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¹⁰Be in Ice Cores and ¹⁴C in Tree Rings: Separation of Production and Climate Effects

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Abstract Cosmogenic radionuclides are more and more used in solar activity reconstructions. However, the cosmogenic radionuclide signal also contains a climate component. It is therefore crucial to eliminate the climate information to allow a better interpretation of the reconstructed solar activity indices. In this paper the method of principal components is applied to ¹⁰Be data from two ice cores from opposite hemispheres as well as to ¹⁴C data from tree rings. The analysis shows that these records are dominated by a common signal which explains about 80% of the variance on multi decadal to multi millennial time scales, reflecting their common production rate. The second and third components are significantly different for ¹⁴C and ¹⁰Be. They are interpreted as system effects introduced by the transport of ¹⁰Be and ¹⁴C from the atmosphere where they are produced to the respective natural archives where they are stored. Principal component analysis improves significantly extraction of the production signal from the cosmogenic isotope data series, which is more appropriate for astrophysical and terrestrial studies.

Keywords Cosmic rays · Cosmogenic isotopes · Principal component analysis

1 Introduction

Cosmogenic radionuclides stored in natural archives such as ¹⁰Be in ice cores and ¹⁴C in tree rings have proven to be very useful in reconstructing past solar activity (Vonmoos et al.

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2006) and changes in the geomagnetic field intensity over many millennia (Muscheler et al. 2005). At present, cosmogenic radionuclides are the only proxy to significantly extend the record of solar activity which is restricted to the past 400 years of sunspot observations. They offer the unique opportunity not only to study the long-term history of solar activity (Solanki et al. 2004; Vonmoos et al. 2006; Steinhilber et al. 2008) and solar forcing (Steinhilber et al. 2009), but also to make predictions about future trends in solar variability (Abreu et al. 2008). However, the cosmogenic radionuclide signal contains also a climate component introduced by the transport of the radionuclides from the atmosphere where they are produced to the archive where they are stored. In order to make full use of the large potential of cosmogenic radionuclides the climate signal must be removed. Fortunately, while both nuclides are produced in a similar way, the response of the ¹⁰Be and the ¹⁴C systems to climate variations is very different by virtue of their different geochemical properties. ¹⁴C enters the global carbon cycle, whereas 10 Be is removed within 1–2 years from the atmosphere by precipitation. Thus, comparing both radionuclides makes it possible to distinguish between climate induced and production (solar/geomagnetic) variations. Since this idea was first put forward by Siegenthaler and Beer (1988), many authors have compared ${}^{14}C$ and ${}^{10}Be$ records and confirmed the presence of a dominant common signal of solar/geomagnetic origin as well as a less dominant climate component in cosmogenic radionuclides (e.g. Beer et al. 1988; Bard et al. 1997; Muscheler et al. 2004; Usoskin et al. 2009). In this article, we go an step further and propose to apply principal component analysis (PCA) to ¹⁰Be from ice cores and ¹⁴C from tree rings in order to decompose them into a production and a climate signal.

2¹⁰Be and ¹⁴C Systems

2.1 The Production of Cosmogenic Radionuclides

Cosmic rays are composed roughly of 90% protons, 9% helium nuclei, and 1% of heavier nuclei. When these highly energetic primary particles of galactic cosmic rays interact with atmospheric N and O, a chain of secondary particles is generated which is responsible for the production of cosmogenic radionuclides. There are two main processes which modulate the production rate of cosmogenic radionuclides in the atmosphere: changes in solar activity and changes in the geomagnetic field intensity. Since ¹⁰Be and ¹⁴C are produced by the same nucleonic secondaries of the cosmic ray induced atmospheric cascade, therefore their production signals are very similar. However, this production signal is modified by climate induced effects on the transport from the atmosphere into the respective archives as discussed in the next section.

2.2 ¹⁰Be and ¹⁴C in the Climate System

Figure 1 illustrates the similarities and differences between ¹⁰Be and ¹⁴C radionuclides in the Earth's system. After production, ¹⁴C oxidizes to CO₂ and enters in the carbon cycle. Within the carbon cycle, ¹⁴C gets involved in exchange processes among the atmosphere, the biosphere and the ocean. Its atmospheric residence time of about 8 years regarding exchange with the ocean is long enough that it can be considered as globally well mixed (Siegenthaler et al. 1980). In contrast, ¹⁰Be has an atmospheric residence time of 1 to 2 years. The fact that ¹⁴C enters the carbon cycle constitutes a fundamental difference between the measured signal in tree rings and the ¹⁰Be signal measured in ice cores. The carbon cycle acts like



Fig. 2 a: Δ^{14} C (per mil) as measured in tree rings. b: Standardized (i.e., subtracting the mean, then dividing by the standard deviation) of 14 C production rate calculated from Δ^{14} C (per mil) by using a carbon cycle model. c: Standardized ¹⁰Be concentrations (GRIP ice core) after being linearly interpolated to 1 year and low-pass filtered with a cutoff 40 years. d: Standardized ¹⁰Be fluxes (GRIP ice core) after being linearly interpolated to 1 year and low-pass filtered with cutoff 40 years.

