and parity assignments in Fig. 2 are determined from the transition multipolarities, which have been obtained from the intensity balances through the levels and the decay patterns. The intensities can be seen in table 1. The intensity is not required to balance when transitioning through the (5^-) isomeric state. The spin and parity assignments are tentative in the absence of directly measured electron conversion coefficients and γ -ray angular correlations.

The half-life of the four-qp isomeric state was measured to be 1.8(4) μ s, from the weighted average of the 432 and 641 keV γ -ray half-lives. The half-lives were measured from the exponential decay curves derived from the time between ion implantation and γ -ray detection (see inset in Fig. 1). The half-life of the (5⁻) two-qp state was previously measured at 120(46) ns [6]. The half-life of this isomeric state was not measured in this work as the statistics were not sufficient to resolve the two different half-lives.

Two γ rays of 432 and 641 keV depopulate the four-qp isomer into a band structure built on a two-qp bandhead. A spin of at least $11\hbar$ for the four-qp state is required by the absence of a transition from the isomeric state to the



Figure 2: Level scheme of ¹⁶⁰Sm. All γ rays above the (5⁻) two-qp state are new. The half-life of the (5⁻) state is from Ref. [6].

 (9^-) state. Spin-parities of 11^+ and 12^- are permitted by the experimental data. Our calculations presented below suggest a $K^{\pi} = 11^+$ assignment for the four-qp state.

To further understand the level scheme blocked-BCS calculations [17] were performed. BCS theory treats the nucleus as a superfluid, where the presence of unpaired particles affects the superfluidity through a "blocking effect". In this work the pairing strengths were fixed as $G_{\pi} = 21.00 \text{ A} \cdot \text{MeV}$ and $G_{\nu} = 20.00 \text{ A} \cdot \text{MeV}$, in accordance with Jain *et al.* [17]. The Nilsson energies were then calculated for a set of deformation parameters; $\epsilon_2 = 0.267$ and $\epsilon_4 = -0.027$, taken from Möller *et al.* [18]. The results can be seen in table 2.

These calculations show that a 6⁻ neutron state with a $\nu_2^{5^-}[523] \otimes \nu_2^{7^+}[633]$ configuration and a 5⁻ proton state with a $\pi_2^{5^-}[532] \otimes \pi_2^{5^+}[413]$ configuration are the lowest energy two-qp states. The combination of these states forms an 11⁺ four-qp state. The two-qp state depopulated by the 878 and 1128 keV transitions was previously suggested to be a (5⁻) state arising from a two-neutron $\nu_2^{5^+}[642] \otimes \nu_2^{5^-}[523]$ configuration [6]. However, our blocked-BCS calculations show that a 5⁻ two-proton configuration is preferred.

The branching ratios in a band can be used to infer the bandhead configuration. The difference between the expected and experimental intrinsic g factor (g_K) can indicate whether a band structure is built on a proton or a neutron bandhead.

The expected intrinsic g factor is calculated from $Kg_K = \Sigma(g_{\Lambda}\Lambda + g_{\Sigma}\Sigma)$, where Λ and Σ are the projections of the orbital angular momentum and intrinsic spin on the symmetry axis respectively, and g_{Λ} and g_{Σ} are the corresponding g factors. g_{Λ} is 0 for neutrons and 1 for

Table 1: Initial level energy, E_i , spin-parity, J_i^{π} , and branching ratio, B_{tot} (corrected for electron conversion) of the levels obtained for ¹⁶⁰Sm in this work. For each γ ray the energy, E_{γ} , γ -ray intensity, I_{γ} relative to the 1128 keV γ -ray intensity, and final level spin, J_f^{π} , are listed

