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1 **Surface to sewer flow exchange through circular inlets during urban**  
2 **flood conditions**

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19

20 **ABSTRACT**

21 Accurately quantifying the capacity of sewer inlets (such as manhole lids and  
22 gullies) to transfer water is important for many hydraulic flood modelling tools.

23 The large range of inlet types and grate designs used in practice makes the  
24 representation of flow through and around such inlets challenging. This study uses  
25 a physical scale model to quantify flow conditions through a circular inlet during  
26 shallow steady state surface flow conditions. Ten different inlet grate designs have

27 been tested over a range of surface flow depths. The resulting datasets have been  
28 used (i) to quantify weir and orifice discharge coefficients for commonly used  
29 flood modelling surface–sewer linking equations; (ii) to validate a 2D finite  
30 difference model in terms of simulated water depths around the inlet. Calibrated  
31 weir and orifice coefficients were observed to be in the range 0.115–0.372 and  
32 0.349–2.038, respectively, and a relationship with grate geometrical parameters  
33 was observed. The results show an agreement between experimentally observed  
34 and numerically modelled flow depths but with larger discrepancies at higher flow  
35 exchange rates. Despite some discrepancies, the results provide improved  
36 confidence regarding the reliability of the numerical method to model surface to  
37 sewer flow under steady state hydraulic conditions.

38 **Key words** | experimental modelling, numerical modelling, surface to  
39 sewer flow exchange, urban flooding, discharge coefficients

## 40 **INTRODUCTION**

41 Current climatic trends mean that the frequency and magnitude of urban  
42 flooding events is forecast to increase in the future (Hammond et al. 2015) leading to  
43 increased damage in terms of loss of business, livelihoods plus increased inconvenience  
44 for citizens (Ten Veldhuis & Clemens 2010). These potential impacts underline the  
45 importance of accurate modelling tools to determine flow paths within and between  
46 overland surfaces and sewer/drainage systems. Existing urban flood models commonly  
47 utilise the 1D Saint-Venant and 2D Shallow Water Equations (SWE) to calculate flows  
48 within sewer pipes and on the surface (overland flow) (Martins et al. 2017b). However,  
49 modelers are also faced with the concern of how to correctly reproduce the hydraulic  
50 behaviour around and within complex and variable hydraulic structures such as  
51 manholes and gullies which are used to connect the surface system to the sewer system.  
52 Unless the inlet is blocked or the sewer is surcharged, these structures allow water to be  
53 drained from the surface. An inaccurate representation of inlet capacity can lead to  
54 incorrect prediction of flow volumes, velocities and depths on the surface (Xia et al.  
55 2017), as well as in the sewer pipes. Due to their geometrical complexity such linking  
56 structures are conventionally represented using weir and orifice equations within urban  
57 flood models (Djordjevic´ et al. 2005; Chen et al. 2007; Leandro et al. 2009; Martins et

58 al. 2017a). However, due to a paucity of datasets, the robust calibration and validation  
59 of such linking methodologies is lacking. In particular, the determination of appropriate  
60 discharge coefficients for such linking equations over a range of hydraulic conditions  
61 and inlet types is required. Experimental studies investigating surface–sewer flow  
62 interaction via gullies and manholes are scarce (Martins et al. 2014). Larson (1947)  
63 identified inlet width and the efficiency of the inlet opening as characteristics of  
64 primary importance to determine inlet capacity; Li et al. (1951, 1954) experimentally  
65 investigated the effectiveness of some grate inlets in transferring flow from surface to  
66 sewer by treating the flow bypassing the grate as separate portions, and Guo (2000a,  
67 2000b) and Almedej & Houghtalen (2003), proposed different modifications to grate  
68 inlet design. Gómez & Russo (2009) investigated the hydraulic efficiency of transverse  
69 grates within gully systems proposing new mathematical expressions to define the  
70 hydraulic efficiency. Gómez & Russo (2011a) studied the hydraulic behaviour of inlet  
71 grates in urban catchments during storm events and Gómez et al. (2011b) presented an  
72 empirical relationship to obtain the hydraulic efficiency as a function of inlet and street  
73 flow characteristics. In further work, Gómez et al. (2013) investigated the hydraulic  
74 efficiency reduction as a result of partially clogged grate inlets. More recently, Rubinato  
75 et al. (2017a) experimentally validated the ability of weir/orifice linking equations to  
76 represent steady flow exchange through a scaled open manhole. However, the  
77 performance was dependent on the calibration of the discharge coefficients as well as a  
78 robust characterisation of the flow within the sewer and flow depth on the surface such  
79 that the hydraulic head difference between surface and sewer flows could be accurately  
80 determined. An accurate representation of flow exchange is therefore also dependent on  
81 correctly modelling of flow conditions (hydraulic head) in the vicinity of the inlet  
82 structure. Literature published to date lacks repeatable tests of different grate inlets  
83 under controlled conditions and an integration of results into modelling tools.  
84 Numerical studies of flows around gullies and manholes are limited due to a lack of  
85 experimental data as well as long computational times when simulating complex 3D  
86 flows (Leandro et al. 2014). However, some studies have been conducted: Lopes et al.  
87 (2015) analysed experimental results from a surcharging jet arising from the reverse  
88 flow out of a manhole after the sewer system became pressurised; Djordjevic´ et al.  
89 (2013) focused on surface recirculation zones formed downstream of gullies; both  
90 studies have used experimental data to model flow patterns inside gullies and manholes  
91 using CFD; Rubinato et al. (2016) studied flow depths around an open circular manhole

92 under drainage conditions and validated a 2D finite difference model. Martins et al.  
93 (2017a) validated two finite volume (FV) flood models in the case where horizontal  
94 floodplain flow is affected by sewer surcharge flow via a manhole demonstrating that  
95 the shock capturing FV-based flood models are applicable tools to model localised  
96 sewer-to-floodplain flow interaction. However, no studies to date have looked  
97 specifically at the influence of different grate cover designs/geometries on flow  
98 exchange capacity, flow conditions around the inlet and the ability of 2D modelling  
99 tools to replicate depths around the inlet over a range of flows. The objective of this  
100 work is to use a physical scale model to collect an extensive series of experimental  
101 datasets describing surface to sewer flow exchange through a circular inlet under steady  
102 state conditions through ten different inlet grate configurations. The datasets are used to  
103 (i) determine appropriate weir/orifice discharge coefficients applicable to describe  
104 exchange flows and (ii) to validate the ability of a calibrated 2D numerical finite  
105 difference method (FDM) to describe observed surface flow depths in the vicinity of the  
106 inlet structure.

