

**AN IMPROVED ALGORITHM FOR CHANNEL ALLOCATION ON DIRECT
SEQUENCE SPREAD SPECTRUM**

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**Thesis submitted in fulfillment of the requirements
For the award of the degree of
Master of Science in Computer**

**Faculty of Computer Systems & Software Engineering
UNIVERSITI MALAYSIA PAHANG**

JULY 2011

ABSTRACT

Graph coloring is an assignment a color to each vertex, which each vertex that adjacent is given a different color. Graph coloring is a useful algorithm for channel allocation on Direct Sequence Spread Spectrum (DSSS). Through this algorithm, each access point (AP) that adjacent gives different channels based on colors available. Welsh Powell algorithm and Degree of saturation (Dsat) are the popular algorithms being used for channel allocation in this domain. Welsh Powell algorithm is an algorithm that tries to solve the graph coloring problem. Dsat algorithm is an algorithm coloring sorted by building sequence of vertices dynamically. However, these algorithms have its weaknesses in terms of the minimum number of channel required. In this study, channel allocation called Vertex Merge Algorithm (VMA) is proposed with aim to minimize number of required channels. It is based on the logical structure of vertex in order to a coloring the graph. Each vertex on the graph arranged based on decreasing number of degree. The vertex in the first place on the set gives a color, and then this vertex is merged with non-adjacent vertex. This process is repeatedly until all vertices colored. The assignment provides a minimum number of channels required. A series of an experiment was carried out by using one computer. Vertex Merge Algorithm (VMA) simulation is developed under Linux platform. It was carried out in Hypertext Preprocessor (PHP) programming integrated with GNU Image Manipulation Program (GIMP) for open and edit image. The experimental results show that the proposed algorithm work successfully in channel allocation on DSSS with the minimum of channels required. The average percentage reduction in the number of required channels among the VMA, Dsat algorithm and Welsh Powell algorithm in the simple graph is equivalent to 0.0%. Meanwhile between the VMA and Dsat algorithm in the complex graph is equivalent to 18.1%. However, VMA and Welsh Powell algorithm is not compared in the complex graph since its drawback in terms of not fulfill the graph coloring concept. This is because there are two adjacent vertices have the same color. Overall, even there is no reduction for number of required channel among VMA, Dsat algorithm and Welsh Powell algorithm in the simple graph, but the outstanding significant contribution of VMA since it has reduction in the complex graph.

