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Bidirectional User Throughput Maximization Based on Feedback Reduction in LiFi Networks

Mohammad Dehghani Soltani, Student Member, IEEE, Xiping Wu, Member, IEEE, Majid Safari, Member, IEEE, and Harald Haas, Fellow, IEEE

Abstract-Channel adaptive signalling, which is based on feedback, can result in almost any performance metric enhancement. Unlike the radio frequency (RF) channel, the optical wireless communication (OWC) channel is relatively deterministic. This feature of OWC channels enables a potential improvement of the bidirectional user throughput by reducing the amount of feedback. Light-Fidelity (LiFi) is a subset of OWCs, and it is a bidirectional, high-speed and fully networked wireless communication technology where visible light and infrared are used in downlink and uplink respectively. In this paper, two techniques for reducing the amount of feedback in LiFi cellular networks are proposed, i) Limited-content feedback (LCF) scheme based on reducing the content of feedback information and ii) Limited-frequency feedback (LFF) scheme based on the update interval. Furthermore, based on the random waypoint (RWP) mobility model, the optimum update interval, which provides maximum bidirectional user equipment (UE) throughput, has been derived. Results show that the proposed schemes can achieve better average overall throughput compared to the benchmark one-bit feedback and full-feedback mechanisms.

Index Terms—LiFi, Downlink, Uplink, Limited Feedback, Channel Update Interval

I. INTRODUCTION

THE ever increasing number of mobile-connected devices, along with monthly global data traffic which is expected to be 35 exabytes by 2020 [1], motivate both academia and industry to invest in alternative methods. These include mmWave, massive multiple-input multiple-output (MIMO), free space optical communication and Light-Fidelity (LiFi) for supporting future growing data traffic and next-generation high-speed wireless communication systems. Among these technologies, LiFi is a novel bidirectional, high-speed and fully networked wireless communication technology. LiFi uses visible light as the propagation medium in downlink for the purposes of illumination and communication. It may use infrared in uplink in order to not affect the illumination constraint of the room, and also not to cause interference with the visible light in the downlink [2]. LiFi offers considerable advantages in comparison to radio frequency (RF) systems. These include the very large, unregulated bandwidth available in the visible light spectrum, high energy efficiency and the rather straightforward deployment with off-the-shelf light

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emitting diode (LED) and photodiode (PD) devices at the transmitter and receiver ends respectively, enhanced security as the light does not penetrate through opaque objects [3]. These notable benefits of LiFi have made it favourable for recent and future research.

It is known that utilizing channel adaptive signalling can bring on enhancement in almost any performance metric. Feedback can realize many kinds of channel adaptive methods that were considered impractical due to problems of obtaining instantaneous channel state information (CSI) at the access point (AP). Studies have proven that permitting the receiver to transmit a small amount of information or feedback about the channel condition to the AP can provide near optimal performance [4]–[7]. Feedback conveys the channel condition, e.g., received power, signal-to-noise-plus-interference ratio (SINR), interference level, channel state, etc., and the AP can use the information for scheduling and resource allocation. The practical systems using this strategy, also known as limited-feedback (LF) systems, provide a similar performance to the impractical systems with perfect CSI at the AP.

It is often inefficient and impractical to continuously update the AP with the user equipment (UE) link condition. However, to support the mobility, it is also essential to consider the time-varying nature of channels for resource allocation problems to further enhance the spectral efficiency. With limited capacity, assignment of many resources to get CSI would evacuate the resources required to transmit actual data, resulting in reduced overall UE throughput [8]. Therefore, it is common for practical wireless systems to update the CSI less frequently, e.g., only at the beginning of each frame. Many works have been carried out to reduce the amount of feedback in RF, however, very few studies focus on lessening the amount of feedback in optical wireless channels (OWCs).

A. Literature Review and Motivation

An overview of LF methods in wireless communications has been introduced in [7]. The key role of LF in single-user and multi-user scenarios for narrowband and wideband communications with both single and multiple antennas has been discussed in [7]. Two SINR-based limited-feedback scheduling algorithms for multi-user MIMO-OFDM in heterogeneous networks are studied in [9] where UEs feed back channel quality information in the form of SINR. To reduce the amount of feedback, nearby UEs grouping and adjacent subcarrier clustering strategies have been considered. In [10], three limited feedback resource allocation algorithms

1

are evaluated for heterogeneous wireless networks. These resource allocation algorithms try to maximize the weighted sum of instantaneous data rates of all UEs over all cells. The authors in [11] proposed the ordered K-best feedback method to reduce the amount of feedback. In this scheme, only the K best resources are fed back to the AP.

An optimal strategy to transmit feedback based on outdated channel gain feedbacks and channel statistics for a single-user scenario has been proposed in [12]. Other approaches are the transmission of the quantized SINR of subcarriers which is the focus of [13] and [14]; and the subcarrier clustering method which is developed in [15] and [16]. In [17], the subcarrier clustering technique has been applied to the OWCs to reduce the amount of feedback by having each user send the AP the information of candidate clusters. A simple and more realizable solution, which is proposed in [18]-[20], is to inform the AP only if their SINR exceeds some predetermined threshold. This is a very simple approach with only a one bit per subcarrier feedback. The one-bit feedback method is very bandwidth efficient. However, using more feedback can provide a slight downlink performance improvement but at the cost of uplink throughput degradation as discussed in [18]. The benefits of employing only one bit feedback per subcarrier and the minor data rate enhancements of downlink using more feedback bits are analyzed in [21]. A one-bit feedback scheme for downlink OFDMA systems has been proposed in [22]. It specifies whether the channel gain exceeds a predefined threshold or not. Then, UEs are assigned priority weights and the optimal thresholds are chosen to maximize the weighted sum capacity. A problem linked to the one-bit feedback technique is that there is a low probability that none of the UEs will report their SINR to the AP so that the scheduler is left with no information about the channel condition. This issue can be solved at the expense of some extra feedback and overhead by the multiple-stage version of the threshold-based method proposed in [23].

The RF relevant limited feedback approaches mentioned above are all applicable to LiFi networks. However, due to the relatively deterministic behavior of LiFi channels, the feedback can be reduced further without any significant downlink throughput degradation. This motivates us to propose two novel limited feedback schemes for LiFi networks.

B. Contributions and Outcomes

In order to get the maximum bidirectional throughput, the amount of feedback should be optimized in terms of both quantity and update interval. In this paper, we propose two methods to reduce the feedback information. The main contributions of this paper are outlined as follows.

- Proposing the modified carrier sense multiple access with collision avoidance (CSMA/CA) protocol suitable for the uplink of LiFi networks.
- Proposing the limited-content feedback (LCF) scheme for LiFi networks which shows a close downlink performance to the full-feedback (FF) mechanism and an even lower overhead compared to the one-bit feedback technique.
- Proposing the limited-frequency feedback (LFF) scheme based on the sum-throughput of uplink and downlink

maximization. Deriving the optimum update interval for the random waypoint (RWP) mobility model and investigating the effects of different parameters on it.

C. Paper Organization

The rest of this paper is organized as follows. The system model of bidirectional LiFi networks is introduced in Section II. The downlink achievable throughput is calculated in Section III. In Section IV, the modified CSMA/CA is proposed and the uplink throughput has been obtained. In Section V, the proposed LCF and LFF schemes are introduced and evaluated. Then, the optimum update interval is derived for the RWP mobility model. Finally, conclusions are drawn in Section VI.

II. SYSTEM MODEL

A. Optical Attocell System Configuration

A bidirectional optical wireless communication system has been considered in this study. In the downlink, visible light is utilized for the purpose of both illumination and communication, while in the uplink data is transmitted through infrared light in order to not affect the illumination constraint of the room. The geometric configuration of the downlink/uplink in an indoor optical attocell network is shown in Fig. 1. The system comprises of multiple LED transmitters (i.e., APs) arranged on the vertexes of a square lattice over the ceiling of an indoor network and there is a PD receiver on the UE. The LEDs are assumed to be point sources with Lambertian emission patterns. To avoid nonlinear distortion effects, the LEDs operate within the linear dynamic range of the current-to-power characteristic curve. In addition, the LEDs are assumed to be oriented vertically downwards, and the UE are orientated upward to the ceiling. Under this condition, the channel model for both downlink and uplink is the same. One AP is only selected to serve the UE based on the UE location. An optical attocell is then defined as the confined area on the UE plane in which an AP serves the UE. Frequency reuse (FR) plan is considered in both downlink and uplink to reduce the co-channel interference and also guarantee the cell edge users data rate. Further details about the FR plan can be found in [24] and [25].

Power and frequency-based soft handover methods for visible light communication networks are proposed to reduce data rate fluctuations as the UE moves from one cell to another [26]. We consider power-based soft handover with the decision metric introduced in [27] as $|\gamma_i - \gamma_i| < \alpha$, where γ_i and γ_i are the SINR of the serving AP and adjacent APs, respectively; and α is the handover threshold. As a result the cell boundaries are shaped like a circle with the radius of r_c . According to the considered soft handover scheme, when the difference of SINR from two APs goes below the threshold, handover occur.

The received optical signal at the PD consists of line of sight (LOS) and/or non-line of sight (NLOS) components. The LOS is a condition where the optical signal travels over the air directly from the transmitter to the UE, while the NLOS is a condition where the optical signal is received at the UE by means of just the reflectors. These two components are characterized as follows.

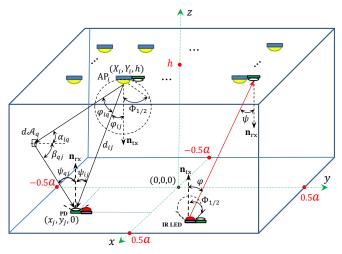


Fig. 1: Geometry of light propagation in LiFi networks. Downlink (consisting of LOS and NLOS components) and uplink (including LOS component) are shown with black and red lines, respectively.

