

Supertranslations and Superrotations at the Black Hole Horizon

Laura Donnay,^{1,*} Gaston Giribet,^{2,3,†} Hernán A. González,^{1,‡} and Miguel Pino^{4,§}

¹Physique Théorique et Mathématique, Université Libre de Bruxelles and International Solvay Institutes,

²Departamento de Física, Universidad de Buenos Aires FCEN-UBA and IFIBA-CONICET,

Ciudad Universitaria, Pabellón 1, 1428 Buenos Aires, Argentina.

³Instituto de Física, Pontificia Universidad Católica de Valparaíso, Casilla 4950, Valparaíso 05101, Chile.

⁴Departamento de Física, Universidad de Santiago de Chile, Casilla 307, Santiago 9170124, Chile.

(Dated: 7 mars 2016)

We show that the asymptotic symmetries close to nonextremal black hole horizons are generated by an extension of supertranslations. This group is generated by a semidirect sum of Virasoro and Abelian currents. The charges associated with the asymptotic Killing symmetries satisfy the same algebra. When considering the special case of a stationary black hole, the zero mode charges correspond to the angular momentum and the entropy at the horizon.

I. INTRODUCTION

Infinite-dimensional symmetries play a central role in the holographic description of black holes. The prototypical example is the microscopic derivation of the entropy of asymptotically AdS₃ black holes [1] in terms of the Virasoro algebra at infinity [2]. Virasoro and affine Kac-Moody algebras also appear in the description of non-AdS black holes in three dimensions [3–7] and, in higher dimensions, they govern the physics in the near horizon of rapidly rotating Kerr black holes [8].

Recently, Hawking, Perry, and Strominger claimed that nonextremal stationary black holes also exhibit infinite-dimensional symmetries in the near horizon region, known as supertranslations [9], and they suggested that this observation could contribute to solving the information paradox for black holes [10]. The symmetry observed in [9] is similar to the one that arises in asymptotically flat spacetimes at null infinity [11–13], usually referred to as Bondi-Metzner-Sachs (BMS). The corresponding algebra is an infinite-dimensional extension of the translation part of Poincaré.

In the last years, BMS algebra has been reconsidered in relation to flat space holography [14–23]; that is, the attempt to extend the AdS/CFT holographic correspondence to asymptotically flat spacetimes. In AdS/CFT, a crucial ingredient is the asymptotic isometry group. From the Anti-de Sitter (AdS) bulk point of view it is seen as the symmetries that preserve the form of the geometry close to the boundary region, where the dual conformal field theory (CFT) is located, while from the point of view of the CFT it corresponds to the local conformal group. In flat space holography, the conformal symmetry at the boundary is replaced by the BMS symmetry at the null infinity region. Furthermore, in addition to BMS super-translations, the symmetries at null infinity include super-rotations and central extensions [16-20, 24]; see also [25]. In presence of black holes, besides the null infinity region, there exists a second codimension 1 null hypersurface near which the geometry is flat : the black hole event horizon. Therefore, a natural question is whether the features associated with holography, such as the enhanced BMS symmetry, also appear in the near horizon geometry of black holes. In this Letter, we will show that for an adequate choice of boundary conditions, the nearby region to the horizon of a stationary black hole exhibits a generalization of supertranslation, including a semidirect sum with superrotations, represented by Virasoro algebra. In this sense, both supertranslations and superrotations arise close to the horizon. However, this particular extension differs from the extended BMS at null infinity [17, 18].

The Letter is organized as follows : In section II A, as entrée, we consider the three-dimensional case. This allow us to identify the appropriate boundary conditions at the horizon and construct a family of exact solutions satisfying them. This family includes, as a particular case, the Bañados-Teitelboim-Zanelli (BTZ) black holes [26]. We compute the algebra obeyed by the asymptotic Killing vectors and show that they expand supertranslations in semidirect sum with superrotations. The charges associated with such asymptotic symmetries are shown to expand the same algebra and by evaluating them on the BTZ solution, we verify that they correspond to the angular momentum and the entropy of the black hole. We follow the same strategy in section IIB, where we address the four-dimensional case. We demonstrate that the symmetry group generated by these charges correspond to two copies of Virasoro algebra and two sets of supertranslations. The zero mode conserved quantities of Kerr black hole coincide with the entropy and the angular momentum.

