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Measurement of Shear Strength and Interface Parameters by Multi-Stage Large-scale Direct/Interface Shear and Pull-out Tests

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3 1 **Measurement of Shear Strength and Interface Parameters by Multi-Stage Large-scale**
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6 **Direct/Interface Shear and Pull-out Tests**
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3 13 **Measurement of Shear Strength and Interface Parameters by Multi-Stage Large-scale**
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6 14 **Direct/Interface Shear and Pull-out Tests**
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8
9 15 **ABSTRACT**
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11 16 It is essential to measure the shear strength of soils and interface parameters between soils and
12
13 17 geosynthetics for the safe design and stability analysis of geosynthetic-reinforced soil
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15 18 structures. These parameters recommended for engineering projects are normally measured by
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17 19 laboratory single-stage direct/interface shear and pull-out tests. The conventional single-stage
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19 20 tests are carried out on at least three representative specimens under three different normal
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21 21 stresses. However, a large quantity of specimens is required for large-scale tests, with tedious
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23 22 sample preparation procedures, so that large-scale single-stage testing becomes very labour
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25 23 intensive, time consuming and expensive. Given that the multi-stage testing method is able to
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27 24 measure the shear strength parameters by testing only one representative specimen, this paper
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29 25 investigates the feasibility, reliability and applicability of the multi-stage testing method in
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31 26 large-scale direct/interface shear and pull-out tests. Two compacted soils and a geogrid were
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33 27 tested using both single-stage and multi-stage tests. It was found that the shear strengths
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35 28 obtained from the multi-stage tests were slightly lower than those obtained from the single-
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37 29 stage tests, and the inferred apparent cohesion and friction angle matched closely. In addition,
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39 30 the limitations of the multi-stage testing method were highlighted. The measured direct shear
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41 31 strength of the soils, the interface shear strength and pull-out shear strength between the soils
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43 32 and the geogrid are also compared and discussed in this paper.
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51 33 **KEYWORDS:** measurement, shear strength, interface parameters, laboratory testing, direct
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53 34 shear, pull-out
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List of Symbols

τ_s	direct shear strength of soil alone
τ_{ds}	interface shear strength between the geogrid and the soil
τ_p	pull-out shear strength between the geogrid and the soil
f_{ds}	direct shear interface coefficient
f_b	pull-out interface coefficient
α	scale effect correction factor
ϕ	internal friction angle
δ_0	friction angle between soil and geogrid ribs
δ	interface friction angle
α_{ds}	the proportion of the surface area of the geogrid ribs in contact with soil
σ_n	normal stress
c	apparent cohesion of soil
c_a	apparent adhesion between the geogrid and the soil
P_R	pull-out resistance per unit width
P_{RS}	frictional component of pull-out resistance
P_{RB}	bearing component of pull-out resistance
L_R	reinforcement length in the anchorage zone
S	spacing between geogrid bearing members
L_R/S	the number of geogrid bearing members
α_B	the fraction of total frontal area of geogrid available for bearing resistance
B	bearing member thickness
σ_b	bearing stress against the geogrid bearing members

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39 Introduction

40 Direct/interface shear and pull-out tests are commonly used laboratory techniques to measure
41 the shear strength parameters of soils and the interface parameters between soils and
42 geosynthetics. These parameters are necessary for the safe design and stability analysis of
43 geosynthetic-reinforced soil structures. The interface shear test is the most appropriate
44 experimental method for the analysis of soil-geosynthetic interaction when the sliding of the
45 soil mass on the reinforcement surface is likely to occur. However, the pull-out test is more
46 relevant to the study of soil-geosynthetic interaction when the failure surface shears through
47 the geosynthetic in the anchorage zone (Change et al. 2000; Palmeira, 2009; Lopes, 2012;
48 Bathurst and Ezzein 2015; Ferreira et al. 2015; Mosallanezhad et al. 2015; Xu et al. 2018a).
49 Nonetheless, both the two testing methods can be adopted in the laboratory to measure the
50 interface parameters between the soil and the geosynthetic, such as interface friction angles,
51 apparent adhesions and interface coefficients. However, the relationship between the interface
52 shear stress and pull-out shear stress mobilised along the soil-geosynthetic interface in these
53 two testing methods is still a very controversial topic and may produce significantly different
54 interface parameters for design. (Bergado et al.1994; Alfaro et al. 1995; Mallick et al. 1996;
55 Lopes and Silvano 2010; Hsieh et al. 2011).

56 Mallick et al. (1996) demonstrated that the surface roughness of the geosynthetic and the
57 interlocking between the soil and geosynthetic could influence the frictional resistance in
58 interface shear tests. Apart from the two factors, the geosynthetic extensibility should be taken
59 into account in pull-out tests. The maximum extension of the geosynthetic in an interface shear
60 test is much smaller than that in a pull-out test. This is because the geosynthetic is usually fixed
61 and clamped on the shear box for interface testing, while the geosynthetic is embedded in the
62 soil with its end being pulled for pull-out testing. Lopes and Silvano (2010) have shown that
63 the average pull-out interface coefficients are approximately 55% of the direct shear interface

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3 64 coefficients for a residual granite soil-geotextile interface in their study, indicating that the pull-
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5 65 out shear strengths obtained from the pull-out tests were much lower than the interface shear
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7 66 strengths obtained from the direct shear tests. By contrast, Hsieh et al. (2011) compared the
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9 67 direct shear and pull-out test results for different types of soil-geosynthetic interfaces and
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11 68 observed that the interface shear stress and pull-out shear stress were close for the crushed
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13 69 stone geotextile interface, while the pull-out shear stress was much higher than the interface
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15 70 shear stress for the crushed stone-geogrid interface. In addition, they also concluded that there
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17 71 existed a linear relationship between the interface shear stress and the applied normal stress for
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19 72 the interface shear tests between crushed stone and geogrid, but the pull-out shear stress
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21 73 appeared to have no consistent relationship with the applied normal stress for the pull-out tests.
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26 74 The earliest literature concerning multi-stage testing that could be found is a Master's thesis
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28 75 written by Gullic in 1970, at the University of Missouri-Rolla, USA. Gullic (1970) performed
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30 76 a series of multi-stage direct shear tests on a cohesionless soil using a small shear box with a
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32 77 diameter of 62.0 mm and a specimen height of 25.8 mm. Five different multi-stage direct shear
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34 78 testing procedures were studied and compared with conventional single-stage results. Later,
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36 79 Gan and Fredlund (1988) proposed a multi-stage direct shear testing method for unsaturated
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38 80 soils by applying multiple matric suctions on the same specimen. More recently, Hormdee et
39
40 81 al. (2012) performed the multi-stage direct shear testing of loess soil under drained conditions
41
42 82 using a conventional small direct shear apparatus. Petro et al. (2017) carried out the standard
43
44 83 and limited displacement multi-stage direct shear tests on rough rock joints, corresponding to
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46 84 the two multi-stage testing procedures. In general, a good agreement was observed based on
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48 85 their obtained plots of shear stress versus shear displacement. However, it would be very
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50 86 difficult to determine when to cease the shearing or when a peak stress has been achieved,
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52 87 especially for brittle rock samples.
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3 88 Similar to the multi-stage direct shear testing, there is also very limited multi-stage pull-out
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5 89 testing research work available. For instance, a Master's thesis written by Pradhan, at The
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7 90 University of Hong Kong, China, can be cited. Pradhan (2003) performed both single-stage
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9 91 and multi-stage pull-out tests on soil nails in completely decomposed granite fill and compared
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11 92 the peak pull-out resistances obtained. He concluded that the peak pull-out resistances obtained
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13 93 from the single-stage tests were higher than those from the multi-stage tests. This is because a
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15 94 continuing reduction in the length of the nail embedded in the soil in the later stages of the
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17 95 multi-stage tests caused a significant reduction in the soil-nail contact surface. Therefore, the
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19 96 peak pull-out resistance obtained was lower than that obtained from the single-stage test under
20
21 97 the same normal stress. Another multi-stage pull-out testing method proposed by Moraci and
22
23 98 Cardile (2009) was actually a cyclic tensile loading test, which differed from the multi-stage
24
25 99 testing method in Pradhan (2003) and that proposed in this paper. Overall, previous studies
26
27 100 have not applied the multi-stage testing method in the large-scale interface shear and pull-out
28
29 101 tests on the soil-geosynthetic interfaces. Therefore, the application of the multi-stage testing to
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31 102 both large-scale direct/interface shear and pull-out tests deserves further investigation.
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38 103 In summary, the main aims of this paper are: 1) to investigate the feasibility, reliability and
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40 104 applicability of the multi-stage testing in large-scale direct/interface shear and pull-out tests by
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42 105 testing the compacted soils and a geogrid, 2) to construct an empirical relationship between the
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44 106 single-stage and multi-stage test results based on the collected data; 3) to study the process of
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46 107 shear stress mobilisation during the shearing and pulling in the direct/interface shear and pull-
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48 108 out tests; and 4) to develop empirical relationships between the measured direct shear strength
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50 109 of the soil, the interface shear strength and pull-out shear strength between the soil and
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52 110 geosynthetic so that they could be predicted from one another.
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57 111 **Soil-geogrid Interaction Mechanism**

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3 112 The stability of geosynthetic-reinforced soil structures is highly dependent on the soil-
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5 113 geosynthetic interfaces. The interaction mechanism between the soil and geotextile (or other
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7 114 simple sheet types of geosynthetics) is only attributed to the frictional resistance mobilised
8
9 115 along the continuous geotextile surface. However, due to the presence of apertures in geogrid
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11 116 products, the interaction mechanism between the soil and geogrid is much more complex than
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13 117 that between the soil and geotextile.
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17 118 The direct shear resistance between the soil and the geogrid in direct shear tests has two
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19 119 components: (1) frictional resistance between the soil and the geogrid ribs along the single
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21 120 shear surface; and (2) frictional resistance between the soil and the soil in the geogrid apertures.
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23 121 This mechanism can be theoretically interpreted using the following equation (Jewell et al.
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25 122 1984):
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27

$$28 \tau_{ds} = f_{ds} \sigma_n \tan \phi = \sigma_n [\alpha_{ds} \tan \delta_0 + (1 - \alpha_{ds}) \tan \phi] \quad (1)$$

29
30 123 where ϕ is the internal friction angle of the soil, δ_0 is the friction angle between the soil and
31
32 124 geogrid ribs, f_{ds} is the direct shear interface coefficient, α_{ds} is the proportion of the surface area
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34 125 of the geogrid ribs in contact with the soil, i.e., the area of ribs (longitudinal and transverse)
35
36 126 relative to the total geogrid area, σ_n is the normal stress and τ_{ds} is the interface shear strength
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38 127 between the geogrid and the soil.
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45 129 From the experimental results of interface shear tests, the interface shear strength τ_{ds} can be
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47 130 interpreted by the Mohr-Coulomb criteria:
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$$50 \tau_{ds} = c_a + \sigma_n \tan \delta \quad (2)$$

51 131 where τ_{ds} is the interface shear strength obtained from the interface shear test, c_a is the apparent
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53 132 adhesion between the geogrid and the soil, and δ is the interface friction angle. Thus, the
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55 133 interface coefficient f_{ds} can then be calculated as:
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$$f_{ds} = \frac{c_a + \sigma_n \tan \delta}{c + \sigma_n \tan \phi} = \frac{\tau_{ds}}{\tau_s} \quad (3)$$

135
136 Additionally, the pull-out resistance also has two components: (1) frictional resistance between
137 the geogrid ribs and the soil above and below the geogrid (double shear surfaces); and (2)
138 passive bearing resistance provided by the transverse ribs in the apertures. This mechanism can
139 be interpreted by the following equation (Jewell 1990):

$$P_R = P_{RS} + P_{RB} = 2f_b L_R \sigma_n \tan \phi \quad (4)$$

141 where P_R is the pull-out resistance per unit width, P_{RS} is the frictional component of the pull-
142 out resistance, P_{RB} is the bearing component of the pull-out resistance, L_R is the reinforcement
143 length in the anchorage zone, f_b is the pull-out interface coefficient. The following equations
144 can be used to evaluate the frictional component P_{RS} and bearing component P_{RB} of the pull-
145 out resistance:

$$P_{RS} = 2\alpha_{ds} L_R \sigma_n \tan \delta \quad (5)$$

$$P_{RB} = \left(\frac{L_R}{S} \right) \alpha_B \sigma_b B \quad (6)$$

148 where S is the spacing between the geogrid bearing members, L_R/S is the number of geogrid
149 bearing members, α_B is the fraction of the total frontal area of the geogrid available for bearing
150 resistance, B is the bearing member thickness, and σ_b is the bearing stress against the geogrid
151 bearing members, which can be calculated using different bearing capacity theories (Peterson
152 and Anderson 1980; Jewell et al. 1985; Matsui et al. 1996).

153 From the experimental results, the pull-out interface coefficient f_b can be further expressed as
154 a ratio of the maximum shear stress mobilised at the soil-geosynthetic interface in the pull-out
155 test to the shear strength of soil alone obtained from the direct shear test:

$$f_b = \frac{P_R}{2L_R(c + \sigma_n \tan \phi)} = \frac{\tau_p}{\tau_s} \quad (7)$$

1
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3 157 where τ_p is the shear strength in the pull-out test, τ_s is the direct shear strength of soil alone.
4
5 158 Therefore, the shear stress mobilised at the soil-geogrid interface in the pull-out test can be
6
7 159 calculated using the following equation:

$$10 \quad 160 \quad \tau_p = \frac{P_R}{2L_R} \quad (8)$$

13
14 161 From the experimental results of the pull-out test, the pull-out shear strength τ_p can also be
15
16 162 interpreted by the interface shear strength parameters as in Eq. (9),

$$19 \quad 163 \quad \tau_p = c_a + \sigma_n \tan \delta \quad (9)$$

22
23 164 where τ_p is the pull-out shear strength obtained from the experimental pull-out results, c_a is the
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25 165 apparent adhesion between soil and geogrid, δ is the interface friction angle. Herein, the
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27 166 interface shear strength parameters c_a and δ are also obtained from a best-fit straight line (that
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29 167 is, the pull-out shear strength failure envelope).

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32 168 The relationship between the pull-out shear strength τ_p and interface shear strength τ_{ds}
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34 169 mobilised along the soil-geogrid interface can be defined as a parameter α , which is also called
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36 170 scale effect correction factor according to the Federal Highway Administration (FHWA) in
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38 171 USA (Christopher et al. 1990; Elias et al. 2001; Berg et al. 2009).

$$43 \quad 172 \quad \alpha = \frac{P_R}{2L_R(c_a + \sigma_n \tan \delta)} = \frac{\tau_p}{\tau_{ds}} \quad (10)$$

46
47 173 From Eqs. (3), (7) and (10), the following relationship between the interface coefficients
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49 174 obtained from the interface shear and pull-out tests can be found:

$$53 \quad 175 \quad \alpha = \frac{f_b}{f_{ds}} \quad (11)$$

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57 176 In summary, the soil-geogrid interaction mechanisms interpreted above in interface shear and
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59 177 pull-out tests are depicted in **FIG 1**, to clearly present each component.

178 **Multi-stage Testing Methodology**

179 The conventional single-stage test needs to be carried out on a minimum of three identical
180 specimens individually under three applied normal stresses, i.e., at least three specimens are
181 required and tested separately. In order to reduce the time and expense of the laboratory testing,
182 it is possible to use only one representative specimen to measure the shear strength, which is
183 defined as the multi-stage testing method (Gullic 1970). The multi-stage testing procedure
184 adopted in this study for direct/interface shear and pull-out tests comprises the following. The
185 specimen is compressed under the first stage normal stress. After the practical completion of
186 compression, the specimen is sheared/pulled out at a constant rate until failure or until a certain
187 predetermined displacement is achieved. When the failure occurs, the test is stopped, and the
188 normal stress is increased to the next predetermined level. The specimen is again allowed to
189 compress under the new normal stress. After that, the specimen is again sheared/pulled out at
190 the same constant rate until the second failure. This process is repeated for three or more stages
191 (see **FIG 2**). Comparing the procedures of the single-stage and multi-stage methods, it is found
192 that carrying out single-stage, large-scale tests are both time consuming and labour intensive,
193 resulting in much higher costs. In general, to measure the shear strength parameters for
194 engineering applications, the total cost of single-stage testing (three tests) will be
195 approximately three times greater than the cost of multi-stage testing (only one test), regardless
196 of more sampling costs that may be involved due to more specimens being required. Therefore,
197 the multi-stage testing method introduced above was attempted in the large-scale
198 direct/interface shear and pull-out tests in this study.

