Towards accurate calculations of Zn^{2+} binding free energies in zinc finger proteins

UNDERGRADUATE HONORS RESEARCH THESIS

Presented in Partial Fulfillment of the Requirements for the Bachelor of Science with Honors Research Distinction in the College of Engineering of the Ohio State University

By

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Undergraduate Program in Chemical Engineering

The Ohio State University

2012

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Abstract

Zinc fingers are Zn²⁺-bound peptide motifs that bind DNA specifically and have great potential in gene therapy. However, the ion binding strength of the zinc finger is not well known, and computing this quantity will allow for the design of more stable zinc finger treatments. Ions in solution are a model system. Molecular dynamics (MD) simulations and the inverse potential distribution theorem were used to estimate the solvation free energies of zinc ions. The zinc coordination shells were stable and the initial coordination shell stayed throughout the 20 ns simulations. Quasichemical (QC) calculations are free energy calculations that partition the system into an inner shell, treated using quantum mechanics, and an outer shell, treated using continuum electrostatics. The theory was extended to multiple ligands in solution and used on Zn^{2+} in water/methanol mixtures, with the inner shell consisting of the six solvent molecules coordinated to the ion and the outer shell consisting of all other solvent. Increasing methanol coordinated to the zinc led to lower inner shell formation free energies but higher outer shell free solvation energies. A sixwater coordination shell was found to be most stable. Using quasi-chemical theory with different concentrations in the outer shell did not yield major differences, but this could have been due to an insufficient treatment of the van der Waals forces. A quasi-chemical approximation using MD to treat the outer shell would fix such problems and will be useful in computing zinc finger ion binding free energies.

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1 Introduction

Metal ions are important biologically because of their structural and reactive role in many proteins. It is estimated that one-third of all proteins are metalloproteins (metal-containing proteins) [1]. They play important roles in reduction/oxidation reactions due to their electron transfer properties. Their highly charged nature also enhances the structural stability of many proteins. One class of such metalloproteins are zinc finger proteins.

Zinc finger proteins are DNA binding proteins with structural Zn^{2+} ions that have demonstrated a high degree of specificity for certain DNA strands. Because of this, they have found applications in gene therapy, as they can be attached to nucleases and used to excise specific DNA sequences. Some researchers have recently demonstrated success in using zinc-finger nucleases to treat viral diseases such as HIV [2] and Hepatitis B [3] by destroying their DNA or required cellular co-receptors. However, the role of the divalent ion in the stability of the protein is not well known. Understanding the effect of mutations on the thermodynamic stability of the Zn^{2+} ion in the zinc finger allows for more stable synthetic zinc fingers to be constructed, increasing the ease and efficacy of using zinc-finger nucleases and other similar therapeutics. Also, as highly specific zinc-binding proteins, these could be used with an embedded fluorescent group as a sensitive zinc detector [4]. Understanding the comparative thermodynamic stability of such a protein to other ions will allow for the development of better models of metalloprotein binding.

Modern experimental methods, such as X-ray diffraction (XRD) and nuclear magnetic resonance (NMR) allow for the characterization of crystal structures. However, XRD cannot be used to determine solution structures, as the protein must be crystallized. Computer simulations must be used to solvate such structures. NMR can be used to determine solution structures, but computer simulations are used to refine such structures to yield more accurate descriptions of the protein conformation. One of the major computer simulation methods used is molecular dynamics (MD). MD simulations are atomistic simulations that use classical mechanics to determine trajectories of the atoms from an initial configuration. These simulations allow for the refinement of experimental structures as well as determination of basic thermodynamic quantities such as solvation free energies and interaction energies. The atomistic nature of MD simulations also allows insight into the mechanisms of atomic processes. MD simulations can be used to generate trajectories that are several ns in length for systems with tens of thousands of atoms. However, for metal ions, classical molecular dynamics simulations are unable to capture the quantum mechanical effects such as charge transfer and polarization. Other computational models must be used to accurately simulate the behavior of the metal ion.

Another method of computational structure determination is based on electronic structure theory. Quantum mechanical (QM) calculations, also known as *ab initio* calculations, derive results from the wavefunctions of the electrons in the system by solving self-consistent field equations. Thermodynamic properties can then be calculated from those wavefunctions using the harmonic approximation [5]. In general, this method is more accurate for calculating structural and thermodynamic properties than molecular dynamics, but is much more computationally demanding. Because of this limitation, QM calculations are only feasible for small systems on the order of tens of atoms. Also, QM does not capture the dynamics of the system. Newer methods such as ab initio molecular dynamics (AIMD) are able to perform dynamics on such systems, but can only be feasibly used with tens of atoms over periods of under 1 ns.

In order to simulate systems with hundreds of atoms accounting for quantum effects on nanosecond timescales, several methods have been devised to link quantum calculations with faster approximations. One is the hybrid quantum mechanics/molecular mechanics (QM/MM) method [6], where a subset of the atoms are treated with quantum mechanics and the rest of the atoms are treated using molecular (classical) mechanics. The two types of simulations are linked together using link atoms that are treated both ways and are attached to atoms from both sets. However, this method is not yet feasible for generating trajectories of protein simulations (tens of thousands of atoms) of sufficient length (several ns) for determining thermodynamic properties.

Another method is the quasi-chemical approximation [7], which partitions molecules into an inner shell and an outer shell. Under this model, the process of solvation can be decomposed into two parts: the formation of the inner shell and the solvation of the inner shell in the outer shell. Quantum mechanics are used to calculate free energies of formation of the inner shell complex, and the free energy of solvation is determined using continuum electrostatics. This method has been used with success on ions in water [8]. Such an approximation is much faster than any quantum simulation, yet also allows for accurate determination of free energies of solvation. However, this approach has not been used for mixtures of water and other solvents, which is a plausible model for considering a protein as a "solvation shell" for an ion.

2 Methods

2.1 Theory

2.1.1 Molecular Dynamics Simulations

Molecular dynamics simulations represent each atom as a point charge and mass with a Lennard-Jones 12-6 potential for van der Waals type forces. Interaction energies are provided from force fields and numerical integration is used to predict movement of atoms, generating an ensemble of states. Free energies can be calculated from these simulations using the principles of statistical mechanics. From the inverse potential distribution theorem [7], the excess chemical potential of a molecule X is

$$\mu_X^{ex} = \frac{1}{\beta} \log \left[\int_{-\infty}^{\infty} e^{\beta \epsilon} P_X(\epsilon) \, d\epsilon \right]$$
(2.1)

where $\beta = \frac{1}{k_B T}$, ϵ is the interaction energies between X and all other species, and P_X is the probability density function of ϵ . Assuming a gaussian distribution for the energies ($P_X(\epsilon) \propto e^{\frac{(\epsilon - \langle \epsilon \rangle)^2}{2\sigma^2}}$) and substituting this into Equation 2.1 results in

$$\mu_X^{ex} = \langle \epsilon \rangle + \frac{\beta \sigma^2}{2} \tag{2.2}$$

2.1.2 Quantum Mechanical Calculations

In QM calculations, an initial geometry is specified, and the wavefunctions of the electrons are solved to determine the internal energy of the system. The second derivatives of the energy functions can then be analyzed to determine the electronic vibrational structure of the system. Such frequency calculations can then be used to determine free energies of formation based on the harmonic approximation [5].

The method of solving the wavefunctions used in this case is density functional theory (DFT), where functionals of the spatial density of electrons are derived from experiment or higher-level ab initio calculations. Since the functionals contain information about different atoms, such an approach is faster than pure ab initio approaches, which do not consider such information.

2.1.3 Continuum electrostatics

In lieu of explicit solvent, solvent effects can be accounted for by treating them from an electrostatics perspective. This is due to the fact that at the distances considered as the outer shell (several \mathring{A}), the van der Waals forces are typically much smaller than the electrostatic interaction with the zinc ion. The generalized Born solvation model [9] was used for the determination of the free energy changes. In this model, the free energy of solvation is approximated as the free energy of taking a charged object of a certain shape from a medium with a dielectric constant of 1 to a medium with the dielectric constant of the desired solvent.

2.1.4 Quasi-Chemical Model

In the quasi-chemical approximation, we decompose the system into two parts: we define an inner shell and an outer shell, and combine the two to determine the solvation free energy. The contribution of the outer shell is defined as the solvation free energy of the complex, and can be calculated using continuum electrostatics. The free energy of the inner shell is defined chemically: given a species X and ligand L, the free energy of the formation of a cluster XL_n is the free energy change of the following reaction:

$$X + nL \rightleftharpoons XL_n$$

This is equivalent to the expression $-kT \ln K_n^{(0)}$, where $K_n^{(0)}$ is the ideal gas reaction rate constant at 1 *atm* and 298 K. This value can be calculated using QM methods. In the case of ions in solvent, the X is the ion species, and the L are the solvent molecules around the ion. A more thorough derivation of quasi-chemical theory can be found in [7].

The free energies are calculated in an ideal gas state at 298 K and 1 *atm*, but we are interested in the liquid state. To correct for this state, the free energy change due to a pressure change is $nkT \ln \left(\frac{P_{liq}}{P_0}\right)$, where P_{liq} is $RT\rho_w$ and ρ_w is the molar density of the solvent. This yields the ideal gas pressure at liquid densities. P_0 is 1 *atm*. This term is also written as $-kT \ln \rho^n$, as it is a density factor, and can be combined with the previous term as $-kT \ln K_n^{(0)}\rho^n$. A further discussion on this topic can be found in Grabowski et al [10].

A particular species X may also have coordination shells with different n. In that case, a term $kT \ln p_X(n)$ is included, where $p_X(n)$ is the probability of X being coordinated by n L's. This term accounts for the fact that this particular arrangement only contributes partially to the free energy. A first-order approximation is to consider only the most probable coordination number \tilde{n} . A more thorough discussion of this term can be found in Asthagiri et al [11].

Combining these terms together results in the expression

$$\mu_X^{ex} = -kT \ln K_{\tilde{n}}^{(0)} \rho^{\tilde{n}} + kT \ln p_X \left(\tilde{n} \right) + \left(\mu_{XL_{\tilde{n}}}^{ex} - \tilde{n} \mu_L^{ex} \right)$$
(2.3)

To extend this method to multiple ligand species, we can consider two ligands, L_1 and L_2 . The reaction is then

$$X + nL_1 + mL_2 \rightleftharpoons XL_{1n}L_{2m}$$

For a first order approximation of the density factor, one can calculate the density of the solution by assuming that this is an ideal solution and approximating the liquid molar density as $\rho_{L_1L_2} = x_{L_1}\rho_{L_1} + x_{L_2}\rho_{L_2}$. This leads to $P_{L_1L_2} = kT\rho_{L_1L_2}$. Although this may not be true, the effect of the term is not very significant in the calculations (see Section 3.2.4). A more accurate approximation could also be performed considering excess molar volumes. The corresponding density factor is then $(n+m)kT\ln\left(\frac{P_{L_1L_2}}{P_0}\right)$. Like before, we may write $\frac{P_{L_1L_2}}{P_0} = \rho$. The probability term can be modified to account for changes in the coordination numbers of n and m. The free energy is then determined to be

$$\mu_X^{ex} = -kT \ln K_{n,m}^0 \rho^{(n+m)} + kT \ln p_X(n,m) + \left(\mu_{XL_{1n}L_{2m}}^{ex} - n\mu_{L_1}^{ex} - m\mu_{L_2}^{ex} \right)$$
(2.4)

2.2 Calculation details

All calculations were performed on the GLENN cluster of the Ohio Supercomputer Center on dual socket nodes with two quad-core 2.5 GHz AMD Opteron processors. Calculation files can be found in Appendix A. More details on the specific calculations performed can be found in the Results section (Section 3).

