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# Probing dark matter with star clusters: a dark matter core in the ultra-faint dwarf Eridanus II

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## ABSTRACT

We present a new technique to probe the central dark matter (DM) density profile of galaxies that harnesses both the survival and observed properties of star clusters. As a first application, we apply our method to the 'ultra-faint' dwarf Eridanus II (Eri II) that has a lone star cluster  $\sim$ 45 pc from its centre. Using a grid of collisional *N*-body simulations, incorporating the effects of stellar evolution, external tides and dynamical friction, we show that a DM core for Eri II naturally reproduces the size and the projected position of its star cluster. By contrast, a dense cusped galaxy requires the cluster to lie implausibly far from the centre of Eri II (>1 kpc), with a high inclination orbit that must be observed at a particular orbital phase. Our results, therefore, favour a DM core. This implies that either a cold DM cusp was 'heated up' at the centre of Eri II by bursty star formation or we are seeing an evidence for physics beyond cold DM.

**Key words:** stars: kinematics and dynamics – galaxies: dwarf – galaxies: haloes – galaxies: individual: Eridanus II – galaxies: star clusters: general – galaxies: structure.

### **1 INTRODUCTION**

The  $\Lambda$  'Cold Dark Matter' ( $\Lambda$ CDM) model gives a remarkable match to the growth of structure on large scales in the Universe (e.g. Tegmark & Zaldarriaga 2002; Planck Collaboration XVI 2014). Yet on smaller scales, inside galaxy groups and galaxies, there have been long-standing tensions (e.g. Klypin et al. 1999; Moore et al. 1999). Key amongst these is the 'cusp-core' problem. Pure dark matter (DM) simulations of structure formation in a ACDM cosmology predict that galaxies should reside within dense central DM cusps with density  $\rho \propto r^{-1}$  (e.g. Dubinski & Carlberg 1991; Navarro, Frenk & White 1996), whereas observations of the rotation curves of dwarf galaxies have long favoured constant density cores (e.g. Flores & Primack 1994; Moore 1994; Read et al. 2017). This may owe to physics beyond CDM, for example self-interacting DM (SIDM; e.g. Spergel & Steinhardt 2000; Kaplinghat, Tulin & Yu 2016), wave-like DM (e.g. Schive et al. 2014), or ultra-light axions (e.g. González-Morales et al. 2017). However, all of these small-scale tensions with  $\Lambda$  CDM arise when comparing models devoid of 'baryons' (stars and gas) with real galaxies in the Universe. There is mounting evidence that bursty star formation during galaxy formation can 'heat-up' DM, transforming a DM cusp to a core (e.g. Navarro, Eke & Frenk 1996; Read & Gilmore 2005; Pontzen & Governato 2012, 2014; Pontzen et al. 2015). The latest simulations, that reach a mass and spatial resolution sufficient to resolve the multiphase interstellar medium, find that DM cores, of approximately the half stellar mass radius in size ( $R_{1/2}$ ), form slowly over a Hubble time (Mashchenko, Wadsley & Couchman 2008; Governato et al. 2010; Pontzen & Governato 2012; Teyssier et al. 2013; Di Cintio et al. 2014; Madau, Shen & Governato 2014; Oñorbe et al. 2015; Read, Agertz & Collins 2016; Tollet et al. 2016; Munshi et al. 2017).

Although the above simulations agree on the size and formation time-scale of DM cores, there remains some disagreement over the DM halo mass at which cusp-core transformations become inefficient,  $M_{200} \equiv M_{\text{pristine}}$ .<sup>1</sup> As pointed out by Peñarrubia et al. (2012), for a fixed  $M_{200}$  if too few stars form, then there will no longer be enough integrated supernova (SN) energy to unbind the DM cusp. Depending on the numerical scheme employed,  $M_{\text{pristine}}$  has been reported to be as high as  $M_{\text{pristine}} \sim 10^{10} \text{ M}_{\odot}$  (e.g. Chan et al. 2015; Tollet et al. 2016) and as low as  $M_{\text{pristine}} \sim 10^8 \text{ M}_{\odot}$  (Read et al. 2016, hereafter R16), where the spread owes primarily to different star formation efficiencies in low-mass haloes (see Section 2.2 and Fig. 1).

 $^{1}M_{200}$  is the virial mass. For satellite galaxies, we define this pre-infall.

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**Figure 1.** The stellar mass-halo mass relation of isolated dwarf galaxies. The symbols correspond to the observational data and the squares to the results from *N*-body simulations. The blue solid lines show the results from abundance matching in  $\Lambda$ CDM using the SDSS field stellar mass function (where the lines are dashed, the results are extrapolated). Eri II is marked by the red star. It appears to be consistent with a 'failed' Leo T, inhabiting a similar DM halo but having its star formation shut down earlier, lowering its  $M_*$  for the same pre-infall  $M_{200}$ .

The above motivates measuring the central DM density of the very faintest galaxies in the Universe. With little star formation, these may be expected to retain their 'pristine' DM cusps (e.g. R16). There is no shortage of such faint dwarf galaxies orbiting the Milky Way, Andromeda, and nearby systems (e.g. Belokurov et al. 2007; Collins et al. 2014; Bechtol et al. 2015; Sand et al. 2015). However, most of these are devoid of gas and so the kinematics of their stars must be used to probe their DM haloes. This is challenging because of a strong degeneracy between their DM density profiles and the orbit distribution of their stars (e.g. Merrifield & Kent 1990; Evans, An & Walker 2009; Read & Steger 2017). For the brighter Milky Way dwarfs, this degeneracy can be broken by using metallicity or colour to split the stars into distinct components with different scale lengths (e.g. Battaglia et al. 2008; Walker & Peñarrubia 2011 and Agnello & Evans 2012, but see Breddels & Helmi 2013 and Richardson & Fairbairn 2014). However, for the fainter dwarfs, there are too few stars to obtain strong constraints (Read & Steger 2017).

An alternative method for probing the central density of dwarf galaxies was proposed by Hernandez & Gilmore (1998), Goerdt et al. (2006), and Sánchez-Salcedo, Reyes-Iturbide & Hernandez (2006). They showed that the globular clusters (GCs) in the dwarf spheroidal galaxy Fornax would rapidly sink to the centre by dynamical friction if Fornax has a steep DM cusp. By contrast, in a constant density core, dynamical friction is suppressed (Read et al. 2006a; Inoue 2009, 2011; Petts, Gualandris & Read 2015; Petts, Read & Gualandris 2016), allowing Fornax's GCs to survive through to the present day. This 'timing argument' was refined by Cole et al. (2012), who used 2800 *N*-body simulations of Fornax's GC system to show that a core is favoured over a cusp, in excellent agreement with split-population modelling of Fornax's

stars (e.g. Walker & Peñarrubia 2011). (Such survival arguments were extended by Peñarrubia, Walker & Gilmore (2009) to the GCs associated with the Sagittarius dwarf.) Although it is likely that Fornax has a DM core, its stellar mass ( $M_* \sim 4 \times 10^7 \,\mathrm{M_{\odot}}$ ; de Boer et al. 2012) is large enough for bursty star formation to drive complete cusp-core transformations (Peñarrubia et al. 2012; R16). Thus, Fornax's core yields inconclusive constraints on the nature of DM.

In this paper, we develop a new method for probing the central DM density of dwarf galaxies that harnesses both the survival and present-day properties of star clusters. Star clusters are dense stellar systems that slowly expand due to two-body relaxation (Hénon 1965; Gieles et al. 2010). In a tidal field, high-energy stars are pushed over the cluster's tidal boundary, slowing down the expansion. Eventually, the cluster's half stellar mass radius becomes a constant fraction of the tidal radius and, from that moment on, the cluster evolves approximately at a constant density set by the tidal field (Hénon 1961; Gieles, Heggie & Zhao 2011). Thus, the observed surface density of low-mass GCs (i.e. those that have undergone sufficient relaxation) can be used as probes of the host galaxy's tidal field and, therefore, its density distribution (Innanen, Harris & Webbink 1983). This allows us to probe the DM distribution in any dwarf galaxy with low-mass star clusters, including those with a much lower stellar mass than Fornax. This is the key idea that we exploit in this work.<sup>2</sup>

To model star clusters sinking in the potential of a host dwarf galaxy, we make use of the semi-analytic dynamical friction model from Petts et al. (2016, hereafter P16), implemented in the direct-summation code NBODY6 (Aarseth 2003). This allows us to model the survival of star clusters, similarly to Cole et al. (2012), but with a complete *N*-body model of the star cluster itself, including two-body effects, binary formation and evolution, and stellar evolution. By comparing a large grid of such models with observational data, we are able to constrain the DM density of dwarf galaxies that host low-mass GCs, independently of timing arguments or stellar kinematic measurements.

As a first application, we apply our method to the ultra-faint dwarf galaxy Eridanus II (Eri II) that was recently discovered by the Dark Energy Survey (DES; Bechtol et al. 2015; Koposov et al. 2015). Eri II is situated 366 kpc from the Sun, at the edge of the MW, with  $M_V = -7.1$ , a half-light radius of  $R_{1/2} = 2.31'$ , and an ellipticity of 0.48. Eri II appears to show an extended star formation history, but follow-up observations are needed to confirm this. Koposov et al. (2015) and Crnojević et al. (2016) found that Eri II has a lone star cluster at a projected distance ~45 pc from Eri II's centre, with  $M_V = -3.5$  and a half-light radius of 13 pc (see Crnojević et al. 2016, Table 1). Compared to the MW's star clusters (Harris 1996, 2010 edition), Eri II's star cluster appears faint and extended, contributing just ~4 per cent of Eri II's total luminosity.

This paper is organized as follows. In Section 2, we describe our method for probing the central DM density of dwarf galaxies using star clusters, and we motivate our priors for modelling Eri II. In Section 3, we present our main findings. In Section 4, we discuss the implications of our results for galaxy formation and the nature of DM. Finally, in Section 5, we present our conclusions.

