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Real-Time Feature Selection Technique with Concept Drift Detection using Adaptive Micro-Clusters for Data Stream Mining

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Abstract

Data streams are unbounded, sequential data instances that are generated with high *Velocity*. Classifying sequential data instances is a very challenging problem in machine learning with applications in network intrusion detection, financial markets and applications requiring real-time sensor-networks-based situation assessment. Data stream classification is concerned with the automatic labelling of unseen instances from the stream in real-time. For this the classifier needs to adapt to concept drifts and can only have a single pass through the data if the stream is fast moving. This research paper presents work on a real-time pre-processing technique, in particular feature tracking. The feature tracking technique is designed to improve Data Stream Mining (DSM) classification algorithms by enabling and optimising real-time feature selection. The technique is based on tracking adaptive statistical summaries of the data and class label distributions, known as Micro-Clusters. Currently the technique is able to detect concept drifts and identify which features have been influential in the drift.

Keywords: Data Stream Mining, real-time Feature Selection, Concept Drift Detection

1. Introduction

Velocity in Big Data Analytics [1] refers to data that is generated at ultra high speed and is live-streamed whereupon the processing and storing of it in real-time (Data Stream Mining, DSM) constitute significant challenges to current computational capabilities [2]. Thus data stream mining algorithms that are capable of learning over a singlepass through the training data are necessary. The general area of Data Stream Mining covered by this paper is Data Stream Classification, which is the prediction of class labels of new instances in the data stream in real-time. Potential applications that need real-time data stream classification techniques are for data streams in the chemical process industry [3], intrusion detection in telecommunications [4], etc. In order to keep as high a predictive accuracy as possible, data stream classification techniques need not only be able to learn incrementally but also be able to adapt to concept drifts.

A concept drift occurs if the pattern encoded in the data stream changes. DSM has developed various realtime versions of established predictive data mining algorithms that adapt to concept drift and keep the model accurate over time, such as CVFDT [5] and G-eRules [6]. The benefit of classifier independent concept drift detection methods is that they give information about the dynamics of data generation [7]. Common drift detection methods are for example ADaptive sliding WINdow (AD-WIN) [8], Drift Detection Method (DDM) [9] and the Early Drift Detection Method (EDDM)[10]. However, no drift detection method devised to-date, can provide potentially highly valuable insights as to which features are involved in the concept drift. For example, if a feature is contributing to a concept drift it can be assumed that the feature may have become either more or less relevant to the current concept. This causal responsibility theoretic perspective of the evaluation of concept drift has inspired the development of a real-time feature tracking method based on feature contribution information for the purpose of feature selection to identify features that have become (more) relevant or irrelevant due to concept drift. Thus, an approach for detecting causality of drifts, providing the feature contribution information for the purpose of tracking features and identifying the relevant features for classification for the purpose of feature selection in real-time has been developed in this research.

Common feature selection techniques are for example Linear Discriminant Analysis (LDA), Canonical Correlation Analysis (CCA), Multi-View CCA, Principal Component Analysis (PCA) [11, 12], and Support Vector Machine (SVM) based techniques. These techniques can be applied on a sample of the data stream before commencing the training and adaptation of a data stream classifier. However, this would not account for changes in the relevance of features for the classification task at hand due

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to concept drift which can be dealt with by re-running the above methods to update the feature rankings in order to accommodate any drifts. However, this can potentially be an expensive procedure especially if there are many dimensions in the data, but it also depends on the user settings of how frequently this feature re-ranking is performed. Hence, the rationale for a single-pass method requiring the re-evaluation of only the features where the classification relevance has changed since the last pass.

This research therefore describes a concept drift detection method for data stream classification algorithms with the feature tracking capability. This enables linking features to concept drifts over a statistical sliding window for feature selection purposes. The method only needs to examine features that have potentially changed their relevance and only when there is an indication that the relevance of a feature may have changed. The proposed method can be used with any learning algorithm either as a real-time wrapper or a batch classifier or realised inside a real-time adaptive classifier [13, 6]. Previous work of the authors has developed a feature tracking technique [14], however, the techniques was not used for feature selection purposes as it suffered from over-fitting on noise and outliers. Thus the contributions of this paper are:

- 1. A new improved Concept Drift detection technique with Feature Tracking capabilities.
- 2. A feature selection technique based upon the causality of drifts obtained through the developed Feature Tracking method.

This paper is organised as follows: Section 2 describes related works, Section 3 summarises the MC-NN classifier whose data representation has been used and modified for the real-time feature selection method presented here. Section 4 introduces the drift detection method developed in this research and Section 5 explains the developed feature tracking method. Section 6 takes these developments forward to devise a real-time feature selection approach. Section 7 provides an empirical evaluation of the developed methods and concluding remarks are given in Section 8.

2. Related Work

2.1. Concept Drift Detection Techniques

A concept drift occurs if the pattern encoded in the data stream changes over time. The gathered data changes or shifts, after a stability period. Identifying a drift point as distinct from noise or outlier, is the first and most challenging task for drift detection algorithms [15, 7]. Thus analytics algorithms need to adapt. This issue of concept drift needs to be considered in order to mine relevant data with appropriate accuracy. At least four types of drift can be identified; gradual, sudden, recurring, and incremental, as well as noise and outliers which may occur in the data stream [15, 7, 16, 17].

Outliers and noise are not concept drifts. Often it is very difficult for concept drift detection methods to distinguish noise and outliers from real concept drift.

There exist standalone concept drift detection techniques that can be used in combination with batch learning algorithms and a sliding window approach. For example one of these techniques is CUmulative SUM (CUSUM) [18]. CUSUM raises alarms when the mean μ of the input data is significantly different from zero. CUSUM is considered to be 'almost memoryless', however, it can only be applied in one statistical direction, i.e., detecting only significant increases in feature values.

Another technique is the Drift Detection Method (DDM) [9]. DDM computes error statistics based on two time windows. A concept drift is triggered for sudden concept drifts only, while gradual concept drifts are not detected [19]. Early Drift Detection Method (EDDM) [10] is an extension of DDM, estimating distribution of the distances among classification errors, however, the method is susceptible to noise. The Exponential Weighted Moving Average (EWMA) [20] is also similar to DDM, but the estimate of the error rate is updated faster for each point in the data stream. The ADaptive sliding WINdow (ADWIN) method [8] makes use of a variable size sliding window, whereas the size is dependent on observed changes. If there is a change then the window size decreases, otherwise it increases. A problem with ADWIN is that windows can become potentially very large and thus the time to adapt a classifier may increase.

However, we are not aware of any drift detection method that also provides information as to the causes of the drift, i.e. which features were involved in the genesis of the drift.

2.2. Feature Selection Techniques

Feature selection is used to reduce the dimensions of data streams, aiming to retain only relevant features (i.e. features highly correlated with class labels). This is because learning good classifiers can be achieved by removing irrelevant features [21, 22].

Many techniques have been proposed for dimensionality reduction such as Linear Discriminate Analysis (LDA), Canonical Correlation Analysis (CCA), Multi-View CCA, and Principal Component Analysis (PCA) [11, 12]. LDA transforms two groups of class labels into two matrices to be matched together. CCA is a statistical method which aims to search a linear subspace in which the correlation between two sets of class labels is maximised. Multi-View CCA [11] is an extension of CCA which searches for a pairwise correlation between all sets of class labels. PCA aims to merge the different feature vectors in a low dimensional space of eigenvectors which keeps their direction unchanged when a linear transformation is applied to them. A very popular mechanism to select relevant features for a classification task is based on Information Gain measure which is also used in building decision trees [23]. The assumption is that the higher the Information Gain of an attribute the more likely it is relevant for the classification task.

The aforementioned feature selection techniques are by no means an exhaustive list of techniques. However, they all share a common placing in that they are typically applied before a classifier is induced. Thus these techniques are not designed for data streams as they do not take into consideration that the relevance of a feature for a classification task may change over time. Thus, real-time feature selection techniques are needed.

2.3. Data Stream Classification

Several methods have been proposed for predictive analytics on data streams. The most notable data stream classifier is probably the Hoeffding Tree family of algorithms. The Hoeffding Tree algorithm by Domingos and Hulten [13] introduces a decision tree incrementally in real-time. The Hoeffding Tree was improved in terms of speed and accuracy by proposing a Very Fast Decision Tree (VFDT) [5]. Although achieving high accuracy using a small sample is the main advantage of these algorithms, concept drift detection cannot be handled as a created sub-tree can only expand from the child nodes onwards. A new version of VFDT, termed CVFTD where C stands for Concept Drift [5], was introduced. Broadly speaking, in CVFDT alternative sub-trees can be induced over time and if an alternative sub-tree outperforms (i.e. in terms of accuracy) the current active sub-tree, then the current sub-tree has to be replaced with the alternative one. However, if subtrees are growing continuously, then a large amount of memory is consumed, also CVFDT is susceptible to noise and unable to handle recurring drifts [24]. Further data stream classification algorithms have been proposed, such as a Similarity Search Structure called the Rank Cover Tree (RCT) [25], Online Data Stream Classification with Limited Labels [26], Prototype-based Classification Model [27], Adaptive Nearest Neighbour Classification for Data Streams [28], Ensemble based Classification [29], VFDR [30], Online Data Stream Classification with limited labels [26], Prototype-based Classification Model [27], DBScan [31], SFNClassifier [32], and G-eRules [6].

Although, most of these algorithms have a built-in concept drift detection capability, none of them takes online feature selection into consideration. If feature selection is applied at all, then it is mostly at the beginning of the data stream and it is assumed that the contribution of each feature to the concept remains invariant over time. However, this is an unrealistic assumption. The relevance of features for the concept may change over time and thus an online feature selection strategy may very well improve the predictive accuracy of the classifier.

2.4. Data Stream Clustering

Clustering is the partitioning and grouping of a particular set of observations according to the similarities of their characteristics. Several Data Stream Cluster Analysis algorithms with minimum time and memory demands have been proposed over the years. These algorithms typically need only one pass through the data in order to adapt to concept drifts. Some notable algorithms here are BIRCH [33], CluStream [34], HPStream [35], E-Stream [36], Clus-Tree [37], HUE-Stream [38], and MC-NN [39].

A notable development of these cluster analysis algorithms is the aforementioned BIRCH which builds statistical summaries of the clusters and is able to learn incrementally. These statistical summaries are also often referred to as Micro-Clusters. However, BIRCH does not forget concepts and thus its ability to adapt to concept drifts is limited. An extension of BIRCH is the ClusTree algorithm mentioned above, it implements a hierarchical data stream clustering algorithm. Also the aforementioned CluStream algorithm extends the Micro-Clusters with a time component, enabling the algorithm to forget old and obsolete concepts. A more recent extension of CluStream is the MC-NN algorithm. MC-NN is also built on a further extension of the CluStream Micro-Clusters, it adds splitting of Micro-Clusters to adapt to concept drift and uses these Micro-Clusters primarily for parallel predictive analytics in real-time. The research presented in this paper is inspired by the ability of MC-NN Micro-Clusters to adapt to concept drift and has developed a new Micro-Cluster structure. Thus MC-NN will be discussed in more detail in Section 3.

Please note, none of the aforementioned techniques is capable of tracking the causality of a concept drift which could be very useful for real-time feature selection. At the moment feature selection is typically ignored in datastream mining tasks or simply applied prior to starting a workflow. The remainder of this paper discusses new concept drift detection method that is able to track feature involvement in concept drift. Furthermore a method is then used to facilitate feature selection in real-time.

3. Micro-Cluster Nearest Neighbour (MC-NN)

This section summarises the previously mentioned MC-NN approach [39]. MC-NN was originally developed for predictive data stream analytics, however, the underlying Micro-Cluster structure of MC-NN has been adapted and extended in this research in order to develop a feature tracker for online feature selection purposes. Thus MC-NN is discussed in greater detail. Essentially there are three operations to adapt MC-NN to concept drifts: (1) absorption of data instances into nearest Micro-Clusters, (2) splitting of Micro-Clusters with high variance and (3) removal of obsolete Micro-Clusters.

3.1. The Structure of MC-NN Micro-Clusters

Micro-Clusters in MC-NN provide statistical summaries of feature values over time stamps. In [39], the structure of Micro-Clusters is: $\langle CF2^x, CF1^x, CF1^t, n, CL, \epsilon, \Theta, \alpha, \Omega \rangle$. Details about the Micro-Cluster structure components are listed in Table 1.

