

# Effectiveness factor of fast ( $\text{Fe}^{3+}/\text{Fe}^{2+}$ ), moderate ( $\text{Cl}_2/\text{Cl}^-$ ) and slow ( $\text{O}_2/\text{H}_2\text{O}$ ) redox couples using $\text{IrO}_2$ -based electrodes of different loading

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**Abstract** The effectiveness factor,  $E_f$  (fraction of the electrode surface that participates effectively in the investigated reaction) of fast ( $\text{Fe}^{3+}/\text{Fe}^{2+}$ ), moderate ( $\text{Cl}_2/\text{Cl}^-$ ) and slow ( $\text{O}_2/\text{H}_2\text{O}$ ) redox couples has been estimated using  $\text{IrO}_2$ -based electrodes with different loading. The method of choice was linear sweep voltammetry (measurement of the anodic peak current) for the  $\text{Fe}^{3+}/\text{Fe}^{2+}$  redox couple and steady-state polarization (determination of the exchange current) for the  $\text{O}_2$  and  $\text{Cl}_2$  evolution reactions. The results have shown that the effectiveness factor depends strongly on the kinetics of the investigated redox reaction. For the  $\text{Fe}^{3+}/\text{Fe}^{2+}$  redox couple, effectiveness factors close to zero (max 4%) have been obtained contrary to the  $\text{O}_2$  evolution reaction where effectiveness factors close to 100% can be achieved, all being independent of  $\text{IrO}_2$  loading. For the  $\text{Cl}_2$  evolution reaction, intermediate values of the effectiveness factor have been found and they

decrease strongly, from 100% down to about 60%, with increasing loading.

**Keywords** DSA<sup>®</sup> (Ti/ $\text{IrO}_2$ ) electrodes ·  $\text{Fe}^{3+}/\text{Fe}^{2+}$  redox couple · Linear sweep voltammetry (LSV) ·  $\text{O}_2$  and  $\text{Cl}_2$  evolution reactions · Effectiveness factor · Relative effectiveness factor

## 1 Introduction

In heterogeneous catalysis, the term effectiveness factor has been introduced by Levenspiel [1]. The effectiveness factor,  $E_f$ , is defined as the ratio of the apparent reaction rate within a pore and the reaction rate not affected by diffusion.

In electrochemistry, the effectiveness factor was presented for the first time by Coeuret et al. in 1976 [2] for a 3D electrochemical reactor for the recovery of metal ions. These authors define the effectiveness factor as the ratio of the measured electrolytic current and the current obtained with an electrode whose overpotential is maintained constant. Later, Savinell et al. [3] used the effectiveness factor,  $E_f$ , for the investigation of dimensionally stable anodes (DSA<sup>®</sup>) consisting of an electrocatalytic porous coating of few micrometer thickness deposited on a conductive metal base, usually Ti. These electrodes are 3D devices and, in principle, have a large surface area.

In this study, different electrochemical measurements (linear sweep voltammetry and steady-state polarization) on Ti/ $\text{IrO}_2$  electrodes with different  $\text{IrO}_2$  loading have been performed for the estimation of the effectiveness factor of three redox couples:  $\text{Fe}^{3+}/\text{Fe}^{2+}$ ,  $\text{O}_2/\text{H}_2\text{O}$  and  $\text{Cl}_2/\text{Cl}^-$ .

These reactions have been used to evaluate the influence of the electrode kinetics on the effectiveness factor,  $E_f$ , (i.e. the effective electrode area that indeed participates in the

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electrochemical reaction). In case of the  $O_2/H_2O$  and  $Cl_2/Cl^-$  redox couples, the experimentally obtained  $E_f$  values will be compared with those predicted by the analytical approach of overpotential distribution within the porous electrode (see details in the Appendix).

## 2 Experimental

The Ti/IrO<sub>2</sub> electrodes have been prepared by thermal decomposition of H<sub>2</sub>IrCl<sub>6</sub> (99.9% ABCR) at 500 °C in air. The aqueous solution of the precursor (46 mM) was applied by a micropipette inside a circular slot ( $\phi = 15$  mm,  $h = 0.5$  mm) on a Ti plate (25 × 25 mm) treated previously in boiling 1 M oxalic acid ( $\geq 97\%$  Fluka) solution. Four electrodes with different loading ( $E_{0.11}$ ,  $E_{0.28}$ ,  $E_{1.81}$  and  $E_{4.07}$ ) have been prepared, where E stands for electrode and the subscript stands for the loading in mg IrO<sub>2</sub> cm<sup>-2</sup>.

