

Rain retrieval method for mesoscale convective systems

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Summary. — The analysis of recent high-resolution aircraft observations over the ocean made by radar and passive microwave radiometer reveals significant problems in relating the brightness temperature measurements of the radiometer with the radar-derived rain rates. A predominant cause of this problem is that the information on rain drops contained in the radiometric measurements is contaminated by scattering and emission from other hydrometeors present in the field of view (fov) of the radiometer. Extensive observations of rain rate made by ship-borne radars and by the multichannel Special Sensor Microwave Imager (SSM/I), with a much larger for, lead to similar conclusions. Considering the variability in the meteorological conditions, and in the hydrometeors spatial distribution, we developed an empirical method to estimate rain rate based on two parameters derived from the SSM/I data, which are related to the convective dynamics. The calibration of this empirical algorithm was performed with radar ground truth for November 1992, available over the TOGA-COARE (Tropical Ocean Global Atmosphere-Coupled Ocean Atmosphere Response Experiment) region. Then the algorithm was applied to the same TOGA-COARE region for the remaining three months available. The comparison between the estimated rain rate and the radar observations gives a correlation coefficient of about 0.85, and the monthly total estimated rainfall has an error of about 13%. This rain retrieval method, tuned for Mesoscale Convective Systems (MCSs), is applicable to the Tropical Rain Measuring Mission (TRMM), where microwave radiometric observations and simultaneous radar observations are available.

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1. - Introduction

Joint aircraft observations of multichannel microwave radiometer and radar made by Heymsfield *et al.* (1996) over the Atlantic ocean adjacent to Florida, reveal

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significant problems in relating the brightness temperatures measured by the microwave radiometer with the radar-derived rain rate on a scale of a few kilometers. Also, the analysis of these aircraft observations shows that the information on rain rates contained in the Special Sensor Microwave Imager (SSM/I) brightness temperature data is weak, and that it is significantly contaminated by emission from other hydrometeors present in the clouds (see also McGhaughey and Zipser, 1996).

Rain retrieval algorithms were evaluated by the Algorithm Intercomparison Project (AIP) (Ebert, 1996) utilizing the ship-borne radar observations over the TOGA-COARE area. In that intercomparison, theoretical and empirical algorithms were evaluated for several rain events, and they explained only about 50% of the variance contained in the instantaneous rain rates on a scale of about 15 to 30 km. Furthermore, the retrieved mean rain rates, averaged over a time period of about 30 days (time span of a ship cruise in the TOGA-COARE) and over an area of about 300×300 km² (radar-scan area), showed errors of about 50% when compared to radar data. The average rain rate was systematically underestimated by about 50% in the first cruise and overestimated by about 50% in the following cruise, about one month later. These systematic biases are linked to variations in meteorological conditions on a time scale of a month to a season.

Radar rain retrieval methods are much more efficient in sensing rain drops, since the backscatter of microwave varies as \mathbf{d}^6 , where \mathbf{d} is the diameter of the rain drops (Battan, 1973). On the contrary, in the passive microwave radiometer rain retrieval techniques, the effect of the physical processes of emission and/or scattering by hydrometeors present in a vertical column of the atmosphere varies approximately as \mathbf{d}^3 (Olson *et al.*, 1996).

Since microwave brightness temperature measurements do not contain sufficient information to retrieve rain rate in different meteorological conditions, on a spatial scale of about 30 km, we have developed an empirical rain estimation method that includes implicitly some information about the MCS dynamics.

Studies of Doneaud *et al.* (1984) and Lopez *et al.* (1989) based on radar observations show evidence of the importance of the rain area and its relationship to area-average rain rate. The GOES Precipitation Index (GPI) method of Arkin and Meisner (1987) based on satellite infrared radiometric data also depends on the rain area as a principal parameter. Based on these studies, we have introduced the rain area in the microwave-radiometer rain retrieval method. This parameter emphasizes the importance of macroscopic structure that relates more closely to MCS dynamics in the atmosphere, rather than the microscopic properties of the rain.

