1

Precision measurement of the first ionization potential of nobelium

2	P. Chhetri, ^{1, 2, *} D. Ackermann, ^{2, 3} H. Backe, ⁴ M. Block, ^{2, 5, 6} B. Cheal, ⁷ C. Droese, ⁸ Ch. E. Düllmann, ^{2, 5, 6} J. Even, ^{6, 9}
3	R. Ferrer, ¹⁰ F. Giacoppo, ^{2,6} S. Götz, ^{2,5,6} F.P. Heßberger, ^{2,6} M. Huyse, ¹⁰ O. Kaleja, ^{2,11,†} J. Khuyagbaatar, ^{2,6}
4	P. Kunz, ¹² M. Laatiaoui, ^{2,6} F. Lautenschläger, ^{1,2} W. Lauth, ² N. Lecesne, ³ L. Lens, ^{2,5} E. Minava Ramirez, ¹³
	A K Mistry 2,6 S Baeder 2,6 P Van Duppen 10 Th Walther 1 A Vakushey 2,6 and Z. Zhang 14
5	$\frac{1}{1}$
6	Institut fur Angewandte Physik, Technische Universität Darmstädt,
7	Schlossgartenstrasse 1, D-04289 Darmstaat, Germany
8	GSI Heimnoitzzentrum für Schwerionenforschung GmoH, Planckstrasse 1, D-04291 Darmstaat, Germany
9	Grana Accelerateur National a Ions Lourus, Da Henri Decquerei, DP 55027 - 14070 Caen Ceaex 05, France
10	Institut für Kernphysik, Johannes Gutenberg-Universität Mainz,
11	⁵ Institut für Kernshemie Johannes Cutenhera Universität
12	Fritz-Strassmann Weg 2 D-55128 Mainz Germany
14	⁶ Helmholtz-Institut Mainz, Staudingerweg 18, D-55128 Mainz, Germany
15	⁷ Department of Physics, Oxford Street, University of Liverpool, L69 7ZE Liverpool, UK
16	⁸ Institut für Physik, Universität Greifswald, Felix-Hausdorff-Strasse 6, D-17489 Greifswald, Germany
17	⁹ KVI-Center for Advanced Radiation Technology, Rijksuniversiteit Groningen,
18	Zernikelaan 25, 9747 AA Groningen, The Netherlands
19	¹⁰ KU Leuven, Instituut voor Kern- en Stralingsfysica, Celestijnenlaan 200D, B-3001 Leuven, Belgium
20	¹¹ Institut für Kernphysik, Technische Universität Darmstadt,
21	Schlossgartenstrasse 9, D-64289 Darmstadt, Germany
22	¹² TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia V6T 2A3, Canada
23	¹³ Institut de Physique Nucléaire Orsay, 15 rue Georges Clemenceau, 91406 Orsay, France
24	¹⁴ Institute of Modern Physics, Chinese Academy of Sciences, 509 Nanchang Rd., 730000 Lanzhou, China
25	(Dated: May 24, 2018)
26	One of the most important atomic properties governing an element's chemical behaviour is the
27	energy required to remove its least-bound electron, referred to as the first ionization potential. For
28	the heaviest elements, this fundamental quantity is strongly influenced by relativistic effects which
29	lead to unique chemical properties. Laser spectroscopy on an atom-at-a-time scale was developed and
30	applied to probe the optical spectrum of neutral nobelium near the ionization threshold. The first
31	ionization potential of nobelium is determined here with a very high precision from the convergence

of measured Rydberg series to be $6.62621 \pm 0.00005 \,\text{eV}$. This work provides a stringent benchmark for

state-of-the-art many-body atomic modelling that considers relativistic and quantum electrodynamic

effects and paves the way for high-precision measurements of atomic properties of elements only

