1	Title: Informing	network	management	using fuzzy	cognitive	maps
-			management		00011010	maps

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- 19 fellowship from the ARC Centre of Excellence for Environmental decisions
- Predicting how management will affect a network is a key challenge of modern conservation.
 Every apprictive management of network
- Fuzzy cognitive maps are a promising method to predict the outcome of network
 management.
- There are two critical methodological issues with fuzzy cognitive maps.

- We describe these issues and show how to overcome them.
- We demonstrate how to use a fuzzy cognitive map to inform management on
 Christmas Island.

28

30 Abstract:

Modern conservation requires robust predictions about how management will affect an ecosystem 31 32 and its species. The large uncertainties about the type and strength of interactions makes model 33 predictions particularly unreliable. In this paper, we show how fuzzy cognitive maps can produce 34 robust predictions in complex and uncertain ecosystems. The use of fuzzy cognitive maps has been 35 increasing markedly, but there are two critical issues with the approach: translation of expert 36 knowledge into the FCM is often done incorrectly; and sensitivity analyses are rarely conducted. 37 Translating expert knowledge is a constant challenge for ecological modellers, often because experts 38 know about the behaviour of a system, but modellers need to know model parameters, which 39 subsequently lead to system behaviour. We describe how to correctly incorporate expert knowledge 40 into FCMs, and we describe how to appropriately conduct uncertainty and sensitivity analysis. We 41 illustrate this process with a previously published network for feral cat and black rat control on 42 Christmas Island. Perverse indirect effects of conservation management are a key concern, and 43 methods to help us make informed decisions are required. Fuzzy cognitive maps are a promising 44 approach for this, but it requires the methodological improvements that we present here.

45

46 Keywords: Species interactions, ecosystem modelling, invasive species, cat control, rat control

47 Introduction:

Environmental systems are complex and interconnected, so even small changes to local processes
can substantially change the future state of populations, ecosystems, and the environment (Shears
& Babcock, 2003; Fortin et al., 2005; Holdo et al., 2009). Conservation initiatives are better
resourced than ever before, but despite best intentions, unintended negative consequences of
management sometimes occur (Dexter, Hudson, James, MacGregor, & Lindenmayer, 2013; Larrosa,
Carrasco, & Milner-Gulland, 2016; Pech & Maitland, 2016). To avoid such perverse outcomes, we
must account for species interactions that govern the dynamics of complex ecosystems. However,

detail about how species affect each other is often lacking, and gathering ecological information can
be expensive and time consuming (Caughlan & Oakley, 2001) – particularly for species interactions
(Dambacher, Luh, Li, & Rossignol, 2003). Since this cost is high, it's important to know whether data
already exists to proceed with management, or whether more data is required. Making robust
predictions about how any action will affect a whole system is vital for informed management
decisions, but, doing this has been a key methodological challenge.

61 Network models are important for informing system management, as they can predict how changes 62 will proliferate throughout a complex system. For example in ecology and conservation, they have 63 been applied to manage ecosystems for threatened species conservation (Ramsey & Norbury, 2009; 64 Bode et al., 2016), and to help improve fisheries management (Smith, Sainsbury, & Stevens, 1999; 65 Fulton et al., 2011; Punt, Butterworth, de Moor, De Oliveira, & Haddon, 2016). However, network 66 models require detailed knowledge about many interactions, and different modelling software can 67 produce qualitatively different predictions (Forrest, Savina, Fulton, & Pitcher, 2015). Hence, we must 68 develop methods to make predictions in systems where data are scarce and the nature of 69 interactions is unknown; fuzzy cognitive maps (FCMs) are a promising solution. 70 A growing body of literature uses FCMs to analyse networks (see Supporting Information S1), and 71 they have been applied broadly in conservation and ecology (Papageorgiou & Salmeron, 2013), 72 facilitated by easily accessible software (eg S. A. Gray, Gray, Cox, & Henly-Shepard, 2013). FCMs 73 utilise expert knowledge about whether entities have positive or negative interactions on each other 74 to predict how changes will proliferate throughout a system (Kok, 2009). Ideal for systems with little 75 data, they can help formalise expert reasoning and predictions (eg Game et al., 2017). For systems

where highly parameterised models are unsuitable, they openly and transparently display the logic

behind expert predictions - an important aspect of conservation decision-making (Blomquist et al.,

