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Transit timing analysis of the exoplanet TrES-5 b. Possible existence of the exoplanet TrES-5 c

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ABSTRACT

In this work, we present transit timing variations detected for the exoplanet TrES-5b. To obtain the necessary amount of photometric data for this exoplanet, we have organized an international campaign to search for exoplanets based on the transit-timing variation (TTV) method and as a result of this we collected 30 new light curves, 15 light curves from the Exoplanet Transit Database (ETD) and 8 light curves from the literature for the timing analysis of the exoplanet TrES-5b. We have detected timing variations with a semi-amplitude of $A \approx 0.0016$ d and a period of $P \approx 99$ d. We carried out the N -body modelling based on the three-body problem. The detected perturbation of TrES-5b may be caused by a second exoplanet in the TrES-5 system. We have calculated the possible mass and resonance of the object: $M \approx 0.24M_{\text{Jup}}$ at a 1:2 Resonance.

Key words: methods: data analysis – methods: numerical – techniques: photometric – techniques: radial velocities – techniques: high angular resolution – planetary systems.

1 INTRODUCTION

There are many methods of searching for exoplanets. The radial velocity and transit photometry methods are the main ones, because most of exoplanet discoveries were made using these two methods (based on statistics from exoplanets.org and exoplanets.eu; Schnei-

der et al. 2011; Han et al. 2014). These techniques most often lead to the discovery of the closest exoplanets, such as hot Jupiters and Saturn type exoplanets around solar-type stars, due to the more apparent interaction of the planet with its host star, which is easily detected in just a short period of time.

Despite this, new exoplanets on more distant orbits in known exoplanet systems are being discovered every year. One of the methods which allows us to predict or discover other exoplanets in known discovered planetary systems is the transit-timing vari-

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ation (TTV) method described by Miralda-Escude (2002), Agol, Steffen & Clarkson (2005), Narita (2009), and Hoyer et al. (2011). This method is based on the periodic variation of the planet's orbit around the parent star manifesting itself as a delay or advance of the moment of the middle of transit, caused by the gravitational influence of another planet or some other more massive object also orbiting around the star.

The first exoplanet with well-detected timing was Kepler-19b. With a period of about 300 d and a semi-amplitude equal to 5 min, the exoplanet Kepler-19c was predicted (Ballard et al. 2011). Following this, the existence of Kepler 19c was confirmed by the radial velocities method (Malavolta et al. 2017). Further exoplanets Kepler-46c (Nesvorný et al. 2012), Kepler-419c (Rebekah et al. 2014), Kepler-338e (Eylen & Albrecht 2015), and KOI-620.02 (Masuda 2014) have also been discovered by the TTV method.

In recent years, with the increase of the quality and quantity of photometric observations during the exoplanet transits, the search for extrasolar planets by means of TTVs has become more effective and relevant.

In this work, we describe the organization of the international observational campaign and the investigation of the detected timing variations of TrES-5b. The exoplanet TrES-5b orbits a cool G dwarf GSC 0 3949–00967 ($V = 13.72$ mag) and was discovered by the Trans-Atlantic Exoplanet Survey in 2011 (Mandushev et al. 2011). The orbital period of the exoplanet TrES-5b predicted in that work is $P = 1.4822446 \pm 0.0000007$ d. The mass and radius of TrES-5b are $M_{\text{pl}} = 1.778 (\pm 0.063) M_{\text{Jup}}$, $R_{\text{pl}} = 1.209 (\pm 0.021) R_{\text{Jup}}$ (Mandushev et al. 2011).

Earlier, the exoplanet TrES-5b was investigated by Mislis et al. (2015) and Maciejewski et al. (2016). In these papers, the information on the orbital parameters of TrES-5b, such as the orbital period P , orbital inclination i_b , radius of planet in stellar radii R_p/R_* , semi-major axis in stellar radii a_b/R_* have been refined. At the same time, although evidence of timing (TTV) for TrES-5b has not been detected, there is also no convincing evidence of its absence.

2 THE SPECKLE INTERFEROMETRY OBSERVATIONS

In 2015 November and 2016 June, high precision imaging of the star TrES-5 was carried out with the 6-m BTA telescope (Special Astrophysical Observatory) using a speckle interferometer. We used an EMCCD (electron-multiplying CCD) to take images with the BTA speckle interferometer. Thus, an image of a faint object represents a set of separate points where the light quanta fall.

The main contribution to the optical image distortion and blurring belongs to the atmospheric turbulence (or atmospheric seeing). For example, for a 6-m aperture of the optical BTA telescope at the wavelength of 550 nm, the diffraction limit of resolution for a point source must be equal to 0.02 arcsec, whereas the real size of the image influenced by the atmospheric effects amounts to 1–2 arcsec, i.e. 100 times more. The speckle interferometry method is a method of observing astronomical objects seen through a turbulent atmosphere with the angular resolution limit close to the diffraction limit.

The principle of the speckle interferometry method is to take high-resolution images with a very short exposure time ($\sim 10^{-2}$ s). Such images consist of a great number of speckles that are produced by the mutual interference of the light beams that fall on the focal plane of a telescope from different parts of the lens. Each speckle looks like an airy disc in the focal plane of a perfect telescope that is not affected by the atmospheric seeing. Atmospheric seeing influences

the image in such a way that a wavefront that reaches a ground-based telescope is always distorted by the optical imperfections of the atmosphere. When taking very short-exposure images we record the speckle distribution at that very instant, while with long exposures the image loses its structure and becomes blurred. In the images of a non-point (extended) source, the speckle pattern (their shape and size) reflects the characteristics of the source itself. For example, if we observe a binary object (a binary star or a binary asteroid), then the speckles are recorded in pairs, and each pair of speckles represents an airy disc from the two components of a binary star or asteroid. In order to obtain information about the structure of the observed object, we accumulated thousands of its snapshots.

Based on two observational sets of speckle interferometry of TrES-5b, two autocorrelation functions of the speckle-interferometry images were obtained. Because the star is faint ($V = 13.7$ mag), the signal-to-noise ratio of the obtained measurements is low precision. Nevertheless, based on the results of two sets of TrES-5 observations, we can argue that there are no components near the star with a brightness difference of about Δm : $0 \text{ mag} \div 1 \text{ mag}$ and at a distance in the range of ρ : $200 \text{ mas} \div 3000 \text{ mas}$, which corresponds to the range: $72 \text{ au} \div 1080 \text{ au}$. Both autocorrelation functions are presented in Fig. 1.