B. Light Propagation Model

The direct current (DC) gain of the LOS optical channel between the *i*th LED and the *j*th PD is given by:

$$H_{\text{LOS},i,j} = \begin{cases} \frac{(m+1)A}{2\pi d_{ij}^2} \cos^m \phi_{ij} g_{\mathbf{f}} g(\psi_{ij}) \cos \psi_{ij}, & 0 \le \psi_{ij} \le \Psi_c \\ 0, & \psi_{ij} > \Psi_c \end{cases},$$
(1)

where A, d_{ij} , ϕ_{ij} and ψ_{ij} are the physical area of the detector, the distance between the ith transmitter and the ith receiver surface, the angle of radiance with respect to the axis normal to the ith transmitter surface, and the angle of incidence with respect to the axis normal to the jth receiver surface, respectively. In (1), g_f is the gain of the optical filter, and Ψ_c is the receiver field of view (FOV). In (1), $g(\psi_i) = \varsigma^2/\sin^2\Psi_c$ for $0 \le \psi_i \le \Psi_c$, and 0for $\psi_i > \Psi_c$, is the optical concentrator gain where ς is the refractive index; and also $m = -1/\log_2(\cos\Phi_{1/2})$ is the Lambertian order where $\Phi_{1/2}$ is the half-intensity angle [28]. The radiance angle ϕ_{ij} and the incidence angle ψ_{ij} of the ith LED and the jth UE are calculated using the rules from analytical geometry as $\cos \phi_{ij} = \mathbf{d}_{ij} \cdot \mathbf{n}_{\mathrm{tx}} / \|\mathbf{d}_{ij}\|$ and $\cos \psi_{ij} = -\mathbf{d}_{ij} \cdot \mathbf{n}_{rx}/\|\mathbf{d}_{ij}\|, \text{ where } \mathbf{n}_{tx} = [0, 0, -1] \text{ and }$ $\mathbf{n}_{rx} = [0, 0, 1]$ are the normal vectors at the transmitter and the jth receiver planes, respectively and \mathbf{d}_{ij} denotes the distance vector between the ith LED and the jth UE and \cdot and $\|\cdot\|$ denote the inner product and the Euclidean norm operators, respectively.

In NLOS optical links, the transmitted signal arrives at the PD through multiple reflections. In practice, these reflections contain both specular and diffusive components. In order to maintain a moderate level of analysis, only first-order reflections are considered in this study. A first-order reflection includes two segments: i) from the LED to a small area $d\mathcal{A}_q$ on the wall; and ii) from the small area $d\mathcal{A}_q$ to the PD. The

DC channel gain of the first-order reflections is given by:

$$\int_{\mathcal{A}_q} \frac{\rho_q(m+1)A}{2\pi^2 d_{iq}^2 d_{qj}^2} \cos^m \phi_{iq} \cos \psi_{qj} g_f g(\psi_{qj}) \cos \alpha_{iq} \cos \beta_{qj} d\mathcal{A}_q,$$
(2)

where \mathcal{A}_q denotes the total walls reflective area; ρ_q is the reflection coefficient of the qth reflection element; d_{iq} is the distance between the ith LED and the qth reflection element; d_{qj} is the distance between the qth reflection element and the jth UE; ϕ_{iq} and ψ_{iq} are the angle of radiance and the angle of incidence between the ith LED and the qth reflective element, respectively; and ϕ_{qj} and ψ_{qj} are the angle of radiance and the angle of incidence between the qth reflective element and the jth UE, respectively [29]. The channel gain between AP_i and AP_i are the angle of both LOS and NLOS components that is expressed as:

$$H_{i,j} = H_{\text{LOS},i,j} + H_{\text{NLOS},i,j}.$$
 (3)

Note that due to symmetry of downlink and uplink channels, (1)-(3) are valid for both downlink and uplink.

C. Low Pass Characteristic of LED

We note that LiFi systems have a very large and unregulated bandwidth, a single AP operating at a particular wavelength is not able to utilize the whole bandwidth and is practically limited by the 3-dB bandwidth of off-the-shelf LEDs. The frequency response of an off-the-shelf LED is not flat and is modeled as a first order low pass filter as, $H_{\rm LED}(w) = e^{-w/w_0}$, where w_0 is the fitted coefficient [30]. The higher the value of w_0 , the wider the 3-dB bandwidth, $B_{\rm 3dB}$. The 3-dB bandwidth of typical LEDs is low, however, the modulation bandwidth, B, can be multiple times greater than $B_{\rm 3dB}$ thanks to utilization of OFDM. In this paper, we consider OFDMA for two purposes: i) to alleviate the low pass effect of LED and ii) to support multiple access. The frequency response of an LED on the kth subcarrier can be obtained as:

$$H_{\text{LED }k} = e^{-2\pi k B_{d,n}/\mathcal{K}w_0},\tag{4}$$

where K is the total number of subcarriers and $B_{d,n}$ is the downlink bandwidth of the nth FR plan.

D. Receiver Mobility Model

We considered the RWP model which is a commonly used mobility model for simulations of wireless communication networks [31]. The RWP mobility model is shown in Fig. 2. According to the RWP model, the UE's movement from one waypoint to another waypoint complies with a number of rules, including i) the random destinations or waypoints are chosen uniformly with probability $1/(\pi r_c^2)$; ii) the movement path is a straight line; and iii) the speed is constant during the movement. The RWP mobility model can be mathematically expressed as an infinite sequence of triples: $\{(\mathbf{P}_{\ell-1},\mathbf{P}_\ell,v_\ell)\}_{\ell\in\mathbb{N}}$ where ℓ denotes the ℓ th movement period during which the UE moves between the current waypoint $\mathbf{P}_{\ell-1}=(x_{\ell-1},y_{\ell-1},0)$ and the next waypoint $\mathbf{P}_{\ell}=(x_\ell,y_\ell,0)$ with the constant velocity $V_\ell=v$. RWP model is more realistic

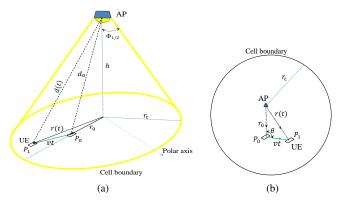


Fig. 2: RWP movement model.

scenario and has been used in many studies for modeling the mobility of UE [32], [33].

The UE distance at time instance t from the AP is $d(t) = \left(r^2(t) + h^2\right)^{1/2}$, where $r(t) = (r_0^2 + v^2t^2 - 2r_0vt\cos\theta)^{1/2}$ with $\theta = \pi - \cos^{-1}\left(\frac{\vec{r_0}\cdot\vec{v}}{|\vec{r_0}||\vec{v}|}\right)$; $\vec{r_0}$ is the initial UE distance vector from the cell center at t=0 with $|\vec{r_0}| = r_0$; and \vec{v} is the vector of UE's velocity with $|\vec{v}| = v$. Here, r_0 has the probability distribution function (PDF) of $f_{\mathcal{R}_0}(r_0) = 2r_0/r_c^2$ and θ is chosen randomly from a uniform distribution with PDF of $f_{\Theta}(\theta) = 1/\pi$. For notation simplicity, the dependency of the equations to time is omitted unless it is confusing.

III. DOWNLINK THROUGHPUT CALCULATION

The channel access protocol in the downlink is assumed to be orthogonal frequency division multiple access (OFDMA) based on DCO-OFDM so as to support downlink multiple access simultaneously. The modulated data symbols of different UEs, X_k , are arranged on \mathcal{K} subcarriers of the OFDMA frame, X. Then, the inverse fast Fourier transform (IFFT) is applied to the OFDMA frame to obtain the time domain signal \tilde{x} . For optical systems that perform intensity modulation, the modulated signal, \tilde{x} , must be both real and positive [34]. This requires two constraints on the entities of the OFDMA frame: i) X(0) $X(\mathcal{K}/2) = 0$, and ii) the Hermitian symmetry constraint, i.e., $X(k) = X^*(\mathcal{K} - k)$, for $k \neq 0$, where $(\cdot)^*$ denotes the complex conjugate operator. Therefore, the OFDMA frame is $X = \zeta[0, X_1, ..., X_{\mathcal{K}/2-1}, 0, X_{\mathcal{K}/2-1}^*, ..., X_1^*]$, the normalizing factor, $\zeta = \sqrt{\mathcal{K}/(\mathcal{K}-2)}$, is multiplied since the 0th and $(\mathcal{K}/2)$ th samples require no energy. Note that the number of modulated subcarriers bearing information is $\mathcal{K}/2-1$. Afterwards, a moderate bias relative to the standard deviation of the AC signal \tilde{x} is used as $x_{DC} = \eta \sqrt{\mathbb{E}[\tilde{x}^2]}$, where η is the conversion factor [35]. The signal $x = x_{DC} + \tilde{x}$ is then used as the input of an optical modulator. In general, the condition $\eta = 3$ guarantees that less than 1% of the signal is clipped. In this case, the clipping noise is negligible [36].

Let $H_j = [H_{i,j}]$, for $i = 1, 2, ..., N_{AP}$, be the downlink visible light channel gain vector from all APs to the UE_j . The UE_j is connected to AP_i based on the maximum channel gain criterion so that $i = \arg_i \max(\mathbf{H}_j)$. Afterwards, the embedded scheduler algorithm in AP_i allocates a number of

subcarriers to the UE_j based on its requested data rate and its link quality. In this study, a fair scheduling method for OFDMA-based wireless systems is considered [37], [38]. The scheduler assigns the kth resource to jth UE according to the following metric:

$$j = \arg\max_{i} \frac{R_{\text{req},j}}{\overline{R_i}},\tag{5}$$

where $\overline{R_i}$ is the average data rate of ith UE before allocating the kth resource, and $R_{{\rm req},j}$ is the request data rate of ${\rm UE}_j$. We note that through this paper, it is assumed that all of the UEs' request data rates are the same, that is $R_{{\rm req},j}=R_{{\rm req}}$, for all j.

Throughout this study, we consider LiFi systems transmitting data based on DC-biased optical OFDM. As shown in [39], the channel can be modelled in the *electrical* domain as an AWGN channel with an average power constraint, and this falls within the Shannon framework which is the upper bound on any achievable data rate. It is assumed that the effect of clipping noise is negligible, the downlink rate of UE_i after scheduling can be obtained as:

$$R_{d,j} = \frac{B_{d,n}}{\mathcal{K}} \sum_{k=1}^{\mathcal{K}/2-1} \log_2 (1 + s_{j,k} \gamma_{d,j,k}),$$
 (6)

where $s_{j,k}=1$ if the kth subcarrier is allocated to the UE_j otherwise $s_{j,k}=0$; $\gamma_{\mathrm{d},j,k}$ is the SINR of UE_j on the kth subcarrier serving by AP_i . It is worth mentiong that the delay spread for typical indoor scenarios is up to 50 ns as shown in [40]. Hence, the cyclic perfix (CP) which is added to the OFDMA signal to mitigate the inter-symbol interference (ISI) due to the channel delay spread is just in order of few bits. Therefore, the effect of delay spread and CP on the achievable data rate is negligible [41].

