

# Safety factor calibration for a new model of shear strength of reinforced concrete building beams and slabs

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## ABSTRACT

When assessing existing structures, the availability of adequate safety factors, calibrated with the most accurate models, and for established target reliability indexes, is of critical importance in order to take the right decision regarding the maintenance/repair/strengthening interventions. In the case of shear resistance in reinforced concrete (RC) structures, when using the current design codes provisions for new constructions in assessment results that, in many cases, existing structures may be considered unsafe, implying large economic costs in strengthening or even dismantling. In this research, a proposal of safety factor relative to a recently developed model for shear strength, for elements with and without transversal reinforcement, based on a reliability-based calibration is presented. A formulation is proposed to determine the adequate strength factor for a selected target reliability index of the existing structure and desired remaining service life by means of a safety factor format, considering the load factors present in the Eurocodes. The calibration is carried out considering typical geometry and load ratios of building floors, as well as normal and high strength concrete. The derived safety factor is almost independent of the chosen remaining service life.

Keywords: safety factor; shear; reinforced concrete; assessment; reliability; building floors; beams, slabs

Bairan JM, Casas JR (2018), “Safety factor calibration for a new model of shear strength of reinforced concrete building beams and slabs”, *Engineering Structures*, 172, 293-303.  
[doi.org/10.1016/j.engstruct.2018.06.033](https://doi.org/10.1016/j.engstruct.2018.06.033)

## 28 1. INTRODUCTION

29 The design process of a new concrete structure, or assessment of an existing one, should verify  
30 a limit-state condition of the form:

$$31 R_d \geq S_d \quad (1)$$

32 Being  $R_d$  and  $S_d$  the design values of the resistance and action-effects, respectively. The semi-  
33 probabilistic approach is the most common methodology used in practical applications. In this  
34 case, the action design value is computed by means of partial factors for loads, as e.g. Eq. (2) for  
35 the case of persistent or transient load situations. Here,  $S_{G,ki}$  and  $S_{Q,kj}$  are the characteristic values  
36 of the permanent action “ $i$ ” and variable action “ $j$ ”,  $\gamma_{Gi}$  and  $\gamma_{Qj}$  are the partial safety factors for  
37 the permanent and variable actions. Variable load  $j=1$  is the leading one, while the accompanying  
38 loads ( $j>1$ ) are affected by a combination factor  $\Psi_j$ , which is less or equal to 1.0.

$$39 S_d = \sum_{i=1}^n \gamma_{Gi} S_{G,ki} + \gamma_{Q1} S_{Q,k1} + \sum_{j>1}^n \gamma_{Qj} \Psi_j S_{Q,kj} \quad (2)$$

40 The design value of the resistance may be computed by means of partial safety factors applied  
41 to materials characteristic values, usually concrete strength and steel yielding strength, as shown  
42 in Eq. (3), where  $f_{ck}$ ,  $f_{yk}$ ,  $\gamma_C$ ,  $\gamma_S$  are the characteristic compressive strength, yielding strength and  
43 partial safety factors of concrete and steel. Alternatively, the design resistance can be obtained  
44 by a strength reduction factor, as shown in Eq. (4). In this case,  $\gamma_R$  is a strength safety factor which  
45 is applied in a global form to the resistance model, this is equivalent to the inverse of the strength  
46 reduction factor ( $\phi$ ).

47 In general, partial load factors account for the possibilities of unfavourable deviation of the  
48 load from its representative value, uncertainties in modelling of the load and of its effects.  
49 Materials partial factors and strength reduction factor account for the possibility of unfavourable  
50 deviation of the material property from the specified value, resisting model uncertainty, the  
51 geometrical deviations not considered explicitly and, in some cases, the consequences of failure.

52 Equations (3) and (4) represent, respectively, the two currently most used approaches in which  
53 safety factors are defined depending on the materials or the resisting mechanism involved, e.g.  
54 shear and bending require different strength reduction factors.

$$55 R_d = R \left( \frac{f_{ck}}{\gamma_C}; \frac{f_{yk}}{\gamma_S} \right) \quad (3)$$

$$56 R_d = \frac{1}{\gamma_R} R(f_{ck}; f_{yk}) = \frac{1}{\gamma_R} R_k = \phi R_k \quad (4)$$

57 If the partial safety factors have been appropriately calibrated, the required level of safety is  
 58 deemed satisfied through the verification of Eq. (1). Strength reduction factors shall be used  
 59 together with the same set of load factors considered in their calibration, in order to approach the  
 60 target reliability. For example, in the 2002 version of ACI-318 [1], the load factors were modified  
 61 to adapt them to the ASCE/SEI-7 [2] general provisions for minimum design loads in order to  
 62 simplify the design process of structures with components of different materials, that required a  
 63 recalibration of the strength reduction factor for shear, see Table 1. However, the alternative set  
 64 of load and strength factors in Annex C of ACI-318 is allowed, if they are used together.

65 In ACI-318 the strength reduction factor also considers the brittle or ductile nature of the  
 66 failure mode. As in the former, the element is more sensitive to larger variation of concrete  
 67 strength in tension and compression and consequences of failure may be higher, hence a more  
 68 conservative value of the resistance, i.e. a lower fractile, is needed to achieve the needed  
 69 reliability.

70 Table 1: Load and strength safety factors in ACI-318 and Eurocodes

	ACI-318-02 [1]		Eurocodes [3, 4]
	Main body	Annex C (prior 2002)	
Dead load factor	1.2	1.4	1.35
Live load factor	1.6	1.7	1.5
Shear strength reduction factor ( $\phi = 1/\gamma_R$ )	0.75	0.85	-
Concrete strength partial safety factor ( $\gamma_C$ )	-	-	1.5
Steel strength partial safety factor ( $\gamma_S$ )	-	-	1.15

71 On the other hand, Eurocodes 2 [3] and 1 [4] provide a set of partial safety factors for steel  
 72 ( $\gamma_S$ ) and concrete ( $\gamma_C$ ) properties, together with a set of partial load factors. The code was  
 73 calibrated for a yearly target reliability index of  $\beta_1 = 4.7$ , which is equivalent to a nominal  
 74 probability of failure in 1 year of approximately  $10^{-6}$  [5].

75 When dealing with the assessment and/or strengthening of an existing building, a question  
 76 about the suitability of using the same partial safety factors of the design of new elements arises.  
 77 In general, there is less uncertainty in the geometrical and material parameters and an increment  
 78 of the safety level may require a much larger economic effort than to achieve the same increment  
 79 in a new design. Additionally, the required remaining service life may be shorter than in new  
 80 constructions.

81 Therefore, the definition of the target reliability level for assessing existing structures should  
82 be based on risk of failure and cost optimization; including repair interventions, losses due to  
83 malfunction, environmental and psychological effects. A framework for establishing the target  
84 reliability corresponding to a remaining service life is available in some codes, as ISO 13822 [6],  
85 ISO 2394 [7], and recommendations, such as fib [8]. Hence, economic optimization can be used  
86 to derive target reliability values. However, human safety levels based on individual and societal  
87 risk for ethical issues should also be considered in the process, as stated in Sýkora et al. [9],  
88 Tanner and Hingorani [10], Steenbergen et al. [11]. As concluded in Steenbergen et al. [11], the  
89 minimum levels related to human safety are often critical target reliabilities for existing structures.

90 After the target reliability index is defined, suitable and properly calibrated resistance models  
91 are needed, including the statistical definition of the model error. The particular case of assessing  
92 shear resistance in existing concrete elements has gained much attention recently, as the current  
93 design provisions have raised doubts regarding the safety of constructed facilities, implying that  
94 many structures are to be strengthened or dismantled. Furthermore, contrary to bending strength,  
95 whose resisting theory is well consolidated, there are currently several shear strength theories,  
96 based on different hypotheses and with different accuracy and complexity levels. In recent  
97 investigations, experimental tests have been conducted in existing structures or elements that were  
98 deemed unsafe according to current design provisions, e.g. Zwicky and Vögel [12], Bergström et  
99 al. [13]. In some cases, shear performance observed by experimentation was much better than  
100 the expected according to the provisions for new structures. The use of adequate non-linear  
101 computational models accounting for non-linear shear behavior have also shown similar results,  
102 Ferreira et al. [14, 15]. Hence, it can be expected certain cost reduction in strengthening of  
103 structures or even no need of posting or substitution, after an advanced assessment of the existing  
104 safety level.

105 However, adequate nonlinear models for shear assessment are not always available, or it is not  
106 possible to systematically build a computational model for a large number of different structures  
107 in a network and perform the probabilistic analyses. Therefore, simpler models that are adequate  
108 for hand or spreadsheet calculations are useful in these cases. In addition, for practical and fast  
109 assessment application in a semi-probabilistic format, the strength reduction factors should be  
110 calibrated.

111 The objective of the present study is to propose adequate reliability-based design/assessment  
112 equations with properly calibrated safety factors for reinforced concrete beams and slabs of  
113 buildings, failing in shear, for a various target reliability indexes. The current method is restricted  
114 to shear failure taking place in sections that have not yielded previously in bending or axial force.

115 The paper is organized in the following way. Section 2 presents a statistical analysis of selected  
116 existing models for shear resistance in concrete members to define the most accurate and  
117 statistically define the corresponding model error. By the use of this model and after the definition  
118 of the sample set, Section 3 carries out the calibration process to define the safety factor, and the  
119 analysis of the results and discussion is presented in Section 4. Finally, the main conclusions are  
120 drawn in Section 5.

## 121 2. SHEAR RESISTANCE MODEL

122 For an appropriate calibration of safety factors, the first step is to derive accurate design  
123 equations for the shear strength capacity of reinforced concrete beams, based on the available  
124 theoretical models, jointly with the statistical characterization of the random variable of the  
125 “model error”. This random variable represents the ratio of the actual response to the model  
126 prediction and is characterized by a statistical distribution, its mean value (or bias ratio) and  
127 standard deviation (or coefficient of variation, CoV).

128 In this paper, a recently mechanical-based formulation for shear-flexure strength of reinforced  
129 concrete beams, proposed in Mari et al. [16], is used. This model assumes a combination of the  
130 four classical shear resisting mechanisms; namely, capacity of the uncracked compression chord  
131 ( $V_c$ ), capacity of the diagonally cracked web ( $V_w$ ) and the contribution of the transverse ( $V_s$ ) and  
132 longitudinal reinforcements ( $V_l$ ). The model provides a set of mechanistic derived closed-form  
133 equations for each action, here summarized in Table 2.

### 134 2.1. DESCRIPTION

135 The main aspects of the model can be explained based on Fig. 1; here, the shear stress  
136 distributions in a reinforced concrete beam are analyzed for the free-body equilibrium of the  
137 segment of the beam between the cross-sections 1 and 2 (Fig. 1a), at the initiation of an inclined  
138 crack in the tensile side and its tip, respectively. As discussed in Marí et al. [16] and Bairán and  
139 Marí [17, 18], the distribution of shear stresses depends on the crack pattern and bond between  
140 concrete and reinforcement. Fig. 1b shows the shear stress distribution for an almost vertical  
141 crack and perfect bond between reinforcement and concrete, the stresses are almost constant in  
142 the tensile cracked portion and corresponds to the so-called *beam-action*. Although acceptable in  
143 wide range of load stages, these hypotheses do not hold up to failure and thus shear stress  
144 distribution varies.

