

State Feedback Predictive Control for Non-linear Hydro-turbine Governing System

Journal:	<i>Journal of Vibration and Control</i>
Manuscript ID	JVC-17-0562
Manuscript Type:	Original Manuscript
Date Submitted by the Author:	14-Aug-2017
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Keywords:	State feedback predictive control, T-S fuzzy model, hydro-turbine governing system, non-linear dynamics, stability
Please select up to 5 subject areas that best reflect the content of your manuscript:	Fundamental dynamics, Modeling, Structural control/vibration mitigation, Non-linear dynamics , Analytical methods, Control theory
Abstract:	The present work introduces a novel predictive control strategy for the analysis of the dynamic performance of hydro-turbine governing systems based on fuzzy logic. Firstly, a six-dimensional non-linear dynamic model of the system is defined. The defined model is applied to a realistic case-study, aiming to investigate the dynamic behavior of the system. In order to deal effectively with the non-linearity of the system under study, the T-S fuzzy approach is adopted. The results demonstrated through the use of the discrete Lyapunov function and Schur complements of matrices suggest that the closed-cycle control system can achieve a global asymptotic stability state. The second part focuses on the quantification of the impact of sudden changes in operating conditions on the overall performance. The numerical results indicate that proposed predictive control method can ensure the performance of the system to be reliable and robust to external inferences. In addition to this, the approach proposed has unquestionable advantages over the traditional PID and model predictive controllers with regard to non-linear systems applications.

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Manuscripts

For Peer Review

Dear Editor *Valder Steffen Jr.*

Thank you for the reviewer's useful comments on our manuscript. We have meticulously read your ideas, and revised the manuscript accordingly. We reply your comments item by item as follows.

Reviewers' Comments to Author:

Reviewer#: 1

Comments to the Author

Title: State Feedback Predictive Control for Non-linear Hydro-turbine Governing System

Journal Name: Journal of Vibration and Control

The organization of this paper is suitable and mathematical proofs are clear. I think that this paper should be revised carefully. I suggest the following comments:

- 1- The novelty of the proposed method should be highlighted carefully.
- 2- The authors should polish the paper suitably.
- 3- In the simulation sections, the proposed control technique is performed to show the control performance without any comparisons with existing methods. There are no numerical simulation results, which can demonstrate the superiority of the proposed control law. I suggest comparing the simulations with the results of the recent (2016 or 2017) related valid references.
- 4- The state of the art is incomplete and the literature review in the introduction section about state feedback should be improved by adding some references as follow:
 - Synchronization of a class of uncertain chaotic systems with Lipschitz nonlinearities using state-feedback control design: A matrix inequality approach; Asian Journal of Control.
 - Composite nonlinear feedback control technique for master/slave synchronization of nonlinear systems; Nonlinear Dynamics.
 - Optimal LMI-based state feedback stabilizer for uncertain nonlinear systems with time-varying uncertainties and disturbances; Complexity.
 - An LMI-based robust tracker for uncertain linear systems with multiple time-varying delays using optimal composite nonlinear feedback technique; Nonlinear Dynamics.

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3 - Robust tracking controller for multivariable delayed systems with input saturation
4 Nonlinear via composite nonlinear feedback; Nonlinear Dynamics.
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6 5- The importance of the problem considered in this paper should be further
7 addressed.
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9 6- The directions to further and improve the work should be added as future
10 recommendation section after 'conclusions' section.
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15 1- The novelty of the proposed method should be highlighted carefully.
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18 √ Many thanks for the reviewer's advice. To highlight the novelty of the proposed
19 method, we have provided a detailed description of the innovations in the fourth
20 paragraph of the introduction. Correspondingly, the contents are 'Inspired by what has
21 been discussed above, there are four innovations of this paper which make the
22 proposed method more appealing compared with previous works. This study firstly
23 consists of the definition of a six-dimensional nonlinear dynamic model for the HTGS,
24 which provides an accurate representation of real systems. The second innovation is
25 the state feedback predictive control of HTGS applied in T-S fuzzy model, which
26 makes the global output of the HTGS model have good mathematical expression
27 characteristics. Thirdly, the SFPC that has both output feedback and state feedback
28 circuits to guarantees the efficient feedback correction of control system as the output
29 feedback channel is disconnected. Finally, the dynamic feedback structure composed
30 by measured state variables of control system that can be able to inhibit the
31 unpredictable interference in advance.'
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- 43 2- The authors should polish the paper suitably.
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46 √ Thanks a lot for the reviewer's advice. Firstly, the co-authors including Prof.
47 Edoardo Patelli and Dr. Silvia Tolo who work at University of Liverpool in UK have
48 tried their best to revise the English of the paper. Secondly, all of our authors have
49 reorganized and double-checked this paper. Now, we believe that this paper could
50 meet the high requirements of *Journal of Vibration and Control*.
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- 56 3- In the simulation sections, the proposed control technique is performed to show
57 the control performance without any comparisons with existing methods. There are
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no numerical simulation results, which can demonstrate the superiority of the proposed control law. I suggest comparing the simulations with the results of the recent (2016 Or 2017) related valid references.

√ Thanks a lot for the reviewer's good comments. A comparative analysis regarding the nonlinear model predictive control (MPC), the PID and the T-S SFPC method proposed in the paper has been added in **Case 6**, which are

'Case 6: Comparison including the MPC, the PID and the T-S SFPC approach

In order to validate the T-S SFPC method proposed in the paper compared with MPC (Diehl et al., 2002 and 2005; Kunisaki et al., 2008; Kirches et al., 2012; Lopez-Negrete et al., 2013; Jaschke et al., 2014; Otsuka et al., 2017; La et al., 2017) and the PID (Ntogramatzidis et al., 2011) methods, a comparative analysis is therefore performed. Here, the PID controller by Ntogramatzidis in the system (39) is expressed as:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = x_3 \\ \dot{x}_3 = -a_0x_1 - a_1x_2 - a_2x_3 + y \\ \dot{\delta} = \omega_0\omega \\ \dot{\omega} = \frac{1}{T_{ab}} \left[m_t - \frac{E'_q V_s}{x'_{d\Sigma}} \sin \delta - \frac{V_s^2}{2} \frac{x'_{d\Sigma} - x'_{q\Sigma}}{x'_{d\Sigma} x'_{q\Sigma}} \sin 2\delta - D\omega \right], \\ \dot{y} = \frac{1}{T_y} (-k_p(r - \omega) - \frac{k_i}{\omega_0} \delta - k_d D^q \omega - y) \end{cases} \quad (41)$$

where k_p, k_i and k_d are PID parameters. The parameters are $k_p = 2.0$, $k_i = 1.0$ and $k_d = 2.0$, $q = 1$.

The initial assumption for the reference solution is $Y_s = [0, 0, 0]^T$. Then, numerical results of MPC, PID and T-S SFPC are shown in **Fig. 9**.

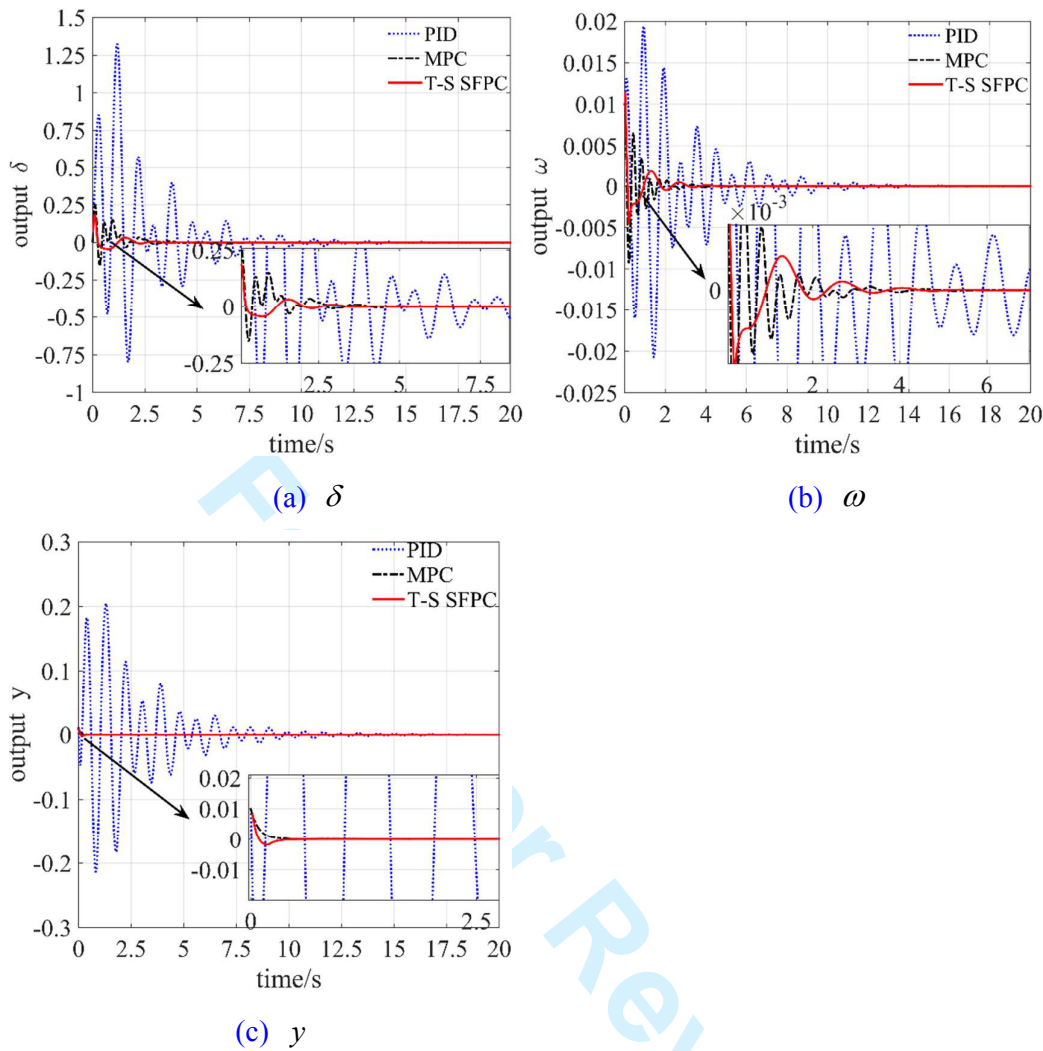


Figure 9. Comparison of control performance obtained with MPC, PID and T-S SFPC approaches; (a) δ (b) ω (c) y

