

# THE UNIVERSITY OF MISSOURI

ENGINEERING REPRINT SERIES

Reprint Number 20

\*\*\*

Engineering Experiment Station  
Columbia, Missouri

# Bulletin

Autotransformer Betters Motor Phase Conversion

JOSEPH C. HOGAN

*Associate Professor of Electrical Engineering*

Reprinted from  
ELECTRICAL WORLD

vol. 144, page 120, October 17, 1955

COLLEGE OF ENGINEERING  
THE ENGINEERING EXPERIMENT STATION

The Engineering Experiment Station was organized in 1909 as a part of the College of Engineering. The staff of the Station includes all members of the Faculty of the College of Engineering, together with Research Assistants supported by the Station Funds.

The Station is primarily an engineering research institution engaged in the investigation of fundamental engineering problems of general interest, in the improvement of engineering design, and in the development of new industrial processes.

The Station desires particularly to co-operate with industries of Missouri in the solution of such problems. For this purpose, there is available not only the special equipment belonging to the Station but all of the equipment and facilities of the College of Engineering not in immediate use for class instruction.

Inquiries regarding these matters should be addressed to

The Director,  
Engineering Experiment Station  
University of Missouri  
Columbia, Missouri

## THE UNIVERSITY OF MISSOURI BULLETIN

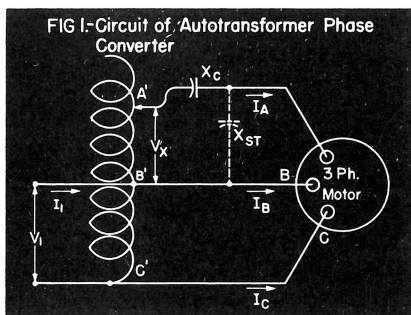
VOL. 57, NO. 20

ENGINEERING EXPERIMENT STATION REPRINT SERIES, NO. 4

Published by the University of Missouri at Room 102, Building T-3, Columbia, Missouri. Entered as second-class matter, January 2, 1914, at post office at Columbia, Missouri, under Act of Congress of August 24, 1912. Issued four times monthly October through May, three times monthly June through September.

500

Jan. 22, 1956



# Autotransformer Betters Motor Phase Conversion

Circuit of new static unit provides 3-phase currents to 3-phase induction motor from a single-phase line and also has a low starting kva requirement

JOSEPH C. HOGAN, Associate Professor, College of Engineering, Department of Electrical Engineering, University of Missouri, Columbia, Mo.

A new type of phase converter for stepping up voltage of one line employs an autotransformer in conjunction with the usual series capacitor. Its use permits relaxation of many limitations on the application of the capacitor-only phase converter, over which it has these advantages:

1. It is the only static phase converter available whose circuit provides balanced 3-phase currents to a 3-phase induction motor from a single-phase line.

2. The starting kva it requires is much less than that of a single-phase motor or a 3-phase motor on balanced 3-phase power.

3. Power factor is improved throughout the operating range of the motor.

4. Starting torque compares favorably with that of a single-phase motor.

5. Starting kva per ft.-lb is less than that of the single-phase or 3-phase motor.

6. Cost of autotransformer phase converter and 3-phase motor is competitive with that of a single-phase motor.

7. Simplicity of the 3-phase motor reduces maintenance.

8. Where 3-phase power may eventually become available, it permits immediate use of 3-phase motors.

9. Converter units of a given horse-power rating may be used with motors smaller than that rating.

A 3-phase motor operates ideally when balanced 3-phase voltages applied to the motor terminals result in balanced line currents. Theoretically this balance prevails for phase

converter-operated induction motors when the following equation is satisfied:

$$Z_m / \theta_m (N / 0^\circ + 1 / -60^\circ) = \frac{X_c}{\sqrt{3}} / 0^\circ \dots \quad (1)$$

where:

$Z_m$  = impedance per phase of the induction motor.  
 $\theta_m$  = power factor angle of the induction motor.

$N = \left| \frac{V_x}{V_{BC}} \right|$  as given by tap setting on the autotransformer.

$X_c$  = reactance of capacitors in series with line A (Fig 1).

As both autotransformer tap setting N and capacitive reactance  $X_c$  may be varied, the above equation can be satisfied for any polyphase induction motor, thus assuring balanced operation at a particular load. As load requirements change, the motor no longer has exactly balanced currents. Accordingly, the values of N and  $X_c$  must be adjusted initially to give balanced operation for the load condition normally encountered.

