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## RESEARCH ARTICLE

# Eye position dependency of nystagmus during constant vestibular stimulation

Christopher J. Bockisch · Elham Khojasteh ·  
Dominik Straumann · Stefan C. A. Hegemann

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**Abstract** Alexander's law, the eye position dependency of nystagmus due to peripheral vestibular lesions, has been hypothesized to occur due to adaptive changes in the brainstem velocity-to-position neural integrator in response to non-reciprocal vestibular stimulation. We investigated whether it develops during passive head rotations that produce constant nystagmus for >35 s. The yaw rotation stimulus consisted of a 1-s acceleration ( $100^\circ/s^2$ ), followed by a lower acceleration ramp (starting at  $7.3^\circ/s^2$  and increasing at  $0.04^\circ/s^2/s$ ) until  $400^\circ/s$  was reached after 38 s. This stimulus was designed to offset the  $\sim 15$  s vestibular ocular reflex time constant (and the 150 s adaptation time constant) and produce constant velocity slow phases. In contrast to peripheral lesions, this vestibular stimulation is the result of real head turns and has the push–pull characteristics of natural movements. The procedure was successful, as the

average velocity of  $31^\circ/s$  was unchanged over the final 35 s of the acceleration period. In all 10 healthy human subjects, we found a large and stable Alexander's law, with an average velocity-versus-position slope of  $-0.366$  in the first half that was not significantly different in the second half,  $-0.347$ . These slopes correspond to integrator time constants of  $<3$  s, are much less than normal time constants ( $\sim 25$  s), and are similar to those observed in patients with peripheral vestibular lesions. Alexander's law also developed, on average, in 10 s. We conclude that Alexander's law is not simply a consequence of non-reciprocal vestibular stimulation.

**Keywords** VOR · Nystagmus · Vestibular · Adaptation · Alexander's law

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C. J. Bockisch (✉) · D. Straumann  
Department of Neurology, University Hospital Zürich,  
Frauenklinikstrasse 26, 8091 Zurich, Switzerland  
e-mail: [chris.bockisch@usz.ch](mailto:chris.bockisch@usz.ch)

C. J. Bockisch  
Department of Ophthalmology, University Hospital Zürich,  
Zurich, Switzerland

C. J. Bockisch · E. Khojasteh · S. C. A. Hegemann  
Department of Otorhinolaryngology, Head and Neck Surgery,  
University Hospital Zürich, Zurich, Switzerland

C. J. Bockisch · D. Straumann · S. C. A. Hegemann  
Zürich Centre for Integrative Human Physiology (ZIHP),  
University Hospital Zürich, University of Zürich,  
Zurich, Switzerland

## Introduction

Spontaneous nystagmus in patients with vestibular lesions often has a dependency on eye position, first described in 1912 (Alexander 1912) and called Alexander's law, where the slow-phase velocity is highest with gaze in the fast-phase direction. Modern measurements have further quantified Alexander's law in patients (Hegemann et al. 2007; Bockisch and Hegemann 2008), and caloric stimulation has been used to simulate peripheral vestibular disorders in healthy subjects and evoke similar patterns of eye position dependency as have been described in patients (Doslak et al. 1982; Robinson et al. 1984; Jeffcoat et al. 2008; Bockisch et al. 2012).

Hess (1982), and shortly thereafter Robinson et al. (1984), proposed that Alexander's law arose from changes in the brainstem/cerebellar velocity-to-position neural integrator, such that the integrator produces a smaller-than-normal command to compensate for elastic forces produced by

the extraocular tissues that pull the eye back to a central position. This would then result in centripetal drift of the eyes, which when added to the constant velocity signal from the vestibular system produces the eye position dependency of velocity.

The oculomotor velocity-to-position neural integrator has been localized to the brainstem [nucleus prepositus hypoglossi (Cannon and Robinson 1987; Cheron and Godaux 1987) and medial vestibular nucleus (McFarland and Fuchs 1992; McConville et al. 1994) for horizontal eye position, and the interstitial nucleus of Cajal for vertical and torsional position (King et al. 1981; Crawford et al. 1991; Crawford and Vilis 1993; Crawford 1994; Helmchen et al. 1998; Farshadmanesh et al. 2007)] and cerebellum (Takemori and Cohen 1974; Zee et al. 1981; Waespe et al. 1983). Typically, the brainstem is modeled as a positive position feedback system that increases the neural integrator time constant to around 12 s, and the cerebellum is modeled as a negative velocity feedback system that further increases the time constant to ~25 s (Optican and Zee 1984; Glasauer 2006).