Campus Plaine C.P. 231, B-1050 Bruxelles, Belgium.

^{*}Electronic address: laura.donnay-at-ulb.ac.be

[†]Electronic address: gaston-at-df.uba.ar

 $^{{}^{\}ddagger}\textsc{Electronic}$ address: hgonzale-at-ulb.ac.be

[§]Electronic address: miguel.pino.r-at-usach.cl

II. ASYMPTOTIC SYMMETRIES AT THE HORIZON

We are interested in studying the symmetries preserved by stationary non-extremal black hole metrics close to an event horizon, first in three dimensions and then we move to the four dimensional case.

A. Three-dimensional analysis

The near horizon geometry of three-dimensional black holes can be expressed using Gaussian null coordinates

$$ds^{2} = f dv^{2} + 2k dv d\rho + 2h dv d\phi + R^{2} d\phi^{2}, \qquad (1)$$

where $v \in \mathbb{R}$ represents the retarded time, $\rho \geq 0$ is the radial distance to the horizon and ϕ is the angular coordinate of period 2π . Functions f, k, h, and R are demanded to obey the following fall-off conditions close to $\rho = 0$:

$$f = -2\kappa\rho + \mathcal{O}(\rho^2),$$

$$k = 1 + \mathcal{O}(\rho^2),$$

$$h = \theta(\phi)\rho + \mathcal{O}(\rho^2),$$

$$R^2 = \gamma(\phi)^2 + \lambda(v,\phi)\rho + \mathcal{O}(\rho^2),$$

(2)

where $\mathcal{O}(\rho^2)$ stands for functions of v and ϕ that vanish at short ρ equally or faster than ρ^2 , consistent with the near horizon approximation. The metric components $g_{\rho\rho}$ and $g_{\rho\phi}$, which do not appear in (1), are supposed to be $\mathcal{O}(\rho^2)$. One can verify that this asymptotic behavior is preserved by the asymptotic diffeomorphisms we will consider, see (4) below. In particular, no order $\mathcal{O}(\rho)$ is generated in the component $g_{\rho\phi}$. Functions θ , λ and γ are arbitrary, the latter describing the shape of the horizon. Boundary conditions (2), apart from gathering the physically relevant solutions, yield finite and integrable charges. Other boundary conditions exist, which yield an additional super-translation current; however, the latter lead to nonintegrable charges. See also the interesting references [27, 28] for different criteria for selecting boundary conditions at the horizon. As we will see, our boundary conditions (2) break Poincaré symmetry.

The constant κ corresponds to the black hole surface gravity. Our boundary conditions assume that κ is a *fixed constant without variation*, i.e., they describe the spectrum of black holes at fixed Hawking temperature $T = \kappa/(2\pi)$. In the case of nonextremal BTZ black hole, this is given by

$$\kappa = \frac{r_+^2 - r_-^2}{\ell^2 r_+},\tag{3}$$

where r_+ and r_- are the outer and inner horizons.

The asymptotic Killing vectors preserving the above

asymptotic boundary conditions are

$$\chi^{v} = T(\phi) + \mathcal{O}(\rho^{3}),$$

$$\chi^{\rho} = \frac{\theta}{2\gamma^{2}}T'(\phi)\rho^{2} + \mathcal{O}(\rho^{3}),$$

$$\chi^{\phi} = Y(\phi) - \frac{1}{\gamma^{2}}T'(\phi)\rho + \frac{\lambda}{2\gamma^{4}}T'(\phi)\rho^{2} + \mathcal{O}(\rho^{3}),$$

(4)

where $T(\phi)$ and $Y(\phi)$ are arbitrary functions and the prime stands for the derivative with respect to ϕ . Under such transformation, the arbitrary functions $\gamma(\phi)$ and $\theta(\phi)$ transform as

$$\delta_{\chi}\theta = (\theta Y)' - 2\kappa T', \quad \delta_{\chi}\gamma = (\gamma Y)'. \tag{5}$$

