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2018

## Influence of Steel Fibres on the Behaviour of RPC Circular Columns Under Different Loading Conditions

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Al-Tikrite, Ahmed and Hadi, Muhammad N. S, "Influence of Steel Fibres on the Behaviour of RPC Circular Columns Under Different Loading Conditions" (2018). *Faculty of Engineering and Information Sciences - Papers: Part B*. 1130.

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# Influence of Steel Fibres on the Behaviour of RPC Circular Columns Under Different Loading Conditions

## Abstract

An experimental program was conducted to investigate the effect of inclusion of steel fibres on the behaviour of Reactive Powder Concrete (RPC) columns. Three different types of steel fibre were used: micro straight steel fibre (MF), macro deformed steel fibre (DF) and waste steel fibre (WF) recovered from discarded tyres. In addition, a hybridization of steel fibres was made up to produce waste-industrial hybridization (WHF) (MF, DF and WF). Twenty reinforced RPC column specimens were prepared and tested under axial concentric, eccentric and flexural loading. Results of testing demonstrated that the ultimate axial load and the corresponding axial deformation increased effectively by the addition of steel fibres, especially at the presence of MF. For the flexural loading, the inclusion of WF and WHF increased the energy absorption of specimens by 470% and 453%, respectively, in comparison with the corresponding reference specimens. Axial load-bending moment (P-M) interaction diagrams were carried out. Results of testing show that WF is a promising material for enhancing the behaviour of RPC under different loading conditions.

## Disciplines

Engineering | Science and Technology Studies

## Publication Details

Al-Tikrite, A. & Hadi, M. N. S. (2018). Influence of Steel Fibres on the Behaviour of RPC Circular Columns Under Different Loading Conditions. *Structures*, 14 111-123.

1 **Influence of Steel Fibres on the behaviour of RPC Circular Columns under Different**  
2 **Loading Conditions**

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9  
10 **Abstract**

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19 especially at the presence of MF. For the flexural loading, the inclusion of WF and WHF  
20 increased the energy absorption of specimens by 470% and 453%, respectively, in  
21 comparison with the corresponding reference specimens. Axial load-bending moment ( $P$ - $M$ )  
22 interaction diagrams were carried out. Results of testing show that WF is a promising material  
23 for enhancing the behaviour of RPC under different loading conditions.

24  
25 **Keywords:** RPC columns; Steel fibres; Load carrying capacity; Energy absorption;  $P$ - $M$   
26 interactions.

27 **1. Introduction**

28 Reactive Powder Concrete (RPC) is known as concrete with superior characteristics and is  
29 being increasingly used. The strength of RPC comes from the utilization of highly refined  
30 admixtures, low water to binder ratio and the exclusion of the coarse aggregate. The RPC is  
31 rated as a concrete with excellent strength and durability [1, 2]. This type of concrete enables  
32 the designers to reduce the size of structural members such as columns in lower stories and  
33 consequently reduces the self-weight of the structure. However, RPC is identified with its  
34 excessive brittleness. It was reported that the increase in the compressive strength of the  
35 concrete results in an increase in the brittleness of the concrete.

36

37 Helices are normally used to confine the core of the concrete columns. However, for high  
38 strength concrete, the transverse reinforcement confinement is less efficient than in normal  
39 strength concrete when used in columns [3-5]. Furthermore, the ACI 318-14 [6] set the limits  
40 for the degree of confinement by setting the pitch of the helices as minimum as 25 mm in  
41 order to avoid the congestion of the helices in the columns. As such, helices are less efficient  
42 when used in the RPC columns. The need to improve the properties of the RPC material is  
43 crucial to mitigate the brittleness issue.

44

45 The incorporation of steel fibre in the concrete enhances the tensile strength, flexural strength  
46 and the toughness of the concrete [7-10]. The way the steel fibre works is by bridging the  
47 developed cracks due to the applied compressive loads or shrinkage and prevents the  
48 widening of cracks. This action continues until the steel fibres debond from the concrete. As a  
49 result, the concrete that includes steel fibre exhibits higher strength and toughness compared  
50 to non-fibrous concrete [11-13]. Moreover, the geometry of steel fibres plays a key role in  
51 improving the properties of the concrete. For example, Olivito and Zuccarello [14] and Xia et  
52 al. [15] stated that length of the steel fibre greatly affect the post ultimate behaviour,

53 toughness and the load carrying capacity of the normal strength concrete. Abbas et al. [13]  
54 stated that short steel fibres affects the flexural properties more than the long steel fibres.  
55 Nataraja et al. [16] and Wu et al. [17] reported that the configuration of the steel fibres affects  
56 the ultimate load and the flexural load-deflection behaviour of normal strength concrete and  
57 the effect of the deformed steel fibres is more than the effect of smooth steel fibres.

58

59 In order to obtain full benefit from the incorporation of steel fibres in the concrete, several  
60 researchers attempted to incorporate two types of steel fibres in the concrete in a process  
61 called hybridization. The hybrid steel fibres is obtained by mixing two types of steel fibres of  
62 different properties in order to make use of the advantages of each steel fibre in improving the  
63 properties of the concrete. For instance, Kang et al. [18] investigated including straight steel  
64 fibres (0.2 mm diameter and 16.3-19.5 mm length) hybridized with different types of  
65 synthetic fibres (basalt, polyvinyl-alcohol, and polyethylene) in Ultra-High Strength Concrete  
66 (UHSC). Results of testing showed that the inclusion of steel fibres and synthetic fibres  
67 effectively improves the tensile strength of UHSC due to the effect of fibres on the crack  
68 development in different stages. Park et al. [19] investigated the effect of including different  
69 types of steel fibres of different geometrical shapes on the tensile behaviour of UHSC. It was  
70 concluded that the tensile stress-strain behaviour, post-crack behaviour and the strength was  
71 noticeably enhanced by the addition of the hybrid steel fibres that included micro smooth and  
72 macro twisted steel fibres. Furthermore, Glavind and Aarre [20], Larsen and Krenchel [21]  
73 and Feldman and Zheng [22] have investigated the effect of hybridization between steel fibres  
74 and polypropylene on the behaviour of concrete. The reported results showed the  
75 hybridization of steel fibres and polypropylene fibres results in the enhancement of the tensile  
76 strength and the fracture energy. The enhancement was attributed to the action of the steel  
77 fibres in improving the ultimate strength while the polypropylene fibres improved the energy  
78 absorption of concrete. Banthia and Sheng [23] reported that the incorporation of two types of

79 fibres of different materials and moduli of elasticity such as steel fibres and carbon fibres  
80 enhanced the strength and the toughness of the concrete. The steel fibres improve the strength  
81 while the carbon fibres improve the toughness of the concrete. Al-Tikrite and Hadi [24]  
82 investigated the inclusion of steel fibre on the mechanical properties of RPC in individual and  
83 hybrid forms. Al-Tikrite and Hadi [24] concluded that the hybridization of steel fibres affects  
84 the ultimate stress, the corresponding strain and the modulus of elasticity effectively. Also,  
85 the post ultimate behaviour of RPC and the energy absorption of RPC were improved  
86 noticeably.

87

88 On the other hand, the negative aspect of utilizing the industrial steel fibres to reinforce the  
89 concrete is the high cost of steel fibres compared to the materials used to produce the  
90 concrete. It is estimated that the cost of 1% by volume of steel fibres included in the Ultra-  
91 High Strength Concrete (UHSC) is higher than the cost of the material used in the mixture  
92 [25]. Also, if the consumption of the natural resources is taken into consideration, the  
93 estimated amount of the industrial fibres that are produced annually is about 60 million  
94 tonnes around the world [26]. Moreover, the cost of steel fibres in some countries may not  
95 justify using it in the concrete [27]. Consequently, to save the cost of steel fibre and to  
96 conserve the natural resources, the need for searching for alternatives to the industrial steel  
97 fibres or to reduce the amount of steel fibres to be added without affecting the properties of  
98 the concrete has become important.

99

100 As such, this study, as a complementary work of a study conducted by Hadi and Al-Tikrite  
101 [28], investigated experimentally the effect of the inclusion of steel fibre on the behaviour of  
102 RPC columns under different loading conditions. The emphasis of the current work is the  
103 investigation of the influence of the inclusion of different types of steel fibres of different  
104 geometry in individual form and in hybrid form on the behaviour of RPC specimens under

105 different loading conditions. The geometry of steel fibres, type (industrial and waste) and  
106 volume content is the main parameters that were considered in this study. Also, the feasibility  
107 of the inclusion of the waste steel fibres (WF) recovered from discarded tyres either  
108 individually or hybridised with the industrial steel fibres in the RPC column specimens tested  
109 under different loading conditions was investigated. Three different types of steel fibres of  
110 different geometry and volume contents were used: straight micro steel fibre (MF), macro  
111 deformed steel fibre (DF) and waste steel fibre (WF) recovered from discarded tyres. A  
112 hybridization of steel fibres was made up to produce waste-industrial hybrid steel fibre  
113 (WHF). The RPC column specimens that included MF and DF had been investigated by Hadi  
114 and Al-Tikrite [28]. For comparison purposes, the abovementioned two groups of column  
115 specimens were included in this research paper. A total of twenty RPC specimens of five  
116 groups were cast and tested in this study. Each group included four specimens, one tested  
117 under concentric loading, two were tested under eccentric loading (25 mm and 50 mm) and  
118 one tested under flexural loading (four-point bending).