145 In the ideal situation of zero bond of the longitudinal reinforcement, its tensile force is constant  
146 between the two sections and the stress distribution is as in Fig. 1c, with a variation of the lever  
147 arm. This leads to a pure *arch-action* in which shear stresses are resisted only in the compression

148 chord. Although completely loss of bond is not likely if ribbed reinforcement with adequate  
149 development length is used, bond deterioration takes place as shear damage propagates. Recently,  
150 Carmona and Ruiz [19] studied the role of bond deterioration on shear resistance on the basis of  
151 fracture mechanics and Yang [20] related the formation of the longitudinal crack at the level of  
152 tensile reinforcement with the on-set of shear failure. Therefore, it is plausible to accept that bond  
153 will develop imperfect during the evolution of shear resisting actions.

154 In the cracked portion of the beam, shear stresses can be resisted by aggregate interlock,  
155 residual tensile stresses and inclined compression stress field. However, after crack opening  
156 increases, it is considered that the residual tensile stresses concentrate in the portion close to the  
157 neutral axis, where crack width is still moderate, and in the uncracked compression chord; while  
158 in the region with larger crack width, mainly the inclined compression strut acts. In this situation,  
159 the distribution of shear stresses is depicted in Fig. 1d. The variation of tensile force is less than  
160 for perfect beam-action and a combination of normal and shear stresses exist in the uncracked  
161 compression chord. This is an intermediate situation between the perfect *beam-action* (Fig. 1b)  
162 and the perfect *arch-action* (Fig. 1c). The compression stresses in the shear cracked portion of  
163 the beam result from the longitudinal component of the inclined compression field.

164 The model was developed for elements that fail in shear before yielding of the longitudinal  
165 reinforcement, so longitudinal reinforcement is elastic and the normal stresses in the compression  
166 zone is considered to follow a linear distribution. The main hypothesis of the model is that, as  
167 shear cracking opens and evolves, the distribution of shear stresses in the critical region varies  
168 from one similar to Fig. 1b to that of Fig. 1d, making the magnitude of shear stresses in the  
169 compression head to increase. The details on the derivation of the model equations can be found  
170 in [16]; however, in the following, a global description of the process is presented.

171 Firstly, the shear contribution of the cracked web ( $v_w$ ) is estimated from the residual tensile  
172 strength according to the concrete's tensile fracture energy and the maximum crack width; which  
173 is computed from the tensile strain in the longitudinal bar and by approximating the crack spacing  
174 by the element's depth. The tensile force resulting from the integration of the previous stresses  
175 is taken orthogonal to the crack's inclination and its vertical component is the shear contribution  
176 of the web.

177 On the other hand, in the presence of transversal reinforcement, its contribution to shear  
178 strength is the summation of all tensile ties crossed by the inclined crack ( $v_s$ ). Also, if transversal  
179 reinforcement exists; the contribution of longitudinal reinforcement (dowel action) is taken into  
180 account ( $v_l$ ). In order to compute the previous components, the inclination of the shear crack is

181 needed. In the shear critical region, the crack inclination is estimated after Eq. (5). In this  
182 equation,  $x/d$  is the ratio of the neutral axis with linear stress distribution and the effective depth.

$$183 \quad \cot \theta = \frac{0.85}{1 - \frac{x}{d}} \quad (5)$$

184 The shear force that must be resisted by the compression zone is computed from equilibrium  
185 by subtracting the three previous components ( $V_w$ ,  $V_l$ ,  $V_s$ ) from the applied shear force, Eq. (6).

$$186 \quad V_c = V_{Ed} - V_w - V_l - V_s \quad (6)$$

187 To determine the shear capacity of the compression chord, the normal and shear forces are  
188 distributed according to an elastic hypothesis. In the presence of closed hoops as transversal  
189 reinforcement, the confining stresses in the compression chord is accounted for. Further, the  
190 tension and compression principal stresses can be computed along the compression chord.

191 Shear failure is assumed to occur when the most critical point in the compression chord reaches  
192 its maximum capacity defined by the failure surface proposed by Kupfer et al. [21], see Fig. 2;  
193 otherwise, the element resists the applied load. In Fig. 2, it is represented the elastic limit observed  
194 in [21], where the Elastic Modulus and Poisson coefficient of concrete starts to vary from the  
195 initial one. The volumetric expansion is the situation prior to failure where concrete lateral  
196 expansion starts. It can be observed that in the compression-tension region, the volumetric  
197 expansion and strength envelope practically coincide. Therefore, in the model, the linear  
198 distribution of compression stresses is considered in the compression chord. Moreover, the  
199 capacity of this resistance mechanism depends on both compression and tension strengths.

200 In order to find the maximum shear strength, an iteration is needed in which the applied load ( $V_{Ed}$ )  
201 is increased until a point in Kupfer's failure surface is found. This process is rather tedious for  
202 practical purposes, so a parametric study was carried out that showed that the solution to the  
203 compression head contribution could be approximated by a linear relationship (Fig. 3), resulting  
204 in Eq. (7).

205 The linearized model is summarized in Table 2, where all terms have been normalized by  $f_{ct}bd$ .  
206 Note that here, the tensile strength is the reference parameter, in contrast to other formulations  
207 that are based on compression strength. The additional symbols in the equations of Table 2 are  
208 defined in Eqs. (11) to (15).

209 The factor  $\zeta$  represents the size effect of the shear capacity of the compression chord, which  
210 was taken similar to the proposal of [22], which was based on experimental observation on beams  
211 without shear reinforcement, Eq. 11. The term " $a$ " is the shear span, given by Eq. (12). It should

212 be noticed that, in this model,  $a$  is computed on the basis of the maximum absolute bending  
 213 moment and shear forces in the region of the beam under consideration up to the point of zero  
 214 moment. Fig. 4 shows how to compute the shear span in the different regions of a beam.

215 For rectangular sections,  $x/d$  can be computed from Eq. (13), with  $\alpha_e$  being the ratio of elastic  
 216 modules of steel to concrete, Eq. (14).  $G_f$  is the fracture energy in Mode I of tension. In case it  
 217 cannot be measured experimentally, Eq. (15) was proposed in [16] as a modification of the  
 218 equation of Model Code [23] to account for the effect of the aggregate size ( $d_{max}$ ).

219 Table 2. Summary of simplified equations derived for the different shear contributing actions

Compression chord	$v_c = \frac{V_c}{f_{ct}bd} = \zeta \left[ (0.88 + 0.70v_s) \frac{x}{d} + 0.02 \right] \quad (7)$
Cracked concrete web	$v_w = \frac{V_w}{f_{ct}bd} = 167 \frac{f_{ct}}{E_c} \left( 1 + \frac{2E_c G_f}{f_{ct}^2 d} \right) \quad (8)$
Longitudinal reinforcement	$v_s > 0 \rightarrow v_l = \frac{V_l}{f_{ct}bd} = 0.25 \frac{x}{d} - 0.05 \quad (9a)$
	$v_s = 0 \rightarrow v_l = 0 \quad (9b)$
Transversal reinforcement	$v_s = \frac{V_s}{f_{ct}bd} = 0.85 \rho_w \frac{f_{yw}}{f_{ct}} \quad (10)$

220  $\zeta = 1.2 - 0.2a \geq 0.65 \quad (11)$

221  $a = \frac{|M_{max, shear span}|}{|V_{max, shear span}|} \quad (12)$

222  $\frac{x}{d} = \alpha_e \rho \left( -1 + \sqrt{1 + \frac{2}{\alpha_e \rho}} \right) \quad (13)$

223  $\alpha_e = \frac{E_s}{E_c} \quad (14)$

224  $G_f = 0.028 f_{cm}^{0.18} d_{max}^{0.32} \quad (15)$

225 This model accounts for the failure mode of tension failure produced by shear forces. Two  
 226 additional failure modes should be verified for the sake of completeness of the shear assessment.  
 227 First, the failure of the diagonal compression stresses in the cracked web, which can be computed  
 228 after Eq. (16) [3], by considering the inclination of the compression field from Eq. (5). Second,  
 229 the capacity of the longitudinal reinforcement to resist the tensile force produced by the bending  
 230 and axial force together with the increment produced by shear given in Eq. (17).

231  $V_{Rd,max} = \alpha_{cw} b_w z V_1 f_{cd} \frac{1}{\cot \theta + \tan \theta} \quad (16)$



$$\Delta F_t = (V_{Ed} - 0.5V_s) \cot \theta \quad (17)$$

233

## 234 2.2. MODEL ERROR

235 The model error was estimated by comparing the prediction against experimental databases  
 236 collected in [24], [25] and [26], for elements with and without transversal reinforcement, as  
 237 presented in [16]. The database included the reported average values of compression strength and  
 238 yielding strength of the reinforcements. The concrete tensile strength was estimated from  
 239 compression strength using [3], see Table 5. The model error was also compared against those  
 240 of Eurocode 2 [3], ACI-318 [1] and Model Code 2010 [23]. The error characteristics of these  
 241 models correspond well with those recently found in [27]. As can be seen in Table 3, the above  
 242 model shows better performance in terms of average and CoV of the model error for both  
 243 situations, which makes it a good option for an assessment model.

244 Table 3. Statistical characterization of the error of different shear resisting models

$V_{test}/V_{pred}$	892 beams without transversal reinforcement				239 beams with transversal reinforcement			
	EC-2	ACI 318-08	MC10 Lev II	Model. [16]	EC-2	ACI 318-08	MC10 Lev III	Model [16]
<b>Average</b>	1.07	1.28	1.20	1.04	1.72	1.25	1.21	1.02
<b>Standard Deviation</b>	0.226	0.346	0.223	0.179	0.638	0.262	0.225	0.169
<b>CoV</b>	0.211	0.271	0.186	0.173	0.371	0.210	0.186	0.166

245

## 246 3. SAFETY FACTOR CALIBRATION

247 The design equation (18) is selected, with a safety factor  $\gamma_R$ .  $V_{R,k}$  is the shear strength  
 248 computed according to Section 2, using the characteristic material properties for concrete tensile  
 249 strength, Eq. (19).

$$250 \frac{1}{\gamma_R} V_{R,k} \geq \sum_i \gamma_{G,i} V_{G,ki} + \gamma_{Q,1} V_{Q,k1} + \sum_{j>1} \gamma_{Q,j} \Psi_j V_{Q,kj} \quad (18)$$

$$251 V_{R,k} = (v_c + v_w + v_l + v_s) f_{ct,k} b d \quad (19)$$

252  $V_{G,ki}$  is the shear force produced by the characteristic value of the dead load  $i$ , and  $\gamma_{G,i}$  is the  
 253 partial safety factor of the dead load  $i$ .  $V_{Q,ki}$  is the shear force due to the characteristic value of  
 254 the leading service load and  $V_{Q,kj}$  is the shear force due to the accompanying load acting in  
 255 combination with the leading one.  $\gamma_{Q,j}$  is the partial safety factor for load  $j$  and  $\Psi_j$  the combination

256 factor for the accompanying load. In this study, the Eurocode partial factors for actions of Table  
 257 1 were used. The characteristic design loads and characteristic material properties were selected  
 258 according to Eurocode 1 and 2 [4, 3].