ABSTRAK

Pewarnaan graf merupakan pemberian warna untuk setiap verteks, untuk verteks yang berdekatan diberikan warna yang berbeza. Pewarnaan graf merupakan suatu algoritma yang digunakan bagi penempatan saluran pada Direct Sequence Spread Spectrum (DSSS). Melalui algoritma ini, setiap akses point (AP) yang berdekatan diberikan saluran yang berbeza berdasarkan warna tertentu. Algoritma Welsh Powell dan algoritma Darjah Kejenuhan (Dsatur) merupakan algoritma-algoritma terkenal yang telah digunakan untuk penempatan saluran dalam bidang ini. Algoritma Welsh Powell merupakan algoritma yang cuba menyelesaikan masalah pewarnaan graf. Algoritma Dsatur adalah algoritma pewarnaan graf yang dibuat dengan urutan verteks secara dinamik. Walaubagaimanapun, algoritma-algoritma ini mempunyai kelemahan dari segi jumlah minimum saluran yang diperlukan. Dalam kajian ini, dicadangkan penempatan saluran yang dikenali sebagai Algoritma Verteks Gabung (VMA) dengan tujuan untuk meminimumkan jumlah saluran yang diperlukan. Hal ini berdasarkan susunan logikal verteks untuk membentuk pewarnaan suatu graf dalam penempatan saluran. Setiap verteks dalam graf disusun berdasarkan penurunan jumlah darjah. Verteks dalam turutan pertama suatu set diberikan warna, kemudian verteks tersebut digabungkan dengan verteks yang tidak berdekatan. Proses ini terus berulang sehingga kesemua verteks diberikan warna. Ketetapan ini telah menyediakan jumlah saluran minimum yang diperlukan. Suatu siri eksperimen telah dijalankan dengan menggunakan sebuah komputer. Simulasi Algoritma Verteks Gabung (VMA) telah dibangunkan di bawah platform Linux. Ia telah dibina dengan bahasa pengaturcaraan Prapemroses Hiperteks (PHP) serta berintegrasikan GNU Image Manipulation Program (GIMP) untuk memaparkan dan mengemaskinikan gambar. Keputusan eksperimen menunjukkan bahawa algoritma yang dicadangkan telah berjaya dalam penempatan saluran pada Direct Sequence Spread Spectrum (DSSS) dengan jumlah saluran minimum yang diperlukan. Purata peratusan penurunan jumlah saluran di antara VMA, Dsatur algoritma dan Welsh Powell algoritma dalam graf sederhana adalah bersamaan dengan 0.0%. Sementara itu, di antara VMA dan Dsatur algoritma dalam graf kompleks adalah bersamaan dengan 18.1%. Namun, VMA dan Welsh Powell algoritma tidak dibandingkan dalam kompleks graf disebabkan kelemahan dalam hal tidak memenuhi konsep pewarnaan graf. Hal ini disebabkan terdapat dua verteks bersebelahan memiliki warna yang sama. Secara keseluruhan, tidak ada penurunan jumlah saluran yang diperlukan antara VMA, Dsatur algoritma dan Welsh Powell algoritma di dalam graf sederhana. Walaubagaimanapun, sumbangan penting VMA adalah penurunan jumlah saluran yang diperlukan di dalam kompleks graf.

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LIST OF SYMBOLS

$A(G)$	Adjacent matrix of graph
c	Color of graph
$C(V)$	Admissible coloring minimizing
E	Edge of graph
E_G	Set edge of graph
F	Set of colors
F'	Subset of colors
G	A graph
M	Set of merge vertex
i	Index of vertex or edge
I	Set index of element graph
j	Index of vertex or edge
k	Number of colors used
n	Number of vertex
$n(G)$	Normal order of graph
$m(G)$	Normal size of graph
l	Initial row in the VMT
R	Set of all possible $ V $ size integers valued rows
S	Set of initial rows the VMT
V_G	Set vertex of graph
$\chi(G)$	Chromatic numbers of graph

LIST OF ABBREVIATION

AP	Access Point
DSatur	Degree of Saturation
DSSS	Direct Sequence Spread Spectrum
EOG	Eye of GNOME
FCC	Federal Communications Commission
GHz	Gigahertz
GIMP	GNU Image Manipulation Program
GNU	GNU's Not Unix
GPL	General Public License
IEEE	Institute of Electronics and Electrical Engineers
ISM	Industrial Scientific and Medical
Mbps	Megabits per second
MHz	Megahertz
PNG	Portable Network Graphic
RGB	Red Green Blue
SS	Spread Spectrum
USA	United State of America
VMA	Vertex Merge Algorithm
VMO	Vertex Merge Operation
VMT	Vertex Merge Table
WLAN	Wireless Local Area Network

CHAPTER 1

INTRODUCTION

1.1 INTRODUCTION

The spectacular development of network and the internet has a big impact to the companies in various types and sizes. The advanced wireless technologies support the development of network, the internet and intranet capability for the mobile workers, isolated area and temporary facilities. Wireless expands and increases the capability of computer networking. The new technologies enable the wireless networking as one of the access in higher velocity and qualified for the computer network and the internet.

The wireless networks based on the Institute of Electrical and Electronics Engineers (IEEE) 802.11 standards (IEEE, 2007). This technology presents important disadvantages if compared with other radio networks, as a shorter range, security issue, difficulties providing inter-network or inter-operator roaming. However, the networks based on the IEEE 802.11 are unquestionably being chosen by most of the users (Gracia, 2005). Its popularity comes noticeable, beyond the evident advantages of the radio networks in contrast to the wired networks.