119

## 120 **2. Experimental Program**

### 121 **2.1 Materials**

122 Three different types of steel fibres of different geometries and volume contents were used:  
123 micro straight steel fibre (MF), macro deformed steel fibre (DF) and waste steel fibre (WF)  
124 recovered from discarded tyres. The ratio of MF, DF and WF used in this study were 4%, 2%  
125 and 3%, respectively. These ratios were shown to be the optimum ratios that improve the  
126 behaviour of RPC under loading based on an earlier study conducted by Al-Tikrite and Hadi  
127 [24] on RPC. A hybridization of steel fibre was made up by blending 50% of the best ratio of  
128 WF and 25% of the best ratios of MF and DF (1% MF, 0.5% DF and 1.5% WF) to produce  
129 the waste-industrial steel fibre (WHF) at 3%. The hybridization of WF, MF and DF was done  
130 after the waste steel fibre WF was measured and grouped into ranges of average diameters

131 and ranges of lengths. Afterwards, randomly selected 1.5% of WF was hybridized with 1%  
132 MF, 0.5% DF to form WHF.

133 The micro straight steel fibres used was of a diameter ( $D = 0.2$  mm), length ( $L = 6$  mm) and  
134 nominal tensile strength of 2900 MPa [29]. The macro deformed steel fibre was of ( $D = 0.55$   
135 mm,  $L = 18$  mm and nominal tensile strength = 800 MPa) [30]. The waste steel fibre  
136 recovered from discarded tyres was obtained from a local source.

137

138 The WF measurements were performed as follows [24]: waste steel fibres were randomly  
139 selected and distributed in ten groups of one hundred steel fibres. Measuring the length and  
140 the diameter of each steel fibre was done by a micrometre. The measurements were  
141 conducted on each steel fibre as follows: Three measurements for the diameter (one at each  
142 end and one in the middle) and one for the length. Also, a tensile strength test was conducted  
143 for two samples from each group. The WF was grouped into average diameters and range of  
144 lengths. The range of lengths and the percentage of WF were distributed according to the  
145 average diameters. The range of the average diameters and lengths measured with the  
146 percentage of each range is shown in Fig. 1. The average length was ( $L_{average} = 22.2$  mm), the  
147 average diameter was ( $D_{average} = 0.22$  mm) and the average tensile strength was 1900 MPa.  
148 Fig. 2 shows steel fibres utilized in this study.

149

150 The RPC mixture reported by Al-Tikrite and Hadi [24] was utilized in this study. The  
151 targeted compressive strength of RPC is 100 MPa. Table 1 presents the constituents of the  
152 RPC mixture.

153

## 154 **2.2 Preparation of specimens, mixing and casting procedure**

155 To investigate the effect of different types of steel fibre included in the RPC circular column,  
156 five groups of twenty RPC specimens of 200 mm diameter and 800 mm length were cast and



157 tested. The first group was the reference specimens which were non-fibrous RPC specimens  
158 (NF). The second group was the RPC specimens that included 4% micro straight steel fibres  
159 (MF). The third group was the RPC specimens that included 2% macro deformed steel fibres  
160 (DF). The fourth group was the RPC specimens that included 3% waste steel fibre recovered  
161 from discarded tyres (WF). The fifth group was the RPC specimens that included 3%  
162 industrial-waste hybrid steel fibres (WHF). Each group included four specimens, one tested  
163 under concentric loading, two tested under eccentric loading (25 mm and 50 mm) and one  
164 tested under flexural loading.

165

166 To identify the RPC specimens, the specimens were labelled as follows: the first part of the  
167 label, NF, MF, DF, WF and WHF represents non-fibrous, micro steel fibre, deformed steel  
168 fibre, waste steel fibre and waste-industrial steel fibre, respectively. The second part of the  
169 label represents the loading conditions, E0, E25, E50 and PB, which represents concentric  
170 loading, 25 mm eccentric loading, 50 mm loading and flexural loading, respectively. For  
171 example, Specimen NF-E0 represents the RPC specimen which is non-fibrous specimen  
172 (reference) tested under concentric loading. Specimen MF-E25 represents the RPC specimen  
173 that included MF tested under eccentric loading at 25 mm. Specimen DF-E50 represents the  
174 RPC specimen that included DF tested under eccentric loading at 50 mm. Specimen WF-PB  
175 represents the RPC specimen that included WF tested under flexural loading (four-point  
176 bending).

177

178 All specimens were longitudinally reinforced with six N12 steel bars (12 mm diameter,  
179 deformed) and confined with steel helix R10 (10 mm diameter, smooth) of a diameter of 150  
180 mm centre to centre. The yield strength of N12 and R10 are 515 MPa and 320 MPa,  
181 respectively. The pitch of the helices was 40 mm. The concrete cover was 20 mm from all  
182 sides. The reinforcement details for all specimens in this study were kept the same to

183 demonstrate the effect of the steel fibre on the behaviour of RPC under different loading  
184 conditions. Table 2 shows the reinforcement details of the specimens.

185

186 The moulds utilized to cast the specimens in this study were plastic tube moulds of 200 mm  
187 inner diameter and 800 mm length. The plastic tube moulds were affixed vertically by a  
188 wooden formwork that was built in the laboratory. The longitudinal steel bars N12 were cut  
189 to length of 760 mm. The helix R10 was coiled at a diameter of 150 mm centre to centre. An  
190 aluminium spacer was used to keep the spacing between the helices at 40 mm. The helix was  
191 fixed vertically to a steel plate base. Two horizontal spacers were used, one at the bottom and  
192 one at the top to position the longitudinal bars accurately. Next, the longitudinal steel bars  
193 were tied to the helix to form the steel reinforcement frame. Then, the steel reinforcement  
194 frames were placed in the plastic tube moulds and prepared for casting. Figures 3 and 4 show  
195 the fabrication and steel reinforcement details of the tested specimens, respectively.

196

197 Mixing and casting procedure of RPC was performed according to Al-Tikrite and Hadi [24].  
198 Firstly, the dry materials including the cement, silica fume, silica flour and the natural fine  
199 sand were placed in the pan of the mixer and mixed for about 4 minutes. Next, 80% and 50%  
200 of the water and superplasticiser, respectively, were mixed together separately and added to  
201 the dry mix and mixed for about 5 minutes. Afterwards, the remaining 20% of the water and  
202 50% of the superplasticiser were mixed separately and added to the mixture and mixing  
203 process continued for an extra 5 minutes until the particles of the constituents started to form  
204 flocks of concrete which is called breaking point. Next, the steel fibres were added to the  
205 mixture and the mixing process continued for further 4 minutes after the addition of steel  
206 fibres until the mixture turned to a flowable mixture. Then, the flowable RPC was placed in  
207 the plastic moulds in layers in order to avoid the entrapment of air voids.

208

209 The curing was done by covering the RPC specimens by a wet hessian fabric to provide a  
210 moist environment for the specimens. Also, plastic sheets were used to cover the hessian  
211 fabric to prevent the evaporation of the curing water. The curing continued for 27 days then  
212 the specimens were prepared for testing.

213

### 214 ***2.3 Instrumentation and testing procedure***

215 Two Linear Variable Differential Transducers (LVDTs) were externally instrumented in  
216 addition to the LVDT of the testing machine to record the total axial deformation. The lateral  
217 deformation that results from eccentric loading and bending loading was recorded by a laser  
218 triangulation installed on the testing machine at mid-height and mid-span of the specimen  
219 tested under eccentric loading and bending loading, respectively.

220

221 A compression testing machine of a capacity of 5000 kN was used for testing the specimens  
222 under different loading conditions. The ends of the specimens that were tested as columns  
223 were capped with a high strength plaster to ensure levelling of the specimens and provide  
224 uniform surfaces. Also, the specimens were wrapped with a single layer of 100 mm wide  
225 CFRP at the ends to prevent the premature failure. Two circular loading heads were used at  
226 the top and bottom of the specimens to apply loading (concentric or eccentric). The loading  
227 heads include three grooves located at the centre, 25 mm and 50 mm. Two surface loading  
228 adjustment plates were used to fit to the groove depending on the type of loading (See Figure  
229 5). The surface loading adjustment plates touch the loading plates of the testing machine and  
230 transfer the load through the loading knives to the specimen. Figure 5 shows the axial loading  
231 equipment of the tested specimens.

232

233 The loading system shown in Figure 6 was used to test the specimens under flexural loading.

234 The loading system consists of two parts. The upper part consists of two rings placed at the

235 top of the specimen and the lower part consists of two rings placed at the bottom of the  
236 specimen to allow the specimen to bend under flexural loading without experiencing crushing  
237 at the loading points and at supports. The length of the beam span was 700 mm divided into  
238 three equal lengths of 233.3 mm. To prevent the shear failure that might occur due to the  
239 short span length to depth ratio of the reference specimen and to guarantee the deflection at  
240 midspan, the plain RPC specimens (reference) were wrapped with two layers of CFRP at the  
241 shear span from both sides. Also, to have a consistent comparison with the reference, the RPC  
242 specimens that included steel fibres were also wrapped with CFRP at the shear span.

243

244 The specimens were tested by loading them with a displacement controlled load at a rate of  
245 0.005 mm/s until failure. A data logger was connected to the LVDTs and the laser  
246 triangulation to record the data every 2 seconds.