are instea	•				
$E_{\rm i}$	J_{i}^{π}	E_{γ}	$I_{\gamma}(rel.)$	$B_{tot}(rel.)$	$J_{\rm f}^{\pi}$
(keV)		(keV)			-
71	(2^+)	$71(1)^{a}$		100	0^{+}
232.9	(4^{+})	161.9(3)	91(11)	100	(2^+)
483.2	(6^+)	250.3(4)	34(6)	100	(4^+)
1361.0	(5^{-})	877.8(4)	24(5)	20(5)	(6^+)
		1127.9(4)	100	80(19)	(4^+)
1468.5	(6^{-})	107.5(3)	26(5)	100	(5^{-})
1602.0	(7^{-})	133.5(3)	53(8)	100	(6^{-})
1754.3	(8^{-})	152.3(4)	45(9)	84(25)	(7^{-})
		286.4(4)	12(3)	16(5)	(6^{-})
1925.7	(9^{-})	171.4(4)	24(5)	62(17)	(8^{-})
		324.1(4)	20(5)	38(11)	(7^{-})
2116.1	(10^{-})	190.4(4)	30(6)	51(12)	(9^{-})
		362.0(3)	35(6)	49(11)	(8^{-})
2325.2	(11^{-})	209.1(5)	6(4)	33(25)	(10^{-})
		399.5(5)	13(4)	67(52)	(9^{-})
2757.3	(11^{+})	432.1(4)	21(5)	25(6)	(10^{-})
		641.1(3)	64(9)	75(18)	(11^{-})

 $^{\rm a}$ The 71 keV γ ray is only observed in coincident spectra.

Table 2: Low-lying quasiparticle states in ¹⁶⁰Sm predicted by blocked-BCS calculations (marked with a B) and potential energy surface calculations (marked with a P). The potential energy surface calculations have only been performed for the lowest energy states.

K^{π}	configuration	$E_x^B(E_x^P)$ (MeV)	E_x^{exp} (MeV)
ν two-q	р		
6^{-}	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{7}{2}^{+}[633]$	$1.401 \ (1.727^{\rm a})$	1.468
3^{+}	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{1}{2}^{-}[521]$	$1.674^{\rm b}$	
5^{+}	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{5}{2}^{-}[512]$	1.953	
3^{-}	$\nu \frac{1}{2}^{-}[521] \otimes \nu \frac{5}{2}^{+}[642]$	2.115	
π two-q	р		
5^{-}	$\pi \frac{5}{2}^{-}[532] \otimes \pi \frac{5}{2}^{+}[413]$	$1.032 (1.457^{\rm a})$	1.361
4^{-}	$\pi \frac{5}{2}^{-}[532] \otimes \pi \frac{3}{2}^{-}[411]$	1.569^{b}	
4^{+}	$\pi \frac{5}{2}^{+}[413] \otimes \pi \frac{3}{2}^{-}[411]$	1.631	
4^{-}	$\pi \frac{5}{2}^{+}[413] \otimes \pi \frac{3}{2}^{-}[541]$	2.107	
four-qp	•		
11^{+}	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{7}{2}^{+}[633],$	$2.433 (3.214^{\rm a})$	2.757
	$\pi \frac{5}{2}^{-}[532] \otimes \pi \frac{5}{2}^{+}[413]$		
8-	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{1}{2}^{-}[521],$	2.706^{b}	
	$\pi \frac{5}{2}^{-}[532] \otimes \pi \frac{5}{2}^{+}[413]$		
10^{+}	$\nu \frac{5}{2}^{-}[523] \otimes \nu \frac{7}{2}^{+}[633],$	2.970^{b}	
	$\pi \frac{5}{2}^{-}[532] \otimes \pi \frac{3}{2}^{-}[411]$		

^a $(\beta_2, \beta_4, \beta_6) = (0.294, 0.052, -0.017), (0.287, 0.046, -0.011),$ and (0.290, 0.048, -0.013) for $K^{\pi} = 6^-, 5^-$, and 11^+ states respectively.

^b 200 keV has been added to these states as they have energetically unfavoured configurations according to the residual spin-spin coupling rule.

Table 3: Experimental g_K values for various transitions in ¹⁶⁰Sm, considering K = 5 and K = 6 bandheads. Two values exist due to the modulus $|g_K - g_R|$. Theoretical values are $g_K = 0$ for neutrons and $g_K = 1$ for protons.