To date, 118 chemical elements are known [1]. Their 58 36 chemical behaviour is mainly determined by the elec- 59 37 tronic configuration. This is subject not only to the $_{60}$ 38 Coulomb interaction, but, with increasing atomic num- 61 39 ber Z, also to large electron-electron correlations, quan-6240 tum electrodynamic (QED) effects as well as relativistic 63 41 effects. These relativistic effects influence the binding 64 42 energy of the valence electrons, thus the chemical prop-65 43 erties, as they cause a shrinking of s and $p_{1/2}$ electron 66 44 orbitals and change the screening of the Coulomb poten- 67 45 tial by the inner-shell electrons [2]. Currently, many- 68 46 body methods such as multi-configuration Dirac-Fock 69 47 (MCDF), relativistic coupled cluster (RCC) and config-70 uration interaction (CI) are employed to study these ef-71 49 fects [3–6]. This has motivated many gas- and liquid- 72 50 phase chemistry experiments, which could be performed 73 51 in the region of the heaviest elements [7–9]. The first 74 53 ionization potential (IP) represents the binding energy $_{75}$ 54 of the most weakly-bound electron of an atom. An ac- $_{_{76}}$ 55 curate determination of the IP provides a crucial test $_{77}$ 56 for our understanding of the electronic structure and the 57

available from heavy-ion accelerator facilities.

chemical properties of an element. According to the actinide concept put forward by G.T. Seaborg [10], the actinide series consists of 15 elements starting from actinium (Ac, Z = 89) and ending with lawrencium (Lr, Z = 103). To date, the IP of 12 elements in the actinide series has been determined using resonance ionization mass spectroscopy, Rydberg convergence and surface ionization techniques [11–17]. Lr is the heaviest element for which the IP has been experimentally determined using a surface ionization technique [17] with a precision of about 0.08 eV and potentially susceptible to unknown systematic effects. Laser spectroscopy offers a far greater precision, in the μeV regime, but its application to the heaviest elements is hampered by the absence of known atomic transitions and the need for element synthesis from nuclear fusion reactions utilizing large accelerator facilities.

Recently, we reported the development of a technique sensitive enough for laser spectroscopic studies of nobelium (Z = 102) on an atom-at-a-time scale [18]. While this marked a first foray of optical spectroscopy into the



FIG. 1. (a) Scan of the second-step excitation $\bar{\nu}_2$ in ²⁵⁴No. The first-step was fixed at $\bar{\nu}_1 = 29,961.457 \,\mathrm{cm}^{-1}$. Series 1 and 2 were measured at a argon gas pressure of 95 mbar. Series 3 was measured at a pressure of 65 mbar, to reduce the buffer gas collision induced quenching. (b) A selected Rydberg resonance proceeding from the intermediate state with Gaussian fits (solid lines) to the data. (c) Resonance ionization signal for delayed Rydberg excitation, series 1 (red points) and 3 (green points), proceeding via the intermediate states. The solid line indicates an exponential fit to the data with lifetime τ about 100 ns (series 1 and 2) and 5 ns (series 3). *Inset*, magnification of delayed ionization of series 3. The α -decay count rates are normalized to a primary beam current of 1 particle μ A.

118

region of the transfermium (Z > 100) elements by ad-100 79 dressing the difficulties mentioned above, an ambiguity¹⁰¹ 80 due to an inter-atomic quenching process in the nobelium¹⁰² 81 atom led to significant uncertainties for the element's IP_{103} 82 [18, 19]. Here we present the results of extended measure-104 83 ments that overcome these limitations of our previous¹⁰⁵ 84 work and which have greatly opened up the versatility of 106 85 the technique. Two complementary methods have since¹⁰⁷ 86 been developed, whereby excitation to Rydberg states108 87 (prior to ionization) proceeds (i) via the direct excita-109 88 tion from an intermediate atomic state, or (ii) following₁₁₀ 89 buffer gas collisional de-excitation to an intermediate ex-111 90 cited state. The first has now enabled the measurement¹¹² 91 of the IP of nobelium with a precision three orders-of-113 92 magnitude greater than that previously reported [18].114 93 For the second, we here exploit a complementary pro-115 94 cess to determine the electronic energy levels also when₁₁₆ 95 the ground state optical transition is forbidden. 117 96