The asymptotic Killing vectors depend on fields defined on the metric. Accordingly, the algebra spanned by Lie brackets does not close. However, by introducing a modified version of Lie brackets [18]

$$[\chi_1, \chi_2] = \mathcal{L}_{\chi_1} \chi_2 - \delta_{\chi_1} \chi_2 + \delta_{\chi_2} \chi_1, \tag{6}$$

one finds that the algebra of the asymptotic Killing vectors is given by

$$[\chi(T_1, Y_1), \chi(T_2, Y_2)] = \chi(T_{12}, Y_{12}), \tag{7}$$

where

$$T_{12} = Y_1 T'_2 - Y_2 T'_1,$$

$$Y_{12} = Y_1 Y'_2 - Y_2 Y'_1.$$
(8)

By defining Fourier modes, $T_n = \chi(e^{in\phi}, 0)$ and $Y_n = \chi(0, e^{in\phi})$ we find

$$i[Y_m, Y_n] = (m - n)Y_{m+n},$$

$$i[Y_m, T_n] = -nT_{m+n},$$

$$i[T_m, T_n] = 0.$$
(9)

This is a semidirect sum of the Witt algebra generated by Y_n with an Abelian current T_n . The set of generators Y_{-1} , Y_0 , Y_1 and T_0 form a $\mathfrak{sl}(2, \mathbb{R}) \oplus \mathbb{R}$ subalgebra.

The T_n generator is a supertranslation associated with the symmetry,

$$v \to v + T(\phi),\tag{10}$$

already observed by Hawking [10] in four dimensions. In the current analysis, we have extended this symmetry by adding a vector field Y_n which is responsible of generating superrotations

$$\phi \to \phi + Y(\phi), \tag{11}$$

on the circle of the horizon geometry.

Transformations (4) have associated conserved charges at the horizon $\rho = 0$. When considering threedimensional Einstein gravity, these can be calculated in the covariant approach [29], yielding the charges

$$Q(\chi) = \frac{1}{16\pi G} \int_0^{2\pi} d\phi \left[2\kappa T(\phi)\gamma(\phi) - Y(\phi)\theta(\phi)\gamma(\phi) \right].$$
(12)

Their Poisson bracket algebra can be computed by noticing that, canonically, these charges generate the transformations (5), i.e., $\{Q(\chi_1), Q(\chi_2)\} = \delta_{\chi_2} Q(\chi_1)$. In Fourier modes, $\mathcal{T}_n = Q(T = e^{in\phi}, Y = 0)$ and $\mathcal{Y}_n = Q(T = 0, Y = e^{in\phi})$, the algebra spanned by \mathcal{T}_n and \mathcal{Y}_n is isomorphic to (9), with no central extensions.

It is worthwhile noticing that by defining the generator

$$\mathcal{P}_n = \sum_{k \in \mathbb{Z}} \mathcal{T}_k \mathcal{T}_{n-k} \tag{13}$$

the algebra spanned by \mathcal{P}_n and \mathcal{Y}_n is \mathfrak{bms}_3 [16]

$$i[\mathcal{Y}_m, \mathcal{Y}_n] = (m-n)\mathcal{Y}_{m+n},$$

$$i[\mathcal{Y}_m, \mathcal{P}_n] = (m-n)\mathcal{P}_{m+n},$$

$$i[\mathcal{P}_m, \mathcal{P}_n] = 0.$$
(14)

Therefore, although our asymptotic symmetries do not contain a Poincaré subgroup, the full BMS symmetry is recovered by means of the above Sugawara construction [30].

Exact solution

Three-dimensional Einstein gravity in the presence of a negative cosmological term allows us to find an exact solution satisfying the above asymptotic boundary conditions, including BTZ black hole as a particular case. Its line element is (1), where the functions read

$$f = -2\kappa\rho + \rho^{2} \left(\frac{\theta(\phi)^{2}}{4\gamma(\phi)^{2}} - \frac{1}{\ell^{2}}\right),$$

$$k = 1,$$

$$h = \theta(\phi)\rho + \rho^{2}\frac{\theta(\phi)}{4\gamma(\phi)^{2}}\lambda(\phi),$$

$$R = \gamma(\phi) + \rho\frac{\lambda(\phi)}{2\gamma(\phi)},$$

(15)

and where λ is defined by

$$\kappa\lambda(\phi) = \theta'(\phi) - \frac{1}{2}\theta(\phi)^2 + \frac{2}{\ell^2}\gamma(\phi)^2 - \theta(\phi)\frac{\gamma'(\phi)}{\gamma(\phi)}.$$
 (16)