\mathbf{K}^{π}	$J_{ m i}^{\pi}$	E_1 and E_2 (keV)	g_K^{exp}
5^{-}	11-	209 and 399	-0.11(27), 0.71(26)
5^{-}	10^{-}	190 and 362	-0.12(14), 0.72(14)
5^{-}	9^{-}	171 and 324	-0.10(16), 0.70(16)
5^-	8-	152 and 286	-0.24(23), 0.84(23)
5^{-}	we	ighted average	-0.13(16), 0.73(16)
6^{-}	11^{-}	209 and 399	0.00(20), 0.60(20)
6^{-}	10^{-}	190 and 362	0.00(10), 0.61(10)
6^{-}	9^{-}	171 and 324	0.03(11), 0.57(11)
6^{-}	8-	152 and 286	-0.13(37), 0.73(37)
6^{-}	we	ighted average	-0.01(16), 0.61(16)

protons, and g_{Σ} is 4.99 for protons and -3.23 for neutrons; attenuated from their free values by a factor of 0.6 [19]. Our BCS calculations have revealed a 6⁻ two-qp state is lowest in energy for neutrons and a 5⁻ two-qp state is lowest in energy for protons. The expected g_K for these configurations is 0 and 1 respectively. The experimental values for g_K are found using the following:

$$\frac{|g_K - g_R|}{Q_0} = 0.933 \frac{E_1}{\delta \sqrt{I^2 - 1}}$$

where g_R is the rotational g factor, taken as 0.3 [19], Q_0 is the intrinsic quadrupole moment, taken to be 7.0 $e \cdot b$ from Sm systematics, and E_1 is the energy of the M1/E2 mixed transition in MeV from an initial state with spin I. The quadrupole/dipole mixing ratio, δ , is calculated using the formula:

$$q = \frac{\delta^2}{1+\delta^2} = \frac{2K^2(2I-1)}{(I-K-1)(I+K-1)(I+1)} \frac{E_1^5}{E_2^5} \lambda_b$$

where λ_b is the γ -ray branching ratio and E_2 is the energy of the E2 transition from the initial state. The results can be seen in table 3. Two values of g_K are given due to the rearrangement of the modulus, $|g_K - g_R|$ in the above equation. These values show that the bandhead regardless of K^{π} must be comprised of a two-neutron state, as they are consistent with the theoretical value of $g_K = 0$, but not with $g_K = 1$.

The assignment of a (6^-) neutron bandhead for the main band structure, rather then a (5^-) neutron bandhead is made on the basis of a lack of observation of a transition from the 7⁻ state to the 5⁻, which would have an energy of 240 keV. The expected γ -ray intensity of this transition was calculated using the g-factor formula, rearranged for I_{γ} and found to be 570(70) counts (assuming E2 multipolarity). This transition, if present, would be easily observable in the γ -ray energy spectrum, with $I_{\gamma}(rel.) = 12(2)$, comparable to the 286 keV peak. As we do not observe this peak, we assign the bandhead to the (6^-) state rather then the (5^-) state.



Figure 3: Reduced hindrance, f_{ν} , of E1 transitions versus the difference between excitation energy of the isomeric state and the rigid rotor energy. Data points taken from Refs. [19, 22–28] and the current work. A pairing energy of 0.9 MeV has been added to odd-A nuclei.

It has been noted in this mass region that β_6 deformation can be significant [18] and can have a measurable effect on the structure of the nucleus [7]. In order to quantify this effect potential energy surface calculations were performed on ¹⁶⁰Sm and its neighbouring nuclei. The total energy of the configurations was minimised in (β_2, β_4) deformation space and $(\beta_2, \beta_4, \beta_6)$ deformation space. For more details see Refs. [20, 21]. The inclusion of β_6 in the calculations has the greatest effect on the 6^- 2-neutron state in 160 Sm, where the energy is reduced by 100 keV. Conversely, the energy of the 5^- 2-proton state increases by 50 keV with the inclusion of β_6 , enabling the 6⁻ state to compete. Consequently, β_6 plays a role in moving the calculated 6^- and 5^- bandheads closer together in energy. The energies of the assigned bandheads calculated using $(\beta_2, \beta_4, \beta_6)$ deformation space are shown in table 2.

The reduced hindrance of a transition removes the dependence of the half-life on energy and the multipole order, λ , of the transition. Therefore we would expect similar reduced hindrance values for isomers around ¹⁶⁰Sm. However, a systematic study of E1 transitions reveals an f_{ν} dependence on $E - E_R$, similar to that known for E2 transitions [29], where E is the energy of the isomeric state and E_R is the rigid rotor energy for the same angular momentum. The rigid rotor energy of ¹⁶⁰Sm was calculated to be 927 keV, using a moment of inertia of $71\hbar^2 \text{ MeV}^{-1}$, found by scaling with $A^{5/3}$ using $85\hbar^2 \text{ MeV}^{-1}$ for ¹⁷⁸Hf. For the (11⁺) isomer this gives $E - E_R = 1.83$ MeV.