In communication systems, SINR is defined as the ratio of the desired electrical signal power to the total noise and interference power and is an important metric to evaluate the connection quality and the transmission data rate. Denoting $P_{\text{elec},i,j,k}$ as the received electrical power of the jth UE on the kth subcarrier, then, $\gamma_{\mathrm{d},j,k} = P_{\mathrm{elec},i,j,k}/(\sigma_{j,k}^2 + P_{\mathrm{int},j})$, where $\sigma_{j,k}^2 = N_0 B_{\mathrm{d},n} / \mathcal{K}$, is the noise on the kth subcarrier of UE_j, and N_0 is the noise power spectral density; $P_{\text{int},j}$ is the interference from other APs on the jth UE. It is assumed that the APs emit the same average optical power and the total transmitted electrical power is equally allocated among K-2 subcarriers so that the received electrical power on the kth subcarrier of the jth UE is equal to $P_{{
m elec},i,j,k}=R_{
m PD}^2P_{{
m d,opt}}^2H_{i,j,k}^2H_{{
m LED},k}^2/(\eta^2(\mathcal{K}-2)),$ where $P_{{
m d,opt}}$ is the transmitted optical power; $R_{
m PD}$ is the PD responsivity; $H_{i,j,k}$ is the frequency response of channel gain on the kth subcarrier. It includes both LOS and the first order reflections. Accordingly, the received SINR of the jth UE on the kth subcarrier can be expressed as:

$$\gamma_{\mathrm{d},j,k} = \frac{R_{\mathrm{PD}}^{2} P_{\mathrm{d,opt}}^{2} H_{i,j,k}^{2} H_{\mathrm{LED},k}^{2}}{(\mathcal{K}-2) \eta^{2} \sigma_{j,k}^{2} + \sum_{i \in \mathcal{S}_{\mathrm{AP},i}} R_{\mathrm{PD}}^{2} P_{\mathrm{d,opt}}^{2} H_{i,j,k}^{2} H_{\mathrm{LED},k}^{2}}.$$
 (7)

where $S_{AP,i}$ is the set of all other APs using the same frequencies as the AP_i .

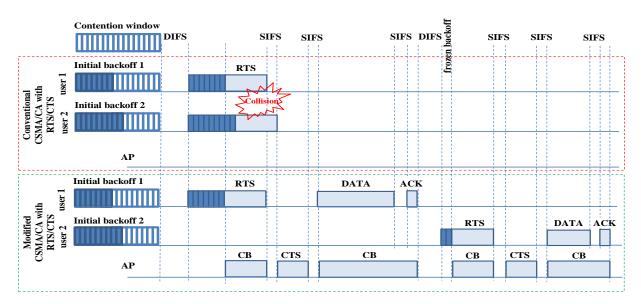


Fig. 3: Conventional and modified four-way handshaking RTS/CTS mechanism

IV. UPLINK THROUGHPUT CALCULATION

A. Uplink Access Protocol

Due to the downlink and uplink asymmetry demand, and because of the ready implementation of CSMA/CA and its capability of being used in hybrid LiFi/WiFi networks and the difficulty of synchronization for TDMA and FDMA being used in uplink, we consider CSMA/CA as the access protocol in the uplink of LiFi networks. CSMA/CA is a multiple access protocol with a binary slotted exponential backoff strategy being used in wireless local area networks (WLANs) [42]. This is known as the collision avoidance mechanism of the protocol. In CSMA/CA, a UE will access the channel when it has data to transmit. Thus, this access protocol uses the available resources efficiently. Once the UE is allowed to access the channel, it can use the whole bandwidth. However, this access protocol cannot directly be used in LiFi networks, because it results in severe "hidden node" problem. Here, we applied two simple modifications to CSMA/CA to minimize the number of collisions in LiFi networks. Firstly, the request-to-send/ clear-to-send (RTS/CTS) packet transmission scheme, which is optional in WLANs should be mandatory in LiFi networks. This is the only way that UEs can notice that the channel is busy in LiFi networks. The reason for this is that different wavelengths are employed in the downlink and uplink of LiFi networks, visible light and infrared, respectively. Thus, the PD at the UE is tuned for visible light and cannot sense the channel when another UE transmits via infrared. Secondly, the AP transmits a channel busy (CB) tone to inform the other UEs that the channel is busy. In the following, the modified CSMA/CA is described in detail.

B. Brief Description of the Access Protocol

In CSMA/CA, UEs listen to the channel prior to transmission for an interval called distributed inter-frame space (DIFS). Then, if there is no CB tone, the channel is found to be idle and the UEs generate a random backoff, \mathcal{B}_i , for

 $j = 1, 2, \dots, N$, where N is the number of competing UEs. The value of \mathcal{B}_i is uniformly chosen in the range [0, w-1], where w is the contention window size. Let $\mathcal{B} = [\mathcal{B}_i]_{1 \times N}$, be the backoff vector of the UEs. After sensing the channel for time interval DIFS, UE_i should wait for $\mathcal{B}_i \times t_{\text{slot}}$ seconds, where $t_{\rm slot}$ is the duration of each time slot. Obviously, the UE with the lowest backoff is prior to transmit, i.e., u_1 th UE, where $u_1 = \arg_i \min(\mathbf{B})$. Then, u_1 th UE sends the RTS frame to the AP before N-1 other UEs. If the RTS frame is received at the AP successfully, it replies after a short inter-frame space (SIFS) with the CTS frame. The u_1 th UE only proceeds to transmit the data frame, after the time interval of SIFS, if it receives the CTS frame. Eventually, an ACK is transmitted after the period of SIFS by the AP to notify the successful packet reception. The AP transmits the CB tone simultaneously with the reception of the RTS packet. The UEs that can hear the CB tone will freeze their backoff counter. The backoff counter will be reactivated when the channel is sensed to be idle again after the period of DIFS. If the AP does not transmit the CB tone, the u_2 th UE who cannot hear the u_1 th UE, will start to send RTS frame after waiting for $\mathcal{B}_{u_2} imes t_{
m slot}$ seconds. Here, the u_2 th UE is called the hidden UE and a collision occurs if $(\mathcal{B}_{u_2} - \mathcal{B}_{u_1}) \times t_{\text{slot}} < t_{\text{RTS}}$, where $t_{\rm RTS}$ is the RTS frame transmission time which is directly proportional to the length of the RTS frame, $L_{\rm RTS}$, and inversely proportional to the uplink rate. The conventional and modified access protocol mechanisms for the case of N=2are illustrated in Fig. 3. As shown in this figure, the issue of the high number of collisions in the conventional CSMA/CA is removed by sending the CB tone during the RTS and data packet transmission.

It is worth mentioning that the CTS packet, CB tone and any other control packets are transmitted on the reserved or dedicated control channels. The mechanism of these channels is similar to WiFi where they are operated on pre-allocated frequencies and specific bandwidth. Since they do not influence the modulated downlink or uplink bandwidth,

the corresponding throughput is not affected [43], [44].

C. Uplink Throughput

In the modified CSMA/CA for LiFi networks, collision only occurs if the backoff time of at least two UEs reach zero simultaneously. Thus, they transmit at the same time and the packets collide. The analysis of normalized throughput and collision probability is the same as the analysis provided in [45]. In the following, we only provide a summary of the equations and further detail is provided in [45]. The normalized uplink throughput is given as:

$$\widetilde{\mathcal{T}}_{\mathbf{u}} = \frac{P_{\mathbf{t}} P_{\mathbf{s}} \mathbb{E}[t_{\mathbf{D}}]}{(1 - P_{\mathbf{t}}) t_{\mathbf{slot}} + P_{\mathbf{t}} P_{\mathbf{s}} \mathbb{E}[t_{\mathbf{s}}] + P_{\mathbf{t}} (1 - P_{\mathbf{s}}) t_{\mathbf{c}}}, \quad (8)$$

where $P_{\rm t}=1-(1-\tau)^N$ is the probability of at least one transmission in the considered backoff slot time, $P_{\rm s}=N\tau(1-\tau)^{N-1}/P_{\rm t}$ is the probability of successful transmission, and $\tau=\frac{2}{w+1}$ is the probability that a UE transmits on a randomly chosen slot time. In (8), $\mathbb{E}[t_{\rm D}]$, $\mathbb{E}[t_{\rm s}]$ and $t_{\rm c}$ are the average transmission time of data packet, the average successful transmission time and collision time, respectively. Assuming that all data packets have the same length, then:

$$\mathbb{E}[t_{\rm s}] = t_{\rm s} = t_{\rm RTS} + {\rm SIFS} + t_{\rm dely} + t_{\rm CTS} + {\rm SIFS} + t_{\rm dely} + t_{\rm HDR} + t_{\rm D} + {\rm SIFS} + t_{\rm dely} + t_{\rm ACK} + {\rm DIFS} + t_{\rm dely},$$

$$\mathbb{E}[t_{\rm D}] = t_{\rm D}, \quad t_{\rm c} = t_{\rm RTS} + {\rm DIFS} + t_{\rm dely}$$
(9)

where $t_{\rm dely}$ is the propagation delay and $t_{\rm HDR}$ is the packet header time which includes both the physical and MAC header. Finally, the uplink throughput of the jth UE can be obtained as follows:

$$R_{\mathbf{u},j} = \frac{\widetilde{\mathcal{T}}_{\mathbf{u}} B_{\mathbf{u},n}}{N} \log_2 \left(1 + \gamma_{\mathbf{u},j} \right). \tag{10}$$

where $B_{\mathbf{u},n}$ is the uplink bandwidth of the nth FR plan and $\gamma_{\mathbf{u},j}$ is the SINR at the AP when communicating with UE_j and it is given as:

$$\gamma_{\mathbf{u},j} = \frac{\left(R_{\mathrm{PD}}P_{\mathrm{u,opt}}H_{i,j}\right)^{2}}{\eta^{2}N_{0}B_{\mathrm{u},n} + \sum_{j \in \Pi}\left(R_{\mathrm{PD}}P_{\mathrm{u,opt}}H_{i,j}\right)^{2}},\tag{11}$$

where Π is the set of other UEs using the same bandwidth as UE_j and communicating with the ith AP, $(i \neq i)$, simultaneously with UE_j ; and $P_{\mathrm{u,opt}}$ is the transmitted uplink power which is assumed to be the same for all UEs.

