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Abstract

We previously reported various solid solution systems that demonstrated the stabilized antiferroelectric (P) phases in NaNbO 3 through lowering the tolerance factor. However, all those reported modifications were achieved by adding A 2+ B 4+ O 3 type solid solutions. A lead-free antiferroelectric (AFE) solid solution xBiScO 3 -(1-x)NaNbO 3 was rationalized by adopting the tolerance factor design rule. Specifically, adding BiScO 3 was found to effectively stabilize the AFE phase without changing the crystal symmetry of NaNbO 3. Microstructure and electron zone axis diffraction patterns from transmission electron microscopy revealed the stabilized AFE (P) phase in this solid solution. Besides, the electric-field-induced polarization with a double-hysteresis loop was observed. The present results pointed out that the strategy could also be applied while adding A 3+ B 3+ O 3 type solid solutions. In addition, it expanded the compositional design that can be applied to antiferroelectric materials.

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Stabilized antiferroelectricity in xBiScO₃-(1-x)NaNbO₃ lead-free ceramics with established double hysteresis loops

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We previously reported various solid solution systems that demonstrated the stabilized antiferroelectric (P) phases in NaNbO₃ through lowering the tolerance factor. However, all those reported modifications were achieved by adding $A^{2+}B^{4+}O_3$ type solid solutions. A lead-free antiferroelectric (AFE) solid solution xBiScO₃-(1-x)NaNbO₃ was rationalized by adopting the tolerance factor design rule. Specifically, adding BiScO₃ was found to effectively stabilize the AFE phase without changing the crystal symmetry of NaNbO₃. Microstructure and electron zone axis diffraction patterns from transmission electron microscopy revealed the stabilized AFE (P) phase in this solid solution. Besides, the electric-field-induced polarization with a double-hysteresis loop was observed. The present results pointed out that the strategy could also be applied while adding $A^{3+}B^{3+}O_3$ type solid solutions. In addition, it expanded the compositional design that can be applied to antiferroelectric materials. *Published by AIP Publishing*. https://doi.org/10.1063/1.5017697

In the 1950s, Kittel predicted the existence of antiferroelectricity.¹ In antiferroelectric (AFE) materials, although the ions are spontaneously polarized, the adjacent translational anti-parallel polarizing directions that constitute a superstructure describe the unit cell. Therefore, in an AFE material, there is no macroscopic polarization. PbZrO₃ (PZ) is a well-known AFE material and has been commercialized for capacitor applications.² AFE materials have an increased permittivity under a high electric field (dP/dE > 0), where the field induced AFE-FE phase transition under an electric field boosts the electrostatic energy density.³

Early work by Nicholson and Cross⁴ on NaNbO₃ reported that in single crystals, a double hysteresis could be observed, but later this has become difficult to verify with both crystals and ceramics. NaNbO₃ has an AFE P (space group Pbma) phase at ambient conditions;^{5–9} however, the double hysteresis loops are rarely observed in NaNbO₃ due to the existence of a metastable ferroelectric (FE) Q (space group P2₁ma) phase.^{10–16} It is further noted that a stabilized AFE phase requires a lower tolerance factor (t).^{16–21} The calculation of the Goldschmidt tolerance factor in an ABO₃-type perovskite is shown in Eq. (1), where r_A , r_B , and r_O are the ionic radii of A-site ions, B-site ions, and oxygen ions, respectively.¹⁶ The Shannon-Prewitt ionic radii²² are applied for the twelvefold and sixfold coordination for A and B sites, respectively,

$$t = \frac{r_A + r_O}{\sqrt{2}(r_B + r_O)}.$$
 (1)

It has been experimentally observed that the polar order can be tuned into antipolar order by decreasing the *t*. The lead-free BiFeO₃ is a good example; the polar R3c phase was transformed into a PbZrO₃-like antipolar phase after adding rare earth elements to lower t.^{23–25} It was found that the rule could also be applied to NaNbO₃, and we predicted a broad range of different solid solution compositions that should host the AFE behavior. Recently, our group has demonstrated that AFE behavior could be obtained by adding CaHfO₃,¹⁰ SrZrO₃,¹¹ and CaZrO₃,^{12,15} which can effectively decrease the tolerance factor and then stabilize the AFE phase in NaNbO₃. The observed zone axis electron diffraction patterns and electric field induced signature AFE double hysteresis P-E loops verified the validity for the NaNbO₃ material system. However, these verifications were all based on using the $A^{2+}B^{4+}O_3$ -type end members. In this work, $A^{3+}B^{3+}O_3$ type BiScO₃ will be used as an alternative end member to modify NaNbO₃. X-ray diffraction (XRD) spectra, phase compositions, and electric properties will be evaluated. In addition, regarding the possible feasibility of commercial applications of NaNbO3 based lead-free ceramics, their performance inferiority compared to lead-based materials has to be considered carefully to meet application requirements.

