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Holographic QCD for H-dibaryon (uuddss)

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Abstract. The H-dibaryon (uuddss) is studied in holographic QCD for the first time. In holographic QCD, four-dimensional QCD, i.e., $SU(N_c)$ gauge theory with chiral quarks, can be formulated with S^1 -compactified D4/D8/D8-brane system. In holographic QCD with large N_c , all the baryons appear as topological chiral solitons of Nambu-Goldstone bosons and (axial) vector mesons, and the H-dibaryon can be described as an $SO(3)$ -type topological soliton with $B = 2$. We derive the low-energy effective theory to describe the H-dibaryon in holographic QCD. The H-dibaryon mass is found to be twice of the $B = 1$ hedgehog-baryon mass, $M_H \simeq 2.00M_{B=1}^{HH}$, and is estimated about 1.7GeV, which is smaller than mass of two nucleons (flavor-octet baryons), in the chiral limit.

1 Introduction

Nowadays, QCD is established as the fundamental theory of the strong interaction, and all the experimentally observable hadrons have been considered as color-singlet composite particles of quarks and gluons. From QCD, as well as ordinary mesons ($\bar{q}q$) and baryons (qqq) in the valence picture, there can exist “exotic hadrons” [1] such as glueballs, multi-quarks [2, 3] and hybrid hadrons, and the exotic-hadron physics has been an interesting field theoretically and experimentally.

The H-dibaryon, $B = 2$ $SU(3)$ flavor-singlet bound state of uuddss, has been one of the oldest multi-quark candidates, first predicted by R. L. Jaffe in 1977 from a group-theoretical argument of the color-magnetic interaction in the MIT bag model [2]. In 1985, the H-dibaryon was also investigated [4, 5] in the Skyrme-Witten model [6–8]. These two model calculations suggested a low-lying H-dibaryon below the $\Lambda\Lambda$ threshold, which means the stability of H against the strong decay. In 1991, however, Imai group experimentally excluded the low-lying H-dibaryon [9], and found the first event of the double hyper nuclei, i.e., ${}^6_{\Lambda\Lambda}\text{He}$, instead. Then, the current interest is mainly possible existence of the H-dibaryon as a resonance state.

Theoretically, it is still interesting to consider the stability of H-dibaryons in the $SU(3)$ flavor-symmetric case of $m_u = m_d = m_s$ [10–12], because the large mass of H may be due to an $SU(3)$ flavor-symmetry breaking by the large s-quark mass, $m_s \gg m_{u,d}$, in the real world. Actually, recent lattice QCD simulations suggest the stable H-dibaryon in an $SU(3)$ flavor-symmetric and large quark-mass region [10, 11].

So, how about the H-dibaryon in the chiral limit of $m_u = m_d = m_s = 0$? Although the lattice QCD calculation is usually a powerful method to evaluate hadron masses, it is fairly difficult to take the chiral limit, because a large-volume lattice is needed for such a calculation to control massless pions.

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In this paper, we study the H-dibaryon and its properties in the chiral limit using holographic QCD [13], which has a direct connection to QCD, unlike most effective models. In particular, we investigate the H-dibaryon mass from the viewpoint of its stability in the chiral limit.

2 Holographic QCD

In this section, we briefly summarize the construction of holographic QCD from a D-brane system [14, 15], and derive the low-energy effective theory of QCD [16] at the leading order of $1/N_c$ and $1/\lambda$ expansions, where the 't Hooft coupling $\lambda \equiv N_c g_{\text{YM}}^2$ is given with the gauge coupling g_{YM} .

2.1 QCD-equivalent D-brane system

Just after J. M. Maldacena’s discovery of the AdS/CFT correspondence in 1997 [17], E. Witten [14] succeeded in 1998 the formulation of non-SUSY four-dimensional pure $SU(N_c)$ gauge theories using an S^1 -compactified D4-brane in the superstring theory. In 2005, Sakai and Sugimoto showed a remarkable formulation of four-dimensional QCD, i.e., $SU(N_c)$ gauge theory with chiral quarks, using an S^1 -compactified D4/D8/ $\overline{\text{D8}}$ -brane system [15], as shown in Fig. 1. Such a construction of QCD is often called holographic QCD.