V. FEEDBACK MECHANISM

Over the last few years, studies have repeatedly illustrated that permitting the receiver to send some information bits about the channel conditions to the transmitter can allow effective resource allocation and downlink throughput enhancement. This feedback information is usually the SINR of a subcarrier at the receiver [7], [10]. However, sending this information is in cost of uplink throughput degradation. Therefore, there is a trade-off between downlink and uplink throughput when the amount of feedback varies. Let's define the feedback factor, ϵ , as the ratio of total feedback time and total transmission time as:

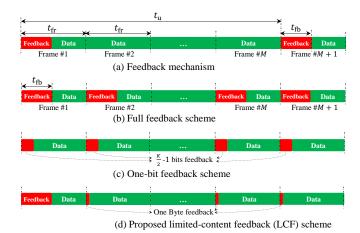


Fig. 4: Feedback schemes.

$$\epsilon = \frac{\sum t_{\rm fb}}{t_{\rm tot}},\tag{12}$$

where $t_{\rm fb}$ is the feedback duration. Fig. 4-(a) denotes a general feedback mechanism, in which feedback information is transmitted periodically after an interval of $t_{\rm u}$. Note that since the feedback information occupies the data portion of the packet, the frame structure remains unchanged. Denoting that the denominator of (12) is the total transmission time which is equal to $t_{\rm tot} = (N_{\rm D} + N_{\rm f})t_{\rm fr}$, where $N_{\rm D}$ and $N_{\rm f}$ are the number of purely data frame and feedback frame in the total transmission time. The total feedback time is $\Sigma t_{\rm fb} = N_{\rm f}t_{\rm fb}$. Replacing these equations in (12), the feedback factor can be obtained as:

$$\epsilon = \frac{N_{\rm f} t_{\rm fb}}{(N_{\rm D} + N_{\rm f}) t_{\rm fr}} = \frac{t_{\rm fb}}{\left(1 + \frac{N_{\rm D}}{N_{\rm f}}\right) t_{\rm fr}}.$$
(13)

Since $t_{\rm tot}=(N_{\rm D}+N_{\rm f})t_{\rm fr}=N_{\rm f}t_{\rm u}$, then $1+\frac{N_{\rm D}}{N_{\rm f}}=\frac{t_{\rm u}}{t_{\rm fr}}$, and substituting it in (13), it can be simplified as:

$$\epsilon = \frac{t_{\rm fb}}{t_{\rm u}}.\tag{14}$$

Then, the uplink throughput of UE_j in consideration of feedback is given by:

$$R_{\mathrm{u},j} = \left(1 - \frac{t_{\mathrm{fb}}}{t_{\mathrm{u}}}\right) \frac{\tilde{\mathcal{T}}_{\mathrm{u}} B_{\mathrm{u},n}}{N} \log_2\left(1 + \gamma_{\mathrm{u},j}\right). \tag{15}$$

Due to the use of DCO-OFDM modulation, the AP requires the SINR information of $\mathcal{K}/2-1$ subcarriers. The extreme and least cases for sending the SINR information are full feedback (FF) and one-bit fixed-rate feedback, respectively. These schemes are shown in Fig. 4-(b) and Fig. 4-(c). In the FF scheme, UEs send the SINR of all subcarriers at the beginning of each data frame. Obviously, this impractical method produces a huge amount of feedback. According to the one-bit feedback technique, the AP sets a threshold for all UEs. Each UE compares the value of its SINR to this threshold. When the SINR exceeds the threshold, a '1' will be transmitted to the AP; otherwise a '0' will be sent. The AP receives feedback from all UEs and then randomly selects a UE whose feedback bit was '1'. The optimal threshold

TABLE I: Simulation Parameters

Parameter	Symbol	Value
Network space	_	$10 \times 10 \times 2.15 \text{ m}^3$
Number of APs	N_{AP}	9
Cell radius	$r_{ m c}$	2.35 m
LED half-intensity angle	$\Phi_{1/2}$	60°
Receiver FOV	$\Psi_{ m c}$	90°
Physical area of a PD	A	1 cm^2
Gain of optical filter	$g_{ m f}$	1
Refractive index	ς	1
PD responsivity	$R_{ m PD}$	1 A/W
Reflection coefficient	$ ho_q$	0.85
Number of subcarriers	\mathcal{K}	2048
Transmitted optical power	$P_{\rm d,opt}$	8 W
Downlink FR bandwidth	$B_{\mathrm{d},n}$	10 MHz
Fitted coefficient	w_0	45.3 Mrad/s
Conversion factor	η	3
Noise power spectral density	N_0	$10^{-21} \text{ A}^2/\text{Hz}$

that provides the maximum expected weighted sum-rate has been calculated in [46]. In this study, we simply choose he threshold to be γ_{\min} which is the minimum possible SNR on all subcarriers. If all the feedback bits received by the AP are zero, then no signal is transmitted in the next time interval. However, in this case, the AP can also randomly choose a UE for data transmission, although for a large number of UEs this method has vanishing benefit over no data transmission when all the received feedback bits are '0' [47].

As can be induced from (14), the feedback factor can generally be reduced by means of either decreasing the content of feedback or increasing the update interval. In the following, we propose the limited-content feedback (LCF) and limited-frequency feedback (LFF) techniques. The former is based on reducing the feedback information in each frame and the latter is based on increasing the update interval.

A. Proposed Limited-content feedback (LCF) Scheme

Unlike RF wireless and optical diffused channels, the frequency selectivity of the channel in LiFi attocell networks is mostly characterized by the limitations of the receiver/transmitter devices (i.e., PD and LED), rather than the multipath nature of the channel [28]. In order to assess the frequency response of the free-space optical channels, computer simulations are conducted. The simulations are performed for a network size of $10 \times 10 \times 2.15$ m³. The network area is divided equally into nine quadrants with one AP located at the center of each. Assume the center of the xy-plane is located in the center of the room as shown in Fig. 1. The other parameters are listed in Table I. The normalized frequency response of the channel gain, $\frac{|H_{i,j}(f)|^2}{|H_{LOS,i,j}(f)|^2}$, for a UE placed at different positions in the room is depicted in Fig. 5. As can be seen, the normalized frequency response fluctuates around the LOS component and the variation of the fluctuation is less than 1 dB. Moreover, the channel gain variation is less significant for UEs that are further away from the walls of the room, due to the lower significance of the first order reflection [25]. Accordingly, the frequency selectivity of LiFi channels is mainly dominated by LED and PD components, and the frequency selectivity of these devices are relatively deterministic although not frequency flat. The average received power at the UE is much more dynamic and is significantly dependent on the position of the UE. Therefore, by only updating the average power, a reasonable estimate of the SINR of all the subcarriers can be obtained. This idea forms the foundation of our LCF scheme.

Fig. 4-(d) represents the principal working mechanism of our proposed LCF scheme. According to the LCF scheme, when a UE connects to an AP, it sends the SINR information of all subcarriers only once at the beginning of the first frame. For the following frames, and as long as the UE is connected to the same AP, it only updates the scheduler on its received average power (i.e., the DC channel component). Once the UE connects to a new AP, it will transmit the SINR information of all subcarriers again. The proposed LCF scheme then simply scales the individual SINR values received in the next frames such that the total average power matches the updated average power [48]. Thus, the estimated SINR on kth subcarrier of jth UE at time instance t is given as:

$$\hat{\gamma}_{\mathrm{d},j,k}(t) \approx \gamma_{\mathrm{d},j,k}(0) \times \frac{\gamma_{\mathrm{d},j,0}(t)}{\gamma_{\mathrm{d},j,0}(0)},\tag{16}$$

where $\gamma_{d,j,k}(0)$ is the downlink SINR of the *j*th UE on the *k*th subcarrier at t=0. The scheduler uses this estimated SINR information for subcarrier allocation according to (5).

The most salient difference between the LCF technique and the one-bit feedback method is that the AP does not have any knowledge about the SINR value of each subcarrier and it just knows that the SINR is above or lower than a predetermined threshold for the one-bit feedback technique. However, thanks to the use of LCF approach, the AP can have an estimation of the SINR value for each subcarrier. In order to compare the downlink performance of FF, one-bit feedback and LCF, Monte-Carlo simulations are executed. The simulation tests are carried out 10^3 times per various number of UEs, and with the parameters given in Table I. In each run, the UEs' locations are chosen uniformly random in the room. Once they settle in the new locations, they update the AP about their subcarrier SINR as explained. Then, the AP, reschedule the resources based on (5). The request data rate of UEs are assumed to be the same. Fig. 6 illustrates the average downlink throughput versus different number of UEs for LCF, FF and one-bit feedback schemes. As can be seen from the results, the performance of the LCF is better than the one-bit feedback scheme and nearly similar to FF scheme. As the number of UEs increase, the gap between the considered feedback schemes also increases. However, the LCF follows the FF fairly good especially for low data request rate. Moreover, compared to the one-bit feedback technique, the LCF scheme occupies less portion of the uplink bandwidth.

B. Proposed Limited-frequency feedback (LFF) Scheme

Due to the slowly-varying nature of the indoor LiFi channels, the UE can update the AP about its channel condition less frequently, especially when the UE is immobile or it moves slowly [49]. The channel variation in OWCs is mainly due to UE's movement and/or its rotation. Varying channel may lead to UE's throughput reduction due to the difference between the current channel and the estimated one.

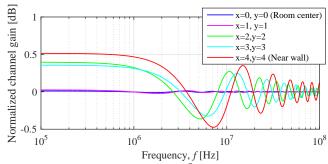


Fig. 5: Normalized channel gain, $\frac{|H_{i,j}(f)|^2}{|H_{\text{LOS},i,j}(f)|^2}$, for different room positions.

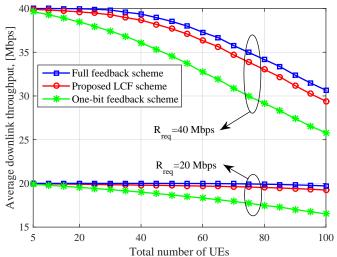


Fig. 6: Average downlink throughput for different feedback schemes (average request data rate: 20 Mbps and 40 Mbps).