Nowadays, it is a common thing to see the coexistence of many Wireless Local Area Network (WLAN) networks in densely populated areas, either of private or of public nature (Hot-Spots), corporative. Domestic users use it to avoid the installation of new wires in their homes and to communicate with other users, in offices or university campuses are used to provide access to the internet or corporative intranets to their employees or students and, lately, operators and Internet Service Provider (ISP) have found a new market offering this access in public places, like hotels, airports or convention centers. With a high density of nodes, the presence of interference increases causing the performance perceived by users to degrade. In order to reduce the effect of interferences in cellular networks, a

channel planning is traditionally used. In cases of 802.11b and 802.11g WLAN networks, frequency channels are a scarce resource, since we can only count on three non overlapping channels. Therefore, the Channel Allocation Problem (CAP) is an important issue to solve.

1.2 CHANNEL ALLOCATION

Channel allocation can be defined as choosing, which channel the access point should use to communicate with the wireless terminals in its subnet without interfering with the transmissions from the other's access points (Mahonen et al. 2004). Understanding of channel allocation is very important because it relates to the overall capacity of wireless local area networks (Carpenter, 2008).

Channel allocation in WLAN 802.11 networks is studied as a part on the design of multicellular WLANs working in infrastructure mode. A good design can be evaluated according to two basic requirements: full coverage of the required area and the provision of a capacity suitable to support the traffic that is generated, without degrading the service as the number of user's increases. Although there is an endless list of parameters to consider, the requirements mentioned above can be obtained with an exhaustive selection of Access Points (APs) locations and the proper set of channels and power levels.

Several research articles have been published regarding channel allocation. Among them were those by (Al Mamun et.al. 2009; Chen et.al. 2008; Duan et.al. 2010; Mahonen et.al. 2004; Malone et.al. 2007; Raj, 2006; Riihijarvi et.al. 2005; 2006; Yuqing et.al. 2010; Yue et.al. 2010; and Zhuang et.al. 2010) Those articles revealed that channel allocation for DSSS is one of the current issues that still unsolved in channel allocation. Therefore, the study on this basis is initiated.

Wireless Local Area Networks (WLANs) operate in unlicensed portions of the frequency spectrum allotted by a regulatory body, like the Federal Communications Commission (FCC) in the United States of America (Goldsmith, 2005; IEEE, 2007). Each WLAN standard (802.11/a/b/g) defines a fixed number of channels for use by

access point (AP) and mobile users. For example, the 802.11b/g standard defines a total of 14 frequency channels of which 1 through 11 are permitted in the United States of America (Guizani, 2004). Actually, channel represents the center of frequency. There is only 5 MHz separation between the center frequencies. The signal falls within about 15 MHz of each side of the center frequency. Consequently, an 802.11b/g signal overlaps with several adjacent channel frequencies. Therefore, only three channels (channels 1, 6, and 11) available for use without causing interference (Gracia, 2005; Rackley, 2007; Theodore, 2001).

The Wireless LAN standard 802.11b and 802.11g in the process of distributing data using Direct Sequence Spread Spectrum (DSSS) technology (Goldsmith, 2005). DSSS works by taking a data stream of zeros and ones and modulating it with a second pattern, the chipping sequence. Various other electronic devices in a home, such as cordless phones, garage door openers, and microwave ovens, maybe use same frequency range. Any such device can interfere with a WLANs network, slowing down its performance and potentially breaking network connections (Perez, 1998; Theodore, 2001).

1.3 PROBLEM STATEMENT

According to the overview in the Section 1.1, DSSS system only has three none overlapping channels are located (Rackley, 2007; Theodore, 2001). When more than three access points (*APs*) are in same location, it may cause interference with another AP. Interference in communications is anything, which alters, modifies, or disrupts a signal as it travels along a channel between a source and a receiver (James, 2008; Stallings, 2003). In addition, interference decreased the network performance.