2. - The rain retrieval method

Radar observations over the TOGA-COARE region in the equatorial Pacific reveal several useful properties of the maritime tropical rain (Short *et al.*, 1997). Since these radars operated continuously, we could follow the life cycle of the MCSs in this region that lasted for several hours. In the early stages of the MCSs, rain from convective cells that have a scale of 1 to 2 km dominates, and the average convective rainfall is greater than the average stratiform rainfall. Later, stratiform rainfall prevails and radar data show an enhancement of reflectivity around 4.5 km altitude, due to melting snow particles (Meneghini and Kumagai, 1994) that fall slowly inside the stratiform clouds. The spatial distribution of rain at any time during the life cycle of the MCS

follows a probability distribution that is analogous to the log-normal type (Jones and Sims, 1978). Meteorological conditions, such as the vertical distribution of winds, humidity, and temperature, play an important role in determining the intensity of rain, and growth and distribution of various hydrometeors in the convective and stratiform cloud systems (Takahashi *et al.*, 1995; McGaughey and Zipser, 1996; Houze and Betts, 1981).

We find that the information given by the SSM/I measured brightness temperatures $T_{85\mathrm{v}}$ and $T_{85\mathrm{h}}$ (the vertical and horizontal polarization in the 85 GHz channel) is preferable to other channels. In these channels, atmospheric water vapor, molecular oxygen, and cloud liquid drops have appreciable absorption. Because of this, when there are non-raining clouds with appreciable optical thickness, the brightness temperature in these channels is close to the temperature of the uppermost cloud liquid layers. When rain develops with no ice phase in the cloud, there is a weak scattering of the 85 HGz radiation due to rain drops. However, when ice particles are present in the clouds above the freezing level, they lead to a significant drop in the 85 HGz brightness temperature due to scattering. This temperature depression gives an indirect indication of precipitation below the clouds (Wu and Weinman, 1984; Spencer, 1986; Adler $et\ al.$, 1991). In addition, the field of view (fov) of the 85 HGz channel, which is about 15 km, is the smallest of all the SSM/I channels.

Based on an examination of the SSM/I data, taken from a satellite orbit over the TOGA-COARE region, we can infer the presence of scattering in a 85 HGz pixel inside this region, and we define a scattering depression $D_{\rm s}$ as

(1)
$$\mathbf{D}_{s} = (T_{85 \text{ h}}^{0} - T_{85 \text{ h}}) - \mathbf{C}^{0},$$

where $T_{85\,\mathrm{h}}$ is the 85 GHz brightness temperature in the horizontal polarization, \mathbf{C}^0 is a constant chosen to set a threshold on \mathbf{D}_{s} , and

(2)
$$T_{85 \text{ h}}^{0} = T_{85 P \text{ max}} - \left(\frac{dT_{85 \text{ h}}}{dP_{85}} \right) \cdot \left(P_{85 \text{ max}} - P_{85} \right).$$

Here P_{85} is the 85 GHz polarization difference $(T_{85\,\mathrm{v}}-T_{85\,\mathrm{h}})$ at a pixel inside the TOGA-COARE region and $P_{85\,\mathrm{max}}$ is the maximum value at some point A within this region, which has a corresponding value $T_{85\,\mathrm{P\,max}}$ of the brightness temperature. A second point B is chosen at the maximum value $T_{85\,\mathrm{h\,max}}$ of the brightness temperature in the same region, which has a corresponding value $P_{85\,\mathrm{T\,max}}$ of the polarization difference.

