

## Speeds of sound and isentropic compressibilities of mixtures containing dipropylene glycol monomethyl ether and n-alkanols at 298.15 K

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**Abstract** Speeds of sound have been measured for binary mixtures of dipropylene glycol monomethyl ether with methanol, 1-propanol, 1-pentanol, and 1-heptanol, as a function of composition, at 298.15 K. The values have been combined with those of densities derived from excess molar volumes to obtain estimates of the product  $K_{s,m}$  of the molar volumes and isentropic compressibility  $\kappa_s$ , and excess quantity  $K'_{s,m}$ . The  $K'_{s,m}$  values are negative over the entire range of composition for all mixtures. The magnitude of  $K'_{s,m}$  increases with the number of carbon atoms in the n-alcohol. The deviation of the speeds of sound  $u^D$  from their values in an ideal mixture were also evaluated for all measured mole fractions. These values are compared with the mixing function  $\delta u$  calculated in the paper. The behaviour of  $u^D$ ,  $\delta u$ , and  $K'_{s,m}$  with composition and the number of carbon atoms in the alcohol molecule is discussed.

**Keywords** Binary liquid mixtures, acoustical parameters, molecular interactions

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### 1. Introduction

In an earlier paper [1], we have reported the results of our measurements of the excess molar volumes of dipropylene glycol monomethyl ether with n-alcohol at 298.15 K. These results suggested structural changes of dipropylene glycol monomethyl ether by alcohol molecules. Since the study of ultrasonic speed and isentropic compressibility in binary liquid mixtures are of considerable interest [2–5] in assessing the nature of molecular interactions and investigating the physico-chemical behaviour of liquid systems, we thought worthwhile to perform measurements of the speed of sound for these mixtures in order to evaluate various thermodynamic properties and functions that give a better understanding of the molecular interactions existing between alkoxyethanol and alkanols. Hence, we report here measured values of speeds of sound in (dipropylene glycol monomethyl ether + methanol, 1-propanol, 1-pentanol, and 1-heptanol) at 298.15 K and atmospheric pressure. The isentropic compressibilities  $\kappa_s$  for all mixtures were estimated by combining the densities derived from excess molar volumes [1] and the speeds of sound. The molar volume were multiplied by the isentropic

compressibilities to obtain estimates of  $K_{s,m}$ . We have also calculated the deviations  $u^D$  of the speeds of sound from those in the ideal mixture  $u^{id}$ , together with the mixing function  $\delta u$  and the excess molar quantities  $K'_{s,m}$ .

### 2. Experimental

Dipropylene glycol monomethyl ether (Merck-Schuchardt, FRG, GC, mass fraction > 95) was used without further purification. Spectroscopic grade alcohols were dried and fractionally distilled as described elsewhere [6]. All samples were kept in tightly sealed bottles to minimize the absorption of atmospheric moisture and CO<sub>2</sub>, and dried over 0.4 nm molecular sieves to reduce water content. Prior to measurements, all liquids were partially degassed at low pressure. The purities of the liquids were checked by measuring their densities with a bipillary pycnometer of about 10 cm<sup>3</sup> capacity. The measurements at 298.15 ± 0.01 K have an estimated reproducibility of 0.3 kg m<sup>-3</sup>. The values obtained for densities were compared with the literature data [6–14] in Table 1. Also given in Table 1 are our measured or literature values of those quantities which are required in the estimation of  $K_{s,m}$ ,  $K'_{s,m}$  and  $u^D$ . Binary

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**Table 1.** Observed and literature values of densities ( $\rho^*$ ), isobaric thermal expansivities ( $\alpha_p^*$ ), molar isobaric heat capacities ( $C_{p,m}^*$ ), ultrasonic speeds ( $u^*$ ), and the product  $K_{\nu,m}^*$  of the molar volume and isentropic compressibility of pure liquid components at 298.15 K

Component	$\rho^*$ (kg m <sup>-3</sup> )		$\alpha_p^*$ (K <sup>-1</sup> )	$C_{p,m}^*$ (J K <sup>-1</sup> mol <sup>-1</sup> )	$u^*$ (m s <sup>-1</sup> )		$K_{\nu,m}^*$ (mm <sup>3</sup> mol <sup>-1</sup> MPa <sup>-1</sup> )
	obs	lit.			obs	lit.	
Dipropylene glycol monomethyl ether	952.7		0.242 <sup>a</sup>	294.6 <sup>b</sup>	1303.1		618.14
Methanol	786.4	786.54 [6] 786.38 [7] 786.61 [8]	1.201 [9]	81.21 [7]	1100.6	1101.80 [8] 1102 [10]	1049.78
1-Propanol	799.4	799.50 [7] 799.35 [9]	1.003 [9]	144.10 [7]	1204.6	1205.17 [8]	862.09
1-Pentanol	811.1	811.15 [6] 811.10 [8]	0.893 [11]	208.4 [12]	1273.9	1275.18 [8]	759.72
1-Heptanol	819.2	819.50 [13] 818.9 [14]	0.845 <sup>b</sup>	271.7 <sup>a</sup>	132.7		692.49

<sup>a</sup>estimated using group additivity, <sup>b</sup>calculated from our measured densities

mixtures were prepared by mass at room temperature with a precision of +0.05 mg. Corrections were made for buoyancy. The composition of each mixture was obtained with an accuracy of  $1 \times 10^{-4}$  from the measured apparent masses of the components. All molar quantities were based upon the IUPAC table of atomic weights [15].

