

Goel, Himanshu and Ling, Sanliang and Ellis, Breanna Nicole and Taconi, Anna and Slater, Ben and Rai, Neeraj (2018) Predicting vapor liquid equilibria using density functional theory: a case study of argon. Journal of Chemical Physics, 148 (22). 224501/1-224501/10. ISSN 1089-7690

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Publishiftge dicting Vapor Liquid Equilibria using Density Functional Theory; A Case Study of Argon

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(Dated: 22 May 2018)



Predicting vapor liquid equilibria (VLE) of molecules governed by weak van der Waals (vdW) interactions using first principles approach is a significant challenge. Due to the poor scaling of post Hartree-Fock wave function theory with system size/basis functions, Kohn-Sham density functional theory (KS-DFT) is preferred for systems with a large number of molecules. However, traditional DFT cannot adequately account for medium to long range correlations which are necessary for modeling vdW interactions. Recent developments in DFT such as dispersion corrected models and nonlocal van der Waals functionals have attempted to address this weakness with varying degree of success. In this work, we predict the VLE of argon and assess the performance of several density functionals and second order Møller-Plesset perturbation theory (MP2) by determining critical and structural properties via first principles Monte Carlo (FPMC) simulations. PBE-D3, BLYP-D3, and rVV10 functionals were used to compute vapor liquid coexistence curves (VLCCs), while PBE0-D3, M062X-D3, and MP2 were used for computing liquid density at a single state point. The performance of PBE-D3 functional for VLE is superior to other functionals (BLYP-D3 and rVV10). For single state point calculations, MP2 performs well for the density and structural features of the first solvation shell in the liquid phase.

Keywords: Density functional theory, Vapor liquid equilibria, Dispersion interactions, First principles Monte Carlo, Liquid structure



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## Publishing INTRODUCTION

The knowledge of thermophysical properties such as vapor liquid equilibria (VLE) is critical for design and development of numerous separation processes. The classical empirical potentials are often parametrized against experimental data for computing thermophysical properties at ambient or subcritical state points.<sup>1–5</sup> The performance of these force fields becomes unreliable when considering properties or state points not included in parametrization. There is also significant emphasis on developing ab initio interatomic potential by using quantum chemical calculations and using it to predict bulk phase properties.<sup>6–25</sup> The potential energy surface for a large number of configurations is generated to fit to the functional form of the force field. This approach is, however, limited to moderately sized molecules with limited conformational degrees of freedom as the computational cost increases significantly with the complexity of the molecule.

Rapid advances in computational resources and efficient algorithms have contributed immensely to the development and application of electronic structure calculations. This expands the capacity to simulate bigger system size, model complex molecules by significantly reducing computational time. Recent density functionals (DF) and post Hartree-Fock (HF) wave function theory can model small molecules with reasonable accuracy. However, modeling condensed phase systems, in particular, multi-phase phenomena such as vapor liquid equilibria, remains a significant challenge. The popular Kohn-Sham density functional theory (KS-DFT)<sup>26,27</sup> is widely used in material science for modeling condensed phase properties. One of the biggest challenges for KS-DFT is to accurately account for weak non covalent interactions.<sup>28-30</sup> Advances in the DFT are largely based on improving the performance of exchange-correlation (XC) functionals by incorporating additional information of the electronic system. Perdew et al.<sup>31</sup> explain the construction of XC functionals through "Jacob's ladder" where different rungs were classified based on the density functional approximations to define XC energies. As of now, there are five rungs starting from local density approximation (LDA),<sup>32,33</sup> generalized gradient approximation (GGA),<sup>34-37</sup> meta-GGA,<sup>38-42</sup> hybrid functionals,<sup>43–47</sup> and random phase approximation (RPA).<sup>48–51</sup> As one climbs higher steps in the ladder, it leads to greater accuracy albeit at higher computational cost. Additional details regarding hierarchy of DF methods can be accessed through the work of Perdew and co-workers.<sup>31,52–54</sup>



Publishing Ver the last two decades or so, many improvements in DFT have been through the addition of dispersion correction terms to the XC energies. A concept similar to "Jacob's ladder" was introduced by Klimeš and Michaelides<sup>29</sup> to classify different DFT based dispersion correction schemes. Going higher on the ladder leads us to greater accuracy, less empiricism, and higher computational cost. At present, the pair-wise additive dispersion correction models<sup>28,55–57</sup> and nonlocal van der Waals (vdW) functionals<sup>58–61</sup> have demonstrated some success in handling weak vdW interactions. These models are usually benchmarked against data sets of dimer energetics and their performance in estimating bulk phase properties precisely is still a concern.