Electrochemical measurements were done in a single-compartment, three-electrode cell (50 ml) made of Teflon using a computer controlled EcoChemie potentiostat (model Autolab<sup>®</sup> PGSTAT 30), and the Ti/IrO<sub>2</sub> electrodes ( $E_{0.11}$ ,  $E_{0.28}$ ,  $E_{1.81}$  and  $E_{4.07}$ ) have been used with an exposed geometric area of 0.78 cm<sup>2</sup> as the working electrode (WE), Pt wire (Goodfellow 99.99%) as the counter electrode (CE) and a mercurous sulfate electrode (MSE: Hg/Hg<sub>2</sub>SO<sub>4</sub>/K<sub>2</sub>SO<sub>4</sub>sat., Radiometer REF621; 0.64 V vs. SHE) as the reference electrode (RE).

In the experiments with the Fe<sup>3+</sup>/Fe<sup>2+</sup> redox couple, linear sweep voltammetric measurements at different scan rates have been performed at 25 °C in an aqueous solution of 50 mM Fe<sup>3+</sup>/Fe<sup>2+</sup> + 1 M HCl. For the O<sub>2</sub> evolution and Cl<sub>2</sub> evolution reaction, (quasi)steady-state polarization measurements with a potential scan rate of 5 mV s<sup>-1</sup> have been performed at 25 °C in aqueous 1 M HClO<sub>4</sub> and 1 M HCl, respectively. All solutions were made using ultrapure (Millipore<sup>®</sup>) water. Potentials are expressed with respect to the mercurous sulfate electrode (MSE) used as a reference electrode.

The specific IrO<sub>2</sub> loading,  $m_{sp}$ , the roughness factor,  $\gamma_{3D}$ , calculated with Eq. 1 and the estimated coating thickness,  $L$ , calculated with Eq. 2, for the four IrO<sub>2</sub> electrodes are shown in Table 1.

**Table 1** Characteristics of the Ti/IrO<sub>2</sub> electrodes used: Specific IrO<sub>2</sub> loading,  $m_{sp}$ , three dimensional roughness factor,  $\gamma_{3D}$  (defined in Eq. 1) and estimated coating thickness,  $L$  (calculated with Eq. 2)

$m_{sp}/\text{mg IrO}_2 \text{ cm}^{-2}$	0.11	0.28	1.81	4.07
$\gamma_{3D}/-$	11.2	28.4	184	413
$L/\mu\text{m}$	0.13	0.32	2.1	4.7

$$\gamma_{3D} = a_{sp} \cdot m_{sp} \quad (1)$$

and

$$L = \frac{m_{sp}}{1000 \cdot \rho \cdot (1 - \varepsilon)} \quad (2)$$

where  $m_{sp}$  is the specific IrO<sub>2</sub> loading (mg IrO<sub>2</sub> cm<sup>-2</sup>),  $a_{sp}$  is the specific surface area (=101.5 cm<sup>2</sup> mg<sup>-1</sup> IrO<sub>2</sub>) of the coating [3],  $\rho$  is the bulk density of IrO<sub>2</sub> (11.7 g cm<sup>-3</sup>) and  $\varepsilon$  is the volume fraction of the pores in the coating (-). Calculations were made assuming  $\varepsilon = 0.26$ , which corresponds to the closest packing of uniform spherical particles.

### 2.1 Ohmic ( $IR_u$ ) drop correction

The ohmic drop correction was performed following the method of Shub [4], which allows the estimation of the total uncompensated resistance of a given system. In this method, it is assumed that the experimentally observed overpotential,  $\eta$  (V), at any current is given by:

$$\eta = a + b \ln I + IR_u \quad (3)$$

where  $a$  is the Tafel constant (V),  $b$  is the Tafel slope (V dec<sup>-1</sup>),  $I$  is the current (A) and  $R_u$  is the total uncompensated resistance ( $\Omega$ ) of the system between the working and the reference electrodes, assumed to be constant and independent of current. Derivation of Eq. 3 with respect to the current density yields Eq. 4, from which  $b$  and  $R_u$  can be obtained by plotting  $\frac{d\eta}{dI}$  Vs.  $I^{-1}$ :

$$\frac{d\eta}{dI} = \frac{b}{I} + R_u \quad (4)$$

The knowledge of  $R_u$  allows the correction of the experimental overpotential by subtracting the ohmic drop  $IR_u$  using Eq. 5:

$$\eta_{\text{corr}} = \eta - IR_u \quad (5)$$

In the numerical calculation, the derivative  $\frac{d\eta}{dI}$  was replaced by the increments  $\Delta\eta/\Delta I$  calculated from each pair of two consecutive experimental points.