Table 1 Adjusting time of the HTGS under MPC, PID and T-S SFPC controllers

	δ			ω			y		
	PID	MPC	T-S SFPC	PID	MPC	T-S SFPC	PID	MPC	T-S SFPC
T/s	16.6	4.8	3.6	16.1	5.8	4.5	16.5	0.5	0.5

The performance results associated with the PID, MPC and T-S SFPC are shown in **Fig. 9** and **Table 1**. It is obvious that the state feedback predictive controller proposed in this paper allows providing better performance for non-linear hydropower system than both PID and MPC. As highlighted in Table 1, compared with MPC, the T-S SFPC can enable the adjusting time of both outputs δ and ω to shorten by 25%

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3 and 22.4%. Furthermore, the fluctuations of the state feedback predictive control
4 method are smaller than those registered for PID and MPC controllers. This implies
5 that the T-S SFPC method is more efficient than the traditional PID approach and
6 MPC in monitoring and acting on the state of the hydropower station on a real-time
7 scale. Thus, the T-S SFPC enjoys an excellent performance in control of the nonlinear
8 hydropower system.
9

10 We have added the correspondingly literatures in reference section, i.e.,

11 Diehl M, Findeisen R, Allgower F, Bock HG, et al. (2005) Nominal stability of
12 real-time iteration scheme for nonlinear model predictive control. *IEE
13 Proceedings-Control Theory and Applications* 152:296-308.

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19 Kirches C, Wirsching L, Bock HG, et al. (2012) Efficient direct multiple shooting for
20 nonlinear model predictive control on long horizons. *Journal of process control*
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22 Kunisaki C, Makino H, Akiyama H, et al. (2008) Predictive factors for anastomotic
23 leakage in the neck after retrosternal reconstruction for esophageal cancer.
24 *Hepato-Gastroenterology* 55:98-102.

25 Lopez-Negrete R, D'Amato FJ, Biegler LT, et al. (2013) Fast nonlinear model
26 predictive control: Formulation and industrial process applications. *Computers &
27 Chemical Engineering* 51:55-64.

28 La HC, Potschka A and Bock HG (2017) Partial stability for nonlinear model
29 predictive control. *Automatica* 78:14-19.

30 Otsuka S, Uono S, Yoshimura S, Zhao S, et al. (2017) Emotion perception mediates
31 the Predictive relationship between verbal ability and functional outcome in
32 High-functioning adults with autism spectrum disorder. *Journal of Autism and
33 Developmental Disorders* 47:1166-1182.'

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follow:

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4 nonlinearities using state-feedback control design: A matrix inequality approach;
5 Asian Journal of Control.
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8 - Composite nonlinear feedback control technique for master/slave synchronization
9 of nonlinear systems; *Nonlinear Dynamics*.
10
11 - Optimal LMI-based state feedback stabilizer for uncertain nonlinear systems with
12 time-varying uncertainties and disturbances; *Complexity*.
13
14 - An LMI-based robust tracker for uncertain linear systems with multiple
15 time-varying delays using optimal composite nonlinear feedback technique;
16 *Nonlinear Dynamics*.
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18 - Robust tracking controller for multivariable delayed systems with input saturation
19 via composite nonlinear feedback; *Nonlinear Dynamics*.
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25 √ Thanks for the reviewer's guidance. In order to improve the readability of this paper,
26 we have added some references about the research progress of state feedback in
27 introduction, the relevant references are as follow:
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29 'Mobayen S and Tchier F (2017) Synchronization of a class of uncertain chaotic
30 systems with Lipschitz nonlinearities using state-feedback control design: A matrix
31 inequality approach. *Nonlinear Dynamics* 20: 1-15.
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33 Mobayen S and Tchier F (2017) Composite nonlinear feedback control technique for
34 master/slave synchronization of nonlinear systems. *Nonlinear Dynamics* 87:
35 1713-1747.
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38 Mobayen S (2016) Optimal LMI-based state feedback stabilizer for uncertain
39 nonlinear systems with time-varying uncertainties and disturbances. *Complexity* 21:
40 356-362.
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43 Mobayen S (2015) An LMI-based robust for uncertain linear systems multiple
44 time-varying delays using optimal composite nonlinear feedback technique.
45 *Nonlinear Dynamics* 80: 917-927.
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48 Mobayen S (2014) Robust tracking controller for multivariable delayed systems with
49 input saturation via composite nonlinear feedback. *Nonlinear Dynamics* 76:827-838.'
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55 5- The importance of the problem considered in this paper should be further
56 addressed.
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3 √ Many thanks for the reviewer's comments. We have comprehensively discussed the
4 importance of the problem considered in this paper, and this topic has also been
5 further addressed.
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8 Firstly, to make this issue clearer, the corresponding contents regarding the
9 importance of the study have been rewritten in introduction, which are 'This high
10 degree of uncertainty and random disturbance have the potential to significantly
11 increase the risks of generator swing and network-disconnecting, it is therefore
12 important to predict the dynamic performance of HTGS. In light of this, implementing
13 a new theoretical and computational tool that is able to fully capture such the
14 uncertainty interference is particularly important (Mahmoud et al., 2005; Donaisky et
15 al., 2015).'

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17 To address the topic mention above, the current research focuses on an approach
18 of the state feedback predictive control for hydraulic-turbine governing systems
19 (HTGS). This method combines the control optimization of non-linear hydro-turbine
20 governing systems with the T-S fuzzy model, which provides the modelling of
21 non-linear systems with arbitrary parameters precision. As a result, this method can
22 effectively control the problems of model mismatch and external disturbance in
23 system by real-time state feedback, and improves the robustness and anti-interference
24 of the HTGS. The proposed method (i.e., T-S SFPC method) and innovations in this
25 paper are clearly clarified in the fourth paragraph of the introduction.
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38 6- The directions to further and improve the work should be added as
39 future recommendation section after 'conclusions' section.
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43 √ Thanks for the reviewer's good advice. We have added the future research direction
44 of this work in the final part of the conclusion, and the added contents are 'Future
45 research work will focus on how to solve the problem of predictive control
46 optimization for high-dimensional systems with input constraints and state delays via
47 intelligent optimization algorithms.'
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52 **Reviewer#: 2**

53 Comments to the Author
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56 In the submitted manuscript, the authors introduced a novel predictive control
57 strategy for the analysis of the dynamic performance of hydro-turbine governing
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3 systems based on fuzzy logic. They also showed that the proposed approach has
4 unquestionable advantages over the traditional PID controllers with regard to
5 non-linear systems applications. However, there exists a number of practical MPC
6 schemes where the problem can be solved on-line by optimization routines that are
7 based on numerical algorithms. The whole category of direct methods for the optimal
8 control is well suited for such problems and real-time feasible algorithms have been
9 developed over the past years. See e.g. the work by Bock, Diehl, Otsuka, Biegler, etc.
10 I would like to see the performance of the proposed predictive control strategy in
11 comparison with the recent MPC algorithms instead of the traditional PID controllers.
12 Comparing the results with those of the traditional PID controllers is not enough to
13 show the superiority of the proposed predictive control strategy.
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23 √ Thanks a lot for the reviewer's good comments. A comparative analysis regarding
24 the nonlinear model predictive control (MPC), the PID and the T-S SFPC method
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28 **‘Case 6: Comparison including the MPC, the PID and the T-S SFPC approach**

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32 and the PID (Ntogramatzidis et al., 2011) methods, a comparative analysis is therefore
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53 and $k_d = 2.0$, $q = 1$.
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56 The initial assumption for the reference solution is $Y_s = [0, 0, 0]^T$. Then,
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numerical results of MPC, PID and T-S SFPC are shown in Fig. 9.