The $xBiScO_3-(1-x)NaNbO_3$ (BSNN-X hereafter. X = 100x) solid solutions were prepared by conventional solid-state reaction. The raw chemicals were Na₂CO₃ (99.95% Alfa Aesar, Ward Hill, MA), Nb₂O₅ (99.9% Alfa Aesar, Ward Hill, MA), Bi₂O₃ (99.5% Alfa Aesar, Ward Hill, MA), and Sc₂O₃ (99.95% Alfa Aesar, Ward Hill, MA). 6 wt. % and 3 wt. % extra Na₂CO₃ and Bi₂O₃ were batched to compensate the volatilization during high-temperature processing, respectively. Na₂CO₃ was weighed and then ball milled in ethanol for 24 h; afterward, Nb₂O₅, Bi₂O₃, and Sc₂O₃ were added and further ball milled for 24 h. Then, the powder was dried at 80°C overnight to remove the ethanol. The batched powder was then calcined at 850 °C for 3 h and then pressed into disk-shaped binder-free pellets. The pellets were sintered at 1350 °C for 45 min. XRD (PANalytical X'pert PRO) was used to examine the crystal phase purity of the sintered ceramics. The microstructure graphs were collected using a transmission electron microscope (TEM) (Philips EM420

microscope) operating at 120 kV. The dielectric constant as a function of temperature was measured via the capacitance of parallel plate samples with known geometric parameters using an LCR meter (HP4284A, Agilent Technologies Inc., Santa Clara, CA) during both heating and cooling. The P-E loop was obtained using a Sawyer-Tower circuit; a sinusoidal field with 0.1 Hz was applied. The critical fields were determined by calculating the polarization current density.

Figure 1 shows the XRD spectra of NaNbO₃, BSNN-1, and BSNN-2; the peaks were indexed using a prototype cubic perovskite structure. As shown in Fig. 1(a), XRD plots of NaNbO₃ and BSNN-1 are presented. It was found that all ceramics are phase pure without noticeable secondary phases. A close analysis of superlattice diffraction spectra at 2θ angles of 36.6° and 55.2° is presented in Fig. 1(b). These peaks at these two positions sequentially correspond to {1 1 ³/₄} and {2 1 ³/₄} AFE superlattice diffraction reflections. The AFE superlattice reflection peaks were observed in the BiScO₃ modified NaNbO₃ as well; it preliminarily implied that the AFE phase was obtained in BSNN.

Further studies on microstructures were carried out by Transmission Electron Microscopy (TEM). Micrographs and the corresponding selected area electron diffraction (SAED)



FIG. 1. X-ray diffraction spectra of (a) NaNbO₃, BSNN-1, and BSNN-2, (b) $\{1 \ 1 \ 3/4\}$ superlattice reflection at 2θ of 36.6°, and (c) $\{2 \ 1 \ 3/4\}$ superlattice reflection at 2θ of 55.2°. The peaks are indexed by the prototype cubic perovskite structure.