3 PHOTOMETRIC OBSERVATIONS

For the exoplanet search by the TTV method, an international observation campaign as part of EXoPlanetary trANsit Search with an International Observational Network (EXPANSION) project was organized. Observatories from Russia, Europe, North and South America with a small and middle diameter of telescopes from 25 cm to 2 m were used for the photometric observations of TrES-5b transits. All the telescopes participated in observational campaign are presented in Table 1.

4 DATA REDUCTION AND ANALYSIS OF LIGHT CURVES

The photometric observations obtained in the campaign were processed by APEX-II, MUNIWIN, or AIP4WIN software. The APEX-II package (Devyatkin et al. 2009) is completely automatic and has many options for the processing of astrometric and photometric observations. This package allows the use of aperture photometry and PSF photometry (PSF fitting). The MUNIWIN (Hroch 2014) as well as AIP4WIN (Tsamis, Margonis & Christou 2013) packages provide easy-to-use tools for all astronomical astrometry and photometry as well as FITS files operations and a simple user interface along with a powerful processing engine.

For all observational sets bias, flat-field and dark calibration images were obtained and subsequently taken into account in photometric data processing. When processing the photometric observations, for each series we chose, as a rule, 5–10 reference stars with brightness close to that of the object located on the frame close to it to reduce the effect of the atmospheric extinction. Based on the processing results, we studied the behaviour of each reference star. If one of them was variable or if its behaviour differed sharply from that of all the remaining stars, then it was excluded from the subsequent processing. The mean values between the derived magnitudes of the reference stars and the magnitude of the object were the sought-for a result – the object's light curve. The precision of the observations was determined using a check star that was chosen from the reference stars and was closest in brightness to the object. We performed the same procedure with the check star as that with

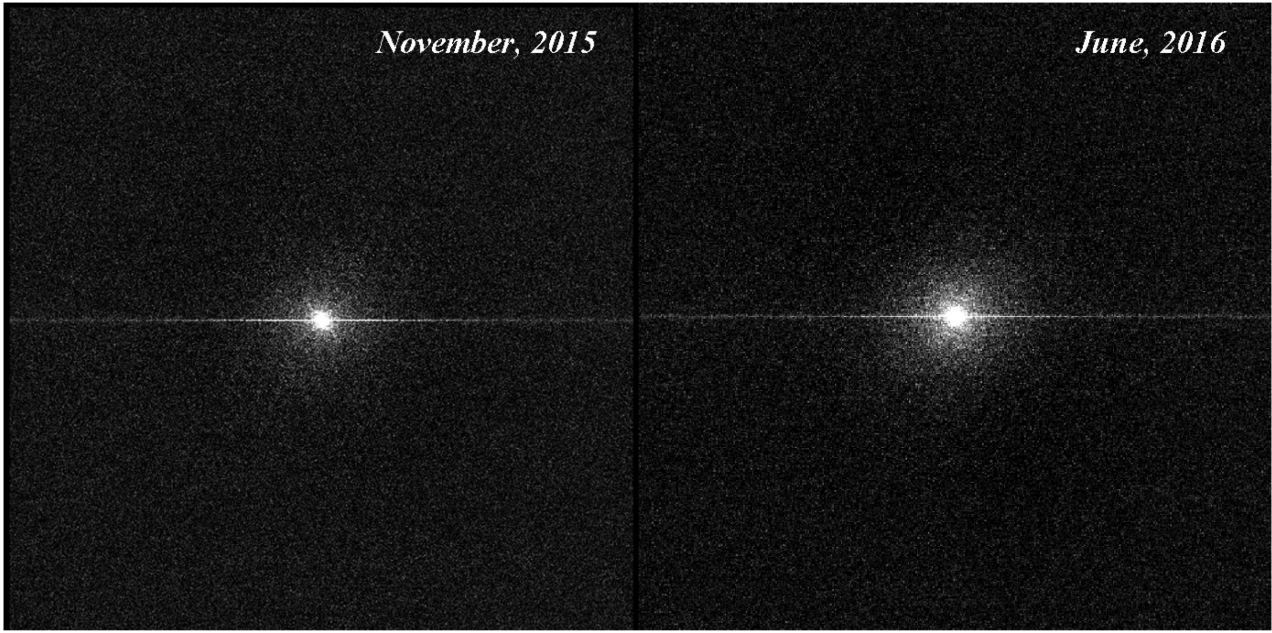


Figure 1. The autocorrelation function of speckle-interferometric images of TrES-5 (obtained on 2015 November and 2016 June with the use of 6-m BTA telescope).

Table 1. Telescopes participating in the observational campaign.

Telescope	Aperture	Location
MTM-500M	0.5m	Pulkovo Observatory (Kislovodsk), Russia
ZA-320M	0.32m	Pulkovo Observatory (Saint-Petersburg), Russia
Zeiss-600	0.6m	ISTP SB RAS, Mondy, Russia
Ritchey-Chretien system	0.82m	Baronnies Provencales Observatory, France
Cassegrain system	0.43m	Baronnies Provencales Observatory, France
Zeiss-2000	2.0m	IC AMER, Peak Terskol, Russia
Meade 14" LX200R	0.35m	Famagusta, Cyprus
Meade 16" ACF OTA	0.406m	Varkaus, Finland
Celestron C14 OTA	0.36m	Varkaus, Finland
Celestron C11EdgeHD	0.28m	Amathay Vésigneux, France
Celestron C11EdgeHD	0.28m	Acton, MA USA
Newton system	0.3m	Elgin, OR USA
Optimised Dall Kirkham system	0.4m	London, Great Britain
PlaneWave CDK700	0.7m	Trottier Observatory, Burnaby, Canada
Meade 8" LX200GPSR	0.203m	Madrid, Spain

Note. Based on the campaign data we obtained 30 new light curves of the transits of TrES-5b. Due to the fact that the host star is quite faint for small and medium aperture telescopes, the star was observed predominantly without the use of filters to increase the SNR. In some cases, R_C and V_C filters of the Johnson–Cousins photometric system were used. The observation log is presented in Table 2.

the object – we found the mean difference between its brightness and the brightness of the remaining reference stars and calculated the standard deviation for the derived light curve, which was considered to be the accuracy of the observations. Thus, we plotted the final light curve obtained based on carried out differential photometry of stars with the smallest standard deviation.