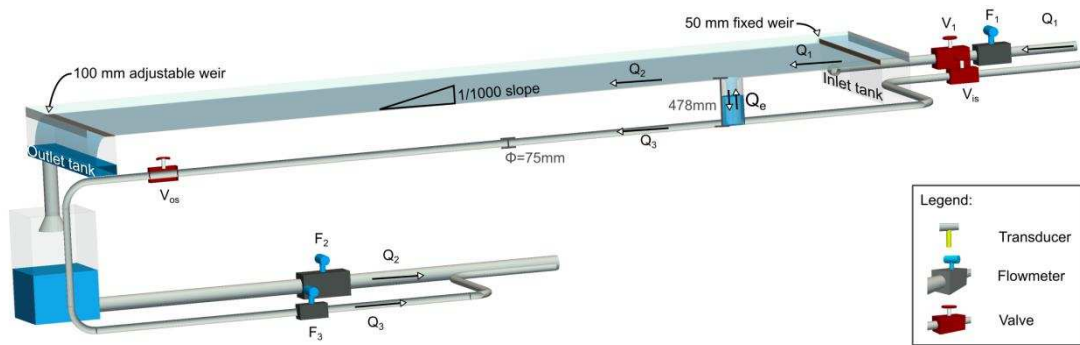
## 107 **METHODOLOGY**

108 This section presents (i) the experimental facility used to collect the data, (ii) hydraulic  
109 conditions for the tests conducted, (iii) a detailed procedure of the methods used to  
110 estimate discharge coefficients of the linking equations and (iv) a description of the  
111 numerical flood model utilised.

### 112 **Experimental model**

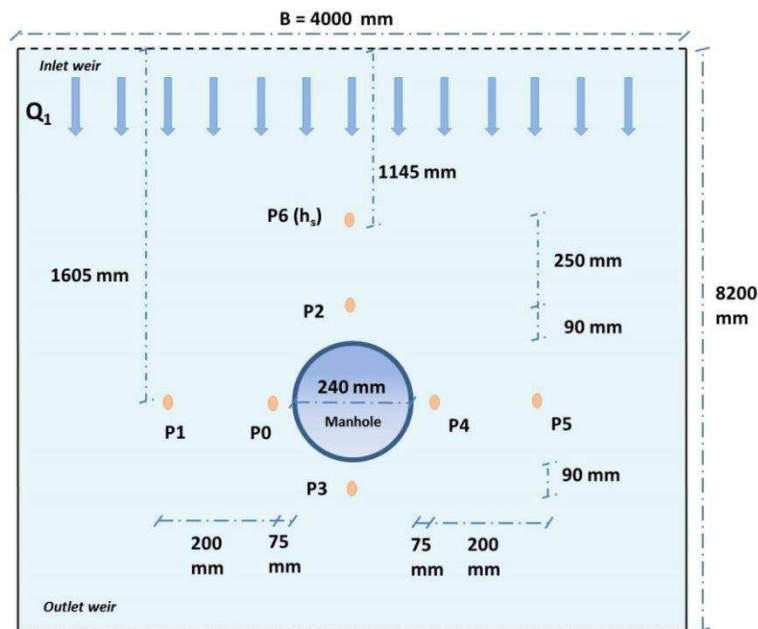
113 The experimental set-up utilised (Figure 1) was assembled at the water laboratory of the  
114 University of Sheffield (UK) (Rubinato 2015). It consists of a scaled model of an urban  
115 drainage system/floodplain linked via a manhole shaft. The floodplain surface (4 m,  
116 width, by 8.2 m, length) has a longitudinal slope of 1/1000. The urban drainage system  
117 is made from horizontal acrylic pipes directly beneath the surface (inner diameter =  
118 0.075 m). One circular acrylic shaft (representing a manhole) with 0.240 m inner  
119 diameter and 0.478 m height connects the surface to the pipes. The facility is equipped  
120 with a SCADA system (Supervision, Control and Data Acquisition) through Labview™  
121 software that permits the setup and monitoring of flow rates within the surface and  
122 sewer systems independently. A pumping system in a closed circuit supplies water

123 within the facility. The inlet pipes ( $V_1$ ,  $V_{is}$ ) are fitted with electronic control valves  
 124 operated via Labview™ software. The surface downstream outlet is a free outfall which  
 125 contains an adjustable height weir.



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127 **Figure 1** | Scheme of the experimental facility (Rubinato et al. 2017b).



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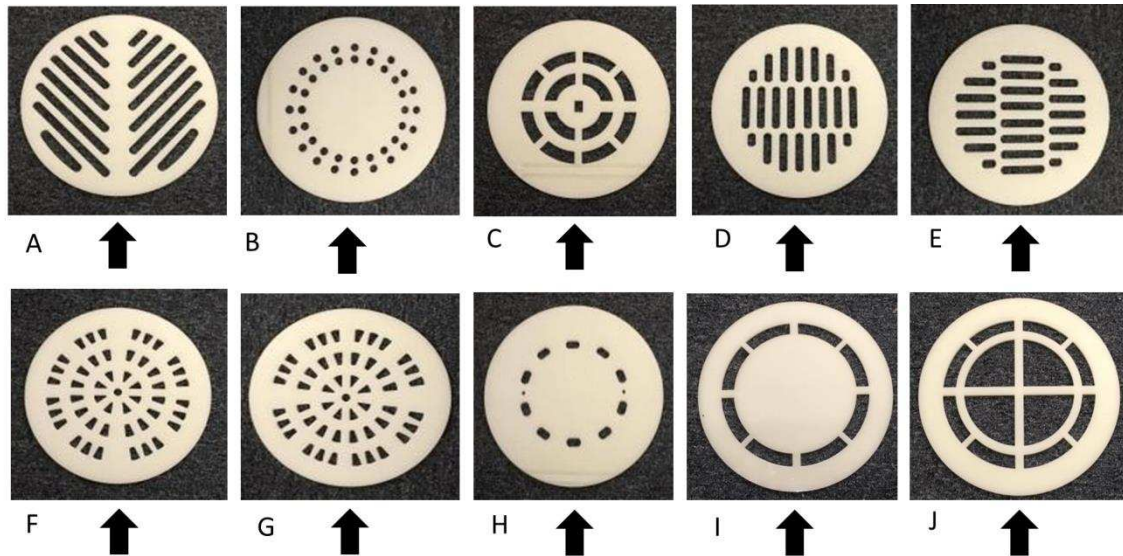
129 **Figure 2** | Location of the pressure transducer measurement points around the surface to  
 130 sewer drainage inlet (not to scale).