247

### 248 **3. Experimental test results and analysis**

#### 249 ***3.1 Modes of Failure***

250 The mode of failure of the tested specimens was governed by loading condition and presence  
251 of fibres. All specimens were tested until failure. It was observed that hairline cracks  
252 appeared in the midheight of the tested specimen at reaching the ultimate axial load that the  
253 specimens can withstand. Afterwards, the load carrying capacity of the specimen started to  
254 decrease until the fracture of the helix.

255

256 It was noticed that the non-fibrous RPC specimens (reference) tested under concentric  
257 loading, eccentric loading (25 mm and 50 mm) and flexural loading failed in a brittle manner  
258 with a loud smashing sound of the concrete cover after reaching the ultimate load followed by  
259 a sudden drop of the load sustained by the specimens. However, the RPC specimens that  
260 included steel fibres and tested under the same loading conditions did not exhibit brittle

261 failure and the failure after reaching the ultimate axial load was gradual with a sound of  
262 ticking resulted from the debonding of fibres from the concrete. Also, the concrete cover did  
263 not exhibit full detachment from the concrete core due to the presence of steel fibres that  
264 bridge the cracks and connect the concrete cover with the concrete core.

265

266 For specimens tested under eccentric and flexural loading, the failure started by crushing of  
267 concrete at the compression zone at midheight of specimens. Vertical hairline cracks  
268 appeared at the compression face while transverse cracks appeared at the tension face. With  
269 the increase in the applied loads, the mouth of the cracks at the tension face started to widen  
270 while the concrete in the compression face started to crush. It was observed that the concrete  
271 cover of the reference specimens tested under eccentric loading exhibited full detachment  
272 nearly along the whole length of the specimen at the compression face. However, the  
273 presence of steel fibres in the RPC specimens delayed the crushing of concrete at the  
274 compression face through the bridging action of the steel fibres that inhibit the initiation and  
275 propagation of cracks. Consequently, the failure of RPC that included steel fibres after  
276 reaching the ultimate axial load was gradual until bonding failure of steel fibres with the  
277 matrix. Afterwards, the concrete core which was dilated due to the initiated cracks started to  
278 apply stresses on the confining helices which provide the concrete core with adequate  
279 stiffness to sustain the applied load [31]. The concrete core sustained the applied loads until  
280 failure. The failure occurred by the fracture of the helices.

281

282 In summary, the presence of steel fibres resulted in the load carrying capacity after reaching  
283 the ultimate axial load was decreased gradually until debonding of steel fibres of the concrete  
284 whereas the concrete core which was dilated due to the initiated cracks started to apply  
285 stresses on the confining helices to sustain the applied load. Figures 7 and 8 shows the failure  
286 modes of the tested specimens.

287

288

### 289 ***3.2 RPC specimens tested under concentric axial load***

290 Five RPC specimens with and without steel fibres were tested under concentric axial load.

291 Table 3 presents the results of the specimens loaded concentrically. It was observed that the

292 addition of steel fibres affected the ultimate axial load of the RPC specimens positively. In

293 particular, the inclusion of MF in the RPC specimen has attained the highest increase in the

294 ultimate axial load under concentric loading in comparison with the other types of steel fibres.

295 The load carrying capacity of Specimen MF-E0 was 32% higher than the ultimate axial load

296 of Specimen NF-E0. This is because short or micro steel fibre affects the strength of concrete

297 more than long steel fibres due to controlling of the early cracking of concrete [32] and the

298 uniform distribution of the micro steel fibres throughout the matrix without entangling

299 between each other. The load carrying capacity of Specimens DF-E0, WF-E0 and WHF-E0

300 was increased by 9%, 23% and 23%, respectively, compared to the load carrying capacity

301 Specimen NF-E0.

302

303 The addition of steel fibre had positively affected the post ultimate behaviour of the RPC

304 specimens through softening of the descending branch of the load-deformation curve and

305 preventing the sudden failure. The improvement of the descending branch of the load-

306 deformation curve comes from an additional action provided by steel fibres through the bond

307 between the steel fibres and the concrete [33]. The action of fibres was noticeable from the

308 ultimate axial load until debonding of fibres from the concrete in the concrete cover whereas

309 the transverse steel reinforcement confinement proceeds to fully sustain the applied load. The

310 effect of steel fibres on the post ultimate behaviour of RPC specimens was noticeable in terms

311 of energy absorption. The energy absorption is defined as the ratio of the area under the load-

312 deformation curve up to the postultimate load to the area under the load-deformation curve up  
313 to the yield load [34-37]:

$$314 \quad \lambda = \frac{A_{\delta_u}}{A_{\delta_y}} \quad (1)$$

315 where,  $\lambda$  is the energy absorption of RPC specimen,  $A_{\delta_y}$  is the area under load-deformation  
316 curve calculated from zero to the deformation that corresponds to the yield axial load and  $A_{\delta_u}$   
317 is the area under the load-deformation curve calculated from zero to the postultimate axial  
318 deformation that corresponds to 85% of the ultimate axial load [34, 38]. The yield axial load  
319 was found by drawing two lines. The first line is a tangent to the load-deformation curve and  
320 meets the curve at the origin. The second line is a horizontal line that touches the curve at the  
321 ultimate axial load. Next, a vertical line is drawn from the intersection of these two lines. The  
322 point that the vertical line intersects the curve represents the yield point [28, 39]. Figure 9  
323 illustrates the calculation of the energy absorption of the tested specimens.

324

325 The post ultimate behaviour of the RPC specimens, however, was different depending on the  
326 type, geometry and amount of steel fibres included in the RPC specimen. Specimen NF-E0,  
327 after reaching the ultimate axial load of 3304 kN, experienced a sudden failure in a brittle  
328 manner with smashing sound due to the spalling of the concrete cover. The load carrying  
329 capacity dropped by 22% to 2564 kN at an axial deformation of 4.6 mm. Afterwards, the  
330 applied load was sustained by the confined core that withstood the applied load until the  
331 fracture of the helix at an axial deformation of 21.5 mm that corresponds to an axial load of  
332 1633 kN.

333

334 For Specimens MF-E0 and DF-E0, the addition of MF and DF delayed the early spalling of  
335 the concrete cover after reaching the ultimate load carrying capacities of 4373 kN and 3607  
336 kN, respectively, and prevented the sudden failure of the load. Also, the descending branch of

337 the axial load-axial deformation curve was gradual until axial loads of 3483 kN and 2668 kN,  
338 respectively, at axial deformations of 6.5 mm and 6.3 mm, respectively. Afterwards, the  
339 confined core sustained the load until failure. Specimens MF-E0 and DF-E0 failed at axial  
340 loads of 1900 kN and 1791 kN, respectively, at axial deformations of 21.7 mm and 22.4 mm,  
341 respectively. The energy absorption of Specimens MF-E0 and DF-E0 was increased by 16%  
342 and 2%, respectively, compared to Specimen NF-E0. The increase in the energy absorption of  
343 Specimen DF-E0 was the lowest compared with its counterparts. This might be attributed to  
344 the sudden widening of the initiated cracks that caused the slippage of DF that bridges the  
345 macro cracks and resists widening of cracks until the applied load that caused widening of  
346 cracks become larger than the bonding between DF and the matrix leading to slippage of  
347 fibres [40].

348

349 The incorporation of WF in the RPC specimens has a positive impact on the ultimate axial  
350 load and post ultimate behaviour of the RPC specimens. The load carrying capacity of  
351 Specimen WF-E0 was increased by 15% compared to Specimen NF-E0. The WF has  
352 effectively delayed the early spalling of the concrete cover after reaching the ultimate load  
353 carrying capacity. The load carrying capacity of Specimen WF-E0 after reaching the ultimate  
354 axial load was decreased gradually up to an axial load of 2685 kN at an axial deformation of  
355 7.3 mm. Specimen WF-E0 failed at an axial load of 1495 kN at an axial deformation of 38.1  
356 mm. The energy absorption of Specimen WF-E0 was increased by 58% compared to the  
357 energy absorption of Specimen NF-E0.

358

359 The addition of the hybrid steel fibres (WHF) improved the post ultimate behaviour of the  
360 RPC specimens noticeably. The early spalling of the concrete cover was effectively delayed  
361 by WHF up to the ultimate load carrying capacity of 4066 kN. Afterwards, the load carrying  
362 capacity decreased gradually up to an axial load of 2577 kN at an axial deformation of 7.4



363 mm. The energy absorption of Specimen WHF-E0 was improved by 67% compared with the  
364 energy absorption of Specimen NF-E0. The improvement in the post ultimate behaviour of  
365 Specimen WHF-E0 could be attributed to the combined action of steel fibres, the short or the  
366 micro steel fibres bridge the micro cracks while the long steel fibres bridge the macro cracks  
367 and prevents widening of cracks [41]. Specimen WHF-E0 failed at an axial load of 1459 kN  
368 at an axial deformation of 45.5 mm. Fig. 10 (a) shows the behaviour of the tested RPC  
369 specimens under concentric loading.