⁹⁷ The experiment was performed behind the velo-¹¹⁹ ⁹⁸ city filter SHIP at GSI, Darmstadt, Germany [20].¹²⁰ ⁹⁹ The isotope ²⁵⁴No (half-life $T_{1/2} = 51$ s) was

produced in the complete-fusion evaporation reaction 208 Pb(48 Ca,2n) 254 No with a cross-section of 2 μ b [21]. The lead sulfide target had an average thickness of $470 \,\mu \mathrm{g/cm^2}$. The ⁴⁸Ca beam from the UNILAC accelerator exhibited a macro-pulse structure of 5 ms beamon and 15 ms beam-off period. The beam intensity at a projectile energy of $4.55 \, A \cdot \text{MeV}$ [22] was typically 0.7 particle μA (about 4×10^{12} particles per second). The beam was additionally gated in accordance with userdefined measurement cycles. The rate of fusion products delivered to the experiment was checked by a retractable position-sensitive 16-strip silicon detector placed at the focal plane of SHIP. The fusion products were separated from the primary beam by the velocity filter SHIP and thermalized inside an optical gas cell, filled with 95 mbar of ultra-high purity argon. A $3.5\,\mu\mathrm{m}$ thick aluminized Mylar entrance foil separated the optical cell from the high vacuum of SHIP. The thermalized fusion products that remained charged were collected on a tantalum filament of $125 \,\mu\text{m}$ diameter. After a collection time of 25 s [23], optimized for the half-life of 254 No, the incoming

beam was switched off for 5s during which the filament₁₇₇ 121 was pulse heated for 300 ms to about 1350 K in order to178 122 evaporate the collected fusion products as neutral atoms.179 123 The temperature of the filament was monitored by a fast₁₈₀ 124 infrared pyrometer (LumaSense, IMPAC IS 6 Advanced).181 125 A two-step photoionization process was then employed₁₈₂ 126 to ionize the atoms. The produced ions were trans-183 127 ported by electric fields onto a silicon detector where they₁₈₄ 128 were identified by their characteristic α -decay energy.₁₈₅ 129 The laser light was provided by two tunable dye lasers₁₈₆ 130 (Lambda Physik FL and LPD series) pumped by two₁₈₇ 131 excimer lasers with a 100 Hz repetition rate at 248 nm_{188} 132 and 308 nm, respectively. The dye laser pulses had a 133 pulse duration of 18 ns with a jitter of about 10 ns. The 134 wavelengths were continuously monitored with a wave-135 length meter (HighFinesse-Angstrom, WS/7-UVU) that₁₈₉ 136 was calibrated to an internal neon lamp. A more detailed₁₉₀ 137 description of the experimental setup and method can be₁₉₁ 138 found in refs. [24-26]. 139 192

A two-colour photon-excitation scheme was used to193 140 search for Rydberg states in ²⁵⁴No. We operated one dye₁₉₄ 141 laser at $\bar{\nu}_1 = 29,961.457 \,\mathrm{cm}^{-1}$ initiating in a first step the 142 ${}^{1}S_{0} \rightarrow {}^{1}P_{1}$ ground state transition [18] while another syn-143 chronized dye laser provided tunable light for the second 144 excitation step, $\bar{\nu}_2$. The atoms that were successfully 145 excited into a Rydberg state were subsequently ionized195 146 either by residual laser light, black-body radiation, or col-196 147 lisional processes. In total, a spectral range of the second₁₉₇ 148 excitation step from 23,000 to $23,650 \,\mathrm{cm}^{-1}$ was scanned₁₉₈ 149 to locate 29 Rydberg states. At a buffer gas pressure199 150 of 95 mbar two different series comprising 22 Rydberg₂₀₀ 151 states were identified as shown in Fig. 1 a (series 1 and₂₀₁ 152 2), significantly adding to those reported previously [18].202 153 However, in this previous work it could not be unambigu-203 154 ously determined from which state the second excitation₂₀₄ 155 step originated, due to the possibility that gas induced₂₀₅ 156 quenching (following excitation to the ${}^{1}P_{1}$ intermediate₂₀₆ 157 state) populates close-lying long-lived states. Reducing207 158 the buffer gas pressure to about 65 mbar, helped to ob-208 159 serve another series (series 3 in Fig. 1 a) with a sub-209 160 stantially reduced count rate. The lowest-lying Rydberg₂₁₀ 161 states from this series showed resolved multiplet struc-211 162 tures (Fig. 1 b), which can be attributed to different fine212 163 structure components. The splitting of the multiplets₂₁₃ 164 decreases with increasing principal quantum number. 215 165