Thus, the AP requires feedback about the current channel condition of the UE to allocate resources efficiently. In this study, we only consider the change of channel due to UE's movement. Based on the information of the UE's velocity, we aim to find the appropriate channel update interval, $t_{\rm u}$, so that the expected weighted average sum throughput of uplink and downlink per user is maximized. Weighted sum throughput maximization is commonly used to optimize the overall throughput for bidirectional communications [50], [51]. The optimization problem (OP) is formulated as:

$$\max_{t_{\mathrm{u}}} \left(\mathbb{E}_{[\mathbf{ro}],[\boldsymbol{\theta}]} \left[\frac{1}{N} \sum_{j=1}^{N} \left(w_{\mathrm{d}} \overline{R}_{\mathrm{d},j}(t_{\mathrm{u}}) + w_{\mathrm{u}} \overline{R}_{\mathrm{u},j}(t_{\mathrm{u}}) \right) \right] \right),$$

where $\overline{R}_{\mathrm{d},j}$ and $\overline{R}_{\mathrm{u},j}$ are the average downlink and uplink throughput of jth UE, respectively; Note that $[\boldsymbol{r}_0] = [r_{01},\cdots,r_{0N}]$ and $[\boldsymbol{\theta}] = [\theta_1,\cdots,\theta_N]$ are random variable vectors with i.i.d entities; $\mathbb{E}_{[\boldsymbol{r}_0],[\boldsymbol{\theta}]}[\cdot]$ is the expectation with respect to the joint PDF $f([\boldsymbol{r}_0],[\boldsymbol{\theta}]) = f(r_{01},\cdots,r_{0N},\theta_1,\cdots,\theta_N)$. Since r_{0j} 's and θ_j 's are i.i.d, we have $f([\boldsymbol{r}_0],[\boldsymbol{\theta}]) = f_{\mathcal{R}_0}(r_{0j})f_{\Theta}(\theta_j)\prod_{i\neq j}f_{\mathcal{R}_0}(r_{0i})f_{\Theta}(\theta_i)$, where $f_{\mathcal{R}_0}(r_{0j})$ and $f_{\Theta}(\theta_j)$ are described in Section II. The expectation can go inside the summation, then, we have $\mathbb{E}_{[\boldsymbol{r}_0],[\boldsymbol{\theta}]}\left[\overline{R}_{\mathrm{d},j}(t_{\mathrm{u}})\right] = \mathbb{E}_{r_{0j},\theta_j}\left[\overline{R}_{\mathrm{d},j}(t_{\mathrm{u}})\right]$ for downlink and $\mathbb{E}_{[\boldsymbol{r}_0],[\boldsymbol{\theta}]}\left[\overline{R}_{\mathrm{u},j}(t_{\mathrm{u}})\right] = \mathbb{E}_{r_{0j},\theta_j}\left[\overline{R}_{\mathrm{u},j}(t_{\mathrm{u}})\right]$ for uplink. Since

 r_{0i} 's and θ_{i} 's are i.i.d, then:

$$\mathbb{E}_{r_{01},\theta_{1}}[\overline{R}_{\mathrm{d},1}(t_{\mathrm{u}})] = \cdots = \mathbb{E}_{r_{0N},\theta_{N}}[\overline{R}_{\mathrm{d},N}(t_{\mathrm{u}})] \triangleq \mathbb{E}_{r_{0},\theta}[\overline{R}_{\mathrm{d}}(t_{\mathrm{u}})]$$

$$\mathbb{E}_{r_{01},\theta_{1}}[\overline{R}_{\mathrm{u},1}(t_{\mathrm{u}})] = \cdots = \mathbb{E}_{r_{0N},\theta_{N}}[\overline{R}_{\mathrm{u},N}(t_{\mathrm{u}})] \triangleq \mathbb{E}_{r_{0},\theta}[\overline{R}_{\mathrm{u}}(t_{\mathrm{u}})].$$

After substituting above equations in (17) and some manipulations, the OP can be expressed as:

$$\max_{t_{\mathrm{u}}} \left(\overline{\mathcal{T}} = w_{\mathrm{u}} \mathbb{E}_{r_{0},\theta} \left[\overline{R}_{\mathrm{u}}(t_{\mathrm{u}}) \right] + w_{\mathrm{d}} \mathbb{E}_{r_{0},\theta} \left[\overline{R}_{\mathrm{d}}(t_{\mathrm{u}}) \right] \right), \quad (18)$$

which is not dependent on any specific UEs. The average is calculated over one update interval, since it is assumed the UE feeds its velocity information back to the AP after each update interval. The opposite behaviour of \overline{R}_u and \overline{R}_d with respect to the update interval (the former directly and the latter inversely are proportional to the update interval), results in an optimum point for $\overline{\mathcal{T}}$. In the following, \overline{R}_u and \overline{R}_d are calculated with some simplifying assumptions.

The exact and general state of SINR at the receiver is provided in (7). However, for ease of analytical derivations, it can be simplified under some reasonable assumptions including: i) the interference from other APs can be neglected due to employing FR plan, ii) $H_{i,j,k} \approx H_{\text{LOS},i,j}$. The latter assumption is based on the fact that in OWC systems, $H_{\text{LOS},i,j} >> H_{\text{NLOS},i,j}$. It was shown in Fig. 5 that the variation of the frequency response fluctuation around the LOS component is less than 1 dB. Using Fig. 1, $\cos\phi_{ij} = \cos\psi_{ij} = h/d_{ij}$, can be substituted in (1), then, the DC gain of the LOS channel is $H_{\text{LOS},i,j} = G_0/d_{ij}^{m+3}$, where $G_0 = \frac{(m+1)A}{2\pi\sin^2\psi_c}g_f\varsigma^2h^{m+1}$. Hence, the approximate and concise equation of SINR at the kth subcarrier of the jth UE is given by:

$$\gamma_{j,k} \approx \frac{Ge^{\frac{-4\pi k B_{\mathrm{d},n}}{\mathcal{K}w_0}}}{\left(r_j^2 + h^2\right)^{m+3}},\tag{19}$$

where $G = \frac{\mathcal{K}G_0^2 R_{\mathrm{PD}}^2 P_{\mathrm{d,opt}}^2}{(\mathcal{K}-2)\eta^2 N_0 B_{\mathrm{d,}n}}$ and r_j is the distance between the UE_j and the center of the cell which is located in it. Substituting (19) in (6), the downlink throughput is given as:

$$R_{d,j} = \frac{B_{d,n}}{\mathcal{K}} \sum_{k=1}^{\frac{\kappa}{2}-1} \log_2 \left(1 + s_{j,k} \frac{Ge^{\frac{-4\pi k B_{d,n}}{\kappa w_0}}}{\left(r_j^2 + h^2\right)^{m+3}} \right). \tag{20}$$

Noting that typically in LiFi cellular networks using FR, SINR values are high enough, we have:

$$R_{d,j} = \frac{B_{d,n}}{\mathcal{K}} \sum_{k=1}^{\frac{\kappa}{2} - 1} s_{j,k} \log_2 \left(\frac{Ge^{\frac{-4\pi k B_{d,n}}{\mathcal{K}w_0}}}{\left(r_j^2 + h^2\right)^{m+3}} \right). \tag{21}$$

The same approximations can be also considered for uplink throughput. Define $G_{\rm u}=\frac{(G_0R_{\rm PD}P_{\rm u,opt})^2}{\eta^2N_0B_{\rm u,n}}$, then, the SINR at the AP is $\gamma_{{\rm u},j}\!=\!G_{\rm u}/(r_j^2+h^2)^{m+3}$. Substituting it in (15), the uplink throughput of UE_j can approximately be obtained as:

$$R_{\mathrm{u},j} \cong \left(1 - \frac{t_{\mathrm{fb}}}{t_{\mathrm{u}}}\right) \frac{\widetilde{\mathcal{T}}_{\mathrm{u}} B_{\mathrm{u},n}}{N} \log_2 \left(\frac{G_{\mathrm{u}}}{\left(r_i^2 + h^2\right)^{m+3}}\right). \tag{22}$$

Without loss of generality and for ease of notations, we consider one of the N UEs for rest the of derivations and remove the subscript j. The average uplink throughput over one update interval is given as:

$$\begin{split} & \overline{R}_{\mathbf{u}} = \left(1 - \frac{t_{\text{fb}}}{t_{\mathbf{u}}}\right) \frac{\widetilde{\mathcal{T}}_{\mathbf{u}} B_{\mathbf{u},n}}{N} \frac{1}{t_{\mathbf{u}}} \int_{0}^{t_{\mathbf{u}}} \log_{2} \left(\frac{G_{\mathbf{u}}}{(r^{2}(t) + h^{2})^{m+3}}\right) dt \\ & = \frac{2(m+3)\widetilde{\mathcal{T}}_{\mathbf{u}} B_{\mathbf{u},n}}{N} \left(1 - \frac{t_{\text{fb}}}{t_{\mathbf{u}}}\right) \left(\frac{1}{2(m+3)} \log_{2} \left(\frac{G_{\mathbf{u}}}{(r^{2}(t_{\mathbf{u}}) + h^{2})^{m+3}}\right) \\ & - \frac{(h^{2} + r_{0}^{2} \sin^{2} \theta)^{\frac{1}{2}}}{v t_{\mathbf{u}} \ln(2)} \tan^{-1} \left(\frac{v t_{\mathbf{u}} - r_{0} \cos \theta}{(h^{2} + r_{0}^{2} \sin^{2} \theta)^{\frac{1}{2}}}\right) + \frac{1}{\ln(2)} \\ & + \frac{r_{0} \cos \theta}{2v t_{\mathbf{u}}} \log_{2} \left(\frac{r^{2}(t_{\mathbf{u}}) + h^{2}}{r_{0}^{2} + h^{2}}\right) - \frac{(h^{2} + r_{0}^{2} \sin^{2} \theta)^{\frac{1}{2}}}{v t_{\mathbf{u}} \ln(2)} \tan^{-1} \left(\frac{r_{0} \cos \theta}{(h^{2} + r_{0}^{2} \sin^{2} \theta)^{\frac{1}{2}}}\right). \end{split}$$

The average downlink throughput over one update interval can be obtained as:

$$\overline{R}_{d} = \frac{B_{d,n}}{\mathcal{K}t_{u}} \int_{0}^{t_{u}} \sum_{k=1}^{k_{req}} \log_{2} \left(\frac{Ge^{\frac{-4\pi k B_{d,n}}{\mathcal{K}w_{0}}}}{(r^{2}(t) + h^{2})^{m+3}} \right) dt$$

$$= \frac{k_{req}B_{d,n}}{\mathcal{K}t_{u}} \int_{0}^{t_{u}} \log_{2} \left(\frac{Ge^{-2\pi (k_{req}+1)B_{d,n}/\mathcal{K}w_{0}}}{(r^{2}(t) + h^{2})^{m+3}} \right) dt$$

$$= \frac{2(m+3)k_{req}B_{d,n}}{\mathcal{K}} \left(\frac{1}{2(m+3)} \log_{2} \left(\frac{Ge^{-2\pi (k_{req}+1)B_{d,n}/\mathcal{K}w_{0}}}{(r^{2}(t_{u}) + h^{2})^{m+3}} \right) - \frac{(h^{2} + r_{0}^{2} \sin^{2}\theta)^{\frac{1}{2}}}{vt_{u} \ln(2)} \tan^{-1} \left(\frac{vt_{u} - r_{0} \cos\theta}{(h^{2} + r_{0}^{2} \sin^{2}\theta)^{\frac{1}{2}}} \right) + \frac{1}{\ln(2)}$$

$$+ \frac{r_{0} \cos\theta}{2vt_{u}} \log_{2} \left(\frac{r^{2}(t_{u}) + h^{2}}{r_{0}^{2} + h^{2}} \right) - \frac{(h^{2} + r_{0}^{2} \sin^{2}\theta)^{\frac{1}{2}}}{vt_{u} \ln(2)} \tan^{-1} \left(\frac{r_{0} \cos\theta}{(h^{2} + r_{0}^{2} \sin^{2}\theta)^{\frac{1}{2}}} \right) \right). \tag{24}$$

where k_{req} is the required number of subcarriers to be allocated to the UE at t=0. With the initial and random distance of r_0 from the cell center, the required number of subcarriers can approximately be obtained as:

$$k_{\text{req}} \cong \frac{\mathcal{K}R_{\text{req}}}{B_{\text{d},n}\log_2\left(G/(r_0^2 + h^2)^{m+3}\right)}$$
 (25)

The exact value and proof are given in Appendix-A. Both the average uplink and downlink throughput given in (23) and (24), respectively, are continuous and derivative in the range $(0,2r_{\rm c}/v)$. Therefore, we can express the following proposition to find the optimal update interval that results in the maximum sum-throughput.