370

371 The configuration of steel fibres plays a key role in enhancing the behaviour of the RPC  
372 specimens. For instance, the RPC specimens that included DF which bridges the macro  
373 cracks have presented early debonding from the concrete due to the slippage of the steel fibre  
374 from the matrix when the applied load become higher than the bond between DF and the  
375 matrix. However, The RPC specimens that included MF which is straight steel fibres that  
376 bridges micro cracks have presented delayed debonding from the matrix. Also, the RPC that  
377 included WF of variant geometrical shapes, as a result of the recovery process from discarded  
378 tyres, have shown delayed debonding from the RPC matrix compared to DF. This might be  
379 attributed to the entrapped air in the corrugation of the deformed steel fibres which causes  
380 lack of contact along the steel fibre with the matrix and finally less bonding between the steel  
381 fibre and the matrix.

382

383 It was noticed that the provided confinement for the column is not significant especially for  
384 the non-fibrous RPC specimens. This is due to the excessive brittleness of RPC that is known  
385 of lack of ductility and experiences sudden failure when the maximum strength is reached.  
386 Moreover, the dilation of RPC is very low due its brittleness. As such, the provided  
387 confinement from the confining helices for RPC specimens is very low due to the failure of  
388 concrete material before the dilated concrete core applies stresses on the confining helices to

389 provide the concrete core with adequate stiffness to sustain the applied load. For instance, for  
390 the non-fibrous RPC specimens, a total spalling of the concrete cover occurred at reaching the  
391 ultimate axial load followed by a sudden drop in the load carrying capacity was noticed.  
392 However, the inclusion of steel fibres as a solution for mitigating the brittleness issue in the  
393 RPC specimens resulted in the load carrying capacity after reaching the ultimate axial load to  
394 decrease gradually until debonding of steel fibres from the concrete whereas the concrete core  
395 withstood the applied load up to failure.

396

### 397 ***3.3 RPC specimens tested under eccentric axial load***

398 Ten RPC specimens were tested under eccentric loading. Five specimens were subjected to  
399 eccentric loading at 25 mm eccentricity and five specimens were subjected to eccentric  
400 loading at 50 mm eccentricity. Table 4 presents the results of the tested specimens under  
401 eccentric loading. It was observed that all of the specimens that were subjected to eccentric  
402 loading have experienced crushing of the concrete cover at the compression face at reaching  
403 the ultimate load carrying capacity. The concrete cover of Specimens NF-E25 and NF-E50  
404 has almost spalled off at the compression face. The ultimate load carrying capacity of  
405 Specimens NF-E25 and NF-E50 were 2194 kN and 1327 kN, respectively. After reaching  
406 ultimate axial load, the load carrying capacity of Specimens NF-E25 and NF-E50 dropped  
407 suddenly by 29% and 51%, respectively, to 1705 kN and 878 kN, respectively. Then, the  
408 applied load was sustained by the confined concrete core of Specimens NF-E25 and NF-E50  
409 until the fracture of confining helix at axial loads of 549 kN and 349 kN, respectively.

410

411 The inclusion of steel fibres in the RPC specimens delayed the early spalling of the concrete  
412 cover which resulted in an increase in the load carrying capacity of the RPC specimens. The  
413 load carrying capacity of Specimen MF-E25 was 2835 kN which is about 29% higher than  
414 the load carrying capacity of Specimen NF-E25. The energy absorption of Specimen MF-E25

415 was improved by 21% compared to the energy absorption of Specimen NF-E25. The load  
416 carrying capacity of Specimen MF-E50 was 1711 kN which is about 29% higher than the  
417 load carrying capacity of Specimen NF-E50. The energy absorption of Specimen MF-E50  
418 was improved by 41% compared to the energy absorption of Specimen NF-E50. The  
419 descending branch of the load-deformation curve of Specimens MF-E25 and MF-E50 was  
420 softened after reaching the ultimate load carrying capacity up to axial loads of 2025 kN and  
421 1405 kN, respectively. Then, the transverse steel confinement started to sustain the applied  
422 loads until the failure of specimens.

423

424 The load carrying capacity of Specimen DF-E25 increased by 2% compared to Specimen NF-  
425 E25. After reaching the ultimate load carrying capacity, the load carried by Specimen DF-E25  
426 decreased about 31% to an axial load of 1710 kN. The energy absorption of Specimen DF-  
427 E25 was higher than the energy absorption of Specimen NF-E25 by 2%. The load carrying  
428 capacity of Specimen DF-E50 increased by 7% compared to the load carrying capacity of  
429 Specimen NF-E50. After reaching the ultimate axial load, the load carrying capacity of the  
430 specimen decreased by about 44% to an axial load of 980 kN. The energy absorption of  
431 Specimen DF-E50 was higher than the energy absorption of Specimen NF-E50 by 4%. The  
432 lower energy absorption provided by DF could be attributed to the slippage of DF that arrests  
433 the macro cracks; cracks that were initiated in the concrete due to loading; when a sudden  
434 widening of cracks occurred which caused the bonding between DF and the matrix to become  
435 lower than the applied load that caused widening of crack and resulted in slippage of DF [42].

436

437 The inclusion of WF in the RPC specimen has positively affected the load carrying capacity  
438 and the energy absorption under eccentric loading. The load carrying capacity of Specimen  
439 WF-E25 was 2496 kN which is 14% higher than the load carrying capacity Specimen NF-  
440 E25. The load carrying capacity of Specimen WF-E50 was 1576 kN which is 19% higher

441 than the load carrying capacity of Specimen NF-E50. The WF that was included in  
442 Specimens WF-E25 and WF-E50 has kept the concrete cover attached to the concrete core  
443 after reaching the ultimate axial load and effectively softened the descending branch up to  
444 axial loads of 2056 kN and 1422 kN, respectively. The energy absorption of Specimen WF-  
445 E25 was higher than the energy absorption of Specimens NF-E25 by 36%. Also, the energy  
446 absorption of Specimen WF-E50 was 45% higher than the energy absorption of Specimen  
447 NF-E50. This is due to the WF includes different sizes of steel fibres as a result of the  
448 recovery process which combines between the actions of the short and long steel fibres in  
449 RPC in inhibiting the cracks' initiation and propagation. Also, the diversity of the geometry  
450 of WF provides a very good bonding with the matrix and results in a considerable restraining  
451 of widening of cracks through bridging the macro cracks and finally prevents the spalling of  
452 the concrete cover to latter stages.

453

454 The load carrying capacity of Specimen WHF-E25 increased by 15% compared to the load  
455 carrying capacity of Specimen NF-E25. Also, the load carrying capacity of Specimen WHF-  
456 E50 increased by 14% compared to the load carrying capacity of Specimen NF-E50. The post  
457 ultimate behaviour of Specimens WHF-E25 and WHF-E50 was improved under eccentric  
458 loading up to axial loads of 2141 kN and 1304 kN, respectively. The energy absorption of  
459 Specimen WHF-E25 was improved by 38% in comparison with the energy absorption of  
460 Specimens NF-E25. Also, the energy absorption of Specimen WHF-E50 improved by 45%  
461 compared to the energy absorption of Specimen NF-E50. This might be due to the combined  
462 action of the short and long steel fibres in inhibiting the initiation and the widening of cracks  
463 and finally keep the concrete cover attached to the concrete core to latter stages. Figure 10 (b)  
464 and (c) shows the behaviour of the tested RPC specimens under 25 mm and 50 mm eccentric  
465 loading.

466

### 467 **3.4 RPC specimens tested under flexural loading (four-point bending)**

468 Five Specimens (NF-PB, MF-PB, DF-PB, WF-PB and WHF-PB) were tested under flexural  
469 loading to investigate the behaviour of specimens under pure flexural load. Table 5 presents  
470 the experimental results of the tested specimens under flexural loading. Figure 10 (d) shows  
471 the flexural load-midspan deflection curves of the tested specimens.

472 The ascending branch of the curve was linear for all specimens. The ultimate flexural load  
473 sustained by Specimen NF-PB (the reference) was 356 kN while Specimens MF-PB, DF-PB,  
474 WF-PB and WHF-PB had sustained about 10%, 6%, 13 and 9% higher flexural load,  
475 respectively, than the reference specimen sustained. Afterwards, the load sustained by the  
476 Specimen NF-PB after reaching the ultimate flexural load dropped suddenly by about 23% to  
477 a flexural load of 274 kN. This drop was because of the crushing of concrete cover at the  
478 compression face of the specimen. However, the addition of steel fibres to the RPC  
479 specimens has softened the descending branch of the load-deflection curve noticeably. The  
480 load sustained by Specimens MF-PB and DF-PB after reaching the ultimate flexural load  
481 decreased gradually to 371 kN and 329 kN, respectively, at a corresponding midspan  
482 deflection of 11.7 mm and 8.03 mm, respectively.

483

484 The ultimate flexural load of Specimen WF-PB was 403 kN which is 13% higher than the  
485 ultimate flexural load of the corresponding reference specimen. The load sustained by  
486 Specimen WF-PB after reaching the ultimate load decreased gradually to a flexural load of  
487 370 kN at a corresponding midspan deflection of 11.4 mm. The energy absorption of  
488 Specimen WF-PB was 470% higher than the energy absorption of Specimen NF-PB. Also the  
489 energy absorption of Specimen WF-PB was higher than the energy absorption of Specimens  
490 MF-PB, DF-PB and WHF-PB. This is attributed to good bonding between WF and RPC  
491 which requires a higher load to pull the fibres out of the concrete. Also, the homogenous  
492 distribution of WF throughout the section inhibits the initiation of the micro cracks and the

493 widening of the macro cracks as the WF includes different sizes of steel fibre of different  
494 lengths which enables WF to have combined actions of the short, middle and long steel fibres  
495 and delayed the spalling of the concrete cover to latter stages. Similar finding were reported  
496 by Aiello et al. [43] in regards to flexural strength of concrete reinforced with WF.