131 Calibrated electro-magnetic (MAG) flow meters ( $F_1$ , inlet floodplain;  $F_2$ , outlet  
 132 floodplain;  $F_3$  outlet sewer) were installed in the upstream and downstream pipes in  
 133 order to measure the surface system inflow ( $Q_1$ ) and surface and sewer outflows ( $Q_2$ ,  
 134  $Q_3$ ) and calculate the steady state drainage rate through the surface to sewer inlet ( $Q_e$ ).  
 135 Each flow meter was independently verified against a laboratory measurement tank. For  
 136 the tests reported here, the sewer inflow was not used (sewer inflow = 0) and all flow

137 therefore entered the facility via the surface inlet weir ( $Q_1$ ). Drainage flow passed via  
 138 the drainage inlet to the sewer outlet ( $Q_e = Q_3$ ), with the remaining flow passing over  
 139 the facility to downstream outlet weir ( $Q_2$ ). Flow depth on the floodplain was measured  
 140 by a series of pressure sensors (of type GEMS series 5000) fitted at various locations  
 141 around the inlet (Figure 2) (with an accuracy of  $\pm 0.109$  mm for the range of water depth  
 142 0–100 mm). Ten different grate types were constructed from acrylic using a laser cutter  
 143 and installed within the drainage structure and tested under steady state conditions in  
 144 order to obtain flow depth vs drainage discharge ( $Q_e$ ) relationships for each grate type.  
 145 The grate opening types were selected based on common types used in different  
 146 countries, and are presented in Figure 3. For each grate opening type the total area of  
 147 empty space ( $A_e$ ) and total effective edge perimeter length ( $P_v$ ) were obtained from the  
 148 AutoCAD drawings prior to fabrication (Table 1). Autocad drawings are included as  
 149 supplementary data.

150 **Table 1** | Technical details of the grids utilised

<b>Grate</b>	<b>Area filled <math>A_f</math> (<math>m^2</math>)</b>	<b>Area empty spaces <math>A_e</math> (<math>m^2</math>)</b>	<b>Void ratio <math>V</math> (%)</b>	<b>Effective perimeter <math>P_v</math> (m)</b>
A	0.0307	0.0145	32.1	3.0364
B	0.0421	0.0031	6.9	1.2520
C	0.0373	0.0079	17.48	1.3880
D	0.0353	0.0099	21.9	2.3794
E	0.0353	0.0099	21.9	2.3794
F	0.0391	0.0061	13.5	2.2586
G	0.0391	0.0061	13.5	2.2586
H	0.0435	0.0017	3.76	0.5128
I	0.0385	0.0067	14.11	1.2428
J	0.0277	0.0175	38.03	1.8816



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**Figure 3** | Grates applied on the top of the inlet (black arrows show the primary direction of the facility inflow  $Q_1$  and hence the orientation of each inlet grate).

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### Hydraulic conditions

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For each grate inlet displayed in Figure 3, eight tests have been completed over a range of surface inflows ( $Q_1$ ) between 4 and 10 l/s set using the upstream valve ( $V_1$ ). This is equivalent to a unit width discharge ( $q_1 = Q_1/B$ ) between 1 and 2.5 l/s. To ensure reliable depth and flow rate quantification for each test, flows were left to stabilise for 5 minutes before flow rates and depths were recorded. Each reported depth/flow measurement is a temporal average of 3 minutes of recorded data after flow stabilisation, such that full convergence of measured parameters is achieved. In all cases, a flat weir was used as the downstream floodplain boundary, and free surface flow was maintained in the pipe system. The upstream flow depth ( $h_s$ ) is reported as the depth recorded at transducer  $P_6$  (Figure 2). Surface flow Froude number ( $Fr$ ) is calculated based on this flow depth and the calculated cross-sectional averaged velocity ( $U$ ) at this position ( $U = Q_1/B.h_s$ ). The hydraulic conditions for each test are detailed in Table 2. Full (non-averaged) datasets from flow meters  $Q_1$ ,  $Q_3$  and transducers ( $P_0$ ,  $P_1$ ,  $P_2$ ,  $P_3$ ,  $P_4$ ,  $P_5$ ,  $P_6$ ) are presented as supplementary data (Table S1) to this paper.

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172 **Table 2** | Hydraulic parameters measured ( $Q_1$ ,  $Q_e$  and  $h_s$ ) and calculated ( $Fr$ ) for the  
 173 tests conducted