259 The next step is to specify the range of possible structures/elements where the obtained safety  
 260 factors will be of application.

### 261 3.1. BUILDING FLOOR DESIGN SET

262 In order to determine the geometric characteristic and applied loads, a reference design set of  
 263 typical floors was created, considering different values of beam length ( $l$ ) and distance between  
 264 adjacent beams ( $s$ ). The combination of values for geometry and material strength in the design  
 265 set are described in Table 4, producing 108 design cases. Here,  $h$  and  $b$  are the depth and width  
 266 of the rectangular beam (see Fig. 5).

267 Table 4. Range of variables in the design set

Variable	Values	N° cases
$l$ (m)	4, 8, 12	3
$s$ (m)	3, 6, 9	3
$l/h$ (-)	10, 15, 20	3
$b/h$ (-)	0.5	1
$f_{ck}$ (MPa)	25, 50, 70, 90	4
Total N° cases considered:		108

268 As described in Section 2.1, in this model, the size effect of  $V_c$  depends on the shear span ( $a$ ).  
 269 Without losing generality, all elements are considered as simply supported. In this case,  $a$  can be  
 270 computed as shown in Fig. 5; hence,  $a$  is uniformly distributed between 1 m and 3 m.

271 It should be noticed that the shear span ratio ( $a/d$ ) is known to affect the shear resistance  
 272 through both moment-shear interaction and size effect [22]. As shown in [16], if the shear failure  
 273 takes place without yielding of the longitudinal reinforcement, the most critical section in shear  
 274 results to be the one in the tip of the crack closest to the point of zero bending. Therefore, the  
 275 effect of accompanying bending moment interaction was conservatively accounted for by  
 276 assuming it as the cracking moment.

277 On the other hand, the number of tests with distributed loads is scant with respect to those with  
 278 point loads. However, it has been observed that the elements with distributed loads tend to have  
 279 higher resistance than the equivalent specimen with point loads, [28], [29], among others. The  
 280 effect of distributed loads in the current model was discussed in [30]. It was observed that the

281 critical shear crack tend to occur closer to the zero-moment section and, on the other, the  
282 maximum reaction can be estimated by adding the resultant of the distributed load from the tip of  
283 inclined crack to the support.

284 The resulting distribution of live to dead load ratio (L/D) is shown in Fig. 6. L/D in the set  
285 ranges between 0.29 and 0.80, with a mean value of 0.60. It should be noticed that the difference  
286 with respect to the range considered in Ellingwood et al [31] (0.25 to 1.5) is justified because  
287 Ellingwood et al considered the wider range of live loads in the Building Code (including stage  
288 floors), while here the calibration is made for office and residential use. When considering office  
289 loads in [31], the range of L/D ratio is consistent with the here used.

290 To avoid bending failure in the representative set of beams the longitudinal reinforcement was  
291 over-designed in bending by a factor of 1.5. The shear reinforcement ratio ( $\rho_w f_{yd}$ ) that would  
292 result from the application of current Eurocode provisions in this design set ranges between 0 and  
293 8.8 MPa, with an average value of 1.17 MPa. 90% of the specimens in the set would require  $\rho_w$   
294  $f_{yd} \leq 3$  MPa, and the lower 60% of the set will require  $\rho_w f_{yd} \leq 1$  MPa, which makes it consistent  
295 with the usual reinforcement ratio used in this kind of structures.

## 296 **3.2 CALIBRATION**

297 The shear resistance safety factor ( $\gamma_R$ ) in Eq. (18) is calibrated based on the selection of a  
298 uniform reliability index (the target value) for the design set; as applied by several authors, e.g.  
299 Melchers [32], Madsen et al. [33], Casas [34], Casas and Chambi [35], Trentin and Casas [36],  
300 among others. Accordingly, when using the design equation (18), it should yield almost uniform  
301 reliability indexes close to the target value ( $\beta^*$ ).

302 In general, the shear resistance for the trial value of  $\gamma_R$  is first computed assuming  $v_s=0$ ; if the  
303 resistance is bigger than the design shear force, then no shear reinforcement is needed. Otherwise,  
304 shear reinforcement is designed. Afterwards, the reliability index of each designed case is  
305 computed by means of FORM (*First-Order Reliability Method*) analysis, with the limit state  
306 function defined in Eq. (20). Here,  $V_R$  is the random variable representing the shear resistance  
307 computed as function of the random variables of Table 5, as shown in Eq. (21).

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313 Table 5. Basic random variables in the resistance term ( $V_R$ )

Variable	Description	Statistical model	$\mu$	CoV	Ref.
$\delta$	Model error	Log-normal	$\rho_w=0$ : 1.04 $\rho_w>0$ : 1.02	0.173 0.166	Table 3
$f_c$	Concrete compression strength	Log-normal	$f_{ck}+8\text{MPa}$	0.05 – 0.147	[3, 37]
$f_{ct}$	Concrete tensile strength	Log-normal	$f_{ctm} = 0.3f_{ck}^{\frac{2}{3}}$ for $f_{ck} \leq 50 \text{ MPa}$ $f_{ctm} = 2.12 \ln\left(1 + \frac{f_{cm}}{10}\right)$ for $f_{ck} > 50 \text{ MPa}$	0.182	[3, 37]
$f_y$	Reinforcement yielding stress	Log-normal	550 MPa	0.055	[37]
$\Delta b$	Geometrical error in section's width	Normal	$0.003b \leq 3\text{mm}$	$\frac{4 + 0.006b \leq 10\text{mm}}{\mu_b}$	[37]
$\Delta d$	Geometrical error in section's effective depth	Normal	10 mm	1	[37]

314 
$$G = V_R - V_E \quad (20)$$

315 
$$V_R = \delta \cdot V_{R,mod}(f_c, f_{ct}, f_y, b + \Delta b, d + \Delta d, A_s, A'_s) \quad (21)$$

316 A random variable ( $\delta$ ) is considered in Eq. (21) to take into account the model error.  
317 According to the recommendations of JCSS [37],  $\delta$  is set as Log-Normal; its parameters were  
318 selected according to the results of Table 3. The parameters of  $\delta$  are defined in Table 5 for  
319 elements without shear reinforcement ( $\rho_w=0$ ) and with shear reinforcement ( $\rho_w>0$ ).

320  $V_E$  is the shear force in the critical section, which is a function of the load random variables of  
321 Table 6. These variables may be considered as uncorrelated because they are due to independent  
322 actions (self-weight, permanent load, live-load, etc.). The nominal value for the self-weight load  
323 is calculated based on the dimensions of the elements and the density of reinforced concrete.

324 Following the recommendations in [37], the live load model is taken, as a Gamma distribution  
325 for the sustained load, with mean and standard deviation  $\mu_q$  and  $\sigma_q$ , respectively. Variations in  
326 time of the sustained load is further taken into account by assuming that the time between load  
327 changes is exponentially distributed. Therefore, the probability function for the maximum  
328 sustained load is given by Eq. (22).

329

330 Table 6. Basic random variables in the action term ( $V_E$ )

Variable	Description	Statistical model	$\mu$	CoV	$\lambda$	T	Ref.
$g_0$	Element weight	Lognormal	$24 \frac{kN}{m^3}$	0.04	-	-	[37]
$g_1$	Surface dead load	Lognormal	$0.45 \frac{kN}{m^2}$	0.04	-	-	[37]
$q$	Live load (kN/m <sup>2</sup> )	Eq. (22)	$0.5 \frac{kN}{m^2}$	1.342	$\frac{1}{5} year^{-1}$	Service life	[37]

331 
$$F_{q,max}(x) = \exp \left[ -\lambda T \left[ 1 - F_q(x) \right] \right] \quad (22)$$

332 Where  $F_q(x)$  is the probability function of the sustained load, T is the reference exposition time  
 333 and  $\lambda$  is the occurrence rate of sustained load changes. Thus,  $\lambda T$  is the mean of the number of  
 334 occupancy changes [37].

335 The parameters of the live load are defined in [36] depending on the user category. For this  
 336 study, the values corresponding to sustained loads in office buildings have been selected, as they  
 337 are representative of a large number of existing buildings.

338 Finally,  $\gamma_R$  is optimized through a least squares minimization of the average error between the  
 339 reliability index ( $\beta$ ) and the target reliability ( $\beta^*$ ), in the design set:

340 
$$e^2 = \frac{1}{n} \sum_{j=1}^n (\beta_j - \beta^*)^2 \quad (23)$$

341 The selection of the proper target reliability index ( $\beta^*$ ) for structural assessment of existing  
 342 structures is currently a subject of active research, Luechinguer and Fisher [38], Steenbergen et  
 343 al. [11], Sýkora et al. [9]. As mentioned before, economic optimization can be used to derive  
 344 target reliability values; however, human safety levels based on individual and societal risk should  
 345 also be considered. As concluded in Steenbergen et al. [11], the minimum levels related to human  
 346 safety are often critical target reliabilities for existing structures. Based on an analysis of the  
 347 consequences to persons in more than 100 buildings collapses presented by Tanner and Hingorani  
 348 [10], Steenbergen et al. [11], these authors recommended a yearly target value of 4.2 (reference  
 349 period  $T_{ref} = 1$  year) for existing buildings, with a collapsed area, larger than 500 m<sup>2</sup> and in the  
 350 consequence class CC2 according to EN 1990 [5].

351 Although the value of  $\beta_1^* = 4.7$ , for  $T_{ref} = 1$  year, is the one mostly accepted in new  
 352 constructions; here, a range of possible target reliability indexes have been considered based on  
 353 the recommendations of JCCS [37], depending on the cost of safety measures and consequences  
 354 of failure (see Table 7). In this way, the sensitivity of the results to this target value can be also  
 355 analysed. The reliability index for service life (T) different than 1 year can be computed by

356 considering the probability of T successive non-failure years, and a rate of load changes  $\lambda$ . The  
 357 reliability index is obtained as shown in Eq. (24).