This QCD-equivalent D-brane system consists of N_c D4-branes and N_f D8/ $\overline{\text{D8}}$ -branes, which give color and flavor degrees of freedom, respectively. In this system, gluons appear as 4-4 string modes on N_c D4-branes, and the left/right quarks appear as 4-8/ $4-\overline{8}$ string modes at the cross point between D4 and D8/ $\overline{\text{D8}}$ branes, as shown in Fig. 1. This D-brane system possesses the $SU(N_c)$ gauge symmetry and the exact chiral symmetry [15], and gives QCD in the chiral limit.

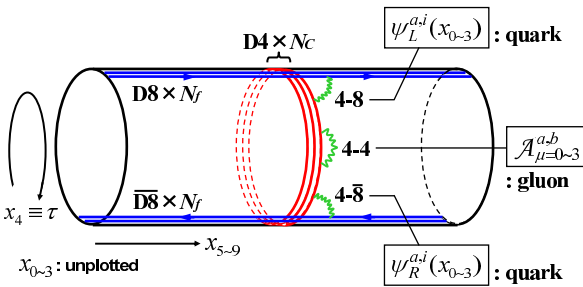


Figure 1. Construction of holographic QCD with an S^1 -compactified D4/D8/ $\overline{\text{D8}}$ -brane system, which corresponds to non-SUSY four-dimensional QCD with chiral quarks [15, 16]. This figure is taken from Ref.[16].

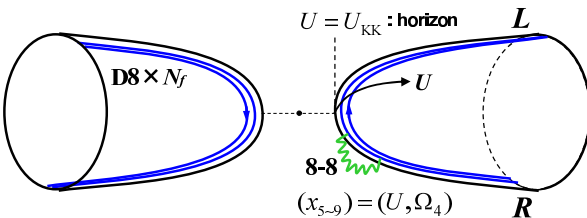


Figure 2. Holographic QCD after the replacement of large- N_c D4 branes by a gravitational background via the gauge/gravity correspondence [14–16]. This figure is taken from Ref.[16].

In holographic QCD, $1/N_c$ and $1/\lambda$ expansions are usually taken. In large N_c , D4-branes are the dominant gravitational source, and can be replaced by their SUGRA solution [15] as shown in Fig. 2, via the gauge/gravity correspondence. In large λ , the strong-coupling gauge theory is converted into a weak-coupling gravitational theory [14]. In this paper, we consider the leading order of $1/N_c$ and $1/\lambda$ expansions.

2.2 Low-energy effective theory

In the presence of the D4-brane gravitational background g_{MN} , the D8/ $\overline{\text{D8}}$ brane system can be expressed with the non-Abelian Dirac-Born-Infeld (DBI) action,

$$S_{\text{D8}}^{\text{DBI}} = T_8 \int d^9x e^{-\phi} \sqrt{-\det(g_{MN} + 2\pi\alpha' F_{MN})}, \quad (1)$$

at the leading order of $1/N_c$ and $1/\lambda$ expansions. Here, $F_{MN} \equiv \partial_M A_N - \partial_N A_M + i[A_M, A_N]$ is the field strength of the $U(N_f)$ gauge field A_M in the flavor space on the D8 brane. The surface tension T_8 , the dilaton field ϕ and the Regge slope parameter α' are defined in the framework of the superstring theory, and, for the simple notation, we have taken the $M_{\text{KK}} = 1$ unit, where the Kaluza-Klein mass M_{KK} is the energy scale of this theory [15].