The speeds of sound in both the pure liquids and their mixtures were measured at 4 MHz using NUSONIC (Mapco, Model, 6080 Concentration Analyzer) velocimeter based on ring-around technique [16] with a single transducer cell. The ultrasonic speeds at 298.15 K are directly obtained from the average round trip period of the ultrasonic wave in a fixed path length between the piezoelectric transducer and reflector. The maximal error of the speed measured relative to water (1496.687 m s<sup>-1</sup> at 298.15 K) [17] is estimated to be less than 0.2 m s<sup>-1</sup>. Further details concerning this apparatus, experimental set-up and operational procedures have been described in our previous work [18,19]. A thermostatically controlled, well stirred water bath whose temperature was controlled to  $\pm 0.01$  K, was used for all measurements.

### 3. Results and discussion

Table 2 gives the experimental results of speed of sound at 298.15 K of all the binary mixtures at various mole fractions. Also listed there are deviations  $u^D$  of the ultrasonic speed from the values  $u^{id}$  calculated for ideal mixtures, the product  $K_{\nu,m}$  of the molar volume and the isentropic compressibility, and their corresponding excess molar quantity  $K_{\nu,m}^E$ .

The  $\kappa_s$  and  $K_{\nu,m}$  have been calculated from the relation:

$$\kappa_s = (\rho \cdot u^2)^{-1} = V_m (M \cdot u^2)^{-1}, \quad (1)$$

$$K_{\nu,m} = -(\partial V_m / \partial p)_s = V_m \cdot \kappa_s = V_m^2 / (M \cdot u^2), \quad (2)$$

where  $\rho$  is the density and  $M = \sum x_i M_i^*$  is the molar mass of the mixture.

**Table 2.** Ultrasonic speeds  $u$ , deviations  $u^D$  from ultrasonic speed in an ideal mixture,  $u^{id}$ , the product  $K_{\nu,m}$  of the molar volume and isentropic compressibility, and the corresponding excess quantity  $K_{\nu,m}^E$  for liquid mixtures at 298.15 K

$x$	$u$ (m s <sup>-1</sup> )	$u^D$ (m s <sup>-1</sup> )	$K_{\nu,m}$ (mm <sup>3</sup> mol <sup>-1</sup> MPa <sup>-1</sup> )	$K_{\nu,m}^E$ (mm <sup>3</sup> mol <sup>-1</sup> MPa <sup>-1</sup> )
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{CH}_3\text{OH}$				
0.0013	1101.9	1.09	42.77	-0.09
0.0024	1103.3	2.30	42.75	0.19
0.0037	1104.6	3.38	42.76	-0.29
0.0057	1106.2	4.63	42.79	-0.40
0.0072	1107.6	5.77	42.80	-0.49
0.0092	1109.3	7.11	42.83	-0.61
0.0117	1111.2	8.55	42.88	-0.74
0.0219	1119.1	14.47	43.08	-1.27
0.0356	1129.3	21.79	43.37	-1.93
0.0522	1141.2	29.93	43.74	-2.68
0.0749	1156.0	39.23	44.35	-3.57
0.0992	1169.9	46.92	45.13	-4.35
0.1327	1186.1	54.25	46.38	-5.17
0.1723	1203.5	60.99	47.93	-5.99
0.1992	1213.2	63.46	49.11	-6.37
0.2482	1229.4	66.69	51.32	-6.94
0.2873	1240.0	67.22	53.21	-7.21
0.3246	1248.7	66.59	55.10	-7.34
0.3509	1254.1	65.59	56.47	-7.38
0.3910	1261.4	63.44	58.63	-7.35
0.4378	1268.8	60.27	61.20	-7.21
0.4792	1274.2	56.72	63.56	-6.98
0.5303	1280.0	51.99	66.53	-6.61
0.5716	1284.5	48.37	68.93	-6.29
0.6069	1287.5	44.71	71.05	-5.94
0.6336	1289.4	41.72	72.69	-5.63
0.6540	1291.0	39.68	73.93	-5.41
0.6796	1292.5	36.71	75.53	-5.08
0.7414	1294.2	28.10	79.60	-4.04
0.7754	1295.6	24.09	81.78	-3.52
0.8071	1297.1	20.71	83.78	-3.06
0.8406	1298.3	19.91	85.94	-2.54
0.8762	1299.6	13.08	88.21	-1.99
0.8959	1300.2	10.91	89.48	-1.67

Table 2. (cont.)