This work is aimed at obtaining vapor liquid coexistence curves (VLCCs), critical properties, and structural properties for argon via first principles Monte Carlo (FPMC) simulations, and assess the performance of several density functionals (GGA, hybrid, and rVV10 nonlocal vdW functionals) along with second order Møller-Plesset perturbation theory (MP2). Being an important noble gas, argon has been studied extensively for establishing benchmarks. Earlier VLE works with FPMC simulations were performed on water,<sup>62–64</sup> methane,<sup>65</sup> methanol,<sup>65</sup> hydrofluorocarbons,<sup>66,67</sup> carbon dioxide,<sup>68</sup> and sulfur dioxide.<sup>68</sup> For argon, the work carried out by Maerzke et al.<sup>69</sup> presents several key results including dimer potential energy curves and liquid structure by using self-consistent polarization density functional theory. However, their bulk phase calculation was limited to single temperature (85 K) tested with BLYP functional. Given the significance of argon as a prototypical system governed by dispersion interactions, it is useful to determine VLE directly from first principles, and examine performance of several density functionals. In the past, most of the studies were performed by using GGA class of functionals and the accuracy of higher rung functionals are rarely tested. With the relatively low cost of GGA functionals, they are still very popular and widely used with reasonable accuracy. However, researchers are moving towards hybrid density functionals and electron correlation methods such as RPA, and MP2, to predict bulk phase properties with greater accuracy as compared to GGA functionals.<sup>70–84</sup>

The rest of the paper is organized as follows. The next section describes the details of density functionals, simulation set up, dispersion models, and Monte Carlo method. In Section III, we present potential energy curves, second virial coefficients, and results obtained from Monte Carlo simulations. The results comprise of VLCCs, Clausius-Clapeyron plots,<sup>85</sup> critical properties, and structural investigation of the liquid phase argon. At last, concluding Publishing arks are presented in Section IV.

#### II. COMPUTATIONAL METHODS

In this work, two sets of simulations were performed. First, we calculate the vapor liquid coexistence curves of argon which involves two thermodynamically connected simulation boxes for computing saturated liquid and vapor densities at different temperatures. Second, using NpT ensemble the density is computed at a single temperature. First set of calculations were performed by using the PBE<sup>37</sup>, BLYP<sup>35,36</sup> GGA functionals and rVV10<sup>86</sup> nonlocal van der Waals functional. The GGA functionals particularly PBE and BLYP are well known, and were extensively used due to reasonable accuracy and modest computational cost. Nonlocal functionals add a nonlocal correlation energy term to the local or semilocal functional, which results increased computational cost to some degree but improves performance. We have used the rVV10,<sup>86</sup> functional which is a revised version of the VV10,<sup>87</sup> functional. The rVV10 functional is chosen because it is one of the best-performing nonlocal correlation functionals for accurate predictions of the equilibrium bond length and interaction energy of argon dimer, and the equilibrium lattice constant and cohesive energy of argon solid.<sup>88</sup> The second set or single temperature calculations were carried out using PBE0,<sup>45,89</sup> M062X,<sup>47</sup> and the second-order Møller-Plesset perturbation theory (MP2).<sup>90–94</sup> We could do these calculations only at a single temperature due to extremely high computational cost. In order to consider the long range dispersion interactions, we have used dispersion correction DFT-D3<sup>57</sup> developed by Grimme and co-workers. The DFT-D3 method is used with PBE, BLYP, PBE0 and M062X functionals, respectively. In order to determine the VLCCs for argon, we have used the canonical version of Gibbs ensemble Monte Carlo (GEMC) method<sup>95</sup> and the  $NpT^{96}$  ensemble was employed to calculate liquid density at a specified temperature and pressure. The GEMC simulation set up utilizes two separate periodic simulation boxes for representing liquid and vapor phases connected thermodynamically via a unified partition function.<sup>97</sup> For GEMC simulation, total number of molecules, total volume of both boxes, and temperature of the system are kept constant. The Monte Carlo simulation contains various trial moves to sample the configurational space. These moves include translation and changes in the volume of the simulation box for NpT simulations. In addition, the swap moves between liquid and vapor boxes were also performed for GEMC simulation to equi-