After data processing, we obtained 30 light curves of the TrES-5b transits. We also obtained 15 light curves selected from the Exoplanet Transit Database (Poddany, Brat & Pejcha 2010) (<http://var2.astro.cz/ETD/>). We have taken the light curves with data quality (DQ) ≤ 3 based on ETD standards, showing only a full transit, as well as clearly defined moments of transit ingress and egress. We have not considered partial transits because the mid-point of a transit may be determined incorrectly due to a possible presence of small but appreciable deviations of the transit durations.

Thus, the total 45 light curves of transits of the exoplanet TrES-5b were prepared for further fitting and analysis. All light curves were detrended against the airmass changes. Time scales of all data series have been converted into the Barycentric Julian Date (BJD) format.

Each transit light curve was modelled with the online EXOFAST applet (Eastman, Gaudi & Agol) available on the NASA Exoplanet Archive (<https://exoplanetarchive.ipac.caltech.edu/index.html>). The Exoplanet Archive’s version of EXOFAST offers IDL-based calculations as the original code of EXOFAST and also provides sufficient back-end computing resources to enable Markov Chain Monte Carlo (MCMC) analysis. The fitting and analysis of light curves in the best-fitting model allow one to get a time of the mid of transit T_{mid} , radius of planet to stellar radii R_p/R_* ratio, LD coefficients u_1 and u_2 of the quadratic law, orbital inclination i_b and total duration of a transit T_{Dur} .

Table 2. Details on new observations reported in this paper.

Date (UT)	Telescope, aperture	Filter	X (airmass change)	Cadence (min)
2013-09-23	CelestronC11, 0.28m	None	1.04→1.29	0.47
2013-10-07	Newton system, 0.3m	None	1.03→1.50	0.98
2013-11-02	Optimized Dall Kirkham system, 0.4m	R_c	1.13→1.47	0.45
2014-02-25	ZA-320 M, 0.32m	None	1.72→1.22	0.54
2014-04-17	MTM-500 M, 0.5m	None	2.05→1.31	1.1
2014-09-30	MTM-500 M, 0.5m	None	1.47→2.1	1.12
2014-10-03	MTM-500 M, 0.5m	None	1.58→1.7	1.5
2014-10-03	Zeiss-2000, 2m	None	1.57→1.7	2.0
2015-02-15	Celestron C14 OTA, 0.36m	None	1.57→1.93	0.46
2015-03-09	MTM-500 M, 0.5m	None	1.12→1.44	0.64
2015-05-18	Zeiss-600, 0.6m	R_c	1.65→1.22	0.87
2015-05-29	Ritchey–Chretien system, 0.82m	V	1.29→1.04	0.47
2015-06-15	Meade 14" LX200R, 0.35m	None	1.95→1.2	0.83
2015-06-18	Meade 14" LX200R, 0.35m	None	1.97→1.3	0.84
2015-07-19	Ritchey–Chretien system, 0.82m	None	1.18→1.04	0.32
2015-08-31	Meade 16ACF OTA, 0.406m	None	1.0→1.18	0.54
2016-03-19	Meade 16ACF OTA, 0.406m	None	1.46→1.12	0.46
2016-03-21	Meade 16ACF OTA, 0.406m	None	1.61→1.23	0.46
2016-03-27	Meade 16ACF OTA, 0.406m	None	1.82→1.3	0.43
2016-04-02	Meade 16ACF OTA, 0.406m	None	1.9→1.51	0.45
2016-06-10	Ritchey–Chretien system, 0.82m	None	1.12→1.05	0.48
2016-06-26	PlaneWave CDK700, 0.7m	None	1.17→1.02	0.49
2016-07-25	Meade 8" LX200GPSR, 0.203m	None	1.21→1.11	0.24
2016-07-28	Cassegrain system, 0.43m	None	1.12→1.03	0.36
2016-07-31	Meade 14" LX200R, 0.35m	None	1.26→1.16	0.81
2016-08-14	PlaneWave CDK700, 0.7m	None	1.08→1.25	0.93
2016-10-28	Celestron C11EdgeHD, 0.28m	None	1.03→1.35	0.28
2016-10-31	Ritchey–Chretien system, 0.82m	None	1.05→1.22	0.45
2016-12-13	Ritchey–Chretien system, 0.82m	None	1.19→1.81	0.44
2017-05-16	Ritchey–Chretien system, 0.82m	I_c	1.89→1.30	0.45

In order to calculate the limb darkening (LD) coefficient in EXOFAST, a band had to be selected. In those cases where observations were carried out without filters, the average wavelength in the sensitivity curve of the CCD camera was determined. Thus, the closest band of sensitivity of photometric observations for each telescope was determined.

The following initial parameters were used for the light curve fitting: surface gravity for assumed mass $\log g = 4.517 \pm 0.012$, effective temperature $T_{\text{eff}} = 5171 \pm 36$, metallicity $[\text{Fe}/\text{H}] = 0.2 \pm 0.1$ and the prior detected orbital period of TrES-5b $P_b = 1.4822446 \pm 0.0000007$ d (Mandushev et al. 2011). The final 30 light curves obtained in the observational campaign with the superimposed model curves after the fitting and the residuals from the best-fitting model are presented in Figs 2(a) and (b).

We re-determined the orbital period $P_b = 1.482247063 \pm 0.0000005$ d. For the determination of $O-C$ (Observation–Calculation) value we calculated the difference between the T_{mid} obtained as a result of fitting the transit light curve and the calculated $T_{(\text{Epoch})}$ obtained from the following ephemeris:

$$T_{(\text{Epoch})} = 2456458.59219(9) + 1.482247(063) \cdot E,$$

where T_0 was taken from Mislis et al. (2015) and E is the cycle number.

The measurements of mid-transit moments T_{mid} , ratio R_b/R_* and LD u_1 and u_2 coefficients are presented in Table 3. Values of uncertainties were calculated using formulae from Carter et al. (2008). Also, we included in Table 3 the values of high-precision follow-up photometry of TrES-5b transits from Mislis et al. 2015 and Maciejewski et al. (2016).

5 SIMULATION OF A THREE-BODY SYSTEM (STAR–PLANET–PLANET)

We carried out a frequency analysis for transit timing data sets including 45 measurements of $O-C$ obtained from the light curves in this work and eight measurements from (Mislis et al. 2015 and Maciejewski et al. 2016) (53 values in total) with the average $\sigma = 1.1$ min. For the analysis, we took into account the weights of the measurements and used the ‘clean’ method, suggested in 1974 by Hogbomom for the cleaning ‘dirty maps’ that are obtained during aperture synthesis in radio astronomy (Hogbom 1974). Subsequently, the method was modified to obtain ‘clean’ spectra in the spectral analysis of time series (Roberts, Lehar & Dreher 1987).