In order to identify the state from which the sec-216 166 ond transition takes place, the α -signal at resonance₂₁₇ 167 was measured as a function of time delay between the₂₁₈ 168 two laser pulses. The first step was kept at $\bar{\nu}_1 =_{219}$ 169 $29,961.457\,\mathrm{cm^{-1}}$ populating the ${}^{1}\mathrm{P}_{1}$ state and the sec-220 170 ond step was set to excite a specific Rydberg state. This₂₂₁ 171 measurement allows us to probe the lifetime of the inter-222 172 mediate state which enables the disentanglement of the₂₂₃ 173 different Rydberg series (see Fig. 1 c). Members of one224 174 series (3) indicate a short-lived intermediate state with225 175 a lifetime of about 5 ns in agreement with the expecta-226 176

tions for the ${}^{1}P_{1}$ state. The intermediate state for the members of the other two series (1 and 2) has a longer lifetime of about 100 ns proving the involvement of an additional intermediate level populated by buffer gas induced quenching of the ${}^{1}P_{1}$ state.

In the data analysis of the individual resonances, we used a χ^2 -minimization routine to extract the relevant parameters. We determined the excitation energy of the Rydberg states from the centroids of single or multiple Gaussian fits to each resolved state or unresolved multiplet, respectively. The excitation energy of the Rydberg states follow a trend given by the Rydberg formula [27]

$$h\bar{\nu}_2(n) = h\bar{\nu}_{\rm lim} - R_m/(n - \delta(n))^2,$$
 (1)

where $h\bar{\nu}_{\text{lim}} = \text{IP} - \text{E}_{\text{interm.}}$ denotes the ionization limit for an intermediate state of energy $\text{E}_{\text{interm.}}$. h is the Planck constant, n is the principal quantum number of the valence electron and R_m is the reduced mass Rydberg constant for ²⁵⁴No. The quantum defect $\delta(n)$ can be parameterized by the Ritz expansion [28]

$$\delta(n) = \delta_0 + \sum_{i=1} B_i / (n - \delta_0)^{2 \cdot i},$$
(2)

where δ_0 and B_i are the fitting parameters. Figure 2 (upper panel) shows the position of all the observed peaks as a function of their principal quantum number (n). The assignment of n was obtained by restricting the quantum defect $\delta(n)$ between 0 and 1. However, this choice for $\delta(n)$ does not affect the results of our analysis. However, the result of the analysis is unaffected by this choice. The best fit according to Eq. (1) to the series associated with the Rydberg states proceeding from the $^1\mathrm{P}_1$ state converged to a value $\bar{\nu}_{\text{lim}} = 23,482.14 \pm 0.27 \,\text{cm}^{-1}$. The presence of the buffer gas induces a shift in the energy of the Rydberg states and thus in the extracted IP. Hence, after the correction arising from the pressure, which is about -0.0060(7) cm⁻¹/mbar for the homologue element ytterbium (Yb, Z = 70) [29], we obtain a first ionization potential for nobelium to IP = 53, 444.0 \pm 0.4 cm⁻¹ corresponding to $6.62621 \pm 0.00005 \,\text{eV}$. Predictions of the IP of nobelium using different theoretical models [4–6, 30] are given in Table I for comparison along with the experimental value obtained in this work.