Table 1: The Structure of MC-NN Micro-Clusters.

Structure	Description
Component	
$CF2^x$	a vector with the sum of squares of the features
$CF1^x$	a vector with the sum of feature values
$CF1^t$	a vector with the sum of time stamps
n	the number of data instances in the cluster
CL	the majority class label of the cluster
ε	the error count
Θ	the error threshold for splitting the Micro-Cluster
α	the initial time stamp
Ω	a minimum (user defined) threshold for the
	Micro-Cluster minimum participation

The components listed in Table 1 are used to compute the centroid for a feature within a Micro-Cluster x:

$$centroid(x) = \frac{CF1^x}{n} \tag{1}$$

and the Variance of a feature within a Micro-Cluster:

$$Variance[x] = \sqrt{\left(\frac{CF2^x}{n}\right) - \left(\frac{CF1^x}{n}\right)^2}$$
(2)

3.2. The Training or Absorbing Instances

Each Micro-Cluster is updated by adding a new instance to its nearest Micro-Cluster's centroid if it is within the boundary (*Variance*) of the Micro-Cluster, (see Figure 1). The error ϵ is decremented by 1 if a new instance matches the *CL*. Otherwise, if the nearest Micro-Cluster does not match the *CL*, then the new instance is still added to the nearest Micro-Cluster, however, the Micro-Cluster error ϵ is incremented by one; also the error ϵ of the nearest Micro-Cluster that matches the *CL* is incremented by 1. In the case that the data instance is outside the boundary (*Variance*) of its nearest Micro-Cluster, then loosely speaking, the instance builds a new Micro-Cluster.

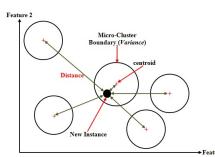


Figure 1: An example of adding a new instance to the nearest Micro-Cluster.

3.3. Splitting of a Micro-Cluster using Variance

MC-NN splits a Micro-Cluster in two new clusters once the error count ϵ reaches Θ and the original Micro-Cluster is removed in order to improve the fit to evolving data streams. The new Micro-Clusters are placed about the original Micro-Cluster feature that has the greatest *Variance* for a feature x (illustrated in Figure 2). The assumption

MC-NN makes here is that the feature with the highest *Variance* is the most likely to contribute to mis-absorption.



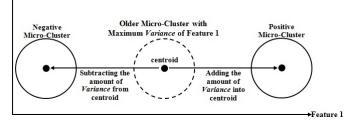


Figure 2: Splitting of a Micro-Cluster according to the feature with the highest Variance.

3.4. Death and Removal of a Micro-Cluster using Triangle Numbers

MC-NN removes a Micro-Cluster (Micro-Cluster *Death*) if it has not participated recently in absorbing data instances, which can be calculated from $CF1^t$ by measuring the Triangle Number (Equation 3). The Triangle Number gives more weight to recent Micro-Clusters than the older ones. If the participation percentage of a Micro-Cluster is lower than Ω then the Micro-Cluster is removed. The assumption MC-NN makes is that older non-participating Micro-Clusters reflect old and potentially obsolete concepts.

Triangle Number
$$\Delta(T) = ((T^2 + T)/2)$$
 (3)

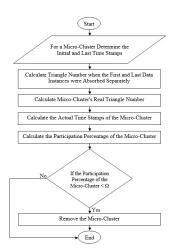


Figure 3: The process of calculating the Triangle Number for a Micro-Cluster.

The process of calculating the Triangle Number is given in Figure 3 and highlighted in an example in Figure 4. Consider the Micro-Cluster in the example. It was created at time stamp 2 and updated with instances at time stamps 4 and 6, the current time stamp is 7 but here it was not updated. On the right hand side of Figure 4 we have depicted the calculations for the different steps involved in the process depicted in Figure 3.

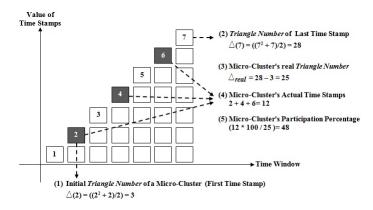


Figure 4: An Example of Triangle Number calculation. The shaded areas signify the time stamps where the Micro-Cluster has participated in absorbing new instances for a particular time stamp

3.5. Taking MC-NN Forward to Develop a Real-time Feature Selection Method

Sections 4, 5 and 6 take some of MC-NN's ideas forward to facilitate real-time feature selection. The basic idea is to monitor Micro-Cluster *Split rates* and *Death rates* in order to detect concept drifts. It is expected that concept drifts will cause a peak in splitting and removing of Micro-Clusters. The *Velocity* and direction of movement of the Micro-Clusters can be used as an indication as to which features have changed and potentially contributed towards a concept drift. Then, in turn, features that have shown significant changes during a concept drift can be examined separately for their relevance to the classification task.

For clarity we note the semantic distinctions in our usage of three terms relating to time and temporal referencing of a point or an interval in the timeline, namely 'time', 'time window', 'time stamp'. In our analysis 'time' and 'time window' are regarded as equivalent references used interchangeably to mean a duration of time as encapsulating a set of data instances with sequential time intervals of fixed length. Whereas 'time stamp' is a means of indexing time, i.e. provides a mark-up for, a particular data instance at a particular point in time. For example assuming a stream has generated 2000 sequential data instances and each time window is of length 1000, then there would be two time windows, time window 1 from time stamp 0to 999 and time window 2 from time stamp 1000 to 1999. This may be for example referred to in the paper as time 1 or time 2 meaning time window 1 and 2.

4. Real-Time Concept Drift Detection Technique using Adaptive Micro-Clusters

The MC-NN algorithm aims to keep a recent and accurate summary of the data stream using Micro-Clusters. Significant changes to these summaries are used in this research to detect concept drift.

4.1. Detecting Concept Drift using Adaptive Micro-Clusters

It is expected that during a concept drift the data distribution changes (causing larger *Variance* within Micro-Clusters), but also it is expected that Micro-Clusters absorb more incorrect data instances (different class labels than the Micro-Cluster). When new concepts arrive, MC-NN adapts by applying *Split* (Micro-Cluster Splitting) and *Death* (Micro-Cluster removal), as explained in Section 3.

Loosely speaking, regarding *Split*, two new Micro-Clusters are generated from the original one when the error counter reaches the error threshold due to false positive participation. Likewise some of the existing Micro-Clusters may stop to participate as they become obsolete and are removed. Both will result in a higher number of *Splits* and *Deaths* over time. In this research we measure *Split* and *Death* rates over time simply by using Equation 4 for each time window. Here n is the number of instances in a time window and i is the index of the current data instance within the time window, starting with 1 within each time window. Figure 5 illustrates an example of monitoring a *Split* or *Death* rate. In this sense the calculation of *Split* and *Death* is conducted gradually instance by instance within a time window.



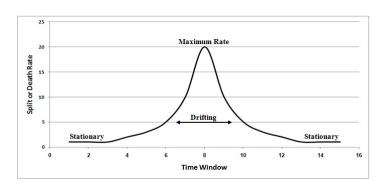


Figure 5: An example of Micro-Cluster Split and Death Rate.

The assumption is the larger both rates are, the more likely it is a concept drift has happened. Using a windowing approach on the data stream, a running average of the *Split* and *Death* rates are calculated separately, as well as the *Percentage Difference* which is given by Equation 5. In the equation i denotes the current time window.

$$Percentage \ Difference = \frac{|Rate_i - Rate_{i-1}|}{(Rate_i + Rate_{i-1})/2} * 100$$
(5)

If the *Percentage Differences* of both, the *Split* and *Death* rates differ from the μ (of the current and previous window) by 50% (default value), then this is considered as a concept drift. In this work the default value of 50% has been used for all experiments as it yielded accurate results in most cases. However, the user may change this to a

different threshold. This is illustrated in Algorithm 1. A worked example is presented in Section 4.2.

Algorithm 1 Detection of Drifts

Input: Micro-Cluster(s) *Split* and *Death* rates for current and previous window

Output: Detection of Drifts

- 1: Calculate the μ of *Split* and *Death* rates over the current and previous window
- Calculate the Percentage Difference for both, Split and 2: Death rates
- 3: if new Split rate > μ (Split rate) AND new Death rate $> \mu$ (Death rate) **AND** Percentage Difference (Split rate) > 50% **AND** *Percentage Difference (Death* rate) > 50% then
- Concept Drift 4:
- 5: reset MC(s)

else 6:

- No Concept Drift 7:
- 8: end if

4.2. Worked Example

Split and Death rates of Micro-Clusters are as shown below in Figure 6 for the seven time windows.

Window	Micro-Cluster Split Rates							
	Split Rate	mean	Percentage Difference	Death Rate	mean	Percentage Difference	Drifting	
W_1	0.1	0	0	0.01	0	0		
W_2	0.1	0.1	0	0.01	0	0		
W_3	0.14	0.12	33.333	0.016	0.013	46.153		
W_4	0.3	0.22	72.727	0.04	0.028	85.714	Detected	
W_5	0.2	/0.25	40	0.03	0.035	28.571		
W_6	0.2	0.2	0	0.03	0.03	0		
W_7	0.2	0.2	0	0.03	0.03	0		
	Percent	age Differenc	$e = ((W_4 - W_3))$	/ mean) x 10	00 = ((0.3 - 0	.14) / 0.22) x 10	00= 72.727	

Figure 6: An example of Concept Drift Detection using the Micro-Clusters Split and Death Rates.

Consider the *Split* and *Death* rates of window (W_4) , which are equal to 0.3 and 0.04. This shows that the Split and Death rates differ from the μ value (i.e., 0.22) and 0.028) by 50% as the Percentage Difference of Split rate equals to 72.727, and the Percentage Difference of Death rate equals to 85.714. This indicates that a drift has occurred. After a concept drift is detected our method identifies which features have been involved in the drift by examining the Micro-Clusters change of Velocity, trajectory and spread of data such as *Variance* or Inter Quartile Range (IQR). This is described in Section 5.

tive Micro-Clusters

The Velocity or Variance of a feature can be derived from MC-NN Micro-Clusters and are calculated once a drift is detected as described in Section 4. The Velocity and Variance can then be analysed to identify features that have been involved in the drift. This information can be used for feature selection purposes which will be explained in Section 6. The tracking of features is potentially influenced by feature-bias, outlier and noise. Thus our method incorporates approaches to counter these influences. The remainder of this section discusses in Section 5.1 how the proposed method addresses potential featurebias, in Section 5.2 it is explained how the method addresses the problem of noise, Section 5.3 then explains how the features are tracked and outliers are taken into consideration. The proposed method uses a different means of measuring participation of Micro-Clusters than original MC-NN, (explained in Section 5.3), which is compared qualitatively in Section 5.3.6.

5.1. Minimising the Effect of Feature-Bias using Real-Time Normalisation

Normalisation is applied to fit the data (i.e., each feature of a new training instance) to be almost distributed in a pre-defined boundary such as [0,100]. Normalisation is used to avoid feature-bias which can potentially lead to mis-classifications as the relevant relations between target class labels and features are considered by the classifier to be more or less important than they actually are.

Three frequently used types of *Normalisation* are i.e. Min-Max (see Equation 6), Decimal Scaling (see Equation 7), and Z-Score (see Equation 8) [40]. These have been considered for inclusion in the proposed method.

$$x = \left(\frac{current \ value - \min x}{\max x - \min x}\right) * \left(\max range - \min range\right) + \min range \quad (6)$$

$$x = \frac{x}{(10^d)} \tag{7}$$

$$x = \frac{x - \mu}{\sigma} \tag{8}$$

x is a feature value of the new data instance. Min-Max is a simple *Normalisation* technique to fit the data in a pre-defined boundary with a min range (default 0) and a max range (default 100). Decimal Scaling moves the decimal point of a feature value x depending on its maximum absolute value whereby d equals to MAX(|y|) < 1 (i.e., the smallest value of a feature y). Lastly, Z-Score normalises a feature value x according to its corresponding μ and σ feature values.