Proposition. Let t_u be continuous in the range of $(0, 2r_c/v)$. The optimal solution to the OP given in (18) can be obtained by solving the following equation:

$$\mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{\mathcal{T}}}{\partial t_{\mathbf{u}}} \right] = w_{\mathbf{u}} \mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{\mathcal{T}}_{\mathbf{u}}}{\partial t_{\mathbf{u}}} \right] + w_{\mathbf{d}} \mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{\mathcal{T}}_{\mathbf{d}}}{\partial t_{\mathbf{u}}} \right] = 0.$$
(26)

For $vt_u \ll h$, the root of (26) can be well approximated as:

$$\widetilde{t}_{\text{u,opt}} \cong \left(\frac{\frac{3\ln(2)}{2(m+3)} w_{\text{u}} t_{\text{fb}} \widetilde{\mathcal{T}}_{\text{u}} B_{\text{u},n} C_1}{w_{\text{d}} v^2 N R_{\text{req}} + C_2 w_{\text{u}} v^2 \widetilde{\mathcal{T}}_{\text{u}} B_{\text{u},n}} \right)^{\frac{1}{3}},$$
 (27)

where

$$C_{1} = \frac{\mathbb{E}_{r_{0}} \left[\log_{2} \left(\frac{G_{u}}{(r_{0}^{2} + h^{2})^{m+3}} \right) \right] \mathbb{E}_{r_{0}} \left[\log_{2} \left(\frac{G}{(r_{0}^{2} + h^{2})^{m+3}} \right) \right]}{\mathbb{E}_{r_{0}, \theta} \left[\frac{(h^{2} + r_{0}^{2} \sin^{2} \theta)^{2}}{(h^{2} + r_{0}^{2})^{3}} \right]},$$

$$C_{2} = \mathbb{E}_{r_{0}} \left[\log_{2} \left(\frac{G}{(r_{0}^{2} + h^{2})^{m+3}} \right) \right].$$
(28)

TABLE II: Uplink simulation parameters

Parameter	Symbol	Value
Transmitted uplink optical power	$P_{\mathrm{u,opt}}$	0.2 W
Uplink FR bandwidth	$B_{\mathrm{u},n}$	5 MHz
Average length of uplink payload	L_{D}	2000 B
Physical header	H_{PHY}	128 b
MAC header	H_{MAC}	272 b
RTS packet size	$L_{ m RTS}$	288 b
CTS packet size	$L_{\rm CTS}$	240 b
ACK packet size	L_{ACK}	240 b
SIFS		$16~\mu \mathrm{s}$
DIFS		$32~\mu \mathrm{s}$
Backoff slot duration	$t_{ m slot}$	$8~\mu s$
Propagation delay	$t_{ m delay}$	$1~\mu \mathrm{s}$
Feedback time	$t_{ m fb}$	0.8 ms

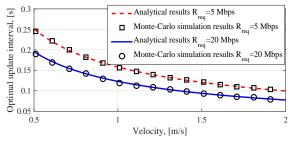
Proof: See Appendix-B

As it can be seen from (27), the optimum update interval depends on both physical and MAC layer parameters. Among them, the UE velocity affects the update interval more than others. Let's fix the other parameters, then $\widetilde{t}_{\mathrm{u,opt}} = C_{\mathrm{const}}/v^{\frac{2}{3}}$,

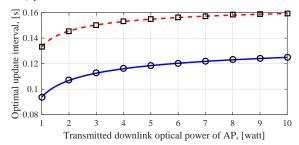
where $C_{\mathrm{const}} = \left(\frac{\frac{3\ln(2)}{2(m+3)}w_{\mathrm{u}}t_{\mathrm{fb}}\tilde{T}_{\mathrm{u}}B_{\mathrm{u},n}C_{1}}{w_{\mathrm{d}}R_{\mathrm{req}} + C_{2}w_{\mathrm{u}}\tilde{T}_{\mathrm{u}}B_{\mathrm{u},n}}\right)^{\frac{1}{3}}$. We study the effect of the UE's velocity and transmitted downlink optical power on the update interval as illustrated in Fig. 7. Analytical and Monte-Carlo simulations are presented for $w_{\rm u}=w_{\rm d}$, N=5 and with the downlink and uplink simulation parameters given in Table I and Table II, respectively. For a fixed t_u, Monte-Carlo simulations are accomplished 10⁴ times, where in each run, the UE's initial position and direction of movement are randomly chosen. Then, for the considered t_{11} , the expected sum-throughput, $\overline{\mathcal{T}}$, can be obtained by averaging out over 10⁴ runs. Afterwards, based on the greedy search and for different $t_{\rm u}$, varying in the range $0 < t_{\rm u} < 2r_{\rm c}/v$, Monte-Carlo simulations are repeated. The optimal update interval corresponds to the maximum sum-throughput. The effect of UE's velocity on optimal update interval for $R_{\rm reg} = 5$ Mbps and $R_{\text{req}} = 20$ Mbps is shown in Fig. 7-(a). Here, we can see the optimal update interval decrease rapidly as UE's speed increases, according to $v^{-2/3}$. Further, Monte-Carlo simulations confirm the accuracy of analytical results provided in (27). Fig. 7-(b) illustrates the saturated effect of transmitted optical power on $t_{u,opt}$. As can be observed, the variation of the optimal update interval due to the alteration of $P_{d,opt}$ is less than 30 ms. From both Fig. 7-(a) and Fig. 7-(b), it can be deduced the lower R_{req} , the higher $t_{\text{u,opt}}$.

Now let's consider an overloaded multi-user scenario with N users. The fair scheduler introduced in (5) tries to equalize the rate of all UEs. For high number of subcarriers, the UEs achieve approximately the same data rate. Accordingly, the on average achieved data rate of UEs in an overloaded network for high number of subcarriers would nearly be $\lambda R_{\rm req}$, where $0 < \lambda < 1$. This system is equivalent to a non-overloaded multi-user system where all UEs have achieved on average their request rate of $\lambda R_{\rm req}$. Then, the approximate optimal update interval that results in near-maximum sum-throughput is given as:

$$\widetilde{t}_{\text{u,opt}} \cong \left(\frac{\frac{3\ln(2)}{2(m+3)} w_{\text{u}} t_{\text{fb}} \widetilde{\mathcal{T}}_{\text{u}} B_{\text{u},n} C_1}{w_{\text{d}} v^2 N \lambda R_{\text{req}} + C_2 w_{\text{u}} v^2 \widetilde{\mathcal{T}}_{\text{u}} B_{\text{u},n}} \right)^{\frac{1}{3}}.$$
(29)



(a) The effect of UE's velocity on optimal update interval $(P_{\rm d,opt}=8{
m watt}).$



(b) The effect of transmitted downlink optical power on optimal update interval ($v=1~{\rm m/s}$).

Fig. 7: The effects of UE's velocity and downlink optical power on optimal update interval for $R_{\rm req}=5$ Mbps and $R_{\rm req}=20$ Mbps, and $N\!=\!5$.

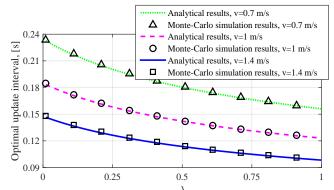


Fig. 8: Optimal update interval versus overload parameter, λ , for different UE's velocity (N=5).

Analytical and Monte-Carlo simulations of an overloaded system are shown in Fig. 8. Three speed values are chosen around the average human walking speed which is 1.4 m/s [52]. Note that to obtain an overloaded system either the number of UEs or their request data rate can be increased. In the results shown in Fig. 8, we fixed the number of UEs to N=5 and increased their $R_{\rm req}$. As can be inferred from these results, as the network becomes more overloaded, the optimal update interval should be increased. The reason for this is that in an overloaded network, due to lack of enough resources updating the AP frequently is useless and it just wastes the uplink resources.

To verify the significance of the update interval in practical systems, three scenarios have been considered. Scenario I: a system without any update interval; Scenario II: a system with the conventional fixed update interval but without looking at the UE's velocity; Scenario III: a system with the proposed update interval and adjustable with the UE's velocity. For

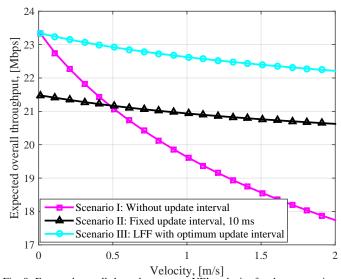


Fig. 9: Expected overall throughput versus UE's velocity for three scenarios; and $R_{\rm req}=20$ Mbps, $w_{\rm u}=w_{\rm d}=1$.

these scenarios, Monte-Carlo simulation results of expected sum-throughput versus different UE's velocity have been obtained and presented in Fig. 9. In scenario I, the UEs only update the AP once at the start of the connection by transmission of the SINR information of $\mathcal{K}/2-1$ subcarriers. For scenario II, the fixed update interval is considered to be $t_{\rm u}=10$ ms and independent of UE's velocity. Fixed update interval is currently used in LTE with $t_{\rm u}=10$ ms by transmission of one-bit feedback information at the beginning of every frame [53]. It is worth mentioning that for practical wireless systems, it is common to transmit feedback frequently, e.g., at the beginning of each frame regardless of the UE channel variation and velocity. As can be seen from the results, the proposed LFF scheme outperforms the conventional method with fixed update interval. For low speeds (up to 0.5 m/s), the conventional fixed update interval even falls behind the system without any update interval. This is due to redundant feedback information being sent to the AP. The gap between LFF and scenario II with fixed update interval is due to both higher uplink and downlink throughput of LFF. LFF provides higher uplink throughput thanks to transmission of lower feedback compared to fixed update interval scheme. Also, in scenario II, the UEs after 10 ms update the AP with one bit per subcarrier, and the AP does not know the SINR value of each subcarrier to allocate them efficiently to the UEs.