The frequency analysis detected a peak at $P \sim 99$ d. The false alarm probability (FAP) is about 0.18 per cent. After ‘cleaning’ the spectrum by means of the algorithm of the ‘clean’ method, no evidence was found for equivalent or greater importance peaks. The periodogram is shown in Fig. 3.

The detected peak at $P \sim 99$ d gives us reason to assume that there is an additional body in the TrES-5 planetary system. To search for it and estimate its mass, as well as the distance from the planet TrES-5b, it was necessary to conduct a dynamic simulation of a possible system consisting of three bodies.

To construct a dynamic model for a triple system ‘star–planet–planet’, we used translational and rotational motion equations for the two and three body problem obtained by G.N. Duboshin (Duboshin 1963).

We used a model in which the motion of three bodies in space is simulated. The shape of such bodies cannot be considered as material points, because the force of interaction between them es-

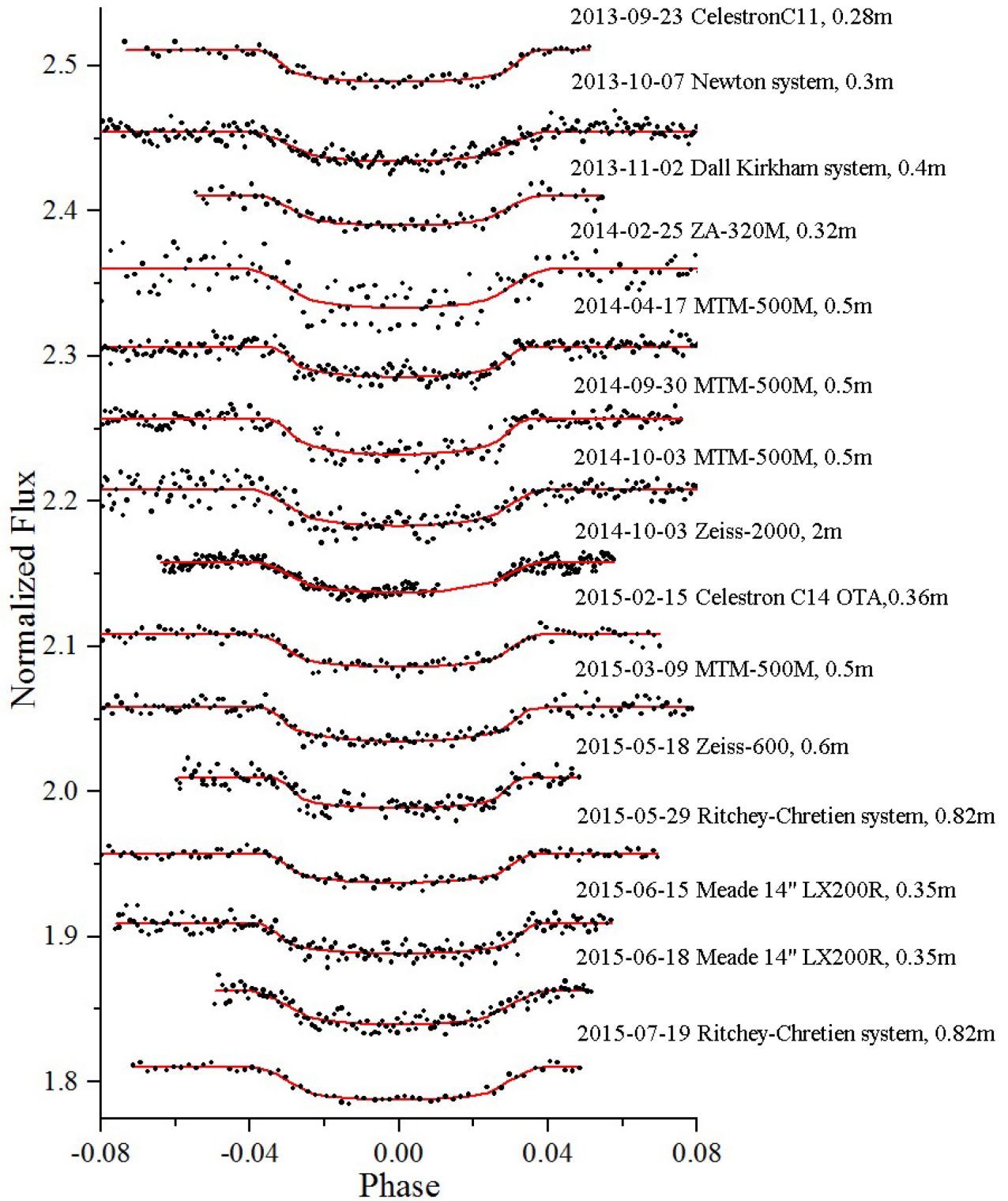


Figure 2. (a) Light curves of TrES-5b transits. The best-fitting curves are plotted with a red line. Residuals are presented on the bottom panel.