Robinson et al. (1984) suggested that the process producing Alexander's law is an adaptive response to the vestibular lesion. Centripetal drift caused by a leaky integrator, when added to the constant velocity drift produced by the vestibular lesion, will reduce eye velocity in the direction of the slow phase, thus aiding vision for some gaze directions. Robinson et al. (1984) also performed several experiments to support the adaptation hypothesis. First, they reported that Alexander's law is not seen during 0.5-Hz sinusoidal head oscillations in normal humans, concluding it is not due to the normal vestibular ocular reflex (VOR). Second, they reported during caloric stimulation the emergence of Alexander's law is delayed by about 25 s relative to the onset of nystagmus, thus giving it the appearance of an adaptive response to non-reciprocal (unilateral) vestibular stimulation (which Robinson et al. called 'unnatural'). Unilateral caloric stimulation, as well as peripheral vestibular lesions, produces non-reciprocal stimulation in the sense that vestibular input from one side is not accompanied by the opposite change from the other side. Finally, during low constant head acceleration on a turntable ( $2.1^\circ/\text{s}^2$  after a velocity step of  $30^\circ/\text{s}$ ), Alexander's law was found but was reported to be weak and constant during the 60 s of stimulation. They interpreted this as meaning that a natural head rotation signal does not evoke Alexander's law; rather, a non-reciprocal pattern of stimulation (unilateral caloric or peripheral lesions) is necessary to provoke the adaptive mechanism.

We recently observed Alexander's law with bilateral bithermal stimulation (cold on one side, warm on the other) (Bockisch et al. 2012), which preserves the normal push-pull pattern of stimulation from real head movements,

which suggests Robinson et al.'s (1984) hypothesis should be re-evaluated. Peripheral vestibular disorders and caloric stimulation contain frequencies that are much lower than those produced by natural head movements and could help explain why Alexander's law has not been observed with higher-frequency head rotations (Robinson et al. 1984; Anagnostou et al. 2011). We therefore sought a stronger test of Robinson et al.'s (1984) hypothesis that only non-reciprocal patterns of stimulation produce Alexander's law. We chose a variant of their constant stimulation experiment, but did so with a paradigm that produces higher levels of nystagmus (simply by using higher velocities and accelerations), because our work in patients found that the strength of Alexander's law increased with higher levels of slow-phase velocity (Hegemann et al. 2007; Bockisch and Hegemann 2008), thus opening the possibility that Alexander's law was low in Robinson et al.'s (1984) constant stimulation experiments because the stimulus was too weak.

## Methods

### Subjects and equipment

Ten subjects with no reported visual or vestibular problems were studied. The experiments conformed to the principles of the Declaration of Helsinki and were approved by the local ethics committee. Subjects gave informed, written consent after the experimental procedure had been explained.

Subjects sat on a rotatable chair controlled with three motor-driven axes (Acutronic, Jona, Switzerland). Only the earth-vertical axis was used in these experiments. Subjects were secured in the chair with safety belts, and the head was fixed to the chair with individually adjusted masks (Sinmed BV, Reeuwijk, the Netherlands). The mask, made of a thermoplastic material (Posicast), was molded to the contour of the head. The center of the head was positioned in or near the chair rotation axis.