78 2010; Donlan, Luque, & Wilcox, 2014)

79 While using expert knowledge to build a network model posits many advantages, relying on opinions 80 of individuals has drawbacks: experts can be biased; translation of knowledge into the FCM can be 81 non-intuitive; and appropriate sensitivity and uncertainty analysis must be conducted. This is 82 important because people are biased in factual estimation (Martin, Burgman, et al., 2012), 83 projection (McCarthy et al., 2004), and ecological decision-making (Burgman, 2005; Holden & Ellner, 84 2016). Translating expert opinion into models is challenging because we intuitively interpret 85 interactions as the effect of one node on another, rather than the per-capita interactions, as 86 required for population models. Given these challenges, it is vital that appropriate sensitivity and 87 uncertainty analyses are conducted. Unfortunately, these points are very rarely addressed in FCM 88 analyses (but see Ramsey & Norbury, 2009; Ramsey et al., 2012; Sacchelli & Fabbrizzi, 2015). Given 89 their widespread use and the potential for misinterpretation, accurate and robust results require 90 updating of current methods.

91 In this paper, we describe how use of fuzzy cognitive maps must change to produce robust 92 predictions in complex systems. First, we offer an overview of the FCM method and describe the 93 methodological issues in detail. We then suggest ways that help translate expert knowledge for 94 FCMs and help to appropriately account for uncertainty. Finally, we illustrate the application of FCM 95 with a case study of an invaded ecosystem on Christmas Island, Australia. We often need to act fast 96 in conservation (Martin, Nally, et al., 2012), but quantitative data is lacking frequently. Utilising 97 expert opinion is a potentially powerful way for making robust predictions in complex systems, and 98 FCMs are a valuable tool for this.

99 Material and methods

100 Christmas Island

101 The Australian Territory of Christmas Island is a small (135 km²), oceanic island about 350 km south

102 of Java and 1,550 km north-west of mainland Australia. Being the top of an extinct underwater

103 volcano the basalt island has never had a connection to the mainland and hence harbours a number

104 of endemic species (James & McAllan, 2014), such as the Christmas Island flying fox (Pteropus 105 natalis), the blue-tailed skink (Cryptoblepharus egeriae), the giant gecko (Cyrtodactylus sadleiri) and 106 the Christmas Island imperial pigeon (Ducula whartoni), only to name a few. Having naturally small 107 population sizes, endemic species are threatened by habitat loss, degradation, introduced diseases 108 and invasive species (Misso and West 2014). These threats have already caused several extinctions 109 on the island (Wyatt et al., 2008; Lunney, Law, Schulz, & Pennay, 2011), and the loss of the Christmas 110 Island pipistrelle was particularly frustrating, given the rescue effort (Lindenmayer, Piggott, & 111 Wintle, 2013). To avoid further extinctions, threatened species on Christmas Island now receive 112 priority attention with management acting on the conservation of individual species, the restoration 113 of degraded land and the removal of damaging invasive species, such as yellow crazy ants (Abbott, 114 Green, & O'Dowd, 2014) and feral cats (Johnston, McCaldin, & Rieker, 2016). 115 Well-documented and wide-ranging impacts of predator control indicate the potential for 116 mesopredator release following the removal of the top-predator from the system. For example 117 removing feral cats has been found to increase the predation pressure on native birds by releasing 118 other invasive species from predation pressure, such as omnivorous black rats (*Rattus rattus*) 119 (Courchamp, Langlais, & Sugihara, 1999; Fan, Kuang, & Feng, 2005; Rayner, Hauber, Imber, Stamp, & 120 Clout, 2007; Ritchie & Johnson, 2009; Prior, Adams, Klepzig, & Hulcr, 2018). To test if mesopredator 121 release is possible in the Christmas Island context, we consider a network of species interactions on 122 Christmas Island (Figure 1) and test the impact of removing feral cats on threatened species and 123 whether rat control would be necessary. The Christmas Island species network, adapted from Han 124 (2016), is a simplification of the real ecosystem, and as with many interaction networks, it was 125 generated to capture the most important and relevant interactions for conservation management 126 (Drossel Barbara & McKane Alan J., 2005).