199 **Experimental Program**

200 *Test Materials*

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3 201 To pursue the objectives of this study, Australian roadbase materials were collected from Pine
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5 202 Mountain Quarry, Brisbane, and tested at the Geomechanics Laboratory of the Geotechnical
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7 203 Engineering Centre at The University of Queensland (UQ). This included Australian Type 2.1
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10 204 granite roadbase (designated as roadbase) and greenstone crusher dust (designated as dust).
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12 205 The particle size distributions of the roadbase materials are given in **FIG 3**. Also, Tensar SS40
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14 206 geogrid (with a tensile strength of 40 kN/m) was used in this study to carry out the interface
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16 207 shear and pull-out tests, as shown in **FIG 4**. This type of biaxial geogrid, manufactured from a
17
18 208 punched polypropylene sheet, is commonly used to reinforce the roadbase materials and to
19
20 209 stabilise weak subgrade soils in road pavement construction in Australia. In summary, the basic
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22 210 properties of the test materials are shown in **TABLE 1**.

26 211 *Testing Equipment*

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29 212 A large-scale direct shear apparatus manufactured by Wille Geotechnik of Germany (capable
30
31 213 of performing both direct/interface shear and pull-out tests) was utilised in this study, as shown
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33 214 in **FIG 5**. The shear box (pull-out box) has dimensions of 300 mm by 300 mm by 200 mm and
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35 215 the sides of the box are 20 mm thick. The machine is moderately stiff to accommodate a load
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37 216 capacity of 100 kN in both horizontal and vertical directions (up to 1000 kPa). The floating
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39 217 upper box is designed to create a gap between the upper and lower halves of the shear box by
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41 218 means of two compression springs. Four linear variable displacement transducers (LVDTs) are
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43 219 installed on the four corners of the top loading cap to measure settlement and tilting. In the
44
45 220 direct shear test, the upper half is fixed and the lower half is sheared, and the shear force
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47 221 mobilised during shearing is measured by a load cell. The geosynthetic can be clamped by
48
49 222 grooved clamping bars on the top of the lower shear box for interface shear testing. A large
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51 223 number of direct and interface shear tests have been carried out using this machine (Xu et al.
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53 224 2018b). Furthermore, the machine can be changed into pull-out testing mode after reassembling
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59 225 some parts, mainly by fixing the lower half of the shear box to the front counter-force beam,

226 and reconnecting the pulling rod together with the load cell to a roller clamp used for clamping
227 and pulling the geosynthetic (see **FIG 5b**). During the shearing or pulling processes, vertical
228 displacement, horizontal displacement and shear force or pull-out force are measured and
229 recorded at desired time intervals.

230 *Testing Program*

231 In order to evaluate the applicability, feasibility and reliability of multi-stage testing in the
232 large-scale direct/interface shear and pull-out tests, both single-stage and multi-stage tests were
233 carried out on the compacted roadbase materials and geogrid, under applied normal stresses of
234 15 kPa, 25 kPa, or 50 kPa, at the displacement rate of 1 mm/min. The normal stresses applied
235 to the specimens represent the typical stress levels found in road pavements. The initial
236 conditions controlled for the soils tested are summarised in **TABLE 2**. The internal shear stress
237 τ_s of soil, interface shear stress τ_{ds} and pull-out shear stress τ_p between the soil and geogrid were
238 obtained and compared in this study. Based on the shear strength results (τ_s , τ_{ds} , and τ_p) obtained,
239 interface coefficients (f_{ds} , f_b and α) were then calculated and analysed.

240 **Results and Discussion**

241 *Single-stage and Multi-stage Direct/Interface Shear Testing*

242 Large-scale, single-stage and multi-stage, direct/interface shear tests were carried out on
243 Roadbase, Dust, Roadbase-Geogrid and Dust-Geogrid. **FIG 6** compares the results of shear
244 stress versus shear displacement plots under applied normal stresses of 15 kPa, 25 kPa or
245 50 kPa. In order to avoid excessive tilting of the top cap during the shearing process, a shear
246 displacement of 30 mm (10% of total strain) was selected for the single-stage direct/interface
247 test, while a shear displacement of 10 mm was selected for each stage of the multi-stage test,
248 with the same total shear displacement of 30 mm after three stages. In addition, shear strength
249 failure envelopes and inferred shear strength parameters are shown in **FIG 7** (see also **TABLE**

1
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3 250 **3** and **TABLE 4**). The failure envelopes were plotted using the shear strength (i.e., the shear
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5 251 stress at failure) against the applied normal stress at failure. Failure was taken as the maximum
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7 252 (ultimate) shear stress attained within a shear strain of 10%. It should be noted that both the
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9
10 253 measured shear stress and applied normal stress were corrected for the area reduction and then
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12 254 plotted to determine the failure envelopes.

15 255 From **FIG 6** and **FIG 7**, it can clearly be seen that the shear stress curves and failure envelopes
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17 256 match quite closely for the single-stage and multi-stage test results. In particular, for the first
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19 257 stage under the applied normal stress of 15 kPa, the shear stress curves are almost identical (see
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21
22 258 **FIG 6**). However, the multi-stage testing method limits the shear displacement that can be
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24 259 applied to each stage. Especially under a high normal stress, more shear displacement is
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26 260 required to reach a peak. Moreover, the earlier stages may affect the shear strength achieved in
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28 261 the later stages, so that the accumulated error of the ultimate shear strength for the last stage is
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30 262 particularly obvious, as shown in **FIG 6**. Therefore, the failure envelopes of the multi-stage
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32 263 results tend to be slightly lower than those of the single-stage results (see **FIG 7**). This agrees
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34 264 with the small-scale, multi-stage direct shear test results available in the literature (Gullic 1970;
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36 265 Hormdee et al. 2012). In addition, the slope of the shear stress curve for the later stages obtained
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38 266 from a multi-stage test tends to be steeper than that obtained from a single-stage test under the
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40 267 same applied normal stress. This indicates that shear stress can be mobilised more rapidly in
41
42 268 the later stages. The soil specimen in a multi-stage test, with a pre-failure surface associated
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44 269 with particle reorientation, would behave in a more brittle manner than a fresh new specimen
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46 270 in a single-stage test. Furthermore, most of the specimens (**FIG 6 a** and **b**) of the large-scale
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48 271 direct shear tests show a strain-hardening behaviour for both single-stage and multi-stage tests;
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50 272 that is, the stress increases with strain without a peak being reached. However, some interface
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52 273 shear tests on the soils and geosynthetic show a slight strain-softening in the post-peak stage if
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55 274 a peak was achieved within 10% of the shear strain, as shown in **FIG 6 c** and **d**. A possible
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275 explanation for the different behaviour of the direct shear and interface shear tests might be
276 that a peak tends to be achieved in interface shear tests due to the soil particle reorientation
277 along the geogrid ribs and apertures. For all the multi-stage tests, because the maximum strain
278 applied to each stage was limited to 3.3% the ultimate shear strength was not obtained.
279 Comparison with the single stage tests without a geogrid, suggests that slight strain-hardening
280 behaviour would be expected, whereas with a geo-grid, slight strain-softening behaviour would
281 be expected. Despite this, the multi-stage tests gave similar shear strength parameters to the
282 single stage tests. As a large shear box can accommodate larger displacements than a small
283 shear box, multi-stage testing using a large shear box can provide more reliable results than
284 those obtained using a small shear box. Also, tedious sample preparation for a large-scale,
285 single-stage direct shear test is both very time consuming and labour intensive because a large
286 quantity of soil specimens is involved.

287 *Single-stage and Multi-stage Pull-out Testing*

288 A pull-out displacement of 60 mm was selected in the single-stage test, while a pull-out
289 displacement of 20 mm was selected for each stage in the multi-stage test, with the same total
290 pull-out displacement of 60 mm after three stages. **FIG 8** shows the pull-out resistance versus
291 pull-out displacement plots under applied normal stresses of 15 kPa, 25 kPa or 50 kPa for the
292 pull-out testing of the geogrid embedded in Roadbase and Dust. The pull-out shear strength
293 failure envelopes obtained by single-stage and multi-stage pull-out testing are compared in **FIG**
294 **9**, showing that the envelopes obtained from the multi-stage tests tend to be slightly lower than
295 those from the single-stage tests, except for one shear strength data point obtained from the
296 multi-stage pull-out testing of Roadbase-Geogrid under the applied normal stress of 50 kPa.
297 The pull-out shear stress τ_p mobilised along the soil-geogrid interface in the pull-out tests was
298 calculated by Eq. 8. As also shown in **FIG 8**, it is noteworthy that the single-stage pull-out test
299 results tend to show an elastic-plastic behaviour with a yield point, while the multi-stage pull-

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3 300 out test results basically show a nonlinear-elastic behaviour. Because the multi-stage pull-out
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5 301 tests were limited to a maximum strain of 3.3% for each stage, it is found that the friction
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7 302 resistance increases with pull-out displacement throughout the pulling process, without a peak
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10 303 being reached. Therefore, similar limitations of the multi-stage testing method in pull-out tests
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12 304 can be listed as: 1) multi-stage pull-out test would limit the pull-out displacement that can be
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14 305 applied to each stage, which may not be sufficient to achieve a peak. This is most noticeable
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16 306 for the final stage under the highest normal stress, which tends to require more pull-out
17
18 307 displacement, and 2) the earlier stages may affect the maximum (ultimate) pull-out resistance
19
20 308 achieved in the later stages. However, the maximum pull-out resistance obtained in this study
21
22 309 still matched quite closely despite these limitations, as shown in **FIG 8** and **FIG 9**. All the pull-
23
24 310 out results for Roadbase-Geogrid and Dust-Geogrid are further summarised in **TABLE 5** for
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26 311 convenience.

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31 312 It should be noted that the high strength geogrids (such as the Tensar SS series) with strong
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33 313 ribs and thick joints have excellent tensile performance, so the extension of the geogrid
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35 314 embedded in roadbase materials was found to be negligible under the road service load (within
36
37 315 50 kPa) in the pull-out tests. The maximum pull-out resistance achieved for the Tensar SS40
38
39 316 geogrid under applied normal stress of 50 kPa ranged from 24 kPa to 28 kPa in this study,
40
41 317 which was still within the ultimate tensile strength 40 kN/m of SS40 (see also **FIG 8**). It should
42
43 318 also be noted that higher applied normal stresses of 75 kPa and 100 kPa were also attempted in
44
45 319 our study; however, sudden rupture failure of the SS40 geogrid at the clamping area was found
46
47 320 to occur frequently, instead of the pull-out failure. This is because the pull-out resistance
48
49 321 achieved was close to its tensile strength 40 kN/m, and the clamper was not capable of gripping
50
51 322 the geogrid sufficiently tightly. **FIG 10** presents two photos of Tensar SS40 geogrid embedded
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53 323 in Roadbase and Dust following the pull-out testing under the applied normal stress of 50 kPa
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55 324 (after removal of the soil on the top of the geogrid). As shown in **FIG 10**, the free end of the
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3 325 geogrid moved together with the front clamping bar during the pulling process, and all the
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5 326 nodes of the geogrid had the same horizontal pull-out displacement. Overall, there was no
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7 327 obvious extension or distortion observed for the geogrid. This observation is different from
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9 328 some previously published pull-out studies on different geosynthetics (Alfaro et al. 1995;
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11 329 Alobaidi et al. 1997; Perkins and Cuelho 1999; Moraci and Gioffre; 2006; Moraci and Recalcati
12
13 330 2006; Hsieh et al. 2011; Ferreira et al. 2015). These different findings could be due to three
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15 331 reasons: 1) the poor mechanical properties of geosynthetics tested; 2) relatively higher normal
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17 332 stress applied in their research, which caused significantly non-uniform deformation of
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19 333 geosynthetics during the pulling processes; and 3) the occurrence of rupture failures of the
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21 334 geosynthetics rather than the expected pull-out failures. The deformation of geosynthetics in the
22
23 335 large-scale pull-out tests is deserved further study using some advanced measurement
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25 336 techniques, such as fiber bragg grating sensors or optical fiber sensors (Pei et al. 2013; Wang
26
27 337 et al. 2015).

338 *Comparisons of Shear Strength Parameters Obtained from Single-stage and Multi-stage*

339 *Tests*

340 Shear strength parameters (c , ϕ) and interface parameters (c_a , δ) were calculated based on the
341 failure envelopes obtained from the single-stage and multi-stage direct/interface shear and pull-
342 out tests. It was found that the apparent cohesions obtained from the multi-stage tests are
343 slightly lower than those from the single-stage tests (see **FIG 11a**). However, the friction angles
344 obtained from the multi-stage tests are not always lower, as shown in **FIG 11b**. In general, they
345 are still very close to the single-stage test results. The errors of the apparent cohesions (either
346 c or c_a) and friction angles (either ϕ or δ) ranged from -2.7 kPa to 0.3 kPa, and -1.8° to 2.4° for
347 all the multi-stage and single-stage tests in this study (see **FIG 11c** and **TABLE 6**). The errors
348 were calculated by the multi-stage test results minus the single-stage test results, as shown in

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2
3 349 Table 6. Therefore, the multi-stage testing method can produce relatively reliable shear strength
4
5 350 parameters for the large-scale direct/interface shear and pull-out tests.
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8 351 *Relationship Between Direct Shear Stress, Interface Shear Stress and Pull-out Shear Stress*
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10
11 352 The relationship between direct shear stress, interface shear stress and pull-out shear stress is
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13 353 still not quite clear due to the different shear mechanisms for a wide range of soils and
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15 354 geosynthetics. It was therefore decided to compare the shear stresses obtained from the
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17 355 direct/interface shear and pull-out tests to seek any potential relationship. **FIG 12** shows the
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19 356 shear stress curves obtained from direct/interface shear and pull-out tests using single-stage
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21 357 and multi-stage testing methods, under applied normal stresses of 15 kPa, 25 kPa or 50 kPa. It
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23 358 can be observed that the shear stress curves of the soil-geogrid interface are quite close to those
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25 359 of soils alone for both the single-stage and multi-stage direct/interface shear testing. However,
26
27 360 the shear stress curves obtained from the pull-out tests tend to flatten out with more horizontal
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29 361 displacement required to reach the failure, indicating that the mobilisation of shear stress along
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31 362 the soil-geogrid interface is much slower in the pull-out tests than in the interface shear tests.
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33 363 The horizontal displacement required for the pull-out tests was doubled (60 mm for the single-
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35 364 stage tests and 20 mm for each stage of the multi-stage tests) compared to the direct shear tests
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37 365 (30 mm for the single-stage tests and 10 mm for each stage of the multi-stage tests), to ensure
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39 366 that the pull-out resistance could be sufficiently developed. It can be clearly observed that the
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41 367 pull-out shear stress mobilised along the soil-geogrid interface is relatively lower than the
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43 368 corresponding interface shear stress within a horizontal displacement of 30 mm under each
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45 369 normal stress. This is most noticeable for the single-stage tests under the highest normal stress
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47 370 of 50 kPa. However, the maximum interface shear stress mobilised is still comparable when
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49 371 the pull-out displacement reached a horizontal displacement of 60 mm (see **FIG 12a-b**). Also,
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51 372 from the multi-stage test results (see **FIG 12c-d**), the same conclusion can readily be drawn. In
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53 373 addition, it is recommended that the required horizontal displacement be increased with
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374 increasing applied normal stress (higher confinement) in order to sufficiently develop the shear
375 stress (see also **FIG 12**).