### 2.2 Estimation of the effectiveness factor

For the Fe<sup>3+</sup>/Fe<sup>2+</sup> redox couple, the effectiveness factor,  $E_f$ , of the IrO<sub>2</sub> electrodes with different loading was calculated through linear sweep voltammetric (LSV) measurements using the relation:

$$E_f = \frac{I_{pa}}{\gamma_{3D} \cdot (I_{pa})_{2D}} \quad (6)$$

where  $I_{pa}$  is the anodic peak current (A) measured with a three-dimensional electrode of a given loading,  $\gamma_{3D}$  the

three dimensional roughness factor (–) and  $(I_{pa})_{2D}$  the theoretical anodic peak current (A) on a polished (two dimensional) electrode calculated with Eq. 7:

$$(I_{pa})_{2D} = (2.69 \times 10^5)n^{3/2}A_g \cdot D_{Fe^{2+}}^{1/2} \cdot C_{Fe^{2+}} \cdot v^{1/2} \quad (7)$$

where  $n$  is the number of exchanged electrons (–),  $A_g$  is the geometric surface area ( $\text{cm}^2$ ),  $D_{Fe^{2+}}$  is the diffusion coefficient of  $Fe^{2+}$  ( $\text{cm}^2 \text{s}^{-1}$ ),  $C_{Fe^{2+}}$  is the concentration of  $Fe^{2+}$  ( $\text{mol cm}^{-3}$ ) and  $v$  is the scan rate ( $\text{V s}^{-1}$ ). For the calculation of  $(I_{pa})_{2D}$  a diffusion coefficient of  $D_{Fe^{2+}} = 5.4 \times 10^{-6} \text{cm}^2 \text{s}^{-1}$ , reported for a polished Pt electrode in aqueous medium [5], has been used.

For oxygen and chlorine evolution, the effectiveness was calculated with respect to the Ti/IrO<sub>2</sub> electrode of lowest loading taken as a reference (relative effectiveness factor,  $E_f^{\text{rel}}$ ) using Eq. 8:

$$E_f^{\text{rel}} = \frac{(j_0)_{3D}/m_{sp}}{(j_0)_{3D}^{\text{ref}}/m_{sp}^{\text{ref}}} \quad (8)$$

where  $(j_0)_{3D}^{\text{ref}}$  and  $m_{sp}^{\text{ref}}$  are, respectively, the exchange current density and the specific loading of the reference 3D electrode (in the present case, the electrode  $E_{0.11}$  with 0.11 mg IrO<sub>2</sub>  $\text{cm}^{-2}$  specific loading).

### 3 Results and discussion

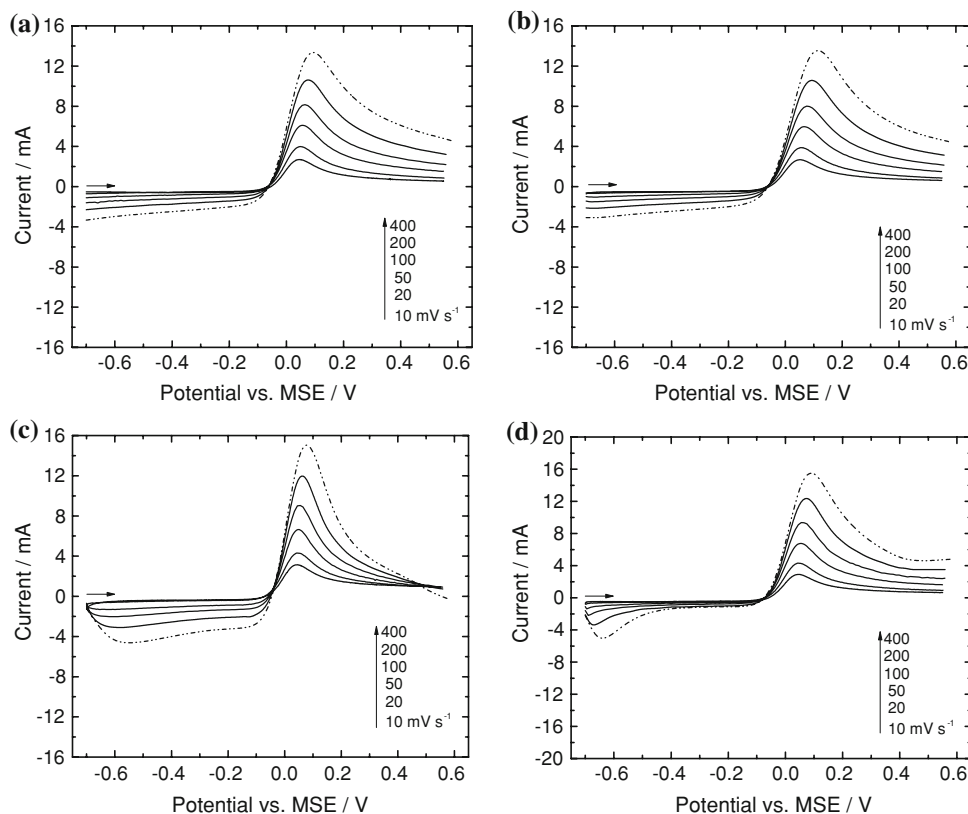
#### 3.1 Effectiveness factor of the $Fe^{3+}/Fe^{2+}$ redox couple