Thus, some of the research problems that arise in channel allocation can be stated as follows:

- How does allocate channel while there is more than three access points in same location?
- How to reduce the number of channels while there is more than three access points in same location?

Figure 1.1 shows the channel allocation problem when there exist more than three access points in the same area.

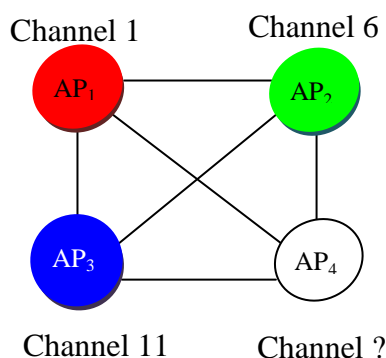


Figure 1.1: An example channel allocated in DSSS

From Figure 1.1 it can be seen that any interference with each other AP. AP₁ interference with AP₂, AP₃ and AP₄. AP₂ was interference with AP₁, AP₃ and AP₄. AP₃ was interference with AP₁, AP₂ and AP₄. AP₄ was interference with AP₁, AP₂ and AP₃. Every AP is given one channel. Based on DSSS channel allocation, the AP₁ given channel 1, AP₂ channel 6, AP₃ channel 11 and AP₄ another channel. When AP₄ is given channel, there was interference between APs. It leads to degradation overall network performance.

Currently, the internet is a very fast growth. Installation of AP more than three is inevitable. One way to solve this problem is minimizing the number of channels used. Several research articles have been published regarding this problem. Dsatur algorithm (Brelaz, 1979) and Welsh Powell algorithm (Welsh, 1967) has been proposed to determine the minimal number of color in the graph coloring theory. Riihijarvi (2006) enhanced Dsatur algorithm by determining the number of channel, based on the high degree of saturation access point. Meanwhile, Rohit (2008) enhance the Welsh Powell algorithm by determining the number of channel, based on high degree of access point. Both of these algorithms, has worked perfectly to determine the number of required channels. However, the number of channels is obtained using this algorithm is still large. Thus, create a new algorithm is motivation in this research to minimize the number of required channels.

1.4 RESEARCH OBJECTIVES

The objectives of the research are as follows:

- a) To propose a new algorithm to allocate and reduce the number of required channels.
- b) To test the performances of the proposed algorithm.

1.5 RESEARCH SCOPE

In this research, the following scope has been identified:

- a) The new algorithm channel allocated for Direct Sequence Spread Spectrum is simulated by using the PHP.
- b) The simulation results will be compared with the Welsh Powell algorithm (Rohit, 2008), and Degree of Saturation (DSatur) algorithm (Riihijarvi, 2006).

The Vertex Merge Algorithm (VMA) is proposed based on the graph coloring in order to reduce the required channel. The motivations of this simulation are to show the clarity of the algorithm, and provide the VMA simulator in order to minimize number of required channels.

1.6 ORGANIZATION OF THESIS

This thesis is organized as follows: Chapter 1 presents the background, problem statement, research objectives, research scope and organization of this thesis. Chapter 2 reviews basic concepts, definitions and theorems in graph theory, wireless technology, as well as algorithms used in this thesis. Chapter 3 proposes the Vertex Merge Algorithm (VMA). The experiment and result are elaborated in Chapter 4. Finally, the conclusion and recommendations for the future research are presented in Chapter 5.

1.7 CONCLUSION

This chapter introduces the channel allocation and Direct Sequence Spread Spectrum (DSSS) technology. Channel allocation in DSSS is the main focus attention

this research has been elaborated. Together with advantages of channel allocation brings specific problems. It occurs since the bigger number of access points. Determine of channel mechanisms to reducing the number of required channel become the issues. Thus suggest that proper strategies are required to solve the problems, which are the significance of this research.