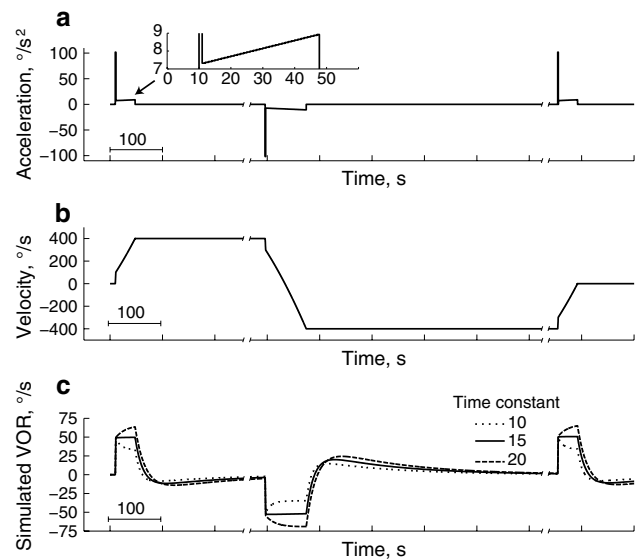
Search coils, produced by Skalar (Delft, the Netherlands) or Universal Trading Ventures, Inc (Cleveland, USA), were used to record the three-dimensional movements of both eyes. Orthogonal magnetic fields with frequencies of 80, 96, and 120 Hz were produced by a head-fixed coil frame ( $0.5 \text{ m}^3$ ). A fast Fourier transform was computed in real time by a digital signal processor to determine the voltage induced by each magnetic field (Primelec, Regensdorf, Switzerland). Eye position signals were digitized with 12-bit accuracy and sampled at 1,000 Hz using National Instruments (Austin, Texas) hardware and Labview software. Data were analyzed off-line with MatLab software (The MathWorks, Boston, MA). Coils were calibrated *in vivo* by having subjects fixate

targets from  $0^\circ$  to  $\pm 25^\circ$ , horizontally and vertically, in  $5^\circ$  increments.

A laser spot ( $\sim 0.25^\circ$  diameter) controlled by two mirror galvanometers was projected onto a chair-fixed screen positioned 80 cm in front of the subject for visual targets.

We first collected data for control trials to measure horizontal gaze evoked nystagmus. In darkness, subjects looked at a pulsed target that moved every 2 s from  $20^\circ$  right to straight ahead, and  $20^\circ$  left, for 1 min. We will refer to each consecutive period of right, center, and left fixations as a fixation sequence. The laser was pulsed (20 ms every second) so that we could direct the subject's gaze direction without visually suppressing nystagmus. Subjects were instructed to look in the direction where they last saw the flashed target and to attempt to keep looking in that direction until they saw a flashed target in a different position.

The goal of the acceleration trials was to produce a vestibular stimulus that would create a constant rotational velocity signal for a long period. The stimulus consisted of an initial velocity step, followed by a period of acceleration that increased slowly with time. We used estimated properties of the vestibular system (yaw time constant of 15 s and adaptation time constant of 150 s) to determine the required rotation profile to produce a constant velocity signal of  $100^\circ/\text{s}$ . (The existence of the adaptation time constant has been determined from studies of long-lasting vestibular stimulation (Leigh et al. 1981; Boumans et al. 1983; Furman et al. 1989). A plausible explanation of such a mechanism is to null small tonic imbalances between the left- and right-side canals.) The stimulus consisted of a 1-s acceleration ramp from  $100^\circ/\text{s}^2$  to  $107^\circ/\text{s}^2$ , followed by a lower acceleration ramp starting at  $7.3^\circ/\text{s}^2$  and increasing at  $0.04^\circ/\text{s}^2/\text{s}$  (Fig. 1). We approximated the initial acceleration period by a 1-s period of constant acceleration of  $100^\circ/\text{s}^2$ , and thereafter, the acceleration stepped to  $7.3^\circ/\text{s}^2$  and increased once a second by  $0.04^\circ/\text{s}^2$  (in other words, we approximated the continuous function by changing the acceleration once per second). The acceleration continued until the velocity reached  $400^\circ/\text{s}$ . After a delay to allow nystagmus to decline, we used the same acceleration sequence, but in the opposite direction to change the rotation speed from  $400^\circ/\text{s}$  to  $-400^\circ/\text{s}$ . Figure 1a, b shows the acceleration and velocity profiles. Figure 1c shows the expected response from a system consisting of dominant time constants of 10, 15, or 20 s, an adaptation time constant of 150 s, and a gain of 0.5. The initial period of a nearly constant response lasts approximately 38 s. When the acceleration stops, the vestibular response decays and reverses direction due to the adaptation component. During the experiment we monitored eye velocity and did not start the second acceleration period until nystagmus appeared to stop (typically about 4 min). The second acceleration period, during the change from  $400^\circ/\text{s}$  to  $-400^\circ/\text{s}$ , lasted