<b>Grate</b>	<b><math>Q_1</math></b>	<b><math>Q_e</math></b>	<b><math>h_s</math></b>	<b><math>Fr</math></b>	<b>Grate</b>	<b><math>Q_1</math></b>	<b><math>Q_e</math></b>	<b><math>h_s</math></b>	<b><math>Fr</math></b>
	(l/s)	(l/s)	(mm)	(/)		(l/s)	(l/s)	(mm)	(/)
A	4.33	0.55	7.28	0.556	B	4.29	0.50	7.26	0.554
	5.00	0.67	7.89	0.569		4.99	0.59	7.92	0.565
	5.66	0.76	8.50	0.576		5.67	0.68	8.60	0.568
	6.32	0.86	9.09	0.582		6.33	0.76	9.15	0.577
	6.93	0.93	9.49	0.599		6.93	0.82	9.63	0.586
	7.51	0.94	10.05	0.595		7.52	0.89	10.12	0.590
	8.22	1.05	10.60	0.601		8.18	0.91	10.64	0.596
	9.29	1.19	11.36	0.612		9.22	0.94	11.42	0.603
C	4.29	0.43	7.53	0.524	D	4.23	0.43	7.72	0.498
	4.97	0.54	8.16	0.539		4.96	0.59	8.40	0.514
	5.66	0.63	8.91	0.538		5.69	0.70	9.24	0.512
	6.32	0.72	9.53	0.542		6.30	0.72	10.11	0.495
	6.95	0.74	10.10	0.546		6.96	0.80	10.72	0.501
	7.54	0.80	10.60	0.552		7.49	0.82	11.18	0.506
	8.21	0.88	11.14	0.558		8.19	0.96	11.70	0.516
	9.28	0.97	11.91	0.570		9.24	1.09	12.49	0.529
E	4.27	0.44	7.36	0.540	F	4.28	0.44	7.40	0.537
	5.00	0.53	8.02	0.555		4.95	0.48	8.07	0.545
	5.68	0.63	8.62	0.566		5.66	0.61	8.75	0.552
	6.31	0.69	9.19	0.572		6.37	0.70	9.40	0.558
	6.96	0.77	9.70	0.582		6.96	0.85	9.74	0.577
	7.51	0.81	10.01	0.582		7.52	0.90	10.20	0.582
	8.19	0.90	10.59	0.600		8.17	0.95	10.63	0.595
	9.24	0.99	11.42	0.605		9.25	1.10	11.49	0.599
G	4.22	0.48	7.60	0.508	H	4.26	0.39	7.25	0.551
	4.93	0.61	8.27	0.523		4.97	0.44	7.96	0.558
	5.63	0.72	9.01	0.525		5.66	0.48	8.68	0.559
	6.26	0.80	9.61	0.530		6.29	0.52	9.35	0.555
	6.87	0.84	10.05	0.544		6.92	0.58	9.82	0.567

	7.52	0.94	10.50	0.558		7.51	0.66	10.30	0.574
	8.21	1.03	11.00	0.568		8.19	0.68	10.77	0.584
	9.22	1.13	11.76	0.578		9.22	0.70	11.57	0.592
I	4.26	0.43	7.28	0.547	J	4.26	0.46	7.44	0.530
	4.97	0.57	7.85	0.571		4.94	0.52	8.13	0.538
	5.64	0.63	8.53	0.571		5.66	0.64	8.78	0.549
	6.27	0.71	9.13	0.573		6.27	0.72	9.39	0.550
	6.92	0.78	9.65	0.583		6.91	0.77	9.87	0.562
	7.51	0.88	10.08	0.593		7.52	0.90	10.35	0.570
	8.16	0.93	10.58	0.599		8.18	0.95	10.84	0.579
	9.22	1.03	11.39	0.605		9.21	0.98	11.66	0.584

174

### 175 Discharge coefficients

176 Within flood modelling applications the weir (1) and orifice (2) equations are  
177 commonly defined as the following (Rubinato et al. 2017a):

$$178 \quad Q_e = \frac{2}{3} C_w \pi D_m \sqrt{2g} (H)^{\frac{3}{2}} \quad (1)$$

179 where  $D_m$  is the diameter of the (circular) inlet (m),  $H$  is the driving hydraulic head  
180 above the interface point accounting for both sewer and surface flows (m).  $C_w$  is the  
181 weir discharge coefficient.

$$182 \quad Q_e = C_o A_m \sqrt{2gH} \quad (2)$$

183 where  $A_m$  is the open area of the inlet and  $C_o$  is the orifice coefficient. In cases  
184 where the sewer is not surcharged, the hydraulic head ( $H$ ) is assumed to be equal to the  
185 surface flow depth. To calibrate discharge coefficients for each grate type, Equations (2)  
186 and (3) were modified to account for the total length of the weir within each grate  
187 design (taken as equal to  $P_v$ ) and total open area (taken as equal to  $A_e$ ). The flow depth  
188 is taken as the measured upstream value ( $h_s$ ).

$$189 \quad Q_e = \frac{2}{3} C_w P_v \sqrt{2g} (h_s)^{\frac{3}{2}} \quad (3)$$

$$190 \quad Q_e = C_o A_e \sqrt{2g} (h_s)^{\frac{1}{2}} \quad (4)$$

## 191 Numerical model

192 The depth-averaged 2D SWEs are commonly used for modelling flows in urban  
193 environments and in rivers and floodplains (Wang et al. 2011). Integrating an inflow  
194 and outflow in/from the sewerage system can be realised by adding suitable source  
195 terms (Lee et al. 2013). The governing equations used for floodplain modelling with  
196 surface to sewer inflows are as follows:

$$197 \quad \frac{\partial h}{\partial t} + \frac{\partial(uh)}{\partial x} + \frac{\partial(vh)}{\partial y} = -q_e \quad (5)$$

$$198 \quad \frac{\partial(uh)}{\partial t} + \frac{\partial(u^2h)}{\partial x} + \frac{\partial(uvh)}{\partial y} = -gh \frac{\partial E}{\partial x} - gn^2 \frac{u\sqrt{u^2 + v^2}}{h^{1/3}} \quad (6)$$

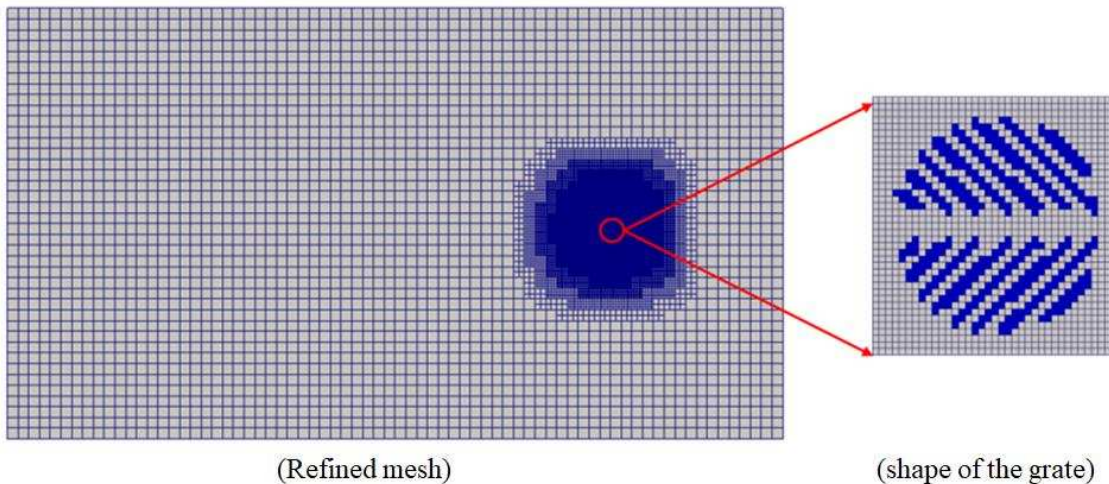
$$199 \quad \frac{\partial(vh)}{\partial t} + \frac{\partial(uvh)}{\partial x} + \frac{\partial(v^2h)}{\partial y} = -gh \frac{\partial E}{\partial y} - gn^2 \frac{v\sqrt{u^2 + v^2}}{h^{1/3}} \quad (7)$$