Publishing ate the chemical potential. The probabilities of volume, swap, and translational move types are 15-20, 20-25, and 60 %, respectively, and the acceptance rate of the moves ranges from 50 to 60 %. Most of the simulations were carried out using with triple-zeta valence basis set augmented with polarization functions (TZV2P) and Godecker-Teter-Hutter (GTH) pseudopotentials.<sup>98,99</sup> For dispersion corrected hybrid functionals (PBE0-D3, M062X-D3), the auxiliary density matrix method (ADMM) with pFIT3 auxiliary basis were employed.<sup>76</sup> The ADMM method benefit is to reduce the computational cost by considering a smaller auxiliary basis for nonlocal Hartree-Fock exchange (HFX) calculations. For MP2 simulation, we used the Gaussian and plane wave MP2 approach with the resolution of identity (RI) approximation<sup>100,101</sup> which was recently implemented in the CP2K code. Triple-zeta quality valence-only correlation consistent type primary basis set and associated auxiliary RI basis set (see the Supplementary Material) were generated and used for the RI-GPW-MP2 calculation. The procedure for generating these basis sets have been discussed in the work of Del Ben et al.,<sup>101</sup> and we refer the interested reader to the original reference for more information. The truncation radius for Coulomb interaction was set to 7 Å for hybrid DFT and MP2 calculations. All computational details such as XC functionals, GTH pseudopotentials, and their plane wave cutoff are explicitly provided in the Supplementary Material. All MC simulations presented in this work have used CP2K software suite (version 2.6.2 and 5.0).<sup>102</sup> CP2K software suite uses KS-DFT to compute interaction energies via Quickstep module<sup>103</sup> employing a hybrid scheme of Gaussian and Plane Wave (GPW) method.

First principles MC simulations require large computational resources. This computational cost can be considerably reduced by using approximate bias potentials to sample the configurational space.<sup>104–107</sup> In this scheme, the configurational space is first sampled by approximate bias potentials for a short sequence of moves followed by DFT calculation. The energy difference between DFT and the approximate bias potential is used to compute acceptance criteria to either accept or reject the entire (short) sequence of moves. We have used 16 moves for the short sequence using approximate bias potentials.<sup>62</sup> The nonbonded interaction parameters for the approximate bias potential are taken from Michels work.<sup>108</sup> All GEMC/NpT simulations (except MP2) were run 500-600 MC cycles. Each cycle refers to N (total number of molecules) moves with Quickstep energy calculations. The first 250-300 cycles were considered to be the equilibration, and the remaining cycles were considered for data collection. The production run was divided into blocks of 50 cycles to calculate the





FIG. 1. Effect of system size (N) on the liquid density of Ar at 85 K and 1 bar. The error bars smaller than symbol size are not shown.

average and standard deviations for saturated liquid and vapor densities. For MP2 simulation, we performed four independent runs by using different seed and probability ratios. Each independent simulations consisted of 175 MC cycles. The first 100 MC cycles were considered as equilibration and the remaining 75 cycles from each independent run were used to calculate average density and corresponding standard deviation. The approximate bias parameters and the numerical values for VLCCs can be found in the Supplementary Material. The critical temperature and critical density of argon for different functional are also calculated by using subcritical VLCC data. For this purpose, the density scaling law with critical exponent 0.325 and the law of rectilinear diameter were used.<sup>109–111</sup> Additionally, the normal boiling point was calculated by fitting vapor pressure data to Clausius-Clapeyron equation.

We performed GEMC calculations with PBE-D3 functional in order to choose an appropriate system size (number of molecules) for this study. The system size considered are 36, 54, 64, 72, 128, and 256 argon atoms. Figure 1 shows the plot for the saturated liquid density of argon as a function of system size. It is evident from the figure that the density converges to large system size limit after 54 particles. There is a somewhat larger standard deviation for the density obtained from 54 particle simulation. The density obtained from the system size of 64 or 72 argon atoms are reliable and appear suitable for the simulation study. Thus, we have used 72 argon atoms for the GGA and hybrid functional (PBE0-D3 and M062X-D3) calculations and 64 particles for MP2 simulations. We have used smaller



Publishing: em size for MP2 simulations because of the significant computational cost associated with the larger simulation cell. We note the MP2 method has recently been applied to study liquid water, and excellent agreements have been obtained with the experiment on water density and radial distribution functions.<sup>71</sup> The initial system set up procedure can be referred from our previous work.<sup>66</sup> The structural analysis for the liquid phase of argon was determined through radial distribution functions (RDF) plots.