 $\theta(\phi)$ and $\gamma(\phi)$ are arbitrary functions, and ℓ stands for the AdS radius. The BTZ black hole is obtained by making the choice $\theta(\phi) = 2r_-/\ell$ and $\gamma(\phi) = r_+$, while choosing κ as (3). In [31], a solution similar to (15) was presented, although with a different boundary condition on the function R^2 .

It is interesting to study the special case $\kappa = 0$ and $\theta = 2\gamma/\ell$. For these values, the metric acquires the form

$$ds^{2} = 2dvd\rho + \frac{4}{\ell}\rho\gamma(\phi)dvd\phi + \gamma(\phi)^{2}d\phi^{2}, \qquad (17)$$

which has been found recently in the context of near horizon geometries of three-dimensional extremal black holes [32]. Note that the remaining symmetry algebra is just one copy of Virasoro.

When taking the flat limit $\ell \to \infty$, solution (15) also solves Einstein equations without cosmological constant. After choosing $\kappa = -J^2/2r_H^3$, its zero mode solution, i.e., $\theta = J/r_H$ and $\gamma = r_H$, corresponds to a flat cosmology with horizon radius r_H [33].

The charges associated with solution (15) are given by (12). Evaluating for the case of the BTZ black hole, they read

$$\mathcal{T}_n = \frac{\kappa r_+}{4G} \delta_{n,0}, \quad \mathcal{Y}_n = -\frac{r_+ r_-}{4G\ell} \delta_{n,0}. \tag{18}$$

Hence, the charge associated with time translations $T_0 = \partial_v$ is the product of the black hole entropy $S = \pi r_+/(2G)$ and its temperature $T = \kappa/(2\pi)$. This means that the particular charge \mathcal{T}_0 , when varying the configuration space by fixing the temperature, corresponds to the entropy of the black hole. On the other hand, the charge associated with rotations along $Y_0 = \partial_{\phi}$ coincides exactly with the angular momentum.

B. Four-dimensional analysis

It is possible to extend the analysis of the first section to four dimensions. A suitable generalization of (1) is given by

$$ds^2 = f dv^2 + 2k dv d\rho + 2g_{vA} dv dx^A + g_{AB} dx^A dx^B,$$
(19)

where coordinates x^A parameterize the induced surface at the horizon. The fall-off conditions on the fields as $\rho \to 0$ are

$$f = -2\kappa\rho + \mathcal{O}(\rho^2),$$

$$k = 1 + \mathcal{O}(\rho^2),$$

$$g_{vA} = \rho\theta_A + \mathcal{O}(\rho^2),$$

$$g_{AB} = \Omega\gamma_{AB} + \rho\lambda_{AB} + \mathcal{O}(\rho^2),$$

(20)

while components $g_{\rho A}$ and $g_{\rho \rho}$ decay as $\mathcal{O}(\rho^2)$ close to the horizon. Here, θ_A and Ω are functions of the coordinates x^A , $\lambda^{AB} = \lambda^{AB}(v, x^A)$ and γ_{AB} is chosen to be the metric of the two-sphere. It is convenient to use stereographic coordinates $x^A = (\zeta, \overline{\zeta})$ on γ_{AB} , in such a way that

$$\gamma_{AB}dx^A dx^B = \frac{4}{(1+\zeta\bar{\zeta})^2}d\zeta d\bar{\zeta}.$$
 (21)

The set of asymptotic conditions is preserved by the following vector fields :

$$\chi^{v} = T(\zeta, \bar{\zeta}) + \mathcal{O}(\rho^{3}),$$

$$\chi^{\rho} = \frac{\rho^{2}}{2\Omega} \theta_{A} \partial^{A} T + \mathcal{O}(\rho^{3}),$$

$$\chi^{A} = Y^{A} - \frac{\rho}{\Omega} \partial^{A} T + \frac{\rho^{2}}{2\Omega^{2}} \lambda^{AB} \partial_{B} T + \mathcal{O}(\rho^{3}),$$