2.2.1 Ions in solution

Simulation files were prepared using VMD 1.8.7 and the solvate plugin. A PDB file containing one ion was created by hand and solvated with a 32 \mathring{A} TIP3P water box.

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and the CHARMM 27 force field. The force field file can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were used. The nonbonded cutoff was set at 12 Å. Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters and methanols were constrained with the SHAKE algorithm. The system was minimized at 0K for 7500 steps, velocities were reinitialized to 298K, and the system was equilibrated for 200 ps. Production runs of 20 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

A QM calculation of the Zn^{2+} ion was performed. DFT calculations were performed using Gaussian 09 Revision A.01 [13]. The Becke three-parameter Lee-Yang-Parr (B3LYP) hybrid exchange-correlation functional and the 6-311++G(2d,p) basis set was used. Initial structures were obtained from MD simulations. Structures were first optimized on a 6-31+ basis set, then on a 6-311+G(d,p) basis set, and finally on the 6-311++G(2d,p) at the VeryTight optimization level. Free energies were obtained using frequency analysis on optimized structures. No imaginary frequencies were found, indicating stable structures. Population analysis according to the CHELPG [14] procedure was used to determine charges. Radii for the different atoms were taken from Stefanovich et al [15]. The radius for Zn^{2+} was set at 2.2 Å, as the value did not change the calculation much. Free energies of solvation were then calculated according to the generalized Born solvation model using the Adaptive Poisson-Boltzman Solver (APBS) 1.3 [16].

2.2.2 Zn²⁺ in methanol/water solutions

Coordination shells with specific numbers of methanols and waters were created by hand-modifying a PDB file generated from the QM optimization of the Zn^{2+} ion above. These were energy-minimized at 0 K in NAMD using the OPLS-ua force field to produce optimized structures. The force field file can be found in A.2. The optimized structures were put in a 2500-atom methanol/water solvent box with 0%, 5%,10%, 15% or 100% MeOH mol% using PACKMOL [17].

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and the OPLS-ua force field. The force field file can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were used. The nonbonded cutoff was set at 12 Å. Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters and methanols were constrained with the SHAKE algorithm. The system was minimized at 0K for 7500 steps, velocities were reinitialized to 298K, and the system was equilibrated for 200 ps. Production runs of 20 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

DFT calculations were performed using Gaussian 09 Revision A.01 [13]. The Becke three-parameter Lee-Yang-Parr (B3LYP) hybrid exchange-correlation functional and the 6-311++G(2d,p) basis set was used. Initial structures were derived from MD simulations. Structures were first optimized on a 6-31+ basis set, then on a 6-311+G(d,p) basis set, and finally on the 6-311++G(2d,p) at the VeryTight optimization level. Free energies were obtained using frequency analysis on optimized structures. No imaginary frequencies were found, indicating stable structures. Population analysis according to the CHELPG [14] procedure was used to determine charges. Radii for the different atoms were taken from Stefanovich et al [15]. The radius for Zn^{2+} was set at 2.2 Å, as the value did not change the calculation much. Free energies of solvation were then calculated according to the generalized Born solvation model using the Adaptive Poisson-Boltzman Solver (APBS) 1.3 [16].

2.2.3 Zn^{2+} in zinc finger protein

The zinc finger motif used consisted of residues 42 to 71 of chain A of the TFIIIA zinc finger (PDB: 1TF6). The zinc finger motif was extracted from the NMR structure, and then hydrogen atoms were added using the PSFGEN module of VMD 1.9.1 [18]. The histidine residues coordinated to the zinc were changed to the neutral (HID) form and the cysteine residues were deprotonated. The protein was then solvated in a $48\mathring{A} \times 48\mathring{A} \times 54\mathring{A}$ TIP3P water box.

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and two force fields. The CHARMM 27 force field modified to include a deprotonated cysteine, which was obtained from parameters for methylthiolate. The AMBER FF09 force field was not modified. The force field files can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were used. The nonbonded cutoff was set at 12 Å. Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters were constrained with the SHAKE algorithm. The system was minimized at 0K for 10000 steps and then heated from 0 K to 298 K over 50 ps and equilibrated for 200 ps. Production runs of 10 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

DFT calculations were performed using Gaussian 09 Revision A.01 [13]. The Becke three-parameter Lee-Yang-Parr (B3LYP) hybrid exchange-correlation functional and the 6-311++G(2d,p) basis set was used. Initial structures were obtained from the NMR structure. Structures were first optimized on a 6-31+ basis set, then on a 6-311+G(d,p) basis set, and finally on the 6-311++G(2d,p) at the VeryTight optimization level. Free energies were obtained using frequency analysis on optimized structures. No imaginary frequencies were found, indicating stable structures. Population analysis according to the CHELPG [14] procedure was used to determine charges. Radii for the different atoms were taken from Stefanovich et al [15]. The radius for Zn²⁺ was set at 2.2 Å, as the value did not change the calculation much. Free energies of solvation were then calculated according to the generalized Born solvation model using the Adaptive Poisson-Boltzman Solver (APBS) 1.3 [16]. QM/MM calculations were performed using NWCHEM 6.1 [19]. The α -carbons of the coordinating protein residues were considered to be the boundary of the QM region. The rest of the protein and a water shell were considered using molecular mechanics. The Amber FF09 force field was used for the MM portion. DFT using the LANL08DZ basis set, which is optimized for transition metals, was used with the B3LYP hybrid functional. Hydrogen link atoms were used. Optimization was performed using the conjugate gradient algorithm. The QM/MM boundary cutoff was set at 9 Å. Electrostatic potential fitting of the QM region was used for parameterization of the QM atoms during the MM optimization. Ten cycles of optimization were performed, with a maximum of 50000 solvent iterations, 10000 protein iterations, and 500 QM core iterations. The resulting optimized structure was then further refined using the DFT calculation methodology above except with the alpha carbons fixed at the optimized positions.

3 Results

3.1 Ions in solution

3.1.1 MD simulations of Na⁺, K⁺ and Zn²⁺ in water

MD simulations of ions in water were performed to verify that results obtained from NAMD were accurate. Interaction energies of the ion with the waters were calculated and fitted to a normal distribution (see Figure 1 and Figure 2).

From these plots, it was determined that the energies were indeed normally distributed, so the free energies were calculated using Eqn 2.2. Results for the different ions (Na⁺, K⁺, and Zn²⁺) are tabulated in Table 1.

The experimental and quasi-chemical values were from Asthagiri et al [8]. From these calculations, it becomes evident that although the free energies calculated using



Figure 1: Na^+ and K^+ interaction energy distributions and gaussian fits from MD simulations.

this method are reasonable, the error increases with increasing atomic number and may be larger than desired. Because of this, a more accurate method will be used to determine free energies.

3.1.2 Quasi-chemical calculation of Zn^{2+} hydration free energy

Quasi chemical theory was applied to the zinc ion in particular to determine more accurate binding free energies. The inner shell radius was determined from the first minimum of the Zn^{2+} -O radial distribution function (see Figure 3). The radial distribution function was calculated from the MD simulations of Zn^{2+} in water.

It was found to contain 6 water molecules. Trajectory analysis determined that the waters coordinating the ligands did not exchange, thus there was a sharplydefined inner shell. QM calculations of the core were then performed according to



Figure 2: Zn²⁺ interaction energy distribution and gaussian fit from MD simulation. Table 1: Solvation free energies for ions in water using MD compared to experimental values and quasi-chemical values

Units in $\left(\frac{kcal}{mol}\right)$	$\langle\epsilon angle$	$\beta \frac{\sigma^2}{2}$	μ_X^{ex}	QC [8]	Exp. [8]
Na^+	-166.9 ± 0.3	81.8 ± 1.4	-85.1 ± 1.5	-96.1	-91.5
K^+	-129.3 ± 0.2	67.2 ± 0.6	-61.9 ± 0.5	-75.2	-74.6
Zn^{2+}	-598.9 ± 0.2	165.2 ± 1.5	-433.8 ± 1.5	-458.1	-471.1

Standard deviations of values from dividing the simulation into 4 time blocks follow \pm .

the methodology in 2.2.3. The zinc solvation free energy and different components of the quasi-chemical free energy of solvation expression (Equation 2.3) can be found in Table 2.

The results agreed rather well with the results from Asthagiri et al [8].

3.2 Zn^{2+} in methanol / water mixtures

In order to extend quasi-chemical theory to mixtures, the Zn^{2+} ion was solvated in mixtures of methanol and water. Parameters for these simulations were derived from



Figure 3: Zn^{2+} -OH₂ radial distribution function

Table 2: Quasi-chemical calculation of Zn^{2+} hydration free energy

$\left(\frac{kcal}{mol}\right)$	$-kT\ln K_{\tilde{n}}^{(0)}$	$\mu_{XL_n}^{ex}$	μ_L^{ex}	μ_X^{ex}	Experimental	[8]
Asthagiri et al $[8]$	-279.2	-199.3	-7.7	-458.1	-471.1	
This work	-282.8	-202.6	-8.1	-462.4	-471.1	

the Optimized Potentials for Liquid Simulations United-Atom (OPLS ua) force field. In this force field, the methyl group of the methanol was approximated as a united atom. Simulations of 2500 solvent atoms and a zinc ion were run at methanol mol% of 0%, 5%, 10%, 15%, and 100%. It was found that the Zn^{2+} ion bound the six atoms around it from the initial configuration very tightly: no atoms coordinated to the zinc ion after minimization exchanged with other atoms in any of the 20 ns NPT production runs at any methanol mole fraction. Based on these results, MD simulations of the Zn^{2+} ion in water were performed with different coordination shells containing *i* waters and 6 - i methanols for *i* ranging from 0 to 4.

3.2.1 Free energies of solvation

Interaction energies between the zinc ion and the all outer shell (non-coordinated solvent) were calculated. The energies were normally distributed. A sample energy histogram can be found in Figure 4.



