

1 **Line Transect Sampling of Primates: Can Animal-to-Observer**  
2 **Distance Methods Work?**

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14 **Short title:** Use of AODs in line transect sampling

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25 **Abstract** Line transect sampling is widely used for estimating abundance of primate  
26 populations. Animal-to-observer distances (AODs) are commonly used in analysis, in  
27 preference to perpendicular distances from the line. This is in marked contrast with  
28 standard practice for other applications of line transect sampling. We formalize the  
29 mathematical shortcomings of approaches based on AODs, and show that they are likely  
30 to give strongly biased estimates of density. We review papers that claim good  
31 performance for the method, and explore this performance through simulations. These  
32 confirm strong bias in estimates of density using AODs. We conclude that AOD  
33 methods are conceptually flawed, and that they cannot in general provide valid estimates  
34 of density.

35

36 **Keywords** animal-to-observer distances • distance sampling • estimating primate density  
37 • Kelker strip • modified Kelker method • primate surveys

38

39

40 **Introduction**

41 Line transect sampling is a ‘distance sampling’ method (Buckland *et al.*, 2001, 2004),  
42 widely used for estimating the abundance of wild animal populations. In most areas of  
43 application, disciplines have standardized their methods and use the software package

44 Distance (Thomas *et al.*, in press). However, methods that in other disciplines are  
45 generally considered to be obsolete are still often used and recommended in primatology:  
46 the Kelker strip (Kelker, 1945) and the ‘modified Kelker method’ (Struhsaker, 1981),  
47 which covers a range of methods based on assessing the effective width of the searched  
48 strip from animal-to-observer distances or AODs. In addition, survey design issues are  
49 often ignored, and the precision of abundance estimates is often not quantified,  
50 compromising studies designed to compare the performance of different methods.

51 In this paper, we first consider strip transect sampling, and the assumptions under  
52 which it is effective. We then explore AOD methods that are conceptually related to strip  
53 transect sampling. Plumptre and Cox (2006) noted that such methods have no  
54 mathematical basis; here we show that they are based on an erroneous interpretation of  
55 the AOD distribution. We review studies that claim good performance of the approach,  
56 and assess its performance using simulation.

57

## 58 **Strip Transect and Related Methods**

### 59 Standard Strip Transect Sampling

60 In standard strip transect sampling (Buckland *et al.*, 2001), we place lines at random in  
61 the survey region, or more commonly, we randomly superimpose a set of equally-spaced  
62 lines on the survey region. An observer walks along each line, recording all animals  
63 within a distance  $w$  of the line, where  $w$  is the strip half-width. Given random placement  
64 of an adequate number of lines through the survey region, this density estimate is  
65 representative of the whole survey region, allowing abundance within that region to be  
66 estimated.

67 Many animals, including primates, tend to occur in groups, termed ‘clusters’ in  
68 the distance sampling literature. In strip transect sampling, we have two main options for  
69 dealing with groups. The first is to ignore them; all animals within a sampled strip are

70 counted, without regard to the groups. Thus for groups that extend beyond the survey  
71 strip, some animals are counted and some not. The second option is to count the whole  
72 group if its centre is within the sampled strip, and not if its centre is beyond the strip.

73

#### 74 *Assumptions*

75 If groups are ignored, the key assumptions are:

- 76 1. Animals that are located within a sampled strip prior to any response to the observers  
77 are certain to be detected and counted.
- 78 2. Animals that are located outside the sampled strips are not counted.

79

80 If groups are the recording unit, the key assumptions are:

- 81 1. Groups whose centres are within a sampled strip prior to any response to the observers  
82 are certain to be detected and counted.
- 83 2. The size of each of these groups is recorded without error.
- 84 3. Groups whose centres are outside of the sampled strip are not recorded.

85

86 In either case, we also assume that there is an adequate sample of randomly-  
87 distributed strips, or a grid of strips randomly positioned, in the survey region. This  
88 assumption is not usually listed, because it is an aspect of survey design, and survey  
89 design is under our control: if we use an appropriate design, we guarantee that the  
90 assumption is met. However, non-randomized designs (e.g. transects along pre-existing  
91 trails) with inadequate replication (fewer than 10 lines; Buckland *et al.* (2001:232)  
92 recommend at least 10-20 lines) are frequent in primate surveys, so we state the  
93 assumption explicitly here. In practice, we usually prefer systematic random designs to  
94 designs in which each transect is independently randomized.

95

97 If individual animals are counted, we can seldom be sure of detecting all animals within  
98 the sampled strips. Even if this is possible, it can be very difficult to determine whether a  
99 detected animal is within the strip, especially for animals close to the edge of the strip. If  
100 groups are recorded, it is generally difficult to estimate the location of the group centre.  
101 For these reasons, it has become standard practice amongst some survey teams to record  
102 the position of the group as being at the location of the first-detected animal (Struhsaker,  
103 1981; Hassel-Finnegan *et al.*, 2008). This animal is more likely to be within the sampled  
104 strip than a randomly selected animal, and consequently, the strategy leads to positive  
105 bias in density estimates. This bias is substantial if average group spread is of similar  
106 magnitude to the strip half-width  $w$ .

107         Line transect sampling (Buckland *et al.*, 2001) relaxes the assumption that all  
108 groups in the strip are detected, but generates similar bias in density estimates if the  
109 location of the group is taken as the location of the first-detected animal. This source of  
110 bias is well-known (e.g. Whitesides *et al.*, 1988), yet the practice persists, and as a  
111 consequence, standard line transect sampling is often considered to overestimate density  
112 in the primate literature (Hassel-Finnegan *et al.*, 2008). Buckland *et al.* (in review)  
113 discuss how to implement standard line transect methods for primates.