<sup>&</sup>lt;sup>2</sup> Note that the cluster's stellar kinematics are also affected by tides, making them additional probes of the properties of the galactic tidal field (e.g. Küpper et al. 2010; Claydon, Gieles & Zocchi 2017).

# 2 METHOD

# 2.1 A new method for measuring the inner DM density of dwarf galaxies

We model the evolution of star clusters orbiting within a host dwarf galaxy using NBODY6DF (P16). This is a publicly available<sup>3</sup> adaptation of NBODY6, which is a fourth-order Hermite integrator with an Ahmad & Cohen (1973) neighbour scheme (Makino & Aarseth 1992; Aarseth 1999, 2003), and force calculations that are accelerated by Graphics Processing Units (GPUs, Nitadori & Aarseth 2012). NBODY6 contains metallicity-dependent prescriptions for the evolution of individual stars and binary stars (Hurley, Pols & Tout 2000; Hurley, Tout & Pols 2002), which we use in our simulations here.

In NBODY6DF, we model the host dwarf galaxy as a static, analytic potential. Dynamical friction is then applied to star cluster members using the semi-analytic model described in P16 (see also Petts et al. 2015). The P16 model has been extensively tested against full *N*-body simulations of dynamical friction in both cored and cusped background potentials, giving an excellent description of the orbital decay in both cases. In particular, it is able to reproduce the 'corestalling' behaviour, whereby dynamical friction is suppressed inside constant density cores (Goerdt et al. 2006; Read et al. 2006a; Inoue 2009, 2011 and see P16 for further details).

We set up a grid of 200 NBODY6DF simulations, varying the density profile (cusped or cored) and the initial orbit and properties of the star cluster. Comparing this grid with observations, we determine the most likely mass distribution for Eri II, and the initial properties of its star cluster. [Eri II is dominated at all radii by its DM halo (see Section 2.2) and so its total mass distribution directly provides us with its DM density profile.] In addition, we run a further 26 simulations to determine how our results depend on the mass, concentration, and inner logarithmic slope of Eri II's DM halo (Section 3.4). We also test whether Eri II's cluster could form and survive in the very centre of Eri II (Section 3.5).

#### 2.2 The DM halo of Eri II

We model the DM halo of Eri II using the coreNFW profile from R16. This is described by a mass  $M_{200}$  and concentration parameter  $c_{200}$ , identical to those used for the cusped Navarro–Frenk–White (NFW) profile (Navarro et al. 1996). However, it allows also for a central DM core. By default, this has a size set by the projected half-light radius of the stars  $R_{1/2}$ , which for Eri II is  $R_{1/2} = 0.28$  kpc<sup>4</sup> (Crnojević et al. 2016). The power-law slope of the core is set by n, where n = 1 produces a flat DM core, whereas n = 0 returns the fully cusped NFW profile.<sup>5</sup>

Eri II's stellar population may be expected to be like other similar stellar mass dwarf galaxies (e.g. Bootes I and Ursa Major I; see McConnachie 2012) that have predominantly old-age stars. Santana et al. (2013) showed that the apparent intermediate-age population in these galaxies is likely due to the presence of blue straggler stars.

#### <sup>3</sup> http://github.com/JamesAPetts/NBODY6df.

<sup>4</sup> The latest estimates of  $R_{1/2}$  are slightly lower than the value we have assumed here,  $R_{1/2} = 246 \pm 13$  pc (Denija Crnojević, private communication), though within the  $2\sigma$  uncertainties. However, as we show in Section 3.4, we are not very sensitive to  $M_{200}$ ,  $c_{200}$ , or the DM core size. As such, the newer value for  $R_{1/2}$  will not affect our results.

<sup>5</sup> In R16, *n* was parametrized by the total star formation time. However, since this is poorly determined for Eri II, we consider here just a range of values for *n*. We discuss this further in Section 4.

However, they could not rule out the presence of an intermediateage population of up to 3 Gyr old. Recent *Hubble Space Telescope* data (propID 14234; subject of a future publication) have confirmed that Eri II's stellar population is similar to those studied by Santana et al. (2013), hence favouring an older population. In this work, we choose to be conservative and assume that the cluster is older than 5 Gyr.

To obtain an estimate of the (pre-infall) halo mass,  $M_{200}$ , for Eri II, we use the recent measurement of its mass within the 3D half-light radius  $M_{1/2} = 1.2^{+0.4}_{-0.3} \times 10^7 \,\mathrm{M_{\odot}}$ , derived from stellar kinematics by Li et al. (2017). We turn this into an  $M_{200}$  by fitting an NFW profile to  $M_{1/2}$  using the  $M_{200}$ - $c_{200}$  relation from Macciò et al. (2007), finding  $M_{200} = 4.7^{+6.9}_{-2.6} \times 10^8 \,\mathrm{M_{\odot}}$ .

To test if the above value for  $M_{200}$  is reasonable, in Fig. 1 we compare the stellar mass ( $M_* \simeq 8 \times 10^4 \,\mathrm{M_{\odot}}$ ; Bechtol et al. 2015) and  $M_{200}$  for Eri II with measurements for other nearby dwarfs; Eri II is marked by the red star. The purple circles show the  $M_*$ - $M_{200}$  relation for isolated gas-rich dwarfs from Read et al. (2017). The dark cyan triangle shows a measurement for the Carina dwarf spheroidal galaxy from Ural et al. (2015). The light cyan diamond shows an estimate for the isolated dIrr Leo T from Read et al. (2017). The blue solid and dashed lines show the  $M_*-M_{200}$  relation derived by Read et al. (2017) from abundance matching in  $\Lambda$ CDM using the SDSS field stellar mass function (the dashed lines show where this is extrapolated). The remaining data points show the latest results from a range of simulations of isolated dwarfs taken from the literature: R16 (magenta); Wang et al. (2015) (green); Chan et al. (2015) (yellow); Wheeler et al. (2015) (blue); and Fitts et al. (2017) (pink). As can be seen, there is a clear discrepancy between most simulations and the data below  $M_{200} \sim 10^{10} \,\mathrm{M_{\odot}}$  that remains to be understood (Jethwa, Erkal & Belokurov 2018). For our paper here, however, this plot demonstrates that our derived  $M_{200}$  for Eri II is in good agreement with estimates for other galaxies of a similar stellar mass. Eri II is consistent with a 'failed' Leo T, inhabiting a similar DM halo but having its star formation shut down earlier, lowering its  $M_*$  for the same pre-infall  $M_{200}$ . This is further evidenced by the lack of detected H I gas, or recent star formation, in Eri II (Crnojević et al. 2016).

In Fig. 2, we show the cumulative mass profiles (left-hand panel) and DM density profiles (right-hand panel) for Eri II that we assume in our fiducial grid of simulations (we explore different halo masses, concentrations, and logarithmic cusp slopes in Section 3.4). The grey lines show the cusped model, and the green lines show the cored model. The middle of the three lines shows  $M_{200} = 5 \times 10^8 \,\mathrm{M_{\odot}}$ that we assume from here on. The top and bottom lines show the upper and lower boundary of  $M_{200}$  estimated from the kinematic measurements (Li et al. 2017). The projected half-light radius of the stars,  $R_{1/2}$ , is marked by the vertical blue line. On the left-hand panel, the measurement of  $M_{1/2}$  for Eri II from Li et al. (2017) is marked by the red data point. As can be seen, due to the  $M_{200}-c_{200}$ relation, changing  $M_{200}$  produces only a small effect on the DM density within  $R_{1/2}$ . Thus, our method will not be very sensitive to  $M_{200}$  (we will verify this expectation in Section 3.4). However, cusped and cored models look very different within  $R_{1/2}$  and this is what we aim to probe in this work.

Finally, the latest version of NBODY6DF only supports a background DM density profile modelled by Dehnen spheres (Dehnen 1993):

$$\rho(r) = \frac{M_0(3-\gamma)}{4\pi r_0^3} \left(\frac{r}{r_0}\right)^{-\gamma} \left(1 + \frac{r}{r_0}\right)^{\gamma-4},\tag{1}$$

where  $M_0$  and  $r_0$  are the mass and scale length, respectively, and  $-\gamma$  is the logarithmic slope of the inner density profile.



Figure 2. DM halo models for Eri II, chosen as described in Section 2.2. The left-hand panel shows the cumulative mass profiles; the right-hand panel shows the logarithmic density profiles. The mass within the projected stellar half-light radius  $M_{1/2}$  is marked by the red data point with error bars on the left-hand panel (taken from Li et al. 2017). The dashed black and green lines show the cusped and cored models explored in this work, respectively. These are the best-fitting Dehnen profile models to the dwarf galaxy models marked by the solid black and green lines, respectively. For our fiducial grid of simulations, we assume Eri II inhabits DM halo with a virial mass of  $M_{200} = 5 \times 10^8 \text{ M}_{\odot}$ . Models with a halo mass at the 68 per cent upper and lower bound of Eri-II's stellar kinematics are marked by the upper and lower grey and green lines. For the core profiles, we used the same halo mass as the cusp profiles with n = 0.9 (corresponding to a Dehnen model with  $\gamma = 0$ ; dashed green line). The vertical blue line on both panels marks the projected half-light radius of Eri II,  $R_{1/2}$ . We explore the effect of varying  $M_{200}$ ,  $c_{200}$ , and the inner logarithmic cusp slope of Eri II's DM halo in Section 3.4.

Thus, to obtain DM profiles suitable for NBODY6DF, we fit the above Dehnen profile to our coreNFW density profiles. These fits are shown by the dashed lines in the right-hand panel of Fig. 2. As can be seen, inside  $R_{1/2}$  (our region of interest), these fits are excellent. Our best-fitting parameters for the cored ( $\gamma = 0$ , which corresponds to n = 0.9 for our coreNFW profile) and cusped ( $\gamma = 1$ , which corresponds to n = 0) models were:  $M_0 = 4.79 \times 10^8 \,\mathrm{M_{\odot}}$  and  $r_0 = 0.877 \,\mathrm{kpc}$  and  $M_0 = 2.94 \times 10^8 \,\mathrm{M_{\odot}}$  and  $r_0 = 1.078 \,\mathrm{kpc}$ , respectively.