358 Table 7. Recommended target yearly reliability indexes,  $\beta_I^*$  (adapted from JCCS [37])

Relative cost of safety measure	Consequences of failure		
	Minor	Moderate	Large
Large (A)	$\beta_I^* = 3.1$ ( $P_{f,1} \approx 10^{-3}$ )	$\beta_I^* = 3.3$ ( $P_{f,1} \approx 5 \cdot 10^{-4}$ )	$\beta_I^* = 3.7$ ( $P_{f,1} \approx 10^{-4}$ )
Normal (B)	$\beta_I^* = 3.7$ ( $P_{f,1} \approx 10^{-4}$ )	$\beta_I^* = 4.2$ ( $P_{f,1} \approx 10^{-5}$ )	$\beta_I^* = 4.4$ ( $P_{f,1} \approx 5 \cdot 10^{-6}$ )
Small (C)	$\beta_I^* = 4.2$ ( $P_{f,1} \approx 10^{-5}$ )	$\beta_I^* = 4.4$ ( $P_{f,1} \approx 5 \cdot 10^{-6}$ )	$\beta_I^* = 4.7$ ( $P_{f,1} \approx 10^{-6}$ )

359 
$$\Phi(\beta(T)) = \Phi(\beta_1)^{\lambda T} \quad (24)$$

360 Similarly, the service life (remaining) of an assessed existing structure, or that of the designed  
 361 strengthening may be different from that of a new construction. It may also be selected in terms  
 362 of the planned future assessments and maintenance. Therefore, in this study the safety factor will  
 363 be calibrated considering a range of different required service lives after the assessment. In this  
 364 sense, the resulting factor will be useful for optimizing the possible combination of interventions.

365

#### 366 4. RESULTS AND DISCUSSION

367 Figure 7 shows the least-square minimization for the case of one year exposition target  
 368 reliability index of  $\beta_I^*=4.2$ , corresponding to the recommendations of Steenbergen et al. [11] for  
 369 existing structures, and an expected remaining time in service of T=20 years. This is equivalent  
 370 to a target reliability of 3.46 during the whole exposition period. By varying the shear safety  
 371 factor used in design according to the resistance model of Section 2.1, the square of the difference  
 372 between the calculated reliability index and the target one is minimized for a value of  $\gamma_R=1.124$ .

373 Similarly, the optimization of  $\gamma_R$  is carried out for the series of  $\beta_I^*$  of 3.3, 3.7, 4.2, 4.4 and 4.7,  
 374 covering the range of recommended values for relative cost of safety measure for moderate and  
 375 large consequences of failure. In addition, service life (T) is varied in the series of 5, 10, 20 and  
 376 50 years, for a total of 20 combinations. The shape of the resulting least-square optimization  
 377 curves is similar to that in Fig. 7. Fig. 8 compares the target reliability index ( $\beta_I^*$ ) for the different  
 378 service life and the average reliability index ( $\beta_{I,average}$ ) in the design set after optimization of the

379 safety factor, for all the cases considered. It can be noticed that the correlation is good, with an  
380 average difference between the target and the average reliability index of 0.88%.

381 The optimized safety factors ( $\gamma_R$ ) for each combination of  $\beta_I^*$  and  $T$  are shown in solid lines in  
382 Fig. 9. It can be observed that the effect of varying the service life is minor. This can be explained  
383 after analysing the influence of  $T$  in both the load and required reliability index. As shown in Eq.  
384 (23), larger exposition time implies a larger magnitude of the observed load with a given  
385 probability of not been exceeded. On the other hand, the target reliability index for a period range  
386 larger than one year, given by Eq. (24), reduces with time. Hence, the two effects compensate.  
387 The optimized values of  $\gamma_R$  can be approximated by Eq. (25). This approximation is represented  
388 in Fig. 9 as dotted lines.

$$389 \quad \gamma_R = 0.237\beta_1^{1.09} \quad (25)$$

390 As can be observed, the range of values for the optimized safety factor is smaller than usually  
391 required for current shear resisting models and design codes. In particular, for target reliabilities  
392 of 4.4 and 4.7, comparable to new constructions, the shear safety factor varies between 1.17 and  
393 1.28 for a service life of 50 years.

394 On the other hand, in assessing existing structures, smaller target reliability indexes can be  
395 justified, on the range of 3.3 and 3.7, based on larger cost of safety measure, as seen in Table 7.  
396 In these cases,  $\gamma_R$  can even take values between 0.83 and 1.0. However, these values are to be  
397 applied to the strength computed with the characteristic values of the material properties.

398 Fig. 10 shows the evolution of the reliability index with several design parameters, computed  
399 for each element of the design, for the case case  $\beta_I^*=4.2$  and service life  $T=20$  years. The shear  
400 safety factor obtained from Eq. (25) is  $\gamma_R= 1.124$  and the target and average reliability indexes  
401 are shown in dashed red and green lines, respectively. The approximation of the average  
402 reliability to the target value is good, although some scatter is observed.

403 Fig. 10a shows the variation of the computed reliability as function of the live to dead load  
404 ratio ( $L/D$ ). Most cases are distributed between 4.4 and 4.1, with a mean value close to the target  
405 value. However, two points show larger values of reliability, between 4.4 and 4.5 for  $L/D$  equal  
406 to 0.3. The influence of  $L/D$  seems to stabilize after  $L/D=0.6$ .

407 On the other hand, Fig. 10b, shows the same distribution when the effective ratio of transverse  
408 reinforcement varies. Reliability indexes are bigger in the region of zero or small transverse  
409 reinforcement ratio. Moreover, the two peak values identified in Fig. 10a lie within this region.  
410 This is explained as the elements not requiring transverse reinforcement, may resist larger shear

411 force than the strictly demanded. For moderate and large shear reinforcement ratios, scatter of  
 412 the computed reliability tends to a stable value of 4.15, only 2% smaller than the target value.  
 413 The smallest observed index is 4.1, only 2.4% less than the target value.

414 Figs. 10c and 10d show the influence of the concrete strength and the effective depth. Besides  
 415 the cases explained above, the scatter is reasonably independent of the concrete class. As for the  
 416 effective depth, it seems to be a slight tendency to increase the reliability index for larger sections.  
 417 However, the latter is correlated with the smaller transverse shear ratio in these points, as can be  
 418 observed in Fig. 11b. Nevertheless, it should be highlighted that the model reliability index does  
 419 not decrease for large size specimens, at least up to 1.2 m depth.

420 Fig. 11 shows the CoV of the computed reliability index of all cases, as computed during the  
 421 calibration. It is evidenced that the scatter of the calibration increases for lower  $\beta_I$ , while it  
 422 reaches an almost uniform value between 0.01 and 0.02 for  $\beta_I > 4$ .

423 Alternatively, one may select a safety factor calibration that achieves a desired confidence  
 424 level of the minimum reliability. In this case, the value of  $\beta_I$  to be used in Eq. (26) may be  
 425 increased to a value larger than the target,  $\beta_{1,d} \geq \beta_1^*$ .  $\beta_{1,d}$  is defined so that it is guaranteed that  
 426 90% of the cases will show individual reliability indexes larger than a certain threshold of the  
 427 target reliability index:  $\beta_{1,individual} \geq c \beta_1^*$ . Here,  $c$  is the fraction of the minimum reliability  
 428 with respect to the target to be guaranteed. This is in agreement with Annex E of [7] if one  
 429 considers that the value that guarantees a safe value 90% of the time is in line with the engineering  
 430 judgement and tradition.

431  $\beta_{1,d}$  can be computed by multiplying the target reliability index ( $\beta_1^*$ ) by a modification factor  
 432 ( $f$ ), as in Eq. (26). The proposed value for factor  $f$  is given in Eq. (27).

$$433 \quad \beta_{1,d} = f \beta_1^* \quad (26)$$

$$434 \quad f = \frac{\beta_{1,d}}{\beta_1^*} = 0.67 + 0.77c - 0.08\beta_1^* \geq 1 \quad (27)$$

435 In order to demonstrate the use of this approach in practice, consider the case of  $\beta_I^* = 3.3$ , for  
 436 a service life of 20 years. As observed in Table 7, this is equivalent to a moderate consequence  
 437 of failure and large cost of safety measure. The safety factor for this mean reliability is,  $\gamma_R =$   
 438 0.862. The reliability indexes for the individuals of the design set assessed with this safety factor  
 439 are shown in Fig. 12a. The average reliability resulted as  $\beta_{1,mean} = 3.416$ , which is larger than the  
 440 target value. However, the smallest individual reliability index in the set is  $\beta_{1,min} = 3.050$ , which



441 is 7.6% smaller than the target. Moreover, 34% of the set shows a computed reliability smaller  
442 than the intended one

443 Consider that it is desired to guarantee, with a 90% confidence, that the minimum reliability  
444 is larger than 0.85 of the target value, then Eq. (27) is used to obtain the modification factor as:  
445  $f = 0.67 + 0.77 \times 0.85 - 0.08 \times 3.3 = 1.06$ . Therefore, the intended reliability index is  
446  $\beta_{1,d} = f \beta_1^* = 1.06 \times 3.3 = 3.50$ . Further, the optimized shear safety factor will be computed  
447 from Eq. 26, as:  $\gamma_R = 0.23 \times 3.50^{1.09} = 0.928$ .

448 The distribution of reliability indexes in the calibration with the latter safety factor ( $\gamma_R =$   
449  $0.928$ ) is shown in Fig. 12b. The mean computed reliability index in this case is 3.60 and the  
450 minimum value in the set is  $3.34 > \beta_1^* = 3.3$ . Hence, in this set there is no element with smaller  
451 reliability index than the target value ( $\beta_1^* = 3.3$ ).

452 In order to show the effect of the model in design and assessment, the required shear  
453 reinforcement ratio in the design set according to the calibrated method, for yearly target  
454 reliabilities 4.7, 4.2 and 3.7, are compared against the current Eurocode and ACI-318 provisions.  
455 Note that the comparison with the ACI-318 is not direct, as the load factors are different from the  
456 ones used here for calibration. Moreover, the quantiles of the specified concrete strength also  
457 differ, so the relationship  $f_c \approx 1.05 f_{ck}$  was used.

458 Figure 13 shows the distribution of reinforcement ratio. When considering the target reliability  
459 of new design ( $\beta_1^* = 4.7$ ), the calibrated method prescribes, in average, higher reinforcement ratios  
460 than the Eurocode and ACI-318. Although, the percentage of elements falling in the region of  
461 small reinforcement ratios ( $\rho_w f_{yd} = 0 - 0.25$  MPa) is similar to the Eurocode when considering  
462  $\beta_1^* = 4.7$ . However, in assessment, when lower reliability index can be justified, the percentage of  
463 elements with zero to small reinforcement ratio increases to almost 27% of the set, although it is  
464 still smaller than the share obtained for ACI-318 in this section. The average ratio for the three  
465 target reliabilities considered are 1.91 MPa, 1.36 MPa and 0.89 MPa, while the average ratios in  
466 the design set for the Eurocode and ACI-318 are 1.17 MPa and 1.29 MPa, respectively. In all  
467 cases, the maximum required reinforcement ratio was smaller than the needed in the Eurocode.

468 Further, the predicted strength for fixed reinforcement ratio and different target reliability  
469 index are compared to the code formulations in Table 8. The relative strength prediction increases  
470 as the target reliability is smaller. The percentage of elements predicted with larger strength than  
471 the code increases to 40% and to 80% in the case of Eurocode for  $\beta_1^*$  equal to 4.2 and 3.7,  
472 respectively and from 60% to 77% in the case of ACI.

