PHYSICAL REVIEW B 97, 245416 (2018)

Editors' Suggestion

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Resonant electron-lattice cooling in graphene

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(Received 20 March 2018; revised manuscript received 28 April 2018; published 19 June 2018)

Controlling energy flows in solids through switchable electron-lattice cooling can grant access to a range of interesting and potentially useful energy transport phenomena. Here we discuss a tunable electron-lattice cooling mechanism arising in graphene due to phonon emission mediated by resonant scattering on defects in a crystal lattice, which displays an interesting analogy to the Purcell effect in optics. In that, the electron-phonon cooling rate is enhanced due to hot carrier trapping at resonant defects. Resonant dependence of this process on carrier energy translates into gate-tunable cooling rates, exhibiting strong enhancement of cooling that occurs when the carrier energy is aligned with the electron resonance of the defect.

DOI: 10.1103/PhysRevB.97.245416

In 1946, Purcell discovered that bringing the energies of atoms into alignment with resonances in optical cavities can dramatically enhance the rate of spontaneous emission [1]. One way of understanding the enhancement is provided by Fermi's golden rule, which mandates that the transition rate is proportional to the density of final states. The latter is enhanced in a cavity at resonance compared to a free-space density of states, providing the means to control the light-matter coupling [2,3]. Here we discuss an electron-phonon analog of the Purcell effect: resonant enhancement of electron-lattice cooling occurring when carrier energies align with electron resonances at defects. Because of Purcell-type enhancement of the density of electronic states at the defects, the on-resonance electrons can emit phonons more efficiently, enhancing the electron-lattice cooling rate and making it gate-tunable. Furthermore, resonant scattering opens up an additional cooling pathway due to the possibility of carrier trapping on localized defects. The latter process, as we will show, boosts phonon emission and electron-lattice cooling.

While these effects are completely generic, they become particularly important in graphene, a material in which energy relaxation pathways of nonequilibrium hot carriers are uniquely sensitive to minute amounts of disorder. In pristine graphene, electron-phonon scattering is suppressed and, as a result, the hot-electron cooling is quite slow [4,5]. The introduction of defects completely changes the situation, giving rise to several different cooling mechanisms that can occur depending on the microscopic properties of the defects as well as system parameters such as carrier density and temperature. Resonant defects with energies near the Dirac point play a special role as the electronic density of Dirac states is low at these energies. As a result, carrier trapping on the defects strongly impacts cooling and phonon emission, as illustrated in Fig. 1.

Previous works on disorder-assisted electron-phonon scattering considered so-called "supercollisions" in which the excess recoil momentum is being absorbed by the impurity whereas the energy is carried away by a thermal phonon [6–11].

This process, through phase-space-enhancement of electronphonon scattering, gives rise to disorder-assisted cooling. However, as this paper shows, it is not the only disorder-related cooling pathway. As we will see, resonant defects provide a fundamentally different cooling mechanism—phonon emission by an electron trapped by a defect—that is distinct from the enhancement of phonon phase space through momentumnonconserving scattering.

Graphene-based nanoscale thermoelectric devices are of wide interest due to the unique electrical and thermal properties of this material [12,13]. This work adds to this exciting field by providing a controllable mechanism of hot carrier cooling. There are two main approaches to low-dimensional nanoscale thermal engineering: phononics engineering [15] and hot carrier manipulation. In the field of graphene phononics, ideas such as gate tunability cooling [14] and defect engineering have been investigated [16,17]. Complementary to that, our work explores the mechanism of hot carrier resonant cooling by localized defects. Additional cooling pathways in nanodevices with on-demand spatial dependence through precision defect engineering are made possible by this physical framework.

Recently impurity-assisted electron-lattice cooling in graphene was imaged using the nanoscale thermometry scanning probe technique [18,19]. It was found that the dominant contribution to cooling arises from resonant scatterers with the energies of the resonances positioned near the Dirac point. It was conjectured that resonant scatterers mediate phonon emission and cooling through the process of trapping band carrier in a localized state (LS) as illustrated in Fig. 1. While this picture seems plausible, the study reported in Refs. [18,19] left a number of key questions unanswered, in particular the origin of the resonances and the extent to which resonant scattering can enhance the cooling rates. Below we present a microscopic picture of cooling due to phonon emission mediated by resonant scattering, and estimate the cooling rate by evaluating the electronic cooling cross section. The cooling rate is sharply enhanced when the Fermi energy