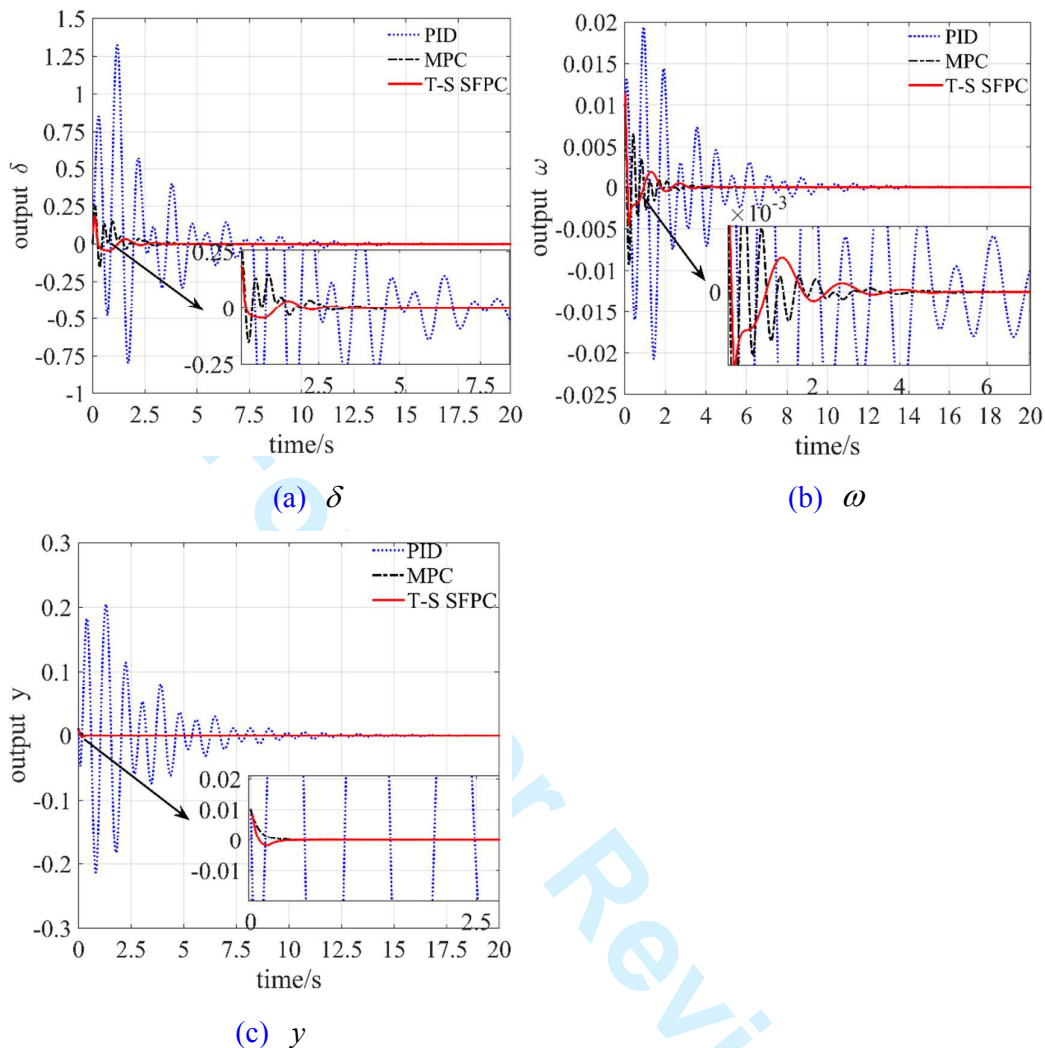


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3 T-S SFPC can enable the adjusting time of both outputs δ and ω to shorten by 25%
4 and 22.4%. Furthermore, the fluctuations of the state feedback predictive control
5 method are smaller than those registered for PID and MPC controllers. This implies
6 that the T-S SFPC method is more efficient than the traditional PID approach and
7 MPC in monitoring and acting on the state of the hydropower station on a real-time
8 scale. Thus, the T-S SFPC enjoys an excellent performance in control of the nonlinear
9 hydropower system.
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11 We have added the correspondingly literatures in reference section, i.e.,

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33 High-functioning adults with autism spectrum disorder. *Journal of Autism and*
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Now, all of the authors would like to appreciate the reviewer's kindness and
useful suggestions to improve our paper!

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3 The manuscript has been resubmitted to your journal. We are looking forward to
4 your positive response.
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7 Yours
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10 Yapeng Yi, Zhiwang Zhang, Diyi Chen, Rui Zhou, Edoardo Patelli, Silvia Tolo
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12 Aug. 14, 2017
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For Peer Review

State Feedback Predictive Control for Non-linear Hydro-turbine

Governing System

Yapeng Yi¹, Zhiwang Zhang¹, Diyi Chen^{1,2*}, Rui Zhou¹, Edoardo Patelli³, Silvia Tolo³

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²*Australasian Joint Research Centre for Building Information Modelling, School of Built Environment, Curtin University, WA, 6102, Australia*

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Abstract: The present work introduces a novel predictive control strategy for the analysis of the dynamic performance of hydro-turbine governing systems based on fuzzy logic. Firstly, a six-dimensional non-linear dynamic model of the system is defined. The defined model is applied to a realistic case-study, aiming to investigate the dynamic behavior of the system. In order to deal effectively with the non-linearity of the system under study, the T-S fuzzy approach is adopted. The results demonstrated through the use of the discrete Lyapunov function and Schur complements of matrices suggest that the closed-cycle control system can achieve a global asymptotic stability state. The second part focuses on the quantification of the impact of sudden changes in operating conditions on the overall performance. The numerical results indicate that proposed predictive control method can ensure the performance of the system to be reliable and robust to external inferences. **In addition to this, the approach proposed has unquestionable advantages over the traditional PID and model predictive controllers with regard to non-linear systems applications.**

Keywords: State feedback predictive control, T-S fuzzy model, hydro-turbine governing system, non-linear, stability

1. Introduction

Hydraulic turbine governing systems (HTGSs) are sophisticated non-linear, multi-input multi-output and non-minimum phase systems, which generally include the turbine, the pressure diversion, the reservoir, the governor, the grid and the load of hydropower systems (Li et al., 2016; Li et al., 2017). However, with the rapid growth of the hydropower installed capacity in the last decades and the subsequent construction of large installations has widened the level of uncertainty affecting the dynamic behavior of HTGSs (Xu et al., 2015). In more detail, the accuracy in the monitoring of these systems is strongly affected by many factors, e.g., the randomness of the load disturbance, the uncertainty related to the non-linear adjustment of the servomotor (Xu et al., 2016; Guo et al., 2015). This high degree of uncertainty and random disturbance have the potential to significantly increase the risks of generator swing and network-disconnecting, it is therefore important to predict the dynamic performance of HTGS. In light of this, implementing a new theoretical and computational tool that is able to fully capture such the uncertainty interference is particularly important (Mahmoud et al., 2005; Donaisky et al., 2015).

During the last decades, traditional algorithms based on the use of a limited number of parameters have been adopted for PID controllers (Martinez-Lucas et al., 2015; Zhang et al., 2015; Zhang et al., 2006; Hao, 2000). However, due to the development of the hydropower industry, the simplified model is not adequately described the uncertainties caused by internal structural parameters of the non-linear systems (Chen et al., 2015). In other words, the theoretical approach behind

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4 traditional control algorithms is not fully adequate to deal with the new challenges
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6 that the engineering practice need to face in the field of hydropower. To fill this gap,
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8 several predictive control methods have been introduced and are nowadays quite
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10 established in the scientific literature (Mobayen et al., 2017; Mobayen, 2014; Cortes
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12 et al., 2008; Liu et al., 2016). Such methods aim to provide on-line optimization and
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14 feedback correction according to the feedback prediction control models (Zhang et al.,
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16 2015; Takacs et al., 2014; Mobayen, 2015). These can solve the problem of
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18 parameters uncertainty in the analysis of the high-dimensional complex model, and
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20 hence enhance the robustness and anti-interference of the system to random
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22 disturbances (Mobayen, 2016; Mobayen et al., 2017; Wang et al., 2016). The research
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24 described in this paper focuses on the analysis of the dynamic characteristics of
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26 HTGSs adopting a predictive control algorithm and aiming to provide a reliable
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28 theoretical background for the safe and stable operation of the hydropower station
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30 (Munoz-Hernandez et al., 2015).

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32 The purpose of the study is achieved through the adoption of the Model
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34 Predictive Control (MPC) method. It refers to use optimization control algorithms to
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36 provide predictions regarding the system behavior, preform rolling optimization and
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38 finally feedback corrections on the basis of the dynamic errors obtained (Kishor, 2008;
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40 Kim et al., 2008; Munoz-Hernandez et al., 2015; Dutta et al., 2016). Many predictive
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42 control algorithms have been implemented an applied in the industrial field in recent
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44 years. One of the first examples have been used this kind of method in the
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46 Boiler-Turbine industry is the Dynamic Matrix Control (DMC) in Ref (Moon et al.,
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2009; Wu et al., 2014). It tackles the output error in the case of steady-state at the cost of a higher computational demand. An alternative to the DMC approach is represented by the Generalized Predictive Control (GPC), adopted in the study by Ref (Zambelli et al., 2012; Errouissi et al., 2016; Tran et al., 2015; Brown et al., 2013). This is a robust adaptive control algorithm but it presents strong limitations in dealing with non-linear systems. To overcome the limitation of previous approaches, the State Feedback Predictive strategy has been proposed: in this kind of algorithms the introduction of a state feedback loop allows to efficiently provide state feedback correction (Zhang et al., 2008; Ji et al., 2009). Furthermore, it is less computational demanding than DMC and GPC approaches and requires only a restrict number of parameters in the model definition. In light of this, the current research focuses on the integration of the state feedback predictive control approach, adopted for the control optimization of non-linear hydraulic turbine systems with the T-S fuzzy model, which provides the modelling of non-linear systems with arbitrary parameters precision (Su et al., 2007; Chen et al., 2013; Lam, 2009; Rastegar et al., 2016).

Inspired by what has been discussed above, there are four innovations of this paper which make the proposed method more appealing compared with previous works. This study firstly consists of the definition of a six-dimensional nonlinear dynamic model for the HTGS, which provides an accurate representation of real systems. The second innovation is the state feedback predictive control of HTGS applied in T-S fuzzy model, which makes the global output of the HTGS model have good mathematical expression characteristics. Thirdly, the SFPC that has both output

feedback and state feedback circuits to guarantees the efficient feedback correction of control system as the output feedback channel is disconnected. Finally, the dynamic feedback structure composed by measured state variables of control system that can be able to inhibit the unpredictable interference in advance.

The organization of this paper is as follows: In Section 2, the proposed integration between state feedback predictive control strategy and the T-S fuzzy model is introduced. In Section 3, a non-linear model of the hydro-turbine governing system is defined. The application of the approach to a realistic case-study and the numerical experiment results obtained are then proposed in Section 4 and Section 5, respectively. Conclusions and discussion in Section 6 close the paper.

2. Proposed strategy

2.1 T-S fuzzy model

A non-linear system can be described as:

$$\begin{cases} \dot{\mathbf{x}}(t) = \mathbf{f}(\mathbf{x}(t), \mathbf{u}(t)) \\ \mathbf{y} = \mathbf{C}\mathbf{x}(t) \end{cases}, \quad (1)$$

where $\mathbf{x}(t) \in \mathbf{R}^n$ and $\mathbf{u}(t) \in \mathbf{R}^m$ satisfy the conditions $\mathbf{x}(t) \in X$, $\mathbf{u}(t) \in U$ with $\forall t \geq 0$, $\mathbf{f}(\cdot)$ is a Lipschitz continuous function in the space $X \times U$, and \mathbf{y} is the output response of the nonlinear system.

In order to approximate the non-linear system, the T-S fuzzy model has been adopted, according to the study by (Wang et al. 2006), the discrete T-S fuzzy state space model can be expressed as:

R_p^i : If $x_1(k)$ is M_1^i , and $x_2(k)$ is M_2^i ,and $x_n(k)$ is M_n^i , then

$$\mathbf{x}(k+1) = \mathbf{A}_i \mathbf{x}(k) + \mathbf{B}_i \mathbf{u}(k) + \mathbf{W}_i, \quad (2)$$

where $i=1,2,\dots,l$; R_p^i denotes the i -th fuzzy rules of the T-S fuzzy model; l is the number of rules; M_j^i ($j=1,2,\dots,n$) denotes fuzzy collection; $\mathbf{x}(k)=[x_1(k), x_2(k), \dots, x_n(k)]^T \in \mathbf{R}^n$ is the state variable; $A_i \in \mathbf{R}^{n \times n}$ and $B_i \in \mathbf{R}^{n \times m}$ denote respectively the system matrix and control matrix of the i -th subsystem; $\mathbf{u}(k) \in \mathbf{R}^m$ is the input variable; \mathbf{W}_i is the constant vector of the i -th subsystem, which is generally considered to be a zero vector, according to the fuzzy modeling method.