376 **FIG 13** compares the failure envelopes of the soil-geogrid interface obtained from the interface
377 shear and pull-out tests. In general, the failure envelopes obtained from the pull-out tests are
378 slightly lower than those obtained from the interface shear tests. It should be noted that area
379 correction for both normal stress and shear stress is necessary since a significant reduction in
380 the contact area would cause an increase in both normal stress and shear stress in large-scale
381 direct/interface shear and pull-out tests. For example, when a normal stress of 50 kPa was
382 subjected to a specimen, the actual applied normal stress at failure was higher than 50 kPa, as
383 shown in **FIG 13**. Therefore, even though some shear strengths obtained from the pull-out tests
384 were found to be higher than those from the interface shear tests, the failure envelopes were,
385 however, generally slightly lower. This is because the horizontal displacement was doubled
386 (60 mm) for the pull-out tests, so that the actual normal stress at failure increased after applying
387 the area correction. Therefore, the obtained failure envelopes were flattened.

388 **FIG 14** compares the direct shear strength of soils τ_s , interface shear strength τ_{ds} and pull-out
389 shear strength τ_p of soil-geogrid interfaces, and their empirical relationships. In general, quite
390 good linear relationships were found in **FIG 14** for both the single-stage and multi-stage results.
391 The interface shear strengths τ_{ds} and pull-out shear strengths τ_p are quite close to the direct shear
392 strengths τ_s of the soils. In addition, interface parameters f_{ds} , f_b , and α calculated by Eqs. (3),
393 (7) and (10) are presented in **FIG 15** and **TABLE 7**. It can be found that the average values of
394 these three parameters (1.043, 0.984 and 0.946) were similar to the linear regression results of
395 all data (1.028, 0.995 and 0.969), which are all quite close to 1. Therefore, based on the
396 interface parameters obtained, these three shear strengths can be correlated with each other.

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3 397 Finally, the relationship between the single-stage and multi-stage test results was constructed
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5 398 through linear regression of all the experimental shear strength data obtained, as shown in **FIG**
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7 399 **16**. It can be found that a good linear relationship exists, although the shear strengths obtained
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9 400 from the multi-stage tests were slightly lower. **FIG 16** has shown the reliability of the multi-
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11 401 stage testing method applied to both large-scale direct/interface shear and pull-out testing of
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13 402 compacted soils and a geogrid.
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16 17 403 **Conclusion**

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20 404 In this paper, a multi-stage testing method was attempted for both large-scale direct/interface
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22 405 shear and pull-out tests. The obtained multi-stage test results were analysed and compared with
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24 406 the obtained conventional single-stage test results. In summary, the main conclusions of this
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26 407 paper are:
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30 408 (1) The multi-stage testing method was successfully applied to large-scale direct/interface
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32 409 shear and pull-out testing of compacted soils and a geogrid, resulting in slightly lower shear
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34 410 strengths and reasonably accurate shear strength and interface parameters for compacted soils
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36 411 and a geogrid.
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39 412 (2) The measured direct shear strengths of soils τ_s , interface shear strengths τ_{ds} , and pull-
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41 413 out shear strengths τ_p of compacted soil-geogrid interfaces are found to be very close in this
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43 414 study, resulting in the interface parameters f_{ds} , f_b , and α close to 1.
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46 415 (3) The mobilisation of the interface shear stress between the soil and geosynthetic in pull-
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48 416 out tests is much slower than that in the interface shear tests, so that more horizontal
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50 417 displacement is required for pull-out tests.
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53 418 (4) The main limitation of multi-stage tests is that it limits the shear/pull-out displacement
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55 419 that can be applied to each stage, which may not be sufficient. Therefore, a suitable
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3 420 displacement for each stage should be chosen with particular caution, considering the
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5 421 properties and the initial conditions of specimens.
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Caption List of Figures

FIG 1 Soil-geogrid interaction mechanisms for interface shear and pull-out testing.

FIG 2 Single-stage and multi-stage testing in: (a) direct/interface shear test and (b) pull-out test.

FIG 3 Particle-size distribution curves of tested soils.

FIG 4 Tensar SS40 geogrid.

FIG 5 Testing equipment: (a) direct/interface shear testing mode and (b) pull-out testing mode.

FIG 6 Single-stage and multi-stage direct/interface shear test results: (a) Roadbase, (b) Dust, (c) Roadbase-Geogrid, and (d) Dust-Geogrid.

FIG 7 Comparisons of failure envelopes for single-stage and multi-stage tests: (a) direct shear and (b) interface shear.

FIG 8 Single-stage and multi-stage pull-out test results: (a) Roadbase-Geogrid and (b) Dust-Geogrid.

FIG 9 Comparisons of failure envelopes for single-stage and multi-stage pull-out tests.

FIG 10 Two photos of Tensar SS40 geogrid embedded in soils after pull-out testing under applied normal stress of 50 kPa: (a) embedded in Roadbase and (b) embedded in Dust.

FIG 11 Comparisons of shear strength parameters obtained from single-stage and multi-stage tests: (a) cohesion, (b) friction angle, and (c) error between two testing methods.

FIG 12 Comparisons of shear stress curves obtained from direct/interface shear and pull-out tests: (a) single-stage test on Roadbase, (b) single-stage test on Dust, (c) multi-stage test on Roadbase, and (d) multi-stage test on Dust.

FIG 13 Comparisons of failure envelopes obtained from interface shear and pull-out tests: (a) single-stage and (b) multi-stage.

FIG 14 Comparisons of shear strengths obtained from direct/interface shear and pull-out tests: (a) τ_{ds} versus τ_s , (b) τ_p versus τ_s , and (c) τ_p versus τ_{ds} .

FIG 15 Calculated value of interface parameters.

FIG 16 Linear regression of shear strengths for single-stage and multi-stage tests.

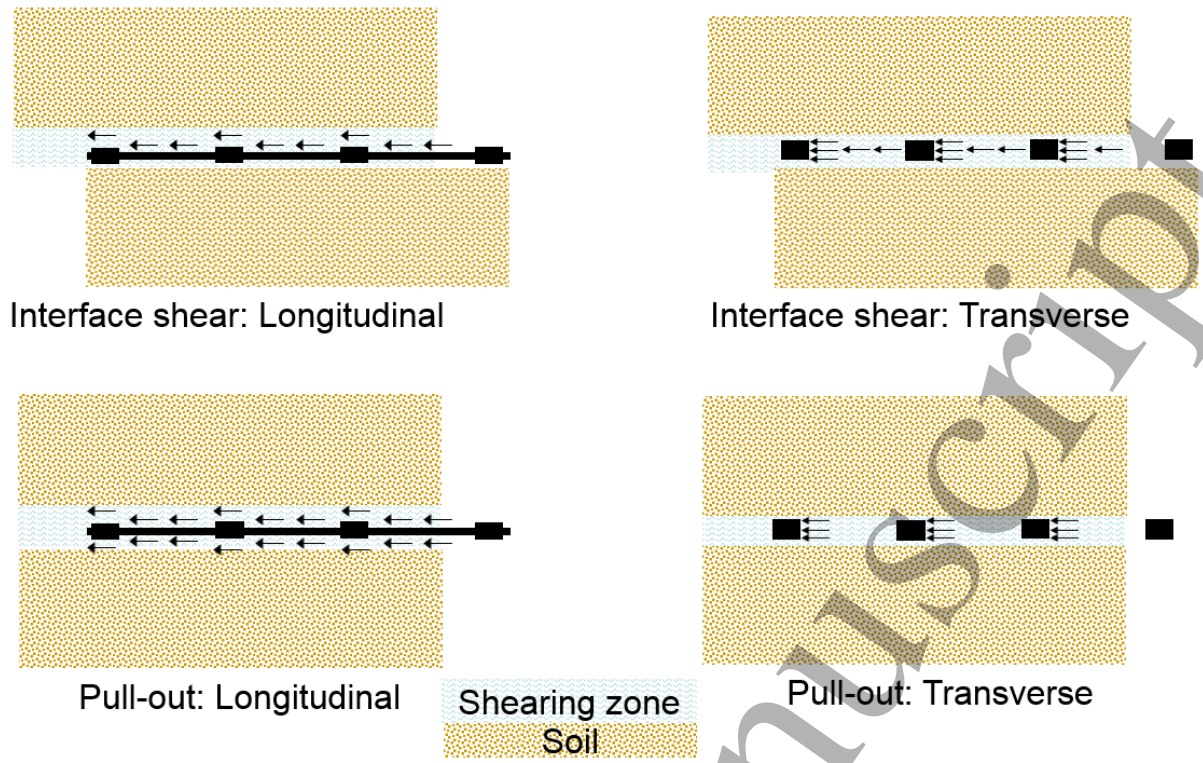


FIG 1 Soil-geogrid interaction mechanisms for interface shear and pull-out testing.

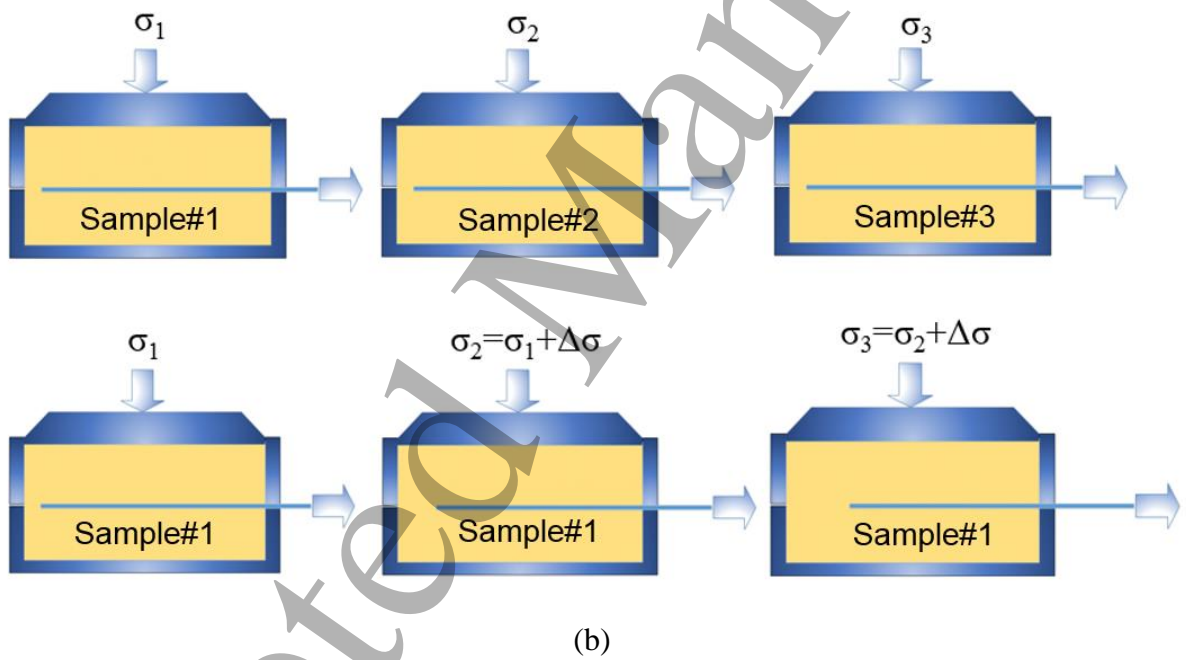
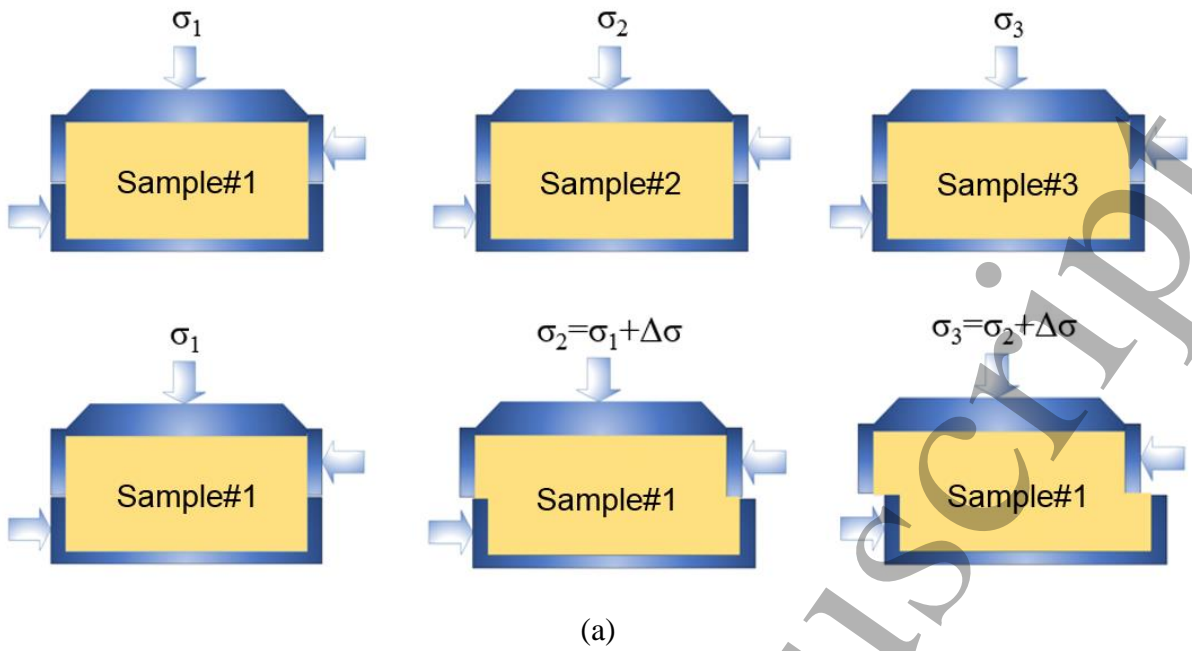


FIG 2 Single-stage and multi-stage testing in: (a) direct/interface shear test and (b) pull-out test.

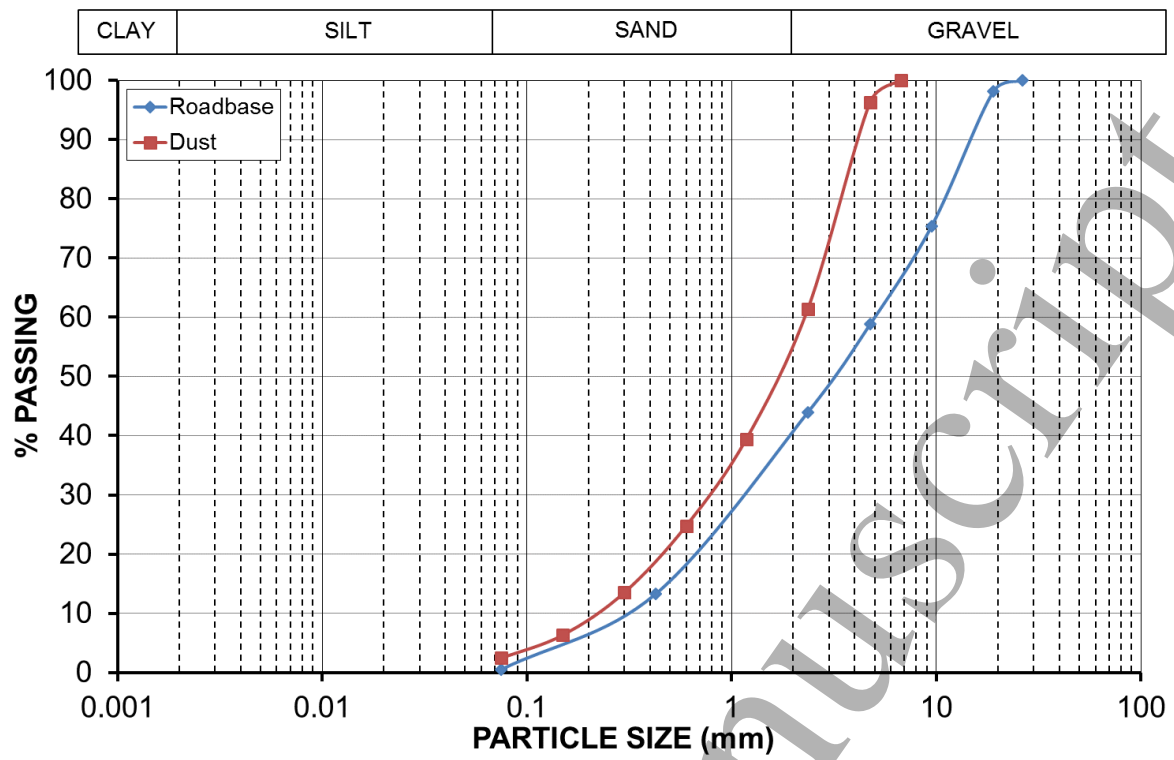


FIG 3 Particle-size distribution curves of tested soils.