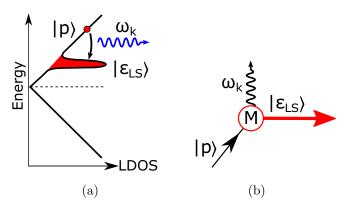


FIG. 1. (a) Schematics showing a hot electron of initial state $|\mathbf{p}\rangle$ being trapped by the impurity forming a resonant state $|\epsilon_{LS}\rangle$, emitting a phonon of energy $\hbar\omega_k$ in the process. (b) The same process shown as a Feynman diagram. The vertex represents the matrix element M in Eq. (12). Note that the outgoing state is the resonant state $|\epsilon_{LS}\rangle$.

is close to the resonance energy of one of the scatterers, turning off quickly when the Fermi level is detuned from the resonance energy. Disorder-assisted resonant cooling is found to dominate over the intrinsic contribution due to momentum-conserving electron-phonon processes. This, along with the ON/OFF switching behavior seen near the resonance, presents the novel possibility of gate-tunable cooling.

I. MODEL OF ELECTRONIC COOLING

Graphene is known to host a wide variety of atomic-scale defects that can act as resonant scatterers, which can trap electrons in quasibound states [20-23]. Ab initio and STM studies [24–26] have shown that quasibound states with energies near the Dirac point arise in a robust manner when adatoms or polar groups such as H, F, CH₃, or OH bind covalently to carbon atoms, transforming the trigonal sp^2 orbital to the tetrahedral sp^3 orbital. Each transformed C atom gives rise to a vacancy in the π band, producing a quasibound state localized near the defect. The energy of such a localized state depends on the adatom type, taking values $\epsilon_{LS} \sim 10-100$ meV, i.e., positioned in the direct vicinity of the Dirac point [24-26]. In transport, such defects act as resonant scatterers, with the scattering cross section exhibiting a sharp resonance at $\epsilon = \epsilon_{LS}$. In contrast, the defects having other symmetries (e.g., adatoms positioned between two C atoms or at a hexagon center) typically form resonances far away from the Dirac point.

Here we shall consider phonon emission by carriers in the presence of such resonant scatterers, assuming that the lattice is at a constant temperature of T_p , forming a thermal phonon bath. We show that the resonance in the local density of states gives rise to enhanced phonon emission in a manner similar to how spontaneous photon emission is enhanced by the optical cavity resonances in the Purcell effect. The Hamiltonian is given by a sum of the electron and phonon parts, and the electron-phonon interaction, $H = H_{\rm el} + H_{\rm ph} + H_{\rm el-ph}$, where

$$H_{\mathrm{ph}} = \sum_{\mathbf{k}} \omega_{\mathbf{k}} b_{\mathbf{k}}^{\dagger} b_{\mathbf{k}}, \quad H_{\mathrm{el-ph}} = \sum_{\mathbf{k},\mathbf{p}} g \sqrt{\omega_{\mathbf{k}}} b_{\mathbf{k}} a_{\mathbf{p}+\mathbf{k}}^{\dagger} a_{\mathbf{p}} + \mathrm{H.c.}$$

and the electron Hamiltonian $H_{\rm el}$, describing free carriers and their interaction with the defects, is discussed below. From the above Hamiltonian, we can calculate the energy dissipation rate through Fermi's golden rule as

$$P = \sum_{\mathbf{p},\mathbf{p}',\mathbf{k}} \omega_{\mathbf{k}} W_{\mathbf{p},\mathbf{p}'\mathbf{k}} (1 - n_{\mathbf{p}'}) n_{\mathbf{p}} (N_k + 1) \delta(\epsilon_{\mathbf{p}'} + \omega_{\mathbf{k}} - \epsilon_{\mathbf{p}})$$
$$- \sum_{\mathbf{p},\mathbf{p}',\mathbf{k}} \omega_{\mathbf{k}} W_{\mathbf{p}'\mathbf{k},\mathbf{p}} (1 - n_{\mathbf{p}}) n_{\mathbf{p}'} N_k \delta(\epsilon_{\mathbf{p}'} + \omega_{\mathbf{k}} - \epsilon_{\mathbf{p}}), \quad (2)$$