**Fig. 1** The *top* and *middle panels* show the stimulus used in the experiments, with head acceleration in **a** and velocity in **b**. The stimulus was an initial step of velocity to about  $100^\circ/\text{s}$ , followed by a slowly increasing acceleration (see inset of **a** that shows an expanded view of the initial 50 s, and “Methods” for details). After the rotation reached  $400^\circ/\text{s}$ , the acceleration stopped, and the velocity remained constant until the subject's nystagmus stopped. The acceleration profile was then inverted, so that there was an initial velocity step from  $400^\circ/\text{s}$  to  $300^\circ/\text{s}$ , followed by a slow change in acceleration until the chair reached  $-400^\circ/\text{s}$ . In **c**, the simulated responses to the stimulus from a system consisting of dominant time constants of 10, 15, or 20 s, and an adaptation time constant of 150 s, and a gain of 0.5 are shown. The velocity response is nearly constant during the acceleration phase, and then during the constant velocity phase, the response declines and reverses direction, before returning toward zero before the next acceleration phase

about 78 s. Finally, the chair decelerated to zero using the same profile as the initial acceleration.

The initial rotation direction was to the right in half the subjects and to the left in the other half.

## Analysis

Data were first filtered with a zero-phase distortion 200-Hz butterworth lowpass filter (butter.m and filtfilt.m, Mathworks). Only horizontal position and velocity were analyzed, and positive rotations are to the left. Since the results for the left and right eyes were similar, we only report the results of the movements of the right eye. Saccades were identified and removed with an interactive computer program that automatically detected saccades when velocity exceeded a threshold (typically  $20\text{--}30^\circ/\text{s}$ , depending upon the noise level) above the median eye velocity calculated over a 1-s window. The automatically marked saccades could be manually adjusted and blink artifacts removed. To ensure that saccadic components were not included in the slow phases, in particular the initial portion which can be

influenced by the more gradual end of saccades, the first 10 and final five samples of each slow phase were discarded.

Nystagmus slow phases shorter than 50 ms were discarded, and slow phases longer than 100 ms were split into two or more parts of at least 50 ms, to ensure, for unbiased statistical analysis, that roughly the same number of data points occurred in each gaze direction. For each of these slow phases (or parts thereof), we calculated the median position and velocity.

Estimates of the change of nystagmus velocity with eye position were made by fitting second-order equations with linear regression to the velocity-versus-position data:

$$\text{Velocity} = \beta_0 + \beta_1 H + \beta_2 H^2,$$

where  $\beta_0$  is the intercept (with units of  $^\circ/\text{s}$ ), or velocity at gaze straight ahead,  $\beta_1$  ( $\text{s}^{-1}$ ) is the slope parameter that describes how velocity changes with horizontal position,  $H$ , and  $\beta_2$  ( $1/^\circ\text{s}$ ) is the second-order component. Inspection of the data showed that velocity generally built up for 3 s following the onset of the change in acceleration and then was fairly constant. So, we discarded the first 3 s of data before further analysis. We did fits to the entire acceleration period (excluding the first 3 s), as well as doing fits to the first and second half of the period, and tested whether the fitted parameters changed using a dummy variable to code for the two time periods (Kleinbaum et al. 1988). Finally, we did linear fits to each fixation sequence, so we could analyze the change in nystagmus in more temporal detail. In order to determine when the slope during the acceleration period first became significantly different from control values, we used Bonferroni-corrected  $p$  values.

When combining data across different rotation directions, we first took the absolute value of the fitted intercepts.