$x$	$u$ (ms <sup>-1</sup> )	$u^D$ (ms <sup>-1</sup> )	$K_{i,m}^*$ (mm <sup>3</sup> mol <sup>-1</sup> MPa <sup>-1</sup> )	$K_{i,m}^k$ (mm <sup>3</sup> mol <sup>-1</sup> MPa <sup>-1</sup> )					
0.9156	1301.4	9.39	90.66	-1.44	0.0921	1277.8	8.35	83.51	-1.07
0.9309	1301.6	7.52	91.68	-1.16	0.1290	1278.8	10.62	83.97	-1.37
0.9507	1302.0	5.27	92.97	-0.82	0.1745	1279.7	12.61	84.60	-1.64
0.9631	1302.3	3.94	93.77	-0.61	0.2223	1281.7	15.24	85.14	-1.99
0.9717	1302.5	3.02	94.33	-0.47	0.2734	1283.4	17.08	85.78	-2.25
0.9849	1302.8	1.62	95.18	-0.26	0.3037	1284.1	17.63	86.21	-2.33
0.9929	1302.9	0.70	95.70	-0.11	0.3448	1285.4	18.45	86.75	-2.45
0.9970	1303.0	0.28	95.97	-0.04	0.4043	1287.1	18.96	87.56	-2.54
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_7\text{H}_{15}\text{OH}$									
0.0007	1204.7	0.11	64.83	-0.01	0.4472	1288.4	19.07	88.14	-2.57
0.0015	1204.9	0.32	64.84	-0.04	0.4965	1289.6	18.57	88.86	-2.51
0.0029	1205.2	0.63	64.86	-0.07	0.5396	1290.4	17.63	89.52	-2.39
0.0039	1206.1	1.55	64.81	-0.17	0.5750	1291.8	17.43	89.96	-2.37
0.0055	1206.9	2.36	64.79	-0.26	0.6138	1293.1	16.81	90.48	-2.30
0.0077	1207.1	2.58	64.86	-0.29	0.6562	1294.4	15.72	91.07	-2.17
0.0116	1208.1	3.31	64.92	-0.41	0.7028	1295.6	14.29	91.75	-1.97
0.0294	1212.1	7.61	65.23	0.88	0.7454	1296.8	12.81	92.36	-1.78
0.0389	1214.2	9.63	65.40	-1.11	0.7863	1297.9	11.19	92.96	-1.56
0.0495	1216.3	11.57	65.63	1.35	0.8273	1299.2	9.62	93.53	-1.34
0.0642	1219.3	14.25	65.93	-1.67	0.8549	1300.0	8.41	93.92	-1.18
0.0819	1222.7	17.12	66.31	-2.02	0.8839	1300.6	6.83	94.37	-0.96
0.0980	1225.7	19.50	66.67	-2.31	0.9062	1301.2	5.71	94.70	-0.80
0.1230	1230.3	22.93	67.23	-2.74	0.9244	1301.4	4.48	95.00	-0.36
0.1562	1235.8	26.50	68.05	-3.21	0.9426	1301.7	3.33	95.29	-0.47
0.1986	1242.5	30.23	69.13	-3.72	0.9618	1302.0	2.07	95.61	-0.29
0.2436	1249.4	33.46	70.28	-4.18	0.9780	1302.3	1.04	95.87	-0.15
0.2794	1252.3	33.14	71.50	-4.21	0.9894	1302.6	0.35	96.05	-0.05
0.3233	1260.0	34.54	73.37	-4.48	0.9970	1302.6	0.25	96.18	-0.04
0.3954	1265.7	34.72	74.95	4.58	$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_7\text{H}_{15}\text{OH}$				
0.4471	1270.5	33.77	76.61	-4.53	0.0011	1327.5	0.09	97.40	0.01
0.4867	1273.9	32.64	77.91	-4.43	0.0031	1327.3	-0.09	97.42	0.02
0.5236	1276.8	31.23	79.15	-4.29	0.0064	1327.1	0.03	97.42	0.01
0.5593	1279.9	30.11	80.30	-4.18	0.0090	1327.0	0.18	97.43	-0.01
0.5889	1282.0	28.67	81.32	-4.01	0.0130	1326.8	0.36	97.43	-0.04
0.6253	1284.4	29.69	82.58	-3.78	0.0229	1326.4	0.90	97.43	-0.11
0.6832	1287.9	23.17	84.63	-3.33	0.0348	1326.0	1.61	97.42	-0.19
0.7316	1290.7	20.08	86.35	-2.92	0.0452	1325.4	1.96	97.45	-0.23
0.7808	1293.3	16.71	88.11	-2.46	0.0596	1324.8	2.65	97.46	-0.32
0.8256	1296.0	13.92	89.69	-2.07	0.0803	1323.8	3.43	97.48	-0.42
0.8593	1297.3	11.13	90.96	1.67	0.1014	1322.7	4.08	97.52	-0.49
0.8920	1298.6	8.47	92.18	-1.28	0.1274	1321.3	4.74	97.57	-0.57
0.9196	1299.7	6.23	93.21	-0.95	0.1612	1219.7	5.64	97.61	-0.69
0.9347	1300.5	5.22	93.74	-0.79	0.1962	1218.2	6.55	97.64	-0.81
0.9469	1301.3	4.55	94.15	-0.69	0.2351	1216.9	7.70	97.61	-0.96
0.9573	1301.5	3.50	94.57	-0.53	0.2699	1216.0	8.81	97.56	-1.11
0.9731	1302.0	2.11	95.17	-0.32	0.3029	1214.1	8.64	97.67	-1.08
0.9887	1302.5	0.75	95.76	-0.12	0.3355	1312.7	8.79	97.70	-1.09
0.9945	1302.6	0.16	95.99	-0.03	0.3737	1311.9	9.62	97.63	-1.20
0.9988	1302.8	0.15	96.15	-0.02	0.4159	1311.4	10.69	97.49	-1.36
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_7\text{H}_{15}\text{OH}$									
0.0012	1274.2	0.04	82.55	-0.01	0.4763	1310.1	11.19	97.39	-1.43
0.0027	1274.2	0.06	82.57	-0.01	0.5322	1308.6	10.92	97.34	-1.39
0.0061	1274.2	0.29	82.62	-0.04	0.5839	1307.6	10.69	97.25	-1.37
0.0077	1274.5	0.69	82.60	-0.09	0.6402	1307.0	10.54	97.08	-1.36
0.0097	1274.7	1.02	82.61	-0.13	0.6819	1306.0	9.61	97.04	-1.23
0.0145	1275.0	1.63	82.65	-0.21	0.7168	1305.5	8.99	96.96	-1.16
0.0268	1275.5	2.87	82.77	-0.36	0.7706	1305.2	5.21	96.77	-1.03
0.0418	1276.2	4.41	82.92	-0.46	0.8238	1305.0	7.18	96.58	-0.94
0.0583	1276.7	5.76	83.11	-0.74	0.8775	1304.9	5.88	96.38	-0.77
0.0740	1277.2	6.99	83.29	-0.89	0.9193	1304.4	4.16	96.29	-0.54
					0.9336	1304.8	4.14	96.17	-0.55
					0.9484	1305.0	3.85	96.08	-0.52
					0.9696	1304.1	2.19	96.13	-0.29
					0.9857	1303.6	1.07	96.14	-0.14
					0.9942	1303.2	0.34	96.17	-0.04