where $n_{\mathbf{p}}$, $n_{\mathbf{p}'}$, and N_k are Fermi and Bose distributions for electrons and phonons with momenta \mathbf{p} , \mathbf{p}' , and \mathbf{k} , and with energies $\epsilon_{\mathbf{p}} = \epsilon_p$, $\epsilon_{\mathbf{p}'} = \epsilon_{p'}$, and $\omega_{\mathbf{k}} = \omega_k$, respectively. The scattering cross section in Eq. (2) equals

$$W_{\mathbf{p},\mathbf{p}'\mathbf{k}} = W_{\mathbf{p}'\mathbf{k},\mathbf{p}} = \frac{2\pi}{\hbar} |M_{\mathbf{p},\mathbf{p}'}|^2,$$
 (3)

where an incoming electron $|\mathbf{p}\rangle$ is scattered into the outgoing state $|\mathbf{p}'\rangle$, emitting or absorbing a phonon with momentum $\mathbf{k} = \mathbf{p} - \mathbf{p}'$.

The matrix element $M_{\mathbf{p},\mathbf{p}'}$, describing phonon emission in the presence of a defect, can be written as a sum of three terms:

$$M_{\mathbf{p},\mathbf{p}'} = \langle \mathbf{p}' | M(k)G_0t + tG_0M(k) + tG_0M(k)G_0t | \mathbf{p} \rangle, \quad (4)$$

where t is the T-matrix for the defect, evaluated at the energies of the in and out states as discussed below, G_0 is the bare electronic Green's function, and

$$M(k) \equiv \langle \mathbf{p}', \mathbf{k} | H_{\text{el-ph}} | \mathbf{p} \rangle = g \sqrt{\omega_k} \delta(\mathbf{p} - \mathbf{p}' - \mathbf{k})$$
 (5)

is the bare electron-phonon scattering matrix element. The three terms in Eq. (4) correspond to resonant scattering at the defect before, after, and both before and after a phonon emission process. The overall process is illustrated in Fig. 1(b).

We will find that the contribution to the cooling rate due to resonant scattering, taken on-resonance, is large compared to the contribution from bare momentum-conserving electronphonon scattering in the absence of disorder. This comparison, which provides a justification for focusing on the disorderassisted elecron-phonon scattering processes, will be made after the resonance-enhanced cooling rate is evaluated.

The bare electron propagator is given by

$$G_0(\mathbf{p}, \epsilon) = \frac{1}{\epsilon - H_0(\mathbf{p}) + i0} \tag{6}$$

with the free-particle tight-binding Hamiltonian given by a 2×2 matrix in the A/B sublattice pseudospin basis

$$H_0 = \begin{pmatrix} 0 & t_h f(\mathbf{p}) \\ t_h f^*(\mathbf{p}) & 0 \end{pmatrix}, \quad f(\mathbf{p}) = \sum_{i=1}^3 e^{i\mathbf{p}\cdot\mathbf{e}_i}. \tag{7}$$

Here \mathbf{e}_i are vectors connecting neighboring C atoms and t_h is the nearest-neighbor hopping parameter.

II. T-MATRIX FOR RESONANT DEFECTS

To describe resonant scatterers, we introduce the diagonal on-site disorder potential $V(\mathbf{x}) = \sum_i V \frac{1}{2} (1 \pm \sigma_z) \delta(\mathbf{x} - \mathbf{x}_i)$ with the plus and minus signs corresponding to defects positioned on sites A or B, respectively. The resonant character of this disorder potential becomes prominent in the limit $V \gg W$, where $W \approx 6$ eV is the graphene bandwidth. This is

(1)

evident from the T-matrix, which describes the defect potential renormalized by multiple scattering processes. For a single defect, taken without loss of generality on an A site at $\mathbf{x} = \mathbf{0}$, the T-matrix equals

$$t(\epsilon) = \frac{\tilde{V}}{1 - \tilde{V} \sum_{\mathbf{p}} G_0(\epsilon, \mathbf{p})} = \frac{\pi v_F^2}{\epsilon \ln \frac{iW}{\epsilon} + \delta} \frac{1 + \sigma_z}{2}, \quad (8)$$

where $\tilde{V} = \frac{1}{2}(1+\sigma_z)V$ and $\delta = \pi v_F^2/V \ll W$. The T-matrix has a resonance centered at $\epsilon_{\rm LS} \approx -\delta/\ln(W/\delta)$, which corresponds to the energy of a localized state. The energy of the resonance $\epsilon_{\rm LS}$ is small, with δ parametrizing the detuning from the Dirac point.