114

115 

### The Kelker Strip

116 The Kelker strip (Kelker, 1945) is a variation on strip transect sampling. Shortest  
117 distances of detected animals from the line (so-called perpendicular distances) are  
118 recorded, as for line transect sampling. These distances are placed into intervals, and  
119 plotted in a histogram, from which the distance out to which all animals are detected is  
120 assessed. When used for primate surveys, groups are recorded, together with the distance  
121 of each group from the line.

122

123 *Assumptions*

124 The assumptions of this approach are essentially the same as for strip transect sampling,  
125 although we now estimate the strip half-width from the distribution of distances from the  
126 line, which requires accurate estimation of distances to the centres of detected groups,  
127 including those groups that are detected beyond the strip.

128

129 *Problems*

130 The method shares with strip and line transect sampling the difficulty of identifying the  
131 location of group centres. For strip transect sampling, this problem can be avoided if it is  
132 possible to record all individuals in the strip, and accurately determine that they are in the  
133 strip. However, because the Kelker strip requires distances from the line to be recorded,  
134 the distance of each detected animal from the line must be recorded to implement this  
135 approach. When groups are recorded, and distances from the line are taken as the  
136 distance of the first animal detected from the line, the method is prone to exactly the  
137 same upward bias as strip and line transect sampling.

138         The method also has problems that line transect sampling does not. First, it is  
139 subjective. Identification of the distance up to which all groups are detected can vary  
140 between analysts and between different choices of interval cutpoints for the histogram.  
141 Second, variance estimates ignore the uncertainty in estimating this distance, and so tend  
142 to be underestimates. Third, many observations are discarded because many animals are  
143 detected beyond the distance at which detection can be assumed certain, reducing  
144 precision. Fourth, for small sample sizes, the method tends to give biased estimates of  
145 abundance. When sample size is small, sampling variation tends to be large, and the  
146 choice of cutpoint can be influenced by chance variation in the proportion of detections  
147 close to the line. If by chance several groups are detected close to the line, there is a

148 tendency to set the cutpoint too small, which can lead to positive bias (Fig. 1). However,  
149 if groups are missed whose centres are inside the selected cutpoint, negative bias will  
150 occur. It is difficult to ensure a balance between these biases.

151

## 152 AOD Methods

153 AODs (called ‘radial distances’ in the line transect literature) are often easier to measure  
154 than perpendicular distances from the line. In this case, observers generally also record  
155 the sighting angle, allowing the perpendicular distance to be calculated (Buckland *et al.*,  
156 2001:5). However, line transect methods that model the AOD rather than the  
157 perpendicular distance have a long history (e.g. Hayne, 1949). They are now seldom  
158 used, as the models are not plausible representations of the detection process (Hayes and  
159 Buckland, 1983). Despite this failing, they were mathematically coherent models.  
160 Unfortunately, this is not true of the AOD models used by primatologists. These have  
161 their origins in surveys conducted in Kibale Forest, Uganda by Struhsaker (1975).  
162 Initially during surveys carried out between 1970-1972, he plotted positions of monkey  
163 groups on maps and from these he calculated the perpendicular distance of each group  
164 from the line. It is not stated what he plotted on the maps: nearest animal, first animal  
165 detected, or group centre. In later surveys in 1974-76, he estimated the AOD by eye.  
166 The density estimates obtained using the perpendicular distances tended to overestimate  
167 the ‘known’ primate density based on knowledge of group sizes and home range of  
168 habituated groups (Struhsaker, 1975). This appears to be because perpendicular distance  
169 from the line to the nearest animal of the group was recorded, as nearly 40% of groups  
170 were recorded at zero distance (suggesting that nearly 40% of detected groups straddled  
171 the line). He then arbitrarily chose to calculate the mean and maximum AOD across  
172 detected groups, where AOD for a group was the distance to the first detected animal,  
173 and used these as estimates of the strip half-width for a Kelker strip analysis. The mean

174 AOD tended to overestimate density of primates while the maximum AOD tended to  
175 underestimate density. He then defined a ‘maximum reliable AOD’ – the distance at  
176 which the frequency of sightings falls when plotting AOD against number of sightings.  
177 This too was used as an estimate of the strip half-width. In each case, only AODs less  
178 than the estimated half-width were included in the density estimate (Struhsaker, 1981).  
179 We can find no published results that show that he compared methods based on  
180 perpendicular distances and AODs measured in the field.

181

### 182 *Assumptions*

183 Beyond the assumption that the selected truncation distance results in a complete count of  
184 primate groups within that same distance of the line, assumptions are never explicitly  
185 stated for the modified Kelker method and its AOD variants. In fact, there is no coherent  
186 framework under which the methods can be justified, so that it is not possible to specify a  
187 full set of assumptions, as will be seen below.

188

### 189 *Problems*

190 The method, like the Kelker strip, is subjective when the ‘maximum reliable AOD’ is  
191 used, so that different analysts may select different truncation distances, and estimation is  
192 sensitive to the choice. When there is a subjective element in the analysis, and estimation  
193 is sensitive to the subjective choice, it is good practice for assessments of the  
194 performance of the method based on populations with known density to be performed  
195 blind – that is, the analyst should be unaware of the true density when generating  
196 estimates.