As two-body interaction term contributes most to the total potential energy of the *n*body system, it can be helpful to assess the performance of various functional for dimer energetics. The potential energy curves (PECs) can provide an insight into the accuracy of bulk phase property prediction. The argon PECs through different functionals are compared at coupled cluster single, double, and perturbative triple excitations  $(CCSD(T))^{112-117}$  level of theory with extrapolation to the complete basis set (CBS) limit.<sup>7</sup> Most of the GPW dimer calculations and VLCCs curves in this work have been performed using the TZV2P basis set, which was found to converge well for the equilibrium bond length and interaction energy of argon dimer. Therefore, it is also beneficial to obtain the PECs from the CCSD(T) using triple zeta basis set. For this purpose, we carried out argon dimer calculation to obtain the PECs from CCSD(T)/aug cc-pVTZ(aVTZ) basis set.<sup>118,119</sup> We have used Boys and Bernardi counterpoise correction<sup>120</sup> for removing the basis set superposition error. The CCSD(T)/aVTZ calculations for potential energy curve were performed by using Gaussian 09 software.<sup>121</sup>

The potential energy curve between two argon atoms can be used to compute the second virial coefficient using the following equation:

$$B_2(T) = -2\pi \int_0^\infty (e^{-U(r)/(k_{\rm B}T)} - 1)r^2 dr$$
(1)

where U(r),  $k_{\rm B}$ , and T represents the dimer potential at separation r, Boltzmann constant, and temperature, respectively. To compute  $B_2(T)$ , we have followed the approached used by Maerzke et al.<sup>69</sup> However, we did not include the quantum corrections to the virial coefficients as they appear to be less than 1 %.<sup>69</sup> In brief,  $B_2(T)$  was determined by using trapezoidal numerical integration in the range of r = 0 - 50.0 Å. The energies were set to a large positive number in the region of r = 0 - 2.0 Å, which results in Mayer function to be -1. For every functional, we have computed the dimer potential energy for r = 2.0-7.0 Å and the local cubic splines were used to interpolate the energies in this region. The po-



**Publishing** ial energies obtained over the region r = 6.25 - 7.0 Å were used to fit the functional form  $-C_6r^{-6}$ . Thereafter, the value for  $C_6$  coefficient were used to extrapolate the potential energies from 7.0 to 50.0 Å.

#### III. RESULTS AND DISCUSSION

#### A. Dimer Energetics

The leading contribution to the total energy for an *n*-body system is from two-body terms. Thus, dimer potential energy curves (PECs) can be a good indicator for the performance of different level of theory for predicting condensed phase thermodynamic properties. Figure 2 shows the PECs of argon with different class of functionals and MP2. The location of the minima and the interaction energy are also listed in Table I. The curve obtained from CCSD(T)/aug-cc-pVTZ(aVTZ) basis set overestimates the equilibrium bond length and underestimates the binding energy when compared with CCSD(T)/CBS or the experiment.

For GGA functionals (PBE and BLYP with dispersion correction D3), the equilibrium bond lengths from both functionals are overestimated by approximately 0.1 Å in comparison with the experiment. The binding energy is largely underestimated for BLYP-D3 and overestimated by PBE-D3 functional compared to the experimental values. This binding energy difference for the BLYP-D3/PBE-D3 functionals can have significant consequences on the nature of VLCCs (see below). In the case with hybrid functionals, the PBE0-D3 functional overestimated the bond length marginally with a difference of 0.09 Å as compared to experiment or CCSD(T)/CBS. The PBE0-D3 functional binding energy at the equilibrium distance is close enough to the experiment or CCSD(T)/CBS, but it fails to carry the similar performance in the long range interaction region where it is more attractive than CCSD(T)/CBS. The M062X functional is based on hybrid meta exchange-correlation functionals and account for short to medium range correlation. The M062X-D3 functional completely fails to determine the equilibrium bond length and it overestimated the value by 0.40 Å. Furthermore, the binding energy obtained from M062X-D3 functional underestimates the experiment well depth.

For the nonlocal functional rVV10, we can see that the calculated equilibrium bond length and the binding energy is in good agreement with the experimental data. The PEC obtained



**iblishing** TABLE I. The location of well depth  $(R_0, \text{ Å})$  and interaction energy  $(E_{int}, \text{ kJ/mol})$  of argon at the minima in the dimer potential energy curve for different functional/potential compared with CCSD(T) and experimental work.