a filter changing the original amplitude and phase of the ¹⁴C production signal (Peristykh and Damon 2003). As a consequence, direct comparison between Δ^{14} C measured in tree rings with ¹⁰Be measured in ice cores is not informative. We must first remove the effect of the carbon cycle on ¹⁴C. Figure 2a shows Δ^{14} C as measured in tree rings (Reimer et al. 2004). Figure 2b shows the corresponding ¹⁴C production rate calculated after applying the carbon cycle model by Oeschger et al. (1975). Figure 2c shows the ¹⁰Be concentrations as measured in ice cores whereas Fig. 2d shows the corresponding ¹⁰Be flux. Comparison of the four panels shows clearly that ¹⁰Be reflects changes in production rate much more directly than ¹⁴C. Furthermore, modelling shows that even a climate change from the present warm period with high solar activity to the Maunder minimum period with very low solar activity has only a small effect on the atmospheric transport and deposition processes of ¹⁰Be, confirming that production is the dominant factor (Heikkilä et al. 2008). Our two main working hypotheses are: (I) the ¹⁰Be and ¹⁴C records can be interpreted as being composed of a production signal, which is common to both radionuclides, and (II) a system signal, which is, most likely, not a common signal. Due to the different geochemical properties the combination of these two cosmogenic radionuclides in a PCA study provides a powerful tool to disentangle production and system effects.

2.3 The Data

In the present work we use ¹⁰Be measured in EDML (Ice core drilled in the framework of the European Project for Ice Coring in Antartica (EPICA); Steinhilber et al. 2011 (submitted)) and GRIP (Greenland Ice Core Project; Yiou et al. 1997) ice cores and ¹⁴C production derived from tree rings (INTCAL04; Reimer et al. 2004). The records employed in the analysis cover a common period of 8180 years from 1210 BP to 9390 BP (740 AD to 7440 BC). The averaged temporal resolution of the EDML time series is 4–5 years. The GRIP data have an average temporal resolution of 2–7 years. The ¹⁰Be records were linearly interpolated to 1 y, resampled to 10 y, and 40 y low-pass filtered. The ¹⁰Be fluxes were calculated from ¹⁰Be concentrations and the corresponding accumulation rates (*Flux* = density of ice * accumulation rate * concentration). The ¹⁴C record has a constant time resolution of 10 years and was 40 y low-pass filtered.

Based on the previous discussion, we assume that the three data sets are composed of a *production signal* P(t), as well as a *system effect signal* S(t). P(t) takes into account the modulation effect of the Sun and the geomagnetic field whereas S(t) represents the effect that the climate exerts on the radionuclides including noise

¹⁰Be_{grip}(t) =
$$P(t) + S_1(t)$$
,
¹⁰Be_{edml}(t) = $P(t) + S_2(t)$,
¹⁴ $C(t) = P(t) + S_2(t)$.

where the subscripts indicate that the radionuclides are influenced differently by the climate. Additionally, the $S_i(t)$ terms may be written as

$$S_i(t) = S_i[K(t)],$$

where K(t) stands for *climate*, an idealized variable which takes into account the temporal evolution of the climate. If the *climate* remains unchanged, then ¹⁴C changes must be equal to ¹⁰Be changes. As can be seen in Fig. 3 (only the interval 4400 to 5800 BP is shown) the three curves are over all very similar, but there are some differences, which must be due to changes in the climate system. To separate the data into two components, we assume that P(t) and $S_i(t)$ are uncorrelated. This assumption is supported by the following arguments: (1) the production does not depend on the climate and (2) although the climate change affects the ¹⁴C and ¹⁰Be systems very differently due to their different geochemical behaviors.



3 Separation of Production and System Effects Using PCA

Given the set of p correlated time series $(X_1(t), X_2(t), X_3(t), \ldots, X_i(t), \ldots, X_p(t))$ (in the present case p = 3, two ¹⁰Be records and one ¹⁴C record), we can use PCA to find a new set of uncorrelated time series $C_j(t)$, $j \le p$ such as the original p time series $X_i(t)$ can be decomposed as a linear combination of them, i.e.

$$X_i(t) = \sum_j \alpha_{i,j} C_j(t) \tag{1}$$

where

- 1. $\alpha_{i,j} = \sigma(X_i) R(C_j, X_i) / \lambda_j^{0.5}$ with $R(C_j, X_i)$ the correlation coefficient between the time series C_i and X_j and σ is the standard deviation.
- 2. λ_j are the eigenvalues of the covariance corresponding to the data matrix whose elements are Cov(X_i, X_j). They give the fraction of the total variance explained by the time series C_j .

The new time series C_j are known as the *principal components* (Jolliffe 2002, see also the electronic supplementary material).