(22)

where we have used γ^{AB} to raise indices and Y^A is a function of x^A only, i.e., $Y^{\zeta} = Y(\zeta)$ and $Y^{\bar{\zeta}} = \bar{Y}(\bar{\zeta})$. Under these transformations, the fields transform as

$$\delta_{\chi}\theta_A = Y^B \partial_B \theta_A + \partial_A Y^B \theta_B - 2\kappa \partial_A T, \delta_{\chi}\Omega = \nabla_B (Y^B \Omega),$$
(23)

 ∇ standing for the covariant derivative on γ_{AB} .

Under modified Lie brackets (6), transformations (22) satisfy

$$[\chi(T_1, Y_1^A), \chi(T_2, Y_2^A)] = \chi(T_{12}, Y_{12}^A), \qquad (24)$$

where

$$T_{12} = Y_1^A \partial_A T_2 - Y_2^A \partial_A T_1, Y_{12}^A = Y_1^B \partial_B Y_2^A - Y_2^B \partial_B Y_1^A.$$
(25)

Notice that the transformations generated by Y^A , in general, are not globally well defined on the two-sphere. The only invertible transformations are those spanning the global conformal group, which is isomorphic to the proper, orthochronous Lorentz group. However, if we focus only on the local properties, all functions are allowed. This was first proposed in [17, 18] in the context of asymptotically flat spacetimes.

By expanding in Laurent modes

$$T_{(n,m)} = \chi(\zeta^{n}\bar{\zeta}^{m}, 0, 0),$$

$$Y_{n} = \chi(0, -\zeta^{n+1}, 0),$$

$$\bar{Y}_{n} = \chi(0, 0, -\bar{\zeta}^{n+1}),$$
(26)

the nonvanishing commutation relations read

$$[Y_{n}, Y_{m}] = (n - m)Y_{n+m},$$

$$[\bar{Y}_{n}, \bar{Y}_{m}] = (n - m)\bar{Y}_{n+m},$$

$$[Y_{k}, T_{(n,m)}] = -nT_{(n+k,m)},$$

$$[\bar{Y}_{k}, T_{(n,m)}] = -mT_{(n,m+k)}.$$
(27)

The exact isometry algebra corresponds to $\mathfrak{sl}(2,\mathbb{C}) \oplus \mathbb{R}$ whose elements correspond to the globally well-defined transformations on the sphere plus $T_{(0,0)}$.

Conserved charges at the horizon turn out to be given by

$$Q(T, Y^A) = \frac{1}{16\pi G} \int d\zeta d\bar{\zeta} \sqrt{\gamma} \ \Omega \left[2\kappa T - Y^A \theta_A \right].$$
(28)

They close under Poisson bracket

$$\{Q(T_1, Y_1^A), Q(T_2, Y_2^A)\} = Q(T_{12}, Y_{12}^A).$$
(29)

By defining $\mathcal{T}_{(m,n)} = Q(\zeta^n \bar{\zeta}^m, 0, 0), \ \mathcal{Y}_n = Q(0, -\zeta^{n+1}, 0)$ and $\bar{\mathcal{Y}}_n = Q(0, 0, -\bar{\zeta}^{n+1})$, we find that these quantities satisfy the same algebra (27).

We can perform the Sugawara construction as we did in the previous section. Defining

$$\mathcal{P}_{(n,l)} = \sum_{m \in \mathbb{Z}} \sum_{t \in \mathbb{Z}} \mathcal{T}_{(m,t)} \mathcal{T}_{(n-m,l-t)}$$
(30)

and using (27), one finds

$$[\mathcal{P}_{(n,l)}, \mathcal{Y}_m] = (n-m)\mathcal{P}_{(n+m,l)}$$

$$[\mathcal{P}_{(n,l)}, \bar{\mathcal{Y}}_m] = (l-m)\mathcal{P}_{(n,l+m)}.$$
(31)

Although this is reminiscent of \mathfrak{bms}_4 , notice that this is not exactly the same algebra as that found in [17, 18].