### 2.3 Eri II's star cluster

We model the initial conditions of Eri II's star cluster as a Plummer sphere (Plummer 1911) with a Kroupa IMF (Kroupa 2001), sampling stars with masses between 0.1 and 100 M<sub>☉</sub> and assuming a metallicity of Z = 0.0008 (corresponding to [Fe/H]  $\simeq -1.5$ ). We assumed a range of initial masses  $M_{\rm cl, 0}$  and half-mass radii  $r_{\rm hm, 0}$ for the cluster to explore how its initial properties impact its final state.

#### 2.4 Exploring parameter space

To explore the parameter space, we ran 200 simulations, 100 for each galaxy model (core and cusp). We varied  $r_{\rm hm, 0}$ ,  $M_{\rm cl, 0}$  and the initial galactocentric distance ( $R_{\rm g, 0}$ ) of the cluster. We allowed the cluster to have an  $r_{\rm hm, 0}$  of 1, 5, 10, 15, and 20 pc; a  $M_{\rm cl, 0}$  of approximately 13 000, 19 000, 25 000, and 32 000 M<sub> $\odot$ </sub>; and  $R_{\rm g, 0}$  of 0.14, 0.28, 0.56, 1.12, and 2.8 kpc. The  $r_{\rm hm, 0}$  range is based on what is found for young massive clusters (Portegies Zwart, McMillan & Gieles 2010). The minimum  $M_{\rm cl, 0}$  is chosen such that after stellar mass loss the mass is always above the mass of the cluster. The maximum mass was chosen such that less than 20 per cent of all stars in the entire galaxy originated from the star cluster, which is a reasonable upper limit (Larsen, Strader & Brodie 2012; Larsen et al. 2014).

For all clusters we adopted circular orbits. This favours the survival of clusters in cusped profiles because eccentric orbits reach closer to the centre of the galaxy where clusters are less likely to survive. (Our assumption that the host dwarf galaxy has a spherical potential similarly favours a cusped profile because in triaxial models there are no circular orbits and only the more damaging radial orbits are allowed.)

Contenta et al. (2017) show how the observations of faint star clusters – like Eri II's star cluster – can be affected by primordial binaries and the retention fraction of black holes, together with observational biases. In our simulations, we did not vary these aspects, which could be degenerate with the initial conditions of the clusters, nor did we vary the initial density profile of the clusters.

Eri II's star cluster is observed at a projected distance  $D_g^{cl} = 45 \text{ pc}$  from the centre of Eri II. Thus, we also need to take into account the probability for the cluster to be observed at that radius in the total likelihood. We estimate the probability  $P(D_g < D_g^{cl}|R_g)$  to observe a cluster (on a circular orbit) within  $D_g^{cl}$  for a given  $R_g$ , assuming a random inclination of the orbital plane with respect to the observer. To compute  $P(D_g < D_g^{cl}|R_g)$ , first we estimate the angle  $\varphi(i, R_g)$ , which defines the angle in which the cluster is observed to be within  $D_g^{cl}$  during 1/4 of an orbit (see Fig. 3), where  $i \in [0, \pi/2]$  is the angle between the pole of the orbit and the line of sight. For circular orbits, the angle  $\varphi(i, R_g)$  is given by

$$\varphi(i, R_{g}) = \begin{cases} \frac{\pi}{2} - \arcsin\left(\frac{\sqrt{1 - D_{g}^{cl}/R_{g}}}{\sin i}\right) & R_{g} > D_{g}^{cl} \\ \frac{\pi}{2} & R_{g} < D_{g}^{cl} \end{cases}.$$
 (2)



**Figure 3.** Schematic representation of two projected orbits with different inclinations of their orbital plane *i* (solid black lines). Eri II's cluster is observed to be 45 pc from the centre of Eri II in projection (dashed red line). We consider that a cluster can be observed as Eri II's star cluster if its orbit is within 45 pc (solid red line). For a given *i*, a larger distance from the centre results in a smaller  $\varphi(i, R_g)$  (see equation 2). Therefore, clusters that orbit in the outskirts of Eri II are unlikely to be observed near the centre.

Secondly, we integrate  $\varphi(i, R_g)$  with respect to  $\cos i$  because for random inclinations of the orbital plane,  $\cos i$  is uniformly distributed. We then divide by a normalization angle,  $\pi/2$ , because  $\varphi(i, R_g)$ considers only 1/4 of an orbit, (see Fig. 3) and we obtain

$$P(D_{\rm g} < D_{\rm g}^{\rm cl} | R_{\rm g}) = \frac{2}{\pi} \int_0^1 \varphi(i, R_{\rm g}) \,\mathrm{d}\cos i.$$
 (3)

By definition,  $0 \le P(D_g < D_g^{cl} | R_g) \le 1$ .

To compare the *N*-body simulations with the observational data, we assumed a stellar mass-to-light ratio of  $M/L_V = 2$ , appropriate for old, metal-poor stellar populations (e.g. McLaughlin & van der Marel 2005), obtaining  $M_{\rm ob} = 4.3 \times 10^3 \,\mathrm{M_{\odot}}$ . We multiply the observed half-light radius ( $r_{\rm hl}$ ) by 4/3 to correct for projection effects (Spitzer 1987), to get an estimate for the 3D half-mass radius  $r_{\rm h, ob} = 17.3 \,\mathrm{pc}^6$  of Eri II's star cluster. To find the model that best fits the observational data, we maximize the likelihood for the fitting parameters ( $r_{\rm hm, 0}$ ,  $M_{\rm cl, 0}$ , and  $R_{\rm g, 0}$ ). The log-likelihood function is

$$\ln \mathcal{L} = -\frac{(r_{\rm h,ob} - r_{\rm hm})^2}{2\sigma_{\rm r}^2} - \frac{\log^2 (M_{\rm ob}/M_{\rm cl})}{2\sigma_{\log(M)}^2} + \ln P(D_{\rm g} < D_{\rm g}^{\rm cl}|R_{\rm g}), (4)$$

where  $\sigma_r = 1.33$  pc and  $\sigma_{\log(M)} = 0.24^7$  are the uncertainties derived from the observation (Crnojević et al. 2016). The last term in the equation above is given by equation (3) and acts as a prior to our likelihood given that it penalizes models that are less likely to be observed simply due to geometrical constraints. Additional free parameters, such as the time when the cluster appears at 45 pc, could be included; however, the age and the orbit of the cluster are unknown. Whereas, the time span when the cluster reproduce

 $^{7}\sigma_{\rm r}$  is the uncertainty on the 3D half-mass radius; whereas  $\sigma_{\log(M)}$  is estimated assuming  $M/L_V = 2$ .

the observations would favour the clusters in the cored galaxy (see Section 3.2), without changing the main results. Therefore we took the simplest approach including only the geometric effects.

By computing  $r_{\rm hm}$ ,  $M_{\rm cl}$  (defined as the sum of the mass of all stars within the tidal radius of the cluster) and  $R_{\rm g}$ , we calculate the likelihood (equation 4) for each output time of the simulation.

#### 2.5 Estimation of the number density profile

To study the structural properties of the clusters in the *N*-body simulations, we used a maximum likelihood fit following the procedure described in Martin, de Jong & Rix (2008). We model the stellar distribution of the clusters using 2D elliptical Plummer and spherical, single-component, King models (King 1966). We fit the models with a Monte Carlo Markov Chain (MCMC) method (EMCEE code, Foreman-Mackey et al. 2013) to optimize the following parameters: projected half-number radius, ellipticity, position angle, and surface density background for the Plummer models; and half-number radius, central dimensionless potential, and background surface density for the King models.<sup>8</sup>

#### 2.6 Qualitative estimation of the size of Eri II's star cluster

We can estimate the maximum radius that a star cluster can have, which corresponds to the situation in which the cluster fills the Roche volume. As described by Hénon (1961), a star cluster in a tidal field evolves at a constant mean density once it fills the Roche volume, which means that the ratio between the  $r_{\rm hm}$  and the Jacobi radius ( $r_{\rm J}$ ) is constant:  $r_{\rm hm}/r_{\rm J} \simeq 0.15$ . The Jacobi radius is defined in King (1962) as

$$r_{\rm J} = \left(\frac{GM_{\rm cl}}{\Omega^2 - \frac{\partial^2 \phi}{\partial R_g^2}}\right)^{\frac{1}{3}},\tag{5}$$

where  $\Omega$  is the angular velocity of the cluster around the galaxy centre,  $\phi$  is the potential of the galaxy, and *G* is the gravitational constant. In Fig. 4, we show that if we use the Dehnen models chosen in Fig. 2 and  $M_{cl} = M_{ob}$ , we can estimate the tidal radius of the cluster as a function of  $R_g$ , assuming that the cluster is on a circular orbit. From this figure, using the ratio  $r_{hm}/r_J \simeq 0.15$ , we find that in a cusped galaxy at  $R_g = 45$  pc (red line), a cluster can be at most as large as  $r_{hm} \sim 1.5$  pc, whereas in a cored galaxy it can be substantially larger ( $r_{hm} \sim 6$  pc).

In practice, however, the ratio  $r_{\rm hm}/r_{\rm J}$  depends on the galactic potential and the number of stars in the cluster. Giersz & Heggie (1997) found that depending on these, it can be as high as  $r_{\rm hm}/r_{\rm J} = 0.4$ . For this reason, we require full *N*-body simulations to obtain quantitative constraints on the central DM density slope in Eri II. None the less, Fig. 4 does give us the correct intuition that clusters will be larger in cored rather than cusped galaxies.