C. LF Schemes Comparison

A comparison between the FF, one-bit, LCF and LFF schemes in case of transmitted overhead is given in Table III. It is assumed that the SINR on each subcarrier can be fedback to the AP using $\mathscr B$ bits, and $M=[\widetilde t_{\mathrm{u,opt}}/t_{\mathrm{fr}}].$ Note that for $M\geq (\mathscr B+1)$, the overhead per frame of the LFF scheme is lower than the one-bit feedback technique. Also, for $M\geq \mathcal K/2$, LFF scheme produces lower overhead per frame in comparison to LCF. For N=5, $\mathscr B=10$, $t_{\mathrm{fr}}=1.6$ ms and $R_{\mathrm{req}}=5$ Mbps the overhead per frame versus different number of subcarriers are illustrated in Fig. 10. The rest of

TABLE III: Comparison of feedback schemes in case of overhead

Scheme	Overhead
Full feedback	$\mathscr{B}(\mathcal{K}/2-1)$ bpf
One-bit feedback	$(\mathcal{K}/2-1)$ bpf
Proposed LCF	₿ bpf
Proposed LFF	$\mathscr{B}(\mathcal{K}/2-1)/M$ bpf

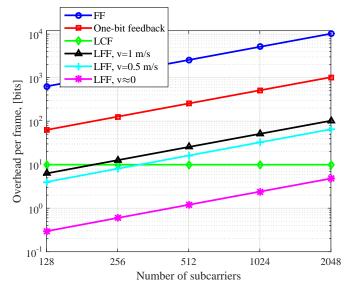


Fig. 10: Transmitted overhead versus different number of subcarriers.

parameters are the same as given in Table I and Table II. As can be observed from Fig. 10, the FF scheme generates a huge amount of feedback overhead especially for a high number of subcarriers. The practical one-bit feedback reduces the overhead by a factor of \mathcal{B} . As can be seen, the LCF always falls below the one-bit feedback method. The gap between LCF and one-bit feedback becomes remarkable for a higher number of subcarriers. The overhead results of the LFF have been also presented for stationary UEs and UEs with low and normal speed. Clearly, the LFF generates the lower feedback overhead per frame as the UE's velocity tends to zero. The expected sum-throughput of different feedback schemes with the same parameters as mentioned above are summarized in Table. IV. As we expected, the LFF outperforms the other schemes when the UEs are stationary. However, the sum-throughput of the LCF method is higher for mobile UEs.

VI. CONCLUSION AND FUTURE WORKS

Two methods for reducing the feedback cost were proposed in this paper: *i*) the limited-content feedback (LCF) scheme, and *ii*) the limited-frequency feedback (LFF) method. The former is based on reducing the content of feedback information by only sending the SINR of the first subcarrier and estimating the SINR of other subcarriers at the AP. The latter is based on the less frequent transmission of feedback information. The optimal update interval was derived, which results in a maximum expected sum-throughput of uplink and downlink. The Monte-Carlo simulations confirmed the accuracy of analytical results. The effect of different parameters on optimum update interval was studied. It was also shown that the proposed LCF and LFF schemes provide

TABLE IV: Comparison of feedback schemes in case of expected sum-throughput, N=5, $R_{\rm req}=5$ Mbps and $w_{\rm u}=w_{\rm d}=1$.

Scheme	Expected sum-throughput $(v = 0 \text{ m/s})$	Expected sum-throughput $(v = 1 \text{ m/s})$
Full feedback	6.67 Mbps	6.67 Mbps
One-bit feedback	7.64 Mbps	7.47 Mbps
Proposed LCF	8.33 Mbps	8.33 Mbps
Proposed LFF	8.35 Mbps	8.08 Mbps

better sum-throughput while transmitting lower amount of feedback compared to the practical one-bit feedback method. The combination of the LCF with the update interval is the topic of our future studies.

APPENDIX

A. Proof of (25)

According to the RWP mobility model, the UE is initially located at \mathbf{P}_0 with the distance r_0 from cell center. The scheduler at the AP is supposed to allocate the resources to the UEs as much as they require. Thus, the achievable data throughput of the UE at t=0 is equal to the requested data rate i.e., $R(0)=R_{\rm req}$. Hence, $k_{\rm req}$ can be obtained by solving the following equation:

$$R_{\text{req}} = \frac{B_{\text{d},n}}{\mathcal{K}} \sum_{k=1}^{k_{\text{req}}} \log_2 \left(\frac{Ge^{\frac{-4\pi k B_{\text{d},n}}{\mathcal{K} w_0}}}{(h^2 + r_0^2)^{m+3}} \right)$$

$$= \frac{B_{\text{d},n}}{\mathcal{K}} \sum_{k=1}^{k_{\text{req}}} \log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}} \right) + \frac{B_{\text{d},n}}{\mathcal{K}} \sum_{k=1}^{k_{\text{req}}} \log_2 \left(e^{\frac{-4\pi k B_{\text{d},n}}{\mathcal{K} w_0}} \right)$$

$$= \frac{k_{\text{req}} B_{\text{d},n}}{\mathcal{K}} \log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}} \right) - \frac{4\pi}{w_0} \left(\frac{B_{\text{d},n}}{\mathcal{K}} \right)^2 \log_2 e^{\sum_{k=1}^{k_{\text{req}}} k}$$

$$= \frac{k_{\text{req}} B_{\text{d},n}}{\mathcal{K}} \log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}} \right) - \frac{2\pi}{w_0} \left(\frac{B_{\text{d},n}}{\mathcal{K}} \right)^2 (\log_2 e) k_{\text{req}}(k_{\text{req}} + 1)$$

$$\Rightarrow k_{\text{req}}^2 + \left(1 - \frac{\log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}} \right)}{\frac{2\pi B_{\text{d},n}}{\mathcal{K} w_0} \log_2 e} \right) k_{\text{req}} + \frac{R_{\text{req}}}{\frac{2\pi}{w_0} \left(\frac{B_{\text{d},n}}{\mathcal{K}} \right)^2 \log_2 e}$$

$$(30)$$

The above equation is a quadratic equation and it has two roots where the acceptable k_{req} can be obtained as follows:

$$k_{\rm reg} =$$

$$\frac{\left(\frac{\log_2\left(\frac{G}{(h^2 + r_0^2)^{m+3}}\right)}{\frac{2\pi B_{d,n}}{\mathcal{K}w_0}\log_2 e} - 1\right) - \sqrt{\left(1 - \frac{\log_2\left(\frac{G}{(h^2 + r_0^2)^{m+3}}\right)}{\frac{2\pi B_{d,n}}{\mathcal{K}w_0}\log_2 e}\right)^2 - \frac{4R_{req}}{\frac{2\pi}{w_0}\left(\frac{B_{d,n}}{\mathcal{K}}\right)^2\log_2 e}}$$

$$\frac{2}{2} \tag{31}$$

If $R_{\mathrm{req}} \ll \frac{w_0}{8\pi} \log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}}\right)$, the approximate number of required subcarriers is $k_{\mathrm{req}} \cong \frac{\mathcal{K}R_{\mathrm{req}}}{B_{\mathrm{d},n} \log_2 \left(\frac{G}{(h^2 + r_0^2)^{m+3}}\right)}$.

B. Proof of Proposition

The optimal solution of the OP given in (18) can be obtained by finding the roots of its derivation that

 1 With the parameters given in Table I the constraint on the requested data rate is $R_{\rm req} << 350$ Mbps.

is $\frac{\partial \mathbb{E}_{r_0,\theta}[\overline{T}]}{\partial t_\mathrm{u}} = w_\mathrm{u} \frac{\partial \mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{u}]}{\partial t_\mathrm{u}} + w_\mathrm{d} \frac{\partial \mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{d}]}{\partial t_\mathrm{u}} = 0$. The expectation value of the average downlink throughput is $\mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{d}] = \iint_{r_0,\theta} \overline{R}_\mathrm{d} f_{\mathcal{R}_0}(r_0) f_\Theta(\theta) \mathrm{d}\theta \mathrm{d}r_0$ and its derivation is equal to $\frac{\partial \mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{d}]}{\partial t_\mathrm{u}} = \frac{\partial}{\partial t_\mathrm{u}} \iint_{r_0,\theta} \overline{R}_\mathrm{d} f_{\mathcal{R}_0}(r_0) f_\Theta(\theta) \mathrm{d}\theta \mathrm{d}r_0$. Since the function inside the integral is derivative on the range $(0,2r_\mathrm{c}/v)$, the derivation operator can go inside the integral as $\iint_{r_0,\theta} \frac{\partial \overline{R}_\mathrm{d}}{\partial t_\mathrm{u}} f_{\mathcal{R}_0}(r_0) f_\Theta(\theta) \mathrm{d}\theta \mathrm{d}r_0$ [54], and this is the expectation value of the derivation of the average downlink throughput, i.e., $\mathbb{E}_{r_0,\theta}[\frac{\partial \overline{R}_\mathrm{d}}{\partial t_\mathrm{u}}]$. Thus, we can conclude that $\frac{\partial \mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{d}]}{\partial t_\mathrm{u}} = \mathbb{E}_{r_0,\theta}[\frac{\partial \overline{R}_\mathrm{d}}{\partial t_\mathrm{u}}]$. Using the same methodology for uplink throughput we have $\frac{\partial \mathbb{E}_{r_0,\theta}[\overline{R}_\mathrm{u}]}{\partial t_\mathrm{u}} = \mathbb{E}_{r_0,\theta}[\frac{\partial \overline{R}_\mathrm{u}}{\partial t_\mathrm{u}}]$. Then, the derivation of (17) can be expressed as:

$$\mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{\mathcal{T}}}{\partial t_{\mathbf{u}}} \right] = w_{\mathbf{u}} \mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{R}_{\mathbf{u}}}{\partial t_{\mathbf{u}}} \right] + w_{\mathbf{d}} \mathbb{E}_{r_0,\theta} \left[\frac{\partial \overline{R}_{\mathbf{d}}}{\partial t_{\mathbf{u}}} \right]. \quad (32)$$

Hence, the root of $\mathbb{E}_{r_0,\theta}[\frac{\partial \overline{T}}{\partial t_{\mathrm{u}}}] = 0$ will be the same as the root of $\frac{\partial \mathbb{E}_{r_0,\theta}[\overline{T}]}{\partial t_{\mathrm{u}}} = 0$.