Finally, let us note that Kerr black hole fits in our boundary conditions (20). An explicit construction of this solution in term of Gaussian normal coordinates can be found in [34]. One can verify that

$$\mathcal{T}_{(0,0)} = \frac{\kappa}{2\pi} \frac{\mathcal{A}}{4G}, \quad \mathcal{Y}_0 = \frac{iaM}{2}, \quad \bar{\mathcal{Y}}_0 = -\frac{iaM}{2}, \quad (32)$$

where \mathcal{A} is the area of the horizon, while M and a are the usual parameters of the Kerr solution. That is, the zero mode of the supertranslation is the product of the black hole entropy with its temperature. Since our boundary conditions are defined by fixing κ , we can associate this charge with Wald entropy. On the other hand, the charge $Q(0, \partial_{\phi}) = -i(\mathcal{Y}_0 - \bar{\mathcal{Y}}_0) = aM$ is the angular momentum. In the case where m and n are different from zero, \mathcal{Y}_n ,

 $\bar{\mathcal{Y}}_n$ and $\mathcal{T}_{(m,n)}$ with $m \neq n$ vanish. In contrast, charges $\mathcal{T}_{(m,m)}$ with $m \neq 0$ diverge. This phenomenon was first noticed in [19] and has been explained in reference [20]. Let us explain the origin of this divergence for the case of Schwarzschild black hole. In this case, the supertranslation charge reads

$$\mathcal{T}_{(m,n)} = \frac{\kappa r_+^2}{4G} \delta_{m,n} I(m), \qquad (33)$$

where $I(m) = \int_0^{\pi} d\theta \sin(\theta) \cot^{2m}(\theta/2)$ is divergent for $m \neq 0$, with the divergence comes from the poles of the sphere. If instead of Laurent modes, the supertranslation $T(\zeta, \overline{\zeta})$ is expanded in spherical harmonics, the charges can be seen to vanish.

III. DISCUSSION

We have shown that the near horizon geometry of nonextremal black holes exhibits an infinite dimensional extension of supertranslation algebra, which in particular contains superrotations. This phenomenon is similar to what happens in the asymptotically flat spacetimes at null infinity, although the algebra obtained differs from the standard extended BMS. We have explicitly worked out the cases of three-dimensional and four-dimensional stationary black holes, for which the zero modes of the charges associated to the infinite-dimensional symmetries were shown to exactly reproduce the entropy and the angular momentum of the solutions.

In the three-dimensional case, we have presented a family of explicit solutions that obey the proposed boundary conditions at the horizon and, therefore, realize the infinite-dimensional symmetry generated by the semidirect sum of Virasoro algebra and supertranslations. Although this family of solutions represent locally AdS_3 spacetimes, they do not satisfy the standard Brown-Henneaux asymptotic conditions at $\rho \to \infty$, as we are imposing boundary conditions at the horizon $\rho \to 0$. In [35], a set of asymptotically AdS₃ boundary conditions were found whose associated charges yield a centrally extended version of algebra (9). It would be interesting to study the relation between such boundary conditions and (2); in particular, to clarify the precise connection between the family of solutions (15) and those presented in [35]. The latter also includes the BTZ black hole as a particular example; however, in contrast to (2), which fixes the black hole surface gravity κ , the boundary conditions considered in [35] are defined by fixing the value of $\Delta = M\ell + J$.

Another question is whether it is possible to modify our boundary conditions in such a way of getting nonvanishing central extensions. In this regard, it is worthwhile mentioning that the boundary conditions we have considered allow for exponentially decaying modes $e^{-\kappa v}X(\phi)$ which yield an extra infinite-dimensional symmetry also associated to an extension of supertranslations. On the other hand, an important point to address is the study of the extremal limit, for which the boundary conditions at the horizon need to be reconsidered since the leading term in g_{vv} vanishes. Finally, it would be worthwhile in-