When the defect concentration is low and the defect potential V is large compared to W, each defect hosts a single resonance state with energy ϵ_{LS} close to the Dirac point, broadened due to hybridization with the states in the Dirac continuum. For a strong defect potential $V \gg W$, the energy ϵ_{LS} is much smaller than the bandwidth W and it has an opposite sign to that of V. This resonance has a half-width of $\gamma \approx \pi \delta/[2 \ln(W/\delta)]$, and it is thus small when δ is small.

The contribution of the defect to the single-particle density of states is given by

$$\frac{1}{\pi} \operatorname{Im} t(\epsilon) = \frac{\pi v_F^2 |\epsilon|/2}{[\epsilon \ln(W/|\epsilon|) + \delta]^2 + (\pi \epsilon/2)^2},\tag{9}$$

where we used the identity $\ln(iW/\epsilon) = \ln(W/|\epsilon|) + i\pi \operatorname{sgn}(\epsilon)/2$. This expression can be viewed as the density of states of pristine graphene $\sim |\epsilon|$ modulated by a resonant energy dependence due to the defect. The peak in the energy dependence of $\operatorname{Im} t(\epsilon)$, positioned near the Dirac point, corresponds to the defect resonance state.

Next we proceed to calculate the cooling power. It will be seen that in realistic regimes the cooling power dependence on electron Fermi energy shows a peak that mimics the defect density of states, with a prefactor that depends on the electron and phonon energy distributions. Microscopically, there are two separate resonant processes. In one, an electron emits phonon after being trapped on the localized state at a defect. In this case, a resonant scatterer traps band electrons on the quasibound state found in the previous section, and the energy difference is released to phonons. In another process, a freely moving electron emits a phonon before or after being scattering by a resonant defect. In this case, due to breaking of translation symmetry by the presence of defects, momentum does not have to be conserved as the defects can absorb recoil momentum from the phonons, thus enlarging the available phase space for the outgoing states. These latter effect are described in Song et al. [7] for weak disorder potential. As we will see, in our case it provides a relatively small contribution to the cooling power in comparison to resonant cooling through the process involving electron trapping on the defect.

III. EVALUATION OF MATRIX ELEMENTS

To evaluate the cooling power, we need to evaluate the matrix element in Eq. (4). We will focus on the experimentally relevant regime of electron and phonon temperatures that are small compared to the resonance energy ϵ_{LS} and

width $\gamma = \pi \delta/[2 \ln(W/\delta)]$. In this case, since the change of electron energy is small compared to $\epsilon_{\rm LS}$ and γ , the process is quasielastic. Also, at not too low temperatures, the phonon momentum values **k** are typically large compared to electron in and out momentum values **p** and **p'**, which are of order k_F . This allows us to approximate $G_0(\epsilon, p) \sim \pm 1/\sigma v k$. The first two terms of Eq. (4) then combine to give a commutator

$$-M(k)t(\epsilon)\frac{[\sigma \cdot \mathbf{k}, \sigma_3]}{2k^2} = M(k)t(\epsilon)\frac{i\sigma \times \mathbf{k}}{vk^2}.$$
 (10)

Here $M(k) = g\sqrt{\omega_k}$ is the bare electron-phonon interaction matrix element.

The third term in Eq. (4) can be evaluated by integrating the product of two Green's functions over internal electron momenta $k < q < k_0 = W/v_F$, giving

$$tG_0 M_0 G_0 t \approx \frac{M(k)}{2\pi v_F^2} \frac{1 + \sigma_3}{2} t(\epsilon') t(\epsilon) \int_k^{k_0} \frac{dq}{q}$$

$$= \frac{M(k)}{2\pi v_F^2} \ln \frac{W}{v_F k} \frac{1 + \sigma_3}{2} t(\epsilon') t(\epsilon). \tag{11}$$

Summing the three terms in Eq. (4) gives

$$M_{\mathbf{p},\mathbf{p}'} = M(k) \frac{i\sigma \times \mathbf{k}}{v_F k^2} t(\epsilon) + \frac{M(k)}{2\pi v_F^2} \ln \frac{k_0}{k} \frac{1 + \sigma_3}{2} t(\epsilon') t(\epsilon).$$
(12)

The two contributions in Eq. (12) can be compared directly by ignoring the matrix structure. Since the process is quasielastic, the difference between ϵ and ϵ' is inessential and the second term, which represents resonant trapping, dominates over the first term.