The theory of other types of phase converters may be treated as a special case of the autotransformer phase converter. Adjusting the tap setting A' to point B' makes  $V_x$  equal to zero. The autotransformer then has no effect on the operation of the phase converter, and the circuit is identical with that in the capacitor-only phase converter. When N equals zero, equation (1) becomes

$$Z_m / \theta_m - 60^\circ = \frac{X_c}{\sqrt{3}} / 0^\circ \dots \quad (2)$$

This equation can only be satisfied when

$$\theta_m = 60^\circ$$

$$X_c = \sqrt{3} Z_m \dots \quad (3)$$

From equation (3) it is seen that only the special case of power factor equal to 0.5 can be balanced. Usually this occurs only when the machine is very lightly loaded. Consequently the autotransformer is essential in phase converters to obtain the desired balanced operation for a motor operating under load.

Table I gives operating characteristics of the autotransformer phase converter derived from tests with a 3-phase, 220-v, 60-cps induction motor rated at 3 hp at 1,165 rpm. Load runs were made with the motor connected directly to a 3-phase line and again to a single-phase line through the phase converter. Separate runs were made for the phase converter adjusted to give balanced conditions.

Results of two runs with the phase converter set to give a balance at 70 and 110% of rated output are shown in Fig 2, where variation in line current is plotted as a func-

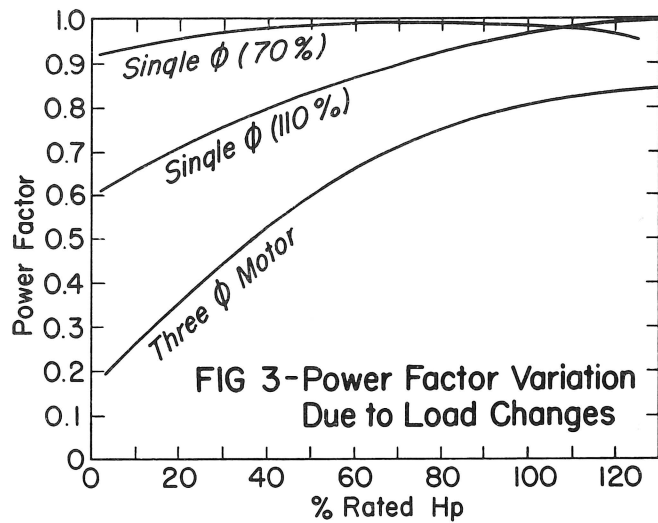
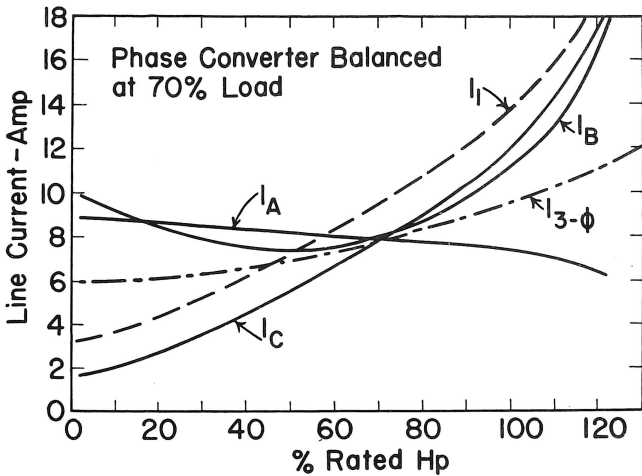
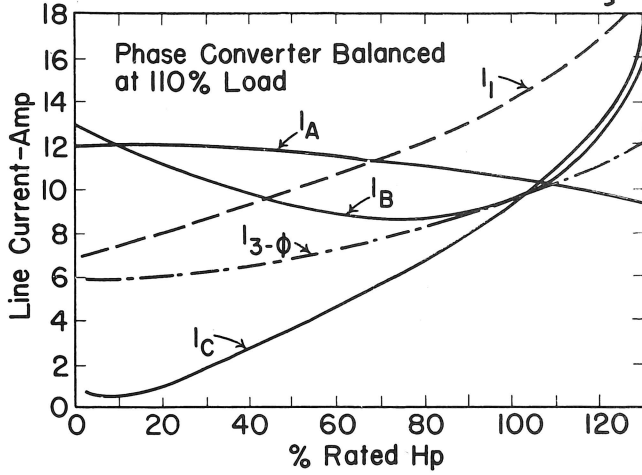
Table I—Operating Comparison, 3 H.P. Induction Motors