The slope of the line AB, introduced in eq. (2), is

(3)
$$(dT_{85 \text{ h}}/dP_{85}) = (T_{85 \text{ h}max} - T_{85 Pmax})/(P_{85 Tmax} - P_{85 max}),$$

and $T^0_{85\,\mathrm{h}}$ is the largest possible value of $T_{85\,\mathrm{h}}$ in the TOGA-COARE region for any given value of P_{85} (see fig. 1). We assume that $T^0_{85\,\mathrm{h}}$ represents non-raining cloud conditions, and that rain starts when $(T^0_{85\,\mathrm{h}}-T_{85\,\mathrm{h}})$ is greater than the threshold value C° , which is empirically set equal to 6 K. If N is the total number of pixels that fit in the TOGA-COARE region, and n is the number of rain pixels where D_{s} is greater than zero, i.e. where rain is present, then the ratio n/N gives the fractional rain area f_{R} , which is the main parameter in our rain retrieval algorithm, in the TOGA-COARE region:

$$f_{\rm R} = n/N .$$

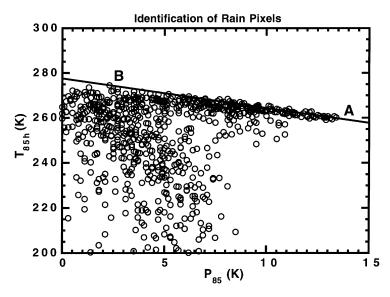


Fig. 1. – Scatter plot of P_{85} vs. $T_{85\,\mathrm{h}}$ for the rain event at 10:31 UTC of day 359 (Dec. 24, 1992) observed by F10 SSM/I over the TOGA- COARE region. The line AB gives the largest value of $T_{85\,\mathrm{h}}$ for any given value of P_{85} .

The scattering depression \mathbf{D}_s of eq. (1) is essentially related to an effective optical depth of the ice hydrometeors contained in the layers of the precipitating clouds above the freezing level. We define the scattering index \mathbf{S} over the entire TOGA-COARE region as

(5)
$$\mathbf{S} = (1/N) \sum_{i=1}^{n} \mathbf{D}_{s_i},$$

where the summation is taken only over those n pixels for which $\mathbf{D}_{\mathbf{s}_i}$ is greater than zero, so that the scattering index \mathbf{S} depends directly on the fractional rain area.

The brightness temperatures at the low frequencies 19 and 37 GHz are strongly related to the emission of hydrometeors (Wilheit *et al.*, 1991; Prabhakara *et al.*, 1992; Petty and Katsaros, 1992; Kummerow *et al.*, 1989), and an emission index **E** in the TOGA-COARE region can be obtained from the same SSM/I data. Let us define P_{19} and P_{37} at a given point in the TOGA-COARE region as $P_{19} = (T_{19\,\text{v}} - T_{19\,\text{h}})$ and $P_{37} = (T_{37\,\text{v}} - T_{37\,\text{h}})$, where $T_{19\,\text{v}}$, $T_{19\,\text{h}}$, $T_{37\,\text{v}}$, and $T_{37\,\text{h}}$ represent the vertical and horizontal polarization brightness temperatures in the 19 and 37 GHz channels, respectively. To a first approximation the quantities P_{19} and P_{37} can be related to the optical depths of the hydrometeors at 19 and 37 GHz.

It can be assumed that where the atmosphere is cloud free, these optical depths represent the relatively small opacities caused by water vapor. At that point P_{19} and P_{37} are determined primarily by the polarizing effect of the sea surface, while at all other points in the TOGA-COARE region the optical depths include the opacity due to cloud liquid drops, rain, and melting and frozen particles in the fov of the radiometer. We can now define an effective emission ratio ${\bf e}$ as

(6)
$$\mathbf{e} = P_{19} / P_{37}.$$

This parameter is nearly independent of wind-induced emissivity changes at the surface, and depends essentially on the total content of rain and other hydrometeors in a column of the atmosphere.