#### **3 RESULTS**

#### 3.1 Cusp versus core

The main result of our investigation is that the presence of a cored DM profile in Eri II allows a star cluster to not only survive in the centre of the galaxy, but also to expand up to  $r_{\rm hm} \simeq 17 \, {\rm pc}$  (i.e.  $r_{\rm hl} \simeq$ 

<sup>&</sup>lt;sup>6</sup> Assuming that light traces mass, which is not necessarily true if the cluster is mass segregated.

<sup>&</sup>lt;sup>8</sup> We used the LIMEPY code (Gieles & Zocchi 2015) to compute the projected density profiles of King models (https://github.com/mgieles/limepy).



**Figure 4.** Estimation of the tidal radius  $(r_J)$  of Eri II's star cluster for a cored (green lines) and cusped (black lines) DM model for Eri II. The red and blue lines mark the observed position of the cluster and the half-light radius of the Eri II, respectively. We assume that the cluster has a fixed mass and is on a circular orbit. Notice that the cored models allow for the cluster to have much a larger size in the inner part of the galaxy than the cusped models.

13 pc), in excellent agreement with observations of Eri II's lone star cluster. By contrast, a cusped DM profile gives a poorer fit overall and requires special conditions that have to be satisfied. In Fig. 5, we show a schematic representation of a simulated cluster in a cusped galaxy (on the left-hand side) and a cored galaxy (on the right-hand side) at times when they best reproduce the observations (shown in the middle). As can be seen, in the cored galaxy (right-hand panel), the star cluster (green) stalls at a radius  $\sim$ 45 pc from Eri II's centre (see the zoomed image in the blue circle that shows its orbital decay and stalling in red). In this case, no special inclination or time are required to reproduce Eri II's star cluster. Notice also that the

cluster appears visibly extended, similarly to Eri II's cluster, and that it shows little to no tidal tails, as expected for a cluster orbiting in a constant density core (e.g. Petts et al. 2016). By contrast, in the cusped case (left), the cluster must orbit much farther ( $R_g > 1$  kpc) from Eri II's centre in order to survive. Now its orbit will only be close enough to Eri II in projection when the red circle lies inside the two solid yellow lines. This happens when the cluster orbits with a high inclination (i > 87:43) of the orbital plane, and is in a particular orbital phase (that occurs for <3 per cent of the total orbit time). In the cusped galaxy, the cluster is denser than in the cored case and less consistent with the data for Eri II's cluster. There are also now two visible tidal tails, as expected for a cluster orbiting in a cusped background.

In Fig. 6, we show the maximum likelihood of our models as a function of  $R_{g,0}$ , varying all the other parameters  $(M_{cl}, r_{hm}, and t)$ , without (left-hand panel) and with (middle panel)  $P(D_g < D_g^{cl}|R_g)$  in the likelihood; and as a function of time, t (varying all the other parameters and including  $P(D_g < D_g^{cl}|R_g)$ , right-hand panel). The shaded grey and green regions show the 68 per cent confidence intervals for the parameters  $R_{g,0}$  and t for the cusped (grey) and cored (green) galaxy, respectively. (Assuming that Wilk's theorem is valid, we used the likelihood ratio to estimate the confidence intervals (Wilks 1938); we do not allow our reported confidence interval to be smaller than the distance between two data points.)

For the clusters in the cored galaxy, the likelihood is bimodal because it is possible to fit the data if the cluster is either in the inner or outer region of the galaxy (see the left-hand panel). For  $R_{g,0} = 0.56$  kpc, the tidal radius of the cluster is close to its minimum and there it is more difficult to increase the cluster's  $r_{hl}$  up to the observed 13 pc. This leads to the dip in the likelihood at this point. However, including the probability  $P(D_g < D_g^{cl}|R_g)$  of observing the cluster at the right position (middle panel) breaks this bimodality, favouring the orbits near the centre with lower  $R_{g,0}$ .

For the clusters evolving in the cusped galaxy, no star cluster can survive in the inner galaxy  $R_{g,0} < R_{1/2}$  for more than 5 Gyr and the likelihood is, therefore, zero for all clusters in that region of parameter space chosen in this study. Considering more massive clusters initially does not necessarily lead to a higher probability of survival, because of the increased importance of dynamical friction. Clusters that orbit outside the scale radius ( $R_{g,0} \gtrsim 1$  kpc) have comparable likelihoods in the cusped and cored models (see left-hand and



Figure 5. Schematic representation of the cluster orbiting in a cusped Eri II (on the left-hand side) and a cored Eri II (on the right-hand side) at times when they best reproduce the observations (Crnojević et al. 2016; shown in the middle). On the top right-hand side, we show a zoom-in of the simulation in the cored galaxy after 6.3 Gyr. The effect of dynamical friction and stalling can be seen in the red lines that depict the cluster's orbit. In the cusped case, the cluster can only survive in the outskirts of Eri II, whereas in the cored case, the cluster can survive in the central region where it is much more likely to match the observations.



**Figure 6.** Comparison of the maximum likelihood of the cored and cusped *N*-body models. The left-hand and middle panels show the maximum likelihood as a function of the initial value of  $R_g$  ( $R_{g,0}$ ) without (left-hand panel) and with (middle)  $P(D_g < D_g^{cl}|R_g)$ . The right-hand panel shows the maximum likelihood as a function of time, *t*, also with  $P(D_g < D_g^{cl}|R_g)$ . The black solid and green dashed lines are for cusp and core models, respectively. The shaded areas show the 68 per cent confidence intervals for  $R_{g,0}$  and *t* for the cored (in green) and cusped (in black) models. The dotted vertical lines show the best-fitting values for  $R_{g,0}$  and *t*. Notice that the cored models have a higher likelihood than the cusped models, especially once the probability of observing the cluster at its current projected distance,  $P(D_g < D_g^{cl}|R_g)$ , is included. As explained in Section 2.2, we studied only the clusters that survive for more than 5 Gyr.

middle panels) because they are similar by construction at large radii (compare the green and black dashed lines in the right-hand panel of Fig. 2). (A measurement of the 3D position of the cluster in Eri II would allow us to completely rule out cusped models. However, to measure a 1 kpc offset from Eri II, an accuracy of 0.006 mag is needed. Even with RR Lyrae, it is only possible at present to reach an accuracy of 0.05 mag.)

The right-hand panel of Fig. 6 shows the maximum likelihood at different times. The black line is for clusters in a cusped galaxy, for which the best fits are the models between 6.5 and 8 Gyr old. The green dashed line is for the cored DM profile, for which the best fits are all models with  $t \gtrsim 7$  Gyr. In the cored galaxy, the best-fitting models are those that survive in the inner part of the galaxy where they can easily expand up to ~17 pc and survive for 14 Gyr. For the cusped galaxy, we can only reproduce the observed properties of Eri II star cluster for a small amount of time and for a small range of  $M_{\rm cl, 0}$  and  $r_{\rm hm, 0}$ . To reproduce Eri II's star cluster in a cusped galaxy, it must therefore have an age of 6.5–8 Gyr. This provides another testable prediction that could fully rule out cusped models.

Finally, even if we accept a high inclination of the orbital plane and the required orbital phase for the cusped case, its star clusters give a poorer fit to the observations than the cored case, because the clusters are not able to expand enough to match the data. We discuss this in more detail, next.

#### 3.2 Best-fitting star cluster models

The best-fitting model in the cusped galaxy has  $M_{cl,0} \sim 3.2 \times 10^4 \,\mathrm{M_{\odot}}$ ,  $r_{\rm hm,0} = 5 \,\mathrm{pc}$ , and  $R_{\rm g,0} = 1.12 \,\mathrm{kpc}$ . The best-fitting model in the cored galaxy has  $M_{cl,0} \sim 1.9 \times 10^4 \,\mathrm{M_{\odot}}$ ,  $r_{\rm hm,0} = 10 \,\mathrm{pc}$ , and  $R_{\rm g,0} = 0.14 \,\mathrm{kpc}$ . Fig. 7 shows the evolution of  $M_{\rm cl}$ ,  $r_{\rm hm}$ ,  $R_{\rm g}$ , and  $P(D_g < D_g^{\rm cl} | R_g)$  for these two models. The red shaded areas show the 68 per cent confidence intervals of the data. (We only have a lower limit for the age of the cluster, because stars younger than 5 Gyr have not been observed; see Section 1.) In Fig. 7, we show that the properties of the star cluster in a cored DM profile reproduce the properties of the observed star cluster for all times  $\gtrsim 5 \,\mathrm{Gyr}$ , whereas in the cusped case, the cluster has to be observed at a specific time. Notice, however, that the cusped model is always at tension with the

data, with its size,  $r_{\rm hm}$ , never quite reaching high enough to match Eri II's star cluster.

As discussed in Section 1, we expect the density of the star cluster to reach an equilibrium due to relaxation-driven expansion and the tidal pruning of high-energy escaper stars. In the left-hand panel of Fig. 7, we see this process happening between 5 and 9 Gyr for the cusped model. Over this period, the cluster evolves at an approximately constant  $r_{\rm hm}/r_{\rm J}$  (Hénon 1961), where  $r_{\rm J}$  is the 'Jacobi' or tidal radius. As a result, the cluster shrinks as  $r_{\rm hm} \propto M^{1/3}$  while it loses mass, and it only has a large  $r_{\rm hm}$  for a limited time (few Gyr). The cluster in the cored galaxy also expands, but at  $\gtrsim 5$  Gyr, the star cluster evolves at roughly constant  $M_{cl}$  and  $r_{hm}$ . This is because the escape rate is very small in compressive tides, and the cluster evolves towards a near isothermal equilibrium configuration, in which the cluster is in virial equilibrium with the tides (Yoon, Lee & Hong 2011; Bianchini et al. 2015; Webb, Patel & Vesperini 2017). This implies that it is more likely to find a cluster in this phase, because it can be in this quasi-equilibrium configuration for a long time ( $\gtrsim 10$  Gyr). The asymptotic value of  $r_{\rm hm}$  of the cluster in the cored galaxy is in excellent agreement with the data for Eri II's star cluster (red shaded region). We note that in our N-body model the cluster density within  $r_{\rm hm}$  evolves to approximately the same value as the (uniform) DM density, hence the cluster density is literally probing the DM density.