- A. Strominger, "Black hole entropy from near horizon microstates," *JHEP* 02 (1998) 009, arXiv:hep-th/9712251.
- [2] J. D. Brown and M. Henneaux, "Central Charges in the Canonical Realization of Asymptotic Symmetries : An Example from Three-Dimensional Gravity," *Commun.Math.Phys.* **104** (1986) 207–226.
- [3] D. Anninos, W. Li, M. Padi, W. Song and A. Strominger, "Warped AdS(3) Black Holes," JHEP 03 (2009) 130, arXiv:hep-th/0807.3040.
- [4] G. Compère and S. Detournay, "Semi-classical central charge in topologically massive gravity," *Class. Quant. Grav.* 26 (2009) 012001, arXiv:hep-th/0808.1911.
- M. Henneaux, C. Martínez and R. Troncoso, "Asymptotically warped anti-de Sitter spacetimes in topologically massive gravity," *Phys. Rev.* D84 (2011) 124016, arXiv:hep-th/1108.2841.
- S. Detournay, T. Hartman and D. M. Hofman, "Warped Conformal Field Theory," *Phys. Rev.* D86 (2012) 124018, arXiv:hep-th/1210.0539.
- [7] L. Donnay and G. Giribet, "Holographic entropy of Warped-AdS₃ black holes," *JHEP* 06 (2015) 099, arXiv:hep-th/1504.05640.
- [8] M. Guica, T. Hartman, W. Song and A. Strominger, "The Kerr/CFT Correspondence," *Phys.Rev.* D80 (2009) 124008, arXiv:hep-th/0809.4266.

vestigating whether this infinite dimension symmetry can have applications to memory effects in black hole physics.

5

To conclude, let us mention that the idea of investigating the symmetries of the horizon has been considered for a long time by different authors; see for instance [36]. Infinite-dimensional symmetries were discussed in a similar context in [37–39]. It would be interesting to study the connection between those works and ours.

The authors thank Glenn Barnich, Geoffrey Compère and Cédric Troessaert for useful discussions. L.D. is a FRIA research fellow of the FNRS Belgium. The work of G.G. has been supported by CONICET. The work of H.G. is supported in part by the Fund for Scientific Research-FNRS (Belgium), by IISN-Belgium and by "Communauté française de Belgique - Actions de Recherche Concertées". The work of M.P. is funded by FONDECYT/Chile grants 7912010045 and 11130083.

(2015).

- [10] S. W. Hawking, "The Information Paradox for Black Holes," arXiv:hep-th/1509.01147.
- [11] H. Bondi, M. G. van der Burg and A. W. Metzner, "Gravitational waves in general relativity. 7. Waves from axi-symmetric isolated systems," *Proc. Roy. Soc. Lond.* A269 (1962) 21.
- [12] R. Sachs, "Gravitational waves in general relativity. 8. Waves in asymptotically flat space-times," *Proc. Roy. Soc. Lond.* A270 (1962) 103.
- [13] R. Sachs, "Asymptotic symmetries in gravitational theories," *Phys. Rev.* **128** (1962) 2851.
- [14] G. Arcioni and C. Dappiaggi, "Holography in asymptotically flat space-times and the BMS group," *Class. Quant. Grav.* 21 (2004) 5655, arXiv:0312186[hep-th].
- [15] G. Arcioni and C. Dappiaggi, "Exploring the holographic principle in asymptotically flat spacetimes via the BMS group," *Nucl. Phys.* B674 (2003) 553, arXiv:0306142[hep-th].
- [16] G. Barnich and G. Compère, "Classical central extension for asymptotic symmetries at null infinity in three spacetime dimensions," *Class. Quant. Grav.* 24 (2007), arXiv:0610130[gr-qc].
- [17] G. Barnich and C. Troessaert, "Symmetries of asymptotically flat 4 dimensional spacetimes at null infinity revisited," *Phys. Rev. Lett.* **105** (2010) 111103, arXiv:0909.2617 [gr-qc].
- [18] G. Barnich and C. Troessaert, "Aspects of the BMS/CFT correspondence," JHEP 1005 (2010) 062, arXiv:1001.1541 [hep-th].

 $\it JHEP~1112~(2011)~105$, arXiv:1106.0213 [hep-th].