473 Finally, it should be taken into account that shear failure is, in general, brittle. In many design  
 474 situations, when high ductility is required for correct performance, e.g. seismic situations, brittle  
 475 failure modes can be prevented by applying “capacity design” approaches or over-strength factors  
 476 in order to provide a larger safety margin to shear failure than bending. These approaches are  
 477 also applicable with the present formulation. However, an advantage of the formulation is  
 478 obtained from the fact that safety factors have been posed in terms of target reliability indexes.  
 479 Hence, it allows for a reliability-based design in which, for example, a higher target reliability  
 480 index can be attributed to shear failure than bending.

481 Although the model was derived from a mechanistic approach, the model error variable was  
 482 calibrated with laboratory experimental data; and this data could not account for all realistic load  
 483 conditions, such as those involving loads of long duration or repeated cyclic loading. However,  
 484 this is a limitation of all shear design models used in practice today and present in the current  
 485 design codes, as all them have been calibrated using laboratory experimental data as well. When  
 486 more experimental data become available for other load situations, such as long-term or cyclic  
 487 loads, the safety factor calibration may be updated accordingly.

488 Table 8. Representative values of the ratio of design shear strength of the calibrated model and  
 489 the design strength of Eurocode and ACI-318 for different target reliability

$V_{Rd,model} / V_{Rd,Code}$	$\beta^*_1=4.7$		$\beta^*_1=4.2$		$\beta^*_1=3.7$	
	EC-2	ACI-318	EC-2	ACI-318	EC-2	ACI-318
Maximum	1.23	3.50	1.65	3.58	2.01	3.66
Minimum	0.45	0.41	0.61	0.44	0.81	0.47
Average	0.75	1.00	0.97	1.15	1.26	1.38
CoV	0.26	0.46	0.25	0.40	0.22	0.37
% $V_{Rd,model} > V_{Rd,Code}$	13.0%	35.2%	39.8%	62.0%	81.4%	76.9%

490

## 491 5. CONCLUSIONS

492 A safety factor for the shear assessment of existing beams and slabs in existing buildings with  
 493 reinforced concrete structures was calibrated. This was carried out using the shear resistance  
 494 model published in [16], that is based on a multi-action principle and considers rational  
 495 quantification of four simultaneous shear resisting mechanisms. The model was found to give the  
 496 best approximation to a large database of shear tests, compared to modern design codes. In its

497 present form, the model was developed for shear failure before yielding of longitudinal  
498 reinforcement.

499 This study has looked into different target values of safety as well as several remaining service  
500 life of the building under assessment. A wide range of reinforced concrete elements, with  
501 geometry and load conditions typical of building constructions was considered in the calibration  
502 of optimal safety factors for shear assessment. The covered sample included elements with and  
503 without shear reinforcement; therefore, the calibration is also suitable for both beams and slabs  
504 with live to dead load ratio (L/D) up to 0.8. The calibration is also adequate for normal and higher  
505 strength concrete, up to 90 MPa.

506 The safety factor proposed should only be used for the failure mode related to tension in the  
507 web and the compression chord capacity. It was not calibrated for crushing of concrete in thin  
508 webs.

509 It was found that the effect of the remaining service life (T) on the value of the optimized  
510 safety factor for shear strength can be neglected, compared to the effect of yearly target reliability  
511 index.

512 An analytical expression (Eq. 25) is proposed to compute the optimal safety factor for the  
513 considered model based on the adopted target reliability. The equation provides a very good  
514 fitting of the average reliability of the design set.

515 Adopting, for example, a yearly target reliability of 4.2, , suggested in [11] as appropriate for  
516 the assessment of existing structures, the corresponding safety factor obtained for the shear  
517 resisting model is 1.13, both for elements with and without transversal reinforcement. Other  
518 values of the safety factor can be derived using Eq. (25), if different target reliabilities are decided.

519 The shear resistance safety factor values of Eq. (25) are those that minimize the quadratic error  
520 between the reliability index of the investigated set and the target reliability value. The scatter of  
521 the observed reliability index ranged between CoV 2% and 9%, being larger for the smaller target  
522 reliability indexes. Hence, a fraction of the set may show less individual reliability indexes than  
523 the target. Therefore, a modification factor of the target reliability was proposed in Eq. (27), in  
524 order to guarantee a minimum individual reliability index with a confidence of 90%. For  $\beta^*_1=4.2$ ,  
525 the application of this modification factor will modify the safety factor from 1.13 to 1.17 when  
526 considering the average reliability index or the guaranteed one.

527 The proposed shear safety factors have to be used jointly with the design equation as defined  
528 in Eq. (18) and the shear strength model as defined in Section 2. These safety factors are

529 applicable to cases similar to those in the range of the sample analysed, which comprises a wide  
530 range of RC elements used in buildings. However, the proposed calibration methodology is  
531 general and may be applied to other shear strength models and other building floor systems. This  
532 approach will allow for quick and a more accurate assessment of existing reinforced concrete  
533 buildings to shear, and therefore, for lower costs of repair and strengthening, resulting on a more  
534 efficient allocation of limited resources, based on explicit target reliability indexes.

535 As shown in the paper, the model uncertainty is a strongly influent variable on the results  
536 derived from a calibration process. Therefore, the safety factors should be always considered to  
537 be valid for the particular case of the model used to obtain the design values of the variables.  
538 When deriving the parameters of the random variable model error, it is also of crucial  
539 importance to use, from the available experimental database, only those tests that correspond to  
540 the failure modes of interest. Failing to do that will derive on unreliable values of the safety  
541 factors.

542 It should be noticed that, although the model is derived from a mechanistic approach, the  
543 model error variable was calibrated with laboratory experimental data; and this data could not  
544 account for realistic load conditions that involve loads of long duration or repeated cyclic loading.  
545 However, this is a limitation of all shear design models used in practice today and present in the  
546 current design codes, as all them have been calibrated using laboratory experimental data as well.

## 547 **ACKNOWLEDGEMENTS**

548 This research was carried out with the support of the Spanish Ministry of Economy and  
549 Competitiveness and the European Regional Development Funds (ERFD), through the research  
550 projects BIA2012-36848, BIA2013-47290-R and BIA2015-64672-C4-1-R.

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- 643

644

## 645 **FIGURE CAPTIONS**

646 Figure 1. Basis of the distribution of shear stresses in shear capacity model

647 Figure 2. Stress envelopes, adapted from Kupfer et al. [21]

648 Figure 3. Parametric analysis for solution of compression chord shear capacity and comparison  
649 against linearized model (Eq. 7, in dashed lines)

650 Figure 4. Example of calculation of shear spans in the regions of a general beam

651 Figure 5. Static scheme of the elements in the design set, definition of the shear span length ( $a$ )  
652 and cross-section dimensions

653 Figure 6. Distribution of live to dead load ratio (L/D) in design set

654 Figure 7. Square error minimization for target  $\beta_l^* = 4.2$  and service life  $T = 20$  years

655 Figure 8. Correlation between average  $\beta$  corresponding to optimized  $\gamma_R$  and target values  $\beta^*(T)$   
656 for different combinations of annual target values  $\beta_l^*$  and service life periods ( $T$ ) ranging from  
657 5 to 50 years

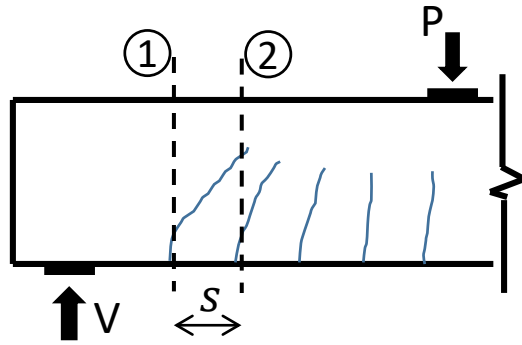
658 Figure 9. Safety factor for different target  $\beta_l^*$  and service life. Eq. (26) shown in dashed lines

659 Figure 10. Distribution of  $\beta_l$  for  $\gamma_{Rf} = 1.124$ , target  $\beta_l^* = 4.2$  and service life  $T = 20$  years with  
660 varying different design parameters

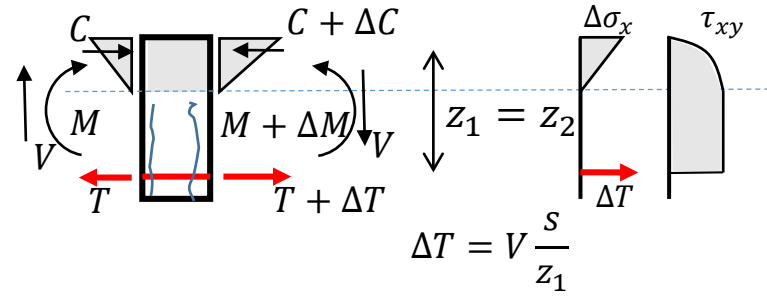
661 Figure 11. Variation of CoV of  $\beta_l$  as function of mean value in the design set

662 Figure 12. Distribution of  $\beta_l$  in the design set. a)  $\gamma_R = 0.862$ , for a mean target  $\beta_l^* = 3.3$ , b)  $\gamma_R =$   
663  $0.928$ , for a target  $\beta_{l,d} = 3.5$

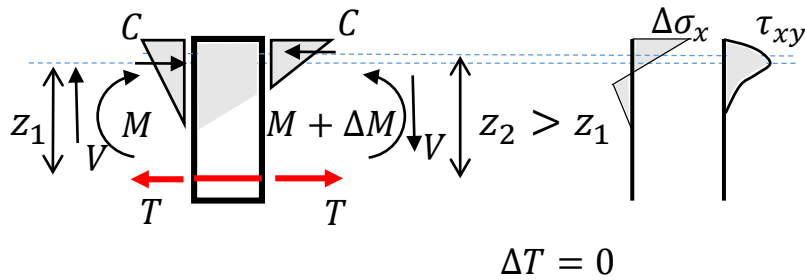
664 Fig. 13 Distribution of the shear reinforcement ratio designed for different  $\beta_l^*$ , Eurocode and ACI-  
665 318