197         Authors who use AOD methods appear not to estimate the precision of their  
198 estimates. Of the papers reviewed below that use the method, only Fashing and Cords  
199 (2000) quoted standard errors, and those were based on repeat surveys of a single line, so



200 do not reflect spatial variation (so-called pseudo-replication, Hurlbert, 1984). Variance  
201 could be estimated as for strip transect sampling, although this fails to incorporate  
202 uncertainty in estimating the strip width.

203         However, there is a more serious problem with these methods, in that their  
204 conceptual framework is erroneous. The methods confuse a probability density function  
205 with a detection function. When a histogram is plotted, showing frequencies of  
206 detections by distance intervals, then the histogram, if rescaled so that the total area of the  
207 histogram bars is unity, provides an empirical estimate of a probability density function:  
208 it shows the relative frequencies of detections by distance. By contrast, the detection  
209 function is the probability of detecting a group, as a function of distance of that group  
210 from the line or, for AOD methods, from the observer. When perpendicular distances  
211 from the line are used, the two functions have the same shape (Buckland *et al.*, 2001:53),  
212 so that the histogram may be used for example to assess the perpendicular distance at  
213 which probability of detection starts to fall. However, if AODs are used, this is no longer  
214 the case (see e.g. Buckland *et al.*, 2001:148). The point at which frequencies start to fall  
215 does not correspond with the point up to which probability of detection is certain. To  
216 illustrate this, we simulated data using the hazard-rate model  $g(y) = 1 - \exp\{-(y/20)^{-2}\}$   
217 for the detection function (Fig. 2), where  $g(y)$  is the probability of detecting an animal  
218 group whose centre is at perpendicular distance  $y$  from the line. Groups had mean size of  
219 three, and half the group spread was 10m. (Full details are given in the simulation study  
220 section below.) We show a histogram of simulated AODs (Fig. 3). The ‘maximum  
221 reliable AOD’ might be taken as 30m or 40m, depending on the judgement of the analyst,  
222 but detectability starts to fall away at around 10m (Fig. 2). The effect is substantial; over  
223 60% of groups are undetected at 30m, and nearly 80% at 40m. In other words, for these

224 values of the maximum reliable distance, we can expect underestimation of density by  
225 over 60% (30m) or nearly 80% (40m).

226 This flaw in the method is self-evident if you consider what is being done. For  
227 example, Hassel-Finnegan (2008) report in their Fig. 2 an estimate of 55m, estimated  
228 from AODs, up to which detection is considered to be certain for white-handed gibbons  
229 *Hylobates lar carpenteri*. However, of 155 detections, 141 of these were not detected  
230 until they were closer to the observer than 55m. Indeed, the median AOD is under 35m.  
231 If animals at 55m were certain to be detected, then AODs of less than 55m should not be  
232 observed – as the observer approaches an animal, then it will be detected at the certain  
233 detection distance of 55m, if not at a greater distance.

234 Marshall *et al.* (2008), while acknowledging that the method lacks a mathematical  
235 basis, state erroneously: ‘Because sighting distance is used rather than distance to  
236 transect, the pattern of decline with distance is a true detection function.’ This is not the  
237 case (Fig. 3). Hence their belief that the method should be used when other methods fail  
238 lacks credibility.

239 There is a further inconsistency in the method, when the histogram is used to  
240 identify the distance up to which detection is certain. AODs are used to estimate  
241 (erroneously) this distance. However, this is then assumed to be the half-width of a strip  
242 centred on the line, rather than the radius of a circle centred on the observer. It is also  
243 used to truncate detections whose AODs are larger. Suppose we use 55m as the  
244 truncation AOD as in Hassel-Finnegan *et al.* (2008). A group that is detected when still  
245 80m away, but which is located on the line, is therefore excluded from the count – but its  
246 location is right at the centre of the strip to which the count supposedly relates.

247 If data quality were otherwise good, each variation of the method would clearly  
248 undercount groups within the sampled strip. If by chance the method does produce a  
249 good estimate, it may be a consequence of defining group location with respect to the

250 observer to be the location of the first detected animal of a group: the upward bias  
251 generated by this strategy might cancel with the downward bias of the modified Kelker  
252 method. There is no assurance that the biases will cancel in general.

253

#### 254 **Review of Papers that have Assessed AOD Methods**

255 Struhsaker (1981) proposed use of the modified Kelker method on the basis that it gave  
256 rise to the least biased estimates of density of red colobus monkeys *Piliocolobus*  
257 *oustaleti*. However, the reason for overestimation of density in his study is evident from  
258 the following quote: ‘... nearly 40% of the 166 sightings of red colobus were over the  
259 census transect and were scored as zero meters from the trail ...’ He does not clarify how  
260 distances were measured in the field, but as all groups ‘over the census transect’ were  
261 recorded as being at zero distance, we can infer that distance of the nearest animal to the  
262 transect was recorded, with predictable overestimation of density; any attempt to salvage  
263 density estimates from such poor distance data will inevitably be subjective and *ad hoc*.  
264 (Another possibility is that the position of the line was not well-defined, so that any  
265 animal or animal group that was close to the line was simply recorded as on the line.)