- [20] G. Barnich and C. Troessaert, "Comments on holographic current algebras and asymptotically flat four dimensional spacetimes at null infinity," *JHEP* 1311 (2013) 003, arXiv:1309.0794 [hep-th].
- [21] G. Barnich, A. Gomberoff and H. A. Gonzalez, "The flat limit of three dimensional asymptotically anti-de Sitter spacetimes," *Phys. Rev.* D86 (2012) 024020, arXiv:1204.3288 [gr-qc].
- [22] G. Barnich, A. Gomberoff and H. A. Gonzalez, "Three-dimensional Bondi-Metzner-Sachs invariant two-dimensional field theories as the flat limit of Liouville theory," *Phys. Rev.* D87 (2013) 124032, arXiv:1210.0731 [hep-th].
- [23] G. Barnich, A. Gomberoff and H. A. Gonzalez, "Dual dynamics of three dimensional asymptotically flat Einstein gravity at null infinity," *JHEP* 05 (2013) 016, arXiv:1303.1075 [hep-th].
- [24] P.-H. Lambert,"Conformal symmetries of gravity from asymptotic methods : further developments," arXiv:1409.4693 [gr-qc].
- [25] T. Banks, "A Critique of pure string theory : Heterodox opinions of diverse dimensions," arXiv:hep-th/0306074.
- [26] M. Bañados, C. Teitelboim and J. Zanelli,"The Black hole in three-dimensional space-time," *Phys. Rev. Lett.* 69 (1992) 1849, arXiv:hep-th/9204099.
- [27] S. Carlip, "Entropy from conformal field theory at Killing horizons," Class. Quant. Grav. 16 (1999) 3327, arXiv:gr-qc/9906126.
- [28] A. J. M. Medved, D. Martin and M. Visser, "Dirty black holes : Space-time geometry and near horizon symmetries," *Class. Quant. Grav.* **21** (2004) 3111, arXiv:gr-qc/0402069.
- [29] G. Barnich and F. Brandt, "Covariant theory of asymptotic symmetries, conservation laws and central charges," *Nucl. Phys.* B633 (2002) 3–82,

arXiv:hep-th/0111246 [hep-th].

- [30] Notice that this relation between bms₃ algebra and the enveloping algebra of û(1) current algebra has been independently found in H. Afshar, S. Detournay, D. Grumiller and B. Oblak, "Near-Horizon Geometry and Warped Conformal Symmetry," arXiv:1512.08233 [hep-th]
- [31] C. Li and J. Lucietti, "Three-dimensional black holes and descendants," *Phys. Lett.* B738 (2014) 48-54, arXiv:hep-th/1312.2626.
- [32] G. Compère, P. Mao, A. Seraj and S. Sheikh-Jabbari, "Symplectic and Killing Symmetries of AdS₃ Gravity : Holographic vs Boundary Gravitons," arXiv:1511.06079 [hep-th].
- [33] L. Cornalba, M. S. Costa, "Time dependent orbifolds and string cosmology", *Fortsch. Phys.* 52 (2004) 145, arXiv:hep-th/0310099.
- [34] I. Booth, "Spacetime near isolated and dynamical trapping horizons", *Phys. Rev.* D87 (2013) 024008, arXiv:1207.6955 [gr-qc].
- [35] G. Compère, W. Song and A. Strominger, "New Boundary Conditions for AdS3", JHEP 05 (2013) 152, arXiv:1303.2662 [hep-th].
- [36] S. Carlip, "Black hole entropy from conformal field theory in any dimension," *Phys. Rev. Lett.* 82 (1999) 2828, arXiv:hep-th/9812013.
- [37] J. i. Koga, "Asymptotic symmetries on Killing horizons," *Phys. Rev.* D64 (2001) 124012, arXiv:gr-qc/0107096.
- [38] M. Hotta, "Holographic charge excitations on horizontal boundary," *Phys. Rev.* D66 (2002) 124021, arXiv:hep-th/0206222.
- [39] M. Hotta, K. Sasaki and T. Sasaki, "Diffeomorphism on horizon as an asymptotic isometry of Schwarzschild black hole," *Class. Quant. Grav.* 18 (2001) 1823, arXiv:gr-qc/0011043.