patterns are shown in Fig. 2. The AFE P and FE Q phases were distinguished by the B-site Nb ion displacement combining with oxygen octahedral tilting on the b axis of the prototype cubic unit cell.^{5,26} The AFE P phase can be denoted as a layered combination of $a^-b^+a^-$ and $a^-b^-a^$ in Glazer notation, and the FE Q phase is denoted as $a^{-}b^{+}a^{-}a^{-}b^{+}a^{-}$ The unit cell is quadrupled and doubled in P and Q phases along the [001] direction of perovskite unit cells, respectively. Consequentially, these enlarged superstructure unit cells display unique electron diffraction patterns. The P and Q phases show the $1/4{010}$ -type and $1/2{010}$ -type diffraction patterns, respectively.²⁶ Extensive TEM characterizations in our previous studies have clearly demonstrated that both the FE Q phase and the AFE P phase coexist in pure NN in the virgin state, which was suggested by the electron diffraction pattern analysis that the AFE P phase is present as the predominant phase, together with a small portion of the FE Q phase.^{10–12,14} The microstructures of NaNbO₃ are shown again in Figs. 2(a) and 2(b). The crystal was composed of micron-sized domains in all compositions. The electron beams were aligned along the [100] zone axis to identify the AFE/FE nature by SAED. As unambiguously revealed by the electron diffraction pattern, the AFE P phase and the FE Q phase were revealed by the $\frac{1}{4}{010}$ type diffraction spots [Figs. 2(e)-2(g)] and $1/2\{010\}$ superlattice spots [Fig. 2(h)], respectively, revealing the phase heterogeneity in NaNbO3 under ambient conditions. Diffuse scattering streaking along the [010] direction was observed in the SAED pattern of the Q phase, indicating the mesoscale nature of the FE Q phase here.¹⁰⁻¹⁴ As demonstrated in the previous studies, a small amount of dopants ($\leq 6 \mod \%$), e.g., CaZrO₃, SrZrO₃, and CaHfO₃, stabilized the AFE P phase over the FE O phase, hence contributing to the double polarization hysteresis loops during bipolar electrical cycles.¹⁰⁻¹² Similar to the systems mentioned above, BiScO₃ doping in the present study was also found to enhance the antiferroelectric phase of NaNbO₃, as revealed by the TEM micrographs shown in Figs. 2(c), 2(d), and 2(i)-2(k). Micron-sized domains of BSNN-1 are shown in Figs. 2(c) and 2(d), and the SAED patterns are shown in Figs. 2(i)-2(k). The symmetry of the AFE P phase was still preserved after BiScO₃ doping. It was found that only $\frac{1}{4}{010}$ type superlattice spots were observed in BSNN-1, suggesting that the AFE phase was well stabilized in the BiScO₃ modified NaNbO₃. A close look at the SAED pattern of BSNN-1 revealed observable streaking along the [010] direction, which is marked by the rectangle in Fig. 2(k); the streaking could be identified as $1/n\{0k0\}$ superlattice spots. It was believed that the streaking was associated with the incommensurate phase.^{28–30} The formation of the incommensurate AFE phase was observed in Pb-based complex perovskites while changing the tolerance factor, order of B site cations, and the size difference between B-site ions,^{31–33} although it was found that the phase was affected by the degree of chemical order and the difference in B-site ionic radii in these cases. A similar incommensurate phase was also reported in the rareearth element doped BiFeO₃ material system.^{25,34} Viehland et al.³⁵ considered that the formation of the incommensurate phase was a result of competition between the AFE phase and the FE phase, in the case of softening zone center (FE) and zone boundary (AFE) phonon modes. As a result, the



FIG. 2. TEM micrographs and selected area diffraction patterns: (a) and (b) domain structure of NaNbO₃; (e), (f), and (g) $\frac{1}{4}{010}$ type diffractions, showing the AFE P phase in NaNbO₃; (h) $\frac{1}{2}{010}$ type diffraction patterns, showing the FE Q phase in NaNbO₃; (c) and (d) domain structure of BSNN-1; and (i)–(k) $\frac{1}{4}{010}$ type superlattice diffraction in BSNN-1. The index is based on the prototype cubic perovskite structure.

incommensurate phase was the result of the AFE and FE phases being a frustrated state due to their respective competition.³⁴ The arrow in Fig. 2(d) shows dislocations along the grain boundaries.

The dielectric properties of BSNN-1 and BSNN-2 are shown in Fig. 3. Figure 3(a) presents the dielectric constant as a function of temperature. Dielectric anomalies were observed at 273 °C and 234 °C in BSNN-1 and BSNN-2 during cooling, respectively, which could be attributed to the phase transition from the orthorhombic AFE R phase with the Pmnm space group to the orthorhombic AFE P phase with the Pbma space group.^{36,37} Together with some important parameters of previously reported NaNbO₃¹² and xCaHfO₃-(1-x)NaNbO₃ (CHNN-X) in Table I,¹⁰ the Curie-Weiss law was adopted to extract important characteristics describing the phase transition; the details can be found in the previous work.¹⁰ It was found that the phase transition temperatures of both heating and cooling decreased due to the addition of BiScO₃. A thermal hysteresis between heating and cooling processes was observed, consistent with the first order AFE-to-AFE (P-to-R) phase transitions. The ratio between the temperature gap (ΔT) of the hysteresis and the phase transition temperature during cooling (T_2) was calculated. Along with the previously reported data, it was found that this value increased with the lowering tolerance factor. It should be noted that BSNN-2 and CHNN-3 had almost identical tolerance factor values, and when took a further look at the Curie-Weiss temperature and the value of $\Delta T/T_2$, identical values were found for these two compositions, suggesting that the tolerance factor plays the dominated role in stabilizing the AFE phase. These observations are consistent with the theory proposed earlier by Levanyuk et al.^{38,39}



FIG. 3. (a) Dielectric constant as a function of temperature during heating and cooling, showing thermal hysteresis; the dielectric anomalies around 270 °C and 230 °C correspond to the first-order phase transitions from the AFE R phase to the AFE P phase. (b) Dielectric loss as a function of temperature during heating and cooling.