CHAPTER 2

FUNDAMENTAL CONCEPTS AND THEORY

2.1 INTRODUCTION

This chapter describes the fundamental philosophical foundation which is a part of methodology. The basic concepts of the Direct Sequence Spread Spectrum (DSSS), channel on direct sequence spread spectrum, graph theory, graph coloring, vertex coloring and graph coloring in channel allocation are presented in this chapter. This chapter also reviews some of the foremost graph coloring algorithm namely the Welsh Powell Algorithm (Rohit, 2008) and Degree of Saturation (Dsatur) (Riihijarvi, 2006). These algorithms are then compared to the proposed Vertex Merge Algorithm (VMA) in Chapter 4, in terms of number of channel required. In particular, the reviewed channel allocation algorithm and proposed channel allocation algorithm are based on these concepts.

2.2 DIRECT SEQUENCE SPREAD SPECTRUM (DSSS)

An increasingly popular form of communications is known as the Spread Spectrum (SS). The Spread Spectrum technique was developed initially for military and intelligence requirements. The essential idea is to spread the information signal over a wider bandwidth in order to make jamming and interception more difficult. The first type of spread spectrum developed became known as frequency hopping. A more recent version is the Direct Sequence Spread Spectrum (DSSS). Both techniques are used in various wireless data network products. They also find use in other communications applications, such as cordless telephones (Bensky, 2008).

DSSS is one of the most widely used types of spread spectrum technology, owing its popularity to its ease of implementation and high data rates (Carpenter, 2008). Most of the equipment or the Wireless LAN device on the market uses DSSS

technology. DSSS is a method for sending data in which sender and recipient system is both on the set wide frequency is 22 MHz divides the available 83.5 MHz spectrum (in most countries) into 3 wide-band 22 MHz channels. The Institute of Electronics and Electrical Engineers (IEEE) 802.11 standard calls for use of the 2.4 GHz ISM band ranging from 2.400 to 2.497 GHz (Theodore, 2001; Goldsmith, 2005).

IEEE set on the use of DSSS data rates 1 or 2 Mbps in the 2.4 GHz Industrial Scientific and Medical (ISM) band, under the 802.11 standard. Meanwhile, the 802.11b standard specified data rate of 5.5 and 11 Mbps. IEEE 802.11b tools that work on 5.5 or 11 Mbps capable of communicating with the tools that 802.11 work on 1 or 2 Mbps 802.11b standard provides for backward compatibility. In 2003, the IEEE 802.11g standard providing a 54 Mbps data rate using the ISM frequencies. The advantage of 802.11g over 802.11a is that it is backward-compatible with 802.11b (IEEE, 2007).

2.2.1. Channel

Channel is a section on the band frequency (Rackley, 2007). This part is very important so that each frequency does not overlap. DSSS system uses a definition of more conventional channels. Each channel is a band that wide frequency the adjacent 22 MHz. Channel 1, for example, the work frequency of 2.401 GHz to 2.423 GHz ($2.412 \text{ GHz} \pm 11 \text{ MHz}$); channel 2 working of 2.406 to 2.429 GHz ($2.417 \pm 11 \text{ MHz}$). Figure 2.1 illustrates this description.