497 The addition of WHF to RPC increased the ultimate flexural load of Specimen WHF-PB by  
498 9% compared to Specimen NF-PB and achieved a ultimate flexural load of 389 kN. The  
499 descending branch of the load-deflection curve was softened effectively and the decrease in  
500 the load sustained by the specimen after reaching the ultimate load was gradual up to a load  
501 of 356 kN at a corresponding midspan deflection of 13.5 mm.

502

#### 503 **4. Experimental axial load-bending moment interaction diagram ( $P$ - $M$ diagram)**

504 For design purposes of columns subjected to different loading conditions, an experimental  
505 axial load-bending moment interaction diagram ( $P$ - $M$  diagram) was drawn based on the test  
506 results. The ultimate axial loads and the ultimate bending moments of the RPC specimens  
507 tested under concentric loading, eccentric loading (25 mm and 50 mm) and flexural loading  
508 were used to construct the  $P$ - $M$  diagram. The  $P$ - $M$  diagram was constructed from four points.  
509 The first point represents the ultimate axial load obtained from the specimens tested under  
510 concentric loading. The second and third points represent the ultimate eccentric axial loads  
511 obtained from the specimens tested under eccentric loading at 25 mm and 50 mm. The fourth  
512 point represents the ultimate bending moment that corresponds to the ultimate flexural load  
513 obtained from specimens tested under flexural loading.

514

515 For the second and third points in the  $P$ - $M$  diagram, the ultimate moment that corresponds to  
516 the ultimate axial load of RPC specimens tested under eccentric load (25 mm and 50 mm)  
517 was calculated as follows:

518 
$$M_u = P_u(e + \delta_{midheight}) \quad (2)$$

519 where,  $M_u$  is the ultimate moment corresponding to the ultimate axial load,  $P_u$  is the ultimate  
520 axial load,  $e$  is the load eccentricity and  $\delta_{midheight}$  is the ultimate lateral deformation that  
521 corresponds to the ultimate axial deformation at midheight.

522 The fourth point is the ultimate bending moment that corresponds to the ultimate flexural load  
523 obtained from the specimens tested under flexural loading. The ultimate moment was  
524 calculated as follows:

525 
$$M_{f,u} = P_{f,u} \times L/6 \quad (3)$$

526 where,  $M_{f,max}$  is the ultimate moment that corresponds to the ultimate flexural load,  $P_{f,p}$  is  
527 the ultimate flexural load,  $L$  is span length of the flexural test. Table 6 presents the  
528 experimental ultimate axial loads and the corresponding ultimate moments of the tested  
529 specimens under concentric, eccentric and flexural loading.

530

531 The inclusion of steel fibres in the RPC specimens has increased the ultimate axial load and  
532 the corresponding moment considerably in comparison with the reference specimens (NF).  
533 However, these increases were dependant on the steel fibres content, geometry and type. The  
534 MF specimens showed the highest axial load and bending moment due to the effect of the MF  
535 on the strength of the RPC through the inhibition of the initiation and propagation of the  
536 micro cracks. The DF specimens showed the lowest ultimate axial load and lowest ultimate  
537 moment compared with the RPC specimens that included MF, HF, WF and WHF. This is  
538 because of the slippage of DF from the matrix due to the sudden widening of the macro  
539 cracks the DF bridges. The WF and WHF specimens showed axial loads and bending  
540 moments lower than the axial load and bending moment of MF specimens. The reason for  
541 this is WF and WHF affect the post ultimate behaviour more than the ultimate axial load. It is

542 worth to mention that the results of the tested specimens that included different types of steel  
543 fibres were consistent and the comparisons among the experimental results obtained indicate  
544 the possibility of repeatability of the results. Figure 11 shows the experimental *P-M*  
545 interaction diagram of the tested specimens under concentric, eccentric (25 mm, 50 mm) and  
546 flexural loading.

547

## 548 **5. Conclusion**

549 The experimental results of testing twenty RPC specimens that incorporated MF, DF, WF and  
550 WHF under concentric, eccentric and flexural loading (four-point bending) are presented in  
551 this paper. The following conclusion can be withdrawn:

- 552 1. The mode of failure of the tested specimens was governed by loading condition and  
553 presence of fibres. The non-fibrous RPC specimens experienced an early spalling of the  
554 concrete cover at reaching the ultimate axial load then a sudden drop of the load carrying  
555 capacity was observed. However, the inclusion of the steel fibres effectively delayed the  
556 early spalling of the concrete cover beyond the ultimate axial load until the pull out of the  
557 fibres from the concrete with gradual decrease of the load carrying capacity. Also, the  
558 concrete cover did not exhibit full detachment from the concrete core after failure.
- 559 2. The addition of MF increased the load carrying capacity of the RPC specimens  
560 considerably compared to the other steel fibres utilized while the inclusion of DF in the  
561 RPC marginally affected the load carrying capacity compared to its counterpart.
- 562 3. The quantity of WF and WHF included in the RPC column specimens is lower than the  
563 quantity of MF which saves the cost of fibres needed to enhance the behaviour of the  
564 RPC column specimen under loading. Moreover, the WF column specimens showed  
565 better behaviour than WHF and DF column specimens and competitive improvement  
566 compared to MF column specimens under different loading conditions which favours  
567 economic and environmental aspects.



- 568 4. The incorporation of WF in the RPC achieved a comparable increase in the ultimate axial  
569 load from 13% to 23% and the energy absorption from 36% to 470%, compared to the  
570 corresponding reference specimens under different loading conditions. Also, the  
571 inclusion of WF hybridized with industrial steel fibre enhanced the ultimate axial load  
572 from 9% to 23% and the energy absorption by 38% to 453% compared to the  
573 corresponding reference specimens under different loading conditions.
- 574 5. The postultimate deformation corresponding to 85% of the ultimate axial load was  
575 markedly improved by the addition of steel fibres. In comparison with the corresponding  
576 reference specimens under different loading conditions, the postultimate deformation was  
577 improved from 37% to 297% when MF was incorporated and from 3% to 251% when  
578 DF was incorporated. The inclusion of WF in the RPC specimens increased the  
579 postultimate deformation from 37% to 523% and from 34% to 357% when WHF was  
580 included.
- 581 6. The inclusion of DF in the waste-industrial hybridization of steel fibres (WHF) affected  
582 the behaviour of the RPC column specimens and decreased the influence of hybridization  
583 on the concrete adversely. As such, the hybridization of WF and MF without DF might  
584 be more reliable and should be further investigated.

585

586 In summary, although using a smaller quantity of fibres, the hybridization of steel fibres  
587 effectively increased the load carrying capacity and the energy absorption of RPC specimens.  
588 However, the total content of the fibres is identical to the one with WF and the content of WF  
589 is lower. As a result, the economic and environmental impacts are lower than in WF case.  
590 Therefore, the inclusion of WF in the RPC specimens as a full replacement is more preferable  
591 economically and environmentally and is feasible and effective in improving the behaviour of  
592 RPC under different loading conditions. Finally, WF is considered as a promising material for  
593 enhancing the behaviour of RPC under different loading conditions.

594

595 **Acknowledgement**

596 The authors would like to express their gratitude to the technical officers in the High Bay  
597 Laboratories of the University of Wollongong, Australia and for their support in performing  
598 the experimental work especially for Mr. Ritchie McLean. Also, the authors would like to  
599 thank Fibercon Australia for providing deformed steel fibres. The first author would like to  
600 acknowledge the Iraqi Government and University of Wollongong, Australia for providing  
601 him with full support for his PhD scholarship.

602

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**Table 1.** RPC mixture constituents

Constituent	Quantity	Unit
Portland cement	955	kg/m <sup>3</sup>
Densified amorphous silica fume	229	kg/m <sup>3</sup>
Natural fine sand (particles size < 600 μm)	974	kg/m <sup>3</sup>
Silica flour (Grade 200)	10	kg/m <sup>3</sup>
Water reducer and retarder	52.6	L/m <sup>3</sup>
Water / binder	0.133	-

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**Table 2.** The main test matrix.

Group	Specimen	Longitudinal reinforcement	lateral reinforcement	Steel fibre type and content	Loading condition
NF	NF-E0	6N12	R10@40 mm	-	Concentric
	NF-E25				Eccentric at 25 mm
	NF-E50				Eccentric at 50 mm
	NF-PB				Flexural
MF	MF-E0	6N12	R10@40 mm	4% MF	Concentric
	MF-E25				Eccentric at 25 mm
	MF-E50				Eccentric at 50 mm
	MF-PB				Flexural
DF	DF-E0	6N12	R10@40 mm	2% DF	Concentric
	DF-E25				Eccentric at 25 mm
	DF-E50				Eccentric at 50 mm
	DF-PB				Flexural
WF	WF-E0	6N12	R10@40 mm	3% WF	Concentric
	WF-E25				Eccentric at 25 mm
	WF-E50				Eccentric at 50 mm



	WF-PB				Flexural
WHF	WHF-E0				Concentric
	WHF-E25				Eccentric at 25 mm
	WHF-E50	6N12	R10@40 mm	1% MF, 0.5% DF and 1.5% WF	Eccentric at 50 mm
	WHF-PB				Flexural

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**Table 3.** Results of specimens tested under concentric loading.