266 Defler and Pintor (1985) assessed the performance of the three modified Kelker  
267 methods based on mean AOD, maximum reliable AOD and maximum AOD, against  
268 known densities of three species (red howler monkey *Alouatta seniculus*, collared titi  
269 monkey *Callicebus torquatus* and brown capuchin *Cebus apella*) in Colombia. Their  
270 design comprised a single, non-random transect; lack of randomization means that we  
271 cannot be confident that the density along the line is representative, and lack of  
272 replication means that there is no basis for assessing precision of estimates. Their results  
273 were very mixed. Mean AOD led to estimated biases of +12%, -30% and +538% for the  
274 three species. Maximum reliable AOD gave estimated biases of +12%, -12% and  
275 +668%. Maximum AOD resulted in estimated biases of -25%, -56% and +226%.

276 Chapman *et al.* (1988) used just 5 transects, subjectively placed. Their known  
277 populations comprised just a single group of each of two species (white-headed capuchin  
278 *Cebus capucinus* and mantled howler monkey *Alouatta palliata*) in Costa Rica. They  
279 used six different methods of measuring distances: ‘the mean, maximum and reliable  
280 perpendicular distance from the transect to the animal first sighted and the mean,  
281 maximum and reliable distance from the observer to the animal.’ Thus all six methods  
282 were prone to bias by assuming that the first animal sighted was at the centre of the  
283 group. The authors did not quantify the precision of their estimates, and did not define  
284 what a ‘reliable’ distance is (there is not a unique definition of it in the literature). Their  
285 estimates show poor performance of all methods, with no clear winner, yet they come  
286 down heavily in favour of methods based on AODs on the grounds that ‘sightings that  
287 occur directly over the transect or at a steep angle to it, are likely to cause bias.’ They do  
288 not clarify why. They also claim that the ability of the observer to estimate perpendicular  
289 distance will be limited when the terrain is rough, which in our view is not a compelling  
290 reason for using the wrong distance. Analyses presented in the paper do not in fact  
291 support the use of AOD methods; rather, misunderstanding of the methods has resulted  
292 in their recommendation to use it.

293 Brugiere and Fleury (2000) did not attempt standard line transect analysis because  
294 they had only 23 detections, yet they considered this sample size to be adequate for ten  
295 other methods of analysis. Their known population comprised just three groups of a  
296 single species (black colobus *Colobus satanas*) in Gabon. Their design comprised just  
297 two transects, subjectively positioned, and they did not quantify precision of estimates.  
298 They used strip counts, with strip half-width pre-set at three values: 60, 80 and 100m;  
299 strip counts, with half-width estimated from the data, using maximum, mean or  
300 ‘maximum reliable’ perpendicular distance; the modified Kelker method, using  
301 maximum, mean or ‘maximum reliable’ AOD; and estimation of the effective strip half-

302 width from a histogram, coupled with adding half the group spread to this distance  
303 (Whitesides *et al.*, 1988). Uncertainty over true density complicated assessment of the  
304 methods, and they drew no firm conclusions on which method was best.

305 Fashing and Cords (2000) analysed data on two species (black-and-white colobus  
306 *Colobus guereza* and blue monkey *Cercopithecus mitis*) in Kenya. They estimated true  
307 densities based on home range data primarily on five groups and three groups  
308 respectively, although data from additional groups were also used. The ‘design’ was of a  
309 single non-random transect, placed along trails. They estimated precision from variation  
310 in repeat runs along the same transect. They estimated transect width using a) the  
311 maximum reliable AOD; b) the maximum reliable perpendicular distance; and c) the  
312 maximum reliable perpendicular distance with the addition of half the group spread, as  
313 recommended by Whitesides *et al.* (1988). They also used the shape-restricted estimator  
314 of Johnson and Routledge (1985) (a type of perpendicular distance detection function  
315 estimator that is seldom used). For both species, the method based on perpendicular  
316 distances, together with the half-group spread correction, gave estimates closest to the  
317 true density. The shape-restricted estimator performed particularly poorly.

318 Hassel-Finnegan *et al.* (2008) used just a single transect to estimate densities of  
319 two species (white-handed gibbons and Phayre’s leaf monkeys *Trachypithecus phayrei*  
320 *crepusculus*) in Thailand. They assessed true density largely on the basis of a single  
321 group for each species, and did not quantify precision of estimates. They used both the  
322 Kelker strip and the modified Kelker method, with truncation distance estimated as the  
323 point at which frequencies in the respective histograms of perpendicular distances and of  
324 AODs started to fall. In addition, they used Distance (Thomas *et al.*, in press) to perform  
325 a standard line transect analysis of perpendicular distances. All detection distances,  
326 whether perpendicular distances or AODs, were measured to the first animal detected of  
327 the group. For both species, Distance and the Kelker strip gave rise to overestimates of

328 the true density, while the modified Kelker method gave estimates very slightly under the  
329 true density. However, given the lack of replication (a single line, and a single group of  
330 each species), it seems that little can be inferred from these results. Hassel-Finnegan *et*  
331 *al.* (2008) quote the papers of Chapman *et al.* (1988) and Fashing and Cords (2000) to  
332 support their contention that analyses based on AODs closely match true densities, while  
333 those based on perpendicular distances overestimate. However, the results of neither  
334 paper support this conclusion.

335 All of the above comparisons are based on studies where true density is  
336 established by studying a small number of habituated groups, and estimating the size of  
337 their home range. There are several reasons why there might be bias in these 'true'  
338 densities. For example home ranges of groups may partially overlap, and because the  
339 transects in these studies are positioned subjectively, they may sample parts of the home  
340 range that are favoured or avoided by the habituated group, leading to a mismatch in the  
341 densities being estimated by the two approaches. This is exacerbated when the sampled  
342 strip(s) extend beyond the home range(s) of the habituated group(s), into other home  
343 ranges. Further, lone males are not included in densities obtained from home range  
344 studies, so that density might be expected to be lower as assessed by this method than  
345 that obtained by appropriate application of line transect sampling methods. In the case of  
346 a population of grey-cheeked mangabeys *Lophocebus albigena* in Uganda (Olupot and  
347 Waser, 2005), Olupot (pers. comm.) estimates that around 30% of males are solitary,  
348 corresponding to around 8% of the total population.