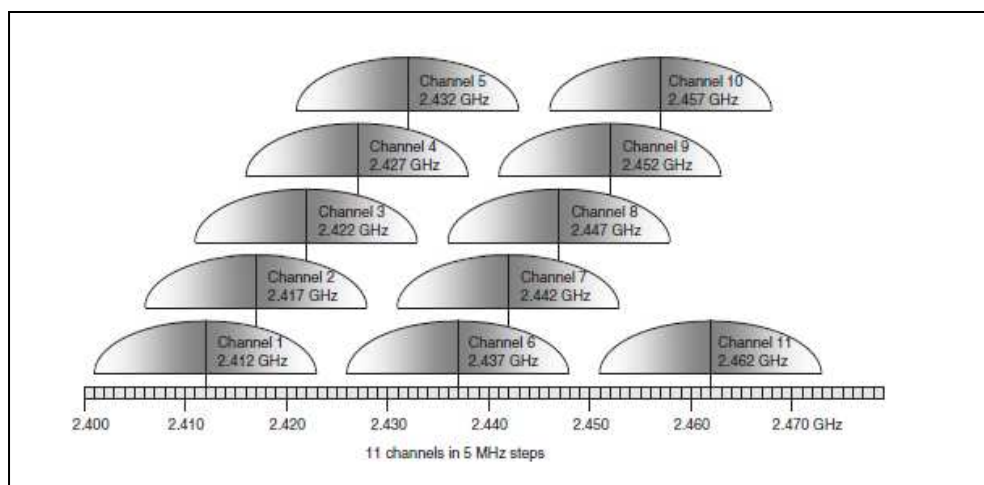


Figure 2.1: DSSS channel allocation (Carpenter, 2008)

An understanding of the legacy 802.11, 802.11b and 802.11g radio is used, its the same important to understand how the IEEE standard divides the 2.4 GHz ISM band into 14 separate channels, as listed in Table 2.1. Although the 2.4 GHz ISM band is dividing into 14 channels, the Federal Communications Commission (FCC) or local regulatory body designate which channels are allowed to be used. Table 2.1 also shows what channels are supported in a sample of a few countries. The regulations can vary greatly between countries (Ahmad, 2003; Carpenter, 2008). Table 2.1 shows a complete list of channels that are used in the United State of America, Europe and Japan. The 802.11b standard defines total number of frequency is 14 channels which 1 through 11 are permitted in the United State of America (USA), 13 in Europe and 14 in Japan. From Table 2.1 can be seen that channels 1 and 2 overlapping with a significant scale. Each frequency listed in this chart is considered a central frequency. From this central frequency, is added and reduced to get an 11 MHz channel with a width of 22 MHz used. Now easily is seeing that channel at the nearness can be overlapping significantly.

Table 2.1: Determining the channel allocation DSSS (Carpenter, 2008)

Channel	Center Frequency (GHz)	USA	Europe	Japan
1	2,412	x	x	x
2	2,417	x	x	x
3	2,422	x	x	x
4	2,427	x	x	x
5	2,432	x	x	x
6	2,437	x	x	x
7	2,442	x	x	x
8	2,447	x	x	x
9	2,452	x	x	x
10	2,457	x	x	x
11	2,462	x	x	x
12	2,467		x	x

13	2,472		x	x
14	2,484			x

Use of DSSS system with the channels overlapping will cause interference between the-system. Because the frequencies node distance of 5 MHz and channels has a wide 22 MHz, the channels may only be placed in the same location if distance of channels 5, separate from one another. For example, channels 1 and 6 does not overlapping. Channel 2 and 7 does not overlapping, etc. There is a maximum of three systems sequence may direct that can be placed on the same location as channels 1, 6 and 11 are channels that are not overlapping theoretically. Three non-overlapping channels that are depicted in Figure 2.2 follows:

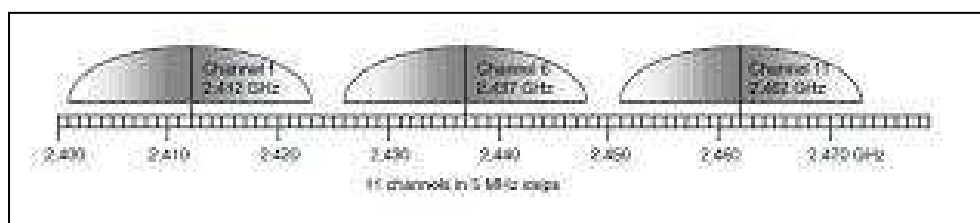


Figure 2.2: DSSS non-overlapping channels (Carpenter, 2008)

To use DSSS systems with overlapping channel (e.g., channel 1 and 2) in the same physical space would cause interference between the systems. DSSS systems using overlapping channel should not be co-located because there will almost always be a drastic or complete reduction in throughput. Because the center frequencies are 5 MHz apart, and the center frequencies for non-overlapping channels must be at least 25 MHz apart, channel should be co-located only if the channel numbers are at least five apart.