After some calculations, one can derive the meson theory equivalent to infrared QCD at the leading order of $1/N_c$ and $1/\lambda$ [15, 16]. For the construction of the low-energy effective theory, we only consider massless Nambu-Goldstone (NG) bosons and the lightest $SU(N_f)$ vector meson $\rho_\mu(x) \equiv \rho_\mu(x)^a T^a \in \text{su}(N_f)$, which we simply call “ ρ -meson”. We eventually derive the four-dimensional effective action in Euclidean space-time $x^\mu = (t, \mathbf{x})$ [16],

$$\begin{aligned} S_{\text{HQCD}} = \int d^4x \left\{ \frac{f_\pi^2}{4} \text{tr}(L_\mu L_\mu) - \frac{1}{32e^2} \text{tr}[L_\mu, L_\nu]^2 + \frac{1}{2} \text{tr}(\partial_\mu \rho_\nu - \partial_\nu \rho_\mu)^2 + m_\rho^2 \text{tr}(\rho_\mu \rho_\mu) \right. \\ \left. - ig_3 \text{tr}\{(\partial_\mu \rho_\nu - \partial_\nu \rho_\mu)[\rho_\mu, \rho_\nu]\} - \frac{1}{2} g_4 \text{tr}[\rho_\mu, \rho_\nu]^2 + ig_1 \text{tr}\{[\alpha_\mu, \alpha_\nu](\partial_\mu \rho_\nu - \partial_\nu \rho_\mu)\} \right. \\ \left. + g_2 \text{tr}\{[\alpha_\mu, \alpha_\nu][\rho_\mu, \rho_\nu]\} + g_3 \text{tr}\{[\alpha_\mu, \alpha_\nu](\beta_\mu, \rho_\nu) + [\rho_\mu, \beta_\nu]\} \right. \\ \left. - ig_4 \text{tr}\{(\partial_\mu \rho_\nu - \partial_\nu \rho_\mu)(\beta_\mu, \rho_\nu) + [\rho_\mu, \beta_\nu]\} - g_5 \text{tr}\{[\rho_\mu, \rho_\nu](\beta_\mu, \rho_\nu) + [\rho_\mu, \beta_\nu]\} \right. \\ \left. - \frac{1}{2} g_6 \text{tr}([\alpha_\mu, \rho_\nu] + [\rho_\mu, \alpha_\nu])^2 - \frac{1}{2} g_7 \text{tr}([\beta_\mu, \rho_\nu] + [\rho_\mu, \beta_\nu])^2 \right\}, \quad (2) \end{aligned}$$

where L_μ is defined with the chiral field $U(x)$ or the NG boson field $\pi(x) \equiv \pi^a(x) T^a \in \text{su}(N_f)$ as

$$L_\mu \equiv \frac{1}{i} U^\dagger \partial_\mu U \in \text{su}(N_f), \quad U(x) \equiv e^{i2\pi(x)/f_\pi} \in \text{SU}(N_f). \quad (3)$$

The axial vector current α_μ and the vector current β_μ are defined as

$$\alpha_\mu \equiv l_\mu - r_\mu \in \text{su}(N_f)_A, \quad \beta_\mu \equiv \frac{1}{2}(l_\mu + r_\mu) \in \text{su}(N_f)_V, \quad (4)$$

with the left and the right currents,

$$l_\mu \equiv \frac{1}{i} \xi^\dagger \partial_\mu \xi, \quad r_\mu \equiv \frac{1}{i} \xi \partial_\mu \xi^\dagger, \quad \xi(x) \equiv e^{i\pi(x)/f_\pi} \in \text{SU}(N_f). \quad (5)$$

Thus, we obtain the effective meson theory derived from QCD in the chiral limit at the leading order of $1/N_c$ and $1/\lambda$ expansions. Note that this theory has just two independent parameters, e.g., the Kaluza-Klein mass $M_{\text{KK}} \sim 1\text{GeV}$ and $\kappa \equiv \lambda N_c / 216\pi^3$ [15, 18], and all the coupling constants and masses in the effective action (2) are expressed with them [16]. As a remarkable fact, in the absence of the ρ -meson, this effective theory reduces to the Skyrme-Witten model [6] in Euclidean space-time,

$$\mathcal{L}_{\text{Skyrme}} = \frac{f_\pi^2}{4} \text{tr}(L_\mu L_\mu) - \frac{1}{32e^2} \text{tr}[L_\mu, L_\nu]^2. \quad (6)$$