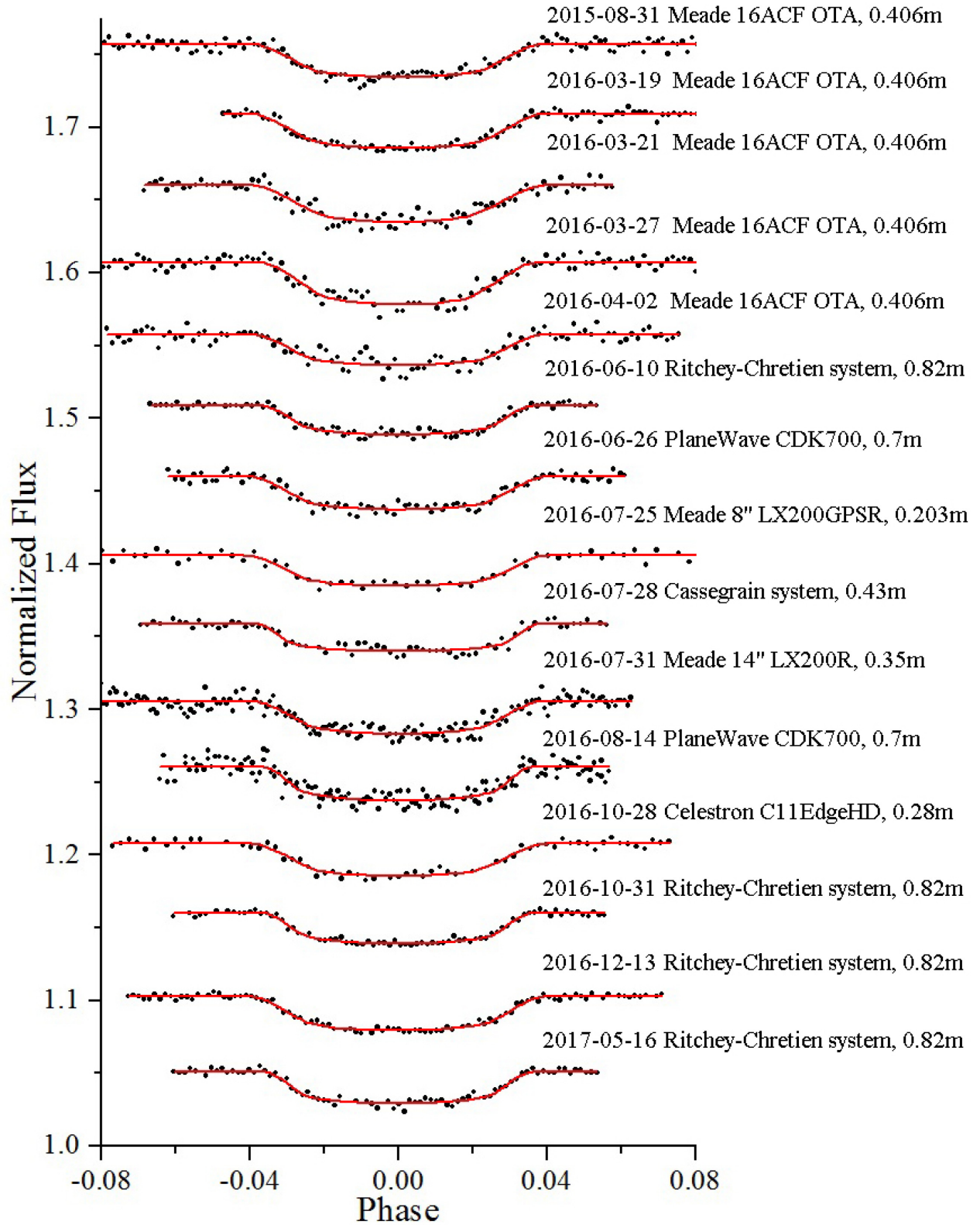


Figure 2. (b) – continued.

sentially depends on their relative orientation. Thus, their prograde and retrograde motion must be considered together.

This problem of prograde–retrograde motion was and continues to be developed in different assumptions about the parameters of the

considered systems. In this numerical investigation of motion in a binary or triple system, each body is considered as a homogeneous triaxial ellipsoid. Differential equations of motion for this system were obtained by G.N. Duboshin (Duboshin 1963). They are derived from

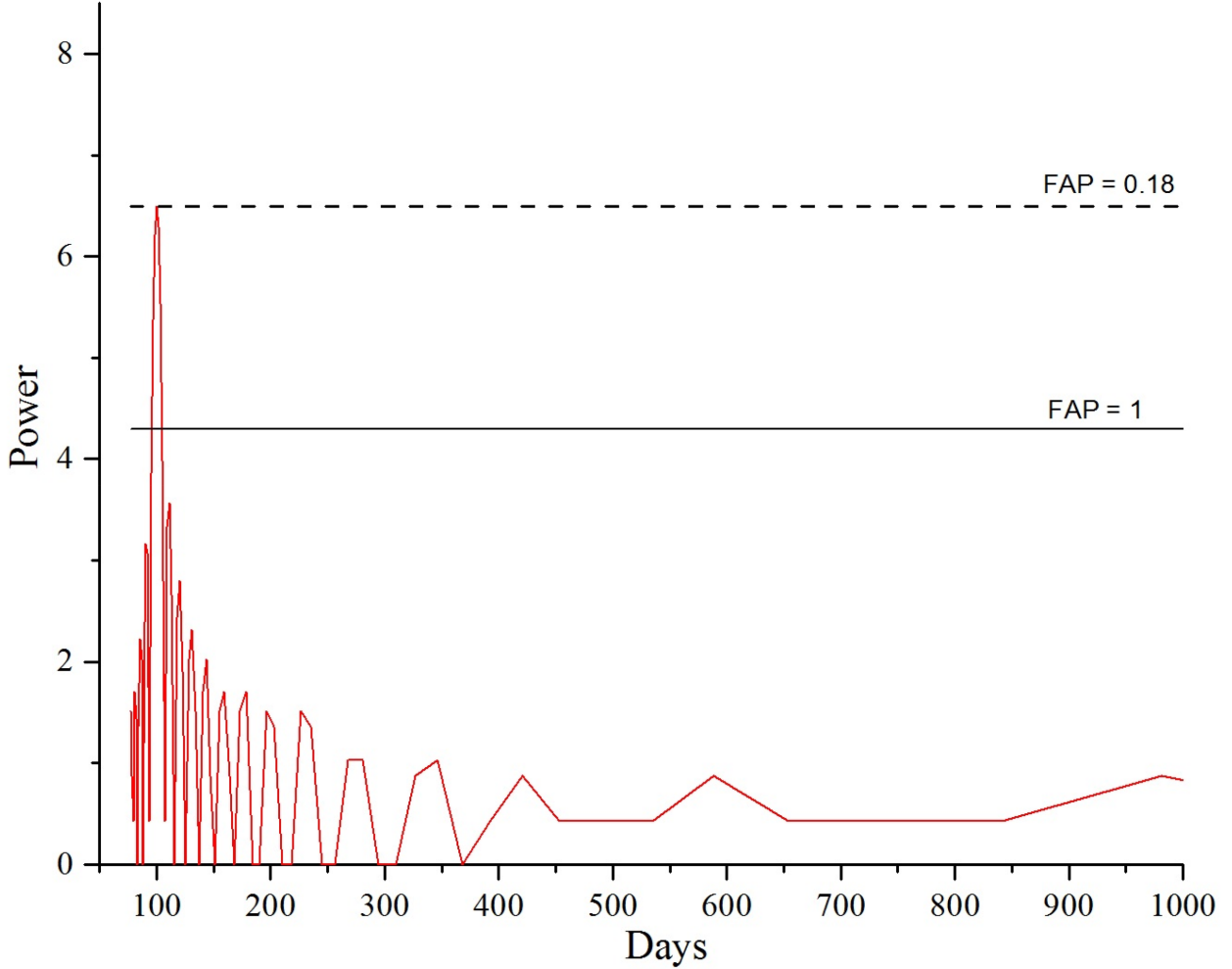


Figure 3. Periodogram of the clean spectrum for the $O-C$ data with a peak at a value of 99 d. Dashed line shows probability with FAP = 1 per cent. Solid line shows probability of the detected peak with FAP = 0.18 per cent.

the general second-order Lagrange equations $\frac{d}{dt} \left(\frac{\partial T}{\partial q'_i} \right) - \frac{\partial T}{\partial q_i} = \frac{\partial U}{\partial q_i}$, where for the generalized coordinates q_i we accepted the absolute rectangular coordinates of the inertia centres (x_i, y_i, z_i) , describing the prograde and retrograde motion, and the Euler angles $(\phi_i, \psi_i, \theta_i)$ describing the rotation of the body.