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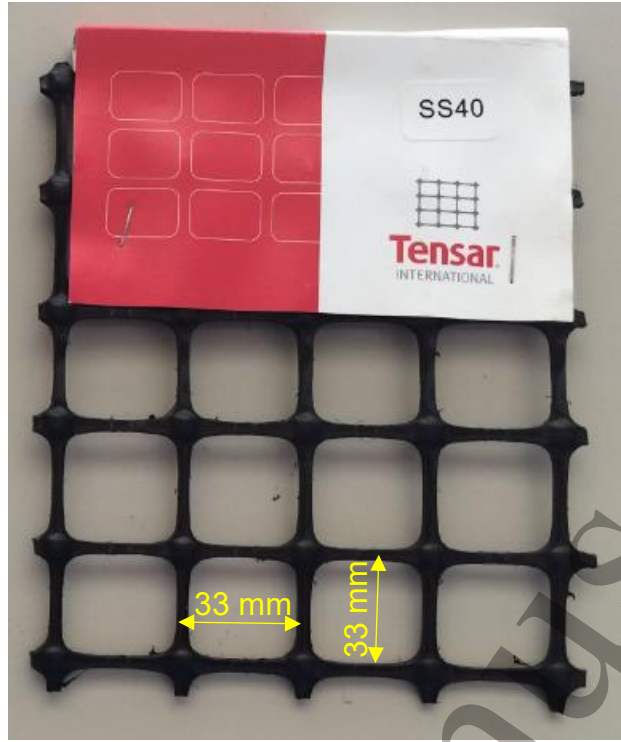


FIG 4 Tensar SS40 geogrid.

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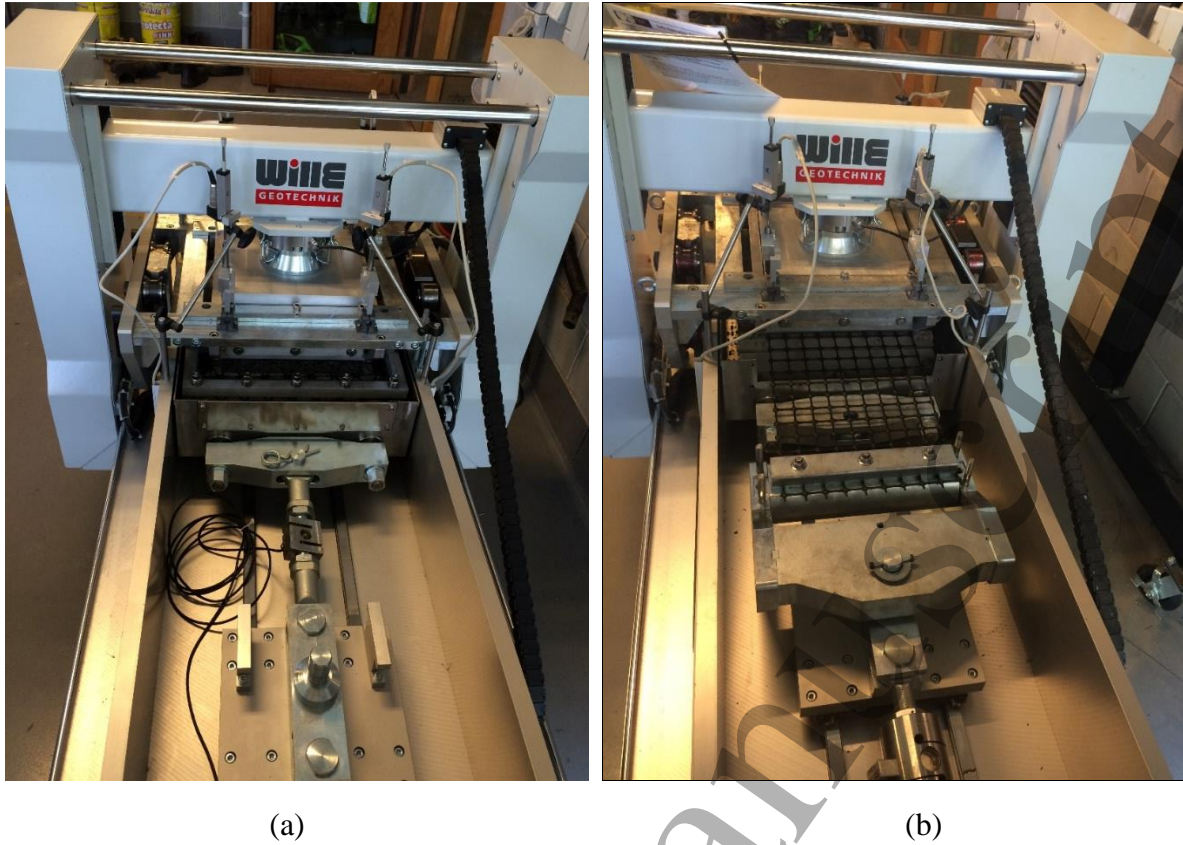
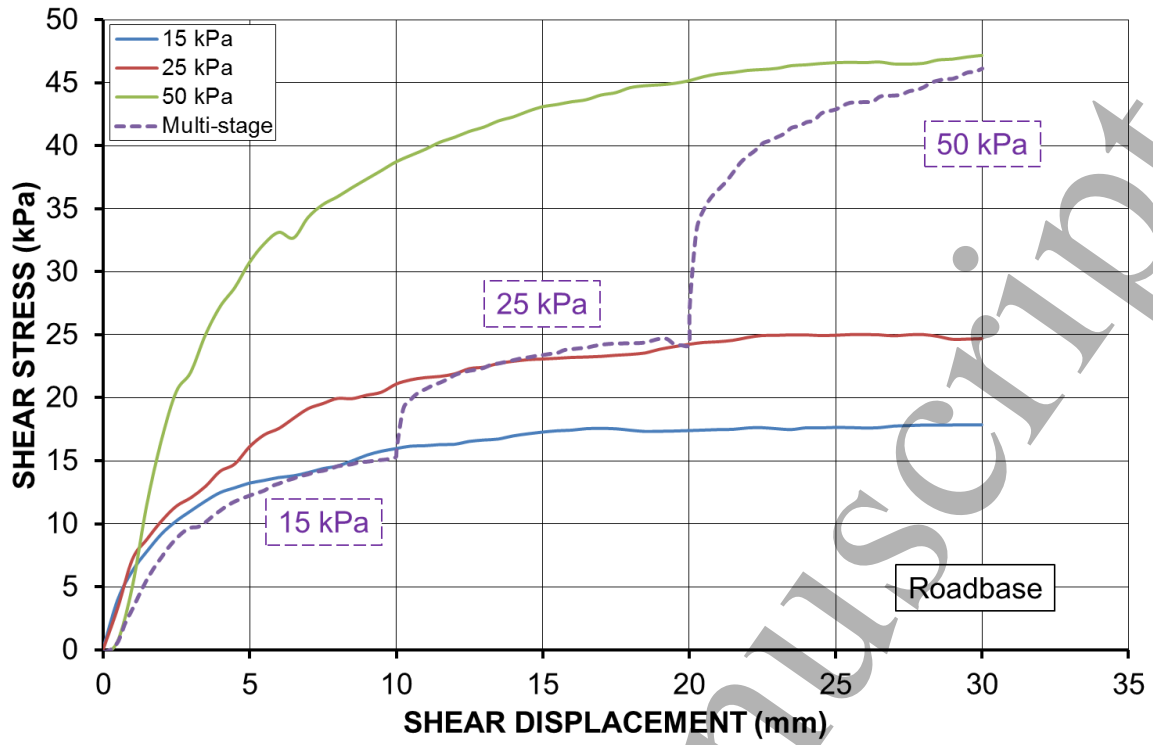
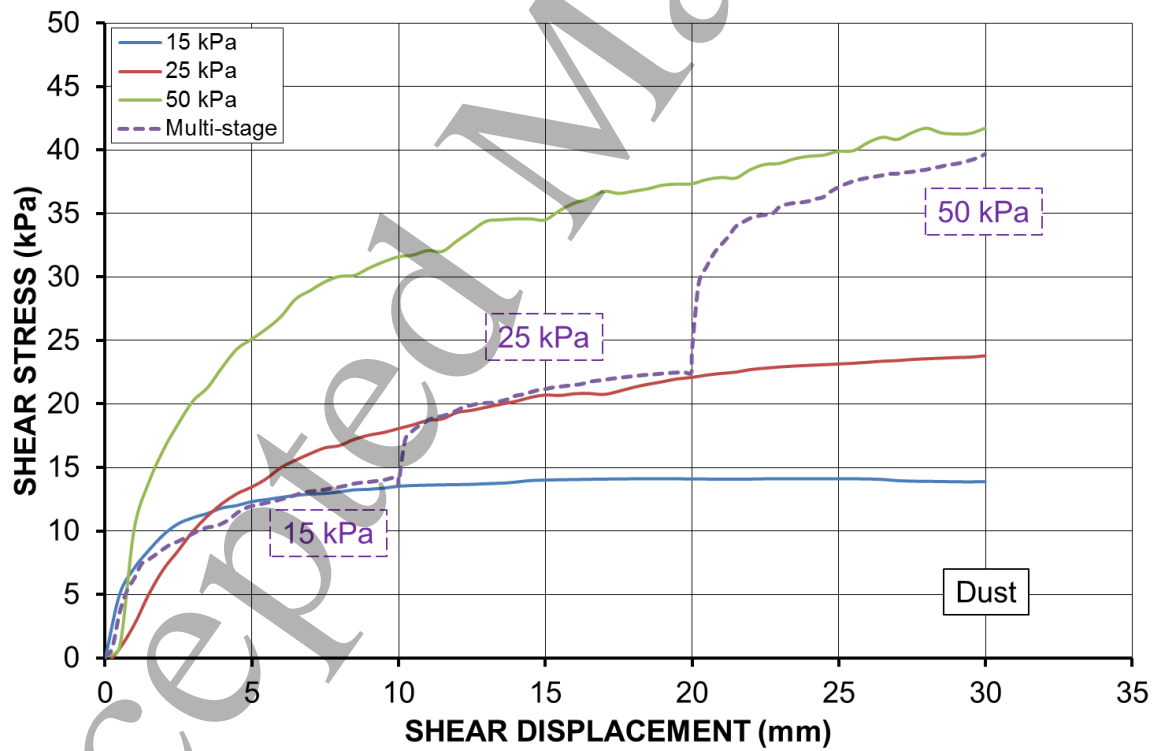


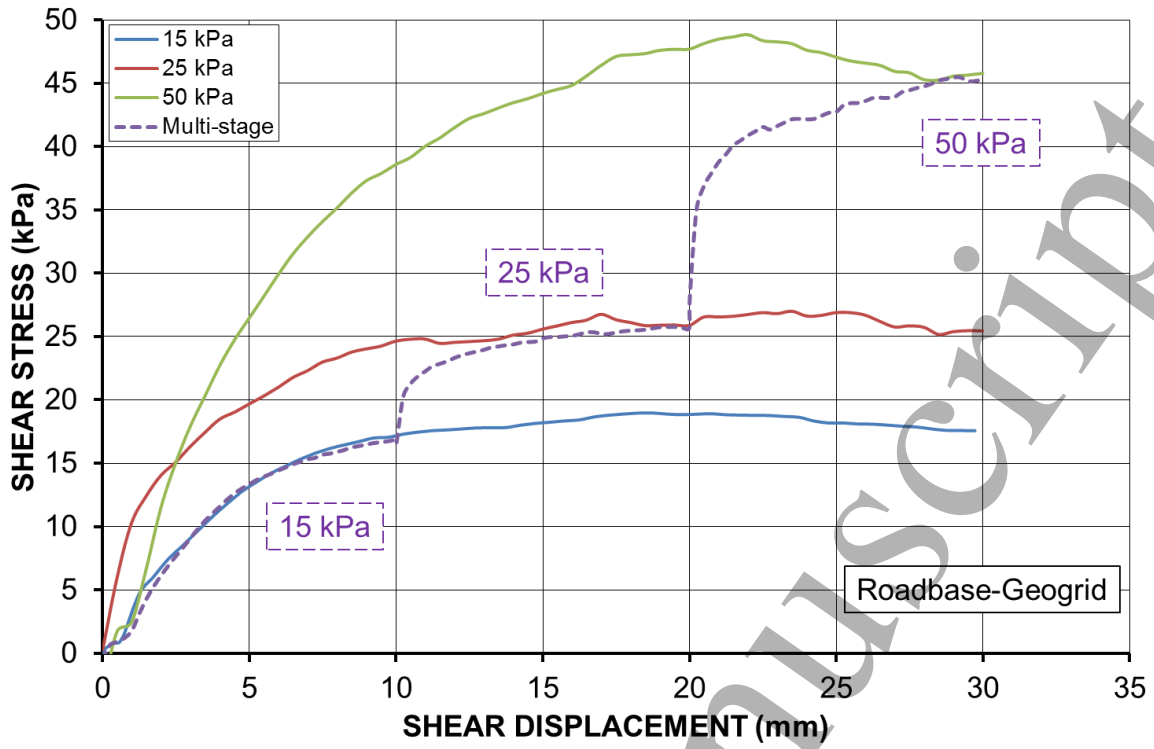
FIG 5 Testing equipment: (a) direct/interface shear testing mode and (b) pull-out testing mode.



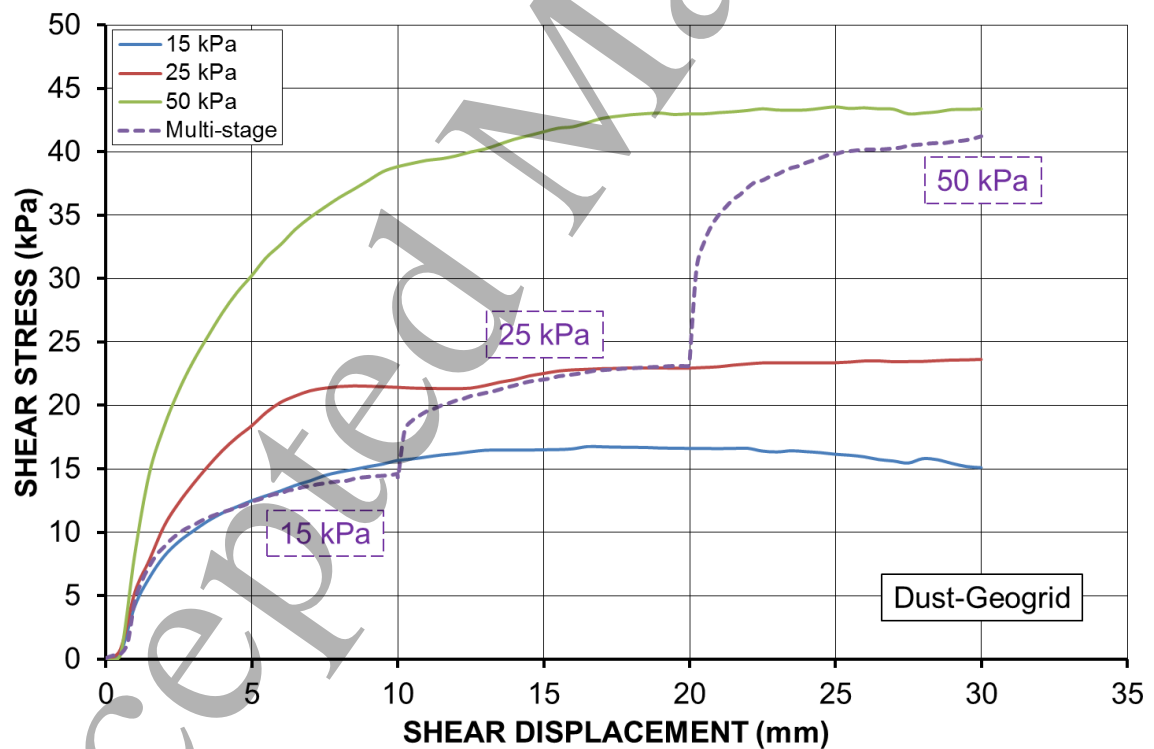
(a)



(b)



(c)



(d)

FIG 6 Single-stage and multi-stage direct/interface shear test results: (a) Roadbase, (b) Dust, (c) Roadbase-Geogrid, and (d) Dust-Geogrid.