In this research, Min-Max Normalisation technique was used as minimum and maximum values of a feature x can easily be reinitialised in real-time when new instances arrive. Equation 6 is applied for every new data instance 5. Real-Time Feature Tracking Technique using Adap-as shown in Figure 7. The alternative techniques mentioned above rely on the standard deviation and the mean and thus require the buffering of data before Normalisation can be applied. This is undesirable in real-time data analytics. However, the Normalisation process described

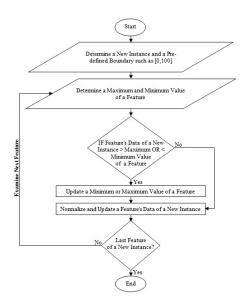


Figure 7: Flowchart of Min-Max Normalisation.

here, Min-Max Normalisation, can be updated incrementally instance by instance. Old instances cannot be renormalised as the original data values are not buffered but absorbed in the statistics of a Micro-Cluster. This could lead to Micro-Clusters not fitting the current concept well anymore. However, this would also contribute to the detection of the concept drift (Micro-Cluster Split) as the Variance of the Micro-Cluster would increase and potentially also the error count. Figure 8 shows an example of Min-Max Normalisation in real-time.

Next the Micro-Cluster by which the normalised data instance should be absorbed has to be determined. For this the training task of MC-NN described in Section 3.1 is applied. However, before the data instance is absorbed a Low Pass Filter (LPF) is applied to the Micro-Cluster to minimise the effect of noise.

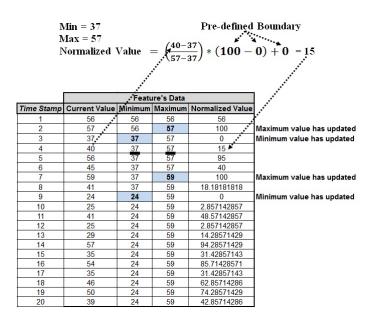


Figure 8: An Example of Min-Max Normalisation in real-time.

5.2. Minimising the Effect of Noise using Low Pass Filter (LPF)

LPF is a filter that passes signals (i.e., the Velocity of a feature) with a frequency lower than a certain cut-off frequency α and attenuates signals with frequencies higher than the cut-off frequency. LPF can be used to minimise the effect of noise [41, 42]. However, there are some other techniques proposed for the purpose of filtering such as the Kalman filter and Grid-based filter which require buffering of data before filtering [43]. Hence, in this work, LPF is used as it can be calculated over a sliding window without buffering of data. Each normalised feature of a new training instance was filtered by LPF together with its nearest Micro-Cluster using Equation 9 in order to improve concept drift detection and feature tracking. This is illustrated in Figure 9 showing a flowchart of LPF.

$$ew \ filter[x] = \alpha * new \ value[x] + (1 - \alpha) * old \ filter[x]$$
(9)

The α threshold is set for 0.5 by default, as this value yielded good results in most cases. However, the user may change this to a different threshold.

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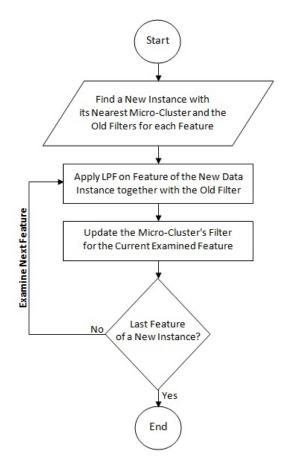


Figure 9: Flowchart of Low Pass Filter.

Figure 10 shows an example of *LPF*. The centroid of each filtered feature of a Micro-Cluster can be calculated. Micro-Clusters with normalised and filtered features are passed to the concept drift detection method which was described in Section 4.

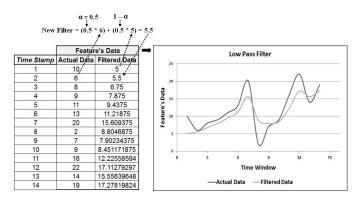


Figure 10: An Example of Low Pass Filter.

5.3. Real-Time Feature Tracking

This section describes real-time feature tracking measuring the *Velocity* and spread of a feature using both *Variance* and Inter Quartile Range (IQR) which can be derived from the captured statistics of the Micro-Clusters.

5.3.1. Velocity of Features

Velocity can be tracked through an extension of the MC-NN Micro-Cluster structure by: $\langle CF1^{hx}, n_h \rangle$. Where these components are equivalent to $CF1^x$ and n. However, the h denotes that these components are historical summaries (taken from the previous time stamp). The Velocity of a feature x can then be calculated using Equation 10. Figure 11 shows an example of feature Velocity with a Micro-Cluster consisting of two features.

$$Velocity[x] = \left| \frac{CF1^x}{n} - \frac{CF1^{h,x}}{n_h} \right| \tag{10}$$

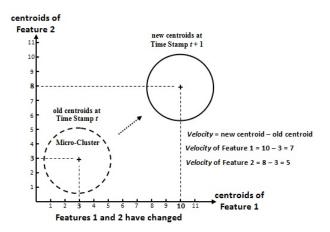


Figure 11: An Example of Feature Velocity.

5.3.2. Measuring of the Data Stream Spread using IQR

In original MC-NN the spread of the values absorbed in a Micro-Cluster is measured using Variance. The spread quantifies how varied the set of a feature's values are. However, the performance of *Variance* can be affected negatively by outliers as they may significantly change μ . Whereas, IQR is considered a more robust method with respect to outliers [44, 45] compared with Variance. The first version of the here presented feature tracker also adopted *Variance* as a measure of the spread of a feature. However, as expected it was observed that this approach did not work very well due to its sensitivity to outliers. Thus IQR was explored as an alternative to Variance in order to obtain a more reliable measure of the Micro-Cluster spread. The evaluation results presented in Section 7.2 compare the performance of the proposed feature tracker as obtained using either Variance or IQR.

This section describes the new extension of the MC-NN Micro-Cluster structure with IQR to split a Micro-Cluster. IQR measures the spread of an ordered set of data (i.e., ascending order) by dividing it into quartiles such as Lower Quartile (Q1), median, and Upper Quartile (Q3). Q1 and Q3 are the middle numbers of the first and second half of an ordered list of feature values, respectively; median is the middle number of an ordered list of data values. IQRis the difference between Q3 and Q1. This is applied for the purpose of splitting a Micro-Cluster which is explained in the next section.

5.3.3. Splitting of a Micro-Cluster using IQR

One purpose of using IQR in this research is to Split a Micro-Cluster once its error count ϵ reaches Θ . The use of ϵ and Θ was described in Section 3. This research prefers IQR over Variance as it is more robust to outliers. The assumption here is that the larger the IQR of a feature, the greater the range of values that have been seen for that feature and thus it may contribute to miss-absorption of new data instances. The new Mirco-Clusters resulting from the *Split* are generated with Q1 and Q3 quartiles. The centroids of the new Micro-Clusters are replaced with either Q1 or Q3 in all dimensions (features). In particular one Micro-Cluster only uses Q1 values and the other only uses Q3 values. This is shown for one dimension only in Figure 12. The original Micro-Cluster is deleted after the Split is performed.

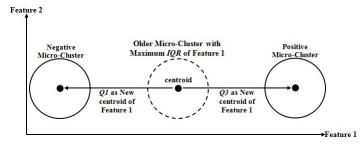


Figure 12: Splitting of a Micro-Cluster with IQR.

Results presented in Section 7.2 compare a version of our approach only using Variance and one using the proposed IQR. The next section provides a worked example on Micro-Cluster splitting for both using Variance and IQR.

5.3.4. Comparison of Splitting using IQR or Variance

This section compares splitting of a Micro-Cluster containing an outlier using IQR and Variance to demonstrate that IQR is a more robust metric to Split Micro-Clusters if there are outliers. For simplicity of this illustration the Split along only one feature is observed.

and consider the value 3000 to be an outlier. Then centroid[x] $= \mu = (1 + 1 + 1.2 + 2.5 + 2.8 + 3 + 4.6 + 5 + 3000)/9 =$ 335.6778.

• Splitting of x with IQR: Median = 2.8, Q1[x] = (1 + 1.2)/2 = 1.1,Q3[x] = (4.6 + 5)/2 = 4.8,IQR[x] = Q3 - Q1 = 3.7,centroid[x] of a Negative Micro-Cluster = Q1[x] = 1.1, centroid[x] of a Positive Micro-Cluster = Q3[x] = 4.8

• Splitting of x with Variance:

$$\left(\frac{CF2^{x}}{n}\right) = ((1*1) + (1*1) + (1.2*1.2) + (2.5*2.5) + (2.8*2.8) + (3*3) + (4.6*4.6) + (5*5) + (3000*3000))/9$$

$$= 1000008.077,$$

$$\left(\frac{CF1^{x}}{n}\right)^{2} = ((1+1+1.2+2.5+2.8+3+4.6+5+3000)/9)^{2} = 112679.5705,$$

$$Variance[x] = \sqrt{\left(\frac{CF2^{x}}{n}\right) - \left(\frac{CF1^{x}}{n}\right)^{2}} = 941.9815,$$

$$centroid[x] \text{ of a Negative Micro-Cluster} = \text{old } centroid[x]$$

$$- Variance[x] = 335.6778 - 941.9815 = -606.3037,$$

$$centroid[x] \text{ of a Positive Micro-Cluster} = \text{old } centroid[x]$$

$$+ Variance[x] = 335.6778 + 941.9815 = 1277.6593.$$

In the example above it can be seen that the original Micro-Cluster centroid is strongly influenced by the outlier. However, it can also be seen that the new centroids after splitting using IQR are within the value range of the feature's values (excluding the outlier), whereas the new centroids after splitting using Variance, as it is performed in original MC-NN, are shifted towards the outlier outside the original Micro-Cluster's value range. Thus, in this research IQR is used to perform Micro-Cluster splits to mediate the influence of outliers.

To use the IQR, the feature data values need to be sorted in an ascending order. To achieve this in a computationally efficient manner, First-In-First-Out (FIFO) principle combined with *SkipList* is used.

5.3.5. First-In-First-Out (FIFO) with SkipList

Firstly, in order to save the feature data values a First-In-First-Out (FIFO) queue is applied where the oldest entry of the queue is handled first. FIFO's size can be set by a user threshold which is less or equal to the size of the statistical windows (time windows). FIFO keeps the most recent data (i.e., feature's data) and needs to be set to a lowest possible size (i.e., less or equal to a window's size) which yields good results. In an initial unpublished feasibility study it was found that a queue size of 1000 works well in most cases in terms of computational efficiency and accuracy. Thus a queue of size 1000 has been used in all experiments presented in this paper. It was also observed in most cases that even if the statistical window size is much larger than 1000, that it is unlikely that more than 1000 Consider a feature's values [x] = 1, 1, 1.2, 2.5, 2.8, 3, 4.6, 5, 3000, instances are absorbed by a single Micro-Cluster. Thus the potential loss of information due to a queue size limit is also unlikely.

> Second, for sorting the FIFO queue of a feature x, a SkipList is used, which is a data structure that allows fast search and insert $O(\log n)$ rather than O(n) operations by updating a linked hierarchy of sub-sequences within an ordered sequence of elements [46, 47]. SkipList is superior to alternative sorting algorithms in terms of computational efficiency as indicated in [48]. Each node in a *SkipList* consists of four directions (up, down, left, and right), as shown in Figure 13. Skipping over fewer nodes than the previous one with each consecutive sub-sequence is the main structure of a *SkipList*. Once splitting of a Micro-Cluster with

larger or maximum IQR is applied, the FIFO queue of each feature x of a Micro-Cluster is then sent to a SkipList.

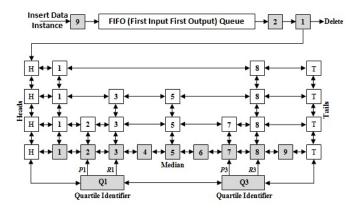


Figure 13: Real-Time sorting of the feature data values using a *SkipList*.

In order to locate and update the position of Q1 and Q3, Quartile Identifiers have been created, which are a data structure connected with head and tail of a *SkipList* as illustrated in Figure 13. A Quartile Identifier consists of two nodes P and R, P is a pointer to either the value or the value next to the left of the quartile Q1 or Q3, and R is a pointer to the next value right of P. The index of Pand R is either 1 or 3, which denotes if the pointers refer to Q1 or Q3 respectively. The Quartile Identifier skips either to the left or right position after each insertion of a new *SkipList* node, as shown in Algorithms 2, 3, and 4. Quartile Identifier of Q1 is located in the middle of the left half of *median* of the *SkipList* and connected with the head of the *SkipList* indicated with letter H in Figure 13. While the *Quartile Identifier* of Q3 is located in the middle of the right half and connected with tail of the SkipList indicated with letter T in Figure 13.