349 Mitani *et al.* (2000) compared censuses of seven species (black-and-white  
350 colobus, Pennant's red colobus *Procolobus pennantii*, baboons *Papio anubis*, blue  
351 monkeys, grey-cheeked mangabeys, red-tailed monkeys *Cercopithecus ascanius* and  
352 chimpanzees *Pan troglodytes*) made along almost the same census route between years at  
353 Ngogo in Kibale Forest. The three authors measured AOD separately for their respective

354 census periods (1975-76 and 1996 Struhsaker; 1997-98 Lwanga; and 1996 Mitani).  
355 They also used a single transect, which formed the shape of a square route. The authors  
356 found great variation in the estimation of AOD between the three of them, showing that  
357 each observer would estimate a very different maximum reliable sighting distance and  
358 that the shape of the sighting distributions differed significantly. They therefore could  
359 not use the modified Kelker method to compare densities between years and resorted to  
360 comparing encounter rates of primate groups per kilometre walked. Variation between  
361 observers with the modified Kelker method eliminates any possibility of comparison  
362 unlike standard perpendicular distance methods where a probability of detection can be  
363 computed for each observer to allow comparisons to be made (Marques *et al.*, 2007).

364 Marshall *et al.* (2008) review four methods: strip transects, the modified Kelker  
365 method, and two methods based on perpendicular distances – distance from the line of  
366 the group centre, and distance from the line of the centre of measurable individuals.  
367 They note that methods based on truncating a substantial proportion of data need larger  
368 sample sizes for comparable precision than methods that do not. They also note that the  
369 assumptions of the modified Kelker method are ‘unknown’. However, they still advocate  
370 its use for when expertise is unavailable to apply other methods, or when the data  
371 (location of group centres, or reliable estimates of mean group spread) or assumptions  
372 (certain detection on the line, accurate measurement to individuals) required by other  
373 methods are unachievable. They justify this recommendation on the grounds that the  
374 method consistently performs well in field trials, a claim that does not stand up to close  
375 scrutiny, as noted above. The recommendation presupposes that the *ad hoc* method will  
376 produce useful estimates when the other methods do not. The observer effects found by  
377 Mitani *et al.* (2000) for example suggest that this is unlikely.

378

## 379 **Simulation Study**

### 380 Simulating Populations and Samples

381 To assess how different methods perform, we simulated data from populations of known  
382 density. This is intentionally an idealized study, with a large sample of lines  
383 systematically spaced with a random start, with certain detection of animals on the line,  
384 no responsive movement, and no measurement error in distances. If methods perform  
385 poorly here, they can certainly be expected to in real studies. For simplicity, we assumed  
386 a rectangular survey region, 20km long and 5km wide. We placed 25 transects in the  
387 region, each 5km long, spaced 800m apart.

388 True number of groups in the survey region was 500, randomly spread through  
389 the region with a uniform density. Mean group size was 3, 10 or 30 animals, so that total  
390 population size was 1500, 5000 or 15000, corresponding to 15, 50 or 150 animals per  
391 square kilometre. We assigned the animals to the 500 groups by first assigning a single  
392 animal to each group. We then generated a random number for each remaining animal  
393 from a continuous uniform distribution on  $(0, 500^p)$ , with  $p = 0.75$ . We raised this  
394 number to the power  $1/p$ , and rounded up to the next integer; the resulting value defined  
395 the group to which the animal was assigned. This ensures greater variation in group size  
396 than would occur if all groups had the same expected size (corresponding to  $p = 1$ ), but  
397 the expectation of mean group size was 3, 10 or 30, as required. We assigned the  
398 position of each animal in a group at random within a circle of radius  $\rho$ , centred at the  
399 assigned group location, with  $\rho = 10, 25$  and 50m. All group centres fell within the  
400 survey region, but individual animals could be assigned a location outside the survey  
401 region. To avoid the complication of partial sampling of groups straddling the boundary,  
402 we extended sampling into a bufferzone, to allow the whole group to be sampled. We did  
403 not count effort (i.e. length of transect) in the bufferzone; this does not create bias



404 because the additional sightings compensate for the ‘missing’ sightings that would have  
405 occurred had groups been simulated whose centres were outside the study region, but  
406 which straddled the boundary.

407 Hayes and Buckland (1983) developed a hazard-rate model of the detection  
408 process. Their model is useful here to simulate the detection process as the observer  
409 approaches a group of animals. In this study, we initially simulated whether or not an  
410 animal was detected independently of other animals in a group. We assumed a hazard  
411 function of the form  $k(r) = ar^{-b}$ , with  $b = 3$  and  $b = 5$ , where  $r$  is distance between the  
412 animal and the observer. If the observer has not yet detected an animal at distance  $r$ , then  
413  $k(r)dx$  is the probability that the animal is detected as the observer advances a small  
414 distance  $dx$  along the line. Given the above form for  $k(r)$ , we can derive the detection  
415 function  $g(y)$ , which is the probability that an animal at distance  $y$  from the line is  
416 detected:  $g(y) = 1 - \exp\{-(y/c)^{-(b-1)}\}$ . We chose  $(c = 20, b = 3)$ , for which  $a = 400$ ,  
417 and  $(c = 30, b = 5)$ , for which  $a = 1215000$ . These two detection functions are shown  
418 (Fig. 2). To mimic the enhanced probability of detecting animals in a group once the first  
419 animal of the group has been detected, we identified all groups for which at least one  
420 animal was detected, and simulated a second ‘pass’ to search for undetected animals in  
421 the group, again using a hazard-rate detection function, but with the scale parameter  $c$   
422 increased by 50% ( $c = 30$  for scenarios with  $b = 3$ , and  $c = 45$  when  $b = 5$ ).