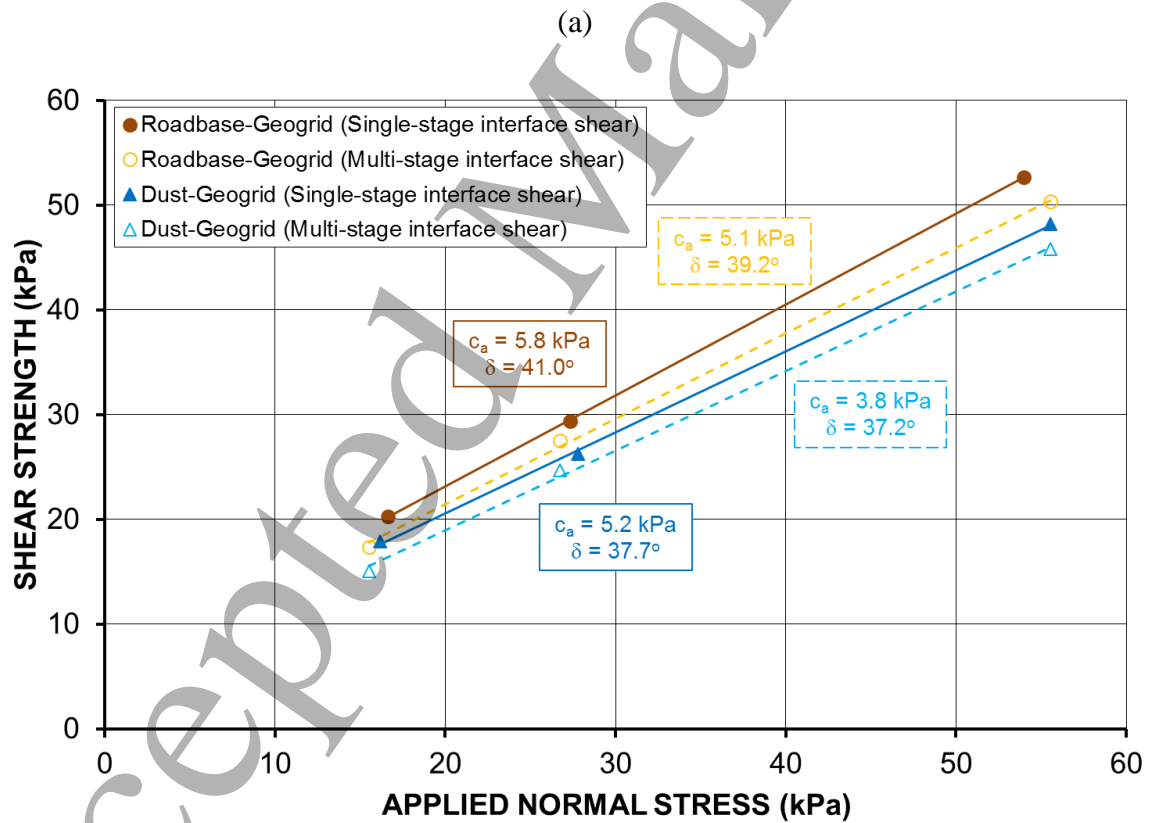
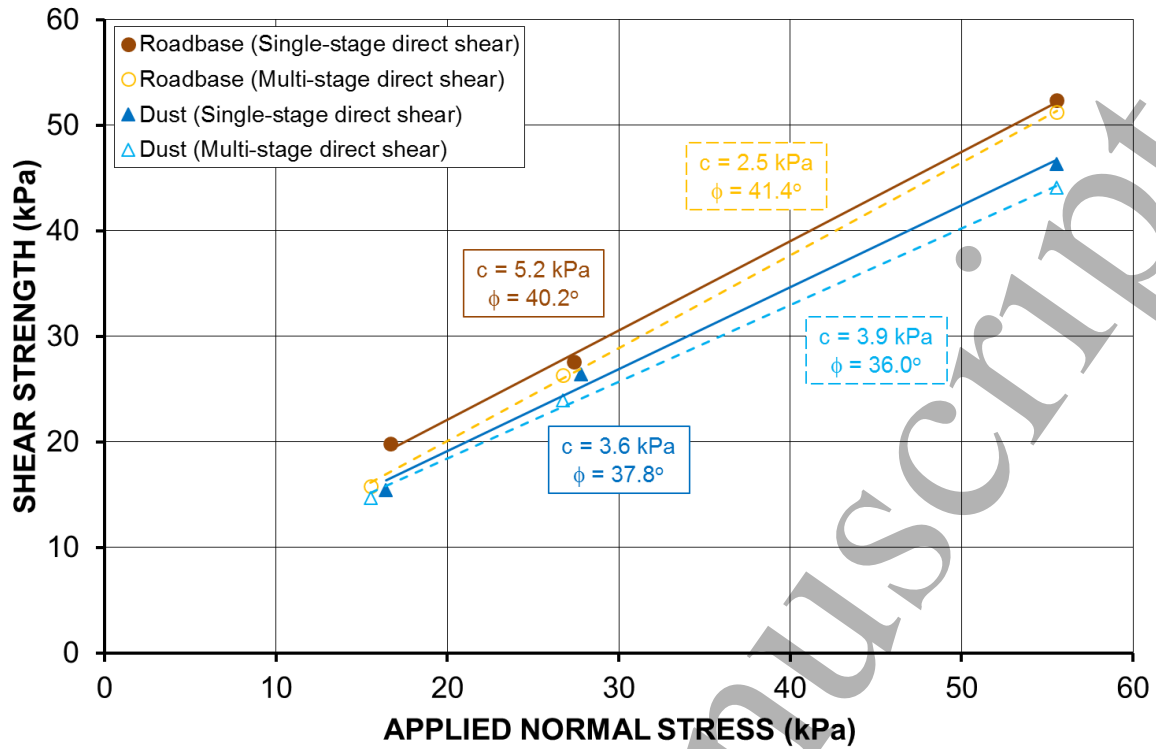
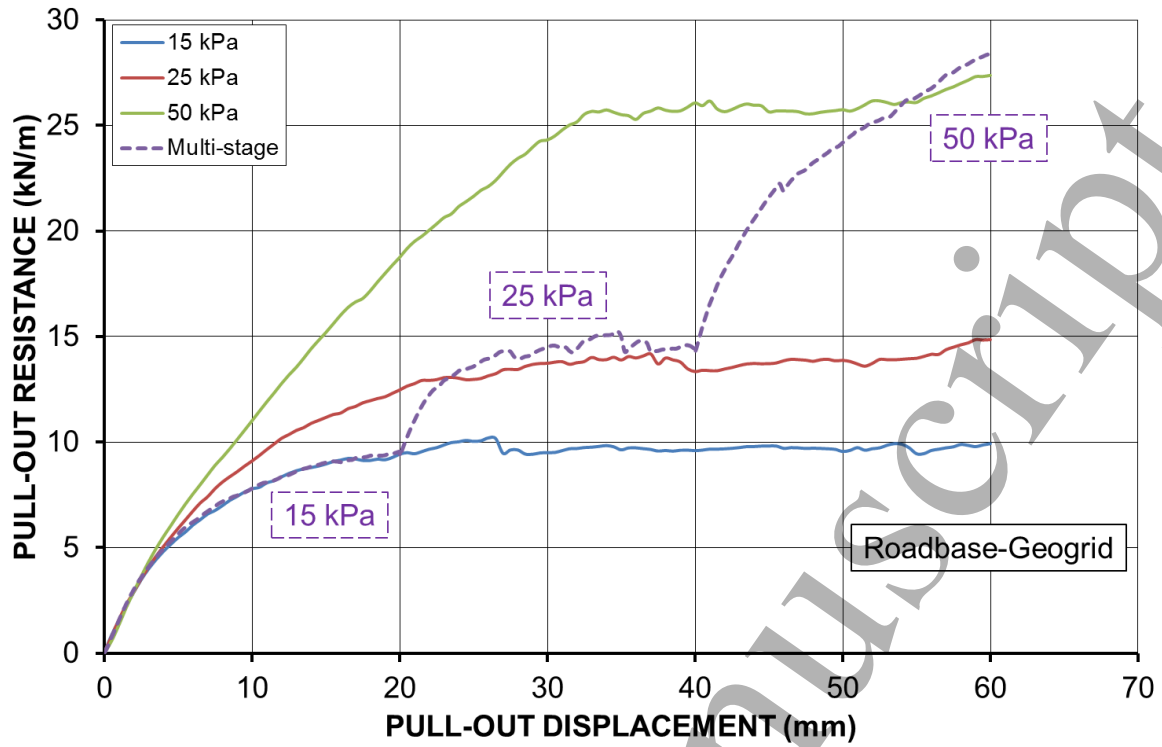
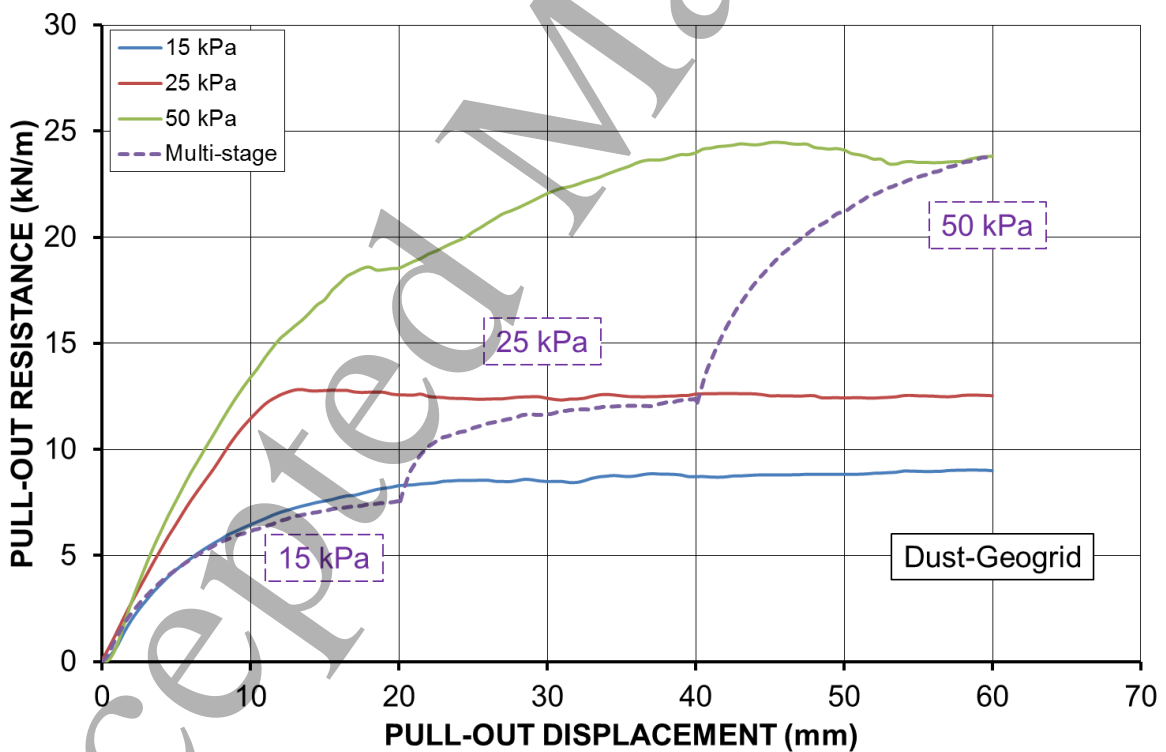


FIG 7 Comparisons of failure envelopes for single-stage and multi-stage tests: (a) direct shear and (b) interface shear.



(a)



(b)

FIG 8 Single-stage and multi-stage pull-out test results: (a) Roadbase-Geogrid and (b) Dust-Geogrid.

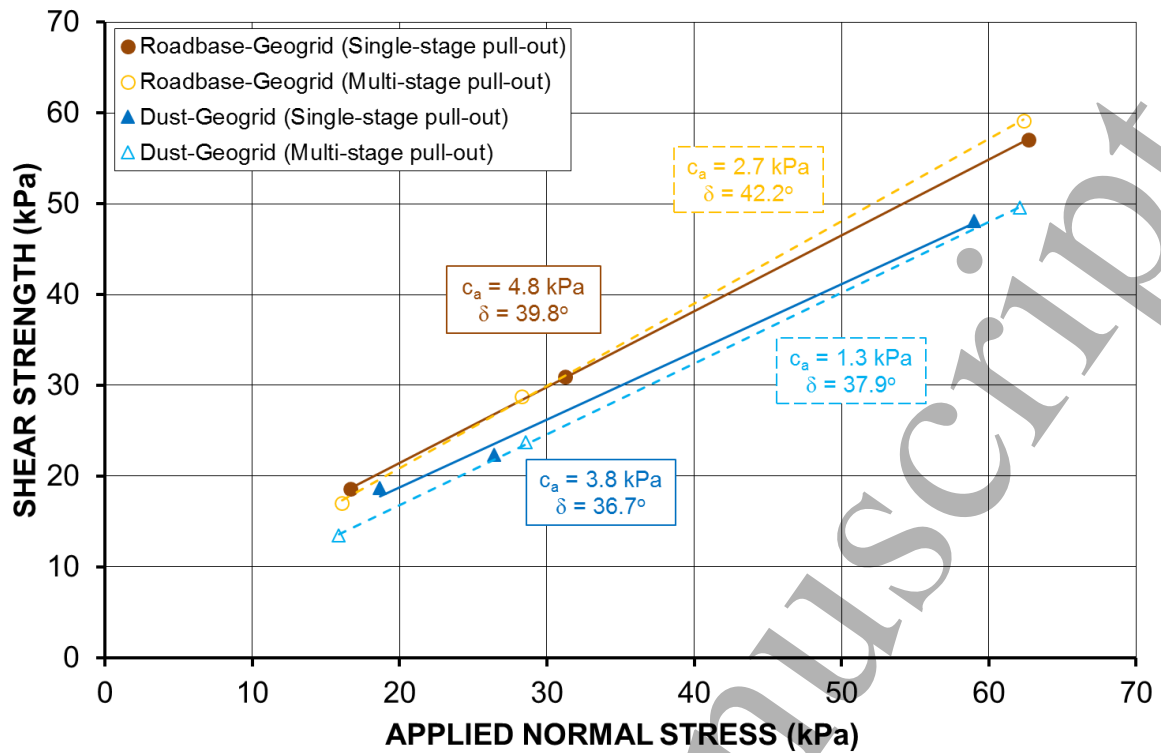
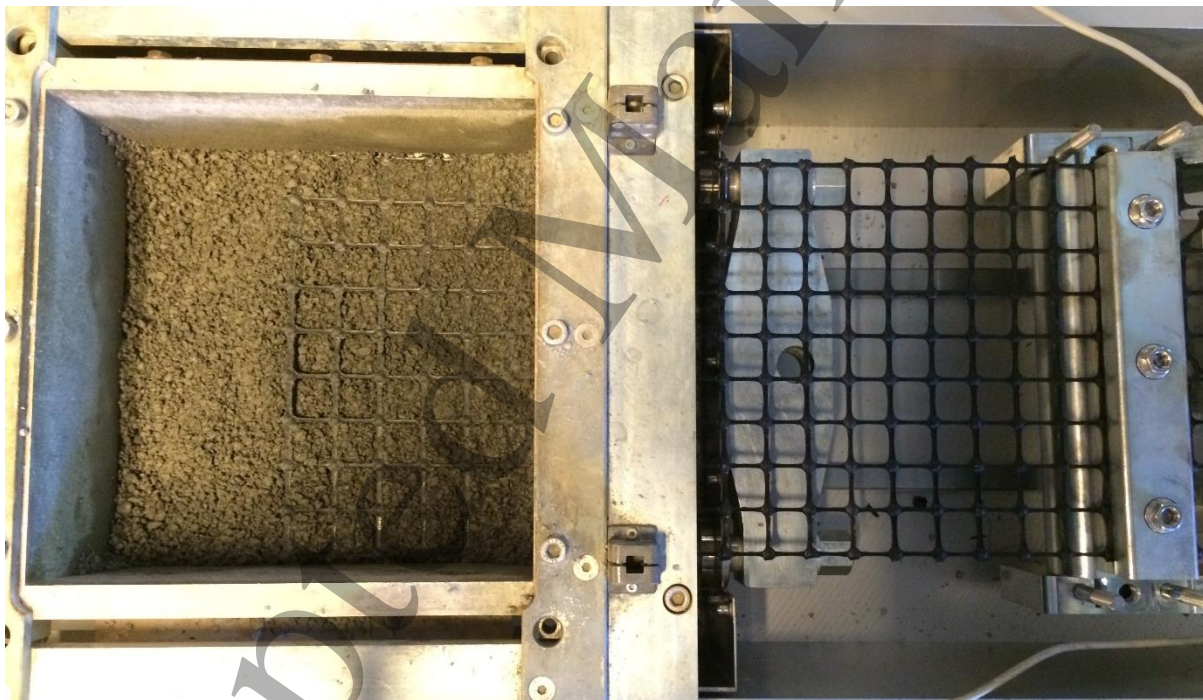


FIG 9 Comparisons of failure envelopes for single-stage and multi-stage pull-out tests.