By summing ${\bf e}$ taken from the radiometric data in the same n pixels where $D_{\mathbf{s}_i}$ is greater than zero, we obtain the total emission due to hydrometeors associated with precipitation present in the grid box. The emission index ${\bf E}$ of the grid box is then defined as

(7)
$$\mathbf{E} = (1/N) \sum_{i=1}^{n} \mathbf{e}_{i}.$$

This summation is taken only over the n pixels so that \mathbf{E} , like \mathbf{S} , depends directly on the fractional rain area $f_{\mathbf{R}}$. Although \mathbf{S} and \mathbf{E} will be correlated because of this, the ratio \mathbf{S}/\mathbf{E} is sufficiently independent of $f_{\mathbf{R}}$ and can be used as a second parameter in the rain retrieval scheme, as shown in fig. 2, obtained from the 87 mesoscale rain events of the four-months TOGA-COARE data. The ratio \mathbf{S}/\mathbf{E} adopted is approximately related to the ratio of the optical depth of the ice hydrometeors in the layers of the clouds above the freezing level and the optical depth of the liquid hydrometeors that are below the freezing level. When heavy convective rain is present, this ratio tends to be large because of strong scattering due to frozen dense hydrometeors. For stratiform clouds with less dense ice hydrometeors that scatter weakly, this ratio is relatively small. Moreover, the data in fig. 2 show that there are more cases of heavy convective rain when $f_{\mathbf{R}}$ is small.

Radar rain observations over the same N pixels of the overlap area can be averaged to give the area average rain rate R_A in the TOGA-COARE region, used as ground

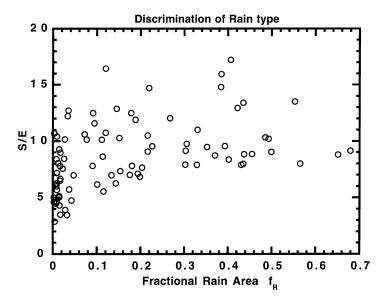


Fig. 2. – Scatter plot of the fractional rain area $f_{\rm R}$ vs. the parameter S/E, that discriminates convective rain from stratiform rain.

truth for the retrieval method:

(8)
$$R_{A} = (1/N) \sum_{i=1}^{N} R_{i},$$

where R_i is the radar-derived rain rate in each 85 HGz pixel, that is greater than a fixed threshold of 0.2 mm/h (see the following section).

3. - Rain retrieval over the TOGA-COARE region

From each orbital pass made by the F10 and F11 satellites over the TOGA-COARE region, we can get one combined radar and radiometric data set in the overlap area. We can then choose for our analysis the data sets that contain rain.

It should be pointed out that, in the TOGA-COARE experiment, the radar and radiometric data are not synchronized perfectly in time because the satellite-borne radiometer takes about 50 s to cover 300 km, while the volume scans of the radars take about 10 minutes. For this reason, the fractional rain area $f_{\rm R}$ determined from radiometric data and the rain rate $R_{\rm A}$ based on radar data will not be matched perfectly in time (Dalu *et al.*, 1998). In the present study we are dealing with area-time averages, and we can assume that this discrepancy can be neglected. Note that in the Tropical Rain Measuring Mission (TRMM), this discrepancy will be minimized.

To test how well $f_{\rm R}$ represents the fractional rain area, we have taken a radar-derived rain rate of 0.2 mm/h as a threshold, and we have calculated an alternate fractional rain area $f_{\rm R>0.2}$ in the overlap area. The correlation coefficient between $f_{\rm R}$, based on radiometric data, and $f_{\rm R>0.2}$, based on radar data, is about 0.92 for the entire TOGA-COARE data, and we can assume that $f_{\rm R}$ represents the fractional rain area.

We obtain similar high correlation coefficients between f_R and $f_{R>0.2}$ with values of the threshold \mathbf{C}^0 in the range of 3 to 6 K. However, the correlation coefficient decreases significantly with a further increase in \mathbf{C}^0 , or with an increase in the radar rain-rate threshold.