Hence, if $\mathbf{y}(k)=[y_1(k) \ y_2(k), \dots, y_m(k)]^T$, and $\mathbf{C}=[\mathbf{c}_1^T, \mathbf{c}_2^T, \dots, \mathbf{c}_m^T]^T \in \mathbf{R}^{m \times n}$ denote the system output matrix, the Eq. (3) is obtained:

$$\mathbf{y}(k) = \mathbf{C}\mathbf{x}(k). \quad (3)$$

2.2 Feedback predictive control based on the T-S fuzzy model

The block diagram of the state feedback predictive control under study in this work is shown in **Fig. 1**. With regard to the diagram, \hat{y} denotes the prediction output obtained by the model inference, y denotes the actual output of the controlled process, and x is a state variable. In the proposed strategy, the state feedback predictive control is performed on the basis of the T-S fuzzy model. The output for the state feedback predictive control is obtained according to the procedure described in the following.

Figure 1. Block diagram of the state feedback predictive control based on the T-S fuzzy model

On the basis of the fuzzy modeling approach, if the vector W_i in Eq. (2) is considered to be a zero vector, then the same equation can be expressed as:

$$x(k+1) = \sum_{i=1}^l h_i(k) A_i x(k) + \sum_{i=1}^l h_i(k) B_i u(k). \quad (4)$$

For the sake of clarity, we set $H_{jA} = \sum_{i=1}^l h_i(k+1) A_i$, $H_{jB} = \sum_{i=1}^l h_i(k+1) B_i$, then

$$\begin{aligned} x(k+p) &= H_{(p-1)A} H_{(p-2)A} \cdots H_{0A} x(k) \cdots \\ &+ H_{(p-1)A} H_{(p-2)A} \cdots H_{1A} H_{0B} u(k) \cdots \\ &+ H_{(p-1)A} H_{(p-2)B} u(k+p-2) + H_{(p-1)B} u(k+p-1) \end{aligned} \quad (5)$$

H_{jA} and H_{jB} are associated to $x(k+q)$ through the derivation process described above. In this case, the membership function under for state x^s results

$$h_i^s = \frac{\mu^i(x^s)}{\sum_{j=1}^l \mu^j(x^s)}, \text{ where } i = 1, 2, \dots, l.$$

Considering $h_i(k+q) = h_i^s$, $q = 1, 2 \cdots p$, then the former conditions become:

$$\begin{aligned} H_{(p-1)A} &= H_{(p-2)A} = \cdots = H_{1A} = \sum_{i=1}^l h_i^s A_i \xrightarrow{\text{define}} A \\ H_{(p-1)B} &= H_{(p-2)B} = \cdots = H_{1B} = \sum_{i=1}^l h_i^s B_i \xrightarrow{\text{define}} B \end{aligned} \quad (6)$$

In light of Eq. (6), Eq. (5) can be rewritten in the form:

$$x(k+p) = A^p x(k) + \sum_{i=1}^p A^{(i-1)} B u(k+p-i). \quad (7)$$

Eq. (7) suggests that to each sample of p_j , the estimated value of the j -th output can be defined as:

$$\hat{y}_j(k+p_j) = C_j A^{p_j} x(k) + \sum_{i=1}^{p_j} C_j A^{i-1} B u(k+p_j-i), \quad (8)$$

where $j = 1, 2 \cdots m$, and p_j is the prediction horizon of the j -th output component $y_j(k)$.

For single-valued state feedback predictive control algorithms, the control horizon is $L=1$. This implies that the control law is subject to modifications only at the time k , while it maintains a constant value in the rest of the time domain (namely $u(k+i) = u(k), i > 0$).

In light of this, Eq. (8) can be expressed as

$$\hat{y}_j(k+p_j) = C_j A^{p_j} x(k) + \mathcal{S}_j(p_j) u(k), \quad (9)$$

where $\mathcal{S}_j(p_j) = \sum_{i=1}^{p_j} C_j A^{i-1} B, j=1,2,\dots,m$.

On the other hand, the feedback compensation of the estimated output results:

$$Y_{c_j}(k+p_j) = \hat{y}_j(k+p_j) + y_j(k) - \hat{y}_j(k), \quad (10)$$

where $\hat{y}_j(k) = C_j A^{p_j} x(k-p_j) + \sum_{i=1}^{p_j} C_j A^{i-1} B u(k-i)$, it is the prediction value of the component $y_j(k)$, using the history state $x(k)$ and the history control $u(k)$.

2.3 Optimal control

$Y_j^s(k+p_j)$ is set-point of the j -th output. Then the predictive error of the j -th output is:

$$e_j = Y_j^s(k+p_j) - y_{c_j}(k+p_j). \quad (11)$$

Introducing Eq. (9) in Eq. (11) it results:

$$e_j = Y_j^s(k+p_j) - \hat{y}_j(k+p_j) - y_j(k) + \hat{y}_j(k), \quad (12)$$

which becomes:

$$e_j = Y_j^s(k+p_j) - C_j A^{p_j} x(k) - \mathcal{S}_j(p_j) u(k) - y_j(k) + \hat{y}_j(k). \quad (13)$$

Under the assumption $E = [e_1, e_2, \dots, e_m]^T$, Eq. (13) can be rewritten as:

$$E = Y^s(k) - Kx(k) - \mathcal{S}(p)u(k) - y(k) + \hat{y}(k), \quad (14)$$

where $y(k) = [y_1(k), y_2(k), \dots, y_m(k)]^T$, $\hat{y}(k) = [\hat{y}_1(k), \hat{y}_2(k), \dots, \hat{y}_m(k)]^T$,

$$Y^s(k) = \begin{pmatrix} Y_1^s(k + p_1) \\ Y_2^s(k + p_2) \\ \vdots \\ Y_m^s(k + p_m) \end{pmatrix}, \mathbf{K} = \begin{pmatrix} C_1 A^{p_1} \\ C_2 A^{p_2} \\ \vdots \\ C_m A^{p_m} \end{pmatrix} \text{ and } \mathbf{S}(p) = \begin{pmatrix} S_1(p_1) \\ S_2(p_2) \\ \vdots \\ S_m(p_m) \end{pmatrix}. \quad (15)$$

The objective function of the problem under study is then expressed as:

$$J = E^T Q E, \quad (16)$$

where Q is a positive definite symmetric matrix. Imposing $\frac{\partial J}{\partial u} = 0$, the optimal control law of the i -th subsystem results:

$$u(k) = \mathbf{S}^{-1}(p)[Y^s(k) - \mathbf{K}x(k) - y(k) + \hat{y}(k)]. \quad (17)$$

Eq. (17) shows that the optimal control law of the system is composed of the state feedback control law and the output feedback control law.

The procedure of the described algorithm is summed up by the flowchart show in

Fig 2:

Figure 2. Flowchart of state feedback predictive control

2.4 Stability analysis

Assuming the model to be accurate and without any disturbance, the condition $y(k) = \hat{y}(k)$ is verified.

Eq. (17) can be expressed as:

$$u(k) = \mathbf{S}^{-1}(p)[Y^s(k) - \mathbf{K}x(k)]. \quad (18)$$

Moreover, the state space of the closed-cycle predictive control system can be expressed as:

$$\begin{cases} x(k+1) = A_c x(k) + B_c Y^s(k) \\ y(k) = Cx(k) \end{cases}, \quad (19)$$

where $A_c = A - BS^{-1}(p)K$, $B_c = BS^{-1}(p)$.

Then Eq. (2) (always assuming $W = 0$) becomes:

$$x(k+1) = \sum_{i=1}^l h_i(k)(A_i - B_i S^{-1}(p)K)x(k) + \sum_{i=1}^l h_i B_i S^{-1}(p)Y^s(k). \quad (20)$$

Since the stability of the closed-cycle system is not related to the value of $Y^s(k)$.

we assume $Y_s(k) = [0, 0, 0]^T$. In this case, Eq. (20) can be simplified as:

$$x(k+1) = \sum_{i=1}^l h_i(k)(A_i - B_i S^{-1}(p)K)x(k). \quad (21)$$

Theorem: If there exists a positive definite symmetric matrix P_i satisfying the linear matrix inequality:

$$\begin{bmatrix} P_i & G_i^T P_r \\ P_r G_i & P_r \end{bmatrix} > 0, G_i = A_i - B_i S^{-1}(p)K, i, r = 1, 2, \dots, l. \quad (22)$$

Then the T-S fuzzy closed-cycle system is global asymptotic stability under the control law of Eq. (17).

Proof: The Lyapunov function for the system described by Eq. (21) is:

$$V(x(k)) = x(k)^T P(x(k))x(k), P(x(k)) = \sum_{r=1}^l h_r(k)P_r. \quad (23)$$

Then $\Delta V = V(x(k+1)) - V(x(k))$

$$= x(k+1)^T \sum_{r=1}^l h_r(k+1)P_r x(k+1) - x(k)^T P(x(k))x(k), \quad (24)$$

where $h_r(k)$ is the weight of the fuzzy rule, and verifies the conditions of

$0 \leq h_i(k) \leq 1$ and $\sum_{i=1}^l h_i(k) = 1$. In light of this,

$$\begin{aligned}
\Delta V &= \left[\sum_{i=1}^l h_i(k) \mathbf{G}_i x(k) \right]^T \sum_{i=1}^l h_r(k+1) \mathbf{P}_r \left[\sum_{j=1}^l h_j(k) \mathbf{G}_j x(k) \right] - x(k)^T \left[\sum_{i=1}^l h_i(k) \mathbf{P}_i \right] x(k) \\
&= \sum_{i=1}^l \sum_{j=1}^l \sum_{r=1}^l h_i(k) h_r(k+1) h_j(k) x(k)^T \left[\mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_j - \mathbf{P}_i \right] x(k)
\end{aligned} \quad (25)$$

Being \mathbf{P}_r is a positive definite symmetric matrix, it can be written as:

$\mathbf{P}_r = \mathbf{D}_r \mathbf{D}_r^T$. Hence Eq. (25) becomes:

$$\begin{aligned}
\Delta V &= \sum_{i=1}^l \sum_{j=1}^l \sum_{r=1}^l h_i(k) h_r(k+1) h_j(k) x(k)^T \left[\mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_j - \mathbf{P}_i \right] x(k) \\
&\leq \sum_{i=1}^l \sum_{j=1}^l \sum_{r=1}^l h_i(k) h_r(k+1) h_j(k) x(k)^T \left[\frac{1}{2} (\mathbf{G}_i^T \mathbf{D}_r \mathbf{D}_r \mathbf{G}_i + \mathbf{G}_j^T \mathbf{D}_r \mathbf{D}_r \mathbf{G}_j) - \mathbf{P}_i \right] x(k) \quad (26) \\
&= \sum_{i=1}^l \sum_{r=1}^l h_i(k) h_r(k+1) x(k)^T \left[\mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_i - \mathbf{P}_i \right] x(k)
\end{aligned}$$

According to the Schur complement of the matrix, the inequality in Eq. (22) holds only under the condition $\mathbf{P}_i - \mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_i > 0$, it is equivalent to $\mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_i - \mathbf{P}_i < 0$, besides, $h_i(k) \geq 0, h_r(k+1) \geq 0$, then:

$$\Delta V \leq \sum_{i=1}^l \sum_{r=1}^l h_i(k) h_r(k+1) x(k)^T \left[\mathbf{G}_i^T \mathbf{P}_r \mathbf{G}_i - \mathbf{P}_i \right] x(k) < 0. \quad (27)$$

The closed-loop system Eq. (21) is globally asymptotical stability.