4 Results

Table 1 shows the calculated coefficients $\alpha_{i,j}$, i.e. the contribution of component *j* to nuclide *i* as expressed by (1). Additionally, the squared correlation coefficients along with the eigenvalues are shown. The eigenvalue corresponding to the first component explains 65% of the total variance whereas the second and third components are responsible for 22% and 14% of the total variance, respectively. Clearly, all the original data sets are well correlated with the first principal component supporting our hypothesis (I) that production dominates both radionuclides. Production changes are indeed responsible for most of the variance in the data. We attribute it to solar activity as well as to geomagnetic field variations.¹ It is remarkable that the α_2 coefficient corresponding to ¹⁴C is significantly smaller than the corresponding α_2 of the two ¹⁰Be records. We note that

¹The effect of the Earth's magnetic field, can be removed by taking into account paleorecords of the geomagnetic field and production calculations (Masarik and Beer 2009).

	α1	α_2	α3
¹⁰ Begrip	0.54	0.79	0.29
¹⁰ Be _{edml}	0.57	-0.60	0.56
¹⁴ C	0.62	-0.13	-0.77
	R^2	R^2	R^2
¹⁰ Be _{grip}	0.55	0.41	0.04
¹⁰ Be _{edml}	0.64	0.23	0.13
¹⁴ C	0.74	0.01	0.24
	λ_1	λ_2	λ3
	65%	22%	14%

	2	
Table 2	$\alpha_{i,i}, R(C_i, X_i)^2$ ar	ıd
l after	synchronization	

	α1	α2	α3
¹⁰ Be _{grip}	0.58	0.72	0.38
¹⁰ Be _{edml}	0.58	-0.70	0.42
¹⁴ C	0.57	-0.02	-0.82
	R^2	R^2	R^2
¹⁰ Be _{grip}	0.77	0.18	0.06
¹⁰ Be _{edml}	0.77	0.16	0.07
¹⁴ C	0.72	0.00	0.27
	λ_1	λ_2	λ_3
	76%	11%	13%

 λ_i after synchronization

Table 1 $\alpha_{i,j}, R(C_i, X_i)^2$ and λ_i before synchronization

- 1. the variance not explained by the first principal component for ${}^{14}C$ is explained only by the third component and
- 2. the variance not explained by the first principal component for both ¹⁰Be records is mainly explained by the second component.

This confirms our initial hypothesis (II) that climate affects the ¹⁴C and ¹⁰Be systems differently. Hence, we attribute the second and third components to the climate effect on the ¹⁴C and ¹⁰Be systems, respectively.

The outcome of the PCA analysis depends critically on the accuracy of the time scales of the involved cosmogenic radionuclide records. While the time scale of ¹⁴C is based on dendrochronology and therefore accurate to one year, the uncertainty of the time scales of the ice cores increases with age to a few decades. This is due to the fact that a perfect annual marker as in the case of trees is missing. In addition ice is flowing which leads to a decrease in the annual layer thickness with increasing depth. As a result of small time shifts, PCA interprets part of the common production changes as a different signal and assigns it to the second component. To test this effect, we slightly adjusted the two ¹⁰Be time scales within the stated uncertainties to the ¹⁴C time scale using wiggle matching (Ruth et al. 2007). The adjustments relative to the original time scales are smaller than 30 y for EDML and smaller than 50 y for GRIP. Now the first principal component explains 76% and the second component 11% of the total variance respectively (Table 2). However, the structure of the data remains relatively unchanged. The α_2 coefficient for ¹⁴C is one order of magnitude smaller than the corresponding values for ¹⁰Be. The third component is still the main non-production source of variability in ¹⁴C, whereas the second component is the main non-production source of variability for both ¹⁰Be data sets. We notice that in both calculations the sign of α_2 for GRIP and EDML are different. This is a mathematical consequence of the PCA method because of the limited number of ¹⁰Be proxies used.

5 Conclusions

The method of PCA confirms that ¹⁰Be and ¹⁴C records which were all low-pass filtered with 40 years are dominated by a common signal which reflects the production rate and explains 76% of the variance on multi decadal to multi millennial time scales. The second and third components account for about 24% of the variance, which is significantly different for ¹⁴C and ¹⁰Be. This can be explained as system effects introduced by the transport of the respective radionuclides from the atmosphere where they are produced to the archive where they are stored (tree rings in the case of ¹⁴C and ice cores in the case of ¹⁰Be). The presence of such a high common variability is remarkable if we take into account that the ¹⁰Be records are from different hemispheres, and that ¹⁰Be and ¹⁴C are characterized by completely different geochemical systems (compare panels (a) and (c) in Fig. 2). We have focused on the decomposition of cosmogenic radionuclides into production and system effects. Since cosmogenic radionuclides are the only tool to reconstruct past solar activity indices such as sunspots and total solar irradiance, it is crucial to eliminate the climate component. PCA is an adequate tool to achieve this aim.

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