The area-average rain-rate estimation method developed in this study is based mainly on the four months of TOGA-COARE radar and radiometric observations, with 87 MCS events at different stages of their evolution. In order to assess the relative importance of $f_{\rm R}$ and ${\bf S/E}$, we have made plots of radar-derived rain rate $R_{\rm A}$ vs. radiometer-derived $f_{\rm R}$, and of $R_{\rm A}$ vs. ${\bf S/E}$ as shown in fig. 3a and b. We find that $f_{\rm R}$, can explain about 65% of the variance contained in $R_{\rm A}$. Furthermore, an examination of fig. 3a reveals that $R_{\rm A}$ tends to increase non-linearly with respect to $f_{\rm R}$. This non-linearity may be approximated with an exponential relationship of the form $R_{\rm A}$ = [exp[$kf_{\rm R}$] - 1], where k is a constant. The parameter ${\bf S/E}$, on the other hand, can explain only about 25% of the variance contained in $R_{\rm A}$.

The indication that $R_{\rm A}$ grows exponentially with $f_{\rm R}$ suggests a feedback mechanism. Basically it implies that, as the area of the MCS increases due to intensification of moist dynamics, the area-average rain rate increases in an exponential fashion. Chiu (1988) indicates a similar relationship between fractional rain area and area-average rain rate. We will use this observational information in our rain retrieval method.

We have analyzed the relationship between R_A and f_R on a monthly basis for the entire TOGA-COARE data, and we find that the slope of the regression line between R_A and $[\exp[kf_R]-1]$ changes considerably from one month to the other. This variation in the slope of the regression line between R_A and $[\exp[kf_R]-1]$ may be

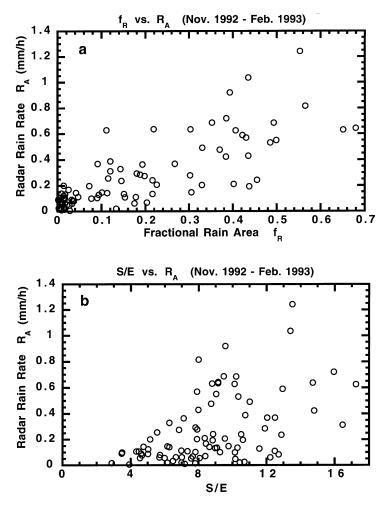


Fig. 3. – a) Scatter plot of fractional rain area $f_{\rm R}$ vs. $R_{\rm A}$, the radar-observed rain rate for the four months of the TOGA-COARE observations. b) Scatter plot of the ratio S/E vs. $R_{\rm A}$, for the same data.

related to the changes in the dynamics of the atmosphere, which effect the fractional rain area on a monthly-to-seasonal time scale. So we cannot apply the relationship between $R_{\rm A}$ and $f_{\rm R}$ developed from one month of data to estimate the rain rate in another month. However, this is possible by scaling $f_{\rm R}$ with $(f_{\rm R_{av}})^{0.5}$, where $f_{\rm R_{av}}$ is the monthly mean value of the fractional rain area. From the TOGA-COARE data we find that the slope of the regression line between $R_{\rm A}$ and $\{\exp[k\cdot f_{\rm R}/(f_{\rm R_{av}})^{0.5}]-1\}$ differs, from one month to the other during the TOGA period, only by about 10%. A value of $f_{\rm R_{av}}$ was calculated for the averaging period of one full month, to have a sufficient number of MCS events. This was done for each month of the TOGA-COARE period (November 1992 to February 1993), and the values of $f_{\rm R_{av}}$ derived from the SSM/I data show a significant change from one month to the other. These monthly variations in $f_{\rm R_{av}}$ are consistent with the radar observations.

Based on the exponential dependence of $R_{\rm A}$ on $f_{\rm R}$ and the scaling indicated above, the following relationship, that includes the variable S/E, is developed to give the estimated rain rate $R_{\rm est}$ for each month:

(9)
$$R_{\text{est}} = \exp\left[0.05 \cdot (\mathbf{S/E}) \cdot [f_R / (f_{R_{av}})^{0.5}]\right] - 1.$$

The coefficient 0.05 was obtained by matching $R_{\rm est}$ with the radar ground truth data $R_{\rm A}$ for the rain events of the month of November 1992, and it is adopted for the independent data sets of the other months. The correlation coefficients between the radar rain rate and the rain rate estimated with eq. (9) for all the rain events in each month are shown in the scatter plots presented in figs. 4a, b, c, and d.