Specimen	NF-E0	MF-E0	DF-E0	WF-E0	WHF-E0
Yield load (kN)	3168	4279	3486	3849	3910
Corresponding deformation to yield load (mm)	4.4	5.5	4.7	4.9	5.0
Ultimate load (kN)	3304	4373	3607	4062	4066
Corresponding deformation to ultimate load (mm)	4.6	5.7	4.9	5.3	5.6
Post ultimate deformation at 85% post ultimate load (mm)	4.7	6.4	5.1	6.9	7.3
Energy absorption	1.1	1.3	1.2	1.8	1.9

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**Table 4.** Results of specimens tested under eccentric loading.

Specimen	Tested under 25 mm eccentricity					Tested under 50 mm eccentricity				
	NF-E25	MF-E25	DF-E25	WF-E25	WHF-E25	NF-E50	MF-E50	DF-E50	WF-E50	WHF-E50
Yield load (kN)	2111	2763	2178	2383	2413	1285	1626	1368	1545	1441
Corresponding deformation to yield load (mm)	3.7	4.5	3.9	4.2	4.1	5.8	7.3	6.2	7.3	7.1
Ultimate load (kN)	2194	2835	2246	2496	2531	1327	1711	1414	1576	1515
Corresponding deformation to ultimate load (mm)	3.9	4.7	4.0	4.5	4.3	6.0	7.8	6.5	7.5	7.4
Post ultimate deformation at 85% post ultimate load (mm)	3.9	5.3	4.0	5.3	5.2	6.0	9.2	6.5	9.4	9.2
Lateral deformation (mm)	2.1	2.8	2.7	2.9	2.8	3.7	4.2	3.9	4.1	3.9
Energy absorption	1.1	1.3	1.1	1.5	1.5	1.1	1.5	1.1	1.5	1.5

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**Table 5.** Results of specimens tested under flexural loading.

Specimen	NF-PB	MF-PB	DF-PB	WF-PB	WHF-PB
Yield load (kN)	307	351	345	358	335
Corresponding deflection to yield load at midspan (mm)	4.3	5.2	5.4	6.2	4.6
Ultimate load (kN)	356	393	379	403	389
Corresponding deflection to ultimate load at midspan (mm)	6.5	7.8	7.6	8.0	7.6
Post ultimate deflection at 85% post ultimate load (mm)	6.6	26.3	23.2	41.2	30.2
Energy absorption	2.0	8.3	7.0	11.6	11.2

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**Table 6.** The ultimate loads and moments of the tested specimens.

Group	Specimen	Ultimate load	Lateral deformation at $P_u$	Midspan deflection at $P_u$	Ultimate moment
		$P_u$ (kN)	$\delta_{\text{lateral}}$ (mm)	$\Delta_{\text{midspan}}$ (mm)	$M_u$ (kN.m)
NF	NF-E0	3304	-	-	0
	NF-E25	2194	2.1	-	59
	NF-E50	1327	3.7	-	71
	NF-PB	356	-	6.5	41
MF	MF-E0	4373	-	-	0
	MF-E25	2835	2.8	-	78
	MF-E50	1711	4.2	-	92
	MF-PB	393	-	7.8	44
DF	DF-E0	3607	-	-	0
	DF-E25	2246	2.7	-	62
	DF-E50	1414	3.9	-	76
	DF-PB	379	-	7.6	44
WF	WF - E0	4062	-	-	0
	WF - E25	2496	2.9	-	69
	WF - E50	1576	4.1	-	85
	WF - PB	403	-	8.0	47
WHF	WHF - E0	4066	-	-	0
	WHF - E25	2531	2.8	-	70
	WHF - E50	1515	3.9	-	81
	WHF - PB	389	-	7.6	45

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811 eccentrically loaded at 25 mm; (c) eccentrically loaded at 50 mm; (d) flexural  
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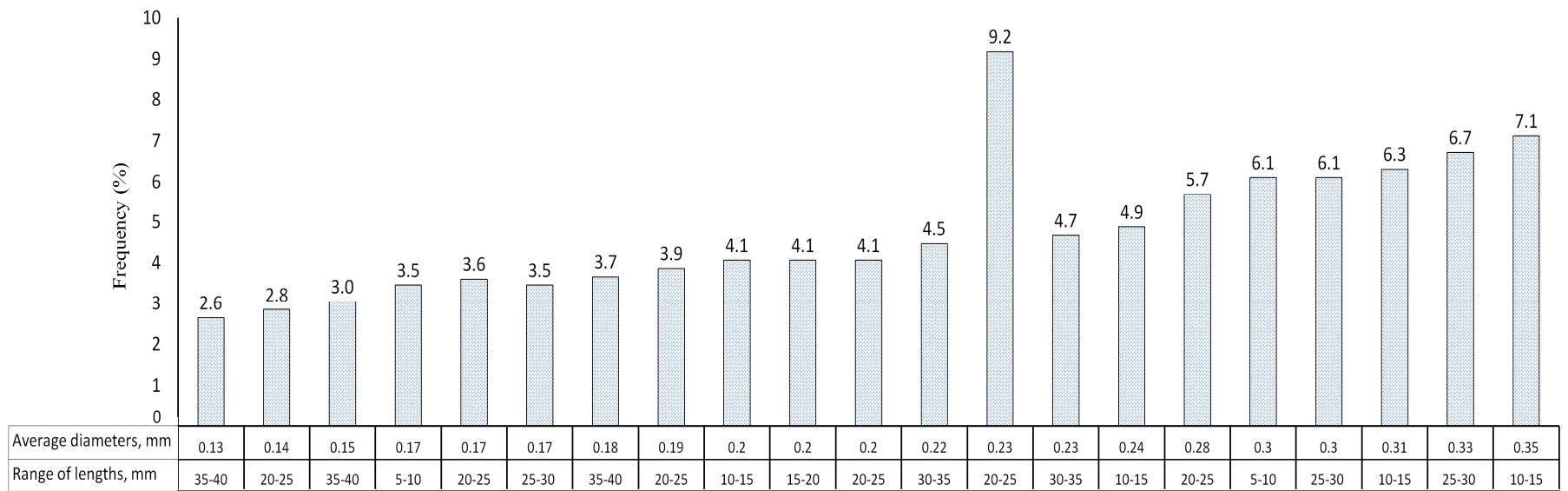
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**Figure 1.** The WF measurements of the diameters and the range of fibre lengths.