Functional	$R_0$	$-E_{ m int}$
PBE-D3/GPW	3.87	1.412
BLYP-D3/GPW	3.85	0.690
m rVV10/GPW	3.77	1.210
PBE0-D3/GPW	3.85	1.155
M062X-D3/GPW	4.10	0.780
MP2/GPW	3.90	0.759
MP2/aVTZ	3.85	1.014
LJ (Vrabec et al. <sup>23</sup> )	3.81	0.969
LJ (Michels et al. $^{108}$ )	3.82	0.994
CCSD(T)/aVTZ	3.89	0.853
$CCSD(T)/CBS^7$	3.767	1.187
$Experiment^{122}$	3.761	1.188
aug-cc-pVTZ (aVTZ)		
complete basis se	et	
(CBS)		
Gaussian plane way	ve	
(GPW)		
Ŧ		

from rVV10 functional matches well with the CCSD(T)/CBS curve until 4 Å. However, the rVV10 PEC does not provide similar accuracy as the distance between particles increase beyond 4 Å. After 4 Å, the interaction energy is slightly underestimated when compared to the CCSD(T)/CBS curve. In addition, the argon PEC with rVV10 functional is in good agreement with the reference curve as shown in the work of Sabatini et al.<sup>86</sup> and Tran and Hutter.<sup>88</sup> Next, the MP2 method well known for accounting electron correlation is computationally efficient as compared to coupled cluster and configuration interaction methods. The results obtained from the MP2/GPW and MP2/aVTZ show the binding energy difference of around 0.25 kJ/mol. Compared to the experimental data, both underestimate the binding



Publishing: gy and overestimate the equilibrium bond length. In summary, the rVV10 functional is the best functional for dimer energetics, which is consistent with our earlier published works on hydrofluorocarbons as well.<sup>66,68</sup> According to the work of Tran and Hutter,<sup>88</sup> the rVV10 functional also perform well as compared to other tested DFT functionals in case of rare gas dimers. After rVV10 functional, the PBE0-D3 functional also does a decent job for equilibrium bond length and binding energy as compared to the experiment/CCSD(T)/CBS. The effective LJ pair potentials developed by Michels et al.<sup>108</sup> and Vrabec et al.<sup>23</sup> underestimate the potential well depth by approximately 16 and 18 %, respectively. Since, the LJ potential by Vrabec et al.<sup>23</sup> can provide an extremely good prediction for vapor liquid coexistence curve, it suggests that many-body polarization effects are repulsive in nature.

### B. Second Virial Coefficients

The second virial coefficients for argon with different functionals and LJ potential<sup>23</sup> are shown in Figure 3 and compared with the experimental<sup>123</sup> and CCSD(T)/CBS<sup>7</sup> date over the range of 100-1000 K. The numerical values for second virial coefficients are also provided in the Table S6 of the Supplementary Material. Among all the functionals and the LJ potential<sup>23</sup> used here, the best performance are shown by the PBE0-D3 and rVV10 nonlocal functional. At lower temperatures (100 to 200 K), the unsigned mean percentage error are 7.5 % and 8.0 % for PBE0-D3 and rVV10 functional as compared to the experimental data. Moreover, the predictions for second virial coefficients at higher temperatures are also in good agreement with experimental data. The next closest results are provided by the LJ potential.<sup>23</sup> For other functionals, the PBE-D3 functional significantly overestimate while BLYP-D3, MP2, and M062X-D3 significantly underestimate  $B_2(T)$ .

### Liquid Density and Structure

The performance of GGA (PBE-D3 and BLYP-D3), rVV10, hybrid (PBE0-D3, M062X-D3), and MP2 method are compared by predicting liquid densities for argon at 85 K and 1 bar. Table II lists down the computed densities for different functionals and MP2. The accuracy of the functionals in predicting density are in this order: MP2>M062X-D3>PBE0-D3>BLYP-D3>PBE-D3>rVV10. Clearly, the MP2 method provides the best estimate of



**Publishing** LE II. Liquid density of argon at T = 85 K and P = 1 bar with different functionals and LJ potential. Experimental data are taken from the NIST chemistry webbook.<sup>124</sup>