The other two series (1 and 2), converged to a mean value of $\bar{\nu}_{\rm lim} = 23,792^{+1}_{-8} \,\rm cm^{-1}$ when taking higher-order corrections to the Ritz expansion (Eq. (2)) into account. Comparing the convergence limits of the series, it becomes clear that series 1 and 2 proceed from a state located about $310 \,\rm cm^{-1}$ below the ${}^{1}P_{1}$ state. A likely assignment for this level at an energy of $29,652^{+8}_{-1} \,\rm cm^{-1}$ is the ${}^{3}D_{3}$ state, predicted to be $159 \,\rm cm^{-1}$ [4] or $20 \,\rm cm^{-1}$ [5] below the ${}^{1}P_{1}$ state. Other lower-lying D-states are predicted to be more than $1000 \,\rm cm^{-1}$ below the ${}^{1}P_{1}$ state. The results have been summarized in Table I.



FIG. 2. Analysis of the Rydberg states. Top panel: the₂₅₇ position of all observed Rydberg states as a function of the₂₅₈ principal quantum number n. The Rydberg-Ritz formula, Eq.₂₅₉ 1, was fitted to the centre position of the peaks and the main peaks of the multiplets belonging to different n. The dashed²⁶⁰ lines indicate the convergence limits of the individual series.²⁶¹ Here, the gap between them corresponds to the energy differ-²⁶² ence between the intermediate (¹P₁ and ³D₃) states. *Inset*,²⁶³ effective level scheme for Rydberg excitation of ²⁵⁴No. Lower₂₆₄ panel: residuals of the fits. The uncertainty of the residu-₂₆₅ als includes the statistical uncertainty (1 σ) from the fit as²⁶⁶ well as the systematic uncertainties (1 σ) from the wavelength determination.

An assignment for each series can be obtained from²⁷⁰ 227 the quantum defect and by comparing our results for no-²⁷¹ 228 belium with literature values for Yb. Figure 3 shows²⁷² 229 the measured quantum defect $\delta(n)$ in Yb and No as a^{273} 230 function of the principal quantum number. The quan-274 231 tum defect values for Yb were calculated using the en-275 232 ergy levels from references [32, 33]. Series 1 and 2 in²⁷⁶ 233 No show a similar l-dependent quantum defect constant²⁷⁷ 234 δ_0 of about 0.9 and 0.1 as the np and nf series in Yb²⁷⁸ 235 (Fig. 3 left panel), respectively, and matches with the²⁷⁹ 236 expectation [34]. The quantum defects of series 1 fea-²⁸⁰ 237 ture a unique trend caused either by strong polarization²⁸¹ 238 effects or a strong perturbation probably due to the pres-²⁸² 239 ence of high-lying perturbing orbitals interfering with the²⁸⁸ 240 Rydberg series, similar to those observed for the np se-285 241 ries in Yb [33]. In the evaluation for extracting the IP_{286} 242 this can be treated perturbatively by using higher order₂₈₇ 243 corrections in the Ritz expansion given in Eq. (2). Series₂₈₈ 244 3, with $\delta_0 \approx 0.7$ is similar to the *nd* series in Yb. Based₂₈₉ 245 on these observations an assignment of np, nf and nd is₂₉₀ 246 proposed for series 1, 2 and 3, respectively. According₂₉₁ 247 to these observations, series 1 and 2 are likely to pro-292 248 ceed via a D-state, substantiating the assignment of the₂₉₃ 249 intermediate state. 294 250

In conclusion the observed high-lying Rydberg states $_{252}$ in nobelium enabled the determination of the first IP $_{296}$

TABLE I. Experimental values of the first IP of nobelium and energy of the $^{3}D_{3}$ level, compared with: IHFSCC, MCDF, CI + all orders.