Figure 4: Interaction energy distribution of Zn^{2+} with non-coordinated solvent molecules (outer shell radius: 3.5 Å) in 15% MeOH and water

Histograms for the other systems can be found in Appendix C.2. The gaussian approximations of the interaction energy distributions were deemed valid, and the solvation free energies were calculated with Equation 2.2. The free energies of solvation are tabulated in Table 3.

Inner shell methanols	Methanol $\operatorname{mol}\%$	Zinc ion binding free energy
2	0	-443
3	0	-438
4	0	-433
5	0	-432
6	0	-428
6	5	-429
6	10	-432
6	15	-434

Table 3: Calculation of $\mathbb{Z}n^{2+}$ ion solvation free energies from MD simulations for various solvents

3.2.2 Radial distribution functions

Radial distribution functions between Zn^{2+} and water oxygen and methanol oxygen and methyl groups were calculated using VMD 1.9.1. [18]. Some are shown below in Figure 5. The other radial distribution functions can be found in Appendix C.1.

From the radial distribution functions, we see that the locations of the peaks do not move with changing solvent methanol composition or coordination shell methanol composition, but the heights of the peaks change. This shows that effect of the methanol on the general structure of the inner shell is minimal, but it does push the outer shell further away from the zinc. This is what most likely explains the trend observed in the solvation free energies above: adding more methanol to the inner shell decreases the stability of the system by virtue of its size. The plots also show that a radius of 3.5 \mathring{A} for the outer shell is a reasonable choice.



Figure 5: Radial distribution functions

3.2.3 Occupancy probabilities

Occupancy probabilities were determined using a VMD Tcl script (See Appendix B.2). For the quasi-chemical approximation, a specific number of each kind of atom in the inner shell is assumed. To verify that this assumption is reasonable, the probability that the area around the ion is occupied by a certain number of waters and methanols was calculated. Table 4 shows the probabilities that an *incorrect* number of atoms each non-hydrogen type were observed. Correctness was defined as the following: for simulations with n MeOH in the coordinated to the ion, there should be n methanol oxygens, n methanol methyl groups, and 6 - n water oxygens within the 3.5 Å boundary.

From the small probabilities in Table 4, we see that the assumption that the shell consists of n methanols and 6 - n waters is reasonable.

n = MeOH	MeOH mol $\%$	$P\left(Me\mathbf{O}H\neq n\right)$	$P\left(\mathbf{Me}OH \neq n\right)$	$P\left(\mathbf{O}H_2 \neq 6-n\right)$
2	0	0	9.1×10^{-3}	2.2×10^{-2}
3	0	0	1.4×10^{-2}	1.6×10^{-2}
4	0	0	1.9×10^{-2}	1.2×10^{-2}
5	0	0	2.6×10^{-2}	9.9×10^{-3}
6	0	0	3.2×10^{-2}	7.4×10^{-3}
6	5	6.7×10^{-5}	3.2×10^{-2}	6.8×10^{-3}
6	10	2.3×10^{-4}	3.3×10^{-2}	7.0×10^{-3}
6	15	2.4×10^{-3}	3.2×10^{-2}	$6.9 imes 10^{-3}$

Table 4: Probabilities that incorrect numbers of each atom type are within 3.5 \mathring{A} of $\rm Zn^{2+}$

These are the probabilities that the specified number of the centers of the atom type in **bold** is within $3.5\mathring{A}$ of the ion.

3.2.4 Quasi-chemical calculations of free energies

Based on the observation that the zinc ion bound the nearest six molecules tightly, and that it always exhibited a hexacoordinated geometry, QM calculations of the Zn^{2+} ion with different coordination shells containing *i* waters and 6 - i methanols for *i* ranging from 0 to 6 were performed, and Equation 2.4 was used to determine the free energies for all the coordination states. It was determined that there were several isomers of some solvation shells. An example of this is shown in Figure 6

QM optimizations of the geometries from Figure 6 revealed that the energy differences were negligible (< 0.1 $\frac{kcal}{mol}$), hence only one isomer was used.

A table (Table 5) of the solvation free energies in water of each coordination state (neglecting the probability term in Equation 2.4) and their contributions is shown below.

Also, we assume ideal solutions to calculate the standard state correction $(-kT \ln \rho^6)$ (see Section 2.1.4). However, since the term is not very large, such an approximation



Figure 6: Two isomers of a Zn^{2+} ion coordinated with 4 MeOH and 2 H₂O.

Table 5: Quasi-chemical calculation of Zn^{2+} solvation free energies with different coordination numbers

Units in $\left(\frac{kcal}{mol}\right)$	$kT\ln K_{n,m}^{(0)}$	$-kT\ln\rho^6$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$n\mu_{L_1}^{ex} + m\mu_{L_2}^{ex}$	μ_X^{ex}
$Zn^{2+} \left[H_2O\right]_6 \left[MeOH\right]_0$	-283	-25.6	-203	-49	-462
$Zn^{2+}\left[H_2O\right]_5\left[MeOH\right]_1$	-285	-25.3	-195	-46	-459
$Zn^{2+}\left[H_2O\right]_4\left[MeOH\right]_2$	-287	-24.9	-187	-43	-455
$Zn^{2+} [H_2O]_3 [MeOH]_3$	-289	-24.5	-180	-41	-453
$Zn^{2+} \left[H_2O\right]_2 \left[MeOH\right]_4$	-291	-24.0	-174	-39	-451
$Zn^{2+} \left[H_2O\right]_1 \left[MeOH\right]_5$	-292	-23.5	-168	-36	-447
$Zn^{2+} \left[H_2O\right]_0 \left[MeOH\right]_6$	-294	-22.8	-162	-34	-445

will not affect the calculation much.

To account for the different solvents, the dielectric constant was adjusted using the methodology in [20]. Table 6 shows the solvation free energies in various mixtures. Table 6: Quasi-chemical calculation of Zn^{2+} solvation free energies in water/methanol mixtures

MeOH mol $\%$	0%		15%		100%	
Dielectric Constant	78.4		65		33	
Units in $\left(\frac{kcal}{mol}\right)$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu^{ex}_{L_{1n}L_{2n}}$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu_{L_{1n}L_{2n}}^{ex}$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu^{ex}_{L_{1n}L_{2n}}$
$Zn^{2+} \left[H_2O\right]_6 \left[MeOH\right]_0$	-203	-49	-202	-48	-199	-47
$Zn^{2+}\left[H_2O\right]_5\left[MeOH\right]_1$	-195	-46	-194	-46	-191	-45
$Zn^{2+} \left[H_2O\right]_4 \left[MeOH\right]_2$	-187	-44	-186	-44	-183	-42
$Zn^{2+} [H_2O]_3 [MeOH]_3$	-180	-41	-179	-41	-176	-40
$Zn^{2+} \left[H_2O\right]_2 \left[MeOH\right]_4$	-174	-39	-174	-39	-171	-38
$Zn^{2+}\left[H_2O\right]_1\left[MeOH\right]_5$	-168	-36	-167	-36	-165	-35
$Zn^{2+} \left[H_2 O\right]_0 \left[MeOH\right]_6$	-162	-34	-162	-34	-159	-33

We see that there are no large differences in free energies from this method along the range of MeOH mol% studied. The main differences in free energy arise from the $\mu_{XL_{1n}L_{2m}}^{ex}$ term. From this calculation, it appears that the water-coordinated state is most favorable even in pure methanol.

Since no exchanges were observed between atoms in the inner shell and atoms outside the inner shell in the simulations, it was not possible to determine the relative probabilities of each coordination state from the trajectories. However, based on the free energy differences of each coordination state, it is possible to determine the relative probabilities: for each coordination state, μ_X^{ex} will be the same, with the differences between the free energies accounted for with the $-kT \ln p_X(0)$ term. Solving for the relative probability in this manner, we obtain the probabilities of each configuration shown in Table 7.

Units in $\left(\frac{kcal}{mol}\right)$	μ_X^{ex}	$p_X\left(n,m\right)$
$Zn^{2+}\left[H_2O\right]_6\left[MeOH\right]_0$	-462	0.997
$Zn^{2+}\left[H_2O\right]_5\left[MeOH\right]_1$	-459	2.33×10^{-3}
$Zn^{2+} \left[H_2O\right]_4 \left[MeOH\right]_2$	-455	7.02×10^{-6}
$Zn^{2+}[H_2O]_3[MeOH]_3$	-453	7.14×10^{-8}
$Zn^{2+}[H_2O]_2[MeOH]_4$	-451	3.09×10^{-9}
$Zn^{2+} [H_2O]_1 [MeOH]_5$	-447	1.03×10^{-11}
$Zn^{2+} [H_2O]_0 [MeOH]_6$	-445	1.35×10^{-13}

Table 7: Probabilities of observing different coordination states of Zn^{2+}

We see that at equilibrium, Zn^{2+} would be coordinated to six waters. Since the free energies in differing solvent do not change by much (see Table 6), we conclude that a six water coordinated Zn^{2+} ion will be the most stable in any water/methanol solvent.

3.2.5 Charge transfer on Zn²⁺ ions in QM calculations

The charges on the Zn^{2+} ion from the different QM calculations were computed using electrostatic fitting (see Table 8).

From these results, we can see that charge transfer plays a significant role in terms of quantum effects in this system. This verifies the need to treat the core with an electronic structure method.

3.3 TFIIIA zinc finger motif

3.3.1 AMBER FF09 simulations

MD simulations were also performed for the zinc finger motif present in TFIIIA. The zinc finger motif was taken from chain A of the TFIIIA, residues 42-71. These residues

Number of Methanols	Charge on $\operatorname{Zn}^{2+}(e)$
0	2.09
1	1.92
2	1.75
3	1.60
4	1.34
5	1.09
6	0.80

Table 8: Charge transfer off of Zn^{2+} ion

$\mathsf{P}\text{-}\mathsf{F}\text{-}\mathsf{P}\text{-}\boldsymbol{C}\text{-}\mathsf{K}\text{-}\mathsf{E}\text{-}\mathsf{E}\text{-}\mathsf{G}\text{-}\boldsymbol{C}\text{-}\mathsf{E}\text{-}\mathsf{K}\text{-}\mathsf{G}\text{-}\mathsf{F}\text{-}\mathsf{T}\text{-}\mathsf{S}\text{-}\mathsf{L}\text{-}\mathsf{H}\text{-}\mathsf{H}\text{-}\mathsf{S}\text{-}\mathsf{L}\text{-}\mathsf{T}\text{-}\boldsymbol{H}\text{-}\mathsf{T}\text{-}\mathsf{G}\text{-}\mathsf{E}\text{-}\mathsf{K}$

Figure 7: Sequence of peptide used. Zinc ligands are in bold.

were chosen as this peptide's properties had been characterized by early studies [4]. The sequence of the peptide is shown in Figure 7.