Functional	$\rho~({\rm g/cm^3})$	St. dev.	% Error
PBE-D3 (at $85 \text{ K}$ )	1.238	0.014	-12.14
BLYP-D3 (at 85 K) $$	1.268	0.016	-10.0
rVV10 (at 85 K) $$	1.621	0.006	15.04
PBE0-D3 (at 85 K)	1.527	0.010	8.37
M062X-D3 (at 85 K)	1.377	0.016	-2.27
MP2 (at 85 K)	1.440	0.014	2.20
LJ (Vrabec et al. <sup>23</sup> )	1.407	0.002	-0.15
Expt. (at 85 K) <sup>124</sup>	1.409	$\sim$	

density with a 2.2% error. From the  $B_2(T)$  values for MP2, one could not have come to the conclusion that MP2 would be able to provide such a good estimate for the liquid density. It appears as the system size increases, MP2 overestimates many-body polarization effects leading to cancellation of errors. The only constraint in doing MP2 calculations for the condensed phase is the need for substantial computational resources. The second best estimate comes from the M062X-D3 functional with an underprediction of 2.3%. We could also test the accuracy of M062X-D3 functional at a slightly higher temperature (105 K) and the computed density is underpredicted by approximately 6.5%. The M062X-D3 does a decent job in computing density in spite of poor performance for well depth location. The performance of another hybrid functional PBE0-D3 is somewhat reasonable for density and PEC of argon. The computed density is overpredicted by 8.4%. The density obtained from BLYP-D3 and PBE-D3 functionals are underestimated by 10 and 12%, respectively. At 85 K, both functionals show similar accuracy for liquid density in spite of the large difference in binding energy, suggesting that at lower temperatures location of the minima in PEC is more important than the binding energy. As described above, the difference of binding energy mainly affects the bulk phase properties at higher reduced temperatures.

The structural features of the liquid phase of argon are explored through analyzing radial distribution function. Figure 4 shows the RDF plots with different functionals at 85 K and its characteristics (location of the first coordination shell and height of the peak) are



blishing LE III. Characteristics (location and height of the first solvation peak) of liquid phase radial distribution function for argon with different functionals and LJ potential.

Functional	r (Å)	g(r)
PBE-D3	3.86	2.808
BLYP-D3	3.74	3.174
rVV10	3.66	3.784
PBE0-D3	3.70	3.395
M062X-D3	3.70	2.632
MP2	3.66	2.982
LJ (Vrabec e	t 3.67	2.943
$al.^{23}$ )		2
$Experiment^{125}$	3.68	3.050
		/

provided in Table III. The experimental RDF is taken from Yarnell et al.<sup>125</sup> Except for PBE-D3 and BLYP-D3, most of the other functionals perform reasonably well in predicting the location of the first coordination shell. The PBE-D3 and BLYP-D3 functionals somewhat overestimate the location of the peak, 3.86 and 3.74 Å, respectively, as compared to the experimental value of 3.68 Å. This is also consistent with the fact that liquid density is underestimated for these functionals. The peak height with PBE0-D3 and rVV10 functional are considerably higher as compared to other functionals and this is largely due to higher densities predicted with both of these functionals. The peak height obtained from M062X-D3 functional is slightly smaller despite a reasonable density prediction. The liquid structure obtained from MP2 based MC simulations is in excellent agreement with experimental data. This is somewhat expected since density obtained with MP2 energetics is also very close to experimental liquid density. The location and the height of the first solvation peak for LJ pair potential is also in good agreement with the experimental data (see Table III).

## D. Vapor Liquid Phase Equilibria

The VLCCs for argon obtained from GEMC simulations are shown in Figure 5. This figure compares the performance of three different functionals (PBE-D3, BLYP-D3 and



Publishing 10) against the experimental data. The overall saturated liquid densities obtained from PBE-D3 and BLYP-D3 functionals are underestimated by 8.5 % and 10 %, respectively. Clearly, PBE-D3 functional's performance is superior to BLYP-D3 functional. Nonetheless, both GGA functionals fail to mimic the slope of saturated liquid and vapor lines. At higher temperatures, the BLYP-D3 functional gives larger error as compared to lower temperatures, whereas for the PBE-D3 functional agreement with experimental data improves with the increase in temperature. The results obtained from both these functionals show the underestimation of dispersion interactions. In the case of rVV10 functional, the overprediction for saturated liquid densities is nearly 23 %. The complete curve shows consistent overprediction of the saturated liquid densities and underprediction of the saturated vapor densities. In other words, the dispersion interactions are largely overestimated.