## Results

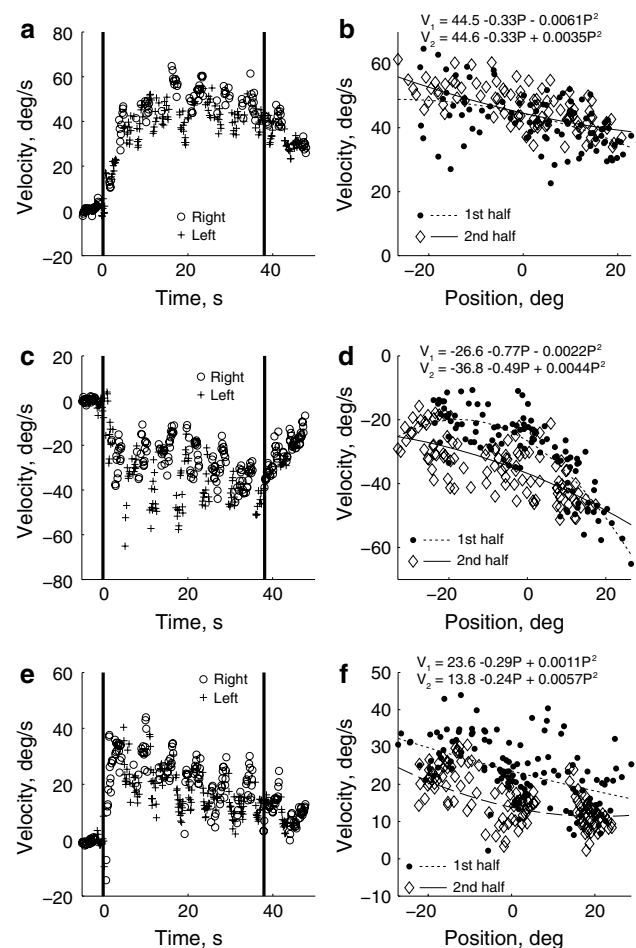
We first measured gaze holding prior to stimulation. The average best-fit, second-order parameters were  $-0.2^\circ/\text{s}$ ,  $-0.031 \text{ s}^{-1}$ , and  $3.7 \times 10^{-6} \text{ } 1/^\circ\text{s}$ . The average intercepts and second-order terms were not significantly different from zero ( $t$  test,  $ps > 0.3$ ), but the average slope term was less than 0 ( $t = 2.9$ ,  $p < 0.05$ ). A leaky velocity-to-position neural integrator with time constant  $\tau$  will produce velocity that varies with horizontal position  $H$  according to the following equation:

$$\text{Velocity} = -\frac{H}{\tau} + \text{bias}$$

where bias is the velocity produced by the vestibular stimulation. So, an integrator time constant can be inferred from the fitted equations by  $-1/\text{slope}$ . The average time constant was 32 s.

## Development of Alexander's law

Eye velocity increased rapidly in the first several seconds after the onset of acceleration. Figure 2 shows examples from three subjects (see also Online resource 1). For the subject in the top row, after the initial increase in eye velocity at the start, the velocity was fairly constant for the remainder of the acceleration period. The fitted second-order equations for the first and second halves are shown in Fig. 2b and are nearly identical, indicating that the eye velocity was very stable. For the subject shown in panels C and D, eye velocity increased from the first to the second halves, whereas



**Fig. 2** Example data, with different subjects shown in each row. The *left column* shows the eye velocity of individual slow phases plotted as a function of time, with different symbols to indicate whether the subject was looking left or right of straight ahead. *Vertical lines* mark the start and end of the acceleration period. The *right column* shows eye velocity of individual slow phases plotted against horizontal position for the acceleration period, excluding the first 3 s. *Different symbols* indicate when the data point was from the first or second half of the experiment. The best-fit, second-order equations for the first and second half of the data are shown at the *top* ( $V$  velocity, with the subscript indicating the first or second half,  $P$  is position)

**Table 1** The average parameters from the best-fit, second-order equations for the control and each acceleration period

Acceleration period	Intercept ( $^{\circ}/s$ )		Slope ( $s^{-1}$ )		Quadratic ( $1/^{\circ}s$ )	
	Mean	$\Delta$	Mean	$\Delta$	Mean	$\Delta$
Control	-0.245		-0.031*		$3.7 \times 10^{-6}$	
1st	30.39***	-0.41	-0.380***	-0.074	-0.0007	-0.0030
2nd	31.09***	-1.17	-0.331*	-0.058	-0.0049	-0.0037
3rd	33.90***	-2.28	-0.483**	0.095**	-0.0068	-0.0049

The column marked “ $\Delta$ ” provides the difference between the first and the second halves (2nd – 1st) of each acceleration period

*t* test results: \*\*\*  $p < 0.001$ , \*\*  $p < 0.01$ , \*  $p < 0.05$

eye velocity decreased over time for the subject in panels E and F.