	3 $\phi$ Motor on 3 $\phi$	3 $\phi$ Motor, Autotran. Ph. Converter		Single $\phi$ Phase Motor
		70% Balance	110% Balance	
Line Volts	220	220	220	230
Breakdown Torque (% Rated Torque) $\phi$	250%	138%	145%	200%
Starting Current (Amps)	48	53	58	70
Starting Torque (% Rated Torque) $\phi$	210%	155%	195%	175%
Starting kva	18.3	11.7	12.8	16.1
Starting kva/ft.-lb.	.645	.57	.49	.68

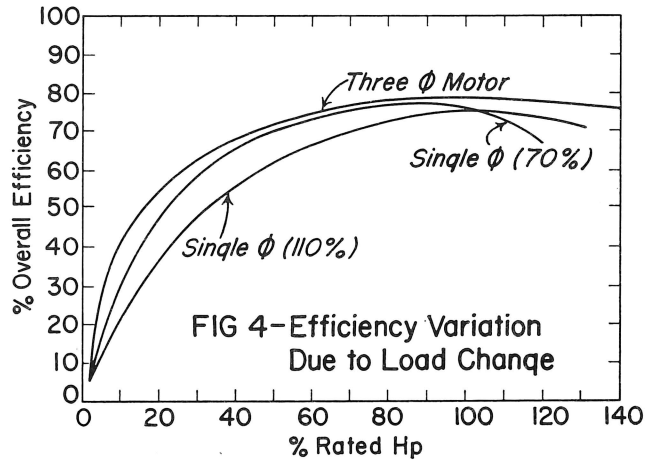
$\phi$  Rated Torque = 13.5 ft.-lbs.

$\phi\phi$  Capacitor Start—Capacitor Run

**FIG 2.-Current Variation from Load Changes**



**FIG 3-Power Factor Variation Due to Load Changes**



**FIG 4-Efficiency Variation Due to Load Change**

tion of horsepower output. The curves show that line currents can be balanced at particular load values, although current unbalance varies considerably as load increases or decreases from the point of balance.

Voltage variation because of line drop is a serious problem on rural single-phase lines. As voltage drop is proportional to line current, it is desirable to keep line current for a given power at a minimum. In other words the power factor should be as close to unity as possible. The excellent single-phase power factor characteristics of the autotransformer phase converter are compared in Fig 3 with the power factor of the 3-phase motor.

In matching a motor to a given load, torque variation as a function of speed is the most important factor. A motor operated through the phase converter has a speed-torque characteristic very similar to that of a motor operated directly on 3-phase up to loads of about 120% of rated horsepower. For loads in excess of this value speed drops very rapidly, and the breakdown torque is much lower than for 3-phase connection. For certain types of load occasionally requiring excessive torques, it may be necessary to use the next larger size motor.

The overall efficiency on single-phase using the phase converter is almost the same as the motor efficiency on balanced 3-phase. The only losses in the phase converter are core and copper losses of the autotransformer. Additional losses, however, occur in the motor for unbalanced operation because of negative sequence losses. This results in overall efficiencies approximately equal to the efficiency on 3-phase at points of balance. As unbalance

increases, the overall efficiency decreases because of the additional motor losses, as shown in Fig 4.

For starting an additional capacitor  $X_{ST}$  is required in the circuit to provide the required starting torque. This capacitor tends to balance currents at starting and is disconnected by means of a relay circuit sensitive to voltage  $V_{AB}$  after the motor comes up to speed. Characteristics at starting (locked rotor) are given in Table I. Characteristics of 3-hp, single-phase, general-purpose induction motors, as taken from recommended values in NEMA Standards, are also given for comparison.

The autotransformer phase converter thus has the lowest, ie, most desirable, value of kva per ft-lb at starting, and the autotransformer is just as essential to the circuit at starting as it is during running conditions. Recent tests on capacitor-only phase converters indicated a starting kva per lb-ft of 0.86, compared with 0.57 for the autotransformer phase converter balanced at 70% rated load.

The autotransformer phase converter-3-phase induction motor combination can be used as a source of power where only single-phase is available without the usual excessive voltage drop during starting. For loads requiring almost constant power the unit can be adjusted to give balanced operation at a high power factor for the particular load.

The autotransformer phase converter has two disadvantages. Although comparable to that of a single-phase motor, its breakdown torque is less than that of the 3-phase induction motor on balanced 3-phase power. Also, its starting torque is about 85% of that of the 3-phase motor and about that of a single-phase induction motor.

## PUBLICATIONS OF THE ENGINEERING REPRINT SERIES

Copies of the complete list of publications may be secured from the Director of the Engineering Experiment Station, University of Missouri

Reprint No.