3. Non-linear modeling of the HTGS

The HTGS modeled in this paper consists of a hydro-turbine system, a penstock system, a generator system, and a servo system. The structure of such system is shown in the diagram of **Fig 3**.

Figure 3. Structure diagram of the hydro-turbine and penstock system

3.1 Hydro-turbine and pressure diversion system

From Ref (Zhang et al., 2015), the transfer function of the pressure in the

diversion system can be expressed as:

$$G_h(s) = -2h_w \frac{\frac{1}{48} T_r^3 s^3 + \frac{1}{2} T_r s}{\frac{1}{8} T_r^3 s^2 + 1}, \quad (28)$$

where h_w is the characteristic parameter of the penstock system, $T_r = \frac{2L}{v}$ is the time constant of the elastic water hammer.

When the hydraulic turbine is not subject to significant load changes, the speed relative deviation can be regarded as $\omega = 0$, the relationship between the hydraulic turbine torque m_t and the output power P_m is obtained as:

$$P_m = m_t. \quad (29)$$

Therefore, the transfer function for the hydro-turbine and the diversion system can be written as:

$$G_t(s) = e_y \frac{1 + e G_h(s)}{1 - e_{qh} G_h(s)}, \quad (30)$$

where e_y , e , e_{qh} denote the main servomotor stroke transfer coefficient, the intermediate variable and the head transfer coefficient of the flow rate, respectively.

Based on Eq. (28) and Eq. (30), the Eq. (30) can be expressed as:

$$G_t(s) = -\frac{e_y}{e_{qh}} \frac{e s^3 - \frac{3}{h_w T_r} s^2 + \frac{24e}{T_r^2} s - \frac{24}{h_w T_r^3}}{s^3 + \frac{3}{e_{qh} h_w T_r} s^2 + \frac{24}{T_r^2} s + \frac{24}{e_{qh} h_w T_r^3}}, \quad (31)$$

According to Eq. (30), the state space equations of the hydro-turbine and penstock system can be rewritten as:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = x_3 \\ \dot{x}_3 = -a_0 x_1 - a_1 x_2 - a_2 x_3 + y \end{cases}. \quad (32)$$

The dynamic equation of the hydro-turbine output torque can be results:

$$m_t = b_3 y + (b_0 - a_0 b_3) x_1 + (b_1 - a_1 b_3) x_2 + (b_2 - a_2 b_3) x_3, \quad (33)$$

where x_1 , x_2 and x_3 are state variables, $a_0 = \frac{24}{e_{qh} h_w T_r^3}$, $a_1 = \frac{24}{T_r^2}$, $a_2 = \frac{3}{e_{qh} h_w T_r}$,

$$b_0 = \frac{24e_y}{e_{qh} h_w T_r^3}, \quad b_1 = -\frac{24ee_y}{e_{qh} T_r^2}, \quad b_2 = \frac{3e_y}{e_{qh} h_w T_r} \quad \text{and} \quad b_3 = -\frac{ee_y}{e_{qh}}.$$

3.2 Generator system

The generator system has been modeled adopting a second-order non-linear model, for which the state equation is expressed as:

$$\begin{cases} \dot{\delta} = \omega_0 \omega \\ \dot{\omega} = \frac{1}{T_{ab}} [m_t - m_e - D\omega] \end{cases} \quad (34)$$

where δ , ω , T_{ab} and D denote respectively the rotor angle, the deviation of the generator rotor speed, the unit mechanical inertia time constant and the damping coefficient.

If the influence of the rotor speed variation on the torque is expressed in terms of its impact on the damping coefficient, the electromagnetic torque of the generator (m_e) results equal to the electromagnetic power (P_e), as shown in Eq. (35).

$$m_e = P_e. \quad (35)$$

Furthermore, the electromagnetic power of the salient rotor hydro-generator can be expressed as:

$$P_e = \frac{E'_q V_s}{x'_{d\Sigma}} \sin \delta + \frac{V_s^2}{2} \frac{x'_{d\Sigma} - x'_{q\Sigma}}{x'_{d\Sigma} x'_{q\Sigma}} \sin 2\delta, \quad (36)$$

where E'_q is the transient voltage of the q axis, V_s is the infinite bus voltage, x'_d is the direct axis transient reactance and x'_q is the quartered axis reactance, $x'_{d\Sigma}$

and $x'_{q\Sigma}$ can be expressed as:

$$\begin{cases} x'_{d\Sigma} = x'_d + x_T + \frac{1}{2}x_L \\ x'_{q\Sigma} = x'_q + x_T + \frac{1}{2}x_L \end{cases}, \quad (37)$$

where x_T is the short-circuit reactance of the transformer, and x_L is the transmission line reactance.

3.3 Hydraulic automatic system

The dynamic characteristics of a hydraulic automatic system are represented in Eq. (38):

$$T_y \frac{dy}{dt} + y = u_y, \quad (38)$$

where y , T_y and u_y denote the incremental deviation of the main servomotor stroke, the response time constant of the servomotor and the control signal, respectively.

From Eq. (28) to Eq. (38), the six-dimension mathematical model of the HTGS firstly proposed in Section 3 can be described as:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = x_3 \\ \dot{x}_3 = -a_0x_1 - a_1x_2 - a_2x_3 + y \\ \dot{\delta} = \omega_0\omega + u_1 \\ \dot{\omega} = \frac{1}{T_{ab}} \left[m_l - \frac{E'_q V_s}{x'_{d\Sigma}} \sin \delta - \frac{V_s^2}{2} \frac{x'_{d\Sigma} - x'_{q\Sigma}}{x'_{d\Sigma} x'_{q\Sigma}} \sin 2\delta - D\omega \right] + u_2 \\ \dot{y} = \frac{1}{T_y} (u_3 - y) \end{cases}, \quad (39)$$

where u_1 , u_2 and u_3 are respectively the three predictive controllers considered.

In order to perform a realistic numerical analysis of the model, system parameters were selected for the input of the model: $\omega_0=314$ rad/s, $T_{ab}=8.0$, $D=0.5$, $E'_q=1.35$,

$$x'_{d\Sigma}=1.15, \quad x'_{q\Sigma}=1.474, \quad T_y=0.1, \quad V_s=1.0, \quad e_{qh}=0.5, \quad e_y=1.0, \quad e=0.7, \quad T_r=1.0, \quad h_w=2.0,$$

$$r=0, \quad a_0=24, \quad a_2=3, \quad b_0=24, \quad b_1=-33.6, \quad b_2=3, \quad a_1=\frac{24}{T_r^2}, \quad \text{and} \quad b_3=-1.4,$$

respectively.

4. Optimal predictive controller design

The T-S fuzzy model is adopted in the present section to linearize the hydro-turbine governing system model previously implemented. The procedure followed consists of various steps as shown in the following:

$$\text{Rule } i: \text{ IF } \delta(t) \text{ is } F_i, \text{ then } \begin{cases} \dot{\mathbf{x}}(t) = \mathbf{A}_i \mathbf{x}(t) + \mathbf{B}_i \mathbf{u}(t) \\ \dot{\mathbf{y}}(t) = \mathbf{C}_i \mathbf{x}(t) \end{cases}, \quad i=1,2,3,4$$

$$\text{where } F_1 = \frac{1}{4} \left(1 + \frac{\delta^2}{v^2} \right), \quad F_2 = \frac{1}{4} \left(1 - \frac{\delta^2}{v^2} \right), \quad F_3 = \frac{1}{4} \left(1 + \frac{\delta^4}{v^4} \right), \quad F_4 = \frac{1}{4} \left(1 - \frac{\delta^4}{v^4} \right),$$

$v=1.6$.

In the current study, a discretization step of 0.02s was adopted in order to obtain an acceptable representation of the initial data.