200 In Equations (5)–(7), (x, y) are the spatial Cartesian coordinates and t is the time (SI  
201 units). h (m) is the water depth u and v (m/s) are x- and y-direction velocities,  
202 respectively. E is the water elevation (m), and n is Manning’s roughness coefficient  
203 (here taken as 0.009 m/s<sup>1/3</sup>, from previous experimental work, e.g., Rubinato et al.  
204 (2017a)). q<sub>e</sub> (m/s) is the area discharge, in this study representing surface to sewer  
205 discharge via the inlet grate. A leap-frog method is used in order to reduce simulation  
206 time, with variables laid on staggered mesh. Fluxes (uh and vh) are located at the  
207 computational cell boundary and water depth (h) is located at the centre of the  
208 computational cell. More detailed information regarding the leap-frog and FDM  
209 methods can be found in Lee (2013).

## 210 Model setup and boundary conditions

211 An adaptive mesh technique (Haleem et al. 2015) is used to reduce the calculation time (Figure  
212 4). In the simulation, the downstream depth measurement point (P<sub>7</sub>) is used to define  
213 downstream boundary conditions, hence the initial number of quadrilaterals was chosen to be 72  
214 × 40 (7.2 m × 4.0 m) to generate a baseline (coarse) mesh with a spatial resolution of around 0.1  
215 m × 0.1 m. A mesh convergence analysis was carried out, which suggested the need for a four  
216 times finer mesh for the model to be able to appropriately resolve the hydrodynamics of the  
217 grate inlet. As shown in Figure 4, up to four levels of refinement are implemented around the  
218 local zone of sewer-to-floodplain interaction (resolution around 6.25 mm × 6.25 mm) and these  
219 are assumed appropriate to replicate the geometry of each grate type. The open cells within each

220 grate area are identified as cells where the  $q_e$  term in Equation (5) is nonzero. The total flow  
221 exchange from surface to sewer is calculated by applying Equation (3) using the experimentally  
222 obtained weir coefficients and simulated upstream water depth at  $P_6$  ( $h_s$ ).  $q_e$  for each open cell is  
223 then calculated based on the total calculated flow exchange and the total open area of each grate  
224 type. All the simulations were run until convergence to a steady state is attained. A mesh  
225 convergence analysis suggested the use of a convergence (depth) threshold-error no bigger than  
226  $10^4$  and no less than  $10^6$ . The initial discharge condition is taken to be the unit width surface  
227 inflow  $q_1$  and a measured velocity profile is used to set water depth at the eastern (upstream)  
228 boundary. This velocity curve was obtained prior to the experiments by measuring ten flows  
229 ( $Q_1$ ) between 2 l/s and 11 l/s and recording the average velocity in the area included between  
230 0.5 and 3.5 m of the total width, with sampling points each 0.5 m. At the southern and northern  
231 boundaries (lateral), a wall boundary condition is employed (reflective). At the western  
232 (downstream) boundary, measured water depth at  $P_7$  is used.



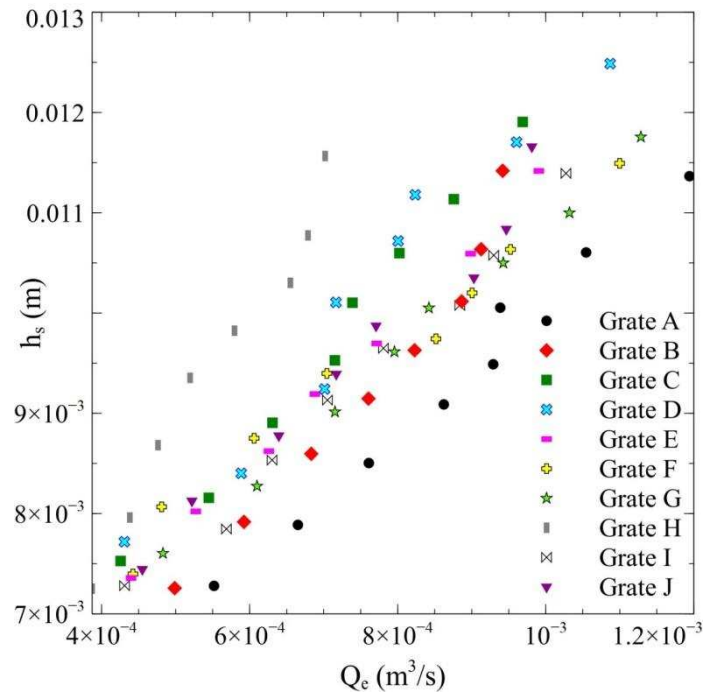
233  
234 **Figure 4** | Mesh characterisation example for grate type A.

## 235 **RESULTS AND DISCUSSIONS**

236 This section presents discharge coefficients estimated for each grate configuration and  
237 the comparison of the 2D finite difference model predictions against observed flow  
238 depths recorded around the inlet at seven different pressure sensor locations ( $P_0$ – $P_6$ )  
239 displayed in Figure 2.

240 **Experimental results and calibrated discharge coefficients**

241 Figure 5 shows the relationship between the upstream water depth ( $h_s$ ) and the  
242 correspondent flow exchange ( $Q_e$ ) through each grate type over the range of flow  
243 conditions tested.