423 For a detected animal, we recorded both the AOD at the time of first detection and  
424 the perpendicular distance from the line. We did not record animals further than 150m  
425 from the line. Sample sizes were typically in the range 60-120.

426

## 427 Estimating Densities

428 For each combination of mean group size, group spread, true density and detection  
429 function, we simulated 100 populations, and surveyed each once. We applied the  
430 following analysis methods.

431

432 1. The modified Kelker method, based on mean AOD, where AOD for each detected  
433 group is the distance of the first detected animal from the group. We took the mean AOD  
434 as an estimate of the strip half-width, and the mean of recorded sizes of detected groups  
435 as an estimate of mean group size in the population.

436 2. The modified Kelker method, based on maximum AOD, where AOD for each  
437 detected group is the distance of the first detected animal from the group. We took the  
438 maximum AOD as an estimate of the strip half-width, and the mean of recorded sizes of  
439 detected groups as an estimate of mean group size in the population.

440 3. The modified Kelker method, based on maximum reliable AOD, where AOD for each  
441 detected group is the distance of the first detected animal from the group. We grouped  
442 AODs into 10m bins, and estimated the half-width of the strip by starting at the bin  
443 closest to the line (0-10m), and identifying the first bin for which the count was at most  
444 one half of the mean count for preceding bins. If for example the mean count in the first  
445 four bins was 10.5, and the count for bin 5 (40-50m) was 5, then the strip half-width was  
446 taken to be 40m, and detections at a greater distance were excluded from the analysis.  
447 We estimated mean group size in the population by the mean of recorded sizes of  
448 detected groups.

449

## 450 Results

451 All three modified Kelker methods have strong negative bias for all scenarios (Table 1).  
452 The bias is consistent across different group sizes and spreads, but differs markedly by

453 detection function. This finding is consistent with the finding by Mitani *et al.* (2000),  
454 that density estimates were not comparable across observers. The bias is especially large  
455 for method 1, the maximum AOD method (-90.7% and -75.7% for the two detection  
456 functions). For method 2, bias was -42.3% for the first detection function and -25.1% for  
457 the second. The corresponding values for method 3 were -43.9% and -28.2%.

458         These biases are not fully explained by bias in recorded group sizes (Table 2).  
459 Interestingly, although bias in recorded group size increases both with mean group size  
460 and with group spread, for methods 2 and 3, bias in density estimates within a method  
461 and detection function is largely independent of mean group size and group spread.  
462 However, as the bias is not consistent across different detection functions, it suggests that  
463 neither method gives a reliable estimate of relative density.

464         The bias is also not attributable to recording distances to the first detected animal,  
465 rather than to the group centre. Using measurements to group centres, AODs would  
466 increase, resulting in larger estimated strip widths, and reduced densities, so that bias  
467 would be even larger.

468         Because the methods have no coherent mathematical framework, it is not possible  
469 to identify the causes of bias, as there are no coherent assumptions that we can assess.

470

## 471 **Discussion**

472 In our simulation study, we found serious biases with estimators based upon AODs.  
473 Hassel-Finnegan *et al.* (2008) criticize conventional line transect sampling as  
474 implemented in Distance because a large number of detections is needed for reliable  
475 analysis. They fail to note that this is even more true of the Kelker strip, for which many  
476 of the observations are discarded (Marshall *et al.*, 2008). With inadequate sample sizes,  
477 choice of truncation distance is more subjective, uncertain and influential.

478 For methods based on selecting a single animal, and using the distance to it as the  
479 distance to the group centre, there is some ambiguity in the literature about whether the  
480 selected animal is the first animal detected or the closest animal. In general, the two are  
481 not the same individual. In our simulations, we assumed that it is the first animal  
482 detected. Struhsaker (1981) recorded 40% of detected groups as being on the line, which  
483 suggests that he used the distance of the closest animal to the line. Alternatively, if his  
484 transect was along trails, it may be that animals directly above the line were the first to be  
485 detected, because they were more visible.

486 We conclude that AOD methods as used by primatologists are conceptually  
487 flawed; the resulting estimates should not be treated as estimates of absolute density.  
488 Whether they are acceptable estimates of relative density depends on many factors.  
489 Estimates are unlikely to be comparable across different observers (Mitani *et al.*, 2000) or  
490 habitats for example. Estimating primate abundance is often difficult compared with  
491 many other taxa, as the animals often reside in hard-to-access, low-visibility areas and are  
492 often clustered, cryptic and highly mobile. Nevertheless, more reliable estimates of  
493 abundance are potentially possible by combining good survey design with better field and  
494 analytic methods (Buckland *et al.*, in review).