Based on the above analysis, the four subsystems by the linearization procedures are discretized as:

$$x(k+1) = \mathbf{M}_i x(k) + \mathbf{N}_i u(k), \quad i=1,2,3,4. \quad (40)$$

On the basis of the optimal control law deduced from the former analysis and Eq. (15), the feedback gain \mathbf{K}_i and inverse matrix \mathbf{S}_i^{-1} are easily obtained as:

Subsystems 1:

$$\mathbf{K}_1 = \begin{bmatrix} 34.2022 & -4.6939 & 4.0229 & 0.5393 & 52.4755 & -0.3704 \\ 0.8954 & -0.1982 & 0.0969 & -0.0134 & 0.5293 & -0.0047 \\ 0 & 0 & 0 & 0 & 0 & 0.1353 \end{bmatrix},$$

$$\mathcal{S}_1^{-1} = \begin{bmatrix} 4.5767 & -157.4012 & -0.3589 \\ 0.0364 & 4.7181 & 0.0777 \\ 0 & 0 & 1.1564 \end{bmatrix}.$$

Subsystem 2:

$$K_2 = \begin{bmatrix} 33.9612 & -4.6746 & 3.9971 & 0.5420 & 51.9193 & -0.3675 \\ 0.8850 & -0.1970 & 0.0958 & -0.0133 & 0.5147 & -0.0046 \\ 0 & 0 & 0 & 0 & 0 & 0.1353 \end{bmatrix},$$

$$\mathcal{S}_2^{-1} = \begin{bmatrix} 4.5756 & -158.0435 & -0.3598 \\ 0.0367 & 4.7902 & 0.0782 \\ 0 & 0 & 1.1564 \end{bmatrix}.$$

Subsystem 3:

$$K_3 = \begin{bmatrix} 34.2309 & -4.6908 & 4.0233 & 0.5393 & 52.5323 & -0.3705 \\ 0.8988 & -0.1985 & 0.0972 & -0.0134 & 0.5334 & -0.0047 \\ 0 & 0 & 0 & 0 & 0 & 0.1353 \end{bmatrix},$$

$$\mathcal{S}_3^{-1} = \begin{bmatrix} 4.5769 & -157.1056 & -0.3596 \\ 0.0366 & 4.7311 & 0.0781 \\ 0 & 0 & 1.1564 \end{bmatrix}.$$

Subsystem 4:

$$K_4 = \begin{bmatrix} 34.2798 & -4.6974 & 4.0291 & 0.5387 & 52.6087 & -0.3711 \\ 0.8985 & -0.1985 & 0.0972 & -0.0134 & 0.5328 & -0.0047 \\ 0 & 0 & 0 & 0 & 0 & 0.1353 \end{bmatrix},$$

$$\mathcal{S}_4^{-1} = \begin{bmatrix} 4.5768 & -157.2653 & 0.1439 \\ 0.0364 & 4.7068 & 0.1730 \\ 0 & 0 & 11.5837 \end{bmatrix}.$$

5. Numerical results

To illustrate the performance of the novel method proposed, the parameters for the numerical application were selected from realistic range: the prediction horizon is equal to 10 ($P=10$), the control horizon to 1 ($L=1$), the softness factor to 0.15 ($e=0.15$), the sampling period as mentioned is 0.02s, and the initial values are set as

$$[x_1, x_2, x_3, d, \omega, y]^T = [0.01, 0.01, 0.01, 0.01, 0.01, 0.01]^T.$$

Case 1: Model match

The output responses for the variables δ, ω, y of the non-linear hydro-turbine governing model with the references $Y_s = [1.5, 0.1, 0.8]^T$ are shown in **Fig 4**.

Figure 4. Output responses for the variables d, ω, y of the system with T-S SFPC controllers; (a) δ (b) ω (c) y

The results obtained highlight that the output response of the variables δ and ω approach the reference Y_s quite rapidly, matching it for at only $t=3.5s$; furthermore, the fluctuation frequency and overshoot result relatively small. These trends indicate that when the load is affected by periodic fluctuations, the controller can guarantee that the effective and fast accomplishment of the equilibrium between the active torque and the resistance torque of the hydroelectric unit. In addition to this, the frequency of the fluctuations the unit can be maintained within acceptable values.

As shown in **Fig. 4 (c)**, the stability of the main servomotor stroke y can be controlled optimally, accomplishing response times within one second and without overshoot. Due to the approximate linear relationship between the main servomotor stroke y and guide vane opening α , which implies the controller to regulate the guide vane so that the hydraulic turbine flow is maintained constant. To sum up, these first results proof the reliability of predictive controllers which are able to lead the system to stability in short time.

Case 2: Tracking performance

Let now assume the variables δ, ω, y to continuously adjust to the variation of working conditions. In this case the values of reference for the output are selected as:

$$Y_s = [1.5, 0.1, 0.8]^T, \quad 0 \leq t \leq 8s; \quad Y_s = [1.7, 0.12, 1.0]^T, \quad 8s \leq t \leq 14s; \quad Y_s = [1.7, 0.12, 1.0]^T,$$

$14s \leq t \leq 20s$. The results of the analysis performed are shown in **Fig. 5**.

Figure 5. Servo tracking response curves under different set points; (a) δ , (b) ω , (c) y

Fig. 5 suggests that the servo tracking speed of the system as well as the output response curves are stationary. This indicates that the system is characterized by an excellent tracking performance adopting the novel control method. More specifically, the output can track the load variation in real-time, so that the hydroelectric generating unit adjusts output power in time and keeps the unit frequency fluctuating within the specified range.

Case 3: Disturbance analysis

During the daily operation of hydropower stations, the system is subject to a wide range of perturbation, possibly caused by the variation or even rejection of the load as well as shutdown procedures etc. Thus, to study the realistic performance of the state feedback predictive control system under these conditions, the HTGS model was applied assuming the occurrence of disturbances for the state variables δ, ω and y , so that: $d_1 = [0.1, 0.03, 0.1]^T, 10s \leq t \leq 12s$. Then, the estimated response of the

hydroelectric system is shown in **Fig. 6**.

Figure 6. System response in the case of perturbations affecting δ, ω, y ; (a) $\delta, 10s \leq t \leq 12s, d = 0.1$ (b) $\omega, 10s \leq t \leq 12s, d = 0.03$ (c) $y, 10s \leq t \leq 12s, d = 0.1$

In spite of the perturbations assumed, also in this case the system appears able to achieve stability. Most importantly, the fluctuation range and the overshoot relatively small, it proving that the HTGS can enter the stable state quickly under the control of the state feedback controller, even if it subject to frequency and load disturbance. Hence, the analysis suggests that the proposed method ensures a good degree of immunity of the controller to interferences.

Case 4: Model mismatch

Former studies available in the literature suggest that steady surges, non-linear processes and external disturbances of the system can lead to model mismatch in long-running predictive control system operation. Therefore, to test the control performance of the state feedback predictive algorithm against these cases, the occurrence of errors affecting the model parameters, $\Delta A \neq 0$, $\Delta B \neq 0$ and $\Delta C \neq 0$ have been considered with regard to the predictive model. The control performance estimated considering such initial imprecision in the parameters is shown in **Fig. 7**.

Figure 7. Response curves for the variables δ, ω, y assuming different error values of the input parameters

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6 **Fig. 7** show that the proposed method enables the HTGS reach to stability rapidly,
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8 with only small fluctuations and overshoot. Therefore, it shows that the state feedback
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10 predictive control system based on T-S fuzzy model can have a good control
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12 performance in overcome model mismatch problems, and provide a strong robustness.
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16 **Case 5: Effects of the prediction horizon**

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18 A further phase of the current study focused on the analysis of the impact of the
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20 prediction horizon on the performance of the approach. In this part, prediction horizon
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22 P is regarded as a variable parameter, the control effects of the P are presented in **Fig.**
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31 **Figure 8.** Response curves d, ω, y for assuming different prediction horizon values;
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34 (a) δ (b) ω (c) y
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39 As shown by the response curve in **Fig. 8**, long prediction horizon values result in
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41 larger overshoot of the system. Therefore, to select a suitable value of the operational
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43 prediction horizon, one of the first things to consider is that a positive definite
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45 symmetric matrix P_i can be found which satisfy the linear matrix inequalities (22), this
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47 condition ensures the closed-cycle system is global asymptotic stability under the
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49 control law (17). In addition, the estimated response rate, overshoot and fluctuation
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51 range are comprehensively considered. Consequently, the prediction horizon is equal
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56 to 10 ($P = 10$) adopted in this paper.
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Case 6: Comparison including the MPC, the PID and the T-S SFPC approach

In order to validate the T-S SFPC method proposed in the paper compared with MPC (Diehl et al., 2002 and 2005; Kunisaki et al., 2008; Kirches et al., 2012; Lopez-Negrete et al., 2013; Jaschke et al., 2014; Otsuka et al., 2017; La et al., 2017) and the PID (Ntogramatzidis et al., 2011) methods, a comparative analysis is therefore performed. Here, the PID controller by Ntogramatzidis in the system (39) is expressed as:

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = x_3 \\ \dot{x}_3 = -a_0x_1 - a_1x_2 - a_2x_3 + y \\ \dot{\delta} = \omega_0\omega \\ \dot{\omega} = \frac{1}{T_{ab}} \left[m_t - \frac{E'_q V_s}{x'_{d\Sigma}} \sin \delta - \frac{V_s^2}{2} \frac{x'_{d\Sigma} - x'_{q\Sigma}}{x'_{d\Sigma} x'_{q\Sigma}} \sin 2\delta - D\omega \right] \\ \dot{y} = \frac{1}{T_y} (-k_p(r - \omega) - \frac{k_i}{\omega_0} \delta - k_d D^q \omega - y) \end{cases} \quad (41)$$

where k_p , k_i and k_d are PID parameters. The parameters are $k_p = 2.0$, $k_i = 1.0$ and $k_d = 2.0$, $q = 1$.

The initial assumption for the reference solution is $Y_s = [0, 0, 0]^T$. Then, numerical results of MPC, PID and T-S SFPC are shown in **Fig. 9**.

Figure 9. Comparison of control performance obtained with MPC, PID and T-S SFPC approaches; (a) δ (b) ω (c) y

Table 1 Adjusting time of the HTGS under MPC, PID and T-S SFPC controllers

The performance results associated with the PID, MPC and T-S SFPC are shown in **Fig. 9** and **Table 1**. It is obvious that the state feedback predictive controller proposed in this paper allows providing better performance for non-linear hydropower system than both PID and MPC. As highlighted in Table 1, compared with MPC, the T-S SFPC can enable the adjusting time of both outputs δ and ω to shorten by 25% and 22.4%. Furthermore, the fluctuations of the state feedback predictive control method are smaller than those registered for PID and MPC controllers. This implies

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3 that the T-S SFPC method is more efficient than the traditional PID approach and
4 MPC in monitoring and acting on the state of the hydropower station on a real-time
5 scale. Thus, the T-S SFPC enjoys an excellent performance in control of the nonlinear
6 hydropower system.
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10 6. Conclusions and discussions

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12 In this paper, the state feedback predictive control algorithm based on the T-S
13 fuzzy model is proposed for hydro-turbine governing systems. It is based on the
14 application of the T-S fuzzy approach to a nonlinear six-dimensional hydroelectric
15 plant system. The proposed methodology not only improves the precision of the
16 prediction model, but also represents accurately the dynamic characteristics of the
17 hydroelectric system. In addition to this, the global asymptotic stability theorem of the
18 close-loop system is proved through the use of the discrete Lyapunov function and
19 Schur complements of matrices. In order to verify the effectiveness and the efficiency
20 of the proposed method, this is applied to a nonlinear hydropower plant system. The
21 results obtained from the numerical analysis, the highlight excellent control
22 performance of the proposed control method in the case of external disturbances,
23 Servo tracking and model mismatch. In the final stage, the novel proposed control
24 method was compared with traditional PID and MPC methods, demonstrating the
25 unquestionable advantages of the proposed method in the non-linear system. And it is
26 worth noting that the results obtained by the overall analysis performed of the T-S
27 SFPC method can provide strong robustness, perfect tracking performance and great
28 anti-interference performance. In conclusion, the T-S SFPC method is a capable
29 control tool particularly suitable for complex non-linear hydroelectric plant systems.
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Future research work will focus on how to solve the problem of predictive control optimization for high-dimensional systems with input constraints and state delays via intelligent optimization algorithms.