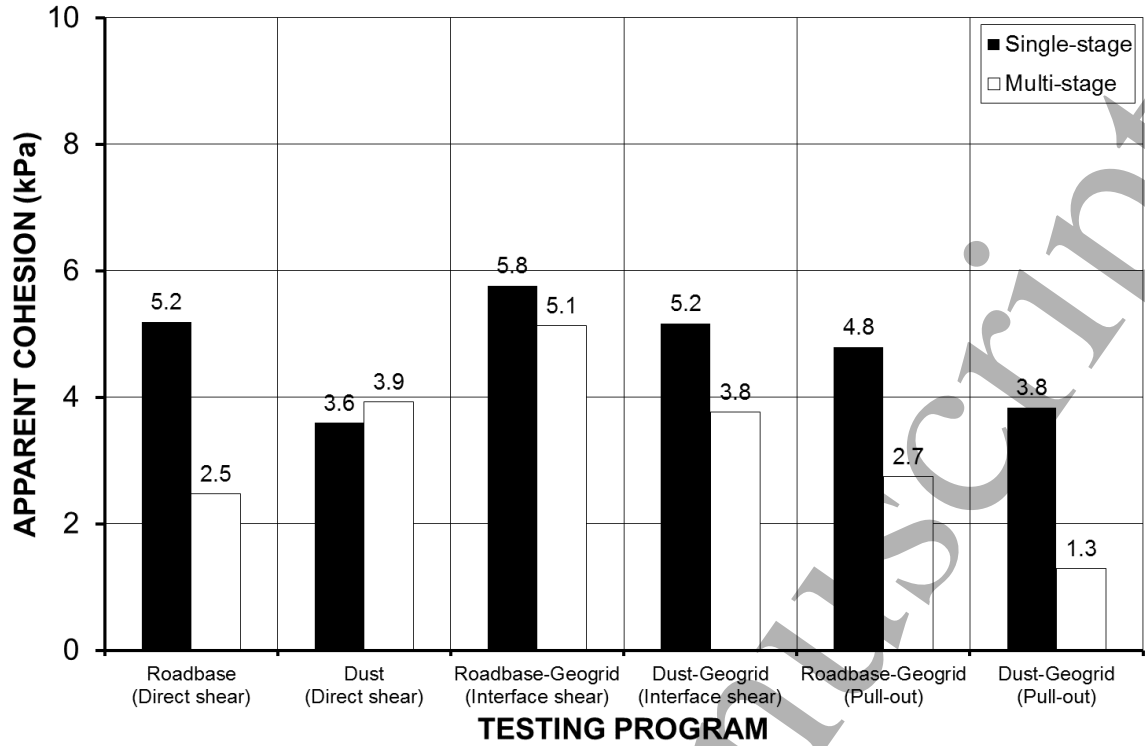


(a)

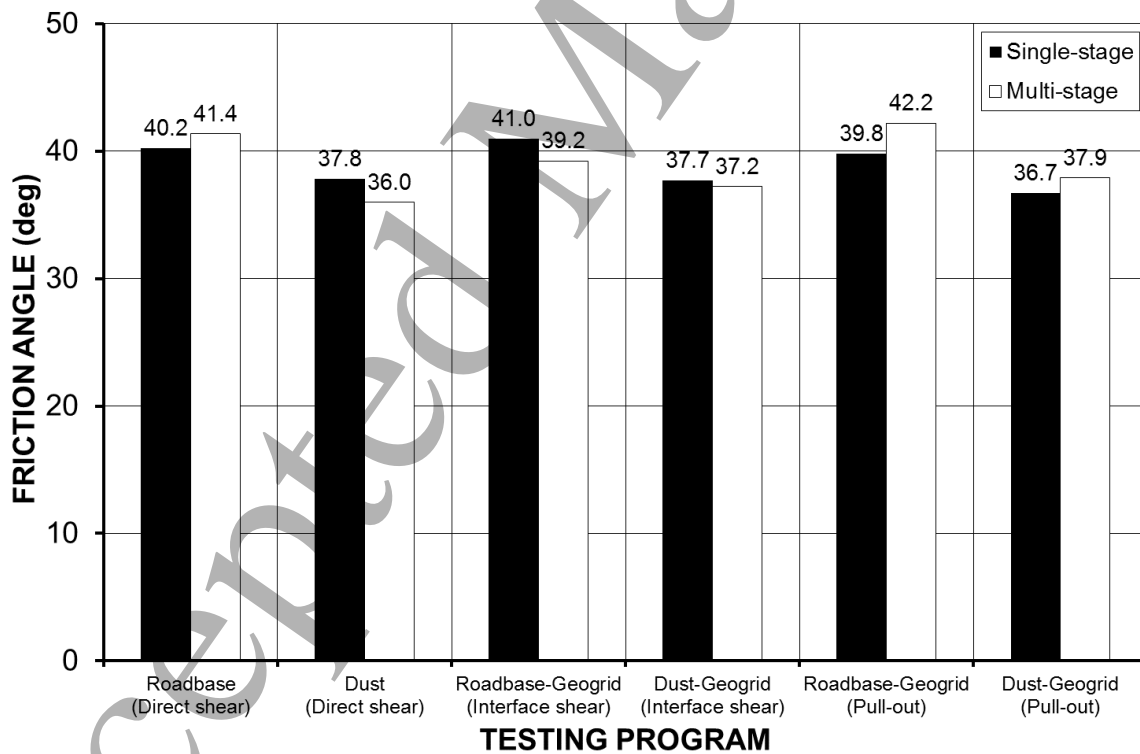


(b)

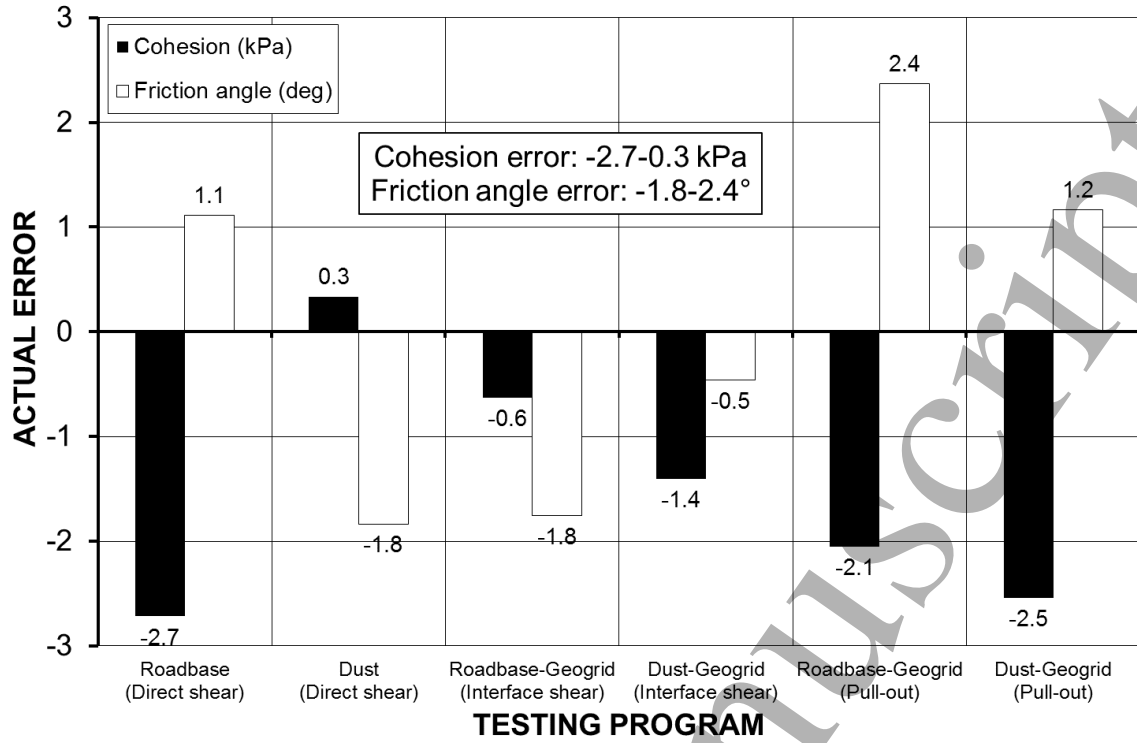
FIG 10 Two photos of Tensar SS40 geogrid embedded in soils after pull-out testing under applied normal stress of 50 kPa: (a) embedded in Roadbase and (b) embedded in Dust.



(a)

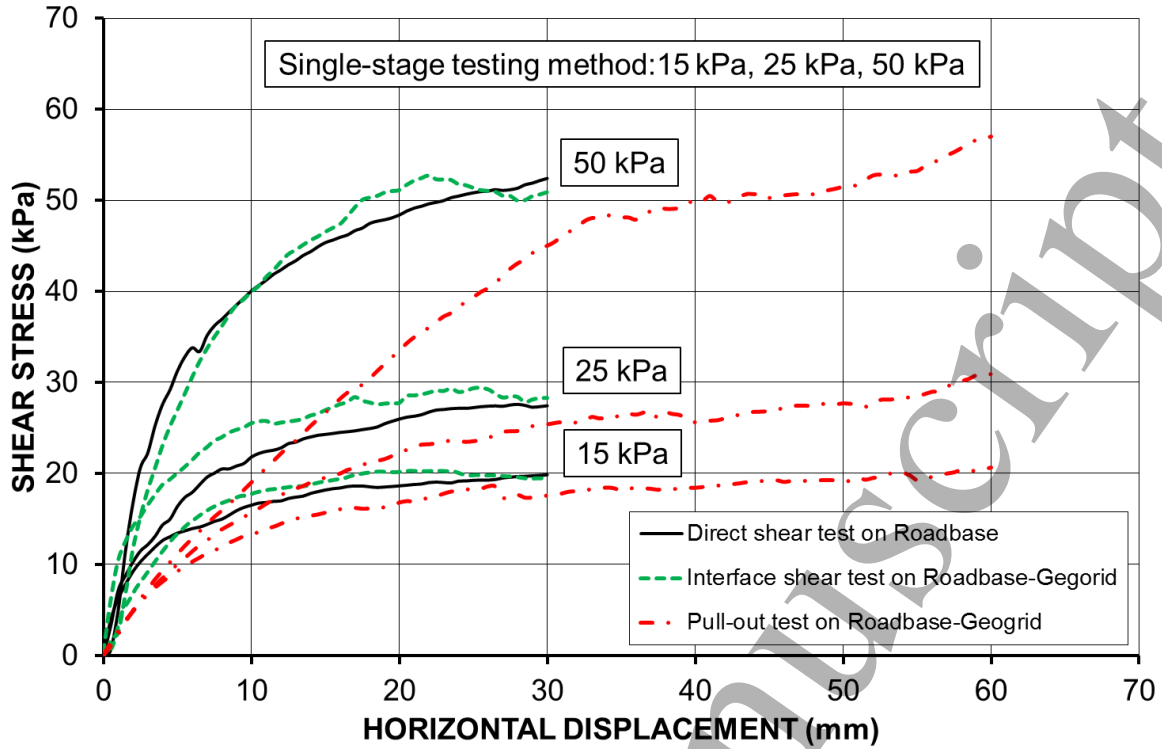


(b)

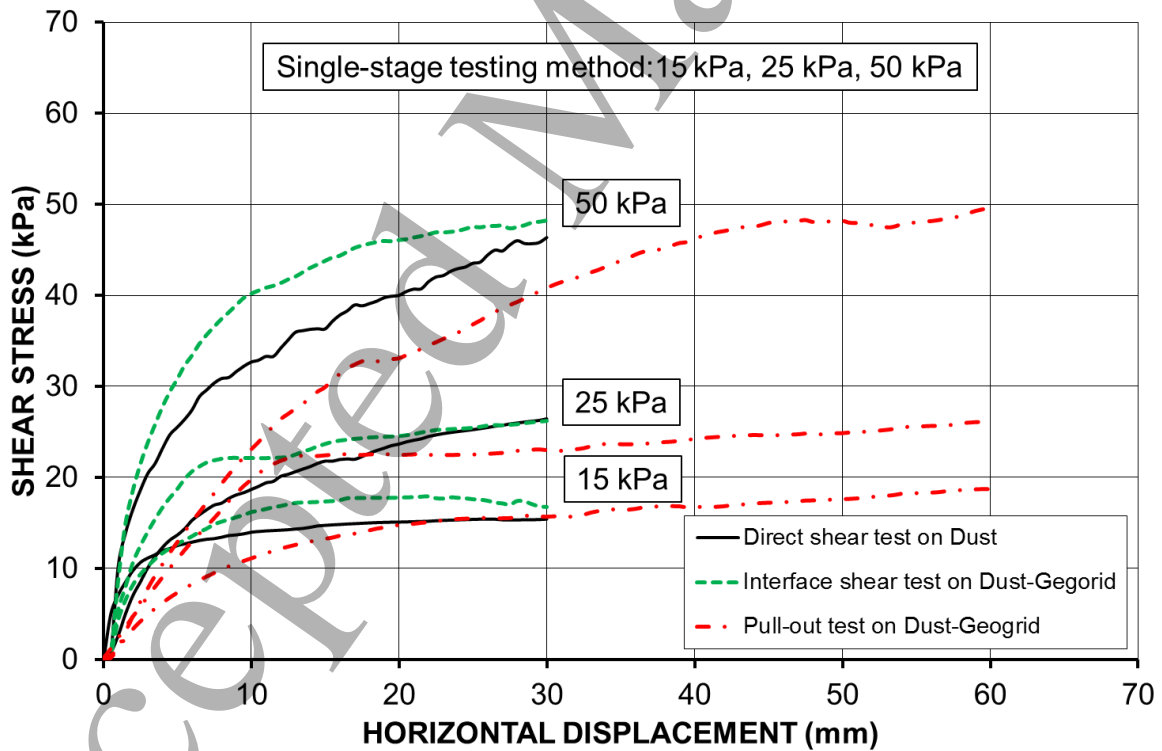


(c)