2.3 DEFINITION OF GRAPH

We define here all the common graphs and graph properties same as standard notation used by Ballobas (1998).

A graph is a mathematical structure consisting of two sets V and E (Diestel, 2010). The elements of V are called *vertices* and the elements of E are called *edges*.

Each edge is identified with a pair of vertices. If the edges of the graph G are identified with ordered pairs of vertices, then G is called a *directed* graph. Otherwise G it is called an *undirected* graph (Koster, 2010). Our discussions in this thesis are concerned with undirected graphs.

We use the symbols v_1, v_2, v_3, \dots to represent the vertices and the symbols e_1, e_2, e_3, \dots to represent the edges of a graph. The vertices v_i and v_j associated with and edge e_i are called the *end vertices* of e_i . The edge e_i is then denoted as $e_i = v_i v_j$. Note that while the elements of E are distinct, more than one edge in E may have the same pair of end vertices. All edges having the same pair of end vertices are called *parallel* or *multiple edges*. Further, the end vertices of an edge need not be distinct. If $e_1 = v_i v_j$, then the edge e_1 is called a *self-loop* at the vertex v_i .

An edge is said to be incident on its end vertices. Two vertices are *adjacent* if they are the end vertices of and edge. If two edges have a common end vertex then these edges are said to be *adjacent* (Bacak, 2004).

For example, in the Figure 2.3 edge e_1 is incident on vertices v_1 and v_2 ; v_3 and v_4 are two adjacent vertices, while e_1 and e_2 are two adjacent edges.

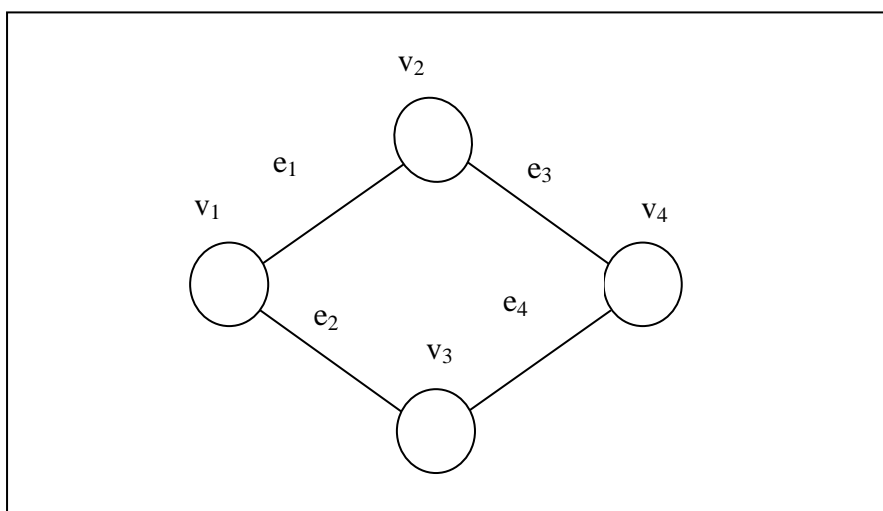


Figure 2.3: A Graph G

The cardinality of the vertex set of a graph G is called the *order* of G and is commonly denoted by $n(G)$, or more simply by n when the graph under considerations is clear. Meanwhile, the cardinality of its edge set is the size of G and is often denoted by $m(G)$ or m . An (n, m) graph has order n and size m . A graph with no edges is called an *empty graph*. A graph with no vertex is called a *null graph*. A *subgraph* of a graph G is a graph whose vertex set is a subset of that of G , and whose adjacency relation is a subset of that of G restricted to this subset.