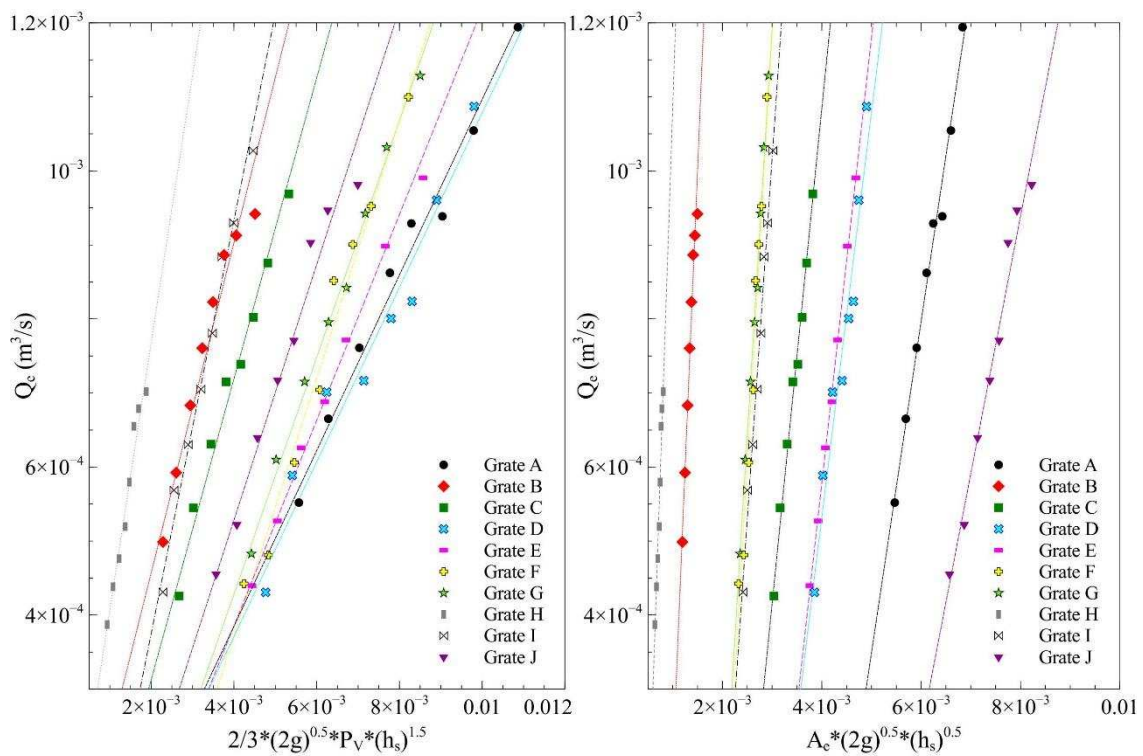
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245 **Figure 5** | The observed relationship between upstream water depth vs surface to sewer  
246 flow exchange for each grate type.

247 The results confirm that the geometry of each grate strongly influences the flow  
248 entering the surface-sewer inlet. When comparing results for similar hydraulic  
249 conditions, grate H ( $A_e = 0.0017 \text{ m}^2$  ;  $P_v = 0.5128 \text{ m}$ ) is the grate that results in the  
250 lowest exchange flows while grate A allows the highest exchange flows ( $A_e = 0.0145$   
251  $\text{m}^2$  ;  $P_v = 3.0364 \text{ m}$ ). It can be noted that while grate A has the highest perimeter values,  
252 its void area is lower than grate J. In general, the results confirm that the exchange flow  
253 capacity of each grate design is more strongly correlated to the effective perimeter than  
254 the void area; however, individual different grate designs can affect the flow patterns  
255 around the void spaces and hence drainage efficiency. To provide a better understanding  
256 of this a further investigation including consideration of the local flow velocity is  
257 required.

258 Calibration of Equations (3) and (4) is achieved by fitting a linear trend between the  
259 terms of the relevant equation and the surface to sewer exchange flow ( $Q_e$ ) for each  
260 grate type (shown in Figure 6). The average goodness of fit of the linkage equations

261 over all grate types (weir equation average  $R^2 = 0.977$ , orifice equation  $R^2 = 0.980$ )  
 262 shows that both weir and orifice equations are shown to be applicable for representation  
 263 of surface to sewer flow exchange in steady flow (confirming previous work, Rubinato  
 264 et al. (2017a)) and that over the range of hydraulic conditions tested here, the weir and  
 265 orifice coefficients can be taken as constant. Calibrating the weir Equation (3) against  
 266 the experimental results provides a discharge coefficient  $C_w$  in the range 0.115–0.372  
 267 based on the variety of grates applied (Table 1). Calibration of the orifice Equation (4)  
 268 against the experimental results provides a discharge coefficient  $C_o$  in the range 0.349–  
 269 2.038. Values for each grate type are provided in Table 3, along with correspondent  
 270 goodness of fit values ( $R^2$ ). Discharge coefficients observed in this study are in the same  
 271 range to those found by Martins et al. (2014) for a  $0.6 \times 0.3 \times 0.3$  m gully under  
 272 drainage conditions ( $0.16 < C_w < 1.00$ ,  $1.36 < C_o < 2.68$ ) but differs to those obtained by  
 273 Bazin et al. (2014) for small ( $0.05 \times 0.05$  m) fully open street inlets ( $0.58 < C_o < 0.67$ ).  
 274 This is likely due to the variation in scales between the experimental facilities used. It is  
 275 noticeable that the orifice equation results in a larger variation in the range of calibrated  
 276 coefficients than the weir equation.