Method	$IP (cm^{-1})$	${}^{3}\mathrm{D}_{3}~(\mathrm{cm}^{-1})$
Experiment (this work)	$53,444.0\pm0.4$	$29,652^{+8}_{-1}$
IHFSCC [4]	$53,\!489{\pm}800$	$29,\!897{\pm}800$
CI + all orders [5]	$54,\!390{\pm}1,\!100$	$30,\!183{\pm}1,\!100$
MCDF [6]	$53,701 \pm 1,100$	
Extrapolation [30]	$53,\!600{\pm}600$	

and the level-energy of the ${}^{3}D_{3}$ state with high precision. In general, we found a good agreement between the predictions and our results. In particular, the intermediate Hamiltonian Fock-space coupled-cluster (IHFSCC) and configuration interaction method combined with the linearized single-double coupled-cluster (CI + all order)calculations deviate by less than 2% from the experimental value for the IP. In the case of the ${}^{3}D_{3}$ state, the deviation is larger compared to other levels potentially due to correlation effects, underestimation of QED effects or both. Our values serve as a benchmark for the treatment of relativistic, QED and electron correlation effects in state-of-the-art calculations predicting atomic properties of the heaviest elements. Our measurements show that nobelium exhibits the highest measured first IP in the actinide series [11, 17]. In analogy to ytterbium, its lanthanide homologue, this corresponds to closed 5fand 7s atomic shells in nobelium. Experimental observations with the second, ionizing, laser excitation step delayed with respect to the first revealed that the Rydberg states are excited from two distinct intermediate atomic levels. This is in agreement with the observation of a fast quenching of the ¹P₁ state to a longer-lived state due to collisions of the excited atom with the buffer gas [19]. From the convergence of the Rydberg series the energetic position of this long-lived state was derived to be 310^{+1}_{-8} cm⁻¹ below the ¹P₁ state. Based on theoretical calculations and the analysis of the quantum defect, a term assignment as ${}^{3}D_{3}$ was made for this new state, inaccessible by direct laser excitation as the optical transition from the ground state is forbidden.

269

This work opens the door for forthcoming precision measurements of various atomic and nuclear properties of still heavier elements using laser spectroscopic techniques, for example the precise determination of the IP for Lr, where the question about the change in the ground-state electronic configuration of Lr, predicted to be $[\text{Rn}]5f^{14}7s^27p_{1/2}$ [35], in contrast to that of its lanthanide homologue lutetium (Lu), $[\text{Xe}]4f^{14}6s^25d$ can now be addressed. Finally, the ability to optically pump the atoms has the potential to make further transitions accessible, not least for the precise extraction of nuclear properties from isotope shifts and hyperfine structure.

Yb No Quantum defect, δ (mod 1) 1 1 nr 0.8 0.8 nd 0.6 0.6 0.4 0.4 ns 0.2 0.2 nf 0 0 40 50 0 10 20 30 10 20 30

Principal quantum number, n

FIG. 3. Quantum defect values for Yb (left panel) and No (right panel). The quantum defects of the three Rydberg series in No and the ns (hollow squares), np (solid triangles), nd (solid spheres) and nf (solid squares) series in Yb are plotted as a function of the principal quantum number n.

343

344

345

346

347

We thank the staff of the GSI ion source and accel-325 297 erator for preparing the stable ⁴⁸Ca beam as we are³²⁶ 298 grateful to the staff of the target lab for providing³²⁷ 299 high-quality lead targets. We acknowledge the techni-³²⁸ 300 high-quality lead targets. we acknowledge the technical support of J. Maurer, H.-G. Burkhard, D. Racano, $_{330}^{329}$ 301 L. Braisz, D. Reemts and I. Kostyuk. This work was_{331} 302 supported by the German Federal Ministry of Research₃₃₂ 303 under contracts 06MZ169I, 06LM236I, FAIR NuSTAR333 304 05P09RDFN4, 05P12RDFN8, and 05P15RDFN1; by the³³⁴ 305 GSI; and by the Helmholtz Association. This project has³³⁵ 306 also received funding from the European Union $\operatorname{Horizon}^{\scriptscriptstyle 336}$ 307 2020 research and innovation programme under the grant³³⁷ 1002 (DNG 4 D2) D 4 1338308 agreement no. 654002 (ENSAR2). D. A. is supported₃₃₉ 309 by the European Commission in the framework of CEA_{-340} 310 EUROTALENTS 2014-2018 (noPCOFUND GA 2013 -341 311 600382). 342 312