The NMR structure of the protein with the zinc binding site is shown in Figure 8. Note that the zinc ion appears to be tetrahedrally coordinated by the four amino acids.

The motif was solvated in a $48\text{\AA} \times 48\text{\AA} \times 54\text{\AA}$ water box, minimized for 10000 steps, and heated to 298 K over 50 ps. Ten nanosecond NPT production runs were performed and were used for trajectory analysis. The CHARMM27 force field was unable to produce a stable structure with the zinc ion within the binding site. However, the AMBER FF09 force field was able to do so. Interaction energies between the Zn²⁺ ion and all other atoms were obtained from the trajectory. The interaction energies were normally distributed (see Figure 9). The solvation free energy was calculated using Equation 2.2, and the components are tabulated in Table 9.

In the equilibrated structure, the Zn^{2+} ion was coordinated to two waters in addition to the four protein ligands as seen in the NMR structure (see Figure 10). In



Figure 8: TFIIIA Zinc finger motif NMR structure with binding site. Grey ball is zinc, yellow is sulfur. The cysteine side chains are on the right, the histidines are on the left.

Table 9: Components of zinc finger solvation free energy

$\langle \epsilon \rangle \left(\frac{kcal}{mol} \right)$	$\frac{\beta\sigma^2}{2} \left(\frac{kcal}{mol}\right)$	$\mu_X^{ex}\left(\frac{kcal}{mol}\right)$
-652	130	-522

order to reproduce the NMR structure, other methods were used to reparameterize the inner core. From the literature, it was determined that the cause of the extra waters in the binding site was inadequate consideration of quantum effects such as charge transfer and polarization [21].

3.3.2 Non-QM methods for accounting for quantum effects

To account for charge transfer, the charges on the Zn^{2+} ion and the surrounding ligands were modified by hand using the charges from Li et al [21], who used the electron densities from a QM optimization calculation to determine the charge transfer. This method did not, however, exclude the waters from entering the zinc finger. Using the CHARMM 27 force field with this parameterization resulted in a stable protein, but



Figure 9: Zinc finger Zn^{2+} interaction energy distribution and gaussian fit.

with the waters in the binding site as shown in Figure 10.

Simulations were also performed using the cationic dummy atom model [22], which uses four charged "dummy atoms" attached to the zinc ion by springs in order to approximate polarization effects. This model was able to successfully predict the structure, but since it constrained the ligands, the vibrational modes would be affected. It was decided to explore chemical and quasi-chemical approaches for determining the free energies.

3.3.3 QM/MM calculations

QM/MM calculations were performed on the zinc finger to determine an optimized QM geometry for the core as well as an optimized MM geometry for the rest of the protein. The side chains of the protein and the zinc ion were treated with DFT using the LANL08DZ basis set, which is optimized for transition metals. The B3LYP hybrid functional was used. The rest of the atoms were treated using the AMBER FF09 force field. QM/MM dynamics at the time lengths required for determination of the free energies were not feasible. QM/MM methods were used to optimize geometries for the zinc finger core in order to have accurate geometries for usage with the quasi-chemical



Figure 10: Zinc finger equilibrated structure. Note the two water molecules in the binding site.

method.

4 Discussion

4.1 Ions in water

4.1.1 MD simulations

From the results in Table 1, we conclude that these simulations do indeed contain good measures of the binding free energy of the Zn^{2+} ion to water. While there are errors on the order of tens of $\frac{kcal}{mol}$, the trends are the same. However, since we are extending these results to measuring stability changes in mutations of proteins, a more accurate method may be necessary.

4.1.2 Quasi-chemical calculation of Zn²⁺ hydration free energy

The hydration free energies calculated using the quasi-chemical method agreed very well with those of Asthigiri et al [8], which demonstrates that the procedure used was accurate enough. The differences are mainly due to the usage of a larger basis set and a different method of solving the Poisson-Boltzman equation.

4.2 Zinc ion in water and methanol

4.2.1 Inner-shell stability

The zinc ion binds its coordinating ligands very tightly. Because of this, any exchanges were not able to be modeled, as the initial configuration of the zinc coordination shell did not change throughout the simulation. Increasing temperature to increase the fluctuations of the atoms was unsuccessful at dislodging any of the coordinating ligands. This effect can also be seen in the relatively sharp peaks of the radial distribution functions (see C.1). Because of this, it was impossible to use simulations to determine the most stable coordination state, so it was done using solvation free energies.

4.2.2 Effect of coordination shell composition

From the quasi-chemical calculations of the free energy of solvation with different coordination states (Table 5, the largest quantity in the calculation of the solvation free energy is the equilibrium constant term $-kT \ln K^{(0)}_{n,m}$. It decreases with increasing methanol around the zinc finger. Such an effect could be due to the fact that the larger system (more atoms) allows the electrons to delocalize more than with water. The outer shell contribution increases greatly with increasing methanols, and it dominates the differences in free energy. This is most likely due to the increasing size of the complex, which can be seen from the radial distribution functions C.1. The decreasing second-shell water peak and increasing third-shell water peaks are due to more of the water being pushed away from the ion. Since it takes more work to take a larger charged sphere into an electric field, it is reasonable that increasing the size would destabilize the system. We also see this pattern in the MD simulations (see Table 3), as the cluster solvation free energies also increase by a similar amount (2-4 $\frac{kcal}{mol}$). Overall, the results suggest that the aqueous coordinated state is the most stable.

There is no experimental data regarding the solvation free energy of the zinc ions in water/methanol mixtures, so it is not possible to compare the simulation data to actual data. However, as the MD simulations and QC calculations agree in terms of the relative differences in free energy between the coordination states, these may still be good estimates of the actual values.

4.2.3 Effect of solvent composition

One concern with the simulations is the different trends with regards to changing the solvent. In the MD simulations (Table 3), it appears that increasing methanol in the solvent actually tends to stabilize the cluster by a significant amount. However, the opposite appears to be true concerning the QC calculations (Table 6). Additional methanol in the solvent (lowering the dielectric constant) is unfavorable, but the effect is not very large. These discrepancies could be due to the nature of the approximations made. In the QC calculations, the outer shell is treated as a purely electrostatic entity. However, along the edges of the cluster, the van der Waals forces could be playing an important role. Because of this, a more advanced quasi-chemical approximation with a higher-level representation of the outer shell may be necessary.

4.3 Zinc fingers

While this work did not truly explore the stability of zinc fingers, some insight was still gained into methods of modeling zinc fingers. Firstly, classical methods are unable to reproduce the tetracoordinated geometry of the zinc finger. This may be due to the nature of the parameterization of the zinc ion in force fields, as in solution, the zinc ion is indeed hexacoordinated.

4.3.1 Application of zinc ion in water/methanol mixtures to zinc finger thermodynamics

Two methods of applying the quasi-chemical method to zinc fingers arise. Firstly, one can consider the entire protein as the ligand in the inner shell. Secondly, one can consider the sidechains of the protein ligands as the inner shell, and the rest of the protein and the water as the outer shell. Both methods have challenges. In the first method, modeling the entire protein using QM would be unfeasible. Also, in order to use the quasi-chemical method, we need to know the solvation free energy of the protein without the zinc ion (see Equation 2.4). Since we do not know the conformation of the protein without the ion, it may be very difficult to estimate accurately. However, if we consider relative binding free energies of different ions instead, we can approximate the relative reaction free energy changes in the protein without the ion cancels out. Thus, this method can be used to determine relative binding free energies.

For the second method, since the quasi-chemical model treats the outer shell electrostatically using the dielectric constant, a dielectric constant for the zinc finger protein is required. This can be calculated from MD trajectories. However, if we mutate only one residue, it may be difficult to have a significant effect on the dielectric constant. As can be seen from Table 6, small dielectric constant changes do not affect the solvation free energy much in that approximation. Also, in a protein, van der Waals and bonded interactions of the sidechains in the inner shell with the outer shell are more important.

To overcome these limitations, the outer shell component of the solvation free energy can also be approximated using the inverse potential distribution theorem and MD with the method described in Section 2.2.3. Several factors need to be addressed before such a calculation can take place. Firstly, the bonded interactions need to be
considered. One of the principle difficulties in QM/MM calculations, another method seeking to bridge quantum and classical simulations, is in the coupling of the two forms of simulation. Methodologies from QM/MM may also be applicable to QC calculations. Secondly, a method of simulating the protein with MD that gives good estimates of the outer-shell free energies is required. Several methods exist, but their effects on the calculation of free energies has yet to be considered. Thirdly, an accurate estimate of the geometry of the inner shell is necessary. This was performed using QM/MM geometry optimizations to determine an accurate inner shell geometry that also considered the overall conformation of the protein.

5 Conclusions

Several methods can be used to estimate the free energy of hydration of ions in solution. Two of these are quasi-chemical theory and the inverse potential distribution theorem. Using the IPDT with MD simulation data yields results accurate to within tens of $\frac{kcal}{mol}$. Quasi-chemical theory uses electronic structures to determine the formation and solvation free energies of a certain complex. The formulation of the IPDT lends itself naturally to mixtures in solutions.

QC theory was also expanded to include different ligands coordinating the species of interest. A derivation can be found in section 2.1.4. The solvation free energy of different coordination states of the Zn^{2+} ion was found to follow two opposite trends. Firstly, the free energy of formation of the inner shell was found to decrease with increasing methanols in the coordination shell. This may be due to the fact that a larger system allows for better electron delocalization, stabilizing the chemical equilibrium. Secondly, the free energy contribution of solvation of the inner shell cluster was found to increase with increasing methanols in the coordination shell. This may be due to the fact that a larger system also requires more work to solvate. This was supported by MD simulations. The second trend was more dominant in the zinc-methanol-water system, and the most favorable hexacoordinated state was the zinc ion with six water molecules.

Extending QC theory to mixtures of solvents reduces to changing the dielectric constant of the solvent and using that to solvate the inner shell cluster. However, this yielded discrepancies with the MD simulations. These discrepancies require further investigation. It was observed, however, that the dielectric constant made little impact on the free energies in the case of water and methanol solutions. This may not be true for mixtures of fluids with more disparate dielectric constants.

From these observations, in order to adapt these methods for determining the binding free energies of the Zn^{2+} ions in zinc fingers, it will be beneficial to use one of two methods. First, the free energy change for different ions in the protein can be measured instead using a quasi-chemical model where the entire protein is in the inner shell as the ion ligand. Secondly, a combined method could be used. In this quasi-chemical framework, the "inner shell" would be considered using QM calculations as before. However, the "outer shell" would be treated using MD simulations and the IPDT to determine solvation free energies of the cluster. Some theoretical issues in computing the binding free energies include computing the core structure accurately, simulating the protein accurately using MD, and the treatment of bonds and van der Waals forces. Several approaches exist for the first and second challenges. The third problem has similarities with problems in calculating energies using QM/MM methods and similar approaches can be used. The ability to accurately compute binding free energies of such proteins will allow for the better design of stable synthetic zinc finger therapies for many genetic and viral disorders.