#### 3.3 Predicted cluster number density profiles

Fig. 8 shows the stellar number density profiles of the best-fitting models in the cusped (left-hand panel) and cored (right-hand panel) case. Crnojević et al. (2016) find the structural parameters of Eri II's star cluster by fitting a Sérsic profile to its surface brightness as measured from integrated photometry. It is possible to similarly derive a surface brightness profile from the *N*-body simulations; however, it proved challenging to directly compare the models to the data. Analysing the image from Crnojević et al. (2016), we found that the result is very sensitive to the number of bins used, the subtraction of background sources, and which bright stars are masked – all of which can change the result of the fitting. Therefore, for our analysis, we used a different approach in which the data from the *N*-body



**Figure 7.** Left-hand panel Evolution of  $M_{cl}$ ,  $r_{hm}$ ,  $R_g$ , and the probability to observe a cluster in projection at  $D_g \le 45pc$ , for the best-fitting cusped model. Right-hand panel: as left-hand panel but for the best-fitting cored model. The red shaded regions show the 68 per cent confidence intervals of the data. (We only have a lower limit for the age of the cluster, because stars younger than 5 Gyr have not been observed; see Section 1.)



**Figure 8.** Left-hand pane number density profile of the best cusp model at 7.5 Gyr. Right-hand panel: number density profile of the best core model at 12 Gyr. The solid red and dashed blue lines indicate the best-fitting Plummer and King profiles, respectively. The number density of background star is estimated using the number density profile of Eri II (Bechtol et al. 2015). On the right-hand panel, the number of background stars is higher because the cluster sits in the inner part of Eri II.

models are not binned. We used only bright stars (massive stars) that are observable. In our case, we chose only stars that are more massive than  $0.75 \text{ M}_{\odot}$ .<sup>9</sup> Furthermore, we included the background stars using the number density profile of Eri II reported in Bechtol et al. (2015), assuming that the stars are uniformly distributed in our simulated field of view.

As can be seen in Fig. 8, a star cluster that evolves in a DM cusp has a different density profile than a star cluster that evolves in a DM core. In the cored galaxy, clusters have a lower concentration parameter,  $c = 0.55 \pm 0.16$ , compared to the cluster in the cusped galaxy ( $c = 0.83 \pm 0.07$ ). Here,  $c \equiv \log(r_t/r_0)$ , where  $r_t$  is the truncation radius and  $r_0$  is the King/core radius. This means that

<sup>9</sup> This mass limit was derived from the observational limit reported in Crnojević et al. (2016) using PARSEC's isochrones v1.2S (Bressan et al. 2012).

the core of the cluster is larger (for a given  $r_{\rm hl}$ ) if it evolves in a DM core. From deeper imaging, it may be possible to derive the projected density profile of the cluster, allowing for a better comparison with our *N*-body simulations.

# 3.4 The effect of varying the mass, concentration, and central logarithmic cusp slope of Eri II's DM halo

In Section 2.2, we showed that for DM haloes that lie on the  $M_{200}$ - $c_{200}$  relation, large changes in  $M_{200}$  produce only a small change in their inner DM density. Here, we test whether we are able to detect such small changes to obtain a constraint on  $M_{200}$  from the survival and properties of Eri II's star cluster alone. To test this, we performed an additional 10 simulations varying  $M_{200}$  over the range  $[1.4 \times 10^8, 10^{11}] M_{\odot}$ . [The upper limit of this range is already



**Figure 9.** The effect of varying the mass, concentration, and central logarithmic cusp slope of Eri II's DM halo. The green and grey lines are the core and cusp models adopt for the simulations (see Fig. 2). The cyan lines are the upper and lower envelope of the additional models we ran varying  $M_{200}$  and  $c_{200}$  and the red and orange lines are the models varying the inner logarithmic cusp slope. Models for which no viable solution for Eri II's star cluster could be found have shaded lines ( $\gamma = 0.5$  and 1).

ruled out by the stellar kinematic measurements for Eri II (Li et al. 2017), but serves to test our sensitivity to  $M_{200}$ .] These models are shown by the cyan lines in Fig. 9.

As anticipated in Section 2.2, we found that we are not sensitive to even large changes in  $M_{200}$  and  $c_{200}$  so long as our Eri II DM halo has a central DM core. By selecting an appropriate  $M_{cl, 0}$ ,  $r_{hm, 0}$ , and  $R_{g, 0}$ , we were able in all cases to reproduce the observations within  $1\sigma$ , similarly to the right-hand panel of Fig. 7.

We then tested our sensitivity to the inner logarithmic DM density slope at a fixed DM halo mass of  $M_{200} = 10^9 \,\mathrm{M_{\odot}}$ , with a concentration set by the  $M_{200}$ - $c_{200}$  relation from Dutton & Macciò (2014). We explored two coreNFW models with n = 0.7 and 0.5, corresponding to Dehnen models (see equation 1) with  $(\gamma, M_0,$  $r_0$  = (0.25, 8.11 × 10<sup>8</sup> M<sub>☉</sub>, 1.363 kpc) and ( $\gamma$ ,  $M_0$ ,  $r_0$ ) = (0.5,  $9.55 \times 10^8 \,\mathrm{M_{\odot}}$ , 1.715 kpc), respectively. These models are shown by the orange and pink lines in Fig. 9. We found that, with an inner density slope of  $\gamma = 0.25$ , we were still able to find star clusters that survive for longer than 5 Gyr and reproduce the observations within  $2\sigma$ , in good agreement with recent results from Amorisco (2017). For the galaxy with  $\gamma = 0.5$ , only one cluster (with  $R_{g,0} = 0.14$  kpc,  $r_{\rm hm, 0} = 5 \,\mathrm{pc}$  and  $M_{\rm cl, 0} \sim 32\,000 \,\mathrm{M_{\odot}}$ ) survived for more than 5 Gyr. However, this cluster gave a poor match to Eri II's star cluster since its  $r_{\rm hm}$  expanded up to 12 pc and then shrank as the cluster's orbit decayed to the centre of the galaxy. A larger inner density profile slope means a smaller tidal radius for the star cluster and, thus - all other parameters being equal - a shorter dissolution time.

#### 3.5 A nuclear star cluster in Eri II?

Eri II's star cluster is offset from the photometric centre of Eri II by  $\sim$ 45 pc (Crnojević et al. 2016). However, given the uncertainties on the photometric centre of Eri II, we consider here the possibility



**Figure 10.** Evolution of  $r_{hl}$  for the clusters in the centre of a cusped (black lines) and cored (green lines) galaxy, with  $r_{hm,0} = (1, 5, 10)$  pc. The red shaded region shows the 68 per cent confidence intervals of the data.

that Eri II's star cluster is, in fact, a nuclear star cluster, defining the centre of the galaxy. A star cluster at the centre of a galactic potential will expand due to two-body relaxation, but without the limiting tidal field. Thus, in a cusped galaxy, a cluster that is tidally destroyed close to the centre of the galaxy (for example, the clusters in the cusped models with  $R_{g,0} = 0.14$  kpc; see Section 3.2) may still survive if placed at  $R_{g,0} = 0.0$  kpc. As pointed out by Amorisco (2017), this could provide a route to Eri II having a DM cusp without destroying its low density star cluster. To test this, we run six additional simulations of a star cluster with  $M_{cl,0} \sim 25000 \text{ M}_{\odot}$ and  $r_{\text{hm},0} = (1, 5, 10)$  pc, set up to lie at the centre<sup>10</sup> of the cored and cusped Eri II DM haloes described in Section 2.2.

In Fig. 10, we show the evolution of  $r_{hl}^{11}$  for these simulations in a cored (green lines) and a cusped (black lines) DM halo. In the cusped case, for  $r_{\rm hm, 0} = 10 \, \rm pc$ ,  $r_{\rm hl}$  does not expand because the cluster is mainly DM dominated and so the cluster stars trace the underlying DM potential. If Eri II's star cluster formed in the centre of Eri II, it must have formed with a size similar to that observed today, but with almost double its current mass.<sup>12</sup> In Fig. 11, we show the velocity dispersion,  $\sigma_v$ , estimated for observable stars within  $r_{\rm hl}$ , for the simulations with  $r_{\text{hm}, 0} = 10 \text{ pc}$  in a cusped (black lines) and cored (green lines) galaxy. In the N-body simulations, both  $M_{cl}$  and the mass of the galaxy  $(M_g)$  within  $r_{\rm hl}$  are known. Thus, using the 'Jeans estimator' formula from Walker et al. (2009), we can estimate the  $\sigma_v$  due to  $M_{cl}$  ( $\sigma_v(M_{cl})$ ; dashed lines), and due to the combined mass of the cluster and the galaxy ( $\sigma_v(M_{cl} + M_g)$ ; solid lines). From this, we conclude that if Eri II has a DM cusp and hosts a nuclear star cluster, then its star cluster will be DM dominated, with a velocity

<sup>&</sup>lt;sup>10</sup> We set up these star clusters as Plummer spheres embedded selfconsistently in their host Dehnen DM haloes, using the MKSPHERICAL program from the AGAMA framework (https://github.com/GalacticDynamics -Oxford/Agama; Vasiliev 2018; see Vasiliev 2017, for another application of this method).

<sup>&</sup>lt;sup>11</sup> This is derived by multiplying  $r_{\rm hm}$  of the observable stars (defined as being only those stars more massive than 0.75 M<sub> $\odot$ </sub> and excluding any dark remnants) by 3/4 to correct for projection effects.