The excess quantities were calculated from :

$$K_{v,m}^E = K_{v,m} - K_{v,m}^{id}, \quad (3)$$

where  $K_{v,m}^{id}$  [20,21] is

$$K_{v,m}^{id} = \sum x_i \left[ K_{v,i}^* - T \cdot A_{p,i}^* \left\{ \left( \frac{\sum x_i \cdot A_{p,i}^*}{\sum x_i \cdot C_{p,i}^*} \right) - \left( \frac{A_{p,i}^*}{C_{p,i}^*} \right) \right\} \right], \quad (4)$$

where,  $A_{p,i}^*$  is product of the molar volume and the isobaric expansivity,  $C_{p,i}^*$  is the isobaric molar heat capacity, and  $K_{v,i}^*$  is the product of the molar volume  $V_i^*$  and the isentropic compressibility  $\kappa_{v,i}^*$ . The  $\rho$  of the mixture at the appropriate mole fractions used in the ultrasonic speed measurements, were obtained from molar volumes of pure components and excess molar volumes from the cubic-spline interpolation reported in Ref. [1].

The deviations of the ultrasonic speeds from their values in an ideal mixture were calculated from [4,21] :

$$u^D = u - u^{id}, \quad (5)$$

$$\text{where } u^{id} = V_m^{id} / (M \cdot K_{v,m}^{id})^{1/2}, \quad (6)$$

Also, the mixing function  $\delta u$  is defined by

$$\delta u = u - \sum x_i u_i^*, \quad (7)$$

The values of  $K_{v,m}^E$ ,  $u^D$ , and  $\delta u$  were fitted for each mixture by an equation of the type :

$$F(x) = x(1-x) \sum_{i=0}^n a_i (2x-1)^i. \quad (8)$$

Values of coefficients  $a_i$ , calculated by the method of least squares with all points weighted equally, and their standard deviations  $\sigma$  are summarized in Table 3. Experimental results for  $K_{v,m}^E$ , and  $u^D$  are plotted against  $x$  in Figures 1 and 2.

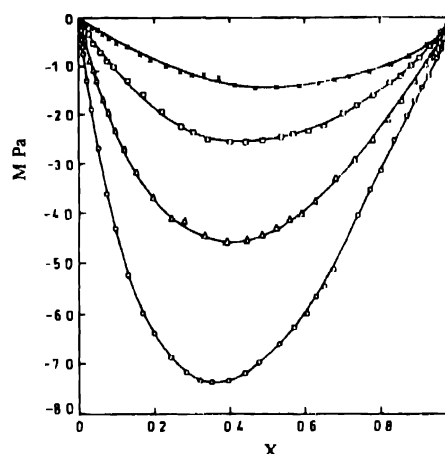


Figure 1. Values of  $K_{v,m}^E$  at 298.15 K for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$ , methanol (o), 1-propanol ( $\Delta$ ), 1-pentanol ( $\square$ ); 1-heptanol ( $\times$ ).

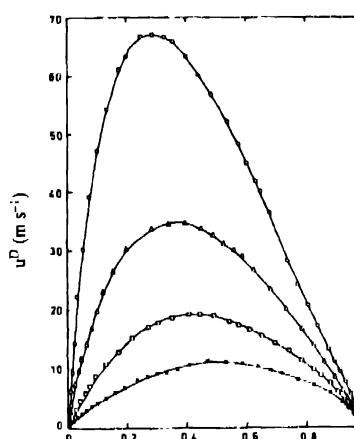


Figure 2. Values of  $u^D$  of the speeds of sound from their ideal values at 298.15 K for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$ , methanol (o), 1-propanol ( $\Delta$ ); 1-pentanol ( $\square$ ), 1-heptanol ( $\times$ ).