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A Sample Input Files

A.1 Gaussian Input Files

A.1.1 Geometry Optimization

%chk=ZnMeOH_1MeOH.2.chk %nproc=8 %nem=8GB # B3LYP/6-31+G(d,p) Opt=(MaxCycles=3000) SCF=Tight

${\it ZnMeOH_1MeOH\ initial\ optimization}$

$2 \ 1$						
Zn						
Ο	1	2.12893				
Н	2	0.96755	1	126.17828		
Н	2	0.96757	1	125.75120	3	170.40655
0	1	2.13616	2	87.12158	3	94.83202
Н	5	0.96761	1	125.02553	2	359.41570
Н	5	0.96745	1	127.44986	2	180.60039
0	3	4.91606	1	7.01409	2	166.75975
Н	8	0.96777	1	125.97754	2	273.69230
Н	8	0.96776	1	126.28971	2	84.80468
С	1	3.27698	2	77.67952	3	274.51543
0	11	1.46857	1	27.07727	2	179.43446
Н	12	0.96628	11	109.55118	1	179.32941
Н	11	1.08519	1	79.64376	2	0.77357
Н	11	1.08816	1	120.94433	2	108.22552
Н	11	1.08818	1	119.82954	2	253.25482
Н	1	2.81424	2	88.72717	3	167.08164
Ο	17	0.96758	1	37.82510	2	92.74253
Н	18	0.96749	17	107.47534	1	178.20228

Ο 1 2.13326 $\mathbf{2}$ 89.99628 3 5.86169Η 200.967511 126.00081 $\mathbf{2}$ 265.86735Η 0.96756126.52056 $\mathbf{2}$ 85.96788 201 %chk=ZnMeOH_1MeOH.2.chk % n proc = 8%mem=8GB $\# \ B3LYP/6-311+G(d,p) \ Opt=(MaxCycles=3000) \ SCF=Tight \ Geom=check \ guess=read$ ZnMeOH_1MeOH opt1 optimization 2 1 %chk=ZnMeOH_1MeOH.2.chk % n proc = 8%mem=8GB # B3LYP/6-311++G(2d,p) Opt=(VeryTight, MaxCycles=3000) SCF=Tight Geom=check guess=read Structure (VeryTight, MaxCycles=3000) SCF=Tight Structure (VeryTight, MaxCycles=3000) SCF=Tight Structure (VeryTight, MaxCycles=3000) Structure (VeryTi

 $ZnMeOH_1MeOH \ \texttt{opt2} \ \texttt{optimization}$

 $2 \ 1$

A.1.2 Frequency and Population Analysis

```
%chk=ZnMeOH_1MeOH.2.chk
%nproc=8
%mem=8GB
# Freq Pop=(ChelpG, ReadRadii) b3lyp/6-311++g(2d,p) geom=checkpoint guess=read
```

 ${\rm ZnMeOH_1MeOH}$ frequency and population analysis

 $2 \ 1$

Zn 2.2 C 2.096 O 1.576 H 1.172

A.2 NAMD Parameters

A.2.1 CHARMM27

Standard CHARMM27 parameters were used, with the CYM residue using the fol-

lowing parameterization:

RESI CYM -1.00! Thiolate form ! Foloppe, N., J. Sagemark, K. Nordstrand, K.D. Berndt, and L. Nilsson ! (2001). J. Mol. Biol. 310:449-470.! Atom types and charges transfered from methythiolate GROUP ATOM N NH1 -0.47 ! ATOM HN Η 0.31! HN-N ATOM CA CT10.07 ! HB1 ATOM HA $H\!B$ 0.09! GROUP HA-CA-CB-SG (thiolate) ! ATOM CB CS -0.38! ATOM HB1 HA HB2 0.09 ! ATOM HB2 HA 0.09 ! O=C ATOM SG SS-0.80! GROUP ATOM C \mathbf{C} 0.51ATOM O Ο -0.51BOND CB CA SG CB N HN N CA BOND O C C CA C +N CA HA CB HB1 CB HB2 IMPR N -C CA HN C CA +N O DONOR HN N ACCEPTOR O C IC –C CA *NHN $1.3479\ 123.9300\ 180.0000\ 114.7700\ 0.9982$ IC –C Ν CA \mathbf{C} $1.3479 \ 123.9300$ 180.0000 105.8900 1.5202IC N 180.0000 118.3000 CA \mathbf{C} +N1.4533 105.8900 1.3498IC +N CA*CΟ 1.3498 118.3000 $180.0000 \ 120.5900$ 1.2306IC CA \mathbf{C} +N+CA $1.5202 \ 118.3000$ $180.0000 \ 124.5000$ 1.4548IC N \mathbf{C} *CA CB $1.4533 \ 105.8900$ 121.7900 111.9800 1.5584IC N \mathbf{C} *CA HA $1.4533 \ 105.8900 \ -116.3400 \ 107.7100$ 1.0837IC N CACB SG $1.4533 \ 111.5600$ 180.0000 113.8700 1.8359IC SGCA*CB HB1 $1.8359 \ 113.8700$ 119.9100 107.2400 1.1134IC SG CA *CB HB2 $1.8359\ 113.8700\ -125.3200\ 109.8200\ 1.1124$

A.2.2 AMBER FF09

Standard FF09 parameters were used.

A.2.3 OPLS-ua

The top	pology fil	e
* DK's	& HP's TO	P
*		
22	1	
MASS	1 HT	1.00800 H ! TIPS3P WATER HYDROGEN
MASS	2 OT	15.99940 O ! TIPS3P WATER OXYGEN
MASS	3 OH	15.99940 O ! Hydronium oxygen
MASS	4 HH	1.00800 H ! Hydronium hydrogen
MASS	$5~\mathrm{HC}$	1.00800 H ! Hydrogen to carbon
MASS	6 HN	1.00800 H !
MASS	7 C	12.00000 C
MASS	8 N	14.00700 N
MASS	$9~\mathrm{HQ}$	1.00800 H
MASS	10 OQ	16.00000 O
MASS	11 BE	9.00000 Be
MASS	12 HS	1.00800 H ! SPCE WATER HYDROGEN
MASS	13 OS	15.99940 O ! TIPS3P WATER OXYGEN
MASS	14 Kr	83.00000 Kr ! Check mass number
MASS	15 Ne	20.00000 Ne ! Check mass number
MASS	$16~\mathrm{KG}$	83.00000 KG ! Krypton Guissani
MASS	$17 \ \mathrm{NG}$	20.00000 NG ! Neon Guissani
MASS	18 HF	1.00800 H ! Formate hydrogen
MASS	19 CF	12.00000 C ! Formate Carbon
MASS	20 OF	15.99940 O ! Formate Oxygen
MASS	21 P	31.0000 P ! Phosphorus
MASS	22 CH4	16.0320 C ! Methane United atom check methane mass
MASS	23 CH3	15.0240 C ! Methyl
MASS	24 OA	15.99940 O ! Alcohol oxygen
MASS	$25~\mathrm{HA}$	1.00800 H ! Alcohol hydrogen
MASS	26 CHE	15.0240 C ! Methyl in Ethane
MASS	27 CHK	15.0240 C ! Methyl KBFF for Methanol JPCB 109 2005 15080-15086
MASS	28 OAK	15.99940 O ! Alcohol oxygen KBFF
MASS	28 HAK	1.00800 H ! Alcohol hydrogen KBFF
MASS	29 NPC	12.0000 C ! Neopentane center carbon

MASS 30 NPX 15.99940 C ! Neopentane methyl groups MASS 196 ZN 65.370000 ZN ! zinc (II) cation

AUTO ANGLES DIHE

 RESI TIP3
 0.000

 GROUP
 OT
 -0.834

 ATOM OH2
 OT
 -0.417

 ATOM H1
 HT
 0.417

 ATOM OH2
 HT
 0.417

 BOND OH2
 H1 OH2 H2
 H2

 ANGLE H1
 OH2 H2
 H2

 ACCEPTOR
 OH2
 CAST NONE

 RESI SPCE
 0.000

 GROUP
 ATOM OH2
 OS
 -0.8476

 ATOM H1
 HS
 0.4238

 ATOM H2
 HS
 0.4238

 BOND OH2
 H1 OH2
 H2 H1 H2

 ANGLE H1
 OH2 H2
 H2

 ACCEPTOR
 OH2
 OH2

RESI 02M -1.000 GROUP ATOM 0M1 OS -0.5000 ATOM 0M2 OS -0.5000 ACCEPTOR 0M1 ACCEPTOR 0M2 PATCHING FIRST NONE LAST NONE

RESI KRYP 0.000 GROUP ATOM Kr Kr 0.000 PATCHING FIRST NONE LAST NONE

RESI MET 0.000 GROUP ATOM CH4 CH4 0.000 PATCHING FIRST NONE LAST NONE RESI MEOH 0.000 GROUP ATOM C CH30.265ATOM O -0.700OA ATOM H HA 0.435BOND C O O H ANGLE C O H DONOR н о ACCEPTOR O C PATCHING FIRST NONE LAST NONE RESI MOHK 0.000 GROUP ATOM C CHK 0.300ATOM O OAK -0.820ATOM H HAK 0.52BOND C O O H C H ANGLE C O H DONOR Н О ACCEPTOR O C PATCHING FIRST NONE LAST NONE RESI ETH 0.000 GROUP ATOM C1 CHE 0.000 ATOM C2 CHE 0.000 BOND C1 C2 PATCHING FIRST NONE LAST NONE 0.000 RESI NEOP GROUP ATOM CC NPC 0.000 ATOM C1 NPX 0.000 ATOM C2 NPX 0.000 ATOM C3 NPX 0.000 ATOM C4 NPX 0.000 BOND CC C1 CC C2 BOND CC C3 CC C4 ANGLE C1 CC C2 C2 CC C3

ANGLEC3CCC4CCC1ANGLEC1CCC3C2CCC4PATCHINGFIRSTNONELASTNONE

RESI KRYG 0.000 GROUP ATOM KG KG 0.000 PATCHING FIRST NONE LAST NONE

RESI NEO 0.000 GROUP ATOM Ne Ne 0.000 PATCHING FIRST NONE LAST NONE

RESI NEG 0.000 GROUP ATOM NG NG 0.000 PATCHING FIRST NONE LAST NONE

 RESI 3PIT
 0.000

 GROUP
 0.000

 ATOM 0H2
 0.000

 ATOM H1
 HT
 0.000

 ATOM H2
 HT
 0.000

 BOND 0H2
 H1
 0.000

 ANGLE H1
 0H2
 H2
 H1
 H2

 ACCEPTOR
 0H2
 NONE
 LAST NONE
 NONE

 RESI H30
 1.000

 GROUP
 ATOM OH2
 OH
 -0.521

 ATOM H1
 HH
 0.507
 41000

 ATOM H2
 HH
 0.507
 41000

 ATOM H3
 HH
 0.507
 41000

 YE
 BOND OH2
 H1
 OH2
 H2
 OH2
 H3

 PATCHING FIRST
 NONE
 LAST NONE
 LAST NONE
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RESI O3H 0.000 GROUP ATOM OH2 OH 0.000