The reduced hindrances of the 432 and 641 keV transitions, and the 878 and 1128 keV transitions were calculated. All four E1 transitions have very similar reduced hindrance values of 21(1), 22(1), 21(2) and 18(2) for 432, 641, 878, and 1128 keV respectively. Following common practice [22–24, 27], F_W has been divided by 10⁴ in an attempt to allow for the hindered nature of K-allowed E1

Nucleus	K^{π}	$t_{1/2}$	E_{γ} (keV)	E (MeV)	$E - E_R$	ν	$f_{ u}$
					(MeV)		
$^{160}\mathrm{Sm}$	(11^{+})	$1.8(4) \ \mu s$	641	2.78	1.83	4	22
^{160}Sm	(11^{+})	$1.8(4) \ \mu s$	432	2.78	1.83	4	21
164 Er [24]	12 +	68(2) ns	555	3.38	2.33	4	9.4
173 Tm [27]	35/2 -	121(28) ns	655	4.05	2.95^{*}	6	8.3
174 Yb [25, 26]	14 +	55(4) ns	786	3.70	2.42	6	9.9
¹⁷⁴ Hf [23]	14 +	$3.7 \ \mu s$	379	3.31	2.03	5	15
¹⁷⁴ Hf [23]	14 +	$3.7 \ \mu s$	155	3.31	2.03	7	8.9
¹⁷⁵ Hf [23]	45/2 +	$2 \ \mu s$	291	4.64	2.34^{*}	4	19
182 Hf [22]	(13+)	$40(10) \ \mu s$	264	2.57	1.54	4	24
¹⁷⁹ W [19]	35/2-	750(80) ns	625	3.35	2.36^{*}	12	4.1
183 Os [28]	43/2 -	27(3) ns	351	5.07	3.25^{*}	4	4.9

Table 4: Data summary of four-qp and higher-order-qp isomers with E1 transitions used in Fig. 3. Those marked with * have 0.9 MeV added to account for pairing energy.

transitions.

A plot of f_{ν} versus $E - E_R$ can be seen in Fig. 3 for E1 transitions with $\nu \ge 4$. Isomers with $\nu < 4$ are less forbidden and therefore excluded. The data are summarised in table 4. The solid line in the plot is taken from statistical calculations for E2 transitions [29]. The data from E1 transitions, including the new data point from the four-qp isomer in ¹⁶⁰Sm agree well with this trend. This relationship is evidence that reduced hindrance is sensitive to the excitation energy of the four-qp isomeric state. This could be due to greater K mixing at higher excitation energies: the density of states increases with excitation energy which statistically leads to more states with the same spin and parity to mix with [29]. To further test this relationship, data on lighter deformed isomers with four-qp states are required.

To date, ¹⁶⁰Sm is the lightest four-qp K isomer observed. Blocked-BCS calculations were performed on lighter nuclei in this region to test the limits of existence of four-qp isomers. The next best candidate is predicted to be a four-qp isomer in ¹⁵⁸Sm, with $K^{\pi} = 10^+$ and E = 2.424 MeV. However, to date only a two-qp isomeric state has been observed in this nucleus [3]. Due to the lower spin, the predicted four-qp isomer in ¹⁵⁸Sm would likely have a shorter half-life than that of ¹⁶⁰Sm. Overall, the calculations show that ¹⁶⁰Sm is the strongest candidate for the lightest four-qp isomer to exist in this region, consistent with our new observations.

In summary, a new four-qp isomer has been observed in 160 Sm with a half-life of $1.8(4)\mu$ s. The level scheme has been extended using the present spectroscopic data. This is the lightest four-qp K isomer observed to date. The new data from 160 Sm agree well with the inverse correlation between reduced hindrance and excitation energy for E1 and E2 transitions, shown here for the first time for E1 transitions. Blocked-BCS calculations reveal 160 Sm and 158 Sm are the best candidates for deformed four-qp isomers. However, further experiments are needed to ascertain the Z and N limits for their existence.