Next, we have used saturated vapor densities to compute the saturated vapor pressures via ideal gas law. This is an approximation which holds well at lower vapor densities. In Figure 6, the Clausius-Clapeyron plots compares the saturated vapor pressures obtained from PBE-D3, BLYP-D3 and rVV10 functionals for argon. The BLYP-D3 functional over predicts the saturated vapor pressures as compared to the experimental data and this is largely due to the higher vapor densities from the VLCCs curve. The saturated vapor pressure curves from PBE-D3 functional shows moderate underprediction for all the state points considered in this study. In the case of rVV10 functional, the saturated vapor pressure curve shows underprediction with larger standard deviation, especially at the lower temperatures. The underprediction of saturated vapor pressure for PBE-D3 and rVV10 functionals is directly associated with the underprediction of saturated vapor densities.

The subcritical VLE data can be used to estimate the critical properties of any compound. The predicted critical temperature  $(T_{\rm C})$ , critical densities  $(\rho_{\rm C})$ , and normal boiling points  $(T_{\rm B})$  are presented in Table IV. The critical temperature for argon is over estimated by 15.2% and 27.8% with the PBE-D3 and rVV10 functionals, respectively. The high error for rVV10 functional is due to the overprediction of saturated liquid densities and underprediction of saturated vapor densities. For PBE-D3, it still performs reasonably well for saturated liquid densities but underprediction of saturated vapor densities takes the critical temperature to the higher value. The critical temperature for argon with BLYP-D3 functional is underestimated by 24%, and this is mainly because of incorrect curvature of the saturated liquid and vapor densities curves. The normal boiling point is obtained by



Publishing LE IV. Critical temperature  $(T_{\rm C})$ , critical density  $(\rho_{\rm C})$ , and normal boiling point  $(T_{\rm B})$  for argon obtained from Monte Carlo simulations. Experimental data are taken from the NIST chemistry webbook.<sup>124</sup> The numbers in the parenthesis are the standard deviations.

Functional	$T_{\rm C}({\rm K})$	$\rho_{\rm C}~({\rm g/cm^3})$	$T_{\rm B}({\rm K})$		
PBE-D3	173.6(4)	0.439(0.03)	102(2)		
BLYP-D3	114.8(8)	0.534(0.10)	67(5)		
rVV10	192.7(5)	0.612(0.04)	105(3)		
LJ (Vrabec et al. <sup>23</sup> )	152.0(1)	0.522(0.005)	87(1)		
$Experiment^{124}$	150.69	0.535	87.5		

using the Clausius-Clapeyron equation. The PBE-D3 and rVV10 functionals overestimate boiling point by 17% and 20%, respectively, whereas the BLYP-D3 functional underpredict by 24%. LJ potential,<sup>23</sup> on the other hand, accurately predicts these thermodynamic properties, which is not surprising give these are parameterized to predict bulk thermodynamic properties.

The VLCCs obtained from different functionals can also be directly related to the dimer PECs for argon. As mentioned above, both functionals (BLYP-D3 and PBE-D3) give very similar results for the location of the well depth but the difference for the binding energy is approximately 0.7 kJ/mol. The underestimation of binding for BLYP-D3 leads to lower saturated liquid densities and higher saturated vapor densities, and this behavior ultimately leads to a lower critical temperature. With PBE-D3 functional, the prediction for saturated liquid densities at lower reduced temperatures  $(T_r = T/T_c)$  are similar to BLYP-D3, but agreement improves at higher reduced temperatures. This is largely due to the difference in binding energy between the functionals. The higher binding energy prediction with PBE-D3 leads to having higher critical temperature as compared to the prediction from BLYP-D3. The rVV10 functional does not reproduce the actual VLCC behavior in spite of PEC that matches well the experiment and CCSD(T)/CBS data for separation less than 4 Å. The overprediction for saturated liquid densities is possibly due to overbinding at larger separations. Therefore, at present, the rVV10 functional is evidently one of the best option to determine accurate geometries for dimer energetics, but it is not sufficiently reliable for computing liquid phase properties of the system. In summary, the PBE functional with D3



Publishidigpersion correction model is a good choice to model vapor liquid equilibria for argon when compared with BLYP-D3 and rVV10 functionals.