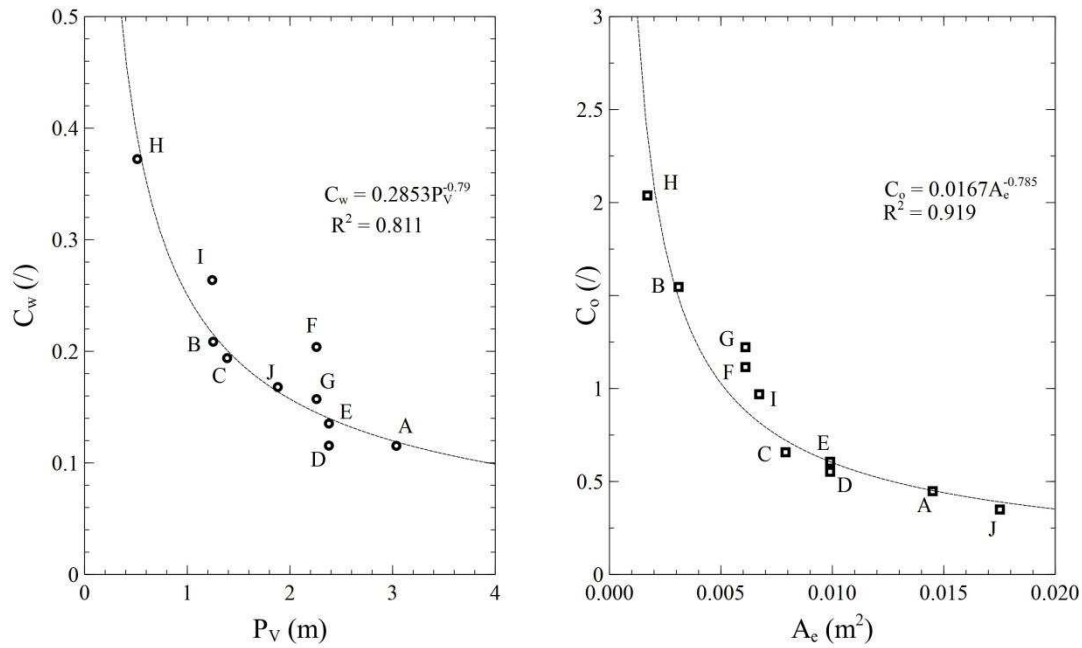


278 **Figure 6** | (left) The relationship between the weir equation (3) for each flow condition  
 279 tested vs the correspondent flow exchange; (right) the relationship between the orifice  
 280 equation (4) vs the correspondent flow exchange.

281 Calibrated discharge coefficients show an inverse trend with the geometrical parameters  
 282 ( $P_v$  or  $A_e$ ) associated with the different grate types, suggesting a higher energy loss  
 283 associated with surface to sewer flow transfer as opening size decreases (Figure 7).  
 284 Figure 7 shows that coefficients approach an approximately constant value ( $C_w \approx 0.115$ ,  
 285  $C_o \approx 0.35$  in this case) as opening size and size and perimeter length increases. The  
 286 consideration of individual grate types shows that the application of the weir equation  
 287 tends to provide higher  $R^2$  values for grate types when the perimeter length value ( $P_v$ ) is  
 288 relatively large (e.g., grate types D and G), while the orifice equation tends to provides  
 289 higher  $R^2$  values for grate types when the perimeter length value is smaller (e.g., grate  
 290 types B and C). This may be due to the increased likelihood of grates with small  
 291 effective perimeters to become ‘drowned’. However, the effect is relatively subtle and  
 292 in some cases the difference in  $R^2$  values is negligible even between designs with large  
 293 or small effective perimeter values (e.g., grate types A and H).

294 **Table 3** | Values of experimentally calibrated weir and orifice coefficients ( $C_w$  and  $C_o$ )  
 295 and correspondent goodness of fit  $R^2$  values

Grate	$C_w$	$R^2$	$C_o$	$R^2$
A	0.115	0.984	0.448	0.987
B	0.208	0.951	1.546	0.974
C	0.194	0.985	0.657	0.991
D	0.115	0.957	0.552	0.950
E	0.135	0.995	0.606	0.998
F	0.204	0.981	1.115	0.994
G	0.157	0.995	1.222	0.976
H	0.372	0.966	2.038	0.967
I	0.264	0.989	0.969	0.989
J	0.168	0.969	0.349	0.978



297

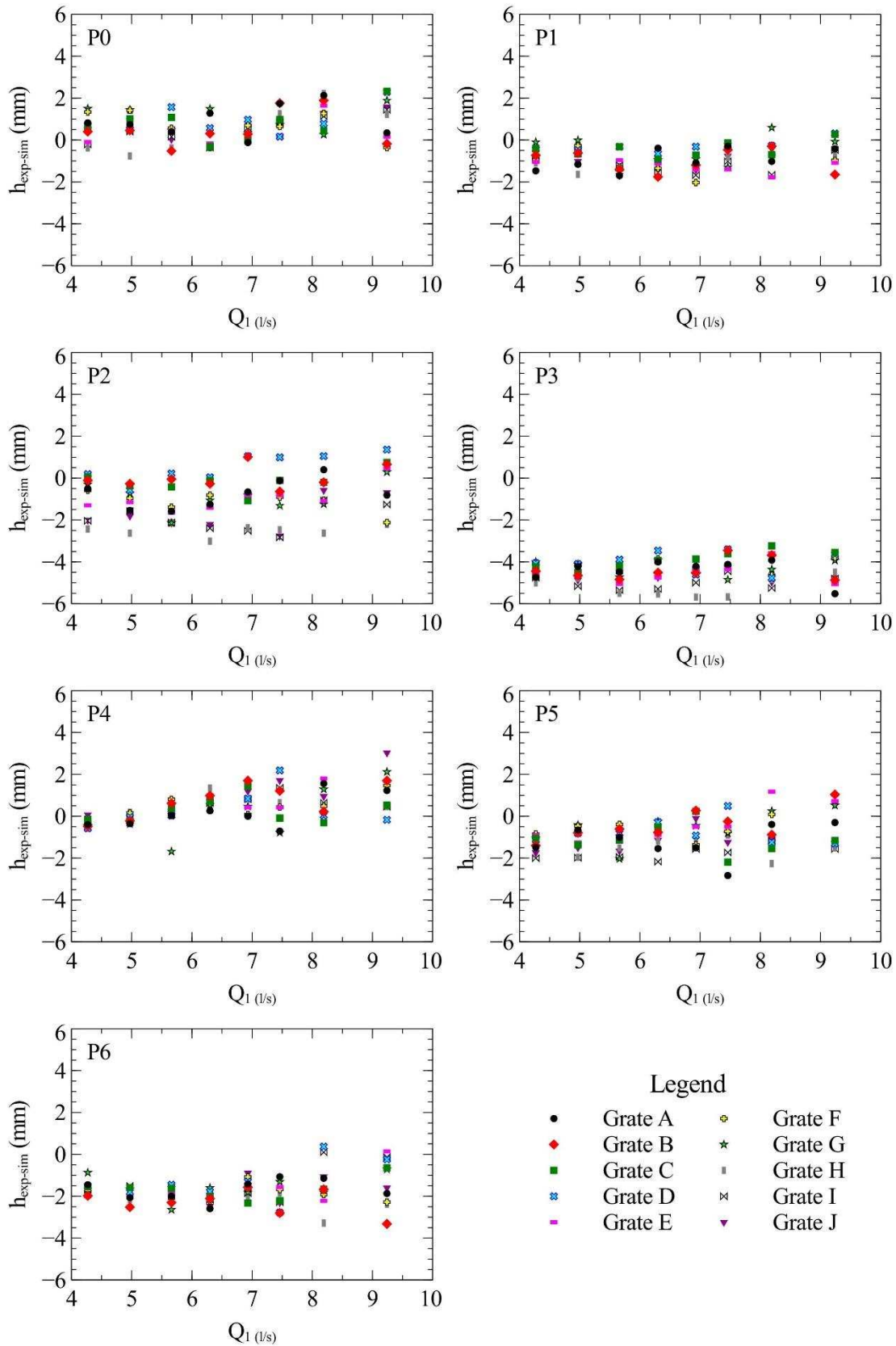
298 **Figure 7** | Relationships between experimentally calibrated weir ( $C_w$ ) and orifice ( $C_o$ )  
 299 coefficients and geometrical parameters for each inlet grate.