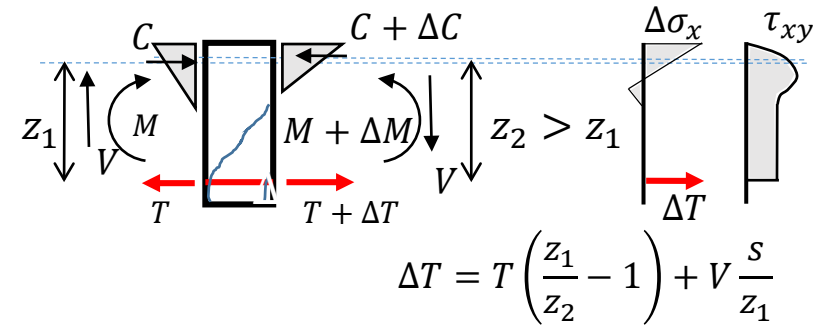
a) Free body cut limited by cross-sections 1 and 2



b) Free body equilibrium and stress distribution for perfect beam-action

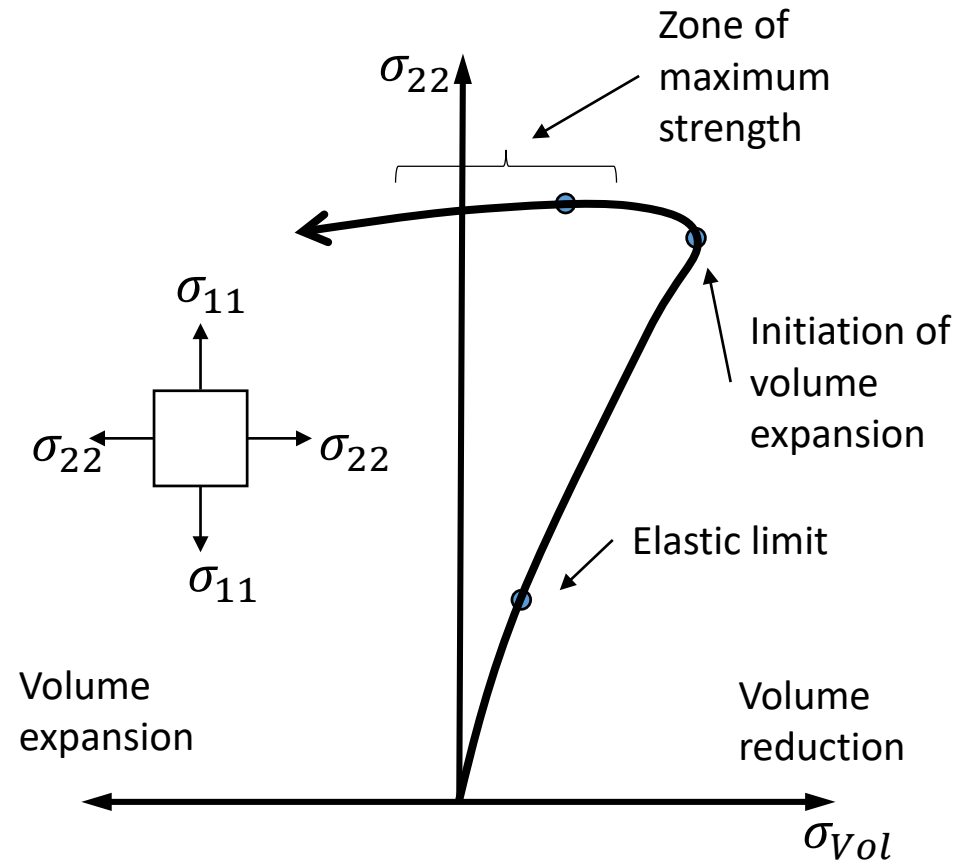
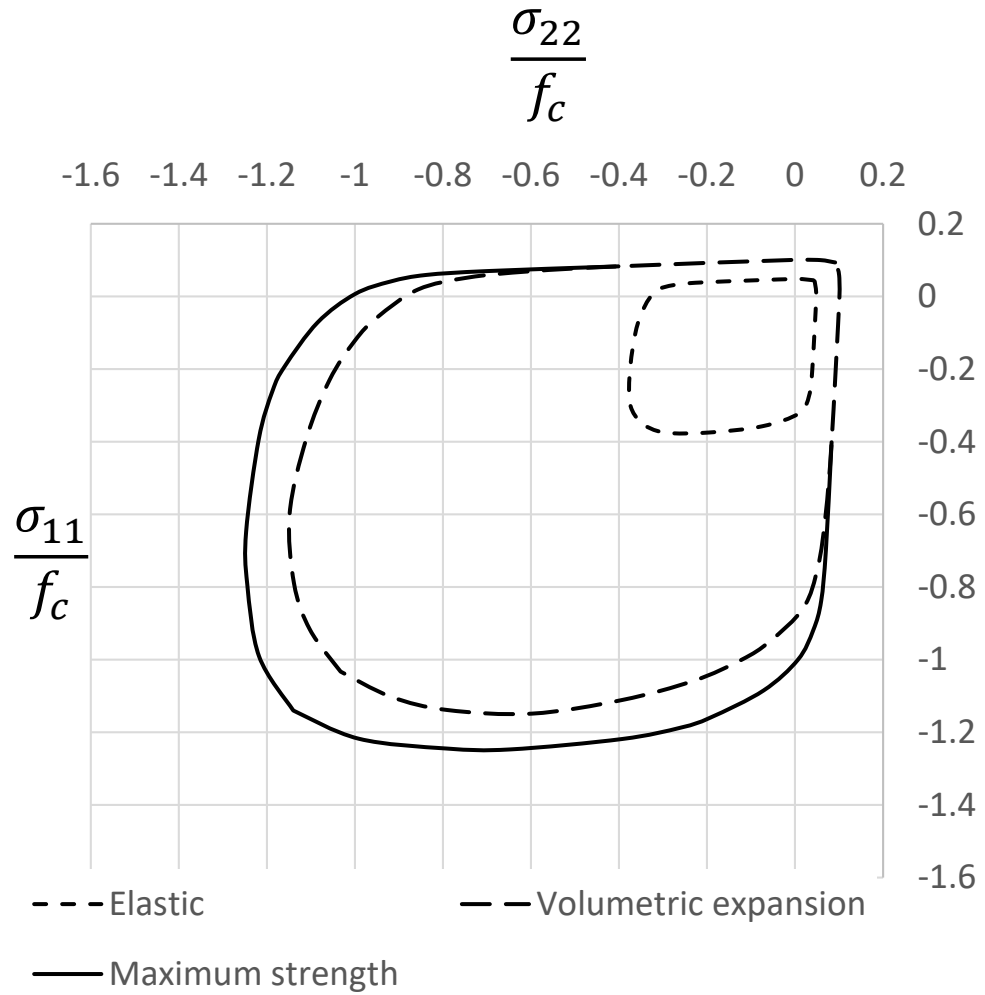


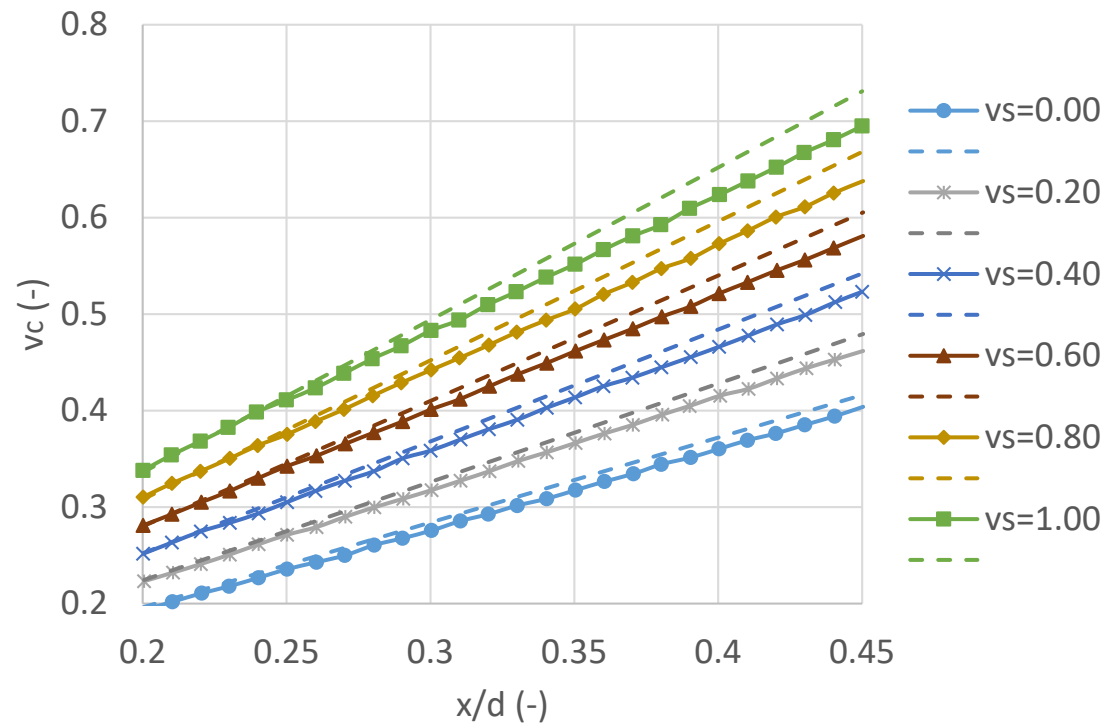
c) Free body equilibrium and stress distribution for perfect arch-action