Table 3. Parameters of eq (8) and standard deviations  $\sigma$

$F(x)$	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$\sigma$
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{CH}_3\text{OH}$						
$\delta u/(\text{m s}^{-1})$	301.64	-171.10	66.25	-78.72	69.56	0.41
$u^D/(\text{m s}^{-1})$	221.82	-177.65	88.96	-119.74	103.05	0.44
$K_{v,m}^E/(\text{mm}^3 \text{ mol}^{-1} \text{ MPa}^{-1})$	-27.64	13.62	-3.43	8.59	-8.57	0.04
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_3\text{H}_7\text{OH}$						
$\delta u/(\text{m s}^{-1})$	84.39	-31.15	21.14	-17.96		0.35
$u^D/(\text{m s}^{-1})$	128.42	-66.69	41.90	-27.79		0.36
$K_{v,m}^E/(\text{mm}^3 \text{ mol}^{-1} \text{ MPa}^{-1})$	-17.54	6.44	-3.61	2.79		0.04
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_5\text{H}_{11}\text{OH}$						
$\delta u/(\text{m s}^{-1})$	4.86	1.02	9.40	-8.63		0.23
$u^D/(\text{m s}^{-1})$	74.21	-17.87	11.55	-3.98		0.23
$K_{v,m}^E/(\text{mm}^3 \text{ mol}^{-1} \text{ MPa}^{-1})$	-10.04	1.87	-1.30	0.42		0.03
$x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_7\text{H}_{15}\text{OH}$						
$\delta u/(\text{m s}^{-1})$	-24.66	7.73	-3.35	3.42	15.40	0.26
$u^D/(\text{m s}^{-1})$	44.11	1.44	-9.79	12.04	32.65	0.30
$K_{v,m}^E/(\text{mm}^3 \text{ mol}^{-1} \text{ MPa}^{-1})$	-5.59	-0.37	-1.20	-1.77	-4.14	0.04

We have attempted to explain the physico-chemical behaviour of the mixtures in order to explore the strength and nature of the interactions between the components by deriving various thermodynamic parameters from the ultrasonic speed and density data. Various parameters such as intermolecular free length  $L_f$  [23], van der Waal's constant  $b$ , molecular radius  $r$  [23], geometrical volume  $B$ , molar surface area  $Y$ , available volume  $V_a$  [22], molar sound velocity  $R$  [24], collision factor  $S$  [25], specific acoustic impedance  $Z$  [26], relative association  $R_A$  [27], and molecular association  $M_A$  [28] have been calculated using the following relations :

$$L_f = K/(u \cdot \rho^{1/2}), \quad (9)$$

$$b = (M/\rho) - (RT/\rho u^2) \left\{ \left[ 1 + (Mu^2/3RT) \right]^{1/2} - 1 \right\}, \quad (10)$$

$$r = (3b/16\pi N)^{1/3}, \quad (11)$$

$$B = (4/3)\pi r^3 N, \quad (12)$$

$$Y = (36\pi N B^2)^{1/3}, \quad (13)$$

$$V_a = V(1 - u/u_\infty), \quad (14)$$

$$V_0 = V - V_a, \quad (15)$$

$$R = M \cdot u^{1/3} / \rho, \quad (16)$$

$$S = uV/u_\infty B, \quad (17)$$

$$Z = u\rho, \quad (18)$$

$$R_A = (\rho_{\text{mix}}/\rho)(u/u_{\text{mix}})^{1/3}, \quad (19)$$

$$M_A = \left[ (u_{\text{mix}}/\sum x_i u_i)^2 - 1 \right], \quad (20)$$

where  $L_f$  is the free length of ideal mixing,  $K$  is a temperature dependent constant ( $= (93.875 + 0.375 T) \times 10^{-8}$ ) [22],  $V_0$  is the volume at absolute zero,  $u_\infty$  is taken as 1600 m s<sup>-1</sup>. These parameters are listed in Table 4 for the pure components. The variation of  $V_a$ ,  $L_f$ ,  $R_A$ ,  $Z$ ,  $R$ , and  $M_A$  for mixtures with mole fraction of  $x$  are graphically shown in Figures 3 and 4.

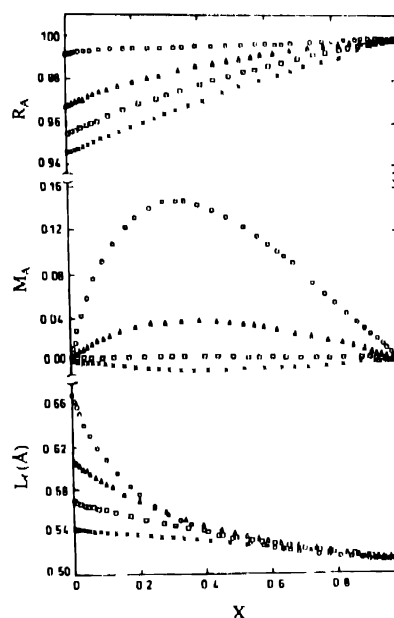


Figure 3.  $L_f$ ,  $R_A$  and  $M_A$  for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$ , methanol (o), 1-propanol ( $\Delta$ ), 1-pentanol ( $\square$ ), 1-heptanol (x).