ATOM H1	ΗH		0.000)	
ATOM H2	ΗH		0.000)	
ATOM H3	ΗH		0.000)	
BOND OH2	H1	OH2	H2	OH2	H3
PATCHING	FIRS	ST NC	NE LA	AST N	ONE

RESI	OH3		0.00	0	
GROUI	2				
ATOM	O1	OS	0.00	0	
ATOM	O2	OS	0.00	0	
ATOM	O3	OS	0.00	0	
ATOM	O4	OS	0.00	0	
ATOM	H5	$_{ m HS}$	0.00	0	
ATOM	H6	$_{ m HS}$	0.00	0	
ATOM	H7	$_{ m HS}$	0.00	0	
ATOM	H8	$_{ m HS}$	0.00	0	
ATOM	H9	$_{ m HS}$	0.00	0	
ATOM	H10	$_{ m HS}$	0.00	0	
ATOM	H11	$_{ m HS}$	0.00	0	
PATCI	HING	FIRST	NONE L	AST 1	NONE

RESI	H5O2			1.000	
GROUI	þ				
ATOM	H1	HQ		0.505	
ATOM	O2	OQ		-0.734	
ATOM	O3	OQ		-0.730	
ATOM	H4	HQ		0.474	
ATOM	H5	HQ		0.505	
ATOM	H6	HQ		0.475	
ATOM	H7	HQ		0.505	
! BON	JD H1	O2	H1	O3	
! BON	JD O2	H6	O2	H7	
! BON	JD 03	H4	O3	H5	
PATCI	HING 1	FIRST	N	ONE LAST NON	Ð

 RESI 205H
 0.000

 GROUP
 4000

 ATOM H1
 HQ
 0.000

 ATOM O2
 OQ
 0.000

 ATOM O3
 OQ
 0.000

ATOM H4	HQ		0.000
ATOM H5	HQ		0.000
ATOM H6	HQ		0.000
ATOM H7	HQ		0.000
! BOND H1	O2	H1	O3
! BOND O2	H6	O2	H7
! BOND O3	H4	O3	H5
PATCHING 1	FIRST	N	ONE LAST NONE

RESI IMD		0.000	
GROUP			
ATOM N1	Ν	-0.090	
ATOM C2	С	0.232	
ATOM N3	Ν	-0.716	
ATOM C4	С	0.217	
ATOM C5	С	-0.375	
ATOM H1	HN	0.318	
ATOM H2	HC	0.102	
ATOM H4	HC	0.082	
ATOM H5	HC	0.230	
PATCHING	FIRST	NONE LAST	NONE

RESI DM	П	0.000	
GROUP			
ATOM N1	Ν	0.000	
ATOM C2	С	0.000	
ATOM N3	Ν	0.000	
ATOM C4	С	0.000	
ATOM C5	С	0.000	
ATOM H1	HN	0.000	
ATOM H2	HC	0.000	
ATOM H4	HC	0.000	
ATOM H5	HC	0.000	
PATCHIN	G FIRST	NONE LAST N	NONE

RESI IMP	•	1.000
GROUP		
ATOM N1	Ν	-0.115
ATOM C2	С	0.011
ATOM N3	Ν	-0.123
ATOM C4	С	-0.140

ATOM C5	\mathbf{C}	-0.122	
ATOM H1	HN	0.399	
ATOM H2	HC	0.230	
ATOM H3	HN	0.403	
ATOM H4	HC	0.232	
ATOM H5	HC	0.225	
PATCHING	FIRST	NONE LAST	NONE

RESI	PMI			0.000	
GROUP	•				
ATOM	N1	Ν		0.000	
ATOM	C2	С		0.000	
ATOM	N3	Ν		0.000	
ATOM	C4	С		0.000	
ATOM	C5	С		0.000	
ATOM	H1	HN		0.000	
ATOM	H2	HC		0.000	
ATOM	H3	HN		0.000	
ATOM	H4	HC		0.000	
ATOM	H5	HC		0.000	
PATCH	IING	FIRST	NO	NE LAST	NONE

RESI BER		2.000	
GROUP			
ATOM BE1	BE	2.000	
PATCHING	FIRST	NONE LAST NONE	

RESI BE4		2.000
GROUP		
ATOM BE1	BE	1.664
ATOM O2	OQ	-1.093
ATOM O3	OQ	-1.093
ATOM O4	OQ	-1.097
ATOM O5	OQ	-1.097
ATOM H6	HQ	0.589
ATOM H7	HQ	0.591
ATOM H8	HQ	0.590
ATOM H9	HQ	0.588
ATOM H10	HQ	0.589
ATOM H11	HQ	0.591

ATOM H12 HQ 0.590 ATOM H13 HQ 0.588 PATCHING FIRST NONE LAST NONE

RESI	FOF	3	-1.000	
ATOM	H1	HF	-0.100	
ATOM	C2	CF	0.620	
ATOM	O3	OF	-0.760	
ATOM	O4	OF	-0.760	
PATCH	ING	FIRST	NONE LAST NONE	2

0.000 RESI BEO GROUP ATOM O1 OF -0.659097ATOM C1 CF 0.498766ATOM O2 OF -0.393698ATOM C2 CF 0.484823ATOM O3 OF -0.390139ATOM O4 OF -0.655186ATOM BE1 BE 1.114531PATCHING FIRST NONE LAST NONE

RESI	BEP		1.00000
GROUI	þ		
ATOM	BE1	BE	1.70000
ATOM	Р	Р	1.90000
ATOM	01	OF	-0.70700
ATOM	O2	OF	-1.30000
ATOM	O3	OF	-0.64400
ATOM	O4	OF	-0.70700
ATOM	H5	HF	0.37900
ATOM	H6	HF	0.37900
PATCI	IING	FIRST	NONE LAST NONE

RESI PHO			-1.00000
GROUP	•		
ATOM	Р	Р	1.36617
ATOM	O1	OF	-0.78008
ATOM	O2	OF	-0.87714
ATOM	O3	OF	-0.70454

```
ATOMO4OF-0.70712ATOMH5HF0.3526ATOMH6HF0.35011PATCHINGFIRSTNONE LAST NONE
```

RESI ZN2 2.00 ! Zinc ion, Roland Stote GROUP ATOM ZN ZN 2.00 PATCHING FIRST NONE LAST NONE

END

The parameter file

 \ast DK's and HP's param file

*

BONDS

$_{\mathrm{HS}}$	$_{ m HS}$	0.000	1.6323	! SPCE HS-HS distance
ΗT	ΗT	0.000	1.5139	! Required for shake
OT	ΗT	450.000	0.9572	!
OS	$_{ m HS}$	450.000	1.0000	! SPCE OS-HS distance is different
OQ	HQ	450.000	0.9572	! Zundel dummy values
OS	OS	450.000	1.3100	! For superoxide largely dummy
OH	HH	450.000	0.9700	
Ν	С	200.000	1.3600	
Ν	HN	450.000	1.0000	
\mathbf{C}	HC	400.000	1.0800	
\mathbf{C}	\mathbf{C}	200.000	1.3600	
OA	HA	553.000	0.9600	! JPCB 111 2007 4467 -4476 &
CH3	OA	386.000	1.4250	! JACS 106 1984 $765-784$
CH3	HA	0.000	1.9550	! Required for shake
CHE	CHE	0.000	1.5300	! JACS 106 1984 $6638 - 6646$
OAK	HAK	553.000	0.9450	! JPCB 109 2005 $15080 - 15086$
CHK	OAK	386.000	1.4300	! JACS 106 1984 $765-784$
CHK	HAK	0.000	1.9480	! For shake
NPC	NPX	268.000	1.5300	! Supplementary info JACS 118 Page 11225
ANGI	ES			

ΗT	OT	ΗT	55.000	104.5200
$_{\mathrm{HS}}$	OS	HS	55.000	109.4000 ! SPCE uses tetrahedral

ΗH	OH	HH	55.000	114.0000	
HQ	OQ	HQ	0.000	0.0000	! Zundel dummy values
OQ	HQ	OQ	0.000	0.0000	! Zundel dummy values
CH3	OA	HA	55.000	108.5000	
CHK	OAK	HAK	55.000	108.5000	! same as OPLS
NPX	NPC	NPX	58.35	109.4700	! Fixing at tetrahedral angle

DIHEDRAL

OQ HQ OQ HQ 0.00 0.000 ! Zundel dummy

NONBONDED nbxmod 5 atom cdiel shift vatom vdistance vswitch cutnb 14.0 ctofnb 12.0 ctonnb 10.0 **eps** 1.0 e14fac 1.0 wmin 1.5

OT	0.000000	-0.152100	1.768200	
ΗT	0.000000	-0.046000	0.224500	
OS	0.000000	-0.155394	1.776600	! SPCE Oxygen
HS	0.000000	0.000000	0.000000	! SPCE hydrogen has no sigma
OQ	0.000000	-0.152100	1.768200	
HQ	0.000000	-0.046000	0.224500	
OH	0.000000	-0.152100	1.768200	
HH	0.000000	-0.046000	0.224500	
Ν	0.000000	-0.017000	1.824000	
С	0.000000	-0.086000	1.908000	
HN	0.000000	-0.015700	0.600000	
HC	0.000000	-0.015000	1.359000	
BE	0.000000	-0.018680	1.143900	! Using Aqvist Li+ parameters
KG	0.000000	-0.335800	2.062500	! Krypton from Guissani/Straatsma
Kr	0.000000	-1.500000	1.829600	! Krypton fit to MP2 results
Ne	0.000000	-0.300000	1.433900	! Neon fit to MP2 results
NG	0.000000	-0.036880	1.703300	! Neon from Guissani/Straatsma
CF	0.000000	-0.070000	2.000000	! Formate carbon
OF	0.000000	-0.120000	1.700000	! Formate oxygen
HF	0.000000	-0.046000	0.224500	! Formate hydrogen
Р	0.000000	-0.585000	2.150000	! Phosphorus atom
CH4	0.000000	-0.294000	2.093390	! Jorgensen methane
CH3	0.000000	-0.207000	2.118650	! Methonal (methyl) JPC 90 1986 1276-1284
OA	0.000000	-0.170000	1.722980	! Alcohol oxygen JPC 90 1986 1276-1284
HA	0.000000	0.000000	0.000000	! Alcohol hydrogen
CHE	0.000000	-0.207000	2.118650	! Ethane (methyl) JACS 106 1984 6638-6646
CHK	0.000000	-0.207270	2.103490	! Methonal (methyl) JPC 90 1986 1276-1284
OAK	0.000000	-0.155500	1.791450	! Alcohol oxygen JPC 90 1986 1276-1284

```
HAK
       0.000000
                 -0.021030
                               0.886750 ! Alcohol hydrogen
NPX
       0.000000
                 -0.145000
                               2.222470 ! JACS 106 1984 6638-6646
NPC
       0.000000
                 -0.050000
                               2.132670 ! JACS 106 1984 6638-6646
ZN
       0.000000
                 -0.250000
                               1.090000 ! ALLOW ION
                ! RHS March 18, 1990
```