<sup>&</sup>lt;sup>12</sup> A cluster in the centre of a cusped galaxy loses mass mainly due to stellar evolution.



**Figure 11.** Evolution of  $\sigma_v$  for clusters with  $r_{\text{hm},0} = 10 \text{ pc}$ , in the centre of a cored (green lines) and cusped (black lines) galaxy. The shaded lines represent the  $\sigma_v$  of the observable stars within  $r_{\text{hl}}$ , estimated from their line-of-sight velocity. The solid and dashed lines are the inferred  $\sigma_v$  using the 'Jeans estimator' from Walker et al. (2009). For the dashed lines, we used  $M_{\text{cl}}$  within  $r_{\text{hl}}$ , whereas for the solid lines we use the sum  $M_{\text{cl}}$  and the mass of the galaxy ( $M_g$ ) within  $r_{\text{hl}}$ .

dispersion<sup>13</sup>  $\sigma_v > 2.5 \text{ km s}^{-1}$ . By contrast, if Eri II has a DM core, its star cluster will have a much lower dispersion of  $\sigma_v < 1.0 \text{ km s}^{-1}$ . These results are in good agreement with Amorisco (2017).

Although we have found viable models where Eri II's star cluster sits at the very centre of a dense DM cusp, we emphasize that – even without a measurement of  $\sigma_v$  – we disfavour these. First, Eri II's star cluster is observed to be clearly offset from the photometric light centre of Eri II. Secondly, our cored model in Section 3.1 naturally reproduces Eri II's star cluster properties without any fine tuning. If Eri II's star cluster sits at the centre of a dense DM cusp, then its properties must be set by its birth properties, requiring more fine tuning than for the cored case.

#### **4 DISCUSSION**

Our key result is that we favour a DM core over a cusp in the ultra-faint dwarf galaxy Eri II. In models with a DM cusp, Eri II's star cluster is rapidly destroyed by tides, whereas in cored models the star cluster survives for more than a Hubble time, naturally reaching an asymptotic size and mass consistent with observations. We found that this occurs for logarithmic DM cusp slopes shallower than  $\gamma = 0.25$ , where  $\gamma$  is the central exponent in the Dehnen profile (equation 1), independently of large changes in the assumed DM halo mass or concentration. The only hope for retaining a DM cusp in Eri II is if its star cluster lies at the very centre of the cusp. We found that such a model can work, but is disfavoured by the observed offset between Eri II's photometric light peak and the projected position of its star cluster. Such a model could be completely ruled out if the velocity dispersion of Eri II's star cluster is observed to be  $\sigma_v < 1.0 \,\mathrm{km \, s^{-1}}$ . These results are in excellent agreement with a recent study by Amorisco (2017).

Our mass model for Eri II has a DM core size set by the projected half-light radius of the stars  $R_{1/2} \sim 0.28$  kpc (see Fig. 2). However, the data only require that there is a DM core where we see Eri II's star cluster today, at a projected distance of 45 pc from the photometric centre of Eri II. Dynamical friction stalling occurs when the tidal radius of the star cluster approximately matches its galactocentric distance (Read et al. 2006a; Goerdt et al. 2010; Petts et al. 2015, 2016). From this, we can derive a minimum DM core size for Eri II of  $r_c > 45$  pc. In this section, we explore what such a DM core means for galaxy formation and the nature of DM.

#### 4.1 Dark matter heating

The size and density of the DM core we find in Eri II is in excellent agreement with predictions from the 'DM heating' model of R16. However, in the R16 model, such a complete DM core would require several Gyr of star formation that may be inconsistent with Eri II's stellar population (see Section 1). However, core formation can be made more efficient if it occurs at high redshift when Eri II's DM halo was less massive (Madau et al. 2014), or if it owes primarily to angular momentum transfer from cold gas clumps sinking by dynamical friction to the centre of the dwarf (El-Zant, Shlosman & Hoffman 2001; Nipoti & Binney 2015). Given these complications, following Peñarrubia et al. (2012), R16, and Read et al. (2017), we focus here on the energy required to unbind Eri II's DM cusp:

$$\frac{\Delta E}{\Delta W} = \frac{M_*}{\langle m_* \rangle \Delta W} \xi \epsilon_{\rm DM},\tag{6}$$

where  $\Delta E$  is the total integrated SN energy,  $\Delta W$  is the energy required to unbind the DM cusp,  $M_*$  is the stellar mass,  $\langle m_* \rangle = 0.83$ is the mean stellar mass,  $\xi = 0.009$  78 is the fraction of mass in stars that go SN (i.e. those with mass  $m_* > 8 \text{ M}_{\odot}$ ), and  $\epsilon_{\text{DM}} = 0.0025$ is the coupling efficiency of the SNe energy to the DM. We assume a Chabrier initial stellar mass function over the stellar mass range  $0.1 < m_*/\text{M}_{\odot} < 100$  (Chabrier 2003). We assume a coreNFW profile when calculating  $\Delta W$  and we take  $\epsilon_{\text{DM}}$  from the simulations in R16. As such, our results are only useful in assessing, at an order-of-magnitude level, whether there is sufficient SN energy in Eri II's stellar population to form its apparent central DM core (e.g. Maxwell, Wadsley & Couchman 2015).

In Fig. 12, we plot  $\Delta E/\Delta W$  as a function of the DM core size  $r_c$ . The horizontal dashed line marks  $\Delta E/\Delta W = 1$ . Above this line, there is enough integrated SN energy to unbind the cusp; below there is insufficient energy. The vertical green line marks the minimum core size,  $r_{c, \min} = 45$  pc set by the current projected position of Eri II's star cluster. The vertical blue line marks the core size assumed in this work,  $r_c = R_{1/2} = 0.28$  kpc. The black and orange shaded regions assume a DM halo mass of  $M_{200} = 5 \times 10^8 \text{ M}_{\odot}$  with a stellar mass  $M_* = 8.3^{+5.1}_{-4.2} \times 10^4 \text{ M}_{\odot}$  (Bechtol et al. 2015, assuming three times their uncertainties), and a concentration parameter of  $c_{200} = 23$  and  $c_{200} = 14$ , respectively. These are the upper and lower 68 per cent confidence intervals of  $c_{200}$  in  $\Lambda$ CDM (Dutton & Macciò 2014). (Note that the R16 simulations assume the upper envelope of this  $c_{200}$  range and so make core formation maximally difficult.)

As can be seen in Fig. 12, there is plenty of energy to produce the minimum core size  $r_c = 45$  pc independently of the assumed  $c_{200}$  or  $M_*$ . However, for the assumed DM halo mass and SN energy coupling efficiency that we assume here, a low  $c_{200}$  and high  $M_*$  for Eri II are required to produce a core as large as  $r_c = R_{1/2} = 0.28$  kpc.

Although the R16 models are able to produce a DM core in Eri II, most other simulations in the literature to date do not find DM

<sup>&</sup>lt;sup>13</sup> Note that none of the clusters in our cusped simulations have an  $r_{\rm hl}$  large enough to be consistent with observations (see Fig. 10). However, in a DM cusp, the enclosed mass goes as  $M \propto r^2$  and so  $\sigma_v^2 \propto r$ . Thus, increasing the size of the cluster will increase  $\sigma_v$ , which is why our results provide a lower bound on the dispersion.



**Figure 12.** The energy required to unbind Eri II's DM cusp as a function of the DM core size,  $r_c$ . We assume for this plot a Chabrier IMF (Chabrier 2003) and a coupling efficiency between SNe and DM of  $\epsilon_{\rm DM} = 0.25$  per cent (R16). The horizontal dashed line marks  $\Delta E/\Delta W = 1$ . Above this line, there is enough integrated SN energy to unbind the cusp; below there is insufficient energy. The vertical green line marks the minimum core size,  $r_{\rm c, min} = 45$  pc set by the current projected position of Eri II's star cluster. The vertical blue line marks the core size assumed in this work,  $r_{\rm c} = R_{1/2} = 0.28$  kpc. The black and orange shaded regions assume a DM halo mass of  $M_{200} = 5 \times 10^8 \,\mathrm{M_{\odot}}$  with a stellar mass  $M_* = 8.3^{+5.1}_{-4.2} \times 10^4 \,\mathrm{M_{\odot}}$  (Bechtol et al. 2015, assuming three times their uncertainties), and a concentration parameter of  $c_{200} = 23$  and  $c_{200} = 14$ , respectively. These are the upper and lower 68 per cent confidence intervals of  $c_{200}$  in  $\Lambda$ CDM (Dutton & Macciò 2014).

cores in haloes below  $M_{200} \sim 7.5 \times 10^9 \,\mathrm{M_{\odot}}$  (e.g. Chan et al. 2015; Oñorbe et al. 2015; Tollet et al. 2016, but see Madau et al. 2014). We can understand the origin of this discrepancy from Fig. 1. As can be seen, the R16 simulations (magenta squares) produce a similar total stellar mass to the Chan et al. (2015) (yellow squares) and Wang et al. (2015) (green squares) simulations but in haloes an order of magnitude lower in mass. [Note that the Wang et al. (2015) simulations are the same as those discussed in Tollet et al. (2016).] This is why cusp-core transformations in the R16 simulations are energetically feasible. The simulations that find no cores below  $M_{200} \sim 7.5 \times 10^9 \,\mathrm{M_{\odot}}$  form almost no stars below this mass scale and so do not have enough integrated SN energy to unbind the DM cusp (see also the discussion in Read et al. 2017). Understanding this apparent discrepancy between the data and simulations in Fig. 1, and the differences between numerical models, remains an open and important problem.

If Eri II is found to have a purely old stellar population, with too few SNe to provide the energy required to unbind its cusp, then we may be forced to move to models beyond  $\Lambda$ CDM. We consider some of these, next.