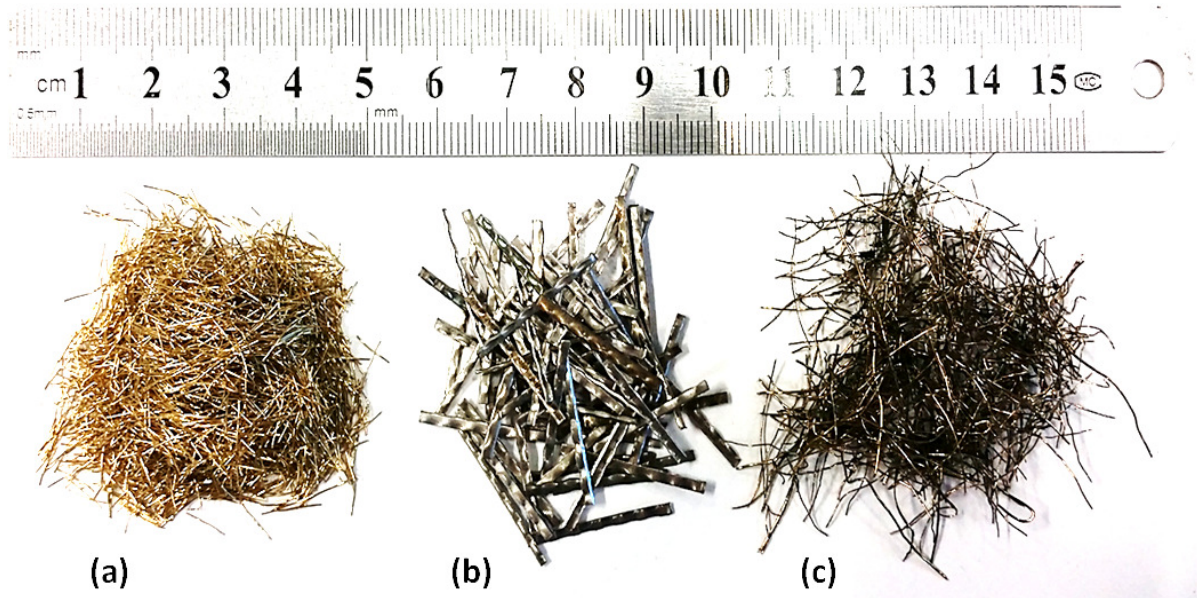
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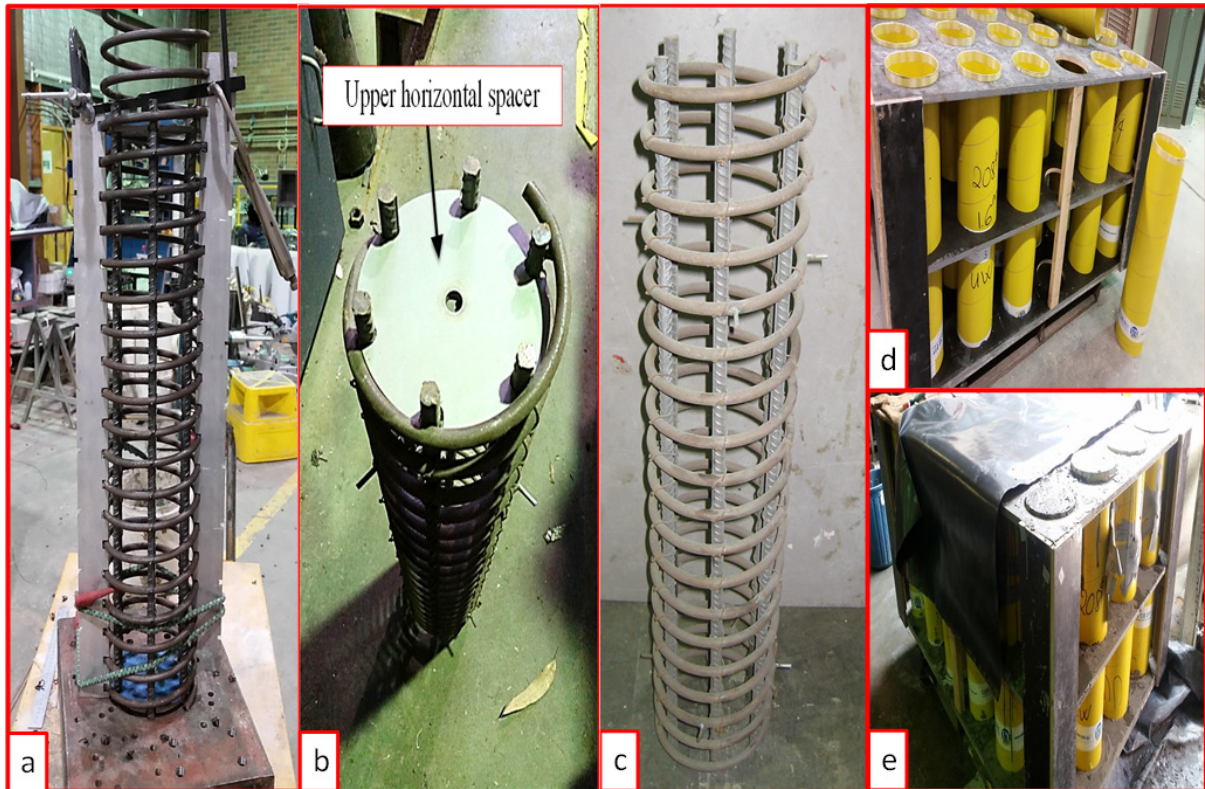
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**Figure 2.** The steel fibres used: (a) Micro straight steel fibre (MF); (b) Macro deformed steel fibre (DF); (c) Waste steel fibre (WF).

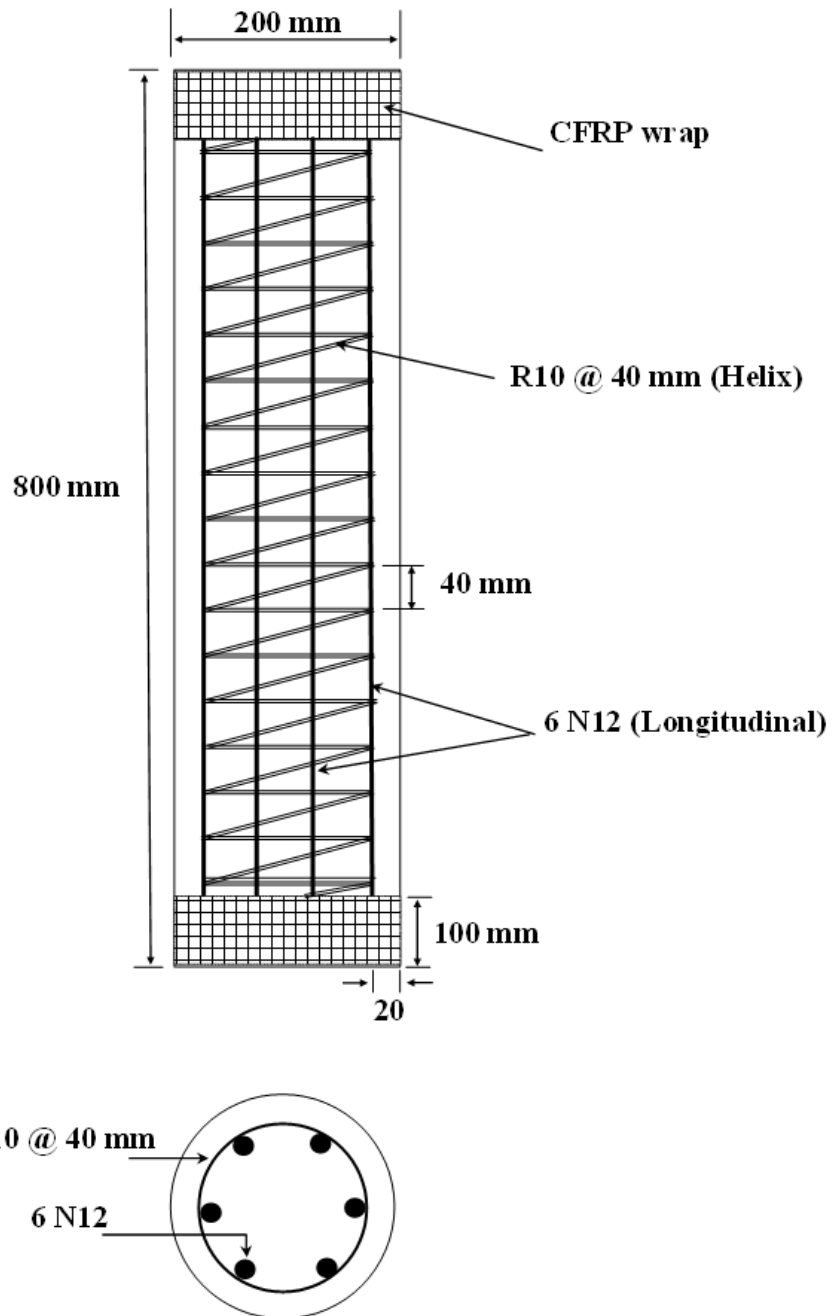
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**Figure 3.** The fabrication of specimens: (a) Assembling steel reinforcement frame; (b) Longitudinal steel bars positioning; (c) Steel reinforcement frame; (d) Specimen formwork; (e) Cast specimens.

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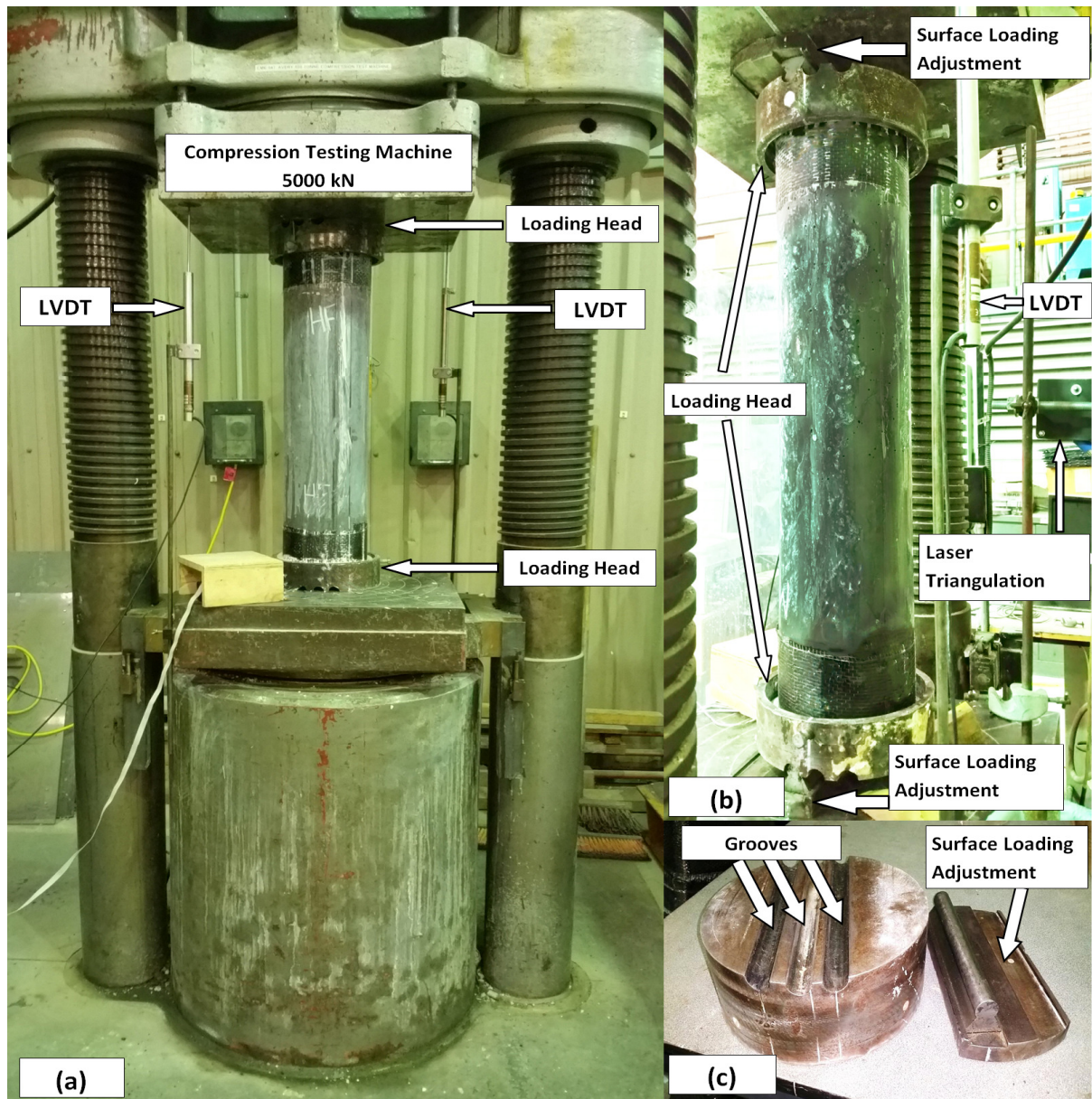


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**Figure 4.** Dimensions and reinforcement details of the tested specimens.