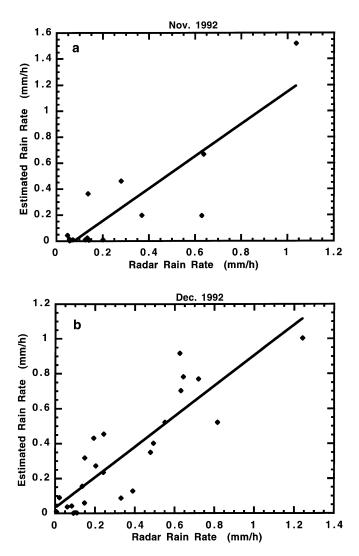


Fig. 4. – Scatter plot of radar observed rain rate $R_{\rm A}$ vs. SSM/I estimated rainfall rate $R_{\rm est}$. The line indicates the linear regression fit. a) Nov. 1992, Corr. Coeff. = 0.89; b) Dec. 1992, Corr. Coeff. = 0.84.

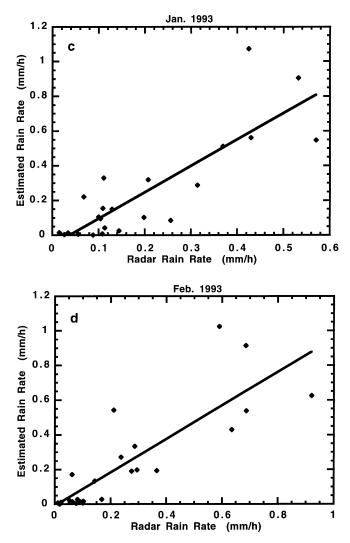


Fig. 4. – Scatter plot of radar observed rain rate $R_{\rm A}$ vs. SSM/I estimated rainfall rate $R_{\rm est}$. The line indicates the linear regression fit. c) Jan. 1993, Corr. Coeff. = 0.76; d) Feb. 1993, Corr. Coeff. = 0.81.

Since $R_{\rm est}$ given by eq. (9) depends strongly on $f_{\rm R}$, this estimate can be more closely related to the dynamics of the atmosphere, rather than to the radiative transfer interactions.

The mean rain rates obtained from all the AIP-3 SSM/I algorithms for each of the three ship cruises (each cruise lasted for about 30 days) were compared with radar data by Ebert (1996). We have done a similar comparison with our retrieval method, and the results are presented in table II below for the three ship cruises within the overlap area in the TOGA-COARE region. The values of $f_{\rm R}$ are based on the data calculated for each cruise. We note that the percentage error in the retrieved mean rain rate is about 10%. In the retrieval algorithms evaluated by the AIP-3 (Ebert et al., 1996), it was

shown that this percentage error is about 50%, because of the presence of biases. In fact, an underestimation of about 50% in the average rain rate retrieved by the AIP-3 algorithms was found in cruise 1 (11 November 1992 to 10 December 1992), while in cruise 2 (15 December 1992 to 18 January 1993) there was an overestimation of about 50% (see Ebert *et al.*, 1996).

The monthly mean rain rates, shown in table I for the calendar months and in table II for the individual cruises, depend on the scaling parameter $(f_{\rm R_{av}})^{0.5}$ that empirically takes into account month-to-month changes in the dynamical state of the atmosphere. We see that this parameter can change by almost a factor of two in the months considered and it is mainly responsible for the reduction of large errors on a monthly time scale that were found in other algorithms. Furthermore, the instantaneous rain rates retrieved from our algorithm (see figs. 4a, b, c, and d) have a correlation coefficient of about 0.85 with respect to radar observations.