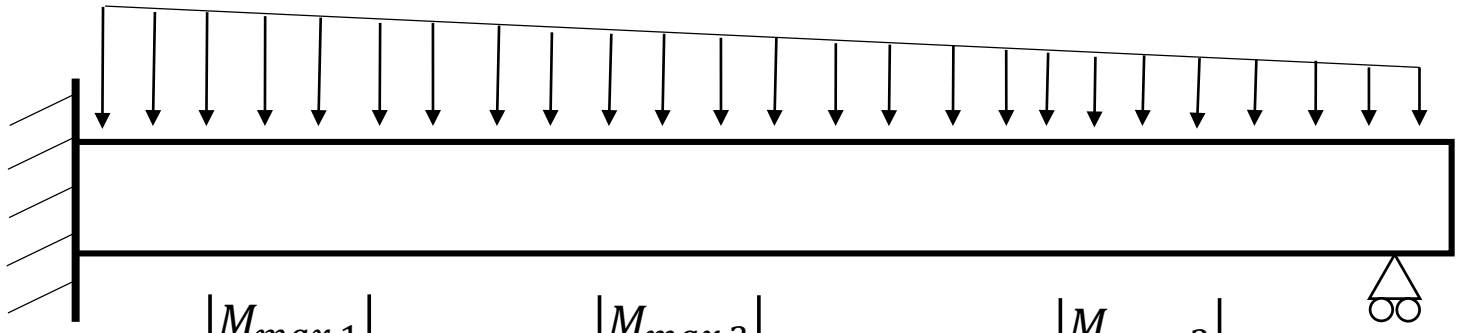


d) Free body equilibrium and stress distribution for combined beam-arch action





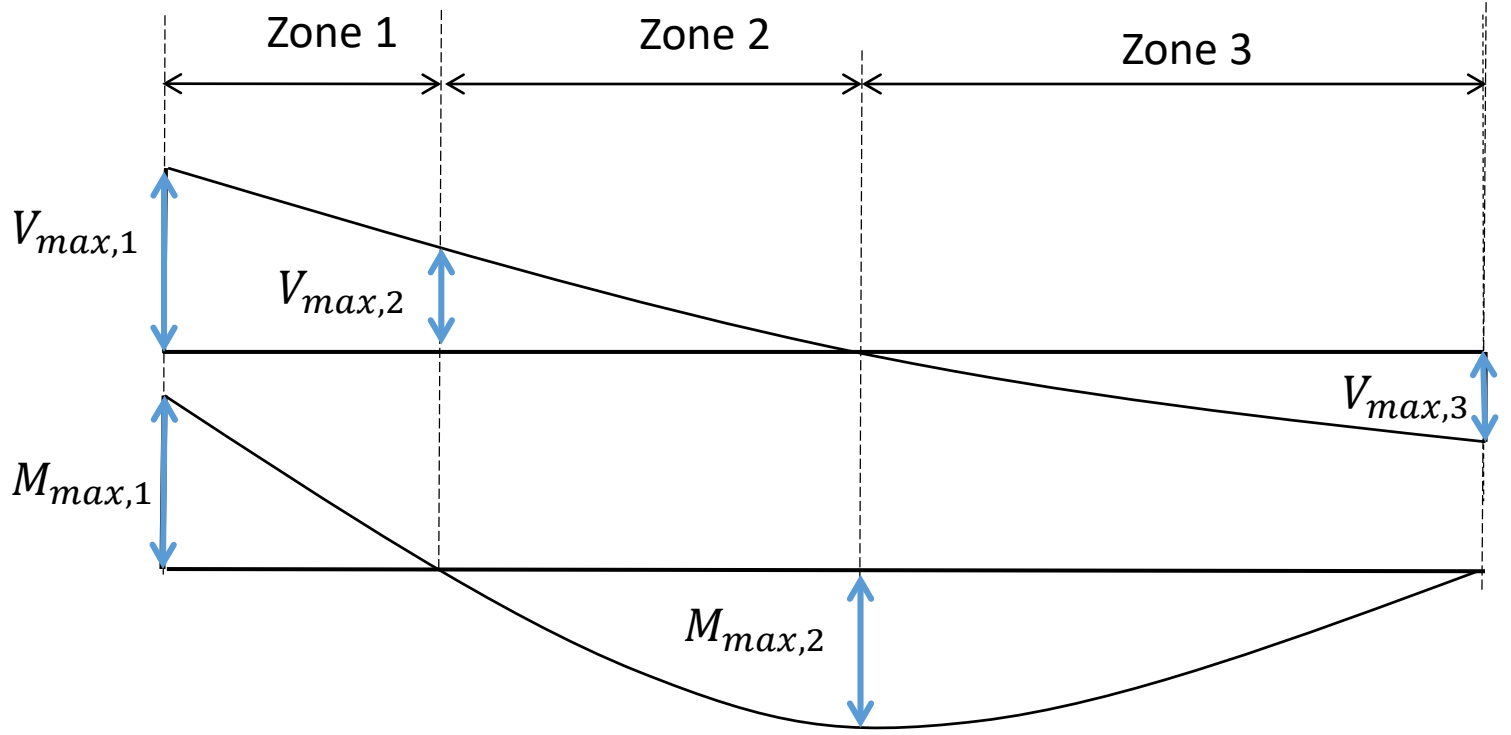


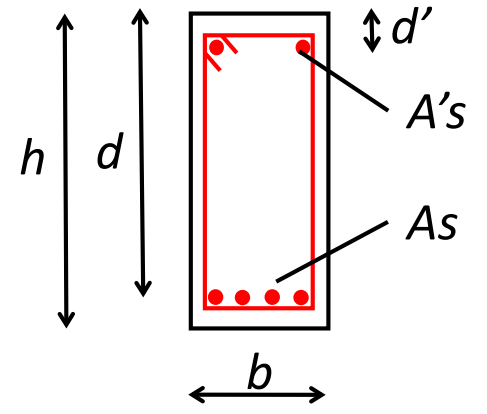
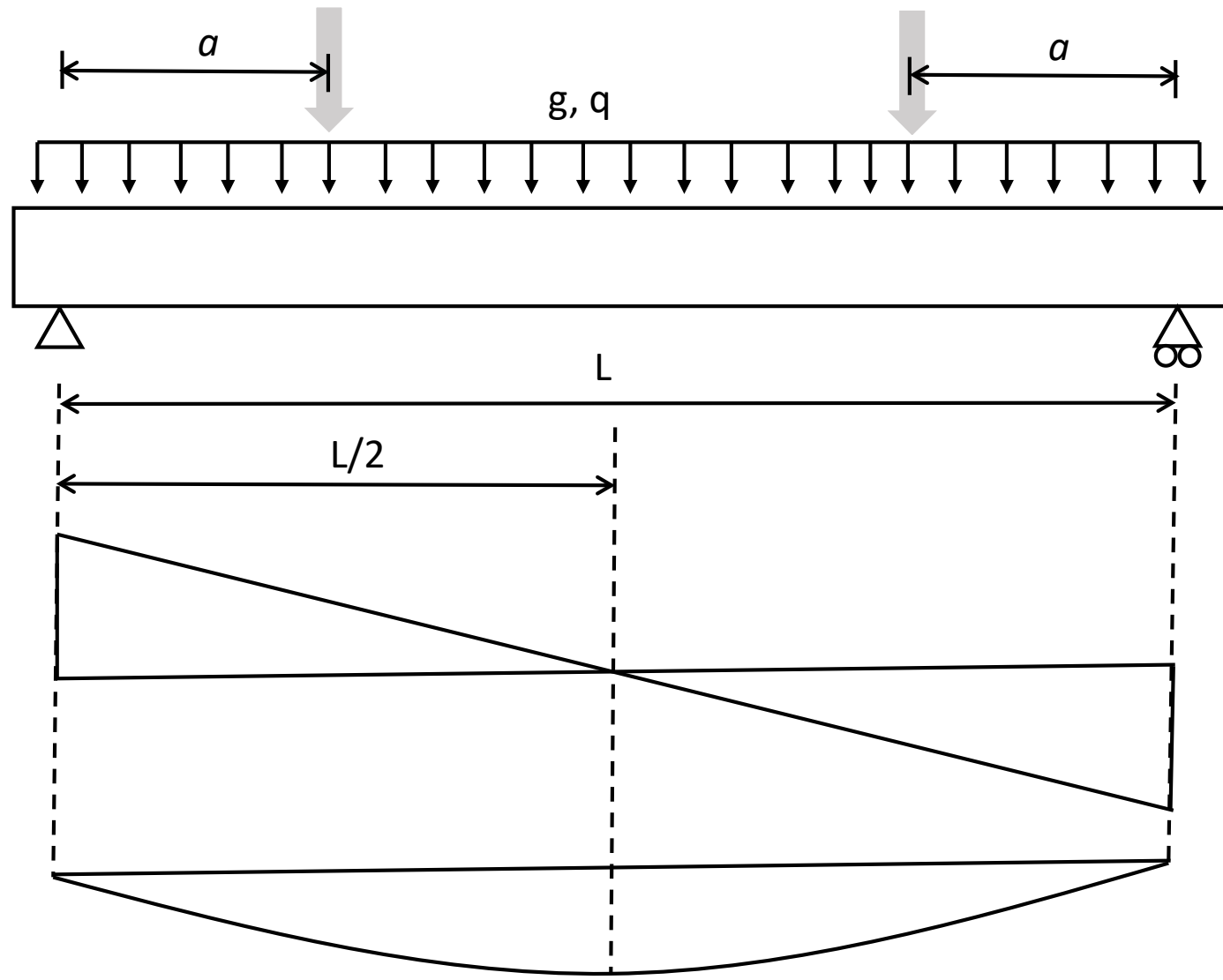


$$a_1 = \frac{|M_{max,1}|}{|V_{max,1}|}$$

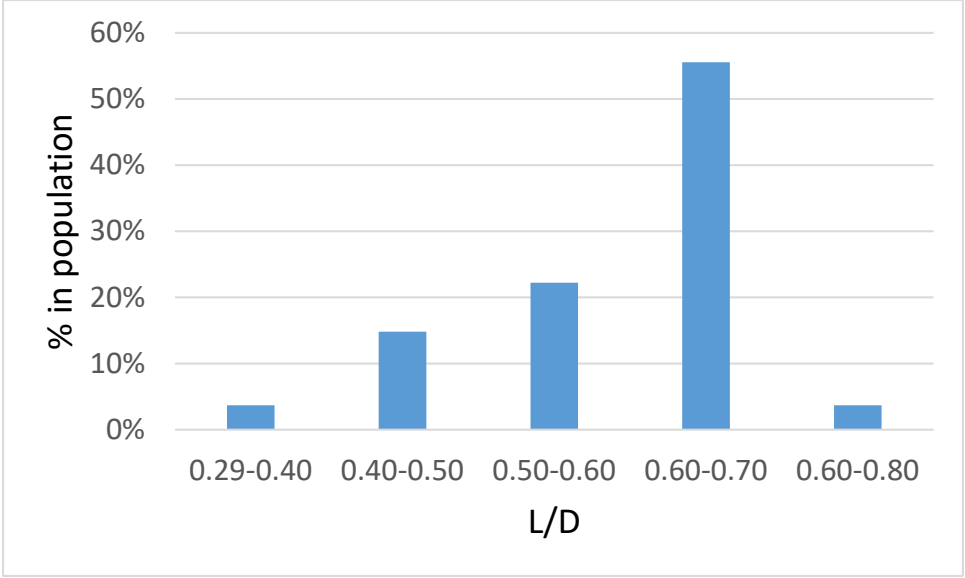
$$a_2 = \frac{|M_{max,2}|}{|V_{max,2}|}$$

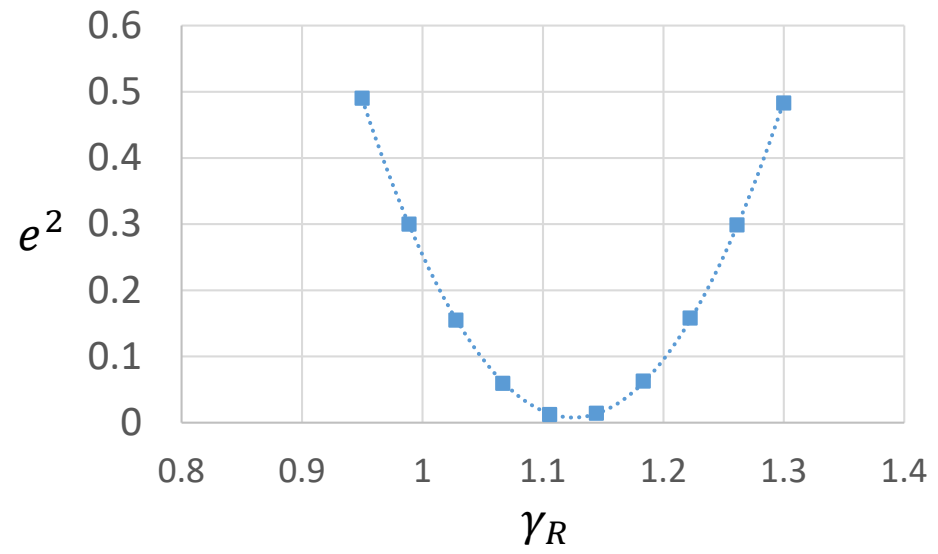
$$a_3 = \frac{|M_{max,2}|}{|V_{max,3}|}$$