#### 4.2 Beyond ACDM

The small-scale puzzles in  $\Lambda$ CDM (see Section 1) have motivated the community to consider alternative models. Some of these can

solve the cusp-core problem without recourse to baryonic 'DM heating'. The most popular of these to date is SIDM (Spergel & Steinhardt 2000). The latest SIDM models have a velocity-dependent interaction cross-section  $\sigma/m(v/v_m)$ , where  $\sigma$  is the DM interaction cross-section, *m* is the mass of the DM particle, and  $v_m$  is a velocity scale (e.g. Kaplinghat et al. 2016; Schneider et al. 2017). This is required for the models to be consistent with constraints from weak lensing on galaxy cluster scales that favour  $\sigma/m < 0.5 \text{ cm}^2 \text{ g}^{-1}$  (e.g. Harvey et al. 2015), while maintaining a much higher  $\sigma/m \sim 2 - 3 \text{ cm}^2 \text{ g}^{-1}$  is required to produce large DM cores in nearby gas rich dwarf galaxies (e.g. Kaplinghat et al. 2016).

Since our focus here is on one low-mass dwarf, we consider instead a simple *velocity -independent* SIDM model. Following Schneider et al. (2017), the velocity-independent interaction crosssection can be written as

$$\frac{\sigma}{m} = \frac{\sqrt{\pi}\,\Gamma}{4\rho_{\rm NFW}(r_{\rm c})\sigma_v(r_{\rm c})},\tag{7}$$

where  $r_c$  is the coreNFW DM core size (R16),  $\rho_{NFW}$  is the *initial* DM density at  $r_c$ ,  $\Gamma = 0.4$  Gyr<sup>-1</sup> is the SIDM interaction rate (taken from coreNFW fits to numerical simulations in SIDM; Schneider et al. 2017), and

$$\sigma_{\nu}(r_{\rm c})^2 = \frac{G}{\rho_{\rm NFW}} \int_{r_{\rm c}}^{\infty} \frac{M_{\rm NFW}(r')\rho_{\rm NFW}(r')}{r'^2} \mathrm{d}r' \tag{8}$$

is the velocity dispersion of the DM at  $r_c$  (assuming that this model is isotropic). Using  $r_c > 45$  pc, we find  $\sigma/m > 0.24$  cm<sup>2</sup> g<sup>-1</sup>, which is consistent with all known SIDM constraints to date.

Another model that could explain Eri II is ultra-light axions (e.g. González-Morales et al. (2017) and references therein). Assuming an ultra-light axion mass of  $m_{\rm a} \sim 10^{-22}$  eV, we obtain for our Eri II halo model,  $r_{\rm c} \sim 0.6$  kpc, which is consistent with our minimum core size  $r_{\rm c} > 45$  pc.

Therefore, alternative DM models such as SIDM and ultra-light axions can produce a core in the ultra-faint Eri II dwarf galaxy.

#### 4.3 Implications of the initial cluster properties

The initial mass of the star cluster in the cored galaxy ( $M_{\rm cl,0} \simeq$  $1.9 \times 10^4 \,\mathrm{M_{\odot}}$ ) suggests that this star cluster resembled a young massive cluster, similar to those we see in the disc of the Milky Way (e.g. Arches, Westerlund 1, NGC 3603). The initial radius  $(r_{\rm hm, 0} \simeq 10 \, {\rm pc})$  is relatively large compared to these low-redshift analogues, which have typical radii of a few pc (Portegies Zwart et al. 2010). We note that the model with  $r_{\rm hm,\,0}\simeq 5\,{\rm pc}$  expands up to  $r_{\rm hm} \sim 15\,{\rm pc}$  and fits the data reasonably well. Our models did not include primordial mass segregation in the cluster initial conditions. If we had assumed that the massive stars formed more towards the centre of the cluster, it would have expanded more as a result of stellar mass-loss (e.g. Zonoozi et al. 2017), allowing for more compact initial conditions. The present day mass of stars and stellar remnants that once belonged to the cluster is  $\sim 10^4 \,\mathrm{M_{\odot}}$ , or  $\sim$ 12 per cent of the total stellar mass in Eri II. Such a high cluster formation efficiency has been reported in other dwarf galaxies when considering metal-poor stars only (Larsen et al. 2014).

#### 4.4 Comparison with other work in the literature

Concurrent with our work, Amorisco (2017) have recently modelled Eri II's central star cluster sinking under dynamical friction, finding that it cannot survive long in a cusped potential, in good agreement with our results here (They also report similar results for the star cluster in Andromeda XXV). The key difference between our studies is that we model the internal structure of Eri II's star cluster, accounting for two-body relaxation and stellar evolution, for the first time. Amorisco (2017) used a collisionless *N*-body code that cannot capture two-body relaxation effects that drive the expansion of the cluster over time. <sup>14</sup> The key advantage of modelling the collisional effects in Eri II's star cluster is that its final mass and size then depend on the local tidal field, and, therefore, on the mass distribution at the centre of Eri II. This gives us an additional probe of the central DM density profile in Eri II that goes beyond a survival argument.

#### **5** CONCLUSIONS

We have presented a new method for probing the central DM density in dwarf galaxies using star clusters. Low-mass star clusters orbiting in the tidal field of a larger host galaxy are expected to reach an equilibrium size due to relaxation-driven expansion and the tidal pruning of high-energy escaper stars. We have used the NBODY6DF collisional N-body code, which includes stellar evolution and dynamical friction, to show that this is indeed the case. As a first application, we have applied our method to the recently discovered ultra-faint dwarf, Eri II. This has a lone star cluster that lies some  $\sim$ 45 pc from its centre in projection. Using a suite of 226 full N-body simulations of the star cluster, we showed that models with a central dark matter core (with an inner logarithmic density slope of  $\gamma < 0.25$ ) are favoured over those with a DM cusp. A DM core naturally reproduces the size and the projected position of Eri II's star cluster. By contrast, dense cusped galaxy models require the cluster to lie implausibly far from the centre of Eri II (>1 kpc), with a high inclination orbit  $(i > 87^{\circ}.43)$  that must be observed at a special orbital phase (<3 per cent of the orbital period).

Our models make several clear predictions that can be tested with deeper observations. If Eri II is cored, then

(i) the cluster can have any age older than  $\sim$ 7 Gyr (as compared to a narrow age range of 6.5 - 8 Gyr in the cusped case);

(ii) there are no tidal tails associated with the cluster;

(iii) the cluster has a low concentration ( $c \sim 0.5$  as compared to  $c \sim 0.8$  in the cusped case).

We also considered the possibility that Eri II's star cluster lies at the very centre of a DM cusp, allowing it to survive tidal disruption. This is already disfavoured by the observed offset between Eri II's photometric light peak and the projected position of its star cluster. However, such a model could be completely ruled out if the velocity dispersion of Eri II's star cluster is found to be  $\sigma_v < 1.0 \text{ km s}^{-1}$ .

We have shown that extended faint star clusters can survive at the centres of dwarf galaxies with DM cores. Such faint star clusters could be liberated from their host dwarf galaxy by Galactic tides that act more efficiently on cored dwarfs (e.g. Read et al. 2006b; Peñarrubia et al. 2010), providing an explanation for some of the recently discovered ultra-faint objects found in the Milky Way (for a discussion see Contenta et al. 2017).

<sup>14</sup> Amorisco (2017) argue that collisional effects can be ignored in extended and faint star clusters. However, this depends on the assumed initial conditions for the cluster. The initial half-mass relaxation time (Spitzer 1987) of our best-fit cluster model is ~2.2 Gyr, computed assuming  $\ln \Lambda = \ln (0.02N)$ (Giersz & Heggie 1996). Since the cluster is older than this, two-body relaxation was important during the evolution of this cluster. The presence of a DM core in the ultra-faint dwarf galaxy Eri II implies that either its CDM cusp was 'heated up' by bursty star formation or we are seeing an evidence for physics beyond CDM.

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#### REFERENCES

- Aarseth S. J., 1999, PASP, 111, 1333
- Aarseth S. J., 2003, Gravitational N-Body Simulations. Cambridge Univ. Press, Cambridge
- Agnello A., Evans N. W., 2012, ApJ, 754, L39
- Ahmad A., Cohen L., 1973, J. Comput. Phys., 12, 389
- Amorisco N. C., 2017, ApJ, 844, 64
- Battaglia G., Helmi A., Tolstoy E., Irwin M., Hill V., Jablonka P., 2008, ApJ, 681, L13
- Bechtol K., Drlica-Wagner A., Balbinot E., Pieres A., Simon J. D., Yanny B., Santiago B., The DES Collaboration, 2015, ApJ, 807, 50
- Belokurov V. et al., 2007, ApJ, 654, 897
- Bianchini P., Renaud F., Gieles M., Varri A. L., 2015, MNRAS, 447, L40
- Breddels M. A., Helmi A., 2013, A&A, 558, A35
- Bressan A., Marigo P., Girardi L., Salasnich B., Dal Cero C., Rubele S., Nanni A., 2012, MNRAS, 427, 127
- Chabrier G., 2003, ApJ, 586, L133
- Chan T. K., Kereš D., Oñorbe J., Hopkins P. F., Muratov A. L., Faucher-Giguère C.-A., Quataert E., 2015, MNRAS, 454, 2981
- Claydon I., Gieles M., Zocchi A., 2017, MNRAS, 466, 3937
- Cole D. R., Dehnen W., Read J. I., Wilkinson M. I., 2012, MNRAS, 426, 601
- Collins M. L. M. et al., 2014, ApJ, 783, 7
- Contenta F., Gieles M., Balbinot E., Collins M. L. M., 2017, MNRAS, 466, 1741
- Crnojević D., Sand D. J., Zaritsky D., Spekkens K., Willman B., Hargis J. R., 2016, ApJ, 824, L14
- de Boer T. J. L. et al., 2012, A&A, 544, A73
- Dehnen W., 1993, MNRAS, 265, 250
- Di Cintio A., Brook C. B., Dutton A. A., Macciò A. V., Stinson G. S., Knebe A., 2014, MNRAS, 441, 2986
- Dubinski J., Carlberg R. G., 1991, ApJ, 378, 496
- Dutton A. A., Macciò A. V., 2014, MNRAS, 441, 3359
- El-Zant A., Shlosman I., Hoffman Y., 2001, ApJ, 560, 636
- Evans N. W., An J., Walker M. G., 2009, MNRAS, 393, L50
- Fitts A. et al., 2017, MNRAS, 471, 3547
- Flores R. A., Primack J. R., 1994, ApJ, 427, L1
- Foreman-Mackey D., Hogg D. W., Lang D., Goodman J., 2013, PASP, 125, 306
- Gieles M., Zocchi A., 2015, MNRAS, 454, 576