3 H-dibaryon as a B=2 Topological Chiral Soliton in Holographic QCD

As a general argument, large- N_c , QCD becomes a weakly interacting meson theory, and baryons are described as topological chiral solitons of mesons [7]. In holographic QCD with large N_c , the H-dibaryon is also described as a $B = 2$ chiral soliton, and its static profile is expressed with the ‘‘SO(3)-type hedgehog Ansatz’’, similarly in the Skyrme-Witten model [4, 5]. Here, the SO(3) is the flavor-symmetric subalgebra of $SU(3)_f$, and its generators $\Lambda_{i=1,2,3}$ are

$$\Lambda_1 = \lambda_7 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad \Lambda_2 = -\lambda_5 = \begin{pmatrix} 0 & 0 & i \\ 0 & 0 & 0 \\ -i & 0 & 0 \end{pmatrix}, \quad \Lambda_3 = \lambda_2 = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \quad (7)$$

which satisfy the SO(3) algebra and the following relations,

$$[\Lambda_i, \Lambda_j] = i\epsilon_{ijk}\Lambda_k, \quad (\mathbf{\Lambda} \cdot \hat{\mathbf{x}})^3 = \mathbf{\Lambda} \cdot \hat{\mathbf{x}}, \quad \text{Tr}[(\mathbf{\Lambda} \cdot \hat{\mathbf{x}})^2 - 2/3] = 0, \quad (8)$$

with $\hat{\mathbf{x}} \equiv \mathbf{x}/r$ and $r \equiv |\mathbf{x}|$. The SO(3)-type hedgehog Ansatz [4, 5, 13] is generally expressed as

$$U(\mathbf{x}) = e^{i[(\mathbf{\Lambda} \cdot \hat{\mathbf{x}})F(r) + (\mathbf{\Lambda} \cdot \hat{\mathbf{x}})^2 - 2/3]\varphi(r)} \in SU(3)_f, \quad F(r) \in \mathbf{R}, \quad \varphi(r) \in \mathbf{R}, \quad (9)$$

where $F(r)$ and $\varphi(r)$ are the chiral profile functions characterizing the NG boson field. Note that $U(\mathbf{x})$ in Eq.(9) is the general form of the special unitary matrix which consists of $\mathbf{\Lambda} \cdot \hat{\mathbf{x}}$, because of Eq.(8). For the topological soliton, the $B = 2$ boundary condition [4, 5] is given as

$$F(\infty) = \varphi(\infty) = 0, \quad F(0) = \varphi(0) = \pi. \quad (10)$$

On the $SU(3)_f$ ρ -meson field, we use the SO(3) Wu-Yang-’t Hooft-Polyakov Ansatz,

$$\rho_0(\mathbf{x}) = 0, \quad \rho_i(\mathbf{x}) = \epsilon_{ijk}\hat{x}_j G(r)\Lambda_k \in \text{so}(3) \subset \text{su}(3), \quad G(r) \in \mathbf{R}, \quad (11)$$

similarly in the $B = 1$ case in holographic QCD [16]. (This $G(r)$ corresponds to $-\tilde{G}(r)$ in Ref.[16].) Thus, all the above treatments are symmetric in the (u, d, s) flavor space.