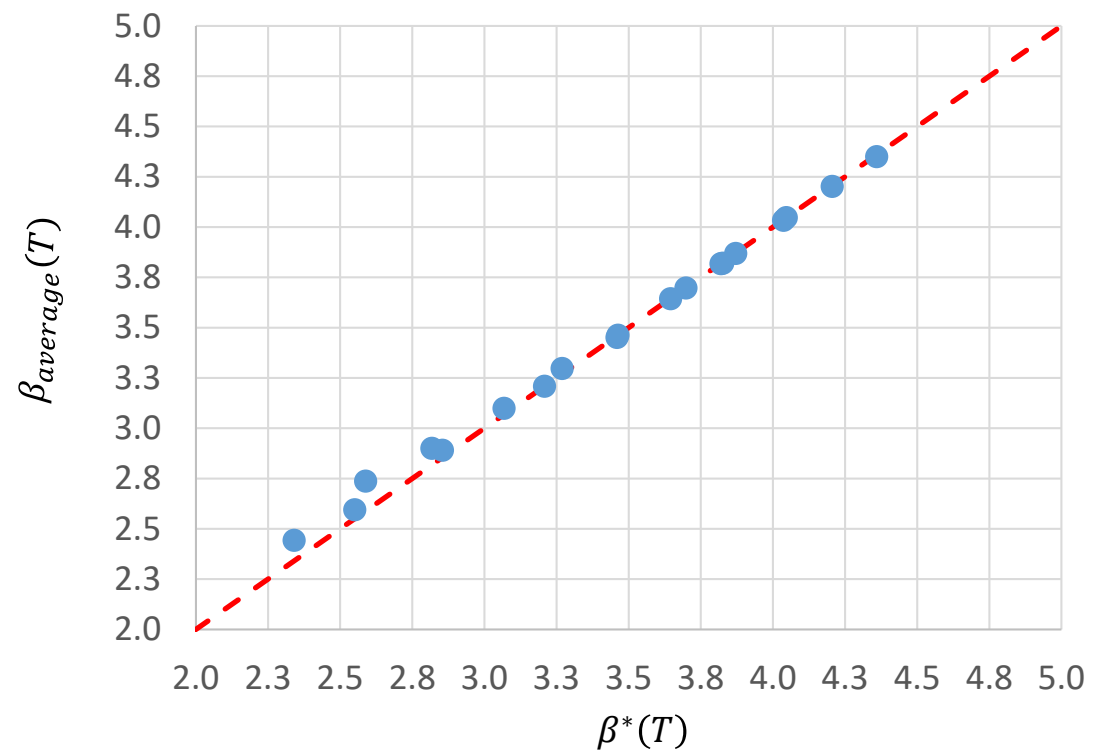


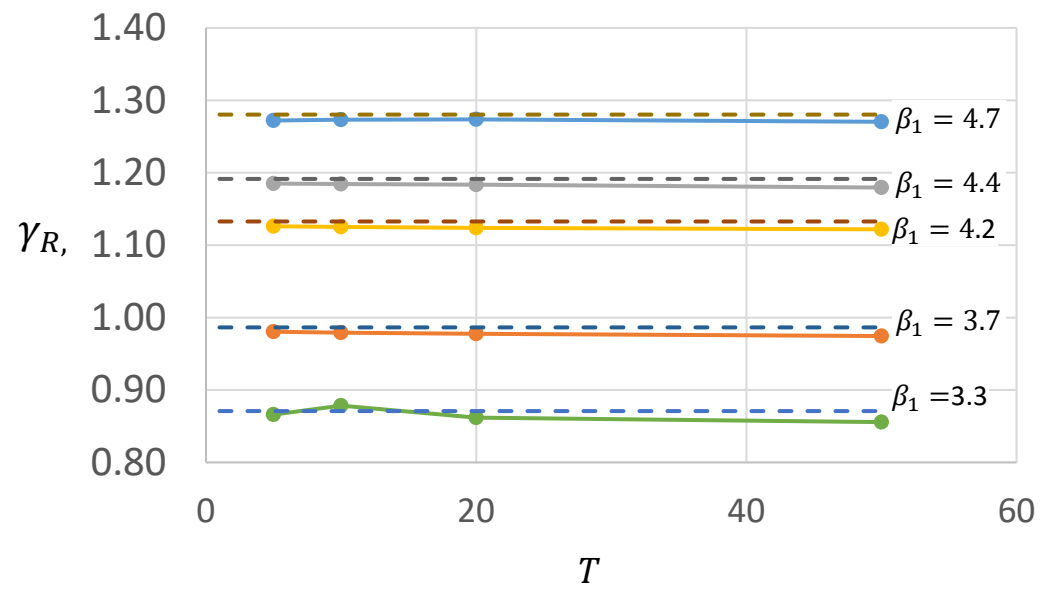


$$a = \frac{M_{max, shear span}}{V_{max, shear span}} = \frac{L}{4}$$

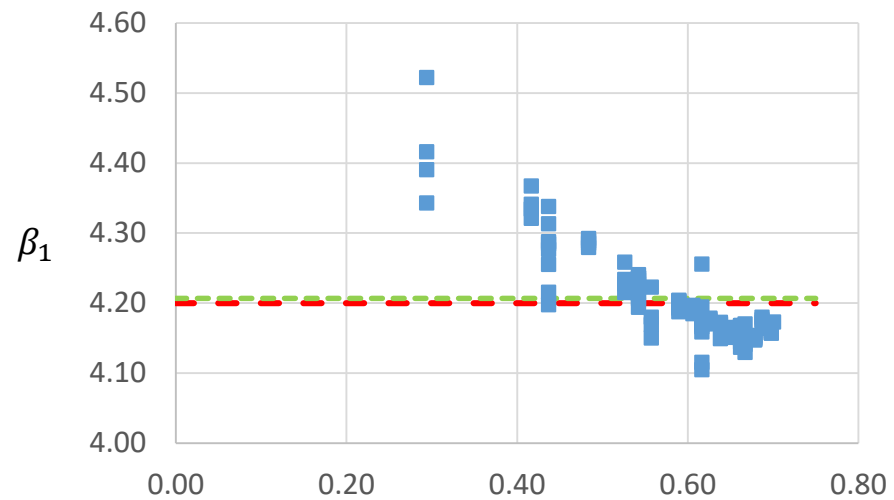




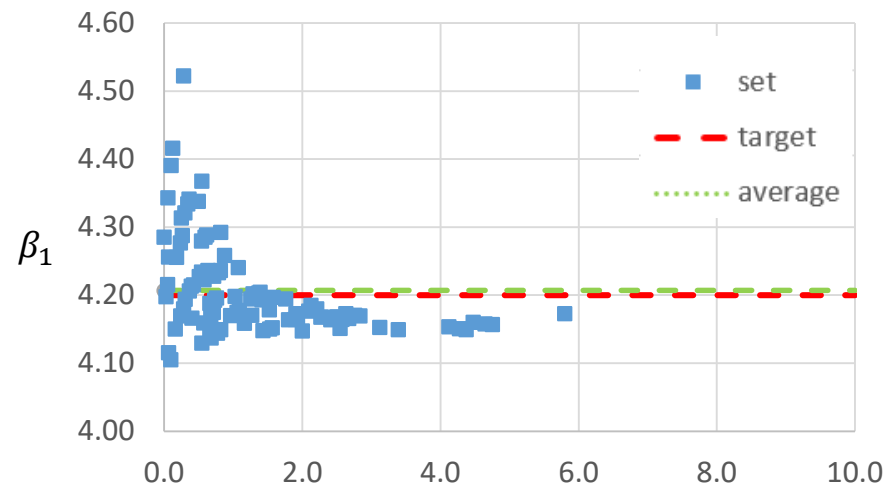




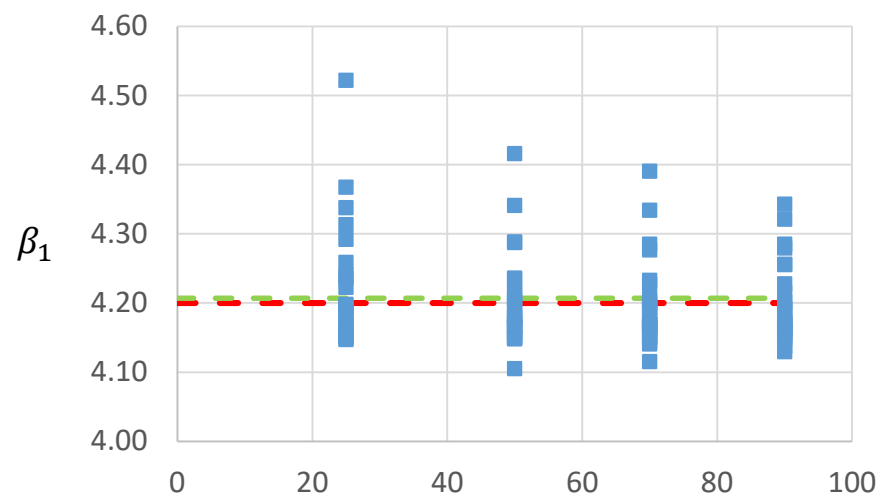




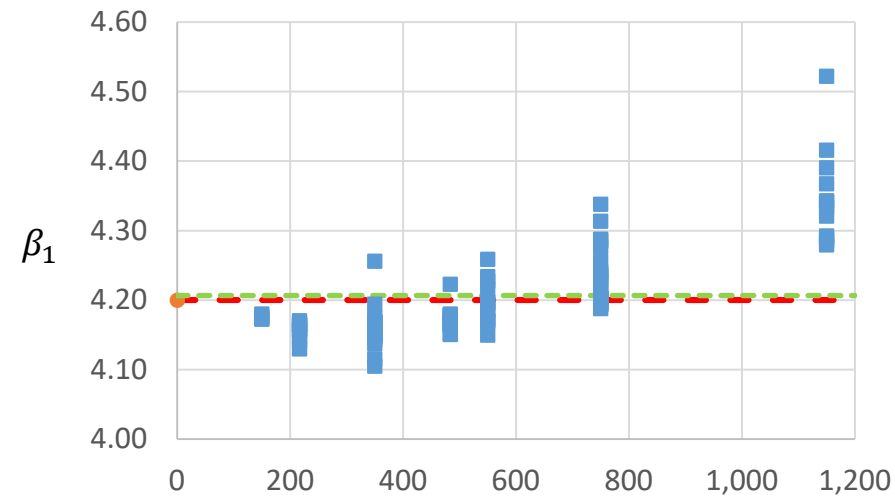
a)  $\frac{L}{D}$



b)  $\rho_w f_y$  [MPa]



c)  $f_{ck}$  [MPa]



d)  $d$  [mm]