In this investigation, the three-body problem was considered for the simulation of a system with a star in the centre and two planets orbiting it. The problem was solved in relative coordinates, with the origin placed in the centre of the star. Thus, for this problem, the final form of the above equations is as follows:

$$\begin{aligned}
 x'_i &= V_{x_i} \\
 y'_i &= V_{y_i} \\
 z'_i &= V_{z_i} \\
 V'_{x_i} &= \frac{(m_0 + m_i)}{m_0 m_i} \frac{\partial U_{i0}}{\partial x_i} + \frac{\partial R_i}{\partial x_i} \\
 V'_{y_i} &= \frac{(m_0 + m_i)}{m_0 m_i} \frac{\partial U_{i0}}{\partial y_i} + \frac{\partial R_i}{\partial y_i} \\
 V'_{z_i} &= \frac{(m_0 + m_i)}{m_0 m_i} \frac{\partial U_{i0}}{\partial z_i} + \frac{\partial R_i}{\partial z_i}
 \end{aligned} \quad (1)$$

$$A_i p'_i - (B_i - C_i) q_i r_i = \left(\frac{\partial U}{\partial \psi_i} - \cos \theta_i \frac{\partial U}{\partial \phi_i} \right) \frac{\sin \phi_i}{\sin \theta_i} + \cos \phi_i \frac{\partial U}{\partial \theta_i}$$

$$B_i q'_i - (C_i - A_i) r_i p_i = \left(\frac{\partial U}{\partial \psi_i} - \cos \theta_i \frac{\partial U}{\partial \phi_i} \right) \frac{\cos \phi_i}{\sin \theta_i} - \sin \phi_i \frac{\partial U}{\partial \theta_i}$$

$$C_i r'_i - (A_i - B_i) p_i q_i = \frac{\partial U}{\partial \phi_i}$$

$$p_i = \psi'_i \sin \phi_i \sin \theta_i + \theta'_i \cos \phi_i$$

$$q_i = \psi'_i \cos \phi_i \sin \theta_i - \theta'_i \sin \phi_i$$

$$r_i = \psi'_i \cos \theta_i + \phi'_i$$

$$(i = 0, 1, 2).$$

The following designations are used: m_i – the mass of the corresponding body, A_i, B_i, C_i – the main central moments of inertia, p_i, q_i, r_i – the projected angular rotation velocity of a body in its own coordinate system, related to the Euler angles through the kinematic equations (Duboshin 1963), R_i – perturbation function, which is calculated from the potential U_{ij} :

$$R_i = \sum_{j=1}^{n'} \left(\frac{1}{m_i} U_{ij} + \frac{1}{m_0} \left(x_i \frac{\partial U_{j0}}{\partial x_j} + y_i \frac{\partial U_{j0}}{\partial y_j} + z_i \frac{\partial U_{j0}}{\partial z_j} \right) \right). \quad (2)$$

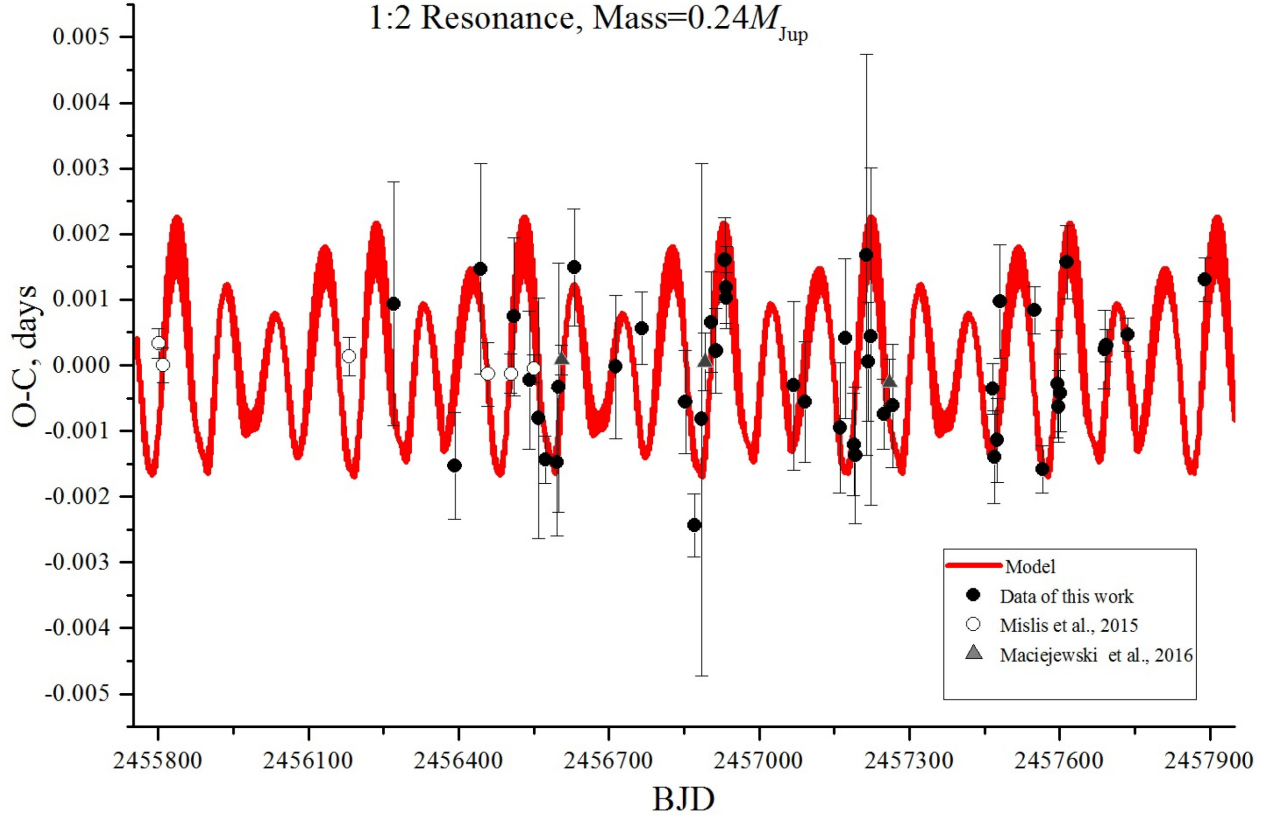


Figure 4. Observed data with a superimposed model curve. Black points – the observations from this work; white points – data from (Mislis et al. 2015); grey triangles – data from (Maciejewski et al. 2016).