495

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498

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555

## Figure legends

Fig. 1. Shown here are two datasets, both generated from a detection function with certain detection out to 40m, and rapidly declining detection probability at larger distances. When by chance there are more detections close to the line, visual inspection of the data leads to selection of a smaller cutpoint for the Kelker method; 20m in this example. When there are more detections close to 40m, the cutpoint is likely to be set at 40m. If we fix the cutpoint in advance, at either 20m for both analyses or 40m, we expect unbiased estimates of density, but if we use 20m for the first analysis and 40m for the second analysis, we overestimate density on average. Dashed lines: mean count with truncation at 40m. Dotted lines: mean count with truncation at 20m.

Fig. 2. The detection functions used in the simulation study. Note that these detection functions apply to each individual animal; the probability that at least one animal of a group will be detected will be larger than shown here – substantially so for large groups. The solid line is  $g(y) = 1 - \exp\{-(y/20)^{-2}\}$  and the dashed line  $g(y) = 1 - \exp\{-(y/30)^{-4}\}$ .

Fig. 3. Histogram of AODs simulated from the hazard-rate model of the detection process,  $g(y) = 1 - \exp\{-(y/20)^{-2}\}$ .



Table 1. Mean (standard deviation in parentheses) of density estimates for the three methods of estimation.

Mean group size	3			10			30		
Half-group spread	10m	25m	50m	10m	25m	50m	10m	25m	50m
True density	15	15	15	50	50	50	150	150	150
$g(y) = 1 - \exp\{-(y/20)^{-2}\}$ :									
Maximum AOD	1.6 (0.7)	1.6 (0.7)	1.6 (0.6)	4.2 (0.6)	4.2 (0.6)	4.3 (0.7)	12.8 (1.3)	13.2 (1.3)	13.1 (1.1)
Mean AOD	8.6 (1.9)	8.5 (1.7)	8.3 (1.5)	29.6 (5.2)	29.2 (4.0)	29.0 (4.0)	85.5 (13.4)	88.2 (12.7)	87.4 (11.9)
Max reliable AOD	8.8 (2.1)	8.4 (1.7)	8.4 (1.6)	28.7 (5.3)	28.2 (4.3)	27.6 (4.2)	80.9 (14.0)	83.4 (12.9)	83.7 (11.2)
$g(y) = 1 - \exp\{-(y/30)^{-4}\}$ :									
Maximum AOD	4.5 (1.3)	4.5 (1.5)	4.7 (1.2)	12.2 (3.5)	11.7 (3.4)	11.8 (4.0)	28.4 (7.1)	28.7 (7.6)	26.4 (7.4)
Mean AOD	10.7 (2.1)	10.8 (1.7)	11.0 (1.9)	39.2 (6.4)	38.3 (5.3)	38.4 (6.0)	113.6 (18.1)	114.1 (17.7)	110.5 (15.1)
Max reliable AOD	10.5 (1.9)	10.3 (1.6)	10.5 (1.7)	37.4 (5.2)	36.4 (4.4)	36.9 (4.9)	108.7 (15.3)	109.2 (15.1)	106.1 (14.2)

Table 2. Estimates of mean group size: sample mean (standard error in parentheses) of recorded group sizes within  $w$  of the line.

Mean group size	3			10			30		
Half-group spread	10m	25m	50m	10m	25m	50m	10m	25m	50m
$g(y) = 1 - \exp\{-(y/20)^{-2}\}:$									
	2.65	2.56	2.33	6.46	6.27	5.68	14.28	14.31	13.29
	(0.20)	(0.19)	(0.14)	(0.39)	(0.36)	(0.33)	(0.89)	(0.97)	(0.82)
$g(y) = 1 - \exp\{-(y/30)^{-4}\}:$									
	2.89	2.79	2.52	8.14	7.67	6.66	19.77	19.08	16.60
	(0.22)	(0.20)	(0.16)	(0.44)	(0.45)	(0.42)	(1.55)	(1.19)	(0.92)

Fig. 1. Shown here are two datasets, both generated from a detection function with certain detection out to 40m, and rapidly declining detection probability at larger distances. When by chance there are more detections close to the line, visual inspection of the data leads to selection of a smaller cutpoint for the Kelker method; 20m in this example. When there are more detections close to 40m, the cutpoint is likely to be set at 40m. If we fix the cutpoint in advance, at either 20m for both analyses or 40m, we expect unbiased estimates of density, but if we use 20m for the first analysis and 40m for the second analysis, we overestimate density on average. Dashed lines: mean count with truncation at 40m. Dotted lines: mean count with truncation at 20m.