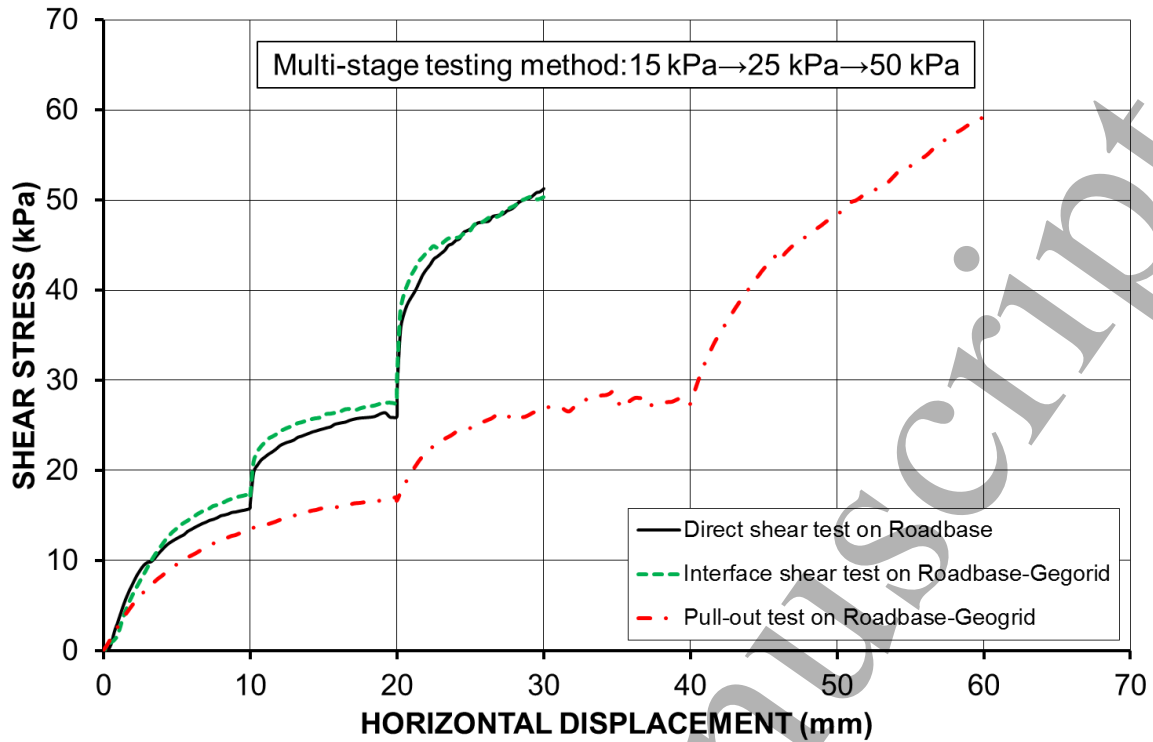
FIG 11 Comparisons of shear strength parameters obtained from single-stage and multi-stage tests: (a) cohesion, (b) friction angle, and (c) error between two testing methods.



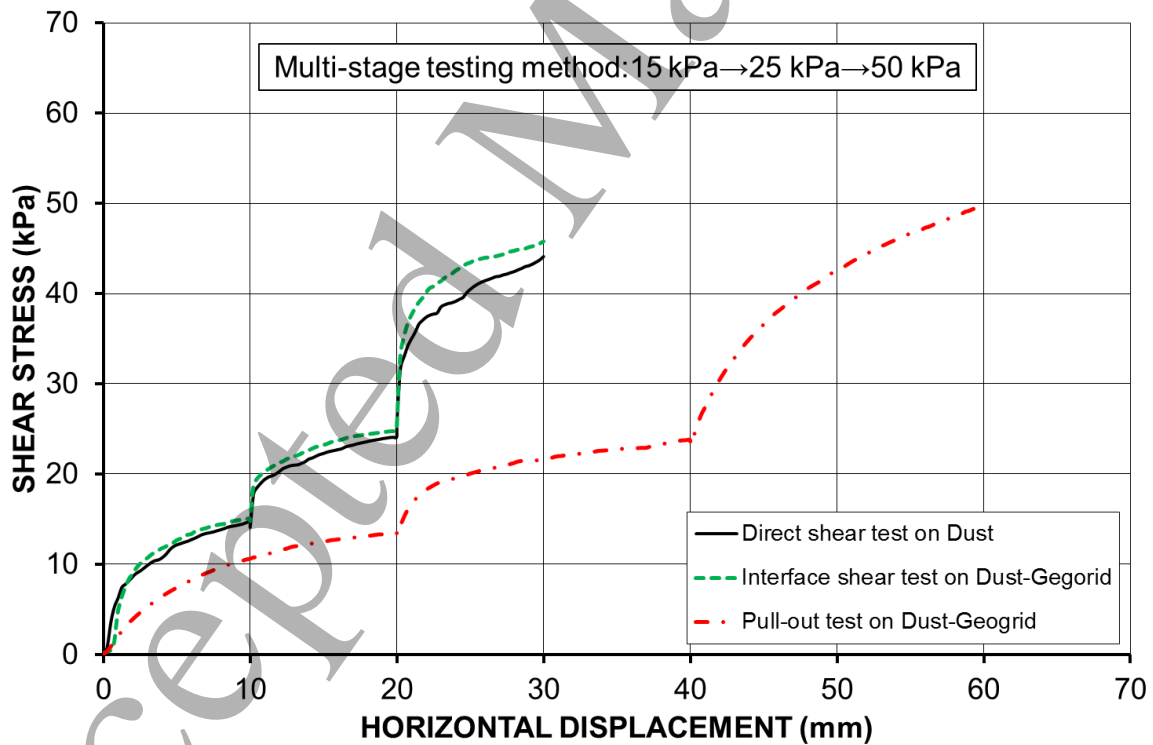
(a)



(b)



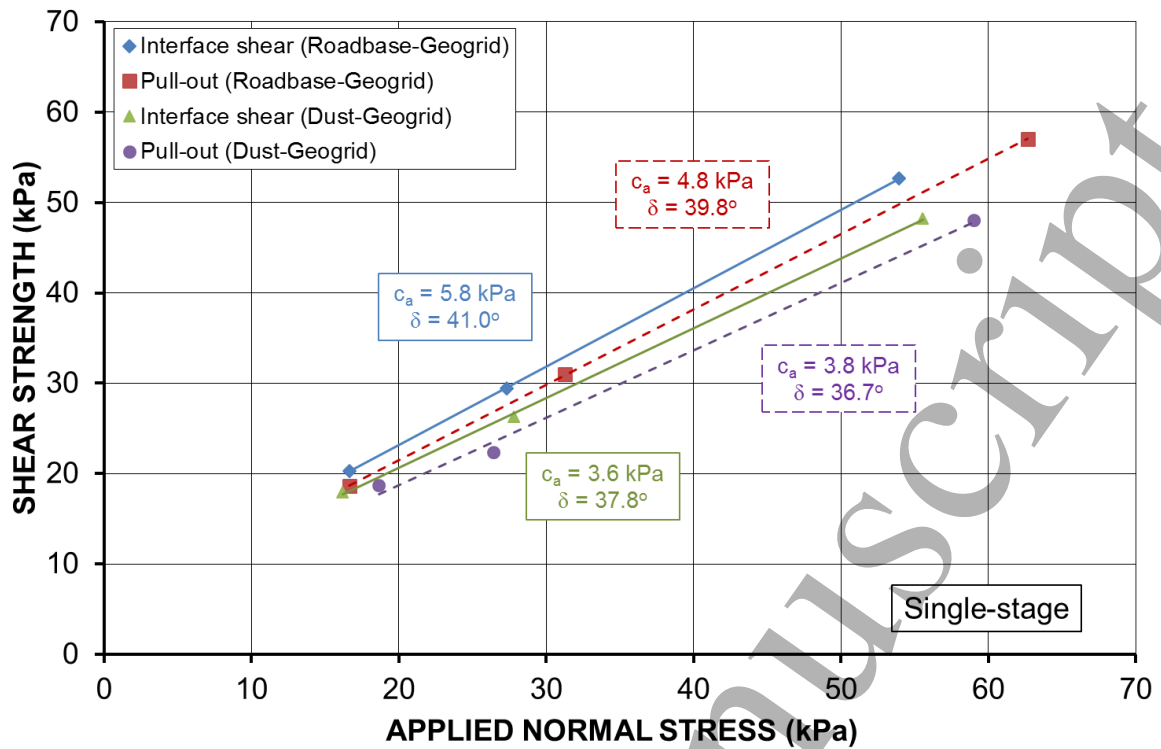
(c)



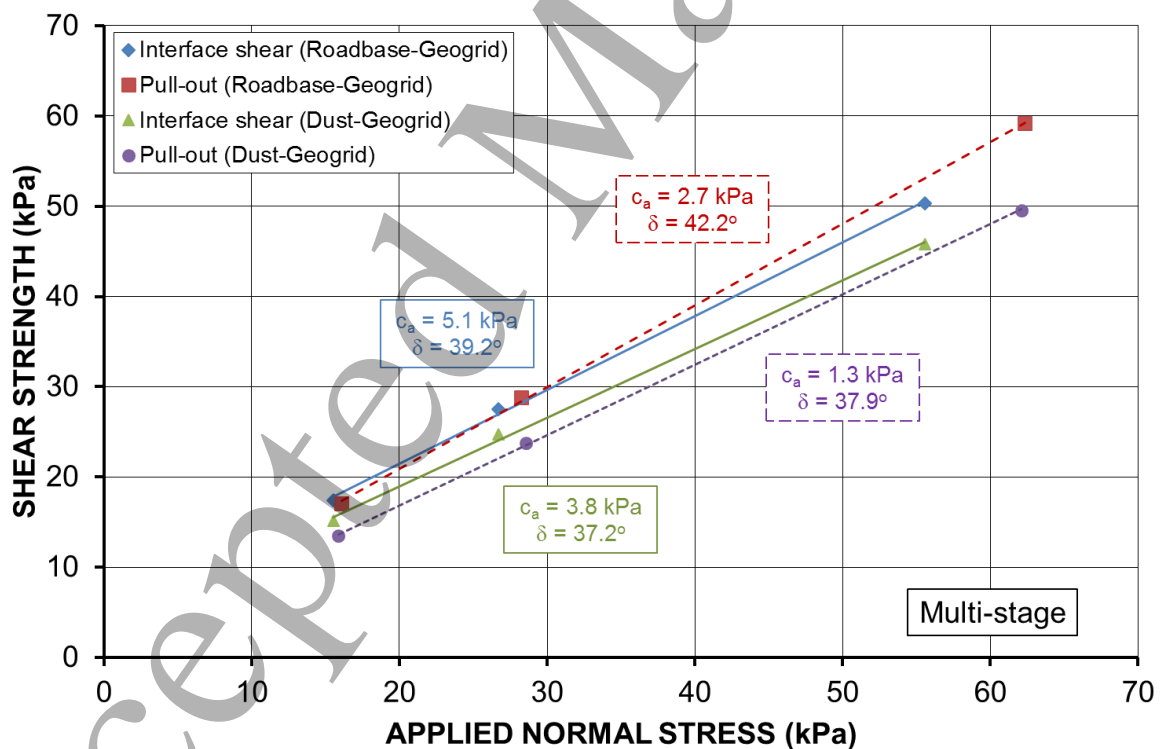
(d)

55
56
57
58
59
60

FIG 12 Comparisons of shear stress curves obtained from direct/interface shear and pull-out tests: (a) single-stage test on Roadbase, (b) single-stage test on Dust, (c) multi-stage test on Roadbase, and (d) multi-stage test on Dust.

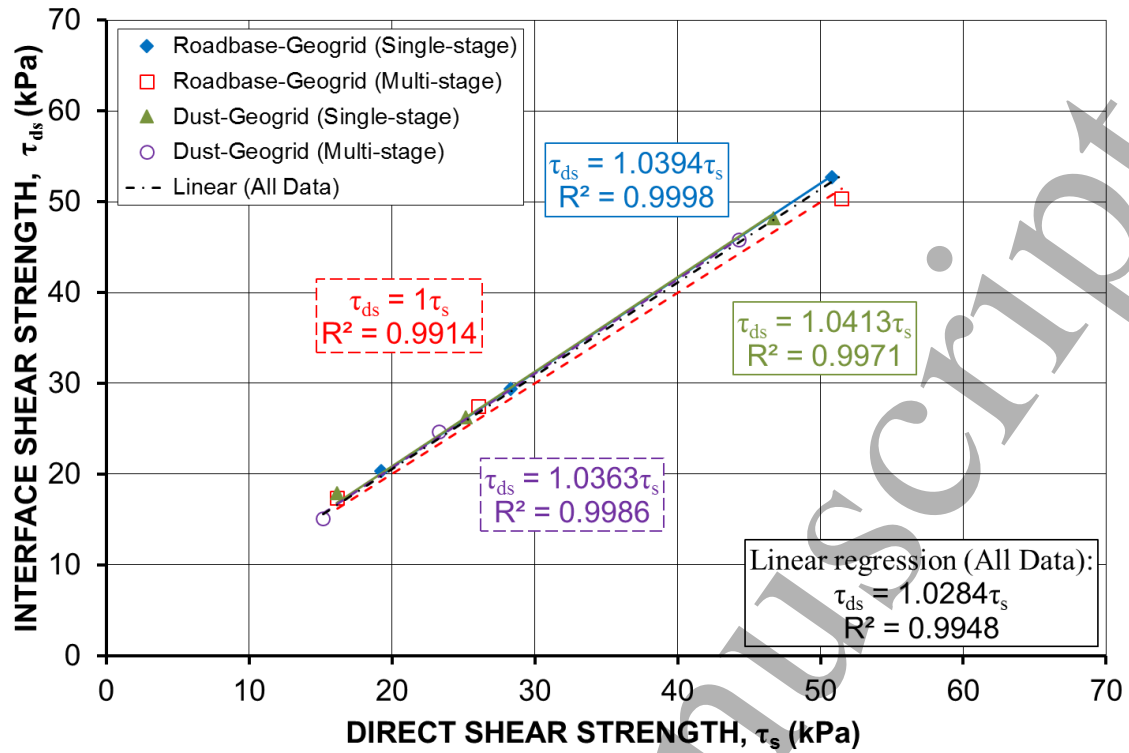


(a)

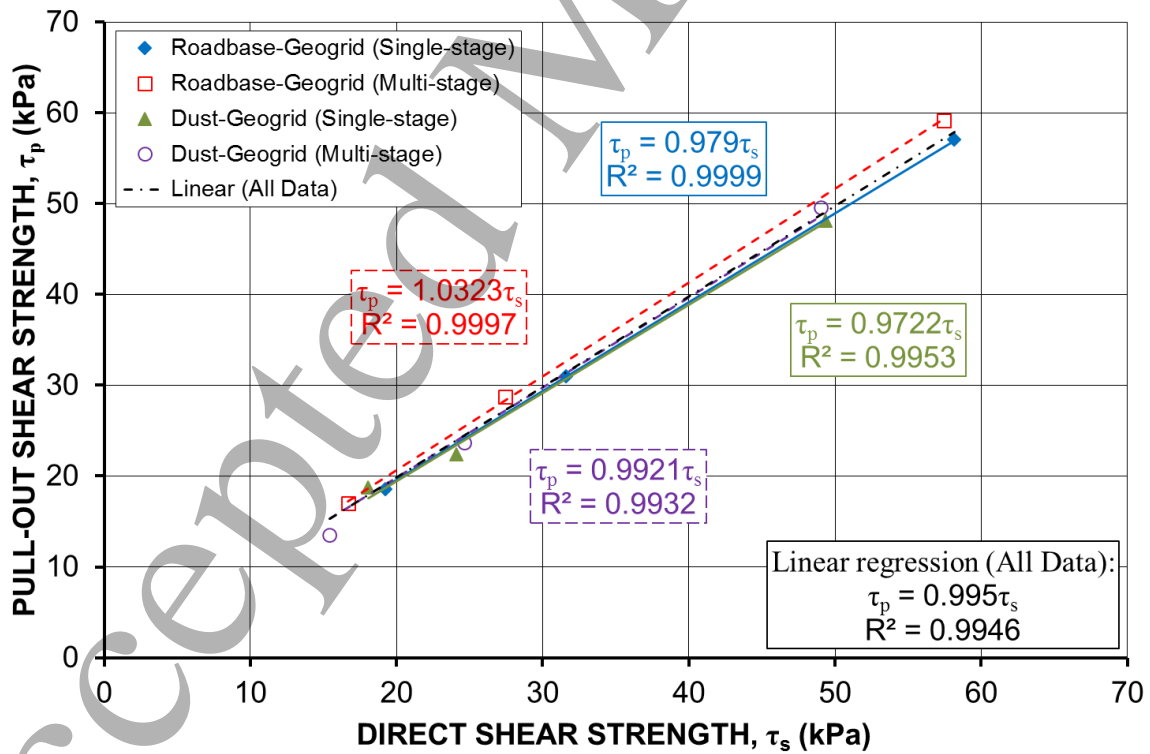


(b)