To better understand the competition between the two terms in Eq. (12), we consider their ratio

$$\frac{M_1}{M_2} \approx \frac{2s}{v_F} \frac{\epsilon \ln \frac{iW}{\epsilon} + \delta}{k_B T \ln \frac{k_0}{k}},\tag{13}$$

where s is the acoustic sound velocity $s \approx 2 \times 10^4$ m/s. Since the velocity ratio s/v is quite small, the second term in Eq. (12) will indeed dominate for the energies near resonance, $\mu \sim \epsilon_{\rm LS}$, and at not too low temperatures. However, a different behavior is expected for energies away from the resonance, since the second term falls off faster than the first term $(1/\epsilon^2$ versus $1/\epsilon$). As a result, the first term can win at large enough ϵ . For a crude estimate, taking the detuning from resonance on the order of $\epsilon_{\rm LS}$ we see that the first term becomes relevant when $k_BT \gtrsim (s/v_F)\epsilon_{\rm LS}$. Taking $\epsilon_{\rm LS} \sim 30$ meV gives T > 5 K, which is close to the measurement temperature in [18,19]. This analysis indicates that the second term dominates at resonance, whereas the first term dominates away from resonance.

IV. COOLING POWER

Next we show that the resonant energy dependence of phonon emission translates into a resonant dependence of the cooling rate as a function of carrier doping. After plugging the matrix element given in Eq. (12) into the expression for the cooling power, Eq. (2), and averaging over \mathbf{p} and \mathbf{p}' angles, we find that the contributions of the first and second terms

separate whereas the cross terms vanish under trace. Therefore, the two terms in Eq. (12) give independent contributions to the cooling power. These contributions describe the two distinct processes discussed above. In the first case, phonon is emitted by a freely moving electron before or after resonant scattering. In the second case, phonon is emitted by an electron which is trapped on a defect.

To evaluate the second contribution, which, according to Eq. (13), is expected to dominate over the first contribution, we use the identity $\sum_{\mathbf{p},\mathbf{p}'} = N \int d\epsilon \ d\epsilon' \ v(\epsilon)v(\epsilon')$, where $v(\epsilon)$ is the density of states per spin per valley and N=4 is the spin and valley degeneracy, assuming unit area. The energy conservation δ function can be used to evaluate one of the integrals, while the other integral can be evaluated by using the quasielastic approximation: $\int_{\infty}^{\infty} d\epsilon \ g(\epsilon)[n(\epsilon) - n(\epsilon - \omega)] \approx -g(\mu)\omega$, where $g(\epsilon)$ is an arbitrary smooth function of ϵ , and the identity $n(\epsilon)[1 - n(\epsilon - \omega)] = N_{\omega}^{e}[n(\epsilon - \omega) - n(\epsilon)]$, with N_{ω}^{e} being the Bose function evaluated at the electronic temperature. The final integral over ω_{k} is of the form

$$\int_{0}^{\infty} d\omega \,\omega^{4} \left(N_{\omega}^{e} - N_{\omega}^{p} \right) = 24 \zeta(5) k_{B}^{5} \left(T_{e}^{5} - T_{p}^{5} \right), \tag{14}$$

where N_{ω}^{p} is the Bose function evaluated at the lattice temperature. Putting everything together, we arrive at

$$P_2(\mu) = A(\mu)k_B^5 \left(T_e^5 - T_p^5\right) \tag{15}$$

for the cooling power per defect. Here μ is the Fermi energy and

$$A(\mu) = \frac{48\zeta(5)}{\pi^2} \frac{D^2}{\hbar^3 \rho s^4} \frac{(\pi/2)^4 \mu^2 \ln^2 \frac{k_0}{k_p}}{\left[\left(\mu \ln \frac{W}{|\mu|} + \delta \right)^2 + \frac{\pi^2}{4} \mu^2 \right]^2}, \quad (16)$$