- \*6. Design of Low Frequency Constant Time Delay Lines, by C. M. Wallis, Professor of Electrical Engineering. Reprinted from Transactions of the A.I.E.E., Vol.71, Part 1, p. 135, April 1952.
- \*7. The Engineer Becomes a Professional Manager, by Harry Rubey, Professor of Civil Engineering. Reprinted from the Journal of Engineering Education, Vol. 43, p. 338, January 1953.
8. Use of the Centrifugal Governor Mechanism as a Torsional Vibration Absorber, by O. A. Pringle, Assistant Professor of Mechanical Engineering. Reprinted from the Transactions of the A.S.M.E., Vol. 75, p. 59, January 1953.
- \*9. How to Plan for the Safe and Adequate Highways We Need, by Harry Rubey, Professor and Chairman of Civil Engineering. Reprinted from the General Motors "Better Highways Awards", 1953.
- \*10. A Dynamic Analogy of Foundation - Soil Systems, by Adrian Pauw, Associate Professor of Civil Engineering. Reprinted from Symposium on Dynamic Testing of Soils, Special Technical Publication No. 156, American Society for Testing Materials, 1953.
11. Ternary System Ethyl Alcohol--n--Heptane-Water at 30°C, by Joseph L. Schweppe, Research Engineer, C. F. Braun and Co. and James R. Lorah, Associate Professor Chemical Engineering. Reprinted from Industrial and Engineering Chemistry, Vol. 26, p. 2391, November 1954.  
The Rectifying Property of Polarized Barium Titanate, by Donald L. Waidelich, Associate Director, Engineering Experiment Station and Professor of Electrical Engineering. Reprinted from Journal of the Acoustical Society of America, Vol. 25, p. 796, July 1953.
12. Chip Breakers Studies 1, Design and Performance of Ground Chip Breakers, Erik K. Henriksen, Associate Professor of Mechanical Engineering  
Balanced Design Will Fit the Chip Breaker to the Job, from American Machinist, April 26, 1954, pp. 117-124, Special Report No. 360  
How to Select Chip Breakers I, II, III, from American Machinist, May 10, 1954, pp. 179, 181, 183, Reference Book Sheets  
Chip Breaking-A Study of Three-Dimensional Chip Flow, from page No. 53-5-9, presented at the A.S.M.E. Spring Meeting, Columbus, Ohio, April 28-30, 1953  
Economical Chip Breakers for Machining Steel, from Technical Aids to Small Business, May 1954, pp. 1-8
13. The Design of Sampled-Data Feedback Systems by Gladwyn V. Lago, Associate Professor of Electrical Engineering and John G. Truxal, Polytechnic Institute of Brooklyn. Reprinted from Transactions of the A.I.E.E., Vol. 73, Part 2, p. 247, 1954.
14. Selection of Personnel by George W. Elliott, Assistant Professor of Mechanical Engineering. Reprinted from the 1954 Transcript of the Midwest Feed Production School.
15. Lightweight Aggregates for Structural Concrete by Adrain Pauw, Associate Professor of Civil Engineering. Reprinted from the Proceedings of the A.S.C.E., Vol. 81, Separate No. 584, January 1955.
16. Coating Thickness Measurements Using Pulsed Eddy Currents by Donald L. Waidelich, Associate Director, Engineering Experiment Station. Reprinted from the Proceedings of the National Electronics Conference, Vol. 10, February 1955.
17. Additions to Sample-Data Theory by G. V. Lago, Associate Professor of Electrical Engineering. Reprinted from the Proceedings of the National Electronics Conference, Vol. 10, February 1955.
18. Additions to Z-Transformation Theory for Sample-Data Systems by Gladwyn V. Lago, Associate Professor of Electrical Engineering. Reprinted from Transactions of the American Institute of Electrical Engineers, Vol. 74, January, 1955.
19. Tension Control for High Strength Structural Bolts by Adrian Pauw, Professor of Civil Engineering and Leonard L. Howard, Lakeland Engineering Associates, Inc., with a discussion on the Turn-of-the-Nut Method by E. J. Ruble, Association of American Railroads. Reprinted from the Proceedings of the American Institute of Steel Construction, National Engineering Conference, April 18-19, 1955.
20. Autotransformer Betters Motor Phase Conversion by Joseph C. Hogan, Associate Professor of Electrical Engineering. Reprinted from Electrical World, Vol. 144, page 120, October 17, 1955.

\*Out of Print