- Gieles M., Baumgardt H., Heggie D. C., Lamers H. J. G. L. M., 2010, MNRAS, 408, L16
- Gieles M., Heggie D. C., Zhao H., 2011, MNRAS, 413, 2509
- Giersz M., Heggie D. C., 1996, MNRAS, 279, 1037
- Giersz M., Heggie D. C., 1997, MNRAS, 286, 709
- Goerdt T., Moore B., Read J. I., Stadel J., Zemp M., 2006, MNRAS, 368, 1073
- Goerdt T., Moore B., Read J. I., Stadel J., 2010, ApJ, 725, 1707
- González-Morales A. X., Marsh D. J. E., Peñarrubia J., Ureña-López L. A., 2017, MNRAS, 472, 1346
- Governato F. et al., 2010, Nature, 463, 203
- Harris W. E., 1996, AJ, 112, 1487
- Harvey D., Massey R., Kitching T., Taylor A., Tittley E., 2015, Science, 347, 1462
- Hénon M., 1961, Ann. d'Astrophysique, 24,
- Hénon M., 1965, Ann. Astrophys., 28, 62
- Hernandez X., Gilmore G., 1998, MNRAS, 297, 517
- Hunter J. D., 2007, Matplotlib: A 2D Graphics Environment. Available at: https://matplotlib.org/ (accessed 2016 July 21)
- Hurley J. R., Pols O. R., Tout C. A., 2000, MNRAS, 315, 543
- Hurley J. R., Tout C. A., Pols O. R., 2002, MNRAS, 329, 897
- Innanen K. A., Harris W. E., Webbink R. F., 1983, AJ, 88, 338
- Inoue S., 2009, MNRAS, 397, 709
- Inoue S., 2011, MNRAS, 416, 1181
- Jethwa P., Erkal D., Belokurov V., 2018, MNRAS, 473, 2060
- Jones E. et al., 2001, SciPy: Open Source Scientific Tools for Python. Available at: https://www.scipy.org/ (accessed 2016 July 21)
- Kaplinghat M., Tulin S., Yu H.-B., 2016, Phys. Rev. Lett., 116, 041302
- King I., 1962, AJ, 67, 471
- King I. R., 1966, AJ, 71, 64
- Klypin A., Kravtsov A. V., Valenzuela O., Prada F., 1999, ApJ, 522, 82
- Koposov S. E., Belokurov V., Torrealba G., Evans N. W., 2015, ApJ, 805, 130
- Kroupa P., 2001, MNRAS, 322, 231
- Küpper A. H. W., Kroupa P., Baumgardt H., Heggie D. C., 2010, MNRAS, 407, 2241
- Larsen S. S., Strader J., Brodie J. P., 2012, A&A, 544, L14
- Larsen S. S., Brodie J. P., Forbes D. A., Strader J., 2014, A&A, 565, A98 Li T. S. et al., 2017, ApJ, 838, 8
- Macciò A. V., Dutton A. A., van den Bosch F. C., Moore B., Potter D., Stadel J., 2007, MNRAS, 378, 55
- Madau P., Shen S., Governato F., 2014, ApJ, 789, L17
- Makino J., Aarseth S. J., 1992, PASJ, 44, 141
- Martin N. F., de Jong J. T. A., Rix H.-W., 2008, ApJ, 684, 1075
- Mashchenko S., Wadsley J., Couchman H. M. P., 2008, Science, 319, 174
- Maxwell A. J., Wadsley J., Couchman H. M. P., 2015, ApJ, 806, 229
- McConnachie A. W., 2012, AJ, 144, 4
- McLaughlin D. E., van der Marel R. P., 2005, ApJS, 161, 304
- Merrifield M. R., Kent S. M., 1990, AJ, 99, 1548
- Moore B., 1994, Nature, 370, 629
- Moore B., Ghigna S., Governato F., Lake G., Quinn T., Stadel J., Tozzi P., 1999, ApJ, 524, L19
- Munshi F., Brooks A. M., Applebaum E., Weisz D. R., Governato F., Quinn T. R., 2017, preprint (arXiv:e-prints)
- Navarro J. F., Eke V. R., Frenk C. S., 1996, MNRAS, 283, L72
- Navarro J. F., Frenk C. S., White S. D. M., 1996, ApJ, 462, 563
- Nipoti C., Binney J., 2015, MNRAS, 446, 1820
- Nitadori K., Aarseth S. J., 2012, MNRAS, 424, 545
- Oñorbe J., Boylan-Kolchin M., Bullock J. S., Hopkins P. F., Kereš D., Faucher-Giguère C.-A., Quataert E., Murray N., 2015, MNRAS, 454, 2092
- Peñarrubia J., Walker M. G., Gilmore G., 2009, MNRAS, 399, 1275

- Peñarrubia J., Benson A. J., Walker M. G., Gilmore G., McConnachie A. W., Mayer L., 2010, MNRAS, 406, 1290
- Peñarrubia J., Pontzen A., Walker M. G., Koposov S. E., 2012, ApJ, 759, L42
- Petts J. A., Gualandris A., Read J. I., 2015, MNRAS, 454, 3778
- Petts J. A., Read J. I., Gualandris A., 2016, MNRAS, 463, 858 (P16)
- Planck Collaboration XVI, 2014, A&A, 571, A16
- Plummer H. C., 1911, MNRAS, 71, 460
- Pontzen A., Governato F., 2012, MNRAS, 421, 3464
- Pontzen A., Governato F., 2014, Nature, 506, 171
- Pontzen A., Read J. I., Teyssier R., Governato F., Gualandris A., Roth N., Devriendt J., 2015, MNRAS, 451, 1366
- Portegies Zwart S. F., McMillan S. L. W., Gieles M., 2010, ARA&A, 48, 431
- Read J. I., Gilmore G., 2005, MNRAS, 356, 107
- Read J. I., Steger P., 2017, MNRAS, 471, 4541
- Read J. I., Goerdt T., Moore B., Pontzen A. P., Stadel J., Lake G., 2006a, MNRAS, 373, 1451
- Read J. I., Wilkinson M. I., Evans N. W., Gilmore G., Kleyna J. T., 2006b, MNRAS, 367, 387
- Read J. I., Agertz O., Collins M. L. M., 2016, MNRAS, 459, 2573 (R16)
- Read J. I., Iorio G., Agertz O., Fraternali F., 2017, MNRAS, 467, 2019
- Richardson T., Fairbairn M., 2014, MNRAS, 441, 1584
- Sánchez-Salcedo F. J., Reyes-Iturbide J., Hernandez X., 2006, MNRAS, 370, 1829
- Sand D. J., Spekkens K., Crnojević D., Hargis J. R., Willman B., Strader J., Grillmair C. J., 2015, ApJ, 812, L13
- Santana F. A., Muñoz R. R., Geha M., Côté P., Stetson P., Simon J. D., Djorgovski S. G., 2013, ApJ, 774, 106
- Schive H.-Y., Liao M.-H., Woo T.-P., Wong S.-K., Chiueh T., Broadhurst T., Hwang W.-Y. P., 2014, Phys. Rev. Lett., 113, 261302
- Schneider A., Trujillo-Gomez S., Papastergis E., Reed D. S., Lake G., 2017, MNRAS, 470, 1542
- Spergel D. N., Steinhardt P. J., 2000, Phys. Rev. Lett., 84, 3760
- Spitzer L., 1987, Dynamical Evolution of Globular Clusters. Princeton Univ. Press, Princeton, NJ
- Tegmark M., Zaldarriaga M., 2002, Phys. Rev. D, 66, 103508
- Teyssier R., Pontzen A., Dubois Y., Read J. I., 2013, MNRAS, 429, 3068
- Tollet E. et al., 2016, MNRAS, 456, 3542
- Ural U., Wilkinson M. I., Read J. I., Walker M. G., 2015, Nature Commun., 6, 7599
- van der Walt S., Colbert C. S., Varoquaux G., 2011, The NumPy Array: A Structure for Efficient Numerical Computation. Available at: http://www.numpy.org/ (accessed 2016 July 21)

Vasiliev E., 2017, ApJ, 848, 10

- Vasiliev E., 2018, MNRAS, preprint (arXiv:1802.08239)
- Walker M. G., Peñarrubia J., 2011, ApJ, 742, 20
- Walker M. G., Mateo M., Olszewski E. W., Peñarrubia J., Wyn Evans N., Gilmore G., 2009, ApJ, 704, 1274
- Wang L., Dutton A. A., Stinson G. S., Macciò A. V., Penzo C., Kang X., Keller B. W., Wadsley J., 2015, MNRAS, 454, 83
- Webb J. J., Patel S. S., Vesperini E., 2017, MNRAS, 468, L92
- Wheeler C., Oñorbe J., Bullock J. S., Boylan-Kolchin M., Elbert O. D., Garrison-Kimmel S., Hopkins P. F., Kereš D., 2015, MNRAS, 453, 1305
- Wilks S. S., 1938, Ann. Math. Statist., 9, 60
- Yoon I., Lee H. M., Hong J., 2011, MNRAS, 414, 2728
- Zonoozi A. H., Haghi H., Kroupa P., Küpper A. H. W., Baumgardt H., 2017, MNRAS, 467, 758

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