Substituting Ansätze (9) and (11) in Eq.(2), we derive the effective action to describe the static H-dibaryon in terms of the profile functions $F(r)$, $\varphi(r)$ and $G(r)$ [13]:

$$\begin{aligned} S_{\text{HQCD}} = & \int d^4x \left\{ \frac{f_\pi^2}{4} \left[\frac{2}{3}\varphi'^2 + 2F'^2 + \frac{8}{r^2}(1 - \cos F \cos \varphi) \right] + \frac{1}{32e^2} \frac{16}{r^2} [(\varphi'^2 + F'^2)(1 - \cos F \cos \varphi) \right. \\ & + 2\varphi'F' \sin F \sin \varphi + \frac{1}{r^2} \{ (1 - \cos F \cos \varphi)^2 + 3 \sin^2 F \sin^2 \varphi \} \\ & + \frac{1}{2} \left[8 \left(\frac{3}{r^2} G^2 + \frac{2}{r} G G' + G'^2 \right) \right] + m_\rho^2 [4G^2] + g_{3\rho} \left[8 \frac{G^3}{r} \right] + \frac{1}{2} g_{4\rho} [4G^4] \\ & - g_1 \left[\frac{16}{r} \left\{ \left(\frac{1}{r} G + G' \right) \left(F' \sin \frac{F}{2} \cos \frac{\varphi}{2} + \varphi' \cos \frac{F}{2} \sin \frac{\varphi}{2} \right) + \frac{1}{r^2} G (1 - \cos F \cos \varphi) \right\} \right] \\ & - g_2 \left[\frac{8}{r^2} G^2 (1 - \cos F \cos \varphi) \right] \\ & + g_3 \left[\frac{16}{r^3} G \left\{ 3 \sin F \sin \frac{F}{2} \sin \varphi \sin \frac{\varphi}{2} + \left(1 - \cos \frac{F}{2} \cos \frac{\varphi}{2} \right) (1 - \cos F \cos \varphi) \right\} \right] \\ & - g_4 \left[\frac{16}{r^2} G^2 \left(1 - \cos \frac{F}{2} \cos \frac{\varphi}{2} \right) \right] - g_5 \left[\frac{8}{r} G^3 \left(1 - \cos \frac{F}{2} \cos \frac{\varphi}{2} \right) \right] \\ & + g_6 [4G^2(F'^2 + \varphi'^2)] + g_7 \left[\frac{8}{r^2} G^2 \left\{ 3 \sin^2 \frac{F}{2} \sin^2 \frac{\varphi}{2} + \left(1 - \cos \frac{F}{2} \cos \frac{\varphi}{2} \right)^2 \right\} \right] \left. \right\} \\ = & \int dt \int_0^\infty dr 4\pi r^2 \varepsilon[F(r), \varphi(r), G(r)]. \quad (12) \end{aligned}$$

4 H-dibaryon Solution in Holographic QCD

To obtain the topological soliton solution of the H-dibaryon in holographic QCD, we numerically calculate the profiles $F(r)$, $\varphi(r)$ and $G(r)$ [13] by minimizing the Euclidean effective action (12) under the boundary condition (10) [19]. The two independent parameters, e.g., M_{KK} and $\kappa \equiv \lambda N_c/216\pi^3$, are set to reproduce the pion decay constant $f_\pi=92.4\text{MeV}$ and the ρ -meson mass $m_\rho=776\text{MeV}$ [15, 16].

For the H-dibaryon solution in holographic QCD, we obtain the chiral profiles, $F(r)$ and $\varphi(r)$, and the scaled ρ -meson profile $G(r)/\kappa^{1/2}$ as shown in Fig. 3, and estimate the H-dibaryon mass of $M_H \simeq 1673\text{MeV}$ in the chiral limit. Figure 4 shows the energy density $4\pi r^2 \varepsilon(r)$ in the H-dibaryon. The root mean square radius of the H-dibaryon is estimated as $\sqrt{\langle r^2 \rangle_H} \simeq 0.413\text{fm}$ in terms of the energy density. For comparison, we calculate the $B = 1$ hedgehog (HH) baryon in holographic QCD with the same numerical condition, and estimate $M_{B=1}^{\text{HH}} \simeq 836.7\text{MeV}$ and $\sqrt{\langle r^2 \rangle_{B=1}^{\text{HH}}} \simeq 0.362\text{fm}$. Thus, the H-dibaryon mass is twice of the $B = 1$ hedgehog-baryon mass, $M_H \simeq 2.00M_{B=1}^{\text{HH}}$.