127 The paucity of information on the strength of interactions between the species in the network128 makes analysing it particularly challenging. Hence, throughout our analysis we only use directional

- 129 knowledge of species interactions whether a species has a positive or negative affect on another –
- 130 and three pieces of information about species impacts (expert opinion of Sarah Legge, Caitlyn Pink
- 131 and Rosalie Wilacy):
- 132 1) The negative effect of cats on rats is bigger than the positive effect of thrushes on cats;
- 133 2) Fruit resources (canopy) have a larger positive effect on flying foxes than flying foxes have a
- 134 positive effect on cats;
- 135 3) Brown boobies have a larger positive effect on cats than on rats.
- 136 Given the large uncertainties, FCM is an appropriate way to proceed.



137

Figure 1: Interaction network for the Christmas Island case study (reproduced from Han (2016)). The species are represented by nodes of invasive (red) and native species (blue). The grey nodes represent resources on the island. Links between species are displayed by solid (direct links) and dashed arrows (uncertain links). For the analysis in this paper, we assume that the uncertain links exist. The pointy end of an arrow indicates the species that receives a benefit from this interaction, the round end indicates a species that is harmed by the interaction.

145 FCM method

146 A FCM map consists of *nodes* representing species or other entities, which are connected by *edges*,

147 representing the interactions between the nodes. The value of each node is typically restricted to be

between 0 and 1, and the interactions strengths are between -1 and 1. A positive value means that a

node has a positive impact on the target node, and a negative value shows a detrimental impact.

150 Self-interactions are generally set to 0, though they can be set to be non-zero (Hobbs et al., 2002;

151 Özesmi & Özesmi, 2004; Steven A. Gray et al., 2015). While predator-prey interactions are common,

this framework allows for all types of interaction including commensalism, mutualism and

153 competition (Herr et al., 2016). For example, to model mutualism between species *i* and *j*, the

154 interactions $a_{i,j}$ and $a_{j,i}$ would both be made positive.

The value of each node is stored in a *state vector*, **n**, and the edge weights are stored in a matrix, **A**. The interaction effect of node *j* on node *i* is a_{ij} . For example, if $a_{ij} = -0.5$, then species *j* is having a negative impact on species *i*. The *state* of each node is given by the sum of all the interaction strengths, multiplied by the node value (see *Translating knowledge into FCMs* for further discussion about interactions). In maps representing interactions between species, the node value is some measure of the abundance of the species associated with that node, and the edges represent the per-capita influence on each other.

$$\boldsymbol{n} = f(\boldsymbol{A}\boldsymbol{n}). \tag{1}$$

The function *f* is the *activation function*. This function maps all states to values between 0 and 1, representing the minimum and maximum value for each node. While the true minimum and maximum abundance could be used, if known, FCMs are best used when in the absence of detailed information, (e.g. carrying capacities). If detailed knowledge is known, one should consider using a more mechanistic model. While there are a range of functions that have been used in the FCM literature, by far the most common is a logistic function:

$$f(x) = \frac{1}{1 + e^{-\lambda x}},\tag{2}$$

168

169 where λ defines the shape of the curve. Typically λ is set to one, although other values have been 170 explored. The choice of activation function has a major influence on results; this is discussed further 171 in the Activation function section below. For a given set of interactions, A, we solve for the 172 equilibrium state by searching for the vector, \boldsymbol{n} , which satisfies equation (1). There are a range of 173 ways to do this (see Supporting Information S2 for details). Once equilibrium has been obtained, we 174 can simulate a management action by adding or removing nodes, by fixing the value of a certain node (eradicating species I would mean fixing $n_i = 0$), or changing interactions. Once we do this, 175 176 we can solve equation (1) again to get the new state of every node and compare it to the original 177 state to see the effect of management (see Supporting Information S3 for details). 178 In the following sections, we propose three modifications for FCMs. The first addresses model 179 uncertainty, the second considers the distinction between the effect strength and interaction

180 strength, while the third modification relates to the choice of activation function.