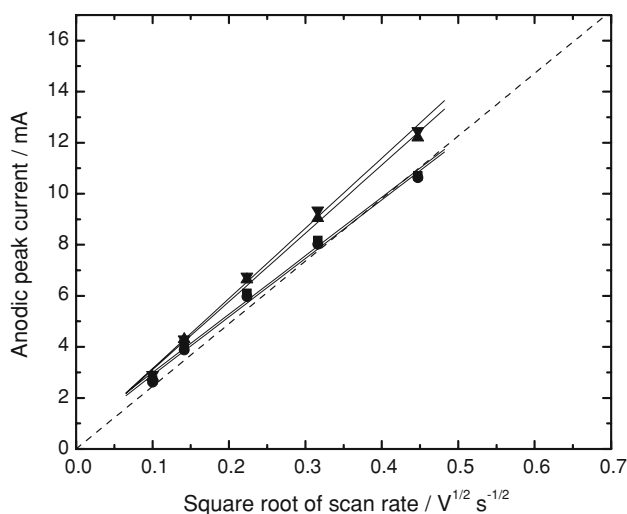
Figure 1a–d shows linear sweep voltammograms without  $IR_u$  drop correction, obtained with four different electrode loadings and using different scan rates. Figure 2 shows the plot of anodic peak current,  $I_{pa}$ , as a function of the square root of scan rate,  $v^{1/2}$ , for different loadings. It is seen that the  $I_{pa}-v^{1/2}$  curves are quasi-independent of loading. This is already an indication that under the investigated conditions, almost exclusively, the 2D surface is involved in the LSV measurements. In fact, calculated with Eq. 6, the experimentally obtained effectiveness factors,  $E_f$ , were found in the 0–4% range. This means that the pores of the 3D structure are not accessible for the reaction due to the fast kinetics of this redox couple.

#### 3.2 Effectiveness factor of the oxygen evolution reaction ( $O_2/H_2O$ )

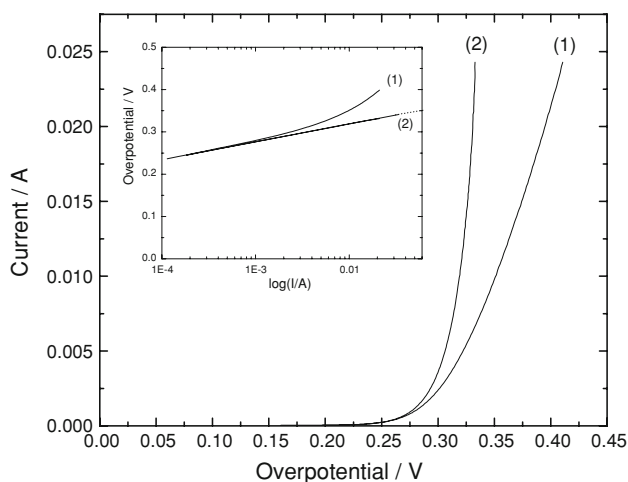
Figure 3 shows a typical polarization curve obtained in 1 M HClO<sub>4</sub> on the Ti/IrO<sub>2</sub> electrode ( $E_{0.11}$ ) before (curve 1) and after (curve 2)  $IR_u$  drop correction using the uncompensated

**Fig. 1** LSV measurements (without ohmic drop correction) in 50 mM  $Fe^{3+}/Fe^{2+}$  + 1 M HCl using four different loadings, **a**  $E_{0.11}$ , **b**  $E_{0.28}$ , **c**  $E_{1.81}$  and **d**  $E_{4.07}$ , and different scan rates, 10, 20, 50, 100, 200 and 400  $\text{mV s}^{-1}$ .  $T = 25^\circ \text{C}$