# IV. CONCLUSIONS

Vapor liquid equilibria along with liquid density and liquid microstructure of argon are predicted using first principles Gibbs ensemble Monte Carlo simulations. Among different theoretical models considered in the present work, MP2 performs extremely well for liquid and the structure of first solvation shell albeit at a significantly higher computational cost compared to density functional methods. The rVV10 nonlocal van der Waals functional performs well for PEC and second virial coefficients, but overpredicts saturated liquid densities indicating many body polarization effects are overestimated. The performance of dispersion corrected hybrid functionals (PBE0-D3 and M062X-D3) is not as good as MP2 for the densities and location of first coordination shell. At last, PBE-D3 performs reasonably well for VLE as compared to BLYP-D3 and rVV10. Overall, our work indicates that MP2/GPW approach is most suitable for predicting condensed phase properties of systems governed by dispersion interactions.

# SUPPLEMENTARY MATERIAL

See Supplementary Material for bias potential parameters, energy cutoff for different simulations, plot for density versus Monte Carlo steps, numerical data used for VLE and Clausius-Clapeyron plots, dimer PEC, second virial coefficients, and basis sets used for RI-MP2 calculations.

# ACKNOWLEDGMENTS

This work is funded by the National Science Foundation (NSF) under grant number CHE - 1265872. S.L. and B.S. were supported by EPSRC (EP/K039296/1 and EP/K038400/1). This research used resources of the National Energy Research Scientific Computing Center, a DOE Office of Science User Facility supported by the Office of Science of the U.S. Department of Energy under contract number No. DE-AC02-05CH11231. This work used the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by National



Publishingence Foundation grant number ACI-1548562. The authors also acknowledge the Texas Advanced Computing Center (TACC) at The University of Texas at Austin for providing HPC resources (Stampede) that have contributed to the research results reported within this paper through XSEDE allocation CHE140141. At last, computational resources at High Performance Computing Collaboratory at Mississippi State University were used for this project.

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FIG. 2. Potential energy curves of argon at different levels of theory. The black stars, red squares, violet triangle up, blue triangle left, magenta triangle down, maroon cross, orange triangle right, turquoise diamonds, green circles, maroon circles and blue triangle down represent data for CCSD(T)/CBS,<sup>7</sup> CCSD(T)/aVTZ (aug-cc-pVTZ), BLYP-D3/GPW, PBE-D3/GPW, PBE0-D3/GPW, rVV10/GPW, M062X-D3/GPW, MP2/GPW, MP2/aVTZ, LJ (Michels et al.)<sup>108</sup> and LJ (Vrabec et al.)<sup>23</sup> potential, respectively. The dashed lines of the corresponding color are guide to the eye.





FIG. 3. Temperature dependance of the second virial coefficient of argon. The black stars, magenta plus, red diamonds, maroon squares, turquoise triangle down, green triangle left, orange triangle right, violet triangle up, and blue circles represent data for experiment,<sup>123</sup> CCSD(T)/CBS,<sup>7</sup> BLYP-D3/GPW, PBE-D3/GPW, PBE0-D3/GPW, rVV10/GPW, M062X-D3/GPW, MP2/GPW, and LJ (Vrabec et al.)<sup>23</sup> potential, respectively. The dashed lines of the corresponding color are guide to the eye.





FIG. 4. Liquid phase radial distribution functions for argon at 85 K. The dash-dotted red, dashed green, and dotted orange color lines represent results obtained with BLYP-D3, PBE- D3, and PBE0-D3, respectively. The solid violet, dashed maroon, dotted blue and dashed magenta color lines represent results obtained with MP2, M062X-D3, rVV10, and LJ (Vrabec et al.<sup>23</sup>) potential, respectively (y-axis is scaled with +2). The solid black line denotes the experimental data taken from Yarnell et al.<sup>125</sup> A bin width of 0.04 Å is used for all RDF plots.







FIG. 5. Vapor-liquid coexistence curves (VLCCs) for argon with different functionals and LJ potential. The solid black lines depict the experimental data and the star represents the experimental critical point.<sup>124</sup> The red diamonds, violet squares, green circles, and magenta plus represent GEMC simulation data with BLYP-D3, PBE-D3, rVV10 and LJ (Vrabec et al.<sup>23</sup>) potential, respectively. The error bars smaller than symbol size are not shown.





FIG. 6. Clausius-Clapeyron plots for argon with different functionals and LJ potential. The solid black lines depict the experimental data.<sup>124</sup> The red diamonds, violet squares, green circles, and magenta plus represent GEMC simulation data with BLYP-D3, PBE-D3, rVV10 and LJ (Vrabec et al.<sup>23</sup>) potential, respectively. The error bars smaller than symbol size are not shown. The dashed lines show a linear fit of the simulation data.