Acknowledgements

This work was carried out at the RIBF operated by RIKEN Nishina Center, RIKEN and CNS, University of Tokyo. All UK authors are supported by STFC. P. H. R. and G. L. are partially supported by the UK National Measurement Office (NMO). P.-A. S. was financed by JSPS Grant Number 23.01752 and the RIKEN Foreign Postdoctoral Researcher Program. J. T. was financed by Spanish Ministerio de Ciencia e Innovación under Contracts No. FPA2009-13377-C02 and No. FPA2011-29854-C04. Zs. D., I. K., and Zs. V. were supported by OTKA contract number K100835. We acknowledge the EUROBALL Owners Committee for the loan of germanium detectors and the PreSpec Collaboration for the readout electronics of the cluster detectors. This work was supported by JSPS KAKENHI Grant No. 25247045.

References

- [1] P. Walker, G. Dracoulis, Nature 399 (1999) 35.
- K. Jain, P. Walker, N. Rowley, Physics Letters B 322 (1994) 27.
 F. Kondev, G. Dracoulis, T. Kibédi, Atomic Data and Nuclear Data Tables 103 (2015) 50.
- [4] E. H. Wang, J. H. Hamilton, A. V. Ramayya, *et al.*, Phys. Rev. C 90 (2014) 067306.
- [5] S. J. Zhu, J. H. Hamilton, A. V. Ramayya, et al., Journal of Physics G: Nuclear and Particle Physics 21 (1995) L57.
- [6] G. S. Simpson, W. Urban, J. Genevey, et al., Phys. Rev. C 80 (2009) 024304.
- [7] Z. Patel, P.-A. Söderström, Z. Podolyák, et al., Phys. Rev. Lett. 113 (2014) 262502.
- [8] M. Hellström, B. Fogelberg, H. Mach, et al., Phys. Rev. C 46 (1992) 860.
- [9] M. Hellström, H. Mach, B. Fogelberg, et al., Phys. Rev. C 47 (1993) 545.
- [10] X. Q. Zhang, J. H. Hamilton, A. V. Ramayya, et al., Phys. Rev. C 57 (1998) 2040.
- [11] C. Gautherin, M. Houry, W. Korten, et al., The European Physical Journal A - Hadrons and Nuclei 1 (1998) 391.
- [12] T. Kubo, D. Kameda, H. Suzuki, et al., Prog. Theor. Exp. Phys. (2012) 03C003.
- [13] Y. Yano, Nuclear Instruments and Methods in Physics Research Section B: Beam Interactions with Materials and Atoms 261 (2007) 1009.

- [14] S. Nishimura, Prog. Theor. Exp. Phys. 2012 (2012) 03C006.
- [15] S. Nishimura, Nucl. Phys. News Int. 22 (2012) 38.
- [16] P.-A. Söderström, S. Nishimura, P. Doornenbal, et al., Nucl. Instrum. Meth. B 317 (2013) 649.
- [17] K. Jain, O. Burglin, G. Dracoulis, et al., Nuclear Physics A 591 (1995) 61.
- [18] P. Möller, J. Nix, W. Myers, W. Swiatecki, Atomic Data and Nuclear Data Tables 59 (1995) 185.
- [19] P. Walker, G. Dracoulis, A. Byrne, *et al.*, Nuclear Physics A 568 (1994) 397.
- [20] F. Xu, P. Walker, J. Sheikh, R. Wyss, Physics Letters B 435 (1998) 257.
- [21] H. L. Liu, F. R. Xu, P. M. Walker, C. A. Bertulani, Phys. Rev. C 83 (2011) 011303.
- [22] R. D'Alarcao, P. Chowdhury, E. H. Seabury, *et al.*, Phys. Rev. C 59 (1999) R1227.
- [24] T. P. D. Swan, P. M. Walker, Z. Podolyák, et al., Phys. Rev. C 86 (2012) 044307.
 [25] C. D. Dracenlis, C. L. Leng, F. C. K. et al., Phys. Rev. C
- [26] G. D. Dracoulis, G. J. Lane, F. G. Kondev, *et al.*, Phys. Rev. C 73 (2006) 019901.
- [27] R. O. Hughes, G. J. Lane, G. D. Dracoulis, et al., Phys. Rev. C 86 (2012) 054314.
- [28] T. Shizuma, K. Matsuura, Y. Toh, et al., Nuclear Physics A 696 (2001) 337.
- [29] P. Walker, D. Cullen, C. Purry, et al., Physics Letters B 408 (1997) 42.