To calculate the potential, we took the members up to the third order inclusive in the decomposition proposed by G.N. Duboshin:

$$U_{ij} \cong Gm_i m_j + Gm_i \frac{A_j + B_j + C_j - 3I_j^{ij}}{2\Delta_{ij}^3} + Gm_j \frac{A_i + B_i + C_i - 3I_i^{ij}}{2\Delta_{ij}^3}, \quad (3)$$

where G is the gravitational constant, $\Delta_{ij} = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2 + (z_i - z_j)^2}$ is the distance between the centres of the bodies, and I_s^{ij} is the moment of inertia relative to the line connecting the centres of inertia of the two bodies. It should be noted that this approximation of the potential works well provided that the distance between the bodies is larger than their size. For the objects under investigation, this condition is generally met.

The system of equations (1) is a system of differential equations of the first order. To obtain its numerical solution, the Dormand–Prince integration method was used, which is based on the 8th order Runge–Kutta method (Hairer, Norsett & Wanner 1993). The integration accuracy was $\sim 10^{-7}$ km. The criterion of a successful implementation of the numerical integration was the constancy of the classical integrals of the system (1) – areas and energy. The accuracy of the results was determined by integrating in the forward and reverse directions. At the same time, the parameters obtained as a result of the reverse integration were compared with the initial conditions.

For the initial simulation parameters, we used the mass of the TrES-5b, the mass of the parent star $M_* = 0.893 (\pm 0.024) M_{\text{Sol}}$

obtained in (Mandushev et al. 2011), and the re-determined value of P_b .

The mass of the third body in the system was set in the range of the mass of the Mars $M \approx 0.1M_{\text{Earth}}$ to the mass of brown dwarf $M = 30 M_{\text{Jup}}$. The simulation was performed at the resonances 1:2, 2:3, 1:3, 3:4, 2:5, 3:5, and 4:5. Thus, we iteratively selected model parameters that would provide the best agreement with the observational data presented in the $O-C$ diagram. The resulting model-based timing at the resonances 2:3, 3:4, 2:5, 3:5, and 4:5, with the period $P \sim 99$ d, was obtained with an amplitude much greater than expected. A further increase of the semi-major axis of the third body, i.e. at the potential resonances 1:4, 1:5, 1:6, etc., in the system would give us a progressive increase of mass estimates for the third object reaching to the mass of a brown dwarf. Wherein the presence of a third body with a mass comparable to the mass of a brown dwarf in an orbit close to TrES-5b’s orbit would be easy to register with the only eight currently available radial velocity measurements presented in Mandushev et al. (2011).

Based on all the considered resonances with masses in the range of $0.1M_{\text{Earth}}$ to $30 M_{\text{Jup}}$, the best agreement of model and observed data was obtained for two cases:

- (i) Resonance 1:2 with the mass of the third body $M_{\text{Planet.2}} \sim 0.24M_{\text{Jup}}$.
- (ii) Resonance 1:3 with the mass of the third body $M_{\text{Planet.2}} \sim 3.15M_{\text{Jup}}$.

The case with $M_{\text{Planet.2}} \sim 3.15M_{\text{Jup}}$ cannot be considered further because of the limitations of the radial velocities registered by Mandushev et al. (2011) for TrES-5b. An object of such mass orbiting