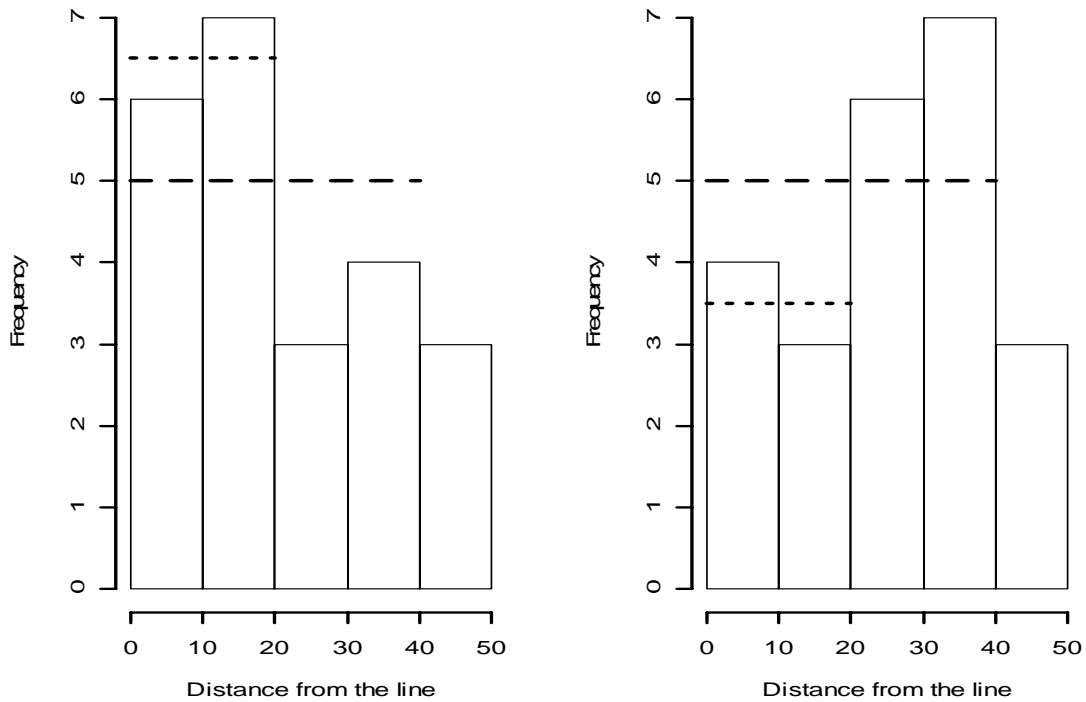


Fig. 2. The detection functions used in the simulation study. Note that these detection functions apply to each individual animal; the probability that at least one animal of a group will be detected will be larger than shown here – substantially so for large groups. The solid line is  $g(y) = 1 - \exp\{-(y/20)^{-2}\}$  and the dashed line  $g(y) = 1 - \exp\{-(y/30)^{-4}\}$ .

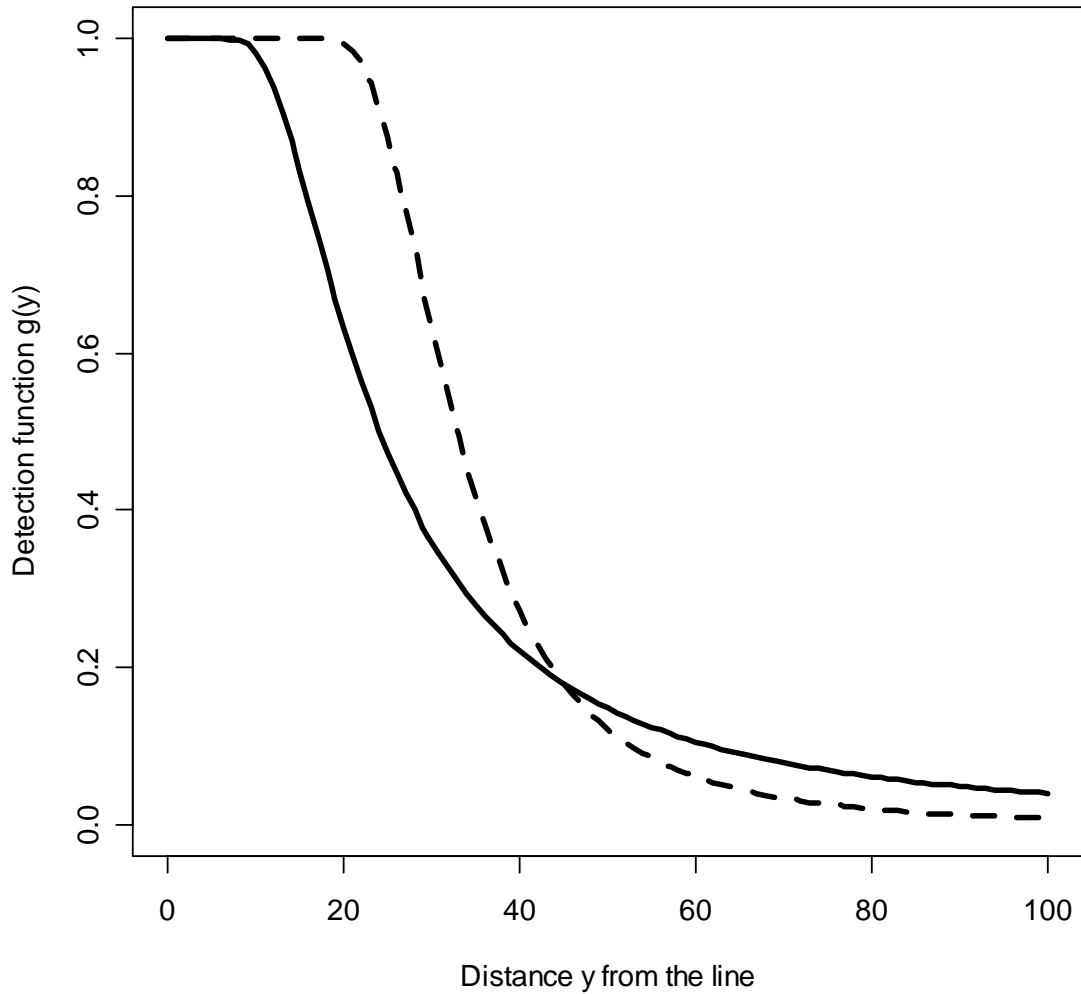


Fig. 3. Histogram of AODs simulated from the hazard-rate model of the detection process,  $g(y) = 1 - \exp\{-(y/20)^{-2}\}$ .