The number of edge incident on a vertex v_i is called the *degree* of the vertex, and it is denoted by $\deg(v_i)$. Sometimes the degree of a vertex is also referred to as its valence. By definition, a self-loop at a vertex v_i contributes 2 to the degree of v_i . A vertex is called *even* or *odd* according to whether its degree is even or odd. A vertex of degree 0 in G is called *isolated vertex* and a vertex of degree 1 is an end-vertex of G . The minimum degree of G is the minimum degree among the vertices of G and is denoted by $\delta(G)$. The maximum degree is defined similarly and is denoted by $\Delta(G)$.

Theorem 2.1 (Euler): The sum of the degrees of a graph is twice the number of edges.

Corollary 2.1: In a graph, there is an even number of vertices having an odd degree.

Proof: Consider separately, the sum of the degrees that are odd and the sum of those that are even. The combined sum is even by the previous theorem, and since the sum of the even degrees is even, the sum of the odd degrees must also be an even. Hence, there must be even number of vertices of odd degree.

To further assumed that G is a simple graph. Graph G with vertex set $V_G = (v_1, v_2, \dots, v_n)$ and edge set $E_G = (e_1, e_2, \dots, e_m)$ can be depicted in the matrix. One matrix is the matrix $n \times n$ adjacent of $A(G) = [a_{ij}]$, where:

$$a_{ij} = \begin{cases} 1, & \text{if } v_i v_j \in E_G \\ 0, & \text{if } v_i v_j \notin E_G \end{cases}$$

Figure 2.4 shows the adjacent matrix of graph G from Figure 2.3

	v_1	v_2	v_3	v_4
v_1	0	1	1	0
v_2	1	0	0	1
v_3	1	0	0	1
v_4	0	1	1	0

Figure 2.4: A Graph G with the adjacent matrix

2.4 COMMON FAMILIES OF GRAPHS

2.4.1 Simple Graph

A *simple graph*, also called a *strict graph* is an *undirected graph* that has no loops or multiple edges and no more than one edge between any two different vertices. In a simple graph with n vertices every vertex has a degree that is less than n . Figure 2.5 shows an example of the simple graph.

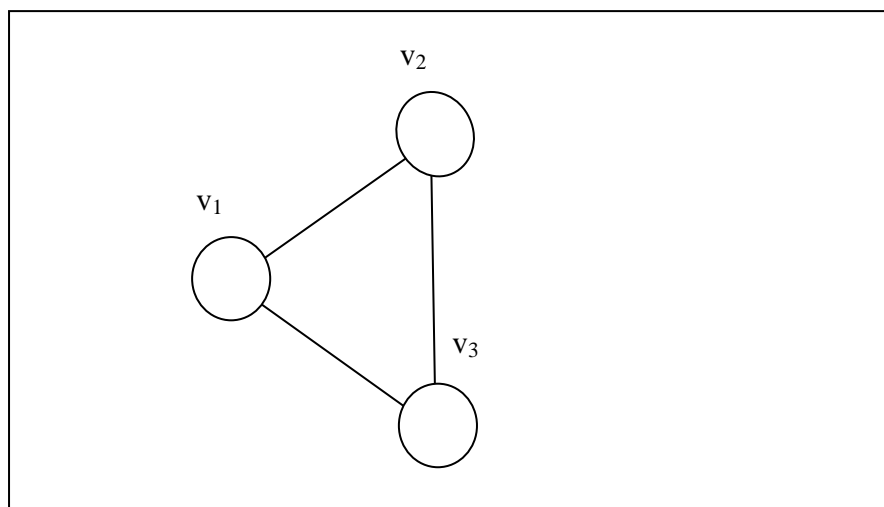


Figure 2.5: A simple graph