Given P and R of a *Quartile Identifier* and if the number of feature values left/right of the median is either even or odd, then quartiles Q1 and Q3 can be calculated using the following equations, where y refers to either Q1 and Q3. If the number of feature values left/right of the median is even then Equation 11 is used and if it is odd then Equation 12 is used.

$$Q_y[x] = (P_y + R_y)/2$$
(11)

$$Q_y[x] = P_y \tag{12}$$

When adjusting the *Quartile Identifiers* in real-time there are three cases to consider depending on whether the number of values of the feature is odd or even and also if the number of values to the left and right of the median is odd or even. For each of the three cases three further scenarios exist depending where the value is inserted in the SkipList. These cases and scenarios are described below including examples.

Case 1: After inserting the new value, the total number of feature values in the SkipList is even and the number of values left or right of the median is odd. In this particular case Algorithm 2 is applied.

Inpu	it : new feature value f , nodes of a $SkipList$ afte
-	ng a new feature value f , previous Quartile Identifier
P1 a	nd <i>P</i> 3.
Out	put: updated Quartile Identifiers P1 and P3
1: ii	f $f \leq value of P1$ then
2:	P1 and $P3$ remain at the same position
3: e	else
4:	if $f > value of P1 and f \leq value of P3$ then
5:	Skip $P1$ to the next value right of $P1$
6:	else
7:	if $f > value of P3$ then
8:	Skip $P1$ to the next value right of $P1$
9:	Skip $P3$ to the next value right of $P3$
10:	end if
11:	end if
12: e	end if
	(before) Median
H +	$ 0.2 \leftrightarrow 0.92 \leftrightarrow 2.1 \leftrightarrow 3.5 \leftrightarrow 4.4 \leftrightarrow 5.5 \leftrightarrow 8.7 \leftrightarrow 9.3 \leftrightarrow 10.9 \leftrightarrow T $
Т	P1 R1 P3 R3

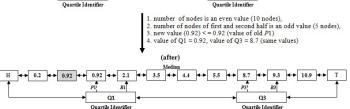


Figure 14: An example of $Quartile \ Identifiers$ update for Case 1 with value inserted left of Q1.

In Figure 14, the number of nodes of the SkipList for the feature is an even value (10 nodes) after adding the new feature value 0.92, and the number of nodes of the first and second half of a SkipList is an odd value (5 nodes). The new value $f \leq value \ of \ P1$, thus lines 1 and 2 in Algorithm 2 are executed and Q1 and Q3 are computed, in this scenario P1 and P3 remain unchanged. The Quartiles are computed using Equation 12.

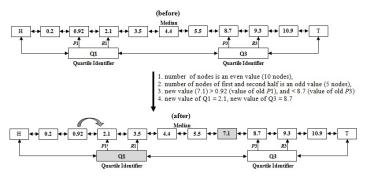


Figure 15: An example of *Quartile Identifiers* update for Case 1 with value inserted between of Q1 and Q3.

In Figure 15, the number of nodes of the *SkipList* for the feature is an even value (10 nodes) after adding the new feature value 7.1, and the number of nodes of the first and second half of a *SkipList* is an odd value (5 nodes). The new value $f > value of P1 and f \leq value of P3$, thus lines 4 and 5 in Algorithm 2 are executed and Q1 and Q3 are computed. In this case P1 is skipped to the next value right of P1 and P3 remains unchanged. The Quartiles are computed using Equation 12.

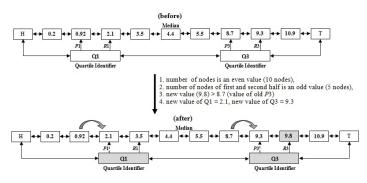


Figure 16: An example of *Quartile Identifiers* update for Case 1 with value inserted right of Q3.

In Figure 16, the number of nodes of the *SkipList* for the feature is an even value (10 nodes) after adding the new feature value 9.8, and the number of nodes of the first and second half of a *SkipList* is an odd value (5 nodes). The new value $f > value \ of \ P3$, thus lines 7 to 10 in Algorithm 2 are executed and Q1 and Q3 are computed. In this case P1 and P3 are skipped to the next value right of P1 and P3 respectively. The Quartiles are computed using Equation 12.

Case 2: After inserting the new value, the total number of feature values in the SkipList is an odd value. In this particular case Algorithm 3 is applied.

Algorithm 3 Adjusting *Quartile Identifiers* for lower and upper quartiles (Q1 and Q3) in terms of Case 2

Input: new feature value f, nodes of a *SkipList* after adding a new feature's value f, previous *Quartile Identifiers* P1 and P3.

Output: updated Quartile Identifiers P1 and P3

- 1: if $f \leq value \ of \ P1$ then
- 2: Skip P1 to the next value left of P1
- 3: else
- 4: **if** $f > value of P1 and f \leq value of P3$ **then**
- 5: P1 and P3 remain at the same position
- 6: else

7:

- if f > value of P3 then
- 8: Skip P3 to the next value right of P3
- 9: end if
- 10: end if
- 11: end if

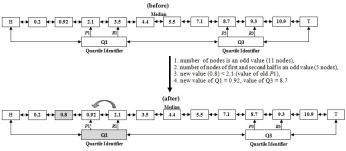


Figure 17: An example of $Quartile \ Identifiers$ update for Case 2 with value inserted left of Q1.

In Figure 17, the number of nodes of the *SkipList* for the feature is an odd value (11 nodes) after adding the new feature value 0.8. The new value $f \leq value \ of \ P1$, thus lines 1 and 2 in Algorithm 3 are executed and Q1 and Q3 are computed. In this case P1 is skipped to the next value left of P1 and P3 remains unchanged. The Quartiles are computed using Equation 12.

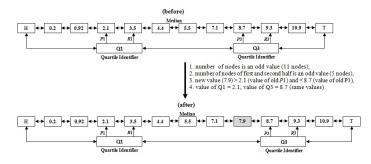


Figure 18: An example of the update for the *Quartile Identifiers* for Case 2 with a value inserted between Q1 and Q3.

In Figure 18, the number of nodes of the *SkipList* for the feature is an odd value (11 nodes) after adding the new feature value of 7.9. The new value $f > value of P1 and f \leq$

value of P3, thus lines 4 and 5 in Algorithm 3 are executed and Q1 and Q3 are computed. In this case P1 and P3 remains unchanged. The Quartiles are computed using Equation 12.

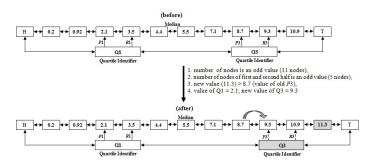


Figure 19: An example of $Quartile \ Identifiers$ update for Case 2 with value inserted right of Q3.

In Figure 19, the number of nodes of the *SkipList* for the feature is an odd value (11 nodes) after adding the new feature value 11.3. The new value $f > value \ of \ P3$, thus lines 7 to 9 in Algorithm 3 are executed and Q1 and Q3 are computed. In this case P3 is skipped to the next value right of P3 and P1 remains unchanged. The Quartiles are computed using Equation 12.

Case 3: After inserting the new value, the total number of feature values in the SkipList is even and the number of values left or right of the median is even. In this particular case Algorithm 4 is applied.

Algorithm 4 Adjusting *Quartile identifiers* for lower and upper quartiles (Q1 and Q3) in terms of **Case 3**

Input: new feature value f, nodes of a *SkipList* after adding a new feature value f, previous *Quartile Identifiers* P1 and P3.

Output: updated Quartile Identifiers P1 and P3

1: if $f \leq value \ of \ P1$ then Skip P1 to the next value left of P12: Skip P3 to the next value left of P33: 4: else if f > value of P1 and f < value of P3 then 5: Skip P3 to the next value left of P36: 7: else if f > value of P3 then 8: P1 and P3 remain at the same position 9: end if 10: end if 11: 12: end if

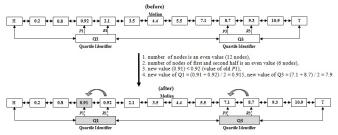


Figure 20: An example of $Quartile \ Identifiers$ update for Case 3 with value inserted left of Q1.

In Figure 20, the number of nodes of the *SkipList* for the feature is an even value (12 nodes) after adding the new feature value of 0.91. The new value $f \leq value \ of \ P1$, thus lines 1 to 3 in Algorithm 4 are executed and Q1 and Q3 are computed. In this case P1 and P3 are skipped to the next value left of P1 and P3 respectively. The Quartiles are computed using Equation 11.

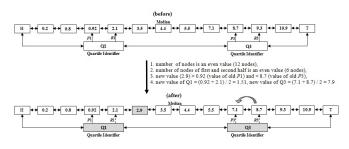


Figure 21: An example of $Quartile \ Identifiers$ update for Case 3 with value inserted between Q1 and Q3.

In Figure 21, the number of nodes of the *SkipList* for the feature is an even value (12 nodes) after adding the new feature value of 2.9. The new value $f > value of P1 and f \leq$ value of P3, thus lines 5 and 6 in Algorithm 4 are executed and Q1 and Q3 are computed. In this case P3 is skipped going to the next value left of P3 and P1 remains unchanged. The Quartiles are computed using Equation 11.

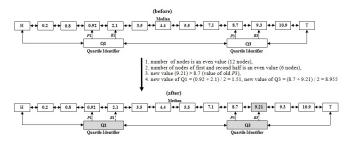


Figure 22: An example of *Quartile Identifiers* update for Case 3 with value inserted right of Q3.

In Figure 22, the number of nodes of the SkipList for the feature is an even value (12 nodes) after adding the new feature value of 9.21. The new value f > value of P3, thus lines 8 to 10 in Algorithm 4 are executed and Q1 and Q3 are computed. In this case P1 and P3 remain unchanged. The Quartiles are computed using Equation 11.

5.3.6. Tracking and Removal of Micro-Clusters with False Positive Participation

This section presents the proposed method for the removal of a Micro-Cluster. This method consists of two main tasks which are counting the number of false positive participations in the Micro-Cluster and measuring the 'difference' between the time stamps of the Micro-Cluster (i.e., difference between the current time stamp and the average of actual time stamps of the Micro-Cluster). Regarding false positive participation, a Micro-Cluster's false positive participation towards the absorption or training task is tracked by counting the number of times that this Micro-Cluster absorbs new instances which belong to a different class label than the actual class label of the Micro-Cluster. The initial value of this counter is 0. The counter is incremented by 1 if the particular Micro-Cluster absorbed a new instance incorrectly. Otherwise, it is decremented by 1 if the particular Micro-Cluster absorbed the new instances correctly (i.e., absorbs a new instance with the same class label as the Micro-Cluster). This subtraction is applied only if the counter value is greater than 0. Regarding measuring difference of time stamp of Micro-Clusters. This is given by the Equation 13.

Difference of Time Stamp =
$$T_{current} - \frac{\sum_{i=1}^{n} (MC's \ Actual \ Time \ Stamp)}{n}$$
 (13)

Where n is a number of data instances absorbed by the Micro-Cluster and $\sum_{i=1}^{n} (MC's \ Actual \ Time \ Stamp)$ is the sum of time stamps of all absorbed data instances of this Micro-Cluster (also known as $CF1^t$) and $T_{current}$ is the current time stamp. The smaller this Difference is, the more recently the Micro-Cluster has participated in absorbing data instances, as time stamps increase over time. After each time stamp, the difference between time stamps of each Micro-Cluster is calculated and the one with the largest difference is identified (the Micro-Cluster that has participated the least recently). If this Micro-Cluster also has a record of incorrect absorptions (absorption counter greater than 0), then the Micro-Cluster is removed. This is because the Micro-Cluster is considered out-dated and thus has potentially also incorrectly absorbed information.

This is a different method for estimating participation in this research compared with the Triangle Number method used in original MC-NN as described in Section 3. The reason for employing a different solution here is that the original MC-NN Triangle Method does not take false positive participation into account. Thus MC-NN may falsely regard a Micro-Cluster that has recently absorbed many false positive instances as relevant. In addition, the here proposed method only requires two steps to calculate the participation of a Micro-Cluster:

- 1. Calculate difference of time stamps.
- 2. Increment/decrement false positive counter.

The required steps for Triangle Number are outlined in Figure 3 in Section 3.4). Thus there are many more steps involved using the original method for calculating Micro-Cluster participation, and this results in unnecessary computational overheads.