### 300 Numerical results

301 Figure 8 displays the difference between the experimental depths, as measured by the  
 302 transducers (Figure 2), with the depths calculated by the numerical model at each  
 303 measurement location ( $h_{exp} - h_{sim}$ ). In most locations the numerical results overestimate  
 304 the experimentally observed water depths. At locations  $P_0$  and  $P_4$  (i.e., 75 mm left and  
 305 right of the inlet), this condition is reversed and the model tends to underestimate  
 306 observed water depths. Despite this, overall, the numerical model provides a good  
 307 representation of the experimental observations within the range of 0–5 mm of the  
 308 experimental values when considering the full range of inlet flow conditions ( $Q_1$ ).  
 309 Modelling errors may be due to the uncertainties related to: (i) the replication of grates  
 310 and the correspondent discretisation of the meshing system adopted; (ii) discrepancies  
 311 in the floodplain bed elevation applied within the model; (iii) minor effects due to any  
 312 skewed inflow from the inlet tank in the experimental model; (iv) use of the upstream  
 313 water depth to calculate total flow exchange instead of actual hydraulic head at each  
 314 exchange cell as well as any discharge coefficient calibration errors; (v) the depth  
 315 averaged nature of the model or other simplifications. Errors are generally seen to be  
 316 smaller for the range of  $Q_1 = [4.2; 7.46]$  l/s. By analysing each measurement location



317 separately,  $P_2$  and  $P_3$  (i.e., just upstream and downstream of the inlet) show the highest  
318 discrepancies (up to 5 mm). This may be related to complex flow patterns forming  
319 upstream and downstream of the inlet (such as water accumulation and separation and  
320 merging of stream flows) that the model may find difficult to fully replicate.  
321 Discrepancies (0–3 mm) are also noted within the pressure measurement  $P_6$  located 460  
322 mm upstream of the centreline of the inlet. For measurement locations less influenced  
323 by the flow entering the inlet, such as  $P_1$  and  $P_5$ , errors are within the range 0–2 mm. In  
324 terms of flow exchange rate, the numerical simulations tend to overestimate the average  
325 exchange discharge (on average by 0.25 l/s). Flow exchange calculations within  
326 modelling tools are sensitive to calculations of relative head within pipe and surface  
327 systems (Rubinato et al. 2017a). In this case, flow exchange is calculated using the  
328 calibrated weir equation based on the numerical simulation of flow depth upstream of  
329 the inlet. Resulting discrepancies in the simulation of hydraulic water depths around the  
330 inlet can therefore be seen to propagate to the calculation of flow exchange rate.  
331



332

333 **Figure 8** | Comparison between the experimental observations and numerical hydraulic

334 heads at each measurement location.

## 335 **SUMMARY AND CONCLUSIONS**

336 This work has explored the experimental and numerical modelling of surface to sewer  
337 flow exchange. A physical model, linking a slightly inclined urban floodplain to a sewer  
338 system, was used to carry out measurements under steady state flow conditions with the  
339 application of ten different circular grates on the top of a surface/sewer linking  
340 structure. Eighty steady state experiments were conducted, during which water levels at  
341 seven locations surrounding the inlet structure were measured. The results have  
342 confirmed the validity of both the weir and orifice linking equations to describe the total  
343 surface to sewer exchange flows through different inlet grates. Calibrated discharge  
344 coefficients have been provided for each grate type tested which were taken as constant  
345 over the range of hydraulic conditions tested. Overall, the calibrated orifice discharge  
346 coefficient showed a larger variation between the grate types. Whilst some evidence  
347 was provided to suggest that the weir equation outperforms the orifice equation when  
348 the effective perimeter of the grate is relatively high, and vice versa, no significant  
349 difference in performance was observed over the range of flow rates tested. Overall  
350 trends suggested that discharge coefficients (i.e. energy losses) decrease as the grate  
351 geometrical parameters (void area and effective perimeter) increase and may converge  
352 to an approximately constant value. In addition, a finite difference numerical model was  
353 tailored to reproduce flow conditions around the inlet structure. Experimentally  
354 calibrated exchange equations were used to define the inflow through each modelled  
355 grate type. The numerical results have been compared with the experiments in terms of  
356 depth around the inlet at seven sampling points and detailed comparisons show a regular  
357 agreement between the numerical and experimental water levels (maximum discrepancy  
358 5 mm). It can therefore be concluded that the proposed 2D numerical approach is able  
359 to model floodplain-to-sewer interaction and flow conditions in the vicinity of the  
360 linking structure reliably, despite the uncertainties generated by the different geometries  
361 of the grates applied and any head variations over the inlet structure. Maximum  
362 discrepancies were observed immediately upstream and downstream of the inlet  
363 structure, likely due to the complex flow patterns generated by the grate types. While it  
364 is not currently feasible to use such methods directly within full scale flood simulations  
365 (due to the small mesh sizes required), the work demonstrates the academic capability  
366 of the modelling technique and validates the model for supplementary studies. It was  
367 also noted that minor discrepancies in the calculation of flow depth propagated to the

368 estimation of flow exchange by the numerical model. Further, more detailed  
369 investigation of the exchange flows and the development of modelling approaches that  
370 can inherently account for spatially variable energy losses, flow depths and flow  
371 exchange rates within different inlet configurations will require characterisation of the  
372 velocity fields such that a full understanding of the flow can be elucidated.

373

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379

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