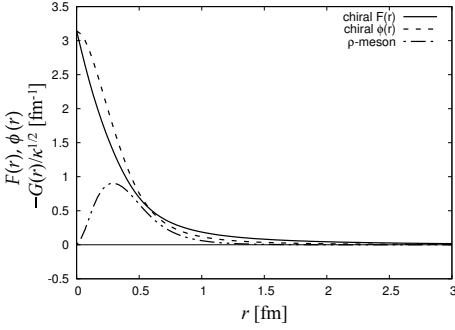


Figure 3. The chiral profiles, $F(r)$ and $\varphi(r)$, and the scaled ρ -meson profile $G(r)/\kappa^{1/2}$ in the H-dibaryon as the $SO(3)$ -type hedgehog soliton solution in holographic QCD. Here, the topological boundary condition of $B = 2$ is $F(0) = \varphi(0) = \pi$ and $F(\infty) = \varphi(\infty) = 0$.

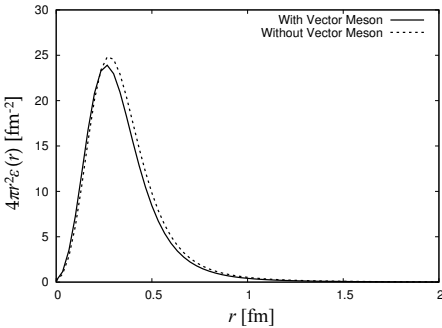


Figure 4. The energy density distribution $4\pi r^2 \varepsilon(r)$ in the H-dibaryon (solid curve), and that without vector mesons (dashed curve) for comparison.

We summarize in Table 1 the mass and the radius of the H-dibaryon and the $B = 1$ hedgehog baryon in holographic QCD. Since the nucleon mass M_N is larger than the $B = 1$ hedgehog mass $M_{B=1}^{\text{HH}}$ by the rotational energy [6, 8], the H-dibaryon mass is smaller than mass of two nucleons (flavor-octet baryons), $M_H < 2M_N$, in the chiral limit.

Finally, we examine the vector-meson effect for the H-dibaryon by comparing with the $\rho(x) = 0$ case. As the result, we find that the chiral profiles $F(r)$ and $\varphi(r)$ are almost unchanged and slightly shrink by the vector-meson effect, and the energy density also shrinks slightly, as shown in Fig. 4.

Table 1. The mass M_H and the radius $\sqrt{\langle r^2 \rangle_H}$ of the H-dibaryon in the chiral limit in holographic QCD, together with those of the $B = 1$ hedgehog (HH) baryon.

| M_H | $\sqrt{\langle r^2 \rangle_H}$ | $M_{B=1}^{HH}$ | $\sqrt{\langle r^2 \rangle_{B=1}^{HH}}$ |
|----------|--------------------------------|----------------|---|
| 1673 MeV | 0.413 fm | 836.7 MeV | 0.362 fm |

As a significant vector-meson effect, we find that about 100MeV mass reduction is caused by the interaction between NG bosons and vector mesons in the interior region of the H-dibaryon.

5 Summary and Concluding Remarks

We have studied the H-dibaryon (uuddss) as the $B = 2$ SO(3)-type topological chiral soliton solution in holographic QCD for the first time. The H-dibaryon mass is twice of the $B = 1$ hedgehog-baryon mass, $M_H \simeq 2.00M_{B=1}^{HH}$, and is estimated about 1.7GeV, which is smaller than mass of two nucleons (flavor-octet baryons), in the chiral limit. In holographic QCD, we have found that the vector-meson effect gives a slight shrinkage of the chiral profiles and the energy density, and also gives about 100MeV mass reduction of the H-dibaryon.

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