6. Real-Time Feature Selection Technique using Adaptive Micro-Clusters

Three main tasks will be explained in this section which are feature analysis, feature selection, and monitoring the relevance of selected features. After detection of a concept drift, the statistical information of the features (i.e., *Velocity* and IQR) is analysed to identify which features were involved in the drift. Loosely speaking only features that had a significant change of their statistical information are re-examined for feature selection using Information Gain in each statistical window. This is based on the assumption that features that have not changed much are also likely to have maintained a similar Information Gain value. This can be used to reduce the computational cost of feature selection by assuming that the Information Gain has not changed for these features and thus re-calculating the Information Gain is not needed. Loosely speaking the method follows the following steps:

- 1. Detect Concept Drift
- 2. Use the Micro-Clusters statistical information (Ve-locity and IQR) to identify features involvement in the drift.
- 3. Re-calculate Information Gain only for features that have been involved in the drift.
- 4. Re-rank features according to their Information Gain.
- 5. Use new Information Gain ranking to select features.

6.1. Feature Analysis and Feature Selection

Feature analysis is facilitated using historical data (i.e. a statistical window between *time-1* and point-of-drift *time*). For the purpose of feature analysis, a counter is kept for each feature of a Micro-Cluster. The counter is incremented by 1 if the particular feature was the feature with the highest IQR. In this paper this is referred to as the history of maximum IQR. Using a windowing approach over the data stream, a running average of *Velocity* rate is calculated. A high Velocity rate combined with maximum IQR during a concept drift indicates that the feature has changed. The assumption here is that this particular feature may have changed its contribution towards the classification technique. Thus feature selection can be limited to only examining features that have changed their *Velocity* rate and IQR when there is a concept drift detected. Features that have changed are temporarily regarded as irrelevant for the data mining task, as large statistical changes have a similar effect as noise. However, the contributions of these features towards the absorption in Micro-Clusters may stabilise after the drift and thus these features are

re-examined in the following time window. This will be explained in more details in the next section. From then onwards only instances comprising the relevant features are passed on to the classifier. This Feature Analysis and Feature Selection method is described in Algorithm 5.

Algorithm 5 Feature Analysis and Feature Selection

Input: Micro-Clusters statistical information (*Velocity* rate [features] and history of maximum *IQR* [features]) of a statistical window between *time-1* and point-of-drift *time*, and instance.

Output: Instance with relevant features

- 1: for each drift detection do
- 2: List *Velocity* rate[features] in order from low to high
- 3: Identify *median* value of the ordered list *Velocity* rate[features]
- 4: for each feature with *Velocity* rate \geq *median* value do
- 5: if feature has history of maximum IQR > 0 value then
- $6: \qquad instance \leftarrow delete \ irrelevant \ feature$
- 7: end if
- 8: end for
- 9: end for
- 10: $Classifier \leftarrow instance with relevant feature(s)$

6.2. Monitoring and Analysis of Temporarily Irrelevant Features

The features (the ones that are temporarily regarded as irrelevant) are monitored in the following statistical window to examine their relevance using Information Gain. The assumption here is that the contribution of this particular feature towards the classification result may have changed significantly. Thus checking relevance can be limited to examining only the features that have been temporarily regarded as irrelevant. If a feature x's Information Gain is greater than μ of Information Gain between window at time-1 and at current time with Percentage Difference greater than 50% it is selected as relevant to a classifier. It should be noted here that Information Gain has been chosen as feature selection metric, as it is a popular metric for this purpose. Thus all experiments in the next section have been obtained using this metric. However, the user may decide to implement a different metric for feature selection if appropriate for the particular application. Likewise the Percentage Difference can be adjusted by the user requirements. However, in the experiments presented in the next section a *Percentage Difference* of 50% was used as it worked well in most cases. Figure 23 presents the aforementioned procedure in a flow chart for more clarity and Figure 24 shows an example of the statistical information (i.e., Velocity rate and IQR as well as Information Gain) of two features for six time windows.

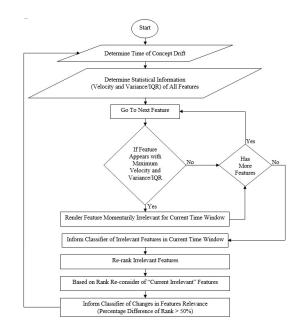


Figure 23: Process of feature selection in real-time .

Point-of-Drift DriftDetected	Velocity Rate 0.0002768524 0.0000265177	History of Maximum IQR 6	Information Gain 0.327553	Velocity Rate	History of Maximum IQR	Information Gain	Description		
Drift Detected	0.0000265177	6	0.327553	0.0000706070		Gain			
Drift Detected		- 1		0.0000706373	2	0.310189	Both features are relevant		
Drift Detected		1	Not calculated	0.0000629003	1	Not calculated	Both features are relevant		
	/0.0123808211	,23	0.021256	0.0000716994	1	Not calculated	+		
,	0.0037991722	, 6	0.020442	0.0000867975	3	Not calculated	Feature 1 is irrelevant		
/	0.0000674918	/ 4	0.268502	0.0000939307	1	Not calculated	+		
,	0.0001149352	1 5 1	Not calculated	0.0000991489	1	Not calculated	Feature 1 is relevant		
Feature 1 is temporarily regarded as irrelevant as it appears with maximum Velocity rate and history of maximum IQR									
/ 2 = 0.144472	2), and								
	as it appea ate and history is selected as /2 = 0.144472	0.0000674918 0.0001149352 1 is temporarily regarded as it appears with maxin ate and history of maximum I is selected as relevant as it /2 = 0.144472), and	1 is temporarily regarded as as it appears with maximum ate and history of maximum IQR is selected as relevant as it appears with 1 /2 = 0.44472), and	1 is temporarily regarded as as it appears with maximum at and history of maximum IQR is selected as relevant as it appears with Information 0 /2 = 0.144472), and	$\frac{1}{1} \begin{array}{c c c c c c c c c c c c c c c c c c c $	0.0000674918 4 10.268502 0.000039307 1 1 is temporarily regarded as as it appears with maximum ate and history of maximum IQR ////////////////////////////////////	0.0000674918 4 0.268502 0.0000939307 1 Not calculated 1 is temporarily regarded as as it appears with Information Gain (W ₃ = 0.268502) greater than mean ((W ₄ 0.0000991498 1 Not calculated		

Figure 24: An example of feature analysis, feature selection, and monitoring of temporarily irrelevant features. Assumed Information Gains are indicated in italics and actual Information Gain calculations are not in italics.

Initially Information Gain is calculated for all features at window W_1 . In this example it is assumed that both features are initially relevant. Drift is detected at window W_3 , consider the *Velocity* rate and history of maximum IQR of feature 1 equal to 0.0123808211 and 23, concurrently. This represents that feature 1 appears with maximum Velocity rate and a history of maximum IQR compared with the remaining features (in this case only feature 2). Thus feature 1 is temporarily regarded as irrelevant to the classifier after W_3 . Information Gains of irrelevant features are then calculated in every time window in order to monitor if they return to being relevant. In this case feature 1 appears again with an Information Gain at $W_5 = 0.268502$, which differs from μ by 50%. This indicates that feature 1 became relevant again for classification tasks after W_5 . Please note that the Information Gain of features that have remained relevant are assumed not to have changed and thus are only re-calculated if there is a drift detected. In this example assumed Information Gains are indicated in italics. For example for feature 2 there is only one Information Gain calculation at the beginning in W_1 . However, should there be another concept drift in the future and feature 2 appears with maximum *Velocity* rate and history of maximum *IQR*, then its Information Gain is likely to have changed and thus it would be re-calculated.

7. Experimental Evaluation

This section first provides information about the experimental setup and then presents an extensive empirical evaluation of the proposed techniques.

7.1. Experimental Setup

The implementation of experiments were realised in the Massive Online Analysis (MOA) framework [49]. Two types of data were used, artificial data stream generators from the MOA framework and real datasets. The reason for also using artificial datasets is because MOAs data stream generators enable the introduction of different kinds of concept drift deliberately and thus allow us to evaluate against a ground truth in terms of concept drift. The source code implemented for this paper has been made available here¹.

7.1.1. Artificial Datasets

The following artificial data stream generators were used: SEA Generator, this data stream was introduced in [50], it generates data comprising continuous attributes, whereas the third attribute is irrelevant for distinguishing between the class labels. The HyperPlane Generator was also used, it creates a linearly separable model. It slowly rotates in 'D' dimensions continuously changing the linear decision boundary of the stream [51]. This constant concept change makes it very difficult for data stream classifiers to keep a good classification accuracy and remain computationally efficient. The final data stream generator used was the **Random Tree Generator**, which was introduced in [13] and generates a stream based on a randomly generated tree. New examples are generated by assigning uniformly distributed random values to features, which then determine the class label using the random tree. Nine datasets were generated using the aforementioned stream generators, each comprising three features, two class labels and a concept drift. The concept drift was always induced gradually half way through the stream by both, inducing a concept drift through the MOA data stream generators implemented methods and by swapping features (sudden concept drift). Details about the concept drift methods of the individual streams can be found in various sources, notably [50, 51, 13]. The reason for inducing concept drift by swapping features is that this enables the testing as to which of the features has changed its contribution to the underlying model. One would expect the

methods proposed here to identify the two swapped features as the cause of the concept drift. For each of these three datasets having concept drift, a second and third version of the datasets has been generated which included different levels of noise in order to validate the robustness of the concept drift detection and feature tracking methods. The participation threshold Ω was set to 50 for each experiment, which yielded good results in most cases [39]. The error threshold Θ was set to the best performing one for each dataset. Table 2 shows an overview of the generated streams including the setting of the proposed technique and which features have been swapped. In the experiments a window size equals to 10% of the total number of instances. The expression **Time t** refers to a particular time window. I.e. according to Table 2 time T=1 refers to instances 1-1000, T=2 to instances 1001-2000, etc. Regarding the FIFO, it was set to 1000 instances, as this setting yielded good results in terms of classification accuracy in most cases. The classification accuracy was calculated using the Prequential Testing method implemented in MOA [52], which essentially calculates a running average of the classification accuracy.

Table 2: Setup of the artificial datasets. Drifts were generated through individual data stream generators and by swapping features.

Dataset	Number of Instances Generated	Start of Concept Drift by Generator	Window Size	Θ	Index of Swapped Features	Start of Swapped Features	Percentage of Noise
SEA	10,000	5000	1000	3	2 with 3	6000	-
SEA	10,000	5000	1000	34	2 with 3	6000	15
SEA	10,000	5000	1000	75	2 with 3	6000	25
HyperPlane	10,000	5000	1000	6	1 with 2	6000	-
HyperPlane	10,000	5000	1000	13	1 with 2	6000	15
HyperPlane	10,000	5000	1000	27	1 with 2	6000	25
RandomTree	10,000	5000	1000	644	1 with 2	6000	-
RandomTree	10,000	5000	1000	726	1 with 2	6000	15
Random Tree	10,000	5000	1000	685	1 with 2	6000	25

7.1.2. Real Datasets

Two sets of experiments were setup. One controlled set of experiments to validate whether the method can detect concept drifts and causality of concept drift on real datasets correctly. For this features were swapped to generate a known ground truth. Four real datasets with continuous features were chosen randomly from the UCI Machine Learning Repository [53]. Table 3 shows an overview of real datasets including setting of the proposed technique and which features were swapped. The second set of experiments was uncontrolled, real data sets where used and no features were swapped, in order to show that the method presented in this paper is robust to more realistic application scenarios. The proposed concept drift detection method, feature tracking method and also feature selection method were applied. The robustness of the method was measured by applying a Hoeffding tree classifier and classification accuracy was monitored over time. Also a control group of experiments was setup, where only a Hoeffding tree classifier was applied thus excluding any

of the techniques developed in this paper. The Hoeffding tree classifier has been chosen as it is one of the most popular data stream classifiers and best performing classifier in the MOA framework [54]. However, our method is independent of the classifier and the user may choose a different classification method. Six real datasets with continuous features were chosen randomly from the UCI Machine Learning Repository [53]. Table 4 shows an overview of real datasets including settings of the proposed technique. For both sets of experiments Ω (threshold for the Micro-Cluster minimum participation) was set to 50 as this yielded good results in most cases. Whereas Θ was set to a relevant value that retrieves good results for each individual dataset. The time window size and FIFO size were chosen the same way as for the artificial data streams (see Section 7.1.1).

Table 3: Setup of the real datasets for the controlled set of experiments for concept drift detection and feature tracking.