TABLE I. Important parameters of the electric properties of NaNbO₃, CHNN, and BSNN. The parameters were calculated from the low-field and high-field dielectric properties. t, tolerance factor; T_0 , Curie-Weiss temperature; C, Curie-Weiss constant; T_1 , phase transition temperature during heating; T_2 , phase transition temperature during cooling; ΔT , the difference between T_1 and T_2 ; and E_F critical electric field to induce AFE-FE switching.

Compositions	t	$T_0(^{\circ}C)$	$C(1 \times 10^5 \cdot K)$	$T_1(^{\circ}C)$	$T_2 (^{\circ}C)$	$\Delta T (^{\circ}C)$	$\Delta T/T_2$	E _F (kV/cm)
NaNbO ₃ ¹⁰	0.9671	118	5.13	393	331	62	0.187	34
BSNN-1	0.9664	108	3.47	344	273	71	0.260	100
BSNN-2	0.9657	31	3.70	299	225	74	0.329	
CHNN-3 ¹⁰	0.9656	31	4.05	311	234	77	0.329	148
CHNN-4 ¹⁰	0.9649	42	3.27	295	190	105	0.553	164

where displacive phase transitions are sensitive to dopants and defects. It was considered that a small amount of defects can smear the first-order phase transition due to the reduction of the effects from order parameter fluctuations and a decrease in jumps of various thermodynamic quantities. The Curie constant was on the scale of 10^5 K, which further suggested that the first-order phase transition occurred at the transition temperature. BSNN materials followed the trend that was reported previously with $A^{2+}B^{4+}O_3$ modified NaNbO₃.

High field measurements were also carried out and plotted from BSNN-1, and the data were collected from the second cycle. Figure 4 shows the high field P-E loop and electronegativity difference vs. tolerance factor. Figure 4(a) shows the signature AFE double hysteresis loop of BSNN-1 and the current density J, which was calculated through



FIG. 4. (a) Electric field induced polarization double hysteresis loops and current density calculated by dP/dt. (b) X-t plot of NaNbO₃ with CaZrO₃, SrZrO₃, CaHfO₃, and BiScO₃ dopants.

dP/dt. Although the P-E loop was not perfectly shaped and saturated due to the conduction contributions caused by the loss of Bi, it indicated that adding BiScO₃ had the AFE phase stabilized in NaNbO3. Three clear peaks were seen in the current density curve and numbered sequentially. The sharp peak 1 in the first quadrant is due to the electric-fieldinduced AFE-FE switching, showing the critical field $E_{\rm F}$ around 100 kV/cm. Compared to the already reported CHNN AFE ceramics as listed in Table I, the E_F of BSNN-1 is lower than those of reported CHNNs, which have lower tolerance factors than the BSNN-1. The trend agrees well with the results previously reported.¹⁰⁻¹² Peaks 2 and 3 in the third quadrant indicate the AFE-to-FE back switching and switching with the applied opposite electric field, respectively. There should be a fourth peak representing the AFE-to-FE back switching in the fourth quadrant; but requiring the opposite field to induce the back switching, in this case, caused the absence in this quadrant. The arrow in Fig. 4(a)marks a hump in the first quadrant; previously, in those heavily modified materials, it was considered that the peak was associated with the phase transition to the incommensurate phase. However, due to an electric field being needed to induce the FE-to-AFE phase transition, it would be logical, in this scenario, that the peak was related to the FE-to-AFE phase transition due to potential overlapping of these two peaks. It was known that the relevant phases present similar energy in the vicinity of the phase boundary. Figure 4(b) shows the electronegativity difference (X) vs. tolerance factor (t) of NaNbO3 with CaZrO3, SrZrO3, CaHfO3, and BiScO₃. Compared to the already reported modification strategy by our group,^{10–12} adding BiScO₃ lowered the tolerance factor faster than with the $A^{2+}B^{4+}O_3$ end members. In addition, it showed not only the opposite trend but also a steeper slope of changing the X. Instead of being more ionically bonded, adding BiScO3 increased the covalency of the bonds. It should be noticed that a more ionic character of the metal-oxygen bonds would lead to more thermally stable perovskite.^{40–42} Therefore, further increasing the amount of BiScO₃ could eventually lead to destabilization of the perovskite structure.

In summary, an AFE xBiScO₃-(1-x)NaNbO₃ solid solution was fabricated and characterized. The stabilization of the AFE phase was proven both microstructurally and electrically. The P-E double hysteresis loop was induced and observed in BSNN-1. Additionally, the incommensurate phase was found in the AFE P phase region in BSNN-1, suggesting the existence of competition between AFE and FE phases in this composition. Furthermore, the results well agreed with the previously reported materials.^{10–12} It further broadened the lead-free AFE material family, and the universality of the tolerance factor rule is further verified.

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