- ³¹³ * P.chhetri@gsi.de
- [†] Present address: Max-Planck-Institut für Kernphysik,³⁴⁸
 69120 Heidelberg, Germany.
- ³¹⁶ [1] L. Öhrström and J. Reedijk , Pure Appl. Chem. **88** (12), $^{350}_{351}$ ³¹⁷ 1225 (2016).
- ³¹⁸ [2] P. Schwerdtfeger *et al.*, Nucl. Phys. A **944**, 551 (2015). ³⁵²
- ³¹⁹ [3] P. Indelicato *et al.*, Eur. Phys. J. D **45**, 155 (2007).
- ³²⁰ [4] A. Borschevsky *et al.*, Phys. Rev. A **75**, 042514 (2007). ³⁵⁴
- ³²² [6] Y. Liu *et al.*, Phys. Rev. A **76**, 062503 (2007).
- ³²³ [7] A. Türler and V. Pershina, Chem. Rev. **113**, 1237 (2013)³⁵⁷
- ³²⁴ [8] Y. Nagame *et al.*, Nucl. Phys. A **944**, 614 (2015).

- [9] A. Türler et al., Nucl. Phys. A 944, 640 (2015).
- [10] G. T. Seaborg, Science **104**, 379 (1946).
- [11] K. Wendt et al., Hyperfine Interact. 277, 55 (2014).
- [12] E. Worden et al., Opt. Soc. Am. B 10, 1998 (1993).
- [13] E. Worden and J. Conway, J. Opt. Soc. Am. 69, 733 (1979).
- [14] A. Coste et al., J. Opt. Soc. Am. 72, 103 (1982).
- [15] N. Erdmann et al., J. Alloys Compd. 271, 837 (1998).
- [16] J. Roßnagel et al., Phys. Rev. A 85, 012525 (2012).
- [17] T. K. Sato *et al.*, Nature **520**, 209 (2015).
- [18] M. Laatiaoui et al., Nature 538, 495 (2016).
- [19] P. Chhetri et al., Eur. Phys. J. D 71, 195 (2017).
- [20] S. Hofmann and G. Münzenberg, Rev. Mod. Phys. 72, 733 (2000).
- [21] Yu.Ts. Oganessian *et al.*, Phys. Rev. C **64**, 054606 (2001).
- [22] M. Leino et al., Eur. Phys. J. A 6, 63 (1999).
- [23] M. Laatiaoui et al., Eur. Phys. J. D 68, 71 (2014).
- [24] H. Backe et al., Eur. Phys. J. D 45, 99 (2007).
- [25] F. Lautenschläger et al., Nucl. Instrum. Methods B 383, 115 (2016).
- [26] M. Laatiaoui et al., Hyperfine Interact. 227 69 (2014).
- [27] V. S. Letokhov, *Laser Photoionization Spectroscopy* (Academic Press, 1987).
- [28] T. F. Gallagher, *Rydberg atoms* (Cambridge University Press, Cambridge, 1994).
- [29] P. Chhetri *et al.*, Acta Physica Polonica Series B 49, 599 (2018).
- [30] J. Sugar, J. Chem. Phys. 60, 4103 (1974).
- [31] M. J. Seaton, Proc. Phys. Soc. (London) 88, 801 (1966).
- [32] P. Camus, A. Débarre and C. Morillon, J. Phys. B: 13, 1073 (1980).
- [33] M. Aymar et al., J. Phys. B: 17, 3645 (1984).
- [34] U. Fano, C. E. Theodosiou and J. L. Dehmer, Rev. Mod.

359

Phys. 48, 49 (1976)[35] A. Borschevsky *et al.*, Eur. Phys. J. D 45, 115 (2007). 360