Dataset	Number of	Number of	Number of	Θ	Index of	Time of
Dataset	Instances	Features	Class Labels	0	Swapped Features	Swapping
Bank	41,188	10	2	1500	1 with 10	6
CoverType	581,012	10	7	12,000	6 and 7 with 8 and 9	3
Diabetes	768	8	2	37	1 with 2	4
KDDCUP	494,021	10	23	1000	2,3, and 4 with 8,9, and 10	4

Table 4: Setup of real datasets for the uncontrolled set of experiments for concept drift detection, feature tracking and feature selection.

Beal Dataset	Number of	Number of	Number of	FIFO Size	Θ
Iteai Dataset	Instances	Features	Class Labels	(Maximum)	0
CoverType	581,012	54	7	1000	10,000
EEG Eye State	14,980	14	2	1000	200
Gesture Phase Segmentation	1,747	19	5	1000	56
Poker Hand	1,000,000	10	10	1000	51,000
Statlog (Landsat Satellite)	4,435	36	7	1000	28
Waveform (with noise)	5,000	40	3	1000	50

7.2. Results

The results presented as first in Section 7.2.1 analysed the effect of noise, feature-bias and outliers on the detection of concept drift. This evaluation is based on original MC-NN using the readily available *Variance* statistics of the Micro-Clusters and *Split* and *Death* rate to detect concept drift. Then in Section 7.2.2, the technique proposed for concept drift detection in Section 4 is compared with the results in Section 7.2.1 to evaluate the proposed feature tracking method. Finally Section 7.2.3 applies the method in combination with a data stream classifier for real-time feature selection and measures the change in accuracy.

7.2.1. Real-Time Concept Drift Detection Technique

The Micro-Clusters *Split* and *Death* rates were used for detecting drifts. For the experiments the default parameters stated in Table 2 of the technique were used. The evaluation incorporated several levels of noise in the artificial data stream, as listed in Table 2 and the real datasets are described in Table 3.

In Figures 25, 26, and 27 the *Percentage Difference* is displayed up to 100%, however, this can be much higher

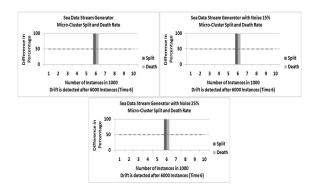


Figure 25: Results of Sea Data Stream Generator for drift detection using Micro-Cluster Percentage Difference of Split and Death rate.

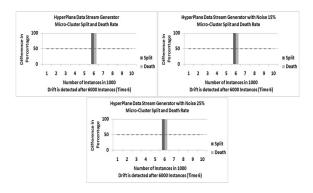


Figure 26: Results of HyperPlane Data Stream Generator for drift detection using Micro-Cluster Percentage Difference of Split and Death rate.

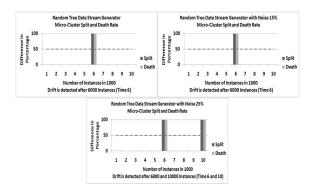


Figure 27: Results of Random Tree Data Stream Generator for drift detection using Micro-Cluster Percentage Difference of Split and Death rate.

than 100%. For readability of the figures a maximum of 100% difference is displayed. Displaying differences above 100% is not interesting as the concept drift detection was triggered once a difference of at least 50% had been reached for both *Split* and *Death* rates. This 100% cut-off is applied on all subsequent figures in this paper referring to *Percentage Differences* of *Split* and *Death* rates. During this time higher *Split* and *Death* rates are expected as the set of Micro-Clusters adapts to the new concept, the feature swap. In the figures, it can be seen that the *Split* and *Death* rates at the time of concept drift (after time 5) increase as expected for all artificial data streams and noise

levels. The noise levels do not seem to affect the concept drift detection considerably; however, for the RandomTree generator with a noise level of 25%, at time window 10, the algorithm did arrive at a false positive detection i.e. detected a concept drift that was not there. This could be an indication that the Micro-Clusters for RandomTree became unstable due to noise. This is discussed further in the next section where mechanisms to deal with noise are incorporated in the feature tracking method.

Next the concept drift detection method was compared with existing state-of-the-art drift detection methods CUSUM, EWMA has a very high *false positive* number of 72, com-DDM, EDDM, EWMA, and ADWIN (see section 2 for more details about these methods) on the same artificial data streams. Table 5 shows the time when each of the methods including the proposed method, detected a drift and if it was detected on time. As it can be seen, the proposed technique always detected the drift at the correct time except for the RandomTree data stream with 25%noise as has been discussed previously.

Table 5: Adaptation to concept drift using the initially proposed and other state-of-the-art techniques.

Generator	Technique	Number of Drift Detections	Times when Drift Detected	Drift Detected
	The Proposed Technique	1	6	Correctly
	CUSUM	1	5	Incorrectly
Sea	DDM	2	5 and 8	Incorrectly
Sea	EDDM	2	5 and 8	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	1	5	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	2	5 and 8	Incorrectly
Sea with Noise 15	DDM	1	5	Incorrectly
Sea with Noise 15	EDDM	2	1 and 4	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	2	5 and 9	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	2	5 and 6	Correctly
	DDM	1	4	Incorrectly
Sea with Noise 25	EDDM	3	1.4. and 6	Correctly
	EWMA	9	1 to 9	Correctly
	ADWIN	3	4,5, and 8	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	1	5	Incorrectly
	DDM	1	5	Incorrectly
HyperPlane	EDDM	1	5	Incorrectly
	EWMA	8	1 to 5 and 7 to 9	Incorrectly
	ADWIN	3	2.5, and 9	Incorrectly
		3	7-7	Correctly
	The Proposed Technique CUSUM	1	6	Incorrectly
TT D1	DDM	2	5 and 7	Incorrectly
HyperPlane		-		
with Noise 15	EDDM	1	5	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	2	2 and 5	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	2	5 and 6	Correctly
HyperPlane	DDM	2	5 and 6	Correctly
with Noise 25	EDDM	2	4 and 7	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	3	2,5, and 8	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	1	5	Incorrectly
RandomTree	DDM	1	5	Incorrectly
nandomme	EDDM	1	5	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	2	5 and 9	Incorrectly
	The Proposed Technique	1	6	Correctly
	CUSUM	1	5	Incorrectly
RandomTree	DDM	1	5	Incorrectly
with Noise 15	EDDM	1	5	Incorrectly
	EWMA	9	1 to 9	Correctly
	ADWIN	2	5 and 9	Incorrectly
	The Proposed Technique	2	6 and 10	Correctly
	CUSUM	1	7	Incorrectly
BandomTree	DDM	-	-	-
with Noise 25	EDDM	-	-	-
W1011 11010C 20	EWMA	9	1 to 9	Correctly
	ADWIN	-	-	correctly
	ADWIN	-	-	-

If a method detects a drift falsely, then this would cause unnecessary adaptation by the classifier to a non-existing

drift. This is referred to as a *false positive*. Correctly detected drifts are referred to as true positives. The number of experiments (each with one actual drift) are shown in Table 6. As there are 9 experiments, there is a total of 9 concept drifts to be detected. In the table it is indicated how many true and false positives each method detected. As can be seen, the proposed technique detected all concept drifts and only had one *false positive* detection. The best competitor in this regard, EWMA, detected 8 true positives, 1 less than the proposed method. However, pared with only 1 for the proposed method. Thus EWMA is triggering frequent and unnecessary adaptation to concept drift. Also the remaining competitors found fewer true positives and a much higher number of false positives compared with the proposed method.

Table 6: Summary of concept drift adaptation experiments referring to Table 5.

Technique	True Positives	False Positives
The Proposed Technique	9	1
CUSUM	2	10
DDM	1	10
EDDM	1	12
EWMA	8	72
ADWIN	0	18
Total:	21	123

The method has also been applied on real datasets as shown in Figure 28 where for each case 1 concept drift has been introduced through the swapping of features as listed in Table 3.

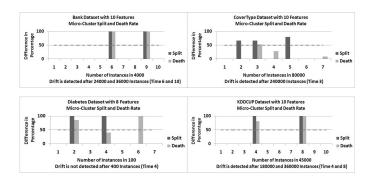


Figure 28: The results of real-dataset for drift detection using Micro-Cluster Percentage Difference of Split and Death rate.

In Figure 28, it can be seen that the *Split* and *Death* Percentage Differences at the time of concept drift increase with Bank dataset, CoverType dataset, and KD-DCUP dataset, indicating that the current set of Micro-Clusters does not fit the concept encoded in the data anymore. Whereas, in the figure, drift is not detected with the *Diabetes* dataset. As these data streams are based on real datasets it is believed that they potentially contain feature-bias, noise and outliers and that these may be the reasons for the proposed method not being able to detect the concept drift. The next section will compare this method with the new proposed feature tracking method, which is more robust to feature-bias, noise and outliers.

7.2.2. Tracking Features using Variance and IQR

The evaluation was based on original MC-NN using the readily available Variance statistics of the Micro-Clusters and Split and Death rates to detect concept drift. This section applies Normalisation and LPF in order to address these effects and compares these results with those from Section 7.2.1. Furthermore this section compares the previously discussed approach for feature tracking based on Variance combined with feature Velocity to the more robust approach based on IQR combined with feature Velocity. For the experiments the default parameters stated in Table 2 (artificial datasets) of the technique were used unless stated otherwise. Regarding the artificial datasets, no Normalisation was applied as the data generators already produced normalised data.

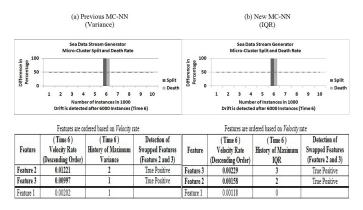


Figure 29: The results of SEA data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

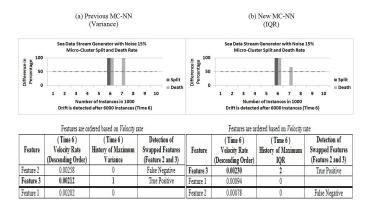


Figure 30: The results of SEA data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

Part (a) of Figures 29, 30, 31, 32, 33, 34, 35, 36, and 37 shows the results for using MC-NN with *Variance* and history of maximum *Variance* for concept drift detection and

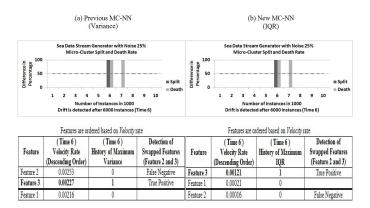


Figure 31: The results of SEA data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

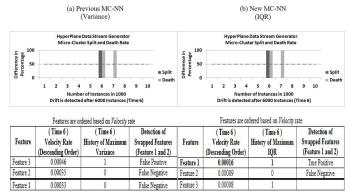


Figure 32: The results of HyperPlane data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

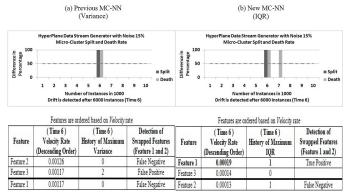


Figure 33: The results of HyperPlane data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

feature tracking, and part (b) of the figures shows the corresponding results for using MC-NN with IQR and history of maximum IQR. Different figures correspond to different data streams and noise levels. Regarding concept drift detection, the same results as the previous section have been achieved for both, using *Variance* and IQR. All concept drifts were detected correctly, however, both methods also detected a false concept drift for time 10 of the RandomTree generator at noise level 25%. However, it is

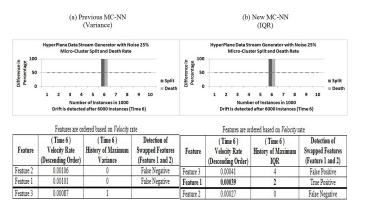


Figure 34: The results of HyperPlane data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

	(a) Previous MC-NN (Variance)				(b) New MC-NN (IQR)				
	Micro-Clus	Random Tree Data Stream Generator Micro-Cluster Split and Death Rate			Random Tree Data Stream Generator Micro-Cluster Split and Death Rate				
Difference in Percentage 0 0 0	■ Split 1 2 3 4 5 6 7 8 9 10 Number of Instances in 1000 Drift is detected after 6000 Instances (Time 6)			Difference in Percentage 0 0	1 2 3 4 Numbr	5 6 7 8 er of Instances in 1000 d after 6000 Instances (1	■ Split 9 10 Fime 6)		
	Features are or	rdered based on Velocity 1	rate		Features are or	rdered based on Velocity 1	ate		
	(Time 6)	(Time 6)	Detection of		(Time 6)	(Time 6)	Detection of		
Feature	Velocity Rate (Descending Order)	History of Maximum Variance	Swapped Features (Feature 1 and 2)	Feature	Velocity Rate	History of Maximum	Swapped Features (Feature 1 and 2)		
Eastern 2		variatice	· · · · · · · · · · · · · · · · · · ·	F (1	(Descending Order)	IQR	· /		
Feature 2	0.00101	U	False Negative	Feature 1	0.00067	17	True Positive		
Feature 3	0.00093	0		Feature 2	0.00066	23	True Positive		
Feature 1	0.00090	1	False Negative	Feature 3	0.00063	13			