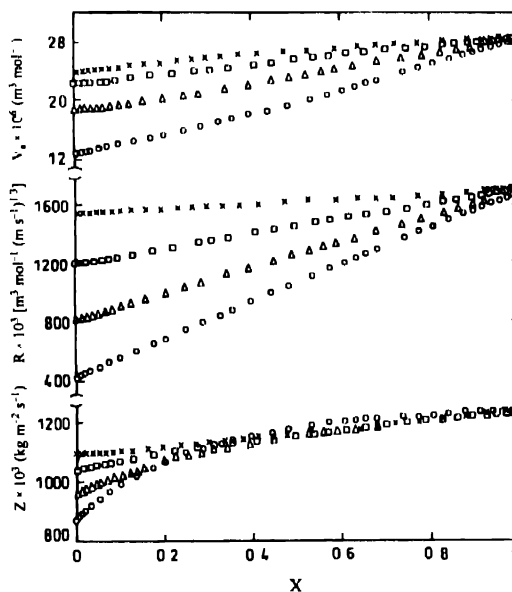
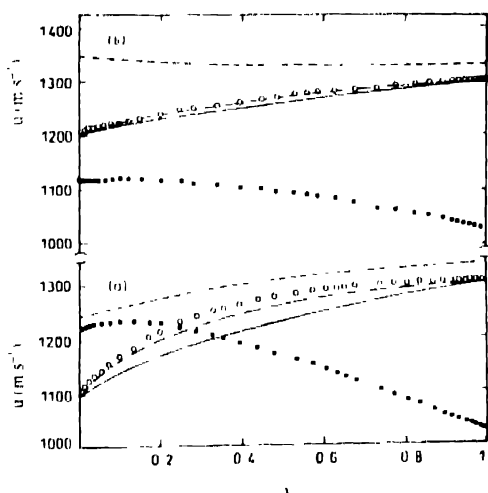


Figure 4.  $Z$ ,  $R$  and  $V_a$  for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$ , methanol (o), 1-propanol ( $\Delta$ ), 1-pentanol ( $\square$ ), 1-heptanol (x).

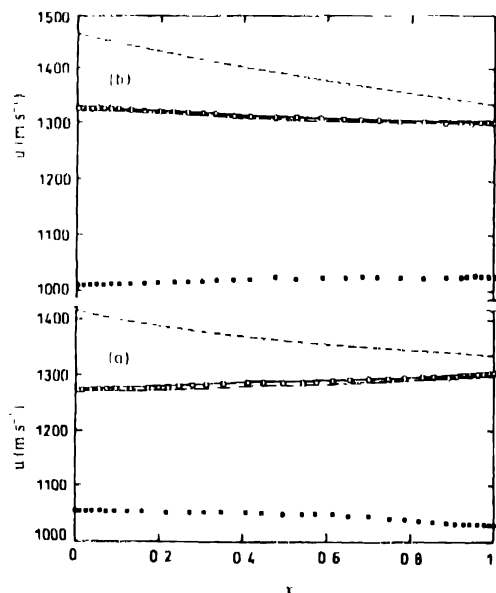
Table 4. Values of the derived parameters of the pure components at 298.15 K

Component	$b \times 10^6$ m <sup>3</sup>	$r$ nm	$B \times 10^6$ m <sup>3</sup> mol <sup>-1</sup>	$S$	$R \times 10^3$ m <sup>3</sup> mol <sup>-1</sup> (m s <sup>-1</sup> ) <sup>1/3</sup>	$V_a \times 10^6$ m <sup>3</sup> mol <sup>-1</sup>	$L_f$ Å	$V_0 \times 10^6$ m <sup>3</sup> mol <sup>-1</sup>	$Y$ Å	$Z \times 10^{-3}$ kg m <sup>-2</sup> s <sup>-1</sup>
Dipropylene glycol monomethyl ether	148.05	0.245	37.08	3.42	1699	28.86	0.512	126.69	45.31	1241
Methanol	36.86	0.154	9.21	3.04	421	12.71	0.667	28.03	17.91	865
1-Propanol	69.69	0.191	17.57	3.22	800	18.58	0.605	56.59	27.54	962
1-Pentanol	102.09	0.216	25.41	3.41	1178	22.15	0.568	86.53	35.22	1033
1-Heptanol	133.20	0.236	33.15	3.52	1545	23.93	0.542	116.69	42.05	1087

It is observed from Figures 3-6 and Table 2 that  $u$ ,  $R_A$ ,  $Z$ ,  $R$ , and  $V_a$  increase with mole fraction of  $x$ , while  $K_{v,m}$  and



**Figure 5.** Experimental and calculated ultrasonic speeds  $u$ ,  $u_{\text{calc}}$ ,  $u_{\text{CTT}}$ ,  $u_{\text{I}}$ ,  $u_{\text{N}}$ ,  $u_{\text{II}}$ ,  $u_{\text{III}}$  for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$  (a) methanol and (b) 1-propanol



**Figure 6.** Experimental and calculated ultrasonic speeds  $u$ ,  $u_{\text{calc}}$ ,  $u_{\text{CTT}}$ ,  $u_{\text{I}}$ ,  $u_{\text{N}}$ ,  $u_{\text{II}}$ ,  $u_{\text{III}}$  for  $x\text{CH}_3[\text{O}(\text{CH}_2)_3]_2\text{OH} + (1-x)\text{C}_n\text{H}_{2n+1}\text{OH}$ , (a) 1-pentanol and (b) 1-heptanol

$L_f$  decrease. The decrease in  $K_{v,m}$  and  $L_f$  with  $x$  in the present investigations, indicates significant interaction between dipropylene glycol monomethyl ether and methanol molecules. The addition of dipropylene glycol monomethyl ether to alkanol tends to cause breaking of self-associated alkanol molecules with a consequent increase in  $u$  and  $L_f$ . However, because of simultaneous formation of strong hydrogen bonds between the unlike molecules, there is a compensating effect resulting in an overall decrease in  $K_{v,m}$  and  $L_f$  or increase in  $u$  with  $x$ .