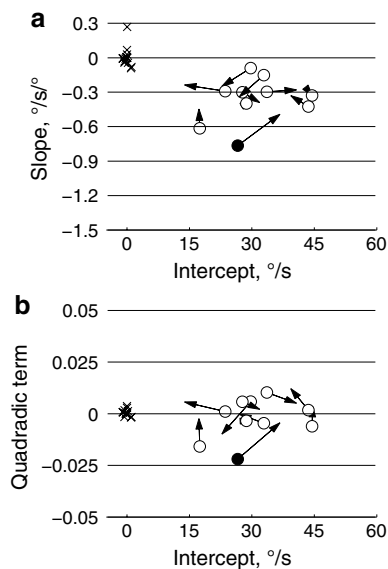
The second-order fits to the entire acceleration period found that while the average slope term was significantly different from zero ( $-0.38$ ,  $t = 9.6$ ,  $p < 0.001$ ), the average quadratic term was not ( $-0.001$ ,  $t = 0.3$ ,  $p = 0.76$ ) (Table 1). In addition, the slope term was significant in all 10 subjects, whereas the quadratic term was significant in only three.

Overall, there was little change in the best-fit, second-order equations between the first and second periods (Fig. 3). The average magnitudes of the intercepts were  $30.8^{\circ}/s$  and  $30.4^{\circ}/s$  for the first and second halves, respectively, and were not significantly different ( $t = 0.2$ ,  $p = 0.84$ ). Likewise, the

best-fit slopes ( $-0.366$  and  $-0.347$ ) were not significantly different ( $t = 0.4$ ,  $p = 0.68$ ), nor were the second-order terms different ( $0.0013$  and  $-0.0017$ ;  $t = 0.92$ ,  $p = 0.38$ ).

To analyze how nystagmus evolved over time in more detail, we did linear fits (since the second-order terms in the previous analysis were not significantly different from zero overall) to each fixation sequence (Fig. 4), including the 3 min after the acceleration in order to analyze the decay of nystagmus. For the first fixation sequence, six of the ten subjects showed slopes that were significantly different from control trials during the first fixation sequence (mean intercept =  $30^{\circ}/s$ , mean slope =  $-0.3$ ). The first significant slope occurred, on average, 10 s after the start of the acceleration. Eye velocity declined rapidly after the acceleration ended and then reversed direction (Fig. 4a). The average maximum reversal velocity (intercept) was  $-9^{\circ}/s$  and occurred 59 s after the end of the acceleration. The slopes declined rapidly, but did not reverse (Fig. 4b); rather, they declined to a value of about  $-0.1$  and then decayed with a time course similar to that of the intercept. Figure 4c shows an apparent relationship between the slope and the intercept, as higher intercepts tend to be associated with steeper slopes.

The results for the second and third acceleration periods were similar (see Table 1). The mean slopes were significantly different from control in all periods, whereas the average quadratic term was not. Recall that the second acceleration period was 78 s long, compared to 38 s for the first and third periods, which could have increased the ability to detect changes in the parameters over time. Nonetheless, the fitted parameters were very stable, with only a small reduction in the slope in the third acceleration period.

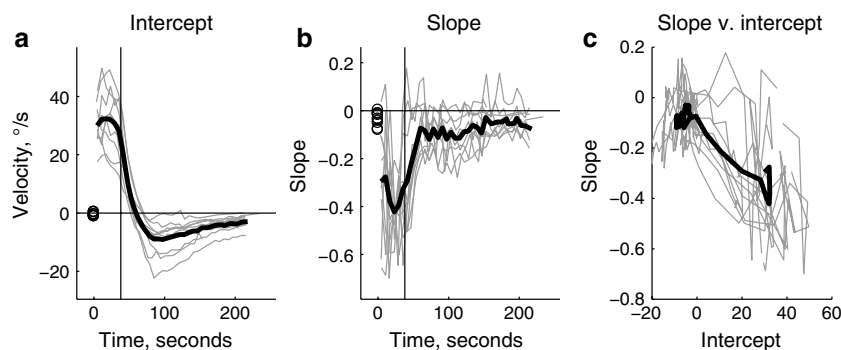


**Fig. 3** The parameters of the best-fit, second-order equations to velocity-versus-position data are shown for the first acceleration period. Panel **a** plots the slope versus the intercept, and **b** plots the quadratic term versus the intercept. Circles show the fits to the first half of the acceleration period, and the arrows end at the values for the second half of the acceleration period. Filled circles indicate the change in slope (**a**) or quadratic (**b**) terms were significant. The X's show control data