181 Model uncertainty

182 Since we have no information about the strength of most interactions, we generate every 183 interaction (elements of A) from a uniform distribution between 0 and 1 or -1 to 0, depending on 184 whether it is a positive or negative interaction, respectively. From this distribution, we draw 100,000 185 parameters (discarding parameter combinations that do not satisfy any post-hoc constraints, as 186 discussed in the following section). We refer to each randomly drawn matrix A that passes all model 187 constrains as a parameter set. For each of these 100,000 parameter sets, we then simulate two 188 management actions: 1) cat control and 2) cat and rat control, comparing the current state to the 189 state after the management interventions. For each parameter set, we store the relative change in 190 each species' state to obtain a distribution of change for each species across the 100,000 parameter

191 sets – a standard approach in common network modelling procedures in conservation (Raymond,

192 McInnes, Dambacher, Way, & Bergstrom, 2011; Baker, Gordon, & Bode, 2016).

193

194 Translating knowledge into FCMs

195 The difference between the *effect strength* and the *interaction strength* is somewhat subtle, yet 196 important distinction. The interactions strengths – the elements of A in the model – define how 197 nodes in the network interact with each other. These per-capita interactions do not vary with the 198 state. The *effect strength*, however, is the actual impact of one node on another: it is the product of 199 the interaction strength and the state and it actually emerges from the model. For example, 200 suppose there were 3,000 cats on an island; the impact of the cats on the bird population is the 201 effect strength. If there were 30,000 cats the effect strength would increase, or if there were only 202 300 cats, the effect strength would be much smaller. In essence, the effect strength incorporates 203 abundances, and it is what is often observed in the field. In contrast, interaction strengths are 204 independent of the abundance; in this example, they would model the impact of a single cat on the 205 bird population. In our framework, we assume that the impact does not change depending on how 206 many other cats there are. Precisely how the effect of one species on another changes with 207 abundance is known as a functional response, and there are a range of ways they are represented in 208 the ecological literature (Holling, 1959; Liu & Tan, 2007). In this paper, the model is a Type 1 209 interaction. Whatever functional response is used, there must be a clear distinction about whether 210 observations correspond to innate aspects (i.e. the interaction strength) or emergent properties (i.e. 211 the effect strength) of the model.

This raises a problem because the model requires interactions strengths, which are notoriously
difficult to estimate (Dambacher et al., 2003; Baker, Bode, & McCarthy, 2016), while effect
strengths, which are much easier to estimate and observe, cannot be directly included in the model.
Despite this problem, many studies ask experts to estimate effect strengths and use them as

interaction strengths (eg Pacilly, Groot, Hofstede, Schaap, & Bueren, 2016; Game et al., 2017). In
fact, we are not aware of any FCM study with expert knowledge that has not done this. As the effect
strength emerges from the model, it is entirely possible that a node that has a 'low strength', could
actually have a relatively large effect in the model, if entered as an interaction strength rather than
effect strength.

221 The three pieces of information about the Christmas Island interactions are all about effect 222 strengths. We include them in the model as *post-hoc* constraints, i.e., for any candidate model, we 223 calculate the effect strength of each interaction to ensure that the model is consistent with our post-224 hoc constraints. For example, for each random realisation of A, we multiply the cat state by the 225 interaction strength of cats on rats and compare that to the product of the state of thrushes and the 226 interaction strength of thrushes on rats. If the magnitude of the latter is greater than the magnitude 227 of the former, we deem the parameter set unviable and discard it. We repeat this for each of the 228 three post-hoc constraints, only allowing the parameter set if it satisfies each post-hoc constraint.

229 Activation function

The choice of the activation function is crucial to the overall results. The commonly used logistic function (Eq. 2) contains the (shape) parameter, λ , which is usually set equal to 1, but other values have been used (Buruzs, Hatwágner, & Kóczy, 2015). An informed choice for λ is critical because changing its value influences the results (Supporting Information S4). Below we suggest a structured way for choosing its value.