**Fig. 2** Anodic peak current,  $I_{pa}$ , from measurements of Fig. 1 as a function of the square root of scan rate,  $v^{1/2}$ , obtained for different electrode loadings: black square:  $E_{0.11}$ , black circle:  $E_{0.28}$ , black up-pointing triangle:  $E_{1.81}$ , black down-pointing triangle:  $E_{4.07}$ . Dashed line shows  $(I_{pa})_{2D}$  calculated with Eq. 7

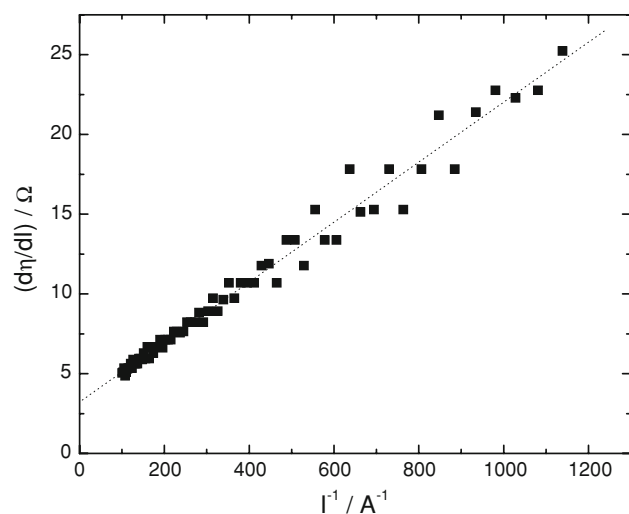


**Fig. 3** Steady-state ( $5 \text{ mV s}^{-1}$ ) polarization curves obtained in 1 M  $\text{HClO}_4$  on the Ti/IrO<sub>2</sub> electrode ( $E_{0.11}$ ) before (curve 1) and after (curve 2) ohmic drop correction. Inset: Tafel lines before (curve 1) and after (curve 2) ohmic drop correction.  $T = 25 \text{ }^\circ\text{C}$

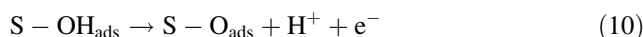
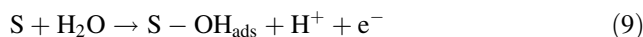
resistance  $R_u (= 3.2 \text{ } \Omega)$  of the cell determined from the intersection of the plot of  $\Delta\eta/\Delta I$  versus  $I^{-1}$  using Eq. 4 (see Fig. 4).

From both the uncorrected and the corrected polarization curves, the Tafel lines were plotted (inset of Fig. 3). It can be seen that in the high overpotential region, the uncorrected curve (curve 1) deviates strongly from linearity. However, the corrected polarization curve (curve 2) is linear, yielding a Tafel slope of  $43 \text{ mV dec}^{-1}$ .

In acidic medium, the following mechanism for  $\text{O}_2$  evolution on oxide electrodes has been proposed [6, 7]:



**Fig. 4** Determination of the uncompensated resistance from the intersection of the plot of  $\Delta\eta/\Delta I$  vs.  $I^{-1}$ , using the data of Fig. 3



In the first step, reaction (9), water is discharged forming adsorbed hydroxyl radicals. These hydroxyl radicals are further discharged forming a higher oxide according to reaction (10), which is finally decomposed to oxygen liberating the active site S following reaction (11).

Depending on the rate-determining step (rds) of this process, different Tafel slopes can be expected:  $120 \text{ mV dec}^{-1}$  if step 1 is the rds,  $40 \text{ mV dec}^{-1}$  if step 2 is the rds and  $15 \text{ mV dec}^{-1}$  if step 3 is the rds. The obtained experimental Tafel slope ( $43 \text{ mV dec}^{-1}$ ) indicates that certainly the formation of the higher oxide is the rate-determining step of the process. In fact, using differential mass spectroscopy (DEMS) measurements with  $^{18}\text{O}_2$ , it has been demonstrated that the higher oxide indeed participates in the oxygen evolution reaction [8]. Furthermore, the exchange current density,  $j_0 (\text{mA cm}^{-2})$ , and the Tafel slope,  $b$ , of the oxidation of the redox couple  $\text{O}_2/\text{H}_2\text{O}$  can be determined using Eq. 3. Table 2 shows the  $j_0$  and  $b$  values obtained for the four investigated Ti/IrO<sub>2</sub> electrodes.