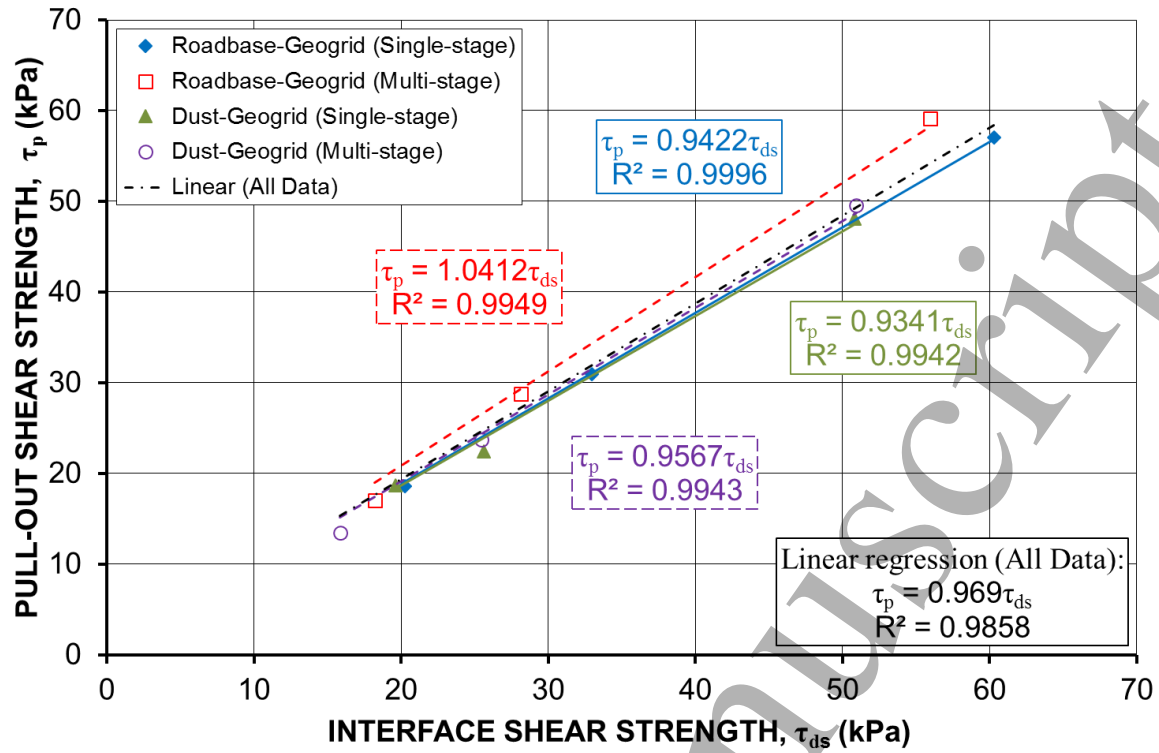
FIG 13 Comparisons of failure envelopes obtained from interface shear and pull-out tests: (a) single-stage and (b) multi-stage.



(a)



(b)



(c)

FIG 14 Comparisons of shear strengths obtained from direct/interface shear and pull-out tests: (a) τ_{ds} versus τ_s , (b) τ_p versus τ_s , and (c) τ_p versus τ_{ds} .

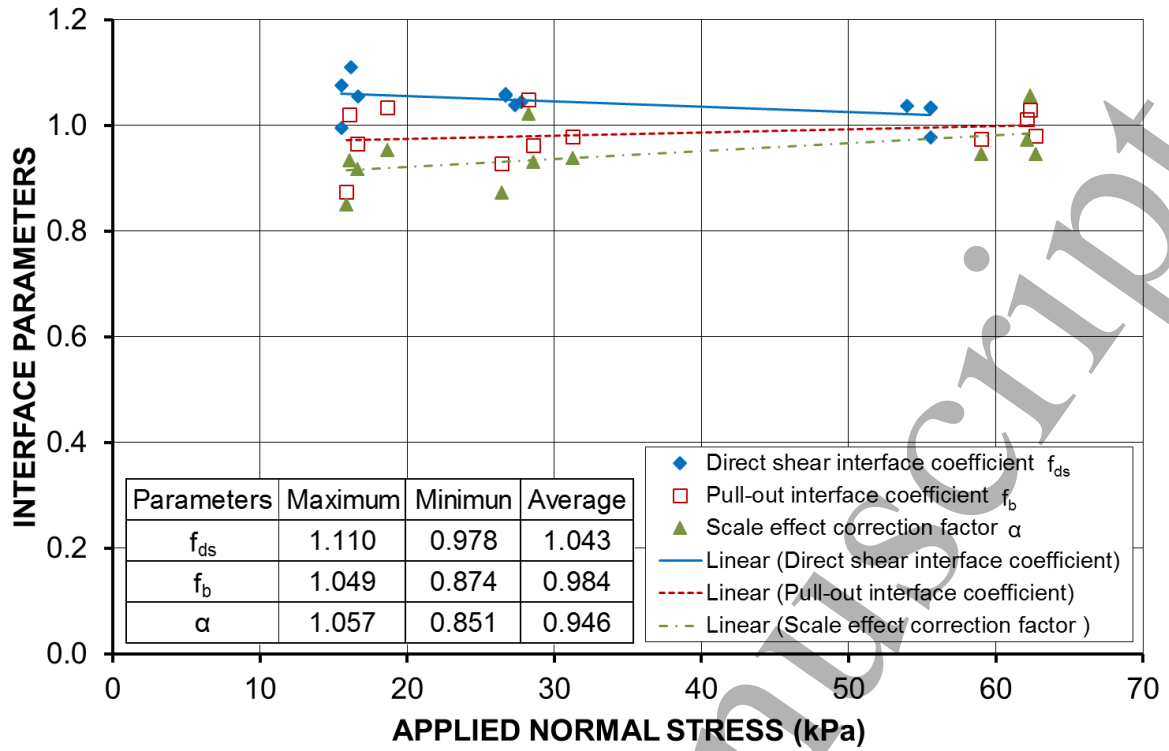


FIG 15 Calculated value of interface parameters.

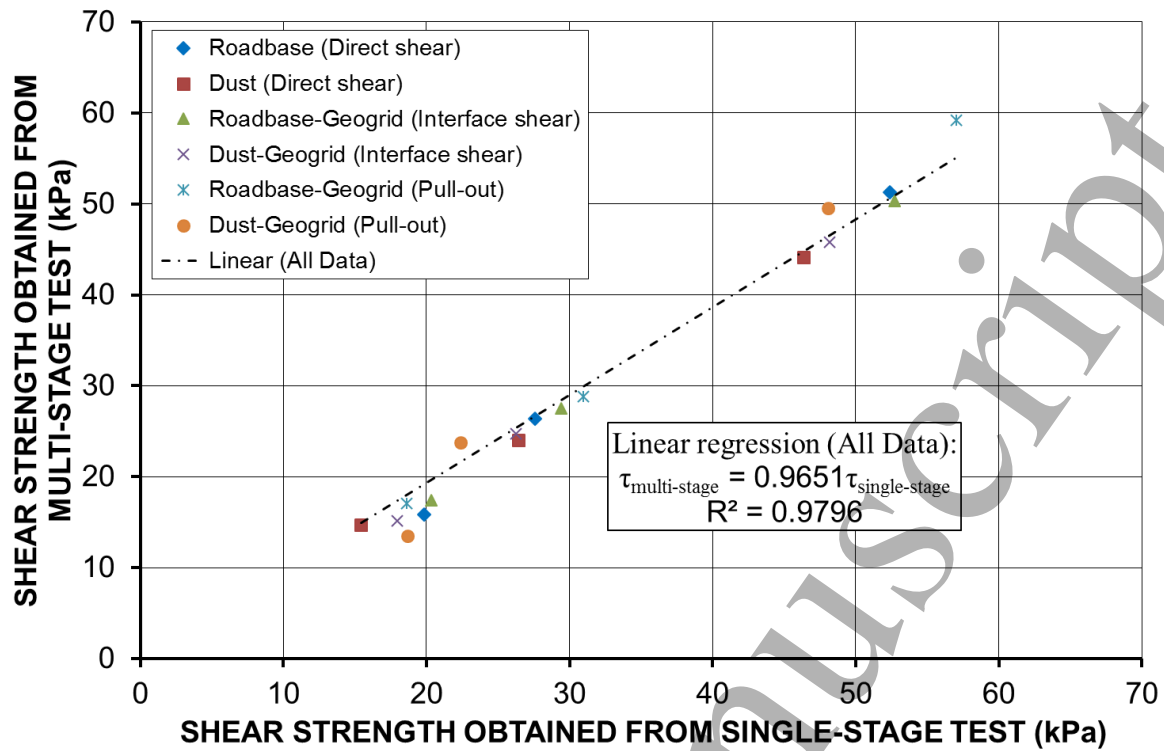


FIG 16 Linear regression of shear strengths for single-stage and multi-stage tests.

Caption List of Tables:

[TABLE 1](#) Basic properties of tested materials.

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[TABLE 3](#) Direct shear test results for Roadbase and Dust.

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[TABLE 5](#) Pull-out test results for Roadbase-Geogrid and Dust-Geogrid.

[TABLE 6](#) Shear strength parameters obtained from direct/interface shear and pull-out tests.

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TABLE 1 Basic properties of tested materials.

Soil	D_{50} (mm)	C_u	C_c	G_s	OMC (%)	ρ_{dmax} (t/m ³)	USCS
Roadbase	3.1	15.45	1.34	2.706	6.1	2.275	GW
Dust	1.8	9.58	1.16	2.725	8.8	2.158	SW
Geogrid	Polymer	Aperture Shape	Tensile Strength (kN/m)	Aperture size (mm)	Nodal thickness (mm)	Nominal rib thickness (mm)	Percentage of opening area (%)
Tensar SS40	Polypropylene	Square	40	33×33	5.8	2.5	77.4

TABLE 2 Initial conditions controlled for tested soils.

Soils	Moisture content (%)	Specimen mass (kg)	Bulk density ρ (t/m ³)	Dry density ρ_d (t/m ³)	Void ratio
Roadbase	4.80	22	1.95	1.86	0.46
Dust	5.03	21	1.85	1.76	0.55

TABLE 3 Direct shear test results for Roadbase and Dust.

Roadbase				Dust			
Single stage		Multi-stage		Single stage		Multi-stage	
σ_n (kPa)	τ_s (kPa)	σ_n (kPa)	τ_s (kPa)	σ_n (kPa)	τ_s (kPa)	σ_n (kPa)	τ_s (kPa)
16.7	19.8	15.5	15.8	16.4	15.4	15.5	14.7
27.4	27.6	26.7	26.4	27.8	26.4	26.7	24.0
55.6	52.4	55.6	51.3	55.6	46.4	55.6	44.1
c (kPa)	φ (°)	c (kPa)	φ (°)	c (kPa)	φ (°)	c (kPa)	φ (°)
5.2	40.2	2.5	41.4	3.6	37.8	3.9	36.0

TABLE 4 Interface shear test results for Roadbase-Geogrid and Dust-Geogrid.

Roadbase-Geogrid				Dust-Geogrid			
Single stage		Multi-stage		Single stage		Multi-stage	
σ_n (kPa)	τ_{ds} (kPa)	σ_n (kPa)	τ_{ds} (kPa)	σ_n (kPa)	τ_{ds} (kPa)	σ_n (kPa)	τ_{ds} (kPa)
16.6	20.3	15.5	17.4	16.2	17.9	15.5	15.1
27.3	29.4	26.7	27.5	27.8	26.3	26.7	24.7
54.0	52.7	55.6	50.4	55.6	48.2	55.6	45.8
c_a (kPa)	δ (°)	c_a (kPa)	δ (°)	c_a (kPa)	δ (°)	c_a (kPa)	δ (°)
5.8	41.0	5.1	39.2	5.2	37.7	3.8	37.2

TABLE 5 Pull-out test results for Roadbase-Geogrid and Dust-Geogrid.

Roadbase-Geogrid				Dust-Geogrid			
Single stage		Multi-stage		Single stage		Multi-stage	
σ_n (kPa)	τ_p (kPa)	σ_n (kPa)	τ_p (kPa)	σ_n (kPa)	τ_p (kPa)	σ_n (kPa)	τ_p (kPa)
16.6	18.6	16.1	17.0	18.6	18.7	15.9	13.5
31.3	31.0	28.3	28.8	26.4	22.4	28.6	23.7
62.7	57.0	62.3	59.2	59.0	48.1	62.1	49.6
c_a (kPa)	δ (°)	c_a (kPa)	δ (°)	c_a (kPa)	δ (°)	c_a (kPa)	δ (°)
4.8	39.8	2.7	42.2	3.8	36.7	1.3	37.9

TABLE 6 Shear strength parameters obtained from direct/interface shear and pull-out tests.

Specimen	Test	Single-stage		Multi-stage		Errors	
		c (kPa)	φ (°)	c (kPa)	φ (°)	c (kPa)	φ (°)
Roadbase	Direct shear	5.2	40.2	2.5	41.4	-2.7	1.1
Dust	Direct shear	3.6	37.8	3.9	36.0	0.3	-1.8
Roadbase-Geogrid	Interface shear	5.8	41.0	5.1	39.2	-0.6	-1.8
Dust-Geogrid	Interface shear	5.2	37.7	3.8	37.2	-1.4	-0.5
Roadbase-Geogrid	Pull-out	4.8	39.8	2.7	42.2	-2.1	2.4
Dust-Geogrid	Pull-out	3.8	36.7	1.3	37.9	-2.5	1.2

Note: For interface shear and pull-out tests, c , φ also stand for the apparent adhesion c_a and interface friction angle δ herein for simplicity.

TABLE 7 Interface parameters obtained from interface shear and pull-out tests.

Specimen	Test	Direct shear		Pull-out test		
		σ_n (kPa)	f_{ds}	σ_n (kPa)	f_b	α
Roadbase-Geogrid	Single-stage	16.6	1.054	16.6	0.966	0.918
		27.3	1.039	31.3	0.979	0.939
		54.0	1.037	62.7	0.980	0.946
	Multi-stage	15.5	1.076	16.1	1.021	0.935
		26.7	1.056	28.3	1.049	1.022
		55.6	0.978	62.3	1.029	1.057
Dust-Geogrid	Single-stage	16.2	1.110	18.6	1.035	0.953
		27.8	1.044	26.4	0.929	0.873
		55.6	1.032	59.0	0.974	0.947
	Multi-stage	15.5	0.995	15.9	0.874	0.851
		26.7	1.059	28.6	0.963	0.931
		55.6	1.035	62.1	1.011	0.973
Average		1.043		0.984	0.946	