The maximum or minimum values of states are restricted by λ and the number of interactions, the latter is itself limited by the number of nodes. We suggest choosing λ such that the maximum allowable state for a node with an average number of interactions is p. The average number of interactions, I_n , is the number of non-zero elements of A, divided by the number of nodes. Hence, we choose λ to satisfy the following equation:

$$\frac{1}{1+e^{-\lambda l_n p}} = p,$$

241 which leads to:

242
$$\lambda = \frac{1}{I_n p} \log\left(\frac{p}{1-p}\right).$$

There is no 'correct' choice for *p*, but we suggest choosing reasonably high values. We draw it randomly for each parameter set from between 0.9 and 0.9999 using the following equation

245
$$p = 1 - 0.1^Z$$
,

246 where $Z \sim unif(1,4)$. Choosing λ in this way ensures that we account for uncertainty in a parameter 247 which is inherently arbitrary.

248 Results

249 Christmas Island

250 We use our FCM method to analyse the effect of i) cat removal and ii) cat and rat removal on the 251 Christmas Island ecosystem. We draw random parameter sets, which each conform to the network 252 structure (Figure 1). We filter out any that don't satisfy the three post-hoc constraints and continue 253 drawing until we reach 100,000 that are acceptable. For each parameter set, we record the 254 percentage change in the abundance of each species when removing cats, and when removing cats 255 and rats (Figure 2). The removal of cats alone has a moderate benefit for many species. However, 256 the subsequent release of rats has a slight negative impact on nocturnal insects and fruit resources. 257 Removing cats and rats together has much greater positive impact on most species. In this case, the 258 only clear loser are kestrels, likely due to the loss of prey.





Figure 2: Percentage median abundance change for each node following cat control (maroon) or cat
 and rat control (green). The error bars represent the 5th and 95th percentiles across the 100,000
 parameter sets.

263 To analyse the confidence in an increase or a decrease of a species' abundance following

264 management, we investigated how frequently species increased in the parameter sets (Figure 3).

265 This indicates that birds of prey (goshawks and hawk owls) are less likely to increase when both

266 invasives are managed as compared to cat control alone, while the opposite is true for all other

267 species.





Figure 3: The percentage of simulations in which a species increases following cat control (maroon)
 or cat and rat control (green) across the 100,000 realisations. A bar at 0 means that this species
 never increased, while if the bar is at 100, it means that the species increased in every simulation.
 The error bars are calculated by resampling the model output with replacement 1,000 times, with

each sample containing 10,000 model outputs. We calculate the frequency of increase for each
sample, and the error bars show the 5th and 95th percentile.

275 Post-hoc constraints

285

276 In our Christmas Island analyses we included three post-hoc constraints. Adding these post-hoc 277 constraints increases the computational time of doing the analysis. To better understand how 278 computational time scales with the number of post-hoc constraints, we considered a further seven 279 arbitrary post-hoc constraints and reran the analysis using zero to ten post-hoc constraints (see 280 Supporting Information S5 for details). We find that the model runs quickly with only a few post-hoc 281 constraints, adding additional constraints increases computational time approximately exponentially 282 (Figure 4). On a typical computer, drawing 100,000 parameter sets can be done within an hour for 283 up to five post-hoc constraints. However, increasing this to ten post-hoc constraints increases 284 computational time to around two days.





are accepted. The bottom plot shows the approximate computational time for drawing 100,000
 acceptable parameter sets, running MATLAB on a computer with a 2.7GHz processor.

291

292 Discussion

293 In this paper, we have presented a way of altering FCM analysis to include expert knowledge of 294 interactions and deal with parameter uncertainty. It is vital that uncertainty is modelled in 295 conservation, and FCMs cognitive maps are no exception. We applied our FCM analysis to a species 296 interaction network from Christmas Island to predict how feral cat and black rat management will 297 affect the ecosystem. Despite large uncertainties in the system, we still showed that the removal of 298 both species likely caused all other modelled species to increase, except for birds of prey, which may 299 suffer some declines following rat removal. Our findings indicate that the system dynamics are very 300 much a product of the network, and the precise interaction strengths are of lesser importance. 301 Beyond making predictions about the system, which can help determine what management actions 302 to take (removing cats vs removing cats and rats), it can inform future management of the system. 303 For instance, in our network, if cats and rats are removed, hawk owls may decline due to a loss of 304 food resources. Given this possibility, targeted monitoring could be implemented to track hawk owl 305 abundance and additional feeding could be a possibility.