Acknowledgements

This work was supported by the scientific research foundation of Natural Science Foundation (51479173, 51279167), Fundamental Research Funds for the Central Universities (201304030577), Scientific research funds of Northwest A&F University (2013BSJJ095), the scientific research foundation on water engineering of Shaanxi Province (2013slkj-12), the Science Fund for Excellent Young Scholars from Northwest A&F University and Shaanxi Nova program (2016KJXX-55).

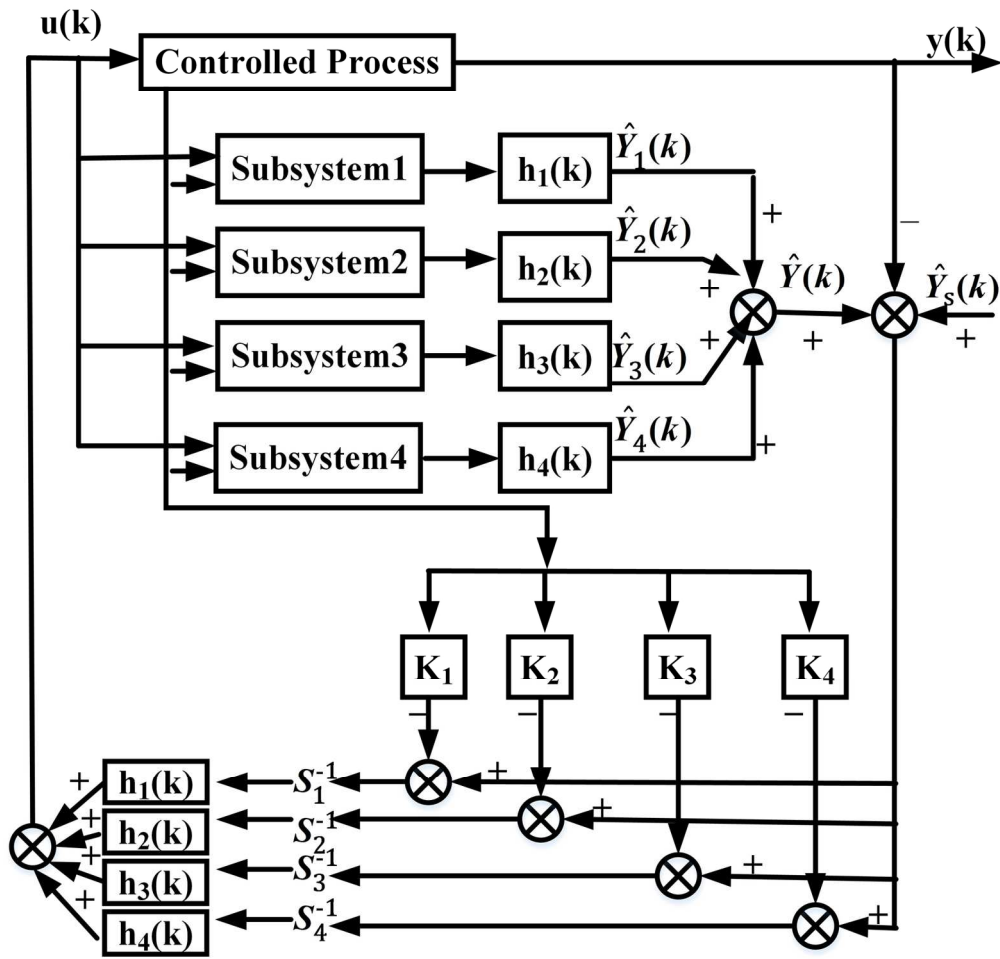
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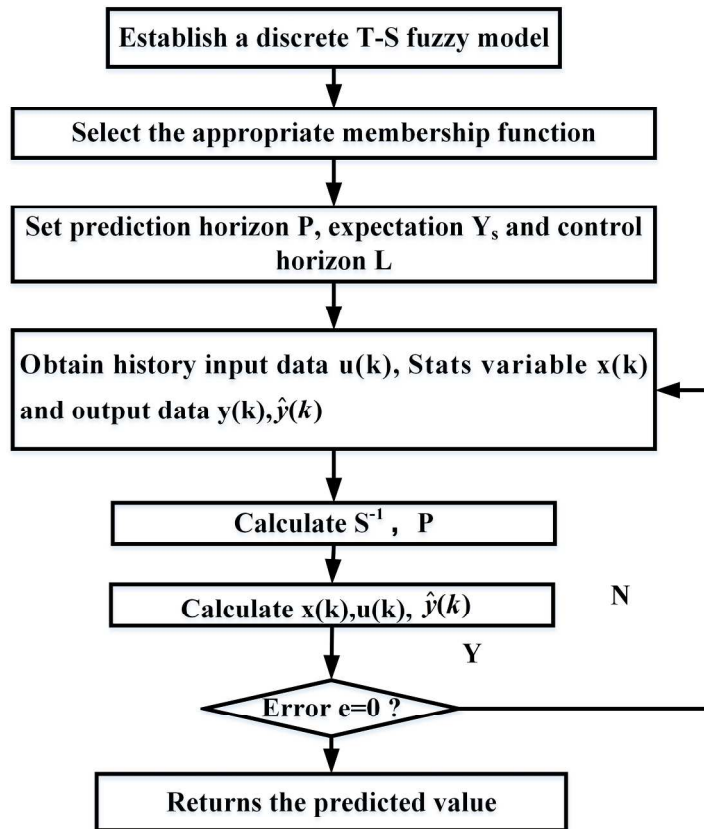
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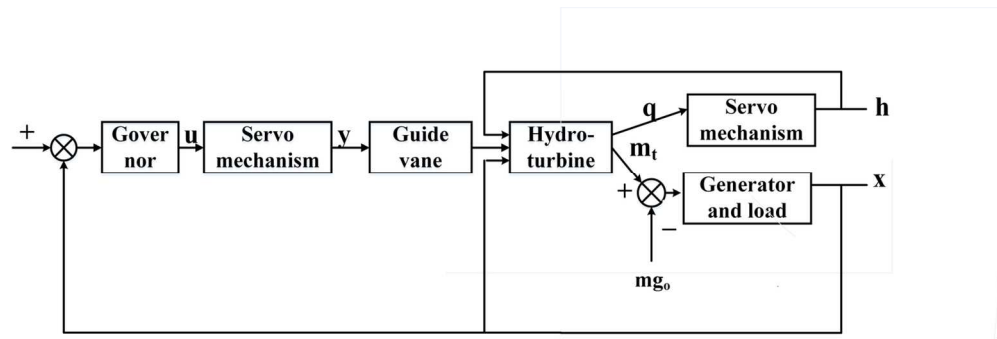


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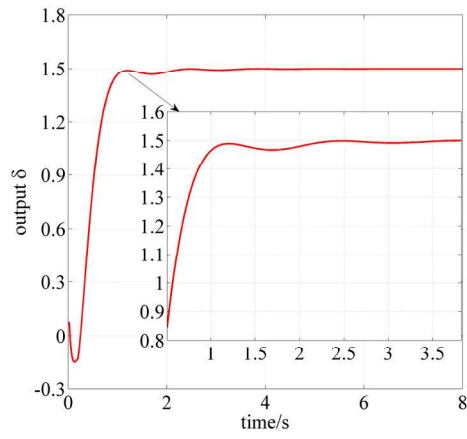
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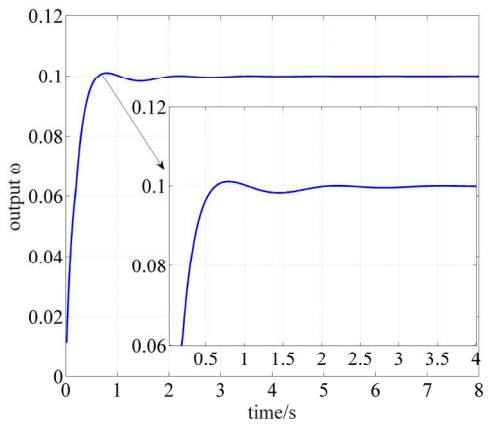
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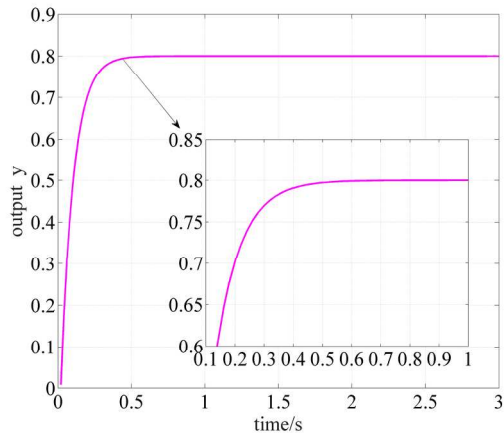
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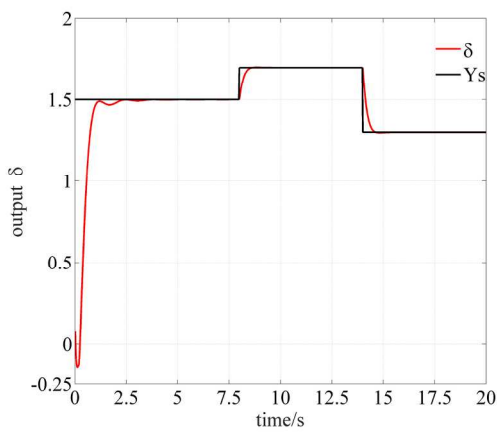