In the present investigation, relative association  $R_1$  is found to increase with mole fraction of dipropylene glycol monomethyl ether (Figure 3) for all the mixtures. Relatively higher values of  $R_A$  for dipropylene glycol monomethyl ether-methanol systems, signifies that unlike interactions are relatively strong compared to like interactions; the former tends to increase while the latter causes a decrease in  $R_1$ . Similarly, Figure 3 shows the large deviations in  $M_1$  for dipropylene glycol monomethyl ether + methanol system and these deviations decrease with increase in the chain length of the alkanol. Thus, it concluded that the non-ideality of the systems varies in the order methanol > 1-propanol > 1-pentanol > 1-heptanol. A sharp increase in  $Z$  and  $R$  with  $x$  (Figure 4) suggests strong interaction between the dipropylene glycol monomethyl ether and methanol molecules.

For all the mixtures studied,  $K_{v,m}^L$  is negative over the whole mole fraction range and shows a minimum in the sequence: methanol > 1-propanol > 1-pentanol > 1-heptanol, while in the same sequence, the minimum is shifted to lower values of  $x$ . This behaviour may be compared with the  $K_{v,m}^L$  results for diethylene glycol monomethyl [29] ether—the magnitude of  $K_{v,m}^L$  decreases from methanol to 1-propanol with the replacement of ethyl by propyl groups at the middle of diethylene glycol monomethyl ether and then the trend is reverse. The overall behaviour of  $K_{v,m}^L$  is similar to that of  $u^D$  but with an opposite variation with the number of carbon atoms in the alcohol molecule. However, the behaviour of  $K_{v,m}^L$  is inconsistent with  $V_m^L$  for 1-pentanol and 1-heptanol [1]. Also, the behaviour of excess molar volume seems to be consistent with a minimum value of  $K_{v,m}^L$  and a maximum value for  $u^D$  with methanol and 1-propanol. This is normal because  $u$  is generally higher when the structure has high rigidity. Negative values of  $K_{v,m}^L$  mean that the structure is less compressible than the corresponding ideal mixture, suggesting that there may be strong intermolecular hydrogen bonding with methanol and 1-propanol. As the ether is added to alcohol, thereby causing a breakdown of self-associated ether, or both and hence contribute to a denser packing of the molecules through hydrogen bonding, the speed of sound increases and  $K_{v,m}^L$  decreases. However,  $V_m^L$  is positive for 1-pentanol and 1-heptanol, although  $K_{v,m}^L$  is negative and  $u^D$  is likewise positive from methanol to 1-heptanol, indicating that when the mixture is created "excess free volumes" decreases and is higher in mixtures containing dipropylene glycol monomethyl ether with methanol. The effect is that with increasing the  $n$ -alkyl chain end length, interstitial accommodation become less important, and the molecules of the two components cannot be easily accommodated

This additional rigidity is a good reason for the positive values of  $u^D$ . As suggested earlier, the volume behaviour of dipropylene glycol monomethyl ether + n-alcohol is the result of several opposing effects; the present results for  $K_{\infty}^L$  and  $u^D$  support this suggestion. Finally, from Figure 7, a similar but opposite variation of  $K_{\infty}^L$  and  $u^D$  with the n-alkyl chain end length of alcohol has been found, whilst  $\delta u$  decreases regularly with  $n$ . Again, it is interesting to note that both  $\delta u$  and  $u^D$  can be correlated well with the  $K_{\infty}^L$ .

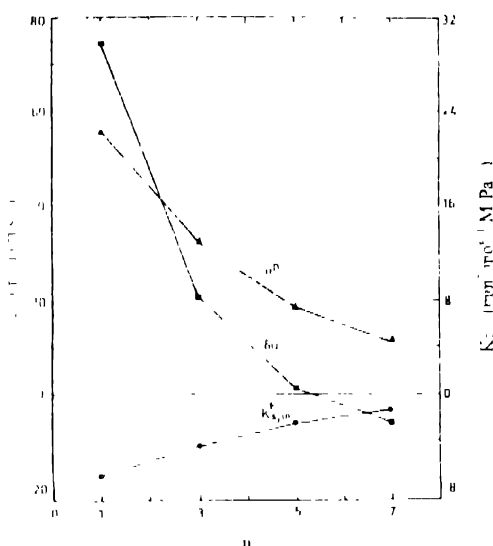


Figure 7. Plots of  $K_{\infty}^L$  (●),  $u^D$  (▲),  $\delta u$  (■) at 298.15 K against  $n$  for (1)  $\text{C}_2\text{H}_5\text{OH}$ , (2)  $\text{C}_3\text{H}_7\text{OH}$ , (3)  $\text{C}_4\text{H}_9\text{OH}$ , (4)  $\text{C}_5\text{H}_{11}\text{OH}$ , (5)  $\text{C}_6\text{H}_{13}\text{OH}$ , (6)  $\text{C}_7\text{H}_{15}\text{OH}$ .