306 While we have focused on how to represent expert knowledge of interactions in a FCM and how to 307 incorporate uncertainty, FCMs face other challenges relating to eliciting expert knowledge. While 308 guidance is available on how to elicit which nodes should be in a network (Prigent, Fontenelle, 309 Rochet, & Trenkel, 2008; Kermagoret, Levrel, Carlier, & Ponsero, 2016), eliciting effect strengths, 310 combining different expert opinions and conducting linguistic sensitivity analysis requires further 311 work. Adding post-hoc constraints reduces the probability that a randomly generated set of 312 interaction strengths will satisfy all post-hoc constraints, which increases the computational time 313 exponentially. Since effect strength can only be incorporated as a post-hoc constraint its estimation increases the computational difficulty of the analysis considerably. We suggest to only use effect
strengths when they are known with high certainty. As our results show, we can obtain consistent
results from little information.

317 If many effect strengths are being used in the model, we suggest that every interaction can be given 318 a qualitative strength indicator, for example weak, medium or strong. Then, for each parameter set, 319 it is required that all the weak interactions are smaller than the medium, which are in turn weaker 320 than the strong. Since the probability of generating suitable parameter sets becomes very small with 321 an increasing number of post-hoc constraints, two options exist to deal with this problem. Firstly, we 322 may allow for an error rate; for example, if 90% of the interactions are in the correct order (ie 90% of 323 the 'strong' effects are stronger than all of the 'moderate' effects), then it could be deemed a 324 suitable parameter set. This in itself can be seen as a way of incorporating linguistic sensitivity into 325 the analysis. Secondly, approaches akin to approximate Bayesian computation (Battogtokh, Asch, 326 Case, Arnold, & Schüttler, 2002; Beaumont, 2010) could help find suitable parameter sets. 327 Generating parameter sets and saving those that most closely meet the post-hoc constraints could 328 help to draw new parameters. This process is repeated until parameter sets that satisfy all post-hoc 329 constraints are obtained. Thirdly, experts can disagree about parameter values; for example, some experts might believe an interaction is strong, while others are convinced about it being medium. In 330 331 these circumstances, we suggest allowing that effect strength to be either medium or strong in the 332 model.

The increased computational time associated with adding constraints also leads to the question of how many simulations should be done. Fundamentally, this boils down to whether the results would change with more simulations. One way to tackle this is to resample the simulations with replacement, as we did in Figure 3, and compare how the results change between different subsamples of the simulations. In our case, we found almost no variation in the frequency of increase and thus we are confident that have done enough simulations. 339 Interpreting model results and understanding the limitations of FCMs is critical. In our case,

predictions of increase or decrease are incredibly consistent across simulations. However, for many species the potential range of abundance change is large. For these species, the only conclusion that we can reach is that the data is insufficient to give a precise prediction of abundance change. With this in mind, stakeholders can chose to accept the level of uncertainty when they are making decisions or they can chose to spend more time and resources to reduce uncertainty. For the latter, these models can help pinpoint the best way to spend those resources to reduce uncertainty most effectively.

347 FCMs have a range of weaknesses, including that they do not incorporate temporal dynamics and 348 that they are phenomenological. Lacking a temporal component, the model cannot predict how long 349 it will take to reach the new equilibrium state, or what path the system will take to get to the 350 equilibrium. This is important because initial observations of the system could differ from model 351 predictions - even if the equilibrium prediction of the model is accurate (Baker, Gordon, et al., 352 2016). This makes it harder for monitoring populations, since it is unclear what decision is to take 353 when a population initially decrease. For Christmas Island, understanding the timescale of recovery 354 requires more information, and managers would need to consider growth rates of species when 355 thinking about how long it would take to move to the new equilibrium. FCMs are designed to be 356 phenomenological, in the sense that we can use expert knowledge of a phenomenon (one node 357 impacts another node) to create a model. We do not have detailed quantitative information on 358 precisely how all the nodes interact (i.e., the mechanisms), and there is no clear way to incorporate 359 this kind of information if it were available. FCM simplifies complex interactions, and is suited to 360 study systems where detailed information is not available, yet, decisions must be made (Martin, 361 Nally, et al., 2012).