Figure 35: The results of Random Tree data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

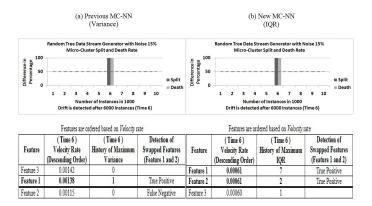


Figure 36: The results of Random Tree data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

likely not to cause a degradation of classification accuracy, as features are merely flagged up to the feature selection method to have potentially changed their relevance but it is then up to the feature selection method to evaluate these features and decide if they should be included. If a concept drift is detected, then the methods use the feature *Velocity* and history of maximum *Variance* or *IRQ* respectively to decide which features should be flagged up to be considered for inclusion or removal from the currently considered

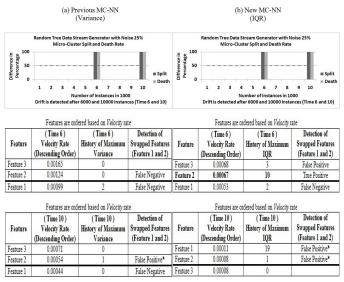


Figure 37: The results of Random Tree data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

features. The results for this are depicted at the bottom part in the aforementioned figures. As a reminder, the features are ranked according to their velocities and the 50% features with the highest *Velocity* are examined closer. As there are 3 features in each stream, the 2 features with the highest *Velocity* are always selected. These features are then flagged up if they also appeared in the history of maximum *Variance* or *IQR* in the previous time window. This has already been explained in greater detail in Section 6.1. It is expected here that features that have been swapped during the concept drift are more likely to be flagged up for inclusion or removal from the currently considered set of features.

Table 7: Summary of the experimental results with artificial datasets generated with noise levels of 0%, 15% and 25%. The results are reported for the Time 6 which is the time of swapped features.

	True	True	False	False
Generator	Positive	Positive	Positive	Positive
	(Variance)	(IQR)	(Variance)	(IQR)
Sea with Noise 0%	2	2		
Sea with Noise 15%	1	1		
Sea with Noise 25%	1	1		
HyperPlane with Noise 0%		1	1	
HyperPlane with Noise 15%		1	1	
HyperPlane with Noise 25%		1		1
Random Tree with Noise 0%		2		2
RandomTree with Noise 15%	1	2		
Random Tree with Noise 25%		1	1*	$2 + 2^*$
Total:	5	12	3	7

Table 7 summarises the feature tracking results presented in Figures 29 to 37. Numbers indicated with a * indicate potentially false positives detections of features that changed their relevance. Potentially in the preceding sentence is to reflect the fact that in this case that there was also an unexpected concept drift. However, it is not possible to verify with absolute certainty if the detection was indeed a false positive. It can be seen that the here presented method based on maximum IQR achieves a much higher *true positive* detection of features that changed. However, it also has a higher number *false positive* detections compared with the method based on Variance. Now the *true positive* figures are based on the fact the features are known to have changed as they have been swapped at the time of concept drift. However, considering the fact that here the native method of each artificial stream generator has also been used for inducing a concept drift then some of the *false positive* detections may very well be *true* positives. Even if they were not true positives, it would merely mean that they are flagged to the feature selection method to be reconsidered for inclusion or exclusion of the feature set to be considered for adaptation. Loosely speaking, correct true positive detection numbers are more important than *false positive* detection numbers.

In order to remove the possibility of changing feature relevance due to artificial concept drift generators, the feature tracking experiments on the artificial datasets were re-conducted. This time no concept drift was introduced apart from the swapping of the features. Thus the only features that have changed their relevance must be the swapped features. The results of these experiments are displayed in Figures 38 to 46. As it can be seen, and as expected, both methods have a lower *false positive* count of flagging features that changed relevance. Again the proposed method based on IQR performs best, it detected all features that were swapped.

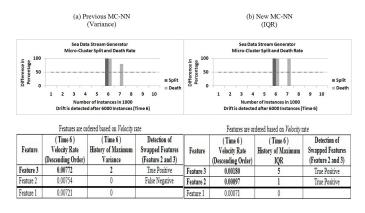


Figure 38: The results of SEA data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

Table 8 summarises the feature tracking results presented in Figures 38 to 46. Altogether there were 18 features swapped so they have all potentially changed their relevance and thus should be identified by the methods. As it can be seen the method based on original MC-NN with Variance identifies 4 features correctly and also resulted in 3 false positives. The proposed method based on IQR detected 16 features that potentially changed their relevance correctly and resulted in 2 false positives. It can be seen that the proposed method based on maximum IQRachieves a much higher true positive detection of features

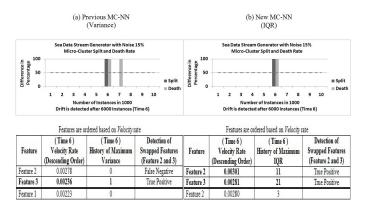


Figure 39: The results of SEA data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

(a) Previous MC-NN (Variance)				(b) New MC-NN (IQR)				
Ifference in Percentage 2001	Sea Data Stream Generator with Noise 25% Micro-Cluster Split and Death Rate				Sea Data Stream Generator with Noise 25% Micro-Cluster Split and Death Rate			
Difference in Percentage 0 0 0	Split 1 2 3 4 5 6 7 8 9 10 Number of Instances in 1000 Drift is detected after 6000 Instances (Time 6)			Difference in Percentage 0 0		5 6 7 8 er of Instances in 1000 d after 6000 Instances (1	= Split = Death 9 10 Time 6)	
	Features are or	dered based on Velocity r	ate		Features are or	dered based on <i>Velocity</i> r	ate	
Feature	(Time 6) Velocity Rate (Descending Order)	(Time 6) History of Maximum Variance	Detection of Swapped Features (Feature 2 and 3)	Feature	(Time 6) Velocity Rate (Descending Order)	(Time 6) History of Maximum IQR	Detection of Swapped Features (Feature 2 and 3)	
Feature 1	0.01186	0		Feature 2	0.00371	7	True Positive	
Feature 2	0.01090	0	False Negative	Feature 3	0.00342	4	True Positive	
Feature 3	0.01017	2	False Negative	Feature 1	0.00334	1		

Figure 40: The results of SEA data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

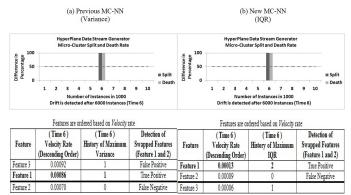


Figure 41: The results of HyperPlane data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

that changed with only 2 *false positives*. The *true positive* figures are based on features that are known to have changed as they have been swapped at the time of concept drift.

Next both approaches were tested on real datasets. For the experiment the default parameters, (stated in Table 3) of the technique were used unless stated otherwise. Realtime Min and Max *Normalisation* and *LPF* were applied to minimise the effect of feature-bias and noise, respec-

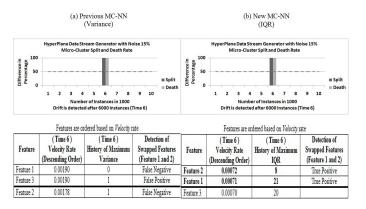


Figure 42: The results of HyperPlane data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

(a) Previous MC-NN (Variance)				(b) New MC-NN (IQR)				
_ 100	HyperPlane Data Stream Generator with Noise 25% Micro-Cluster Split and Death Rate			_ 100	bise 25%			
Difference in Percentage 0 00		5 6 7 8 er of Instances in 1000 d after 6000 Instances (Split 9 10 Death Time 6)	Difference in Percentage 0 00		5 6 7 8 er of Instances in 1000 d after 6000 Instances (1	= Split = Death 9 10	
	Features are or	dered based on Velocity 1	ate		Features are or	dered based on Velocity 1	ate	
Feature	(Time 6) Velocity Rate (Descending Order)	(Time 6) History of Maximum Variance	Detection of Swapped Features (Feature 1 and 2)	Feature	(Time 6) Velocity Rate (Descending Order)	(Time 6) History of Maximum IQR	Detection of Swapped Features (Feature 1 and 2)	
Feature 2	0.00158	1	True Positive	Feature 2	0.00029	9	True Positive	
Feature 1	0.00133	0	False Negative	Feature 1	0.00027	11	True Positive	
Feature 3	0.00121	0		Feature 3	0.00026	10		

Figure 43: The results of HyperPlane data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

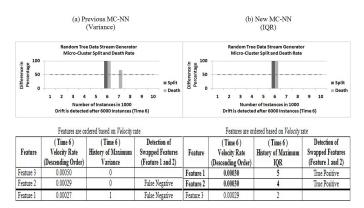


Figure 44: The results of Random Tree data stream generator with a noise level of 0% for tracking features using Micro-Clusters.

tively. A random number of random feature pairs have been selected to be swapped in order to validate whether the feature tracking method can identify the changed features.

Figures 47, 48, 49, and 50 visualise the results for concept drift detection and feature tracking in the same way as Figures 29 to 37 do for the artificial data streams. Again part (a) of the figures refers to the method based on variance and part (b) of the figures refers to the method based

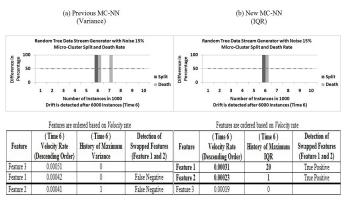


Figure 45: The results of Random Tree data stream generator with a noise level of 15% for tracking features using Micro-Clusters.

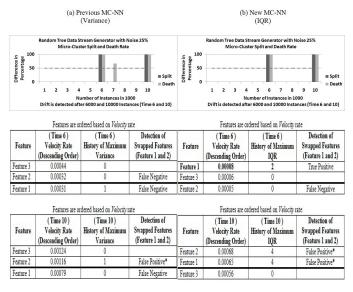


Figure 46: The results of Random Tree data stream generator with a noise level of 25% for tracking features using Micro-Clusters.

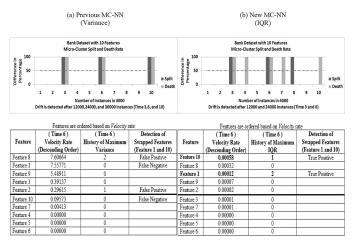
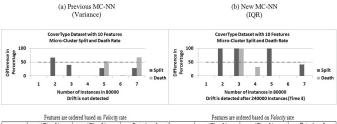


Figure 47: The results of Bank dataset with 10 features for tracking features using Micro-Clusters.

Table 8: Summary of the experimental results with artificial datasets generated with noise levels of 0%, 15% and 25%. The results are reported for Time 6 which is the point at which features had been swapped.

	True	True	False	False
Generator	Positive	Positive	Positive	Positive
	(Variance)	(IQR)	(Variance)	(IQR)
Sea with Noise 0%	1	2		
Sea with Noise 15%	1	2		
Sea with Noise 25%		2		
HyperPlane with Noise 0%	1	1	1	
HyperPlane with Noise 15%		2	1	
HyperPlane with Noise 25%	1	2		
RandomTree with Noise 0%		2		
RandomTree with Noise 15%		2		
RandomTree with Noise 25%		1	1*	2*
Total:	4	16	3	2



Feature	(Time 3) Velocity Rate	(Time 3) History of Maximum	Detection of Swapped Features	Feature	(Time 3) Velocity Rate	(Time 3) History of Maximum	Detection of Swapped Features
	(Descending Order)	Variance	(Features 6,7,8 and 9)		(Descending Order)	IQR	(Features 6,7,8 and 9)
Feature 9	0.54267	0	False Negative	Feature 9	0.13627	0	False Negative
Feature 1	0.38065	0		Feature 1	0.08728	0	
Feature 7	0.31810	0	False Negative	Feature 8	0.07995	1	True Positive
Feature 8	0.30382	0	False Negative	Feature 2	0.07212	82	False Positive
Feature 2	0.21634	0	and the provide the	Feature 7	0.04696	23	True Positive
Feature 5	0.15249	0		Feature 10	0.04182	0	
Feature 10	0.15043	0		Feature 5	0.04157	0	
Feature 3	0.09466	0		Feature 3	0.04001	0	
Feature 4	0.08274	0	100000000000000000000000000000000000000	Feature 4	0.01528	2	
Feature 6	0.01658	0	False Negative	Feature 6	0.00392	0	False Negative

Figure 48: The results of CoverType dataset with 10 features for tracking features using Micro-Clusters.