For comparison, we have calculated the theoretical values of ultrasonic speeds from the following empirical equations:

Collision Factor Theory [23]:

$$u_{CTT} = u_{\infty} \left\{ xS_1 + (1-x)S_2 \right\} \left[ \left\{ xB_1 + (1-x)B_2 \right\} / V \right], \quad (21)$$

Free length theory [22]:

$$u_{FLT} = K / (L_f \rho^{1/2}), \quad (22)$$

Junjie equation [30]:

$$u_j = \left\{ (xM_1 / \rho_1) + (1-x)M_2 / \rho_2 \right\} / \left[ \left\{ xM_1 + (1-x)M_2 \right\}^{1/2} \times \left\{ (xM_1 / \rho_1 u_1^2) + (1-x)M_2 / \rho_2 u_2^2 \right\}^{1/2} \right], \quad (23)$$

Nomoto equation [31]:

$$u_N = \left[ \left\{ xR_1 + (1-x)R_2 \right\} / \left\{ xV_1 + (1-x)V_2 \right\} \right]^3. \quad (24)$$

The computed  $u_{CTT}$ ,  $u_{FLT}$ ,  $u_j$  and  $u_N$  values are shown in Figures 5 and 6 for comparison with experimental values for

all the mixtures. The results clearly indicate that the simple Nomoto expression and collision factor theory predict the experimental data extremely well for all the mixtures except with 1-propanol whereas the Junjie expression shows the maximum deviation and the free length theory gives the greatest deviations for all the present binary mixtures.

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### References

- [1] A Pal and H Kumar *J. Solution Chem.* (2001) (in press).
- [2] A Pal and A Kumar *Acoust. Letts.* **22**, 168 (1999).
- [3] A Pal, S Sharma and A Kumar *Indian J. Pure Appl. Phys.* **38**, 174 (2000).
- [4] G Douheret, A Pal and M I Davis *J. Chem. Thermodyn.* **22**, 99 (1990).
- [5] G Douheret, C Moreau and A Viillard *Fluid Phase Equilib.* **26**, 221 (1986).
- [6] J A Riddick and W B Bunger *Organic Solvents: Physical Properties and Methods of Purification* 3rd edn (New York: Wiley-Interscience) (1970).
- [7] G C Benson, P I D'Arcy and O Kiyohara *J. Solution Chem.* **9**, 931 (1980).
- [8] O Kiyohara and G C Benson *J. Chem. Thermodyn.* **11**, 861 (1979).
- [9] G C Benson and O Kiyohara *J. Solution Chem.* **9**, 791 (1980).
- [10] A Arce, J Martinez-Apitos, J Mendoza and A Soto *J. Chem. Engg. Data* **41**, 724 (1996).
- [11] J I Hales and J H Ellender *J. Chem. Thermodyn.* **8**, 1177 (1976).
- [12] R C Wilhoit and B J Zwolinski *Phys. Chem. Ref. Data supplement No. 1* 2 (1973).
- [13] J A Riddick, W B Bunger and T Sakano *Organic Solvents: Physical Properties and Method of Purification* 4th edn (New York: Wiley-Interscience) (1986).
- [14] M I Aralaguppi, C V Iadar and T M Aminabhavi *J. Chem. Engg. Data* **44**, 216 (1999).
- [15] IUPAC Commission on Atomic Weights and Isotopic Abundance, 1985, *Pure Appl. Chem.* **50**, 1677 (1986).
- [16] R Garnsev, R J Boe, R Mahoney and J A Litovitz *J. Chem. Phys.* **50**, 5222 (1969).
- [17] V A Del Grosso and C W Mader *J. Acoust. Soc. Am.* **52**, 1442 (1972).
- [18] A Pal and G Dass *J. Indian Chem. Soc.* **76**, 446 (1999).
- [19] Y P Singh *PhD Thesis* (University of Kurukshetra, India) (1996).
- [20] G C Benson and O Kiyohara *J. Chem. Thermodyn.* **11**, 1061 (1979).
- [21] G Douheret, C Salgado, M I Davis and J I Oya *Thermochim. Acta* **207**, 313 (1992).

- [22] B Jacobson *J. Chem Phys* **20** 927 (1952)
- [23] W Schaaffs *Acustica* **33** 272 (1975)
- [24] M R Rao *Indian J. Phys.* **14** 109 (1940)
- [25] W Schaaffs *Z. Phys* **114** 110 (1974)
- [26] R K Dewan, C M Gupta and S K Mehta *Acustica* **65** 245 (1988)
- [27] A Ali and A K Nain *Indian J. Pure Appl. Ultrason.* **22** 10 (2000)
- [28] S K Mehta, R K Chauhan and R K Dewan *J. Chem Soc Faraday Trans.* **92** 1167 (1996)
- [29] A Pal and A Kumar *Acoust. Letts* **20** 203 (1997)
- [30] Z Junjie *J China Univ Sci Techn* **14** 298 (1984)
- [31] O Nomoto *J. Phys Soc Jpn.* **13** 298 (1958)