## Discussion

We found an eye position dependency of the slow phase of nystagmus during constant vestibular stimulation similar to Alexander's law. Like Robinson et al. (1984), we found it was mostly stable during the entire period of stimulation, as

**Fig. 4** The time course of linear fits to each fixation sequence. *Thin lines* are individual subjects, and the *thick black line* is the mean. *Circles* at time = 0 are control data. **a** Intercepts. **b** Slopes. **c** The slopes are plotted relative to the intercepts



the magnitude was similar in the first and second halves of the acceleration period. Alexander's law was also apparent in 6/10 subjects in the first fixation sequence and occurred on average 10 s after the onset of acceleration. Unlike the results of Robinson et al. (1984), however, the size of the effect was large and similar to what occurs in patients. Here, we found slopes of about  $-0.4$  for nystagmus velocities of  $30^\circ/\text{s}$ , which are comparable to our patient studies where we found slopes of about  $-0.3$  to  $-0.4$  for velocities around  $25^\circ/\text{s}$  (Hegemann et al. 2007; Bockisch and Hegemann 2008).

Robinson et al. (1984) concluded that the eye position dependency found during constant acceleration (natural stimulation, in the sense that normal push-pull stimulation pattern is maintained, albeit for an unusual duration) was different from that observed in patients and with caloric stimulation (non-reciprocal and therefore unnatural stimulation, because a change in vestibular input from one side is not accompanied by the opposite change from the other side), because (1) the magnitude was small and (2) it did not evolve over time. This led Robinson et al. to conclude that Alexander's law was an adaptive response, as it reduced eye velocity in some gaze directions, to non-reciprocal stimulation. We suggest this is incorrect for three reasons. First, the small magnitude was likely because the velocity and acceleration were lower than what we used (a  $30^\circ/\text{s}$  velocity step followed by  $2.1^\circ/\text{s}^2$ , compared to a  $107^\circ/\text{s}$  step followed by an acceleration ramp that began at  $7.1^\circ/\text{s}^2$ ), since the magnitude of Alexander's law increases with increasing nystagmus. Second, in their caloric stimulation study of three subjects, they report that the peak of Alexander's law was delayed, on average, 25 s from the peak of nystagmus velocity, and from this they concluded that Alexander's law needs 25 s of non-reciprocal stimulation to develop. However, in their data a clear eye position dependency is apparent before the peak nystagmus; the fact that the peak position dependency was delayed cannot be used to conclude that Alexander's law was not developing earlier. In our experiment, Alexander's law was found on average 10 s after the onset of stimulation. Third, in our recent study

with caloric stimulation, we observed Alexander's law with bilateral bithermal stimulation (cold on one side, warm on the other) (Bockisch et al. 2012). This stimulus preserves the push-pull pattern of natural stimulation and is further evidence against the Robinson et al.'s (1984) hypothesis.

Doslak (Doslak et al. 1979, 1982) proposed that Alexander's law occurs because of an eye position dependency within the VOR pathway. According to the model, whenever the difference between the right and left canal signals exceeds a threshold, an eye velocity signal is added that depends upon eye position. Our finding that Alexander's law occurs with constant vestibular stimulation, with very little change over time, supports the Doslak model. However, the Doslak model also predicts that the velocity-versus-position slope should be independent of nystagmus speed (above a threshold), but that is not the case in our study (Fig. 4c), nor with caloric stimulation (Bockisch et al. 2012). The model of Doslak et al. also predicts Alexander's law should occur with the normal VOR, yet it is not found with 0.5-Hz sinusoidal head rotations on a turntable (Robinson et al. 1984) or head impulses (Anagnostou et al. 2011; Anastasopoulos and Anagnostou 2012).

Jeffcoat et al. (2008) proposed a different account of Alexander's law, where the gain of extraocular motor neurons varies with position and whether the velocity inputs come from increased or decreased canal activity. This hypothesis was based on the findings that eye movements and abducens neuron responses to short duration auditory stimuli depend upon eye position (Zhou et al. 2004, 2007). Jeffcoat et al. (Jeffcoat et al. 2008) proposed that with decreased canal activity, the abducens neuron gain *decreases* with adducting eye position, thus producing Alexander's law in patients with vestibular lesions and unilateral cold caloric stimulation. With increased canal activity, abducens neuron gain *increases* with adducting eye position. This model thus predicts a reversed Alexander's law with unilateral warm caloric stimulation, which they reported (Jeffcoat et al. 2008). With normal, reciprocal stimulation of the canals, the gain changes with eye position cancel, producing a VOR that does not depend on eye position. Thus, this model does

not predict Alexander's law during constant acceleration protocols, as we observed here, nor with bilateral bithermal caloric stimulation (Bockisch et al. 2012).