where $k_p \approx k_B T_e/s$ is the typical momentum of an emitted phonon, and we used the relation between the electron-phonon coupling constant and the graphene deformation potential $g^2 = D^2/2\rho s^2$, with $D \approx 50$ eV, and ρ is the mass density of the graphene sheet. The quantity $P_2(\mu)$ vanishes in equilibrium as a result of detailed balance, but it is nonzero when the system is driven out of equilibrium, as one would expect. For a numerical estimate we use the value $D^2/(\hbar^2 \rho s^2 v_F^2) = 1.86 \times 10^{19} J^{-1}$. After scaling the Fermi energy by 1 meV and temperature by 1 K, we evaluate the numerical factors to obtain

$$P_2(\mu) = \frac{\mu^2 \ln^2 \frac{k_0}{k_p} (T_e^5 - T_p^5) [1 \text{ meV}]^2}{\left[\left(\mu \ln \frac{W}{|\mu|} + \delta \right)^2 + \frac{\pi^2}{4} \mu^2 \right]^2 [1 \text{ K}]^5} \times 260 \text{ fW}. \quad (17)$$

This contribution peaks near the resonance energy, falling off as $1/\mu^2$ at large detuning. Here and below we explicitly show the cooling power μ dependence, which is sometimes referred to as the *cooling power spectrum* [19].

The contribution of the first term in Eq. (12) can be evaluated in a similar manner, giving [6]

$$P_1(\mu) = 9.62 \frac{g^2 k_B^3 (T_e^3 - T_p^3)}{2\hbar^3 v_F^2} v^2(\mu) |t(\mu)|^2.$$
 (18)

where $v(\mu) = |\mu|/2\pi \hbar^2 v_F^2$ is the density of states. After scaling the Fermi energy by 1 meV and temperature by 1 K,

this expression becomes

$$P_1(\mu) = \frac{\mu^2 (T_e^3 - T_p^3) [1 \text{ K}^{-3}]}{\left(\mu \ln \frac{W}{|\mu|} + \delta\right)^2 + \frac{\pi^2}{4} \mu^2} \times 0.28 \text{ fW}.$$
 (19)

The total cooling rate per defect is then given by $P_{\text{tot}}(\mu) = P_1(\mu) + P_2(\mu)$.

It is instructive to compare the cooling rates due to resonant scattering with the intrinsic contribution of pristine graphene [4,5]. The cooling power per unit area due to momentum-conserving processes can be written as

$$P_0(\mu) = N \nu^2 \sum_{\theta_{\mathbf{p}}, \theta_{\mathbf{p}}'} \frac{2\pi}{\hbar} g^2 \omega_k |\langle \mathbf{p}' | \mathbf{p} \rangle|^2 \left(N_{\omega_k}^e - N_{\omega_k}^p \right) \omega_k^2$$
 (20)

with the phonon energy $\omega_k = \hbar s |\mathbf{p} - \mathbf{p}'|$ and the coherence factor $|\langle \mathbf{p}'|\mathbf{p}\rangle|^2 = \cos^2(\theta_{\mathbf{p},\mathbf{p}'}/2)$. Here $\sum_{\theta_{\mathbf{p}},\theta'_{\mathbf{p}}}$ denotes averaging over the Fermi surface through $\oint \oint \frac{d\theta_{\mathbf{p}}d\theta'_{\mathbf{p}}}{(2\pi)^2}$. We parametrize

$$|\mathbf{p} - \mathbf{p}'| = 2k_F x, \quad 0 < x < 1.$$
 (21)

Writing $|\langle \mathbf{p}'|\mathbf{p}\rangle|^2 = 1 - x^2$ and $d\theta_{\mathbf{p},\mathbf{p}'} = \frac{2dx}{\sqrt{1-x^2}}$, we can express the cooling power as

$$P_0(\mu) = Nv^2 \frac{2}{\pi} \int_0^1 dx \sqrt{1 - x^2} \frac{2\pi}{\hbar} g^2 \left(N_{\omega_k}^e - N_{\omega_k}^p \right) \omega_k^3, \tag{22}$$

where $\omega_k = 2sxk_F$.