Our suggestions regarding the changes to the FCM methodology are not to give better 'results', but
help to make FCM into a more reliable methodology that properly handles uncertainty. As we have

364 described, actually setting accurate values for interactions parameters is incredibly difficult and, 365 particularly in these low-information situations, uncertainty will always exist. Using point estimates 366 of parameters can give results that are simple to communicate, but not explicitly accounting for the 367 uncertainty means those results give a false sense of certainty about the impact of management 368 (Baker, Bode, et al., 2016). Our methodology clearly shows the limits of what you can conclude from 369 a FCM in a specific situation. However, learning what we don't know isn't a dead-end – in fact it can 370 provide a clear path forward, illuminating the steps required to make an open and transparent 371 decision.

372 Conservation decision-making will always involve trade-offs and carry risks (Hirsch et al., 2011;

373 McShane et al., 2011). Networks of multiple interacting species, or different stakeholders exacerbate

this complexity. Mathematical modelling can help predict management outcomes, but any model is

375 only as good as its input data. Hence, it is vital that methods are updated to both translate expert

opinion into modelling frameworks and account for the large uncertainties that are present. If this is

377 done, FCMs can become an important decision-making tool.

378 Data Accessibility

- 379 Code to reproduce all of the results in this paper has been included as online supporting
- 380 information. https://doi.org/10.6084/m9.figshare.5674681

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553 S1: Literature search

554 We performed a literature search to get an indication of how use of fuzzy cognitive maps has

- changed through time in conservation and ecology, and to quantify the prevalence of sensitivity and
- uncertainty analysis in the field. We conducted the search using Web of Science on the 14th of
- 557 March, 2017. Our search criteria were:
- TOPIC: (fuzzy cognitive map*) AND TOPIC: (ecology OR environment* OR conservation) Timespan:
 1996-2017. Indexes: SCI-EXPANDED, SSCI, A&HCI, CPCI-S, CPCI-SSH, BKCI-S, BKCI-SSH, ESCI, CCREXPANDED, IC.
- 561 While this did not return every paper in conservation and ecology that has used fuzzy cognitive
- 562 maps, it does give an indication of change in use over time. This search returned 248 records, and
- we removed 161 records manually which, based on the title, clearly did not relate to our search
- 564 (many of which were from the education field, about e-learning environments). We then
- downloaded each of the remaining 87 articles and kept those which used fuzzy cognitive maps in an
- 566 environmental or conservation management context, or if they were explanations on how to use
- 567 fuzzy cognitive maps. We also recorded whether each article conducted any type of sensitivity or
- uncertainty analysis. The full list of articles is given in Supplementary Table S1. Following this, 50
- articles remained. 5 of these had a sensitivity or uncertainty analysis. There has been clear increase
- 570 fuzzy cognitive maps through time, although there has been no clear increase in the number of
- 571 papers conducting sensitivity or uncertainty analysis (Figure 1).
- 572



- Figure 5: The number of papers published in each year using fuzzy cognitive maps since 1997. The
 blue bars represent the number of papers, and the orange bars are the number of papers that
 included a sensitivity or uncertainty analysis.
- 577
- 578

579 S2: Solving for steady state

580 The equation

$$\boldsymbol{n} = f(\boldsymbol{A}\boldsymbol{n}) \tag{3}$$

is a non-linear equation, and as such, there is no direct method to solve it. Rather, iterative methods are used. The most common method is fixed point iteration. This is done by starting from an initial guess, n_0 , and iterating the following

$$\boldsymbol{n}_{i+1} = f(\boldsymbol{A}\boldsymbol{n}_i) \tag{4}$$

584 Until $|\mathbf{n}_{i+1} - \mathbf{n}_i| < \eta$, where η is a very small number, such as 10^{-6} . Another option is to use a 585 Gauss-Seidell scheme with the parameter $\omega < 1$:

$$\boldsymbol{n}_{i+1} = \omega f(\boldsymbol{A}\boldsymbol{n}_i) + (1-\omega)\boldsymbol{n}_i.$$
⁽⁵⁾

586 This alternative method can help convergence.

587 Apart from these two iterative methods, most scientific programming languages include numerical

588 methods for solving nonlinear equations that could be used. For example, the function 'fsolve' in589 MATLAB.