The effectiveness factor,  $E_f$ , of the Ti/IrO<sub>2</sub> electrodes can be also predicted from an analytical approach (see Eq. 17 and details in the Appendix) and compared with the experimental relative effectiveness factor calculated with Eq. 8. For the prediction, the coating was modelled with close packing of uniform spherical particles ( $\varepsilon = 0.26$ ) having an estimated diameter of 2 nm to give a specific particle area of  $a_p = 3 \times 10^{-7} \text{ cm}^{-1}$ , and a bulk electrolyte conductivity of  $\gamma_0 = 0.37 \text{ } \Omega^{-1} \text{ cm}^{-1}$  was considered. Table 3 shows that, as predicted, the experimental relative

**Table 2** Exchange current density,  $j_0$ , and Tafel slope,  $b$  (see Eq. 3), of the  $O_2/H_2O$  redox couple for four Ti/IrO<sub>2</sub> electrodes of different specific loading,  $m_{sp}$ , and the three dimensional roughness factor,  $\gamma_{3D}$  (defined in Eq. 1)

$m_{sp}/\text{mg cm}^{-2}$	$\gamma_{3D}/-$	$j_0/\text{mA cm}^{-2*}$	$b/\text{V dec}^{-1}$
0.11	11.2	$1.34 \times 10^{-6}$	0.043
0.28	28.4	$2.75 \times 10^{-6}$	0.043
1.81	184	$2.35 \times 10^{-5}$	0.043
4.07	413	$6.02 \times 10^{-5}$	0.043

\* Reported for 1 cm<sup>2</sup> geometric (projected) area

**Table 3** Oxygen evolution reaction: Comparison of the predicted (see Appendix) and experimental (Eq. 8) relative effectiveness factors,  $E_f^{\text{rel}}$ , for various IrO<sub>2</sub> loadings

$m_{sp}/\text{mg cm}^{-2}$	Prediction		Experimental	
	$K/-$	$E_f^{\text{rel}}/-$	$j_{0(3D)}/\text{mA cm}^{-2*}$	$E_f^{\text{rel}}/-$
0.11	0.00005	1.00**	$1.34 \times 10^{-6}$	1.00**
0.28	0.0001	1.00	$2.75 \times 10^{-6}$	0.81
1.81	0.0008	1.00	$2.35 \times 10^{-5}$	1.07
4.07	0.0018	1.00	$6.02 \times 10^{-5}$	1.21

The estimated experimental error of  $E_f^{\text{rel}}$  is 20%

\* Reported for 1 cm<sup>2</sup> geometric (projected) area

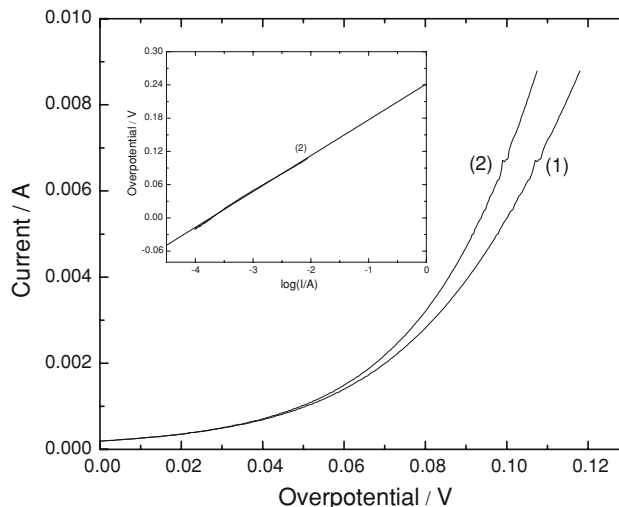
\*\* Taken as a reference

effectiveness factors,  $E_f^{\text{rel}}$ , are close to unity (found between 0.8 and 1.2), indicating that practically the whole active 3D surface of the coating participates in this reaction (so almost 100% of effectiveness factor). Two factors contribute in the obtained high effectiveness factor: The  $O_2/H_2O$  reaction is slow (low  $j_0$  value) and there is no concentration gradient within the coating as water is the reactive species present in excess.

### 3.3 Effectiveness factor of the chlorine evolution reaction ( $Cl_2/Cl^-$ )

Figure 5 shows a polarization curve typical for all Ti/IrO<sub>2</sub> electrode loadings obtained in 1 M HCl before and after  $IR_u$  drop correction using the uncompensated resistance determined from the intersection of the plot of  $\Delta\eta/\Delta I$  versus  $I^{-1}$  using Eq. 4. From the corrected polarization curves, the Tafel lines were plotted (inset of Fig. 5) and the exchange current density (for 1 cm<sup>2</sup> geometric area),  $j_0$ , of the redox couple  $Cl_2/Cl^-$  has been determined using Eq. 3 for the four investigated IrO<sub>2</sub> loadings (Table 4).