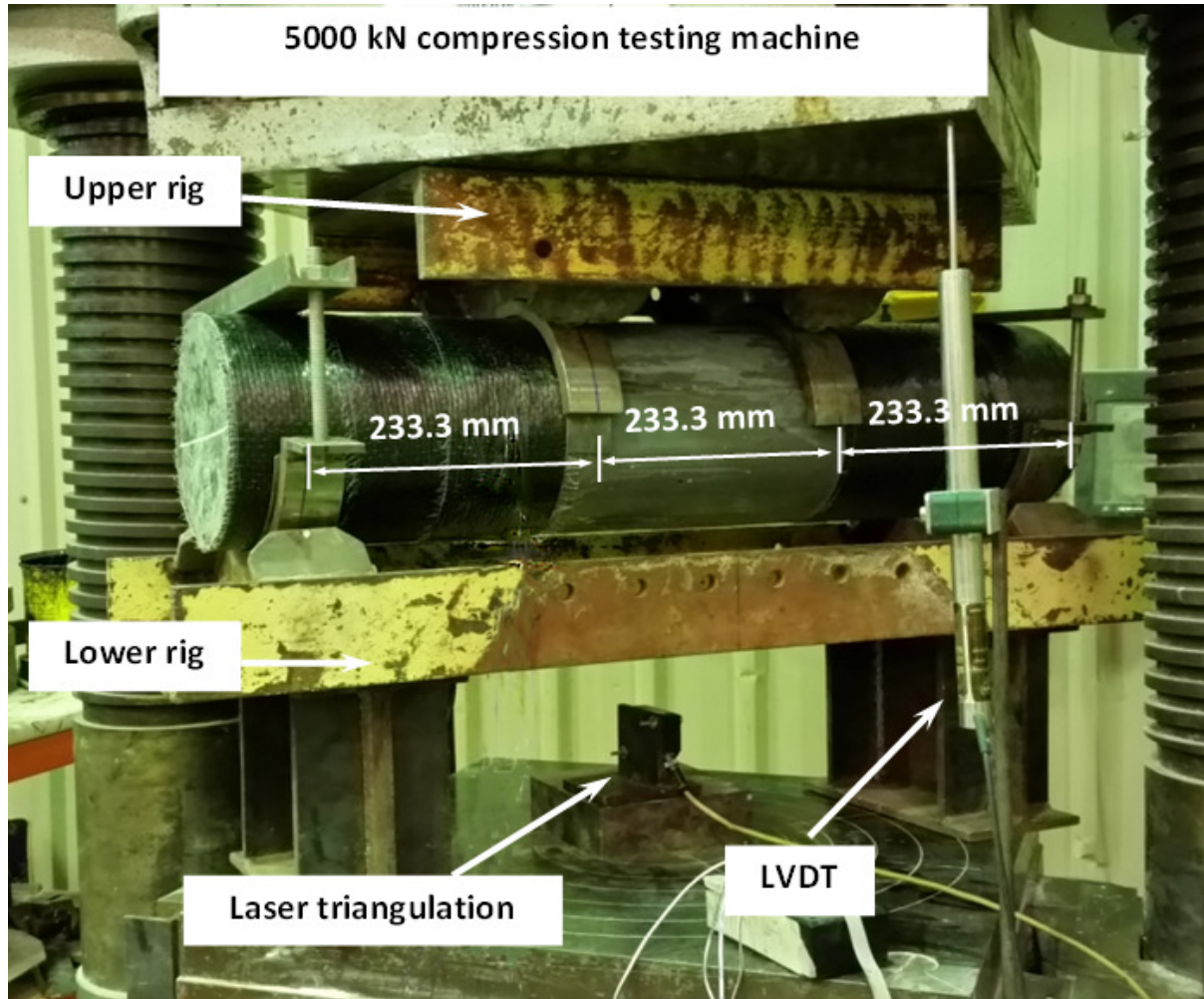
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**Figure 5.** The compression testing machine equipment: (a) Specimen HF-E0 concentrically loaded; (b) Specimen WHF-E25 eccentrically loaded; (c) Loading head details.

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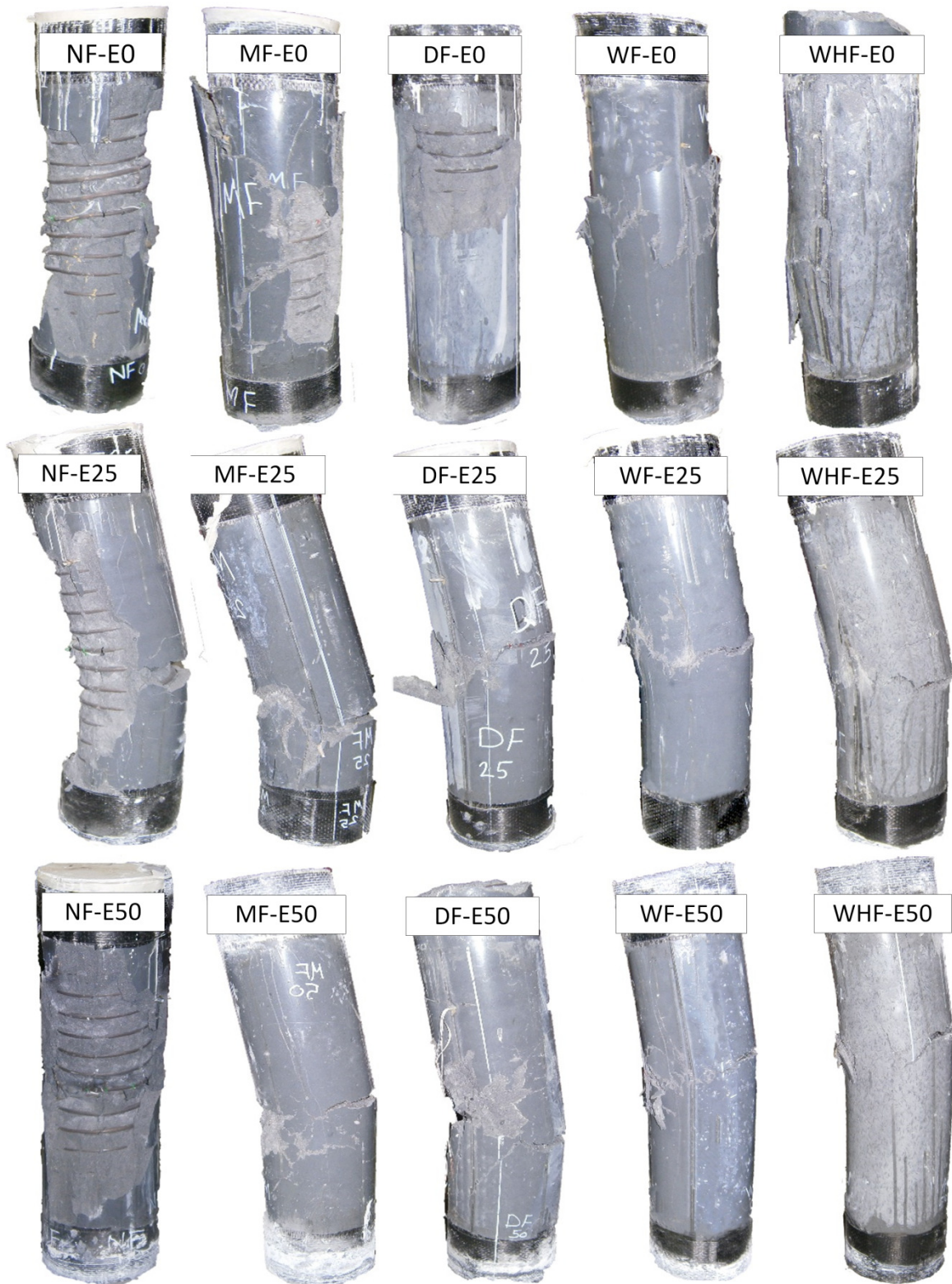
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**Figure 6.** The flexural load test equipment during testing Specimen WF-PB.



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