Constant acceleration and caloric stimulation protocols that show Alexander's law produce very low-frequency stimulation, whereas the VOR studies that do not show Alexander's law use higher-frequency stimuli. Alexander's law then may be a consequence of the velocity-to-position neural integrator being insensitive to very low-frequency signals. One reason for this could be that natural head movements contain mainly high-frequency components. Another reason could be to make the integrator insensitive to small imbalances in the tonic stimulation from the left and right vestibular canals. While another mechanism to compensate for such imbalances exists [up-regulation of tonic inputs following peripheral lesion (Smith and Curthoys 1989)], this mechanism operates on a timescale of hours or days (Ris and Godaux 1998).

If Alexander's law is a consequence of low-frequency stimulation, then it is tempting to speculate on the role of the velocity-storage mechanism, which enhances the low-frequency canal response in order to correctly interpret linear acceleration signals from the otoliths (Laurens and Angelaki 2011). While the linear VOR is highly eye position dependent, to produce Alexander's law would require target distance to change with eye position, being nearer when in the fast-phase direction. The flashed targets in our setup were presented on a flat screen, with no distance difference for left and right targets. Thus, there is not an obvious functional connection between the velocity-storage mechanism and Alexander's law.

A different explanation of Alexander's Law in acute unilateral vestibular deficit has recently been proposed by Khojasteh et al. (2012). Due to the vestibular lesion and insufficient tonic activity on the ipsilesional primary afferents, the ipsilesional vestibular nucleus is silenced, while the contralesional vestibular nucleus becomes hyperactive (Smith and Curthoys 1989). Khojasteh et al. (2012) suggested that this asymmetry in the response of the bilateral vestibular nuclei reduces the linear operating range of the central VOR circuits, which perform the integration of velocity signals. The gain of the brainstem positive feedback loop thus becomes dependent on the merging neural activity, making the integration process dependent on eye movement signals. They hence propose that in the slow-phase direction (side of the lesion) integration of eye signals is insufficient (leaky), while in the fast-phase direction the integrator could become unstable. Khojasteh et al. (2012) further speculated that the persistent stimulation of the primary vestibular afferents by very low-frequency stimuli could in the same manner saturate the vestibular nucleus on one side, while pushing the other vestibular nucleus into inhibitory cutoff, thus producing

eye position-dependent integration similar to unilateral vestibular lesions.

Patients suffering from spontaneous nystagmus due to an acute vestibular tone asymmetry show velocity that varies with position in a nonlinear fashion (Hegemann et al. 2007; Bockisch and Hegemann 2008). We did not find similar effects here, or in our experiments with caloric stimulation (Bockisch et al. 2012). Perhaps, in patients there are adaptive mechanisms to suppress nystagmus which cause the nonlinear behavior, since these patients typically had nystagmus for several days before being measured. In their model of the velocity-to-position neural integrator, which was developed to describe congenital nystagmus, Optican and Zee (1984) proposed that eye position-dependent nonlinearities were necessary to account for changes in nystagmus waveforms with eye position that occur in these patients. Perhaps, modifications to such mechanisms require either more time than was available in the protocol used here (patients were typically measured hours or days after the onset of symptoms) or the presence of retinal slip information that was excluded in our experiments by performing them in the dark.

Clinicians often treat the presence of Alexander's law in spontaneous nystagmus as a sign of a peripheral vestibular lesion, though we suggest it is not conclusive. If Alexander's law is in fact a consequence of low-frequency velocity inputs to the velocity-to-position neural integrator, from any source, then Alexander's law ought to occur. One example of this is pursuit after-nystagmus (Marti et al. 2005). However, with other forms of nystagmus, such as infantile nystagmus syndrome, the Alexander's law mechanism might be invoked, but the variation in eye velocity with position would be difficult to detect due to the complex (and temporally unstable) velocity inputs.

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