The same approaches as those given for  $O_2$  evolution have been used for the estimation of the predicted and experimental relative effectiveness factor,  $E_f^{\text{rel}}$ . Again, the lowest IrO<sub>2</sub> loading ( $E_{0.11}$ ) has been used as a reference. Table 5 shows that both the predicted and the experimental



**Fig. 5** Steady-state (5 mV s<sup>-1</sup>) polarization curves obtained in 1 M HCl on the Ti/IrO<sub>2</sub> electrode ( $E_{0.11}$ ) before (curve 1) and after (curve 2) ohmic drop correction. Inset: Tafel line after ohmic drop correction (curve 2)

**Table 4** Exchange current density,  $j_0$ , of the  $Cl_2/Cl^-$  redox couple for four Ti/IrO<sub>2</sub> electrodes of different specific loading,  $m_{sp}$ , and the three dimensional roughness factor,  $\gamma_{3D}$  (defined in Eq. 1)

$m_{sp}/\text{mg cm}^{-2}$	$\gamma_{3D}/-$	$j_0/\text{mA cm}^{-2*}$
0.11	11.2	0.22
0.28	28.4	0.56
1.81	184	2.32
4.07	413	4.83

\* Reported for 1 cm<sup>2</sup> geometric (projected) area

**Table 5** Chlorine evolution reaction: comparison of the predicted (see Appendix) and experimental (Eq. 8) relative effectiveness factors,  $E_f^{\text{rel}}$ , for various IrO<sub>2</sub> loadings

$m_{sp}/\text{mg cm}^{-2}$	Prediction		Experimental	
	$K/-$	$E_f^{\text{rel}}/-$	$j_{0(3D)}/\text{mA cm}^{-2*}$	$E_f^{\text{rel}}/-$
0.11	0.019	1.00**	0.22	1.00**
0.28	0.050	1.00	0.56	0.98
1.81	0.32	0.97	2.32	0.64
4.07	0.72	0.86	4.83	0.59

The estimated experimental error of  $E_f^{\text{rel}}$  is 20%

\* Reported for 1 cm<sup>2</sup> geometric (projected) area

\*\* Taken as a reference

relative effectiveness factor decreases with the IrO<sub>2</sub> loading, the latter being found between 1.0 and 0.6 in a reasonable agreement with prediction. Hence, with the  $Cl_2/Cl^-$  redox couple, the effectiveness is situated between those with  $O_2/H_2O$  and  $Fe^{3+}/Fe^{2+}$  redox couples because its kinetics is also intermediate between those of  $O_2/H_2O$  and  $Fe^{3+}/Fe^{2+}$ .

## 4 Conclusions

From this study, the following conclusions can be drawn:

- Linear sweep voltammetric (LSV) measurements with the  $\text{Fe}^{3+}/\text{Fe}^{2+}$  redox couple have shown that the  $I_{\text{pa}}$  vs.  $v^{1/2}$  plots are quasi-independent of loading, and effectiveness factors,  $E_f$ , in the range of 0 to 4% were obtained. This means that under the investigated conditions, only the 2D electrode surface area of the Ti/IrO<sub>2</sub> electrode is involved in the LSV measurements.
- The investigation of the kinetics of O<sub>2</sub> and Cl<sub>2</sub> evolution shows that chlorine evolution is much faster than oxygen evolution. With the  $E_{0,11}$  electrode, exchange current density of 0.22 mA cm<sup>-2</sup> was found for chlorine evolution, and only  $1.3 \times 10^{-6}$  mA cm<sup>-2</sup> for oxygen evolution.
- The relative effectiveness factors,  $E_f^{\text{rel}}$ , for O<sub>2</sub> evolution are close to unity (between 0.8 and 1.2) for all IrO<sub>2</sub> loadings, which show that practically all the 3D surfaces work effectively. However, for the Cl<sub>2</sub>/Cl<sup>-</sup> redox couple  $E_f^{\text{rel}}$  values between 0.6 and 1 were found, and they decrease with the IrO<sub>2</sub> loading. Just as its kinetics, the effectiveness factor of the Cl<sub>2</sub>/Cl<sup>-</sup> redox couple also lies between those of the O<sub>2</sub>/H<sub>2</sub>O and Fe<sup>3+</sup>/Fe<sup>2+</sup> redox couples. The experimentally obtained effectiveness factors for both O<sub>2</sub> and Cl<sub>2</sub> evolution are in reasonably good agreement with the prediction based on the analytical approach.