This expression behaves differently depending on whether the temperature T is greater or smaller than the Bloch-Gruneisen temperature $T_{\rm BG} = \hbar s k_F$. For $T \gg T_{\rm BG}$ we can approximate the Bose distribution as $N_{\omega_k} \approx \frac{T}{\omega_k}$. Using the identity $\int_0^1 dx \, x^2 \sqrt{1-x^2} = \frac{1}{4} \Gamma^2(3/2) = \frac{\pi}{16}$, we obtain

$$P_0(\mu) = B(\mu)k_B(T_e - T_p),$$
 (23)

with $B(\mu) = \pi N \hbar g^2 v^2(\mu) k_F^2 s^2$. The numerical factors can be evaluated to give

$$P_0(\mu) = 9.2 \times 10^{-3} \frac{(T_e - T_p)\mu^4}{[1 \text{ K}][1 \text{ meV}]^4} \text{ fW } \mu\text{m}^{-2}.$$
 (24)

In the limit $T \ll T_{\rm BG}$ the integral over x, which is dominated by $x \ll 1$, can be estimated as

$$P_{0}(\mu) = Nv^{2} \frac{2}{\pi} \int_{0}^{\infty} dx \frac{2\pi}{\hbar} g^{2} \left(N_{\omega_{k}}^{e} - N_{\omega_{k}}^{p}\right) \omega_{k}^{3}$$

$$= 4Nv^{2} g^{2} \frac{3\zeta(4)}{\hbar^{2} s k_{F}} k_{B}^{4} \left(T_{e}^{4} - T_{p}^{4}\right)$$

$$= 3.0 \times \frac{\left(T_{e}^{4} - T_{p}^{4}\right) |\mu|}{[1 \text{ K}^{4}][1 \text{ meV}]} \text{ fW } \mu\text{m}^{-2}. \tag{25}$$

To compare $P_0(\mu)$ to the resonant scattering contribution, Eq. (17), we have to consider the physical measurement process. In such a measurement, the tip picks up the thermal signal from a sensing region with area A_s , and thus the cooling power contribution from P_0 is given by $A_s P_0$. With the experimentally realistic value of $A_s = 100 \times 100$ nm², and assuming that there is only one defect in such a region,

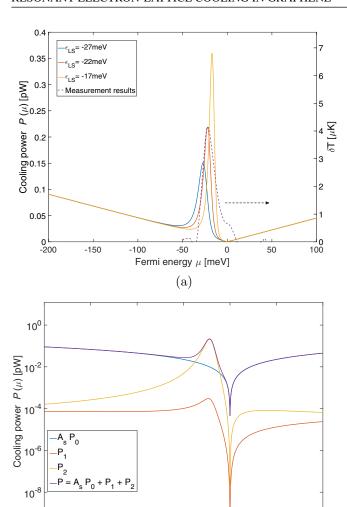


FIG. 2. A plot of the cooling power, in the presence of resonant scatterers vs Fermi energy for several values of the scatterer energy $\epsilon_{\rm LS}$ [Eqs. (26) and (17)]. Local temperature change [Eq. (29)], which is proportional to the cooling power, is shown on the right axis. The curves are sharply peaked on resonance, falling off rapidly away from resonance. The purple dashed line shows the experimental curve from [19], where peaks in cooling power due to resonant scatterers were observed near $\epsilon \approx -22$ meV. The intrinsic contribution [Eq. (24)] vanishes at the Dirac point and remains low, compared to the peaks, throughout the range of Fermi energies plotted. (b) Semilog plot showing the relative contributions of P_0 , P_1 , and P_2 for $\epsilon_{\rm LS} = -22$ meV. P_1 is small throughout the range of μ .

Fermi energy μ [meV]

(b)

we construct the quantity

-200

-150

-100

$$P(\mu) = A_s P_0(\mu) + P_1(\mu) + P_2(\mu). \tag{26}$$

50

100

We plot the cooling power Eq. (26) in Fig. 2(a), for three different values of ϵ_{LS} , and with the parameters $\ln(k_0/k_p) = 5.6$, $T_e = 4.25$ K, $T_p = 4.2$ K. The sharp peaks near ϵ_{LS} come from the contribution of P_2 , while P_1 affects the tails of the peak, as can be seen in Fig. 2(b). The intrinsic contribution P_0 is smaller than that of the defects at all energies shown in Fig. 2(a). As a result, the resonant peak in the cooling rate due to the defects dominates near charge neutrality.