END

A.3 NAMD Input files

A.3.1 Ion and Solvent MD

Running simulation for ZnMeOH with 5 mol% $M\!eO\!H$

#######################################	- - -	/////////////////////////////////////
## ADJUSTABLE PARAMETERS		##
		/////////////////////////////////////

set simname	MeOH_15
structure	\$simname.psf
coordinates	\$simname.pdb
set temperature	298
set outputname	\$simname

firsttimestep 0

++++++++++++++++++++++++++++++++++++++	- - -
## SIMULATION PARAMETERS	##

Input paraTypeCharmm on parameters par.inp temperature \$temperature

Force-Field Parameters

exclude	scaled 1-4
1-4scaling	1.0
cutoff	12
switching	on
switchdist	10
pairlistdist	13.5

Integrator Parameters timestep 2.0 ;# 1fs/step rigidBonds none ;# needed **for** 2fs steps nonbondedFreq 1 fullElectFrequency 2 stepspercycle 10

# Constant Temperat	ure	Control
langevin	on	;# do langevin dynamics
langevinDamping	5	;# damping coefficient (gamma) of $5/ps$
langevinTemp		\$temperature
langevinHydrogen	off	;# don't couple langevin bath to hydrogens

Periodic Boundary Conditions

cellBasisVector1	35	0	0
cellBasisVector2	0	35	0
cellBasisVector3	0	0	35
cellOrigin	12	12	12

wrapAll on

Fixed Atoms
#fixedAtoms on
#fixedAtomsFile \$simname.pdb
#fixedAtomsCol B
PME (for full-system periodic electrostatics)
PME yes
PMEGridSizeX 64
PMEGridSizeY 64
PMEGridSizeZ 64

 # Constant Pressure Control (variable volume)

 useGroupPressure
 yes ;# needed for rigidBonds

 useFlexibleCell
 no

 useConstantArea
 no

langevinPistononlangevinPistonTarget1.01325 ;# in bar -> 1 atmlangevinPistonPeriod100langevinPistonDecay50langevinPistonTemp\$temperature

Output

outputName	\$outputn	ame	
restartfreq	1000	;#	1000 steps = every 1 ps
dcdfreq	125		
xstFreq	1000		
outputEnergies	500		
outputPressure	500		

+++++++++++++++++++++++++++++++++++++++	
## EXTRA PARAMETERS	////
+++++++++++++++++++++++++++++++++++++++	

A.3.2 Protein MD

+++++++++++++++++++++++++++++++++++++++	
## JOB DESCRIPTION	##
+++++++++++++++++++++++++++++++++++++++	#######################################

Minimization , Equilibration , and measuring pair interactions between

set simname	zinc_finger
amber	yes
parmfile	berg_dz.top
coordinates	berg_dz.pdb
bincoordinates	berg_dz.coor
binvelocities	berg_dz.vel
set temperature	298
set outputname	berg_dz
firsttimestep	0

+++++++++++++++++++++++++++++++++++++++	########
## SIMULATION PARAMETERS	##
+++++++++++++++++++++++++++++++++++++++	/////////////////////////////////////

Force-Field Parameters

exclude	$\operatorname{scaled} 1-4$
1-4scaling	1.0
cutoff	12
switching	on
switchdist	10
pairlistdist	13.5

Integrator Parameters

timestep	1.0	;#	$1 \mathrm{fs} / \mathrm{ste}$	р		
rigidBonds	all	;#	needed	for	$2\mathrm{fs}$	steps
nonbondedFreq	1					
fullElectFrequency	2					
stepspercycle	10					

Constant Temperature Control langevin on ;# do langevin dynamics langevinDamping 5 ;# damping coefficient (gamma) of 5/ps

langevinTemp \$temperature

langevinHydrogen

off ;7

Periodic Boundary Conditions

cellBasisVector1	47	0	0
cellBasisVector2	0	53	0
cellBasisVector3	0	0	47
cellOrigin	0	0	0

wrapAll on

PME (for full-system periodic electrostatics)
PME yes
PMEGridSizeX 64
PMEGridSizeY 64
PMEGridSizeZ 64

Constant Pressure Control (variable volume)

useGroupPressure	yes	;#	needed	for	rigidBonds
useFlexibleCell	no				
useConstantArea		no			

langevinPiston	on
langevinPistonTarget	1.01325 ;# in bar \rightarrow 1 atm
langevinPistonPeriod	200
langevinPistonDecay	100
langevinPistonTemp	\$temperature

Output

outputName	\$output	name
restartfreq	500	;# 500steps = every 1ps
dcdfreq	500	
xstFreq	500	
outputEnergies	10	
outputPressure	10	

A.3.3 Trajectory Analysis

#######################################	+++++++++++++++++++++++++++++++++++++++
## JOB DESCRIPTION	##
+++++++++++++++++++++++++++++++++++++++	

Calculating Interaction Energies between zinc and water

###	///-	##	44	<u> - </u>	44	#	-	#	44	#	#1	44	+#	#	#+	#	H	4	#	#-	#	Ή	+#	#	#	#	++	#	#	#-	#	H	#	#	#-	#	H	H	+#	#	#	#	#+	#	11	H	H	ŧ
##	А	D,	JU	SЛ	ΓA	Bl	LE	ł	PA	R	Al	M	E	ΓF	R	S																														#	+	Ł
 - - 	/// -	 - 	44	 - 	44	#		#	4-1	4	#	44		//	#-	#		4		#-	#	44	++	#	#	#	///	4	//	#-	44	// /	4	//	#-	4	// /	H	4	#	#	#	#-	44	+	++	H	ŧ

set simname	MeOH_15
structure	\$simname.psf
coordinates	\$simname.pdb
extendedSystem	\$simname.xsc
<pre>set temperature set outputname</pre>	298 \$simname.pair
firstTimestep	0
pairInteraction	on

pairInteractionGroup1 0

pairInteractionFile \$simname.meth.pdb

 ${\tt pairInteractionGroup2} \ 1$

pairInteractionCol

В

Input

paraTypeCharmm	on
parameters	par.inp
temperature	\$temperature

Force-Field Parameters

exclude	$\operatorname{scaled} 1-4$
1-4scaling	1.0
cutoff	12
switching	on
switchdist	10
pairlistdist	13.5
COMmotion	yes

Periodic Boundary Conditions

cellBasisVector1	36	0	0
cellBasisVector2	0	36	0
cellBasisVector3	0	0	36
cellOrigin	0	0	0

wrapAll

PME (for full-system periodic electrostatics)

on

PME	yes
PMEGridSizeX	64
PMEGridSizeY	64
PMEGridSizeZ	64

Output

outputName \$outputname

7	4	#		E	X	1	Π	R	A		F	2	1	F	l	1	V	1	E	Ι	ł	T)	R	S	5																																																					ŧ	#	#	Ĺ
_	ų	11	11	11	11	4	н	1	μ	4	1	Ц	ų	4	4	4	μ	1	μ	4	4	4	4	μ	1	н	ų	1	Ь	ų		Ц	ų		4	ų	11	4	1	μ	1	Ц	u	4	4	4	1	/	ų	4	4	Ь	μ	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	4	н	4	11	11	1	4	н	4	11	11		μ	y.,	ų	μ	4	μ	4	μ.	11	4		4	μ	4	Ļ
7	t	++-	Ħ	++	H	1	4	H	4-	Ħ		4	t	Ħ	1	4	t	11	4	t	Ħ	-h	+	+	+	4	t	Ħ	4	t	Ħ	7	t	Ħ	7	t	Ħ	1	++	H	Ħ	4	+	Ħ	7	t	Ħ	Н	t	Ħ	-11	4	7-	Ħ	1	4	$t \rightarrow$	H	Ħ	++	1	4	$t \rightarrow$	1	H	Ħ	4	++	t	Ħ	Ħ	-	++	+	Ħ	Ħ	-	t + t	H	++	-

```
set ts 0
coorfile open dcd $simname.dcd
while { ![coorfile read] } {
   firstTimestep $ts
   run 0
   incr ts 1
}
coorfile close
```

A.4 NWCHEM Input files

A.4.1 Preparation

 $\# {\rm Creates}$ files for optimization of the berg zinc fingerG

```
start berg
prepare
system berg
source berg_orig.pdb
new_top new_rst
center
 orient
 solvate 5.0
modify atom 202:ZN quantum
modify atom 45:_CB quantum
modify atom 45:3HB quantum
modify atom 45:2HB quantum
modify atom 45:_SG quantum
modify atom 50:_CB quantum
modify atom 50:3HB quantum
modify atom 50:2HB quantum
modify atom 50:_SG quantum
modify atom 63:_NE2 quantum
```

```
modify atom 63:_CG quantum
 modify atom 63:_ND1 quantum
 modify atom 63:_CE1 quantum
 modify atom 63:_CD2 quantum
 modify atom 63:_HD2 quantum
 modify atom 63:_HE1 quantum
 modify atom 63:_HD1 quantum
 modify atom 67:_NE2 quantum
 modify atom 67:_CG quantum
 modify atom 67:_ND1 quantum
 modify atom 67:_CE1 quantum
 modify atom 67:_CD2 quantum
 modify atom 67:_HD2 quantum
 modify atom 67:_HE1 quantum
 modify atom 67:_HD1 quantum
 update lists
ignore
 write berg.rst
 write berg.pdb
\mathbf{end}
```

task prepare

A.4.2 Optimization

```
memory total 8192 mb
scratch_dir scratch
start berg
# LANL2DZ ECP EMSL Basis Set Exchange Library 2/8/12 1:45 PM
# Elements
                                         References
# ----
\# H - Ne: T. H. Dunning Jr. and P. J. Hay, in Methods of Electronic Structure
# Theory, Vol. 2, H. F. Schaefer III, ed., PLENUM PRESS (1977)
# Na - Hg: P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 270 (1985).
# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 284 (1985).
# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 299 (1985).
#
BASIS "ao basis" PRINT
\#BASIS SET: (4s) \rightarrow [2s]
Η
     \mathbf{S}
```