591 S3: Solving for equilibrium under management

- 592 There are three broad management situations that can be easily modelled using a FCM: node
- removal, node addition and node manipulation. The first two situations are easily solved. Adding or
- removing a node creates a new network, and to find the state of the new network, one would simply
- follow the procedure outlined in S2 for the new network. To run the analysis with node manipulation
- is a small extension. For example, from our case study, if we wanted to predict the effect of
- 597 suppressing cats by 50%, we would firstly calculate the equilibrium state of the system and store the
- 598 cat abundance. We would then fix cat abundance at 50% and solve Eq. (1) for all of the other node
- 599 values, given the fixed cat abundance.

600

602 S4: Activation function

603 The activation function can have a big impact on the results. Here, we show results from a simple

network (from Baker *et al.* 2016) to demonstrate this. We use a small network for this as it easier to

see differences between sets of results on a small network and because this is to demonstrate what
 the phenomenon is and that it can arise in real networks. This network is to help understand about

607 the role of dingoes in Australian ecosystems, and we show results the difference between network

- 608 nodes when dingoes are included, compared to when dingoes are absent, using a fuzzy cognitive
- 609 map. Rather than draw λ randomly, as we suggest, here we genereate results using three distinct
- 610 values to show what effect λ has on model outputs (Figure 2). The absolute change in the system
- 611 state varies dramatically with the value of λ .



612

620

613Figure 6: The percentage change in state for each node, after the introduction of the dingo to the614network for different values of λ . The circles show the median and the error bars depict the 5th and61595th percentile.

616 Next, instead of considering percentage change, we look at how frequently a node increased with

617 dingo introduction (Figure 3). We find that this is remarkably robust to changing λ . Hence,

618 predictions about whether nodes increase or decrease with management appear to be much more 619 robust, compared to predictions of the change in the state of nodes.



Figure 7: The frequency that nodes increase with the introduction of dingoes in the dingo network
 (Baker et al. 2016) across 10,000 parameter sets for varying values of λ.

624 **S5: Computational impact of post-hoc constraints**

- To test the computational burden of adding post-hoc constraints, we supplement the list ofChristmas Island post-hoc constraints to get a list of 10:
- 627 1) Cats have a bigger (negative) effect on rats than thrushes have a (positive) effect.
- Fruit resources (canopy) have a larger positive effect on flying foxes than flying foxes
 have a positive effect on cats; Thrushes are more strongly predated by rats than cats.
- 630 3) Brown boobies have a larger positive effect on cats than on rats.
- 631 4) Goshawks have a bigger impact on Tropicbirds than Rats do.
- 5) Insects (diurnal) have a bigger positive for Thrushes than on white eyes.
- 6) Fruit has a bigger positive impact on frugivorous birds than cats have negative impact634 on frugivorous birds,
- 635 7) Rats have a bigger impact on geckos than on insects.
- 636 8) Thrushes have a bigger impact on insects than white eyes do.
- 637 9) Cats benefit more from tropicbird than from gecko.

We emphasise that these are simply to test computational times, and are not representative ofChristmas Island.

- 640 We test the computation time to generate acceptable parameter sets for 0 through 10 constraints.
- 641 For each number of constraints, we generate 10,000 acceptable parameter sets. For each parameter
- 642 set, we also randomise which constraints are being used (e.g. if we are using four constraints, we
- randomly sample four from the above list each time). We only draw 10,000 parameter sets due to
- the computational time required, particularly with many constraints. For each number of parameter
- sets, we record the number of attempts were required to get 10,000 acceptable sets. To estimate
- the time required to generate 100,000 parameter sets, we divide the time to get 100,000 parameter
- sets with not constraints by the proportion of acceptable parameter sets for each number of
- 648 constraints.