V. COMPARISON TO EXPERIMENT

To make a direct comparison with the measurement results reported in Ref. [19], which employ a nanoscale probe to detect local changes in temperature, we convert the cooling power to local temperature change as follows. We assume that the power dissipated at the defect generates phonons which then carry heat flux radially outward. Since the graphene monolayer is encapsulated by hBN, we assume that the heat flux is generated in the entire graphene/hBN stack rather than just the graphene monolayer. We assume that the phonons propagate ballistically in the individual layers, and also make transitions between different layers due to scattering at interfaces and disorder, resulting in momentum relaxation at significantly shorter length scales than those for energy relaxation. The heat flux due to this phonon flow can thus be modeled by a 2D heat conduction equation $\mathbf{j} = -\kappa \nabla T$, where \mathbf{j} is the radial heat flux and κ is the 2D conductivity of the graphene/hBN system. Substituting the continuity equation for the heat flux $\nabla \cdot \mathbf{j} = P(\mu)\delta(\mathbf{r})$, with the defect taken to be at the origin, into the heat equation, we obtain

$$\nabla^2 \delta T(\mathbf{r}) = -\frac{P(\mu)}{\kappa} \delta(\mathbf{r}). \tag{27}$$

The local temperature change of the graphene/hBN system is

$$\delta T(r) = \frac{P(\mu)}{2\pi\kappa} \log \frac{L}{r},\tag{28}$$

where L is the distance to the heat reservoir for which $\delta T=0$, which is of order the distance to the system edge, and a is the thickness of the graphene/hBN stack. The thermal conductivity κ can be written as $\kappa=\frac{1}{2}sc_p'l_{\rm mfp}$, where c_p' is the specificheat capacity of the graphene/hBN system, and $l_{\rm mfp}$ is the momentum relaxation mean free path of the phonons. If we denote $c_p=9\zeta(3)k_B^3T_p^2/(\pi s^2)$ as the specific-heat capacity of the monolayer graphene, we can define the dimensionless ratio $Z\equiv c_p'/c_p$ to account for the contribution from the hBN layers. In the limit where the phonon modes of the different atomic layers are decoupled, Z is equal to the number of atomic layers. A typical value of r would be of order $l_{\rm mfp}$, and we assume $l_{\rm mfp}\sim 2\pi\hbar s/k_BT_p$ to be of the scale of the phonon thermal wavelength. With these assumptions, we obtain

$$\delta T_p = \frac{\hbar}{18\pi\zeta(3)Z} \frac{P(\mu)}{k_B^2 T_p} \log \frac{L}{l_{\text{mfp}}}.$$
 (29)

The experimental curve from [19] is plotted in Fig. 2(a) for comparison, with the temperature axis shown on the right. We find that the data are consistent with the theoretical prediction for $\epsilon_{\rm LS}\approx-22\,$ meV if we choose $Z\approx151\,$ for $L\approx1\,$ $\mu{\rm m}.$ Since the thickness of the graphene/hBN system is about 50 nm, which corresponds to about 150 atomic layers, this value of Z is physically reasonable. We also note that $\epsilon_{\rm LS}\approx-22\,$ meV agrees with the energy of a defect formed by a hydrogen adatom [18]. This highlights the use of resonance cooling as a way to identify the nature of a defect.

VI. CONCLUSIONS

In conclusion, we have shown that resonant defects result in resonant electron-lattice cooling phenomena. The underlying

physics of these processes is distinct from that considered before, which was based on an enhancement of phonon phase space in electron-phonon scattering. The sharp peak in $P(\mu)$ near ϵ_{LS} enables the switching of electron cooling ON and OFF through precise tuning of the Fermi energy. In direct analogy with how the Purcell effect is used to control photon emission in optics, resonantly enhanced phonon emission, occurring around the localized defects, can be used to control cooling. One can envision the design of specific cooling pathways and, through defect engineering, the development of new approaches to control heat flow in nanosystems.

Note added. It has come to our attention during the review process that Ref. [27] has come to similar conclusions.

ACKNOWLEDGMENTS

J.F.K. would like to acknowledge financial support from the Singapore A*STAR NSS program. E.Z. acknowledges the support by the Minerva Foundation with funding from the Federal German Ministry of Education and Research. L.S.L. and E.Z. acknowledge the support of the MIT International Science and Technology Initiative through MIT-Israel Seed Fund.

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