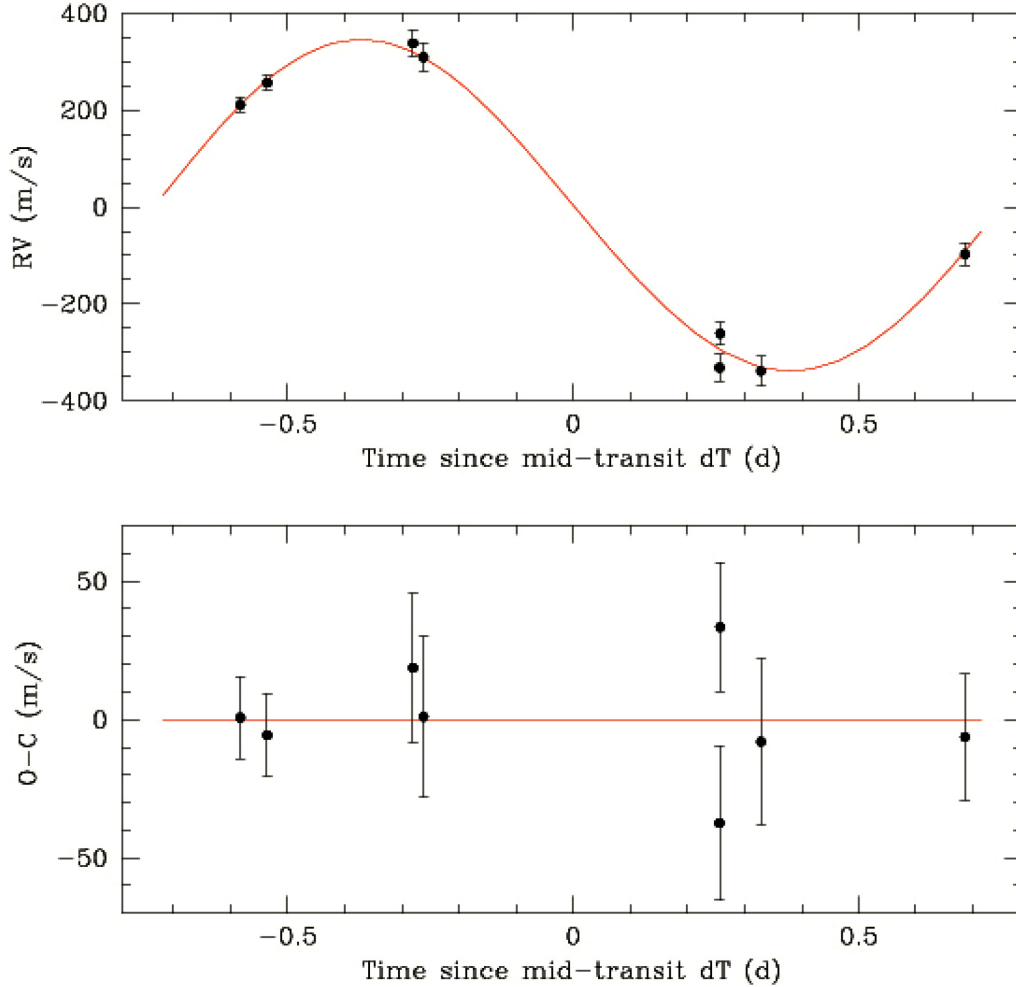


Figure 5. Top: (black points) radial velocities with uncertainties for the star TrES-5 from Mandushev et al. (2011) with (solid line) best-fitting model to the eight radial velocities for the fixed orbital period of TrES-5b $P_b = 1.482247063$ days. Bottom: The residuals from the best fit-model and radial velocities.

around the star with a 1:3 resonance would produce radial velocities exceeding 400 m s^{-1} , that could be simply detected based on the RV analysis.

As the result, Fig. 4 shows the simulated transit timing of TrES-5b interacting with a third body in the system. For the model and all presented in the Table 3 observations the reduced $\chi^2_{Model} = 0.32$, whereas for the case of linear ephemerides $\chi^2_{Lin} = 0.57$. Thus, it can be argued that our model curve (red series – Fig. 4) based upon a 1:2 resonance and ~ 99 -d period agrees better with the distribution of observations (points – Fig. 4) than the linear model.

6 RADIAL VELOCITIES ANALYSIS WITH DATA FROM LITERATURE

For the radial velocities (RV) analysis of the host star of TrES-5b, we searched data in the literature and RV archives. There are only eight measurements of RV of the star TrES-5 presented in Mandushev et al. (2011).

We analysed available set of RV data using the MCMC code described in Gillon et al. (2012). This software uses a Keplerian model of (Murray & Correia 2010) to fit the RVs. We obtained the physical parameters of the planet from the set of the parameters that were perturbed randomly at each step of the Markov chains (jump pa-

Table 4. The planetary parameters for the model with fixed re-determined period P_b .

Parameter	Value	Units
Period, P_b	$1.482247063 \pm 0.0000005$	d
Eccentricity, e	0.017 ± 0.012	
Semi-major axis, a	0.02447 ± 0.00021	au
RV semi-amplitude, K	343 ± 11	m s^{-1}
Minimum mass, $M_p \sin i$	1.784 ± 0.066	M_{Jup}

rameters), stellar mass, and radius. Free eccentricity was assumed. The prior physical parameters of the star $\log g = 4.517 \pm 0.012$, $T_{\text{eff}} = 5171 \pm 36$, $[\text{Fe}/\text{H}] = 0.2 \pm 0.1$ were used. As for the orbital period of TrES5b modelling, we used fixed value $P_b = 1.482247063$ d.

As the result of the modelling, we obtained the best fit-model with $\chi^2 = 4.5$ for the eccentricity $e = 0.017 \pm 0.012$. The planetary parameters are presented in Table 4.

The plot of the model with the residuals for the eight RV measurements are presented in Fig. 5. The RMS of the fitting procedure

is 20 m s^{-1} and the maximum deviation from this model reaches 36.3 m s^{-1} .

When carrying out a similar analysis of radial velocities using the period $P_b = 1.4822446 \text{ d}$ presented in Mandushev et al. (2011), the best-fitting model is $\chi^2 = 6$. Thus, our model with $\chi^2 = 4.5$ gives orbital parameters of TrES-5b that are a little more accurate when compared with the model of Mandushev et al. (2011).

7 DISCUSSION AND CONCLUSIONS

Based on an analysis of the photometric observations of transits of TrES-5b, obtained as part of EXPANSION project to study the TTV of the exoplanet, with the use data from the ETD and high-precision photometry from Mislis et al. (2015) and Maciejewski et al. (2016), transit timing variations of TrES-5b with a period of about 99 days was detected.

The resulting speckle-interferometric observations with the 6-m BTA telescope allow us to confidently announce the absence of any objects close to the host star with a brightness difference of $\Delta m: 0 \text{ mag} \div 1 \text{ mag}$ and in the distance range of $\rho: 200 \text{ mas} \div 3000 \text{ mas}$. This fact indicates the absence of any components near TrES-5 of stellar masses greater than the mass of a brown dwarf at distances $72 \text{ au} \div 1080 \text{ au}$.

To estimate the mass and calculate the orbital parameters for the third component in the system perturbing the orbit of TrES-5b, we conducted an N -body simulation at the resonances 1:2, 2:3, 1:3, 3:4, 2:5, 3:5, and 4:5.

Based on the conducted N -body simulation we detected the simulated transit timing variations for a perturbing Neptune mass body at the 1:2 resonance are in good agreement with the period $P \sim 99 \text{ d}$, amplitude, and profile obtained from the TrES-5b observations. Thus, we were able to predict a possible existence of planet TrES-5c with a mass $M_{\text{TrES-5c}} \sim 0.24 M_{\text{Jup}}$ at the 1:2 resonance to TrES-5b.

At the same time, on the other resonances, taking into account the correlation between observations and N -body simulation, and also based on the radial velocities analysis of the parent star, we did not find any evidence for the existence of other bodies in the system close to the orbit of TrES-5b.

It should be noted that the estimate of the radial velocity for a planet with a mass of $0.24 M_{\text{Jup}}$ with the orbital period of 2.96 d (which corresponds to a resonance of 1:2) would produce an RV variation with semi-amplitude of about $35\text{--}40 \text{ m s}^{-1}$ for a circular orbit. On the basis of only eight measurements of the radial velocities of TrES-5 presented in Mandushev et al. (2011), we cannot conduct a search for a secondary planet in this system. But the results of our RV analysis of the RMS (20 m s^{-1}) and the maximum deviation of the observed values from the model-fit curve (36 m s^{-1}) model may indicate the existence of additional perturbations in the system that cannot be explained by the only exoplanet investigated in the system.

To verify the possible existence or absence of the exoplanet TrES-5c, additional high-precision radial velocity and photometric measurements of TrES-5 are necessary.

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