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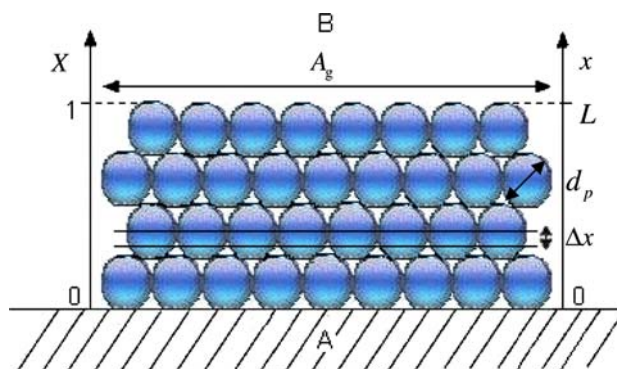
## Appendix: Analytical solution of the effectiveness factor

Coeuret et al. [2] attributed the observed decrease of effectiveness with increasing electrode thickness to an overpotential distribution in the electrolyte within the coating. In order to determine the effectiveness of a DSA<sup>®</sup> electrode, we have adopted this approach proposed originally for the design of a porous medium for the recovery of heavy metals. As illustrated in Fig. 6, we consider a differential element of thickness,  $\Delta x$ , and cross-section,  $A_g$ , and we suppose no concentration gradient in the pores.

Considering that the electronically conductive phase of the coating is equipotential, one can obtain for the overpotential,  $\eta$ , as a function of the dimensionless distance,  $X$ , the following second order linear ordinary differential equation:

$$\frac{d^2\eta(X)}{dX^2} - K^2\eta(X) = 0 \quad (12)$$

whose solution is written as



**Fig. 6** Schematic representation of the DSA<sup>®</sup> electrode according to a spherical particle configuration (SPC) consisting of IrO<sub>2</sub> spherical particles with diameter,  $d_p$ , showing a differential element of thickness,  $\Delta x$ , and cross-section,  $A_g$ .  $L$  is the thickness of the coating and  $X$  is the dimensionless distance. (a) Ti substrate; (b) electrolyte

$$\frac{\eta(X) - \eta(0)}{\eta(1) - \eta(0)} = \frac{\cosh(KX) - 1}{\cosh(K) - 1} \quad (13)$$

The dimensionless number  $K^2$  includes the morphological parameters like specific particle area,  $a_p$  (cm<sup>-1</sup>), void fraction of the DSA<sup>®</sup> coating, porosity,  $\varepsilon$  (-), thickness of the coating,  $L$  (cm), the apparent electrolyte conductivity ( $\gamma$ ) and the kinetics of the investigated electrochemical reaction ( $j_0$ ). For spherical particles, the specific area,  $a_p$ , is equal to  $6/d_p$ , where  $d_p$  is the particle diameter (cm). The apparent electrolyte conductivity within the DSA<sup>®</sup> coating,  $\gamma$ , depends on the void fraction,  $\varepsilon$ , as follows [2]:

$$\gamma = \gamma_0 \left( \frac{2\varepsilon}{3 - \varepsilon} \right) \quad (14)$$

where  $\gamma$  is the apparent electrolyte conductivity inside the DSA<sup>®</sup> coating ( $\Omega^{-1}$  cm<sup>-1</sup>), and  $\gamma_0$  is the bulk electrolyte conductivity ( $\Omega^{-1}$  cm<sup>-1</sup>).

Using the low-field approximation of the Butler-Volmer relationship,

$$j = j_0 \frac{F}{RT} \cdot \eta \quad (15)$$

where  $j$  is the current density (A cm<sup>-2</sup>),  $j_0$  is the exchange current density (A cm<sup>-2</sup>),  $F$  is the Faraday constant 96485 (C mol<sup>-1</sup>),  $R$  is the molar gas constant 8.31 (J mol<sup>-1</sup> K<sup>-1</sup>),  $T$  is the temperature (K) and  $\eta$  is the overpotential (V), the parameter  $K$  is given by Eq. 16:

$$K^2 = \frac{1}{\gamma} L^2 j_0 \frac{F}{RT} (1 - \varepsilon) a_p \quad (16)$$

Finally, the effectiveness factor,  $E_f$ , of the DSA<sup>®</sup> coating can be calculated from  $K$  with Eq. 17:

$$E_f = \frac{\tanh(K)}{K} \quad (17)$$

## References

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