The retrieval method developed here is potentially capable of satisfying the main objective of the TRMM mission, which is to derive monthly-mean rainfall over a latitude-longitude grid box of $5^{\circ} \times 5^{\circ}$ with an error of about 10% (Simpson, 1988).

Equation (9) has to be determined with the help of the radar data over a latitude-longitude grid of $5^{\circ} \times 5^{\circ}$ and on a time scale of about a month. Since in the TRMM mission about one third of the radiometric data are co-located with the radar data, $f_{\rm R}$ and the coefficient in eq. (9) can be determined on a month-to-month basis. Since the microwave radiometer and radar will be closely synchronized in the TRMM mission, errors arising from non-simultaneous data should be negligible.

Table I. – Comparison of mean mesoscale rain rates (mm/h) within the overlap area for all the MCS events in a month. $R_{\rm est}$ is estimated from SSM/I and $R_{\rm A}$ is observed by radar. NR is the number of MCS events and $(f_{R_{\rm av}})$ is the mean fractional rain area. %Error = $100 \cdot (R_{\rm est} - R_{\rm A})/R_{\rm A}$.

	NR	Corr. Coeff.	$1/(f_{\rm R_{av}})^{0.5}$	$R_{ m A}$	$R_{ m est}$	%Error
Nov. 92	15	0.89	3.17	0.265	0.236	- 11
Dec. 92	24	0.84	1.86	0.358	0.346	- 4
Jan. 93	23	0.76	2.57	0.195	0.242	24
Feb. 93	25	0.81	2.58	0.248	0.229	- 8

Table II. – Same as Table I, but for three TOGA-COARE ship cruises. %Error = $100 \cdot (R_{\text{est}} - R_{\text{A}})/R_{\text{A}}$.

	NR	Corr. Coef.	$1/(f_{ m R_{av}})^{0.5}$	$R_{ m A}$	$R_{ m est}$	%Error
Cruise 1 Nov. 10-Dec. 92	20	0.87	3.31	0.235	0.214	10
Cruise 2 Dec. 92-18 Jan. 93	35	0.84	2.04	0.297	0.326	- 9
Cruise 3 Jan. 23-Feb. 93	32	0.82	2.43	0.255	0.236	8

4. - Conclusions

Independent studies (Heymsfield, 1996; McGhaughey and Zipser, 1996; Ebert, 1996) show that the measurements made by multichannel dual-polarization microwave radiometers do not contain sufficient information to retrieve accurate rain rates on a scale comparable to the radiometer field of view. This is mainly because the passive microwave radiometric data have poor sensitivity to rain drops and are contaminated by scattering and emission from other hydrometeors (Smith and Mugnai, 1992). These limitations led us to attempt to retrieve rain rate from microwave radiometric data with an empirical method on a larger scale, such as the scale of MCS events.

We have developed an algorithm that can give mesoscale rain rate over ocean with a correlation coefficient of about 0.85 with respect to the radar data, and also a quantitative estimate of the monthly rainfall. In this method, variation in the rain area produced by the variations in the atmospheric dynamics on a time scale of about a month is factored out in an empirical fashion. This helps to minimize any systematic bias in the estimated monthly-mean rain rate. It is necessary to tune this retrieval method on a monthly basis with the help of the radar data. Backscatter measurements made by a radar operating in the centimeter wavelength range, are more specific to rain drops.

The radiometer rain retrieval method presented here can be used for the TRMM data. In the TRMM mission, satellite-borne radar observations are limited to a narrow swath of 220 km, while the microwave radiometer swath is 760 km wide (Simpson *et al.*, 1996). The radar data overlap with about 30% of the area covered by the radiometer, and this can be used to tune the microwave radiometer rain retrieval method, geographically and seasonally. The radiometer rain retrievals can be used to fill gaps, in space and time, in the radar data and improve spatial and temporal coverage.

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