Using the Leibniz integral rule the derivation of (23) can be obtained as:

$$\begin{split} &\frac{\partial \overline{R}_{\mathrm{u}}}{\partial t_{\mathrm{u}}} = \frac{-2(m+3)\widetilde{T}_{\mathrm{u}}B_{\mathrm{u},n}}{Nt_{\mathrm{u}}^{2}} \left(1 - \frac{2t_{\mathrm{fb}}}{t_{\mathrm{u}}}\right) \left(\frac{t_{\mathrm{u}}}{2(m+3)}\log_{2}\left(\frac{G_{\mathrm{u}}}{(r^{2}(t_{\mathrm{u}}) + h^{2})^{m+3}}\right) \\ &- \frac{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}{v\ln(2)} \tan^{-1} \left(\frac{vt_{\mathrm{u}} - r_{0}\cos\theta}{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}\right) + \frac{r_{0}\cos\theta}{2v}\log_{2}\left(r^{2}(t_{\mathrm{u}}) + h^{2}\right) \\ &- \frac{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}{v\ln(2)} \tan^{-1} \left(\frac{r_{0}\cos\theta}{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}\right) - \frac{r_{0}\cos\theta}{2v}\log_{2}\left(r_{0}^{2} + h^{2}\right) \\ &+ \frac{t_{\mathrm{u}}}{\ln(2)}\right) + \frac{\widetilde{T}_{\mathrm{u}}B_{\mathrm{u},n}}{Nt_{\mathrm{u}}}\left(1 - \frac{t_{\mathrm{fb}}}{t_{\mathrm{u}}}\right)\log_{2}\left(\frac{G_{\mathrm{u}}}{(r^{2}(t_{\mathrm{u}}) + h^{2})^{m+3}}\right) \end{split} \tag{33}$$

Using the sum of inverse tangents formula, $\tan^{-1}(a) + \tan^{-1}(b) = \tan^{-1}\left(\frac{a+b}{1-ab}\right)$, (33) can be further simplified as:

$$\begin{split} &\frac{\partial \overline{R}_{\mathrm{u}}}{\partial t_{\mathrm{u}}} = \frac{-2(m+3)\widetilde{\mathcal{T}}_{\mathrm{u}}B_{\mathrm{u},n}}{Nt_{\mathrm{u}}^{2}} \left(1 - \frac{2t_{\mathrm{fb}}}{t_{\mathrm{u}}}\right) \left(\frac{r_{0}\cos\theta}{2v}\log_{2}\!\left(\frac{r^{2}(t_{\mathrm{u}}) + h^{2}}{r_{0}^{2} + h^{2}}\right)\right) \\ &- \frac{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}{v\ln(2)} \tan^{-1}\!\left(\frac{\frac{vt_{\mathrm{u}}}{(h^{2} + r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}}{1 - \frac{r_{0}\cos\theta(vt_{\mathrm{u}} - r_{0}\cos\theta)}{h^{2} + r_{0}^{2}\sin^{2}\theta}\right) + \frac{t_{\mathrm{u}}}{\ln(2)}\right) \\ &+ \frac{\widetilde{\mathcal{T}}_{\mathrm{u}}B_{\mathrm{u},n}t_{\mathrm{fb}}}{Nt_{\mathrm{u}}}\log_{2}\!\left(\frac{G_{\mathrm{u}}}{(r^{2}(t_{\mathrm{u}}) + h^{2})^{m+3}}\right). \end{split}$$

This is the exact derivation of the average uplink achievable throughput respect to $t_{\rm u}$, however, for $vt_{\rm u}\ll h$, this equation can be further simplified. Substituting $r(t_{\rm u})=(r_0^2+v^2t_{\rm u}^2-2r_0vt_{\rm u}\cos\theta+h^2)^{1/2}$ in logarithm term, ignoring the small terms and using the approximation $\ln(1+x)\cong x$ for small values of x, we arrive $\log_2\left(1+\frac{v^2t_{\rm u}^2-2r_0vt_{\rm u}\cos\theta}{r_0^2+h^2}\right)\cong \log_2\left(1-\frac{2r_0vt_{\rm u}\cos\theta}{r_0^2+h^2}\right)\cong \frac{-2r_0vt_{\rm u}\cos\theta}{\ln(2)\left(r_0^2+h^2\right)}.$ Considering the rule of small-angle approximation for inverse tangent, it can also be approximated by its first two terms of Taylor series as $\tan^{-1}(x)\cong x-x^3/3$ for small x. Noting that $t_{\rm fb}\ll t_{\rm u}$, the approximate derivation is given as follows:

$$\frac{\partial \overline{R}_{u}}{\partial t_{u}} \cong \frac{-2(m+3)\widetilde{T}_{u}B_{u,n}}{\ln(2)Nt_{u}^{2}} \left(1 - \frac{2t_{fb}}{t_{u}}\right) \left(\frac{(vt_{u})^{3}(h^{2} + r_{0}^{2}\sin^{2}\theta)^{2}}{3v(h^{2} + r_{0}^{2})^{3}} + t_{u}\right)
- \frac{r_{0}^{2}\cos^{2}\theta t_{u}}{r_{0}^{2} + h^{2}} - \frac{t_{u}(h^{2} + r_{0}^{2}\sin^{2}\theta)}{h^{2} + r_{0}^{2}}\right) + \frac{\widetilde{T}_{u}B_{u,n}t_{fb}}{Nt_{u}^{2}} \log_{2}\left(\frac{G_{u}}{(r_{0}^{2} + h^{2})^{m+3}}\right)
= -\frac{2(m+3)\widetilde{T}_{u}B_{u,n}v^{2}(h^{2} + r_{0}^{2}\sin^{2}\theta)^{2}t_{u}}{3N\ln(2)(h^{2} + r_{0}^{2})^{3}}
+ \frac{\widetilde{T}_{u}B_{u,n}t_{fb}}{Nt_{u}^{2}} \log_{2}\left(\frac{G_{u}}{(r_{0}^{2} + h^{2})^{m+3}}\right) \tag{35}$$

Using the Leibniz integral rule to calculate the derivation of average downlink throughput, and the sum of inverse tangents formula to simplify it, the derivation of the average downlink throughput is given as:

$$\frac{\partial \overline{R}_{d}}{\partial t_{u}} = \frac{-2(m+3)k_{\text{req}}B_{d,n}}{\mathcal{K}t_{u}^{2}} \left(\frac{r_{0}\cos\theta}{2v}\log_{2}\left(\frac{r^{2}(t_{u})+h^{2}}{r_{0}^{2}+h^{2}}\right) + \frac{t_{u}}{\ln(2)}\right) - \frac{(h^{2}+r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}{v\ln(2)} \tan^{-1}\left(\frac{vt_{u}}{(h^{2}+r_{0}^{2}\sin^{2}\theta)^{\frac{1}{2}}}\right) - \frac{r_{0}\cos\theta(vt_{u}-r_{0}\cos\theta)}{(h^{2}+r_{0}^{2}\sin^{2}\theta)}\right).$$
(36)

This is the exact derivation of the average downlink achievable throughput respect to $t_{\rm u}$, however, using the approximation rules for $vt_{\rm u} \ll h$, the well-approximated derivation is given as follows:

$$\frac{\partial \overline{R}_{d}}{\partial t_{u}} \cong \frac{-2(m+3)k_{\text{req}}B_{d,n}}{\mathcal{K}t_{u}^{2}} \left(-\frac{r_{0}^{2}\cos^{2}\theta t_{u}}{\ln(2)(r_{0}^{2}+h^{2})} - \frac{t_{u}(h^{2}+r_{0}^{2}\sin^{2}\theta)}{\ln(2)(h^{2}+r_{0}^{2})} + \frac{(vt_{u})^{3}(h^{2}+r_{0}^{2}\sin^{2}\theta)^{2}}{3v\ln(2)(h^{2}+r_{0}^{2})^{3}} + \frac{t_{u}}{\ln(2)} \right) \\
= \frac{-2(m+3)k_{\text{req}}B_{d,n}v^{2}t_{u}(h^{2}+r_{0}^{2}\sin^{2}\theta)^{2}}{3\mathcal{K}\ln(2)(h^{2}+r_{0}^{2})^{3}}.$$
(37)

The exact optimum time, $t_{\rm u,opt}$, can be obtained numerically by solving (26) after substituting $\frac{\partial \overline{R}_{\rm d}}{\partial t_{\rm u}}$ and $\frac{\partial \overline{R}_{\rm u}}{\partial t_{\rm u}}$ given in (33) and (36). However, we can approximately obtain a closed form for optimum update interval denoted as $\widetilde{t}_{\rm u,opt}$ by using (35) and (37). Taking into account that $vt_{\rm u} \ll h$ the closed solution form for optimum update interval is given as:

$$\widetilde{t}_{\mathrm{u,opt}} \cong \left(\frac{\frac{3\ln(2)}{2(m+3)}w_{\mathrm{u}}t_{\mathrm{fb}}\widetilde{\mathcal{T}}_{\mathrm{u}}B_{\mathrm{u},n}C_{1}}{w_{\mathrm{d}}v^{2}NR_{\mathrm{req}} + C_{2}w_{\mathrm{u}}v^{2}\widetilde{\mathcal{T}}_{\mathrm{u}}B_{\mathrm{u},n}}\right)^{\frac{1}{3}},$$

where

$$\begin{split} C_1 &= \frac{\mathbb{E}_{r_0} \bigg[\log_2 \!\! \left(\! \frac{G_{\mathrm{u}}}{(r_0^2 + h^2)^{m+3}} \right) \bigg] \, \mathbb{E}_{r_0} \bigg[\log_2 \!\! \left(\! \frac{G}{(r_0^2 + h^2)^{m+3}} \right) \! \bigg]}{\mathbb{E}_{r_0, \theta} \!\! \left[\! \frac{(h^2 + r_0^2 \sin^2 \theta)^2}{(h^2 + r_0^2)^3} \right]} \\ C_2 &= \mathbb{E}_{r_0} \!\! \left[\log_2 \!\! \left(\! \frac{G}{(r_0^2 + h^2)^{m+3}} \right) \! \right]. \end{split}$$

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