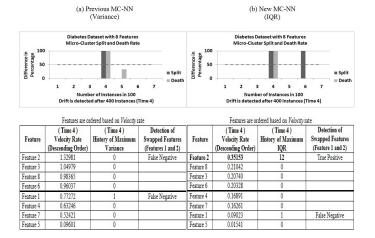


Figure 49: The results of Diabetes dataset with 8 features for tracking features using Micro-Clusters.

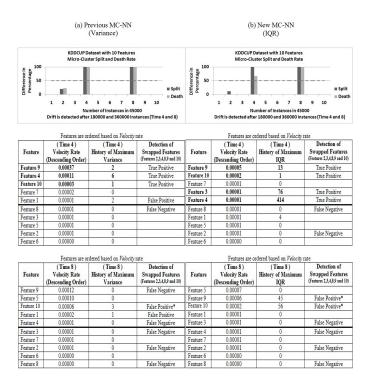


Figure 50: The results of KDDCUP dataset with 10 features for tracking features using Micro-Clusters.

on IQR. Regarding drift detection in Figures 47, 48, 49, and 50, it can be seen that the Split and Death rates at the time of concept drift increase (i.e., time when the features are swapped), indicating that the current set of Micro-Clusters does not fit the concept encoded in the data anymore and a concept drift is detected correctly for every dataset and method examined in the figures. Please note there are further concept drifts detected at different times than the features were swapped, which could be due to the fact that real data was used and thus there may be concept drifts that are not known. This is one of the reasons why the method was also evaluated on artificial datasets earlier in this section, as the ground truth for the artificial datasets was known. At this stage it is assumed that high Split and Death rates other than during the time when features were swapped are due to natural concept drift. As the ground truth for the concept drift is known only at the time of feature swapping, the evaluation of correct feature tracking was focussed on the time of feature swapping only.

Regarding the results for the *Bank* dataset in Figure 47, both methods identify a concept drift correctly at the time the features were swapped (in this case 2 features). The method based on IQR is superior to the method based on *Variance*, as it identified both swapped features correctly, whereas the method based on *Variance* did not identify any correctly. A similar result can be observed for the *Diabetes* dataset (see Figure 49), both methods identify a concept drift correctly at the time the features were swapped. Again the method based IQR is superior

to the method based on Variance, as it identified 1 of the swapped features correctly, whereas the method based on Variance did not identify any correctly. Regarding the results for the CoverType dataset (see Figure 48), again the method based on IQR was superior by identifying 2 of the swapped features (in this case 4 features) correctly whereas the method based on Variance did not identify any correctly, because a drift was not detected. For the dataset based on KDDCUP (see Figure 50) 6 features were swapped and again the method based on IQR was superior by identifying 4 features correctly and the method based on Variance only identifying 3 features correctly.

These results are summarised in Table 9. It can be seen that the method based on IQR generally achieves a much higher number of *true positive* identification of changed features compared with the method based on *Variance*. Also the method using IQR has a lower *false positive* number than the method using *Variance*.

Numbers indicated with a * in Table 9 indicate potentially false positives detections of features that changed their relevance. Potentially means in this case that there was also an unexpected concept drift, hence it is not possible to verify with absolute certainty if the detection was indeed a false positive.

Table 9: Summary of the experimental results with real datasets. The results are reported for the time of drift onset (Table 3) which is the time at which features were swapped.

Dataset	True Positive (Variance)	True Positive (IQR)	False Positive (Variance)	False Positive (IQR)
Bank		2	2	
CoverType		2		1
Diabetes		1		
KDDCUP	2	4	$2 + 2^*$	2*
Total:	2	9	6	3

Experiments have been conduced in a controlled environment on artificial datasets and in a less controlled environment on real datasets. Both methods based on IQR and Variance have been evaluated and compared on all test cases. It was observed that the method based on IQR identified all known concept drifts correctly whereas the method based on Variance did miss one known concept drift of a real data stream. Furthermore, it was found that the method based on IQR identified more changed features correctly compared with the method based on Variance. Loosely speaking the method based on IQR has shown to be superior to the method based on IQR has been chosen to evaluate the real-time feature selection strategy in the next section.

7.2.3. Real-Time Feature Selection

In the previous sections the paper examined the capability of the developed method to identify concept drifts and to track whether features have undergone a significant change. The purpose was to use this method to re-examine the relevance of the features for the classification task. It has been found that the method based on IQR preformed best in all respects. Thus the experiments in this section are conducted with the method based on IQR. This section evaluates the use of the method as feature selection technique as described in Section 6. The method is applied on a couple of real datasets with a larger number of features than in the previous more controlled experiments, with no known ground truth, to evaluate the effect of the methods in real scenarios. Information about the datasets can be found in Table 4 in Section 7.1.2. It should be noted that the *CoverType* dataset has been re-used for the experiments here under uncontrolled conditions. This time all 54 features were included. It is expected that this original version of *CoverType* is more challenging for data mining algorithms to induce good models compared with the reduced version used earlier in the controlled experiments in Section 7.2.2. The data stream classifier chosen to be used with the developed method was the Hoeffding Tree [13]. The reason for choosing the Hoeffding Tree was due to its popularity and the fact that it is considered to be one of the most accurate data stream classifiers [55, 52]. The Hoeffding Tree classifier is training and updating incrementally instance by instance. From the start of the experiments all features are considered relevant, and the proposed method may at any time during the experiment detect a concept drift and flag features as relevant or irrelevant after a drift has been detected. Thus at any time during the experiment the Hoeffding Tree classifier selects only the feature values of relevant features and accordingly uses only the currently relevant features for training and incrementally updating the model. Figure 51 shows the accuracy differences over time the method achieved using IQR for real-time feature selection in comparison with applying the Hoeffding Tree classifier as standalone method. As it can be seen in the figure, Hoeffding Trees using the proposed method generally achieved a better accuracy over time. Only during a few time windows the method achieved a marginally lower accuracy.

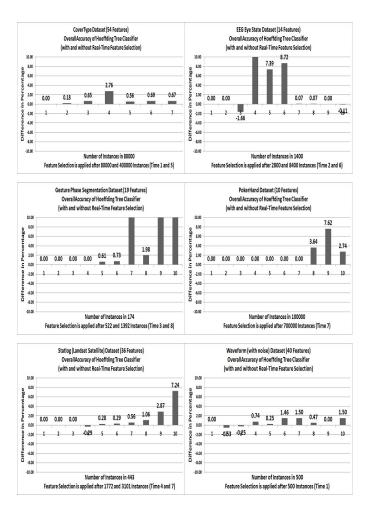


Figure 51: The results of real-time feature selection with uncontrolled datasets using Micro-Clusters.

Table 10 summarises the results for the experiments depicted in Figure 51. It states the average accuracy achieved with and without using the proposed real-time feature selection method. It also indicates at which time window features and how many features have been re-evaluated for inclusion or removal from the current feature set considered by the Hoeffding Tree. As can be seen the method actively re-evaluated features for inclusion in the tree at various times and achieved on average a higher accuracy compared with standalone Hoeffding Trees (not employing the proposed real-time feature selection method).

Table 10: Summary of the results for the experiments using real datasets with Hoeffding tree classifier.

Real Dataset	OverallAccuracy Average (with Real-Time Feature Selection)	OverallAccuracy Average (without Real-Time Feature Selection)	Time of Applying Real-Time Feature Selection	Number of Features Flagged
CoverType	79.81	79.19	(2 to 4) and (6 to 7)	1
EEG Eye State	83.68	81.49	(3 to 5) and (7 to 10)	1
Gesture Phase Segmentation	80.23	72.18	(4 to 7) and (9 to 10)	1
Poker Hand	51.75	51.02	8 and 10	5
Statlog (Landsat Satellite)	81.63	80.68	(5 to 6) and (8 to 10)	5
Waveform (with noise)	80.68	80.26	2 to 10	1

Loosely speaking the results show that the proposed real-time feature selection method indeed improves the accuracy of data stream classifiers.

8. Discussion and Conclusions

This paper has investigated the problem of real-time feature selection. At present the focus of data stream mining lies in the development of data mining algorithms rather than on pre-processing methods. Thus at present there are no developments for truly real-time feature selection given a data streaming input space. This is important as features may potentially change their relevance for data mining tasks based on certain measures of relevance such as Information Gain. Thus the three objectives of this paper were to develop a real-time pre-processing method that could (a) detect a concept drift, (b) identify features that were involved in a concept drift and thus potentially changed their relevance and (c) build and validate a real-time feature selection method based on the aforementioned developments. The starting point for this research was the MC-NN classifier. This research was not concerned with the classification capabilities of MC-NN but in the behaviour of its underlying model during concept drift. The MC-NN model is based on adaptive statistical Micro-Cluster summaries of the absorbed data stream instances that can *Split* into new Micro-Clusters, change their size/position in the feature space or be removed (Micro-Cluster death) in order to adapt to concept drift. The research proposed in this work was based on two hypotheses on the behaviour of MC-NN in this regard:

(1) The *Split* and *Death* rates are expected to increase during a concept drift and thus could be used as a measure to detect concept drift in real-time; and (2) the direction of the Micro-Cluster movement in feature space during concept drift and their *Velocity* indicate which features are involved in the concept drift. This could be used as a measure if the relevance of a feature for a data mining task has changed.

MC-NN originally used variance as a statistical measure to *Split* the Micro-Cluster. During this research it was expected that variance as an indirect measure for concept drift adaptation would be susceptible to potential outliers and noise. Thus an alternative method has been explored for adapting micro-clusters based on IQR. Both methods have been evaluated with respect to hypothesis 1 and 2 on artificial data streams and real datasets. In addition for both methods a Low Pass Filter (LPF) was also incorporated to filter out noise and normalisation to reduce feature bias. The original MC-NN did not make use of LPF or normalisation. The evaluation of the proposed method initially focused on the approach based on the already available MC-NN statistical measure, namely Variance. Thus the method was evaluated on artificial data streams and real datasets with artificially induced concept drifts. It was observed that the method did detect concept drifts very for the artificial data streams compared with competing alternative concept drift detection methods. It achieved a very high true positive detection number and resulted in only one *false positive* detection. For the real datasets the method detected all but one arti-

ficially induced concept drift correctly but also detected further concept drifts. These drifts may have been natural and thus previously unknown concept drifts. Thus in the next step of the evaluation LPF, Normalisation and IQR were used as an alternative measure for feature splitting and concept drift detection. To allow a fair comparison, LPF and Normalisation were applied on both methods based on variance and the method based on IQR. Both versions of the method were compared with regards to concept drift detection and feature tracking for the artificial data streams and the real datasets (with induced concept drift). For the artificial data streams all induced concept drifts were detected correctly by both versions of the method and for the real datasets one concept drift was missed but only by the method based on variance. Regarding feature tracking, the method based on IQR clearly outperformed the method based on Variance. The method based on IQR achieved a high true positive identification of features that were actually features involved in concept drift and a low number of *false positive* identifications. Thus the method based on variance was considered not suitable for feature tracking and the next step of the evaluation focussed only on the method based on IQR for feature selection. Here the method for feature selection was tested based on feature tracking using IQR. The evaluation was conducted in an uncontrolled environment on 6 case studies with data streams based on real datasets. Thus the ground truth for feature relevance and concept drift were not known. Hence the impact of the method on the classification accuracy over time was measured and also the extent to which the method actually identified features with changing relevance. The data stream classification method chosen was the popular Hoeffding Tree algorithm. The results showed that the method detected various concept drifts throughout the streams and identified features for re-evaluation for their relevance. It was also shown that the classifier achieved a higher average accuracy when using the proposed method compared with not using the method. Overall the research represents a first attempt to resolve real-time feature selection for data stream mining tasks. It has been shown that the method can indeed identify concept drift, track features and identify features that may have changed their relevance for the data mining task in real-time. It has also been shown that the proposed method can improve the accuracy of data stream classification tasks.

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