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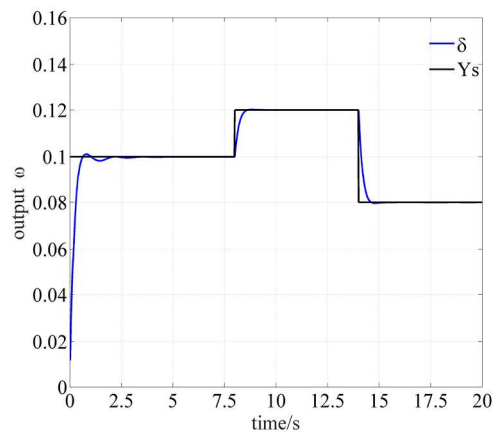
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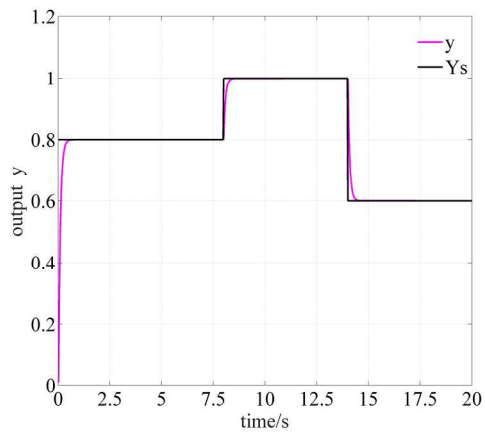
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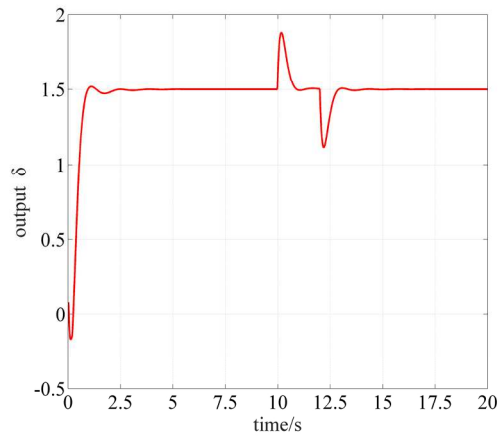
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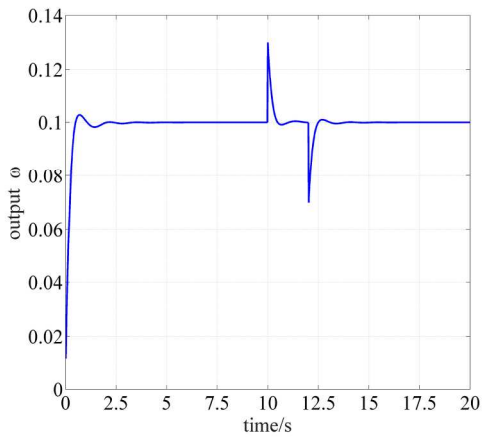


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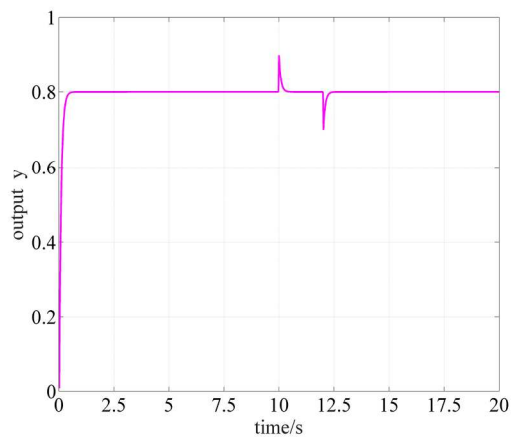
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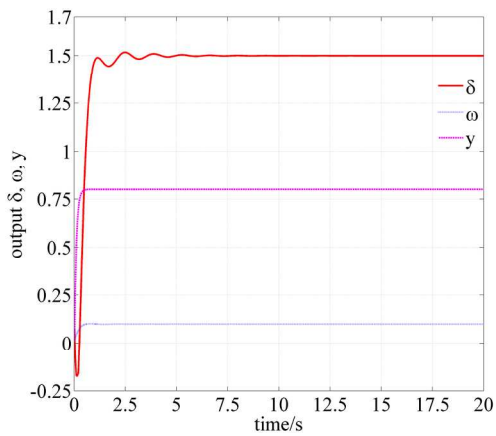


194x89mm (300 x 300 DPI)

Peer Review

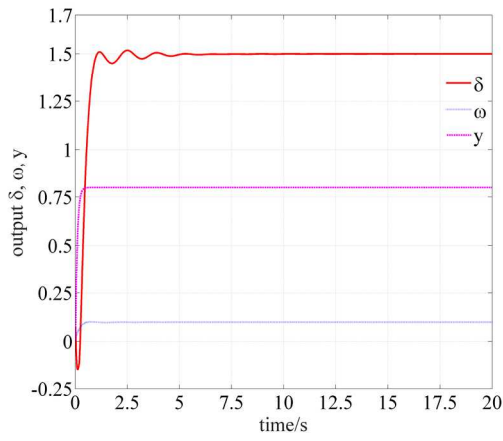
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194x89mm (300 x 300 DPI)

Peer Review

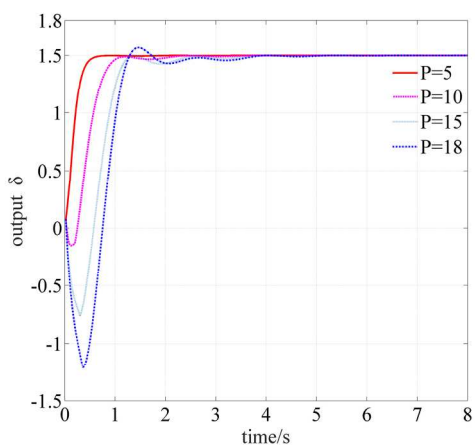


194x89mm (300 x 300 DPI)

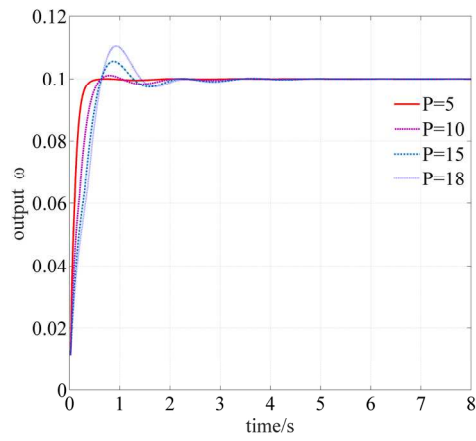
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194x89mm (300 x 300 DPI)

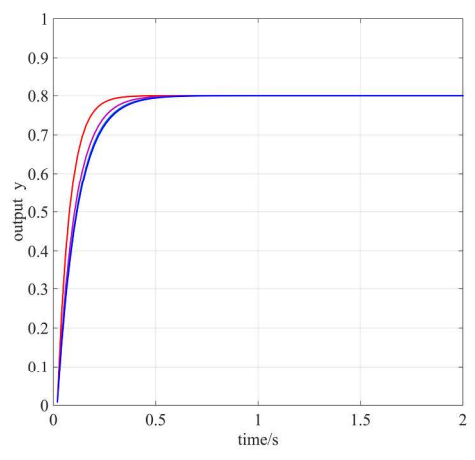


194x89mm (300 x 300 DPI)

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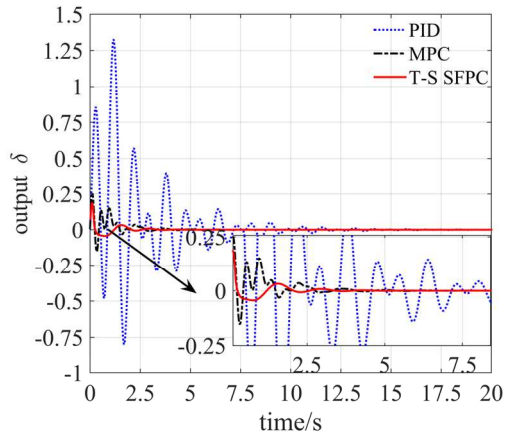
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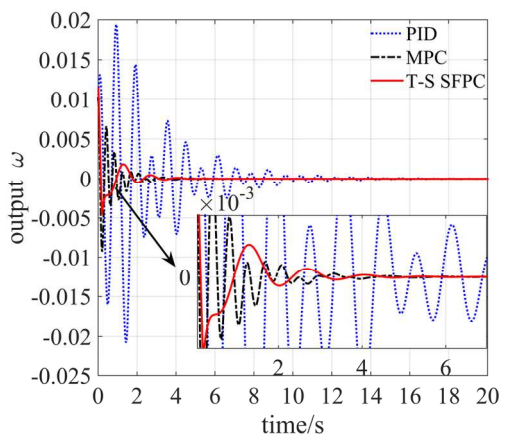
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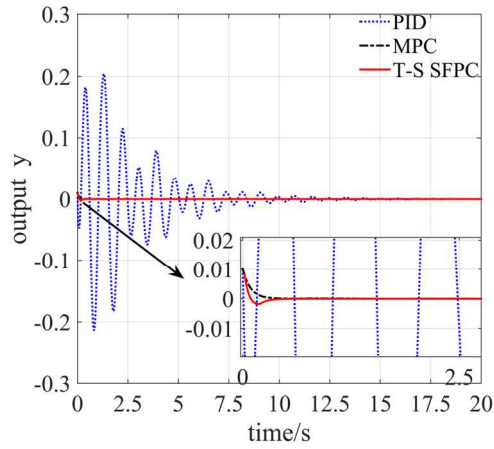


159x69mm (300 x 300 DPI)

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159x69mm (300 x 300 DPI)



159x69mm (300 x 300 DPI)

Peer Review

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Table 1 Adjusting time of the HTGS under MPC, PID and T-S SFPC controllers

	δ			ω			γ		
	PID	MPC	T-S SFPC	PID	MPC	T-S SFPC	PID	MPC	T-S SFPC
T/s	16.6	4.8	3.6	16.1	5.8	4.5	16.5	0.5	0.5

For Peer Review