19.2384000	0.0328280
2.8987000	0.2312040
0.6535000	0.8172260
H S	
0.1776000	1.0000000
#BASIS SET: (10s,5p) ->	[3s,2p]
C S	
4233.0000000	0.0012200
634.9000000	0.0093420
146.1000000	0.0454520
42.5000000	0.1546570
14.1900000	0.3588660
5.1480000	0.4386320
1.9670000	0.1459180
C S	
5.1480000	-0.1683670
0.4962000	1.0600910
C S	
0.1533000	1.0000000
C P	
18.1600000	0.0185390
3.9860000	0.1154360
1.1430000	0.3861880
0.3594000	0.6401140
C P	
0.1146000	1.0000000
$\#BASIS SET: (10s, 5p) \rightarrow$	[3s,2p]
N S	
5909.0000000	0.0011900
887.5000000	0.0090990
204.7000000	0.0441450
59.8400000	0.1504640
20.0000000	0.3567410
7.1930000	0.4465330
2.6860000	0.1456030
N S	
7.1930000	-0.1604050
0.7000000	1.0582150
N S	
0.2133000	1.0000000

```
N P
```

	26.7900000	0.0182540			
	5.9560000	0.1164610			
	1.7070000	0.3901780			
	0.5314000	0.6371020			
Ν	Р				
	0.1654000	1.0000000			
#BAS	SIS SET: $(3s, 3p)$	-> [2s,2p]			
\mathbf{S}	S				
	1.8500000	-0.5324335			
	0.4035000	1.2763801			
\mathbf{S}	S				
	0.1438000	1.0000000			
\mathbf{S}	Р				
	4.9450000	-0.0608116			
	0.4870000	1.0132686			
\mathbf{S}	Р				
	0.1379000	1.0000000			
#BA\$	SIS SET: (3s,2p,5	$5d) \rightarrow [2s, 2p, 2d]$			
Zn	S				
	0.7997000	-0.6486112			
	0.1752000	1.3138291			
Zn	S				
	0.0556000	1.0000000			
Zn	Р				
	0.1202000	1.0000000			
Zn	Р				
	0.0351000	1.0000000			
Zn	D				
	68.8500000	0.0258532			
	18.3200000	0.1651195			
	5.9220000	0.4468212			
	1.9270000	0.5831080			
Zn	D				
	0.5528000	1.0000000			
END					
# El	lements		References		
#					
# Na	a – Hg: P. J. Hay	y and W. R. Wadt, J.	Chem. Phys.	82, 270	(1985).
#	P. J. Hay	y and W. R. Wadt, J.	Chem. Phys.	82, 284	(1985).
#	P. J. Hay	y and W. R. Wadt, J.	Chem. Phys.	82, 299	(1985).
#					

ECP	
S nelec 10	
S ul	
1 532.6685222	-10.0000000
2 108.1342248	-85.3593846
$2 \qquad 24.5697664$	-30.4513290
2 7.3702438	-10.3745886
2 2.3712569	-0.9899295
S S	
0 106.3176781	3.0000000
1 100.8245833	10.6284036
2 53.5858472	223.6360469
2 15.3706332	93.6460845
2 3.1778402	28.7609065
S P	
0 101.9709185	5.000000
1 93.2808973	6.0969842
2 65.1431772	285.4425500
2 24.6347440	147.1448413
2 7.8120535	53.6569778
2 2.3112730	8.9249559
Zn nelec 18	
Zn ul	
1 386.7379660	-18.0000000
2 72.8587359	-124.3527403
2 15.9066170	-30.6601822
2 4.3502340	-10.6358989
2 1.2842199	-0.7683623
Zn S	
0 19.0867858	3.0000000
1 5.0231080	22.5234225
2 1.2701744	48.4465942
2 1.0671287	-44.5560119
2 0.9264190	12.9983958
Zn P	
0 43.4927750	5.0000000
1 20.8692669	20.7435589
2 21.7118378	90.3027158
2 6.3616915	74.6610316

```
\mathbf{2}
          1.2291195
                                          9.8894424
Zn D
\mathbf{2}
        13.5851800
                                         -4.8490359
          9.8373050
                                          3.6913379
\mathbf{2}
\mathbf{2}
          0.8373113
                                         -0.5037319
END
dft
           xc b3lyp
\mathbf{end}
\operatorname{md}
           system berg
           noshake
\mathbf{end}
qmmm
           bqzone 9
           region qm
                                             solvent
                                 mm
           maxiter 500
                                  10000
                                             50000
           ncycles 10
           density static
           xyz berg.optim
\mathbf{end}
```

task qmmm dft optimize

B Calculation Scripts

B.1 Radial Distribution Function

```
VMD code:

mol new PPP

mol addfile DDD type dcd first FFF waitfor all

set ion [atomselect top "resname ZN2"]

$ion num

set meth_o [atomselect top "name O and pbwithin 15 of resname ZN2"]

$meth_o num

set meth_c [atomselect top "name C and pbwithin 15 of resname ZN2"]

$meth_c num
```

```
set wat_0 [atomselect top "name OH2 and pbwithin 15 of resname ZN2"]
$wat_0 num
set frames [molinfo 0 get numframes]
set frames [expr "$frames - 1"]
puts $frames
set res_0 [measure gofr $ion $meth_0 delta 0.1 rmax 10 first 0 last $frames usepbc true selupdate t
set res_c [measure gofr $ion $meth_c delta 0.1 rmax 10 first 0 last $frames usepbc true selupdate t
set wat_0 [measure gofr $ion $wat_0 delta 0.1 rmax 10 first 0 last $frames usepbc true selupdate tr
set out [open "OOO" w]
puts $out $res_0
puts $out $res_c
puts $out $wat_0
```

MATLAB Code

%Reads a gofr file generated from VMD and %plots the radial distribution function function plot_gofr(filename) A=importdata(sprintf('%s.gofr.fmt',filename), '_'); plot(A(1,:), A(4,:), '-k', A(5,:), A(8,:), '--b', A(9,:), A(12,:), '-.g', 'LineWidth',5) lh=legend('Zn-MeO', 'Zn-MeC', 'Zn-H2O') set(lh, 'FontSize',30); xlabel('r_(Angstroms)', 'FontSize',30) ylabel('g(r)', 'FontSize',30); axis([0 6 0 3]); set(gca, 'FontSize',30); print(sprintf('thesis_plots/%s_gofr.png', filename), '-dpng', '-r300'); end

B.2 Occupancy Probability

```
lappend meth_o_ctr 0
         lappend meth_c_ctr 0
         lappend num $counter
}
set frames [molinfo 0 get numframes]
for {set counter 0} {$counter < $frames } {incr counter} {</pre>
         wat_o frame counter
         $meth_o frame $counter
         $meth_c frame $counter
         $wat_o update
         $meth_o update
         $meth_c update
         set wat_o_ind [$wat_o num]
         if {$wat_o_ind >= [llength $wat_o_ctr]} {set $wat_o_ind [expr [llength $wat_o_ctr] - 1]}
         set meth_o_ind [$meth_o num]
         if \{\text{smeth}_o, \text{ind} \ge [\text{llength} \text{smeth}_o, \text{ctr}]\} {set \text{smeth}_o, \text{ind} [\text{expr} [\text{llength} \text{smeth}_o, \text{ctr}] - 1]
         set meth_c_ind [$meth_c num]
         if {$meth_c_ind >= [llength $meth_c_ctr]} {set $meth_c_ind [expr [llength $meth_c_ctr] - 1]
```

set wat_o_ctr [lreplace \$wat_o_ctr \$wat_o_ind \$wat_o_ind [expr [lindex \$wat_o_ctr \$wat_o_ind
set meth_o_ctr [lreplace \$meth_o_ctr \$meth_o_ind \$meth_o_ind [expr [lindex \$meth_o_ctr \$meth
set meth_c_ctr [lreplace \$meth_c_ctr [\$meth_c num] [\$meth_c num] [expr [lindex \$meth_c_ctr

}

set out [open 'WWW' w]
puts \$out \$num
puts \$out \$wat_o_ctr
puts \$out \$meth_o_ctr
puts \$out \$meth_c_ctr
close \$out

B.3 MD Free energy

After using the pair interaction energy script (Appendix A.3.3), the nrg file is further

processed

```
#!/usr/bin/perl -w
my($input, $title, $output)=@ARGV;
print "
A=importdata('$input');
allnrg=A(50:17500,:); \%interaction energy
```

```
intnrg=allnrg(:,6);
 elec=allnrg(:,3);
 vdw=allnrg(:,4);
mean(intnrg)
 std(intnrg)
 G=mean(intnrg)+var(intnrg)/2*beta;
B=exp(intnrg * beta);
C\!\!=\!\!sum(B) \ ./ \ length(B); \ \backslash \% This \ is \ the \ sum \ over \ the \ probabilities
D=log(C) / beta \%solving e^{(b*mu)} for mu
 [E,F] = hist(intnrg, 150);
E = E/sum(E);
 [thefit,thegof]=fit(F', E', 'gauss1')
 semilogy(F,E, 'ob')
 \mathbf{hold} \ \mathrm{on}
 semilogy(F, feval(thefit, F'));
 xlabel('Pair_interaction_energy_(kcal/mol)')
 ylabel('Probability')
 \tille(sprintf('Zn^{2+}/non-first-shell interaction energies, $title. \\\tille(sprintf('Zn^{2+}/non-first-shell interaction energies, $title(sprintf('Zn^{2+}/non-first-shell interaction energies, $title(sprint
 \mathbf{axis}\left(\left[\min(F)-10, \ \max(F)+10, \ \min(E), \max(E) \ \right]\right);
 print('-djpeg', '$output.hist.jpg');
 disp(', n')
 disp(sprintf('Approx:_%6.4f_Gaussian:_%6.4f_%6.4f_%6.4f_%6.4f_%6.4f_%6.4f_%6.4f_, ..., var(elec), var(elec), mea
```

C Results

- C.1 Radial distribution functions
- C.2 MD Interaction Energy Histograms



Figure 11: $Zn^{2+} [H_2O]_3 [MeOH]_3$ in water


Figure 12: $Zn^{2+} [H_2O]_1 [MeOH]_5$ in water



Figure 13: $Zn^{2+} [H_2O]_4 [MeOH]_2$ in water



Figure 14: $Zn^{2+} [H_2O]_3 [MeOH]_3$ in water



Figure 15: $Zn^{2+} [H_2O]_2 [MeOH]_4$ in water



Figure 16: $Zn^{2+} [H_2O]_1 [MeOH]_5$ in water



Figure 17: $Zn^{2+} [H_2O]_0 [MeOH]_6$ in water



Figure 18: $Zn^{2+} [H_2O]_0 [MeOH]_6$ in 5% MeOH and water



Figure 19: $Zn^{2+} [H_2O]_0 [MeOH]_6$ in 10% MeOH and water



Figure 20: $Zn^{2+} [H_2O]_0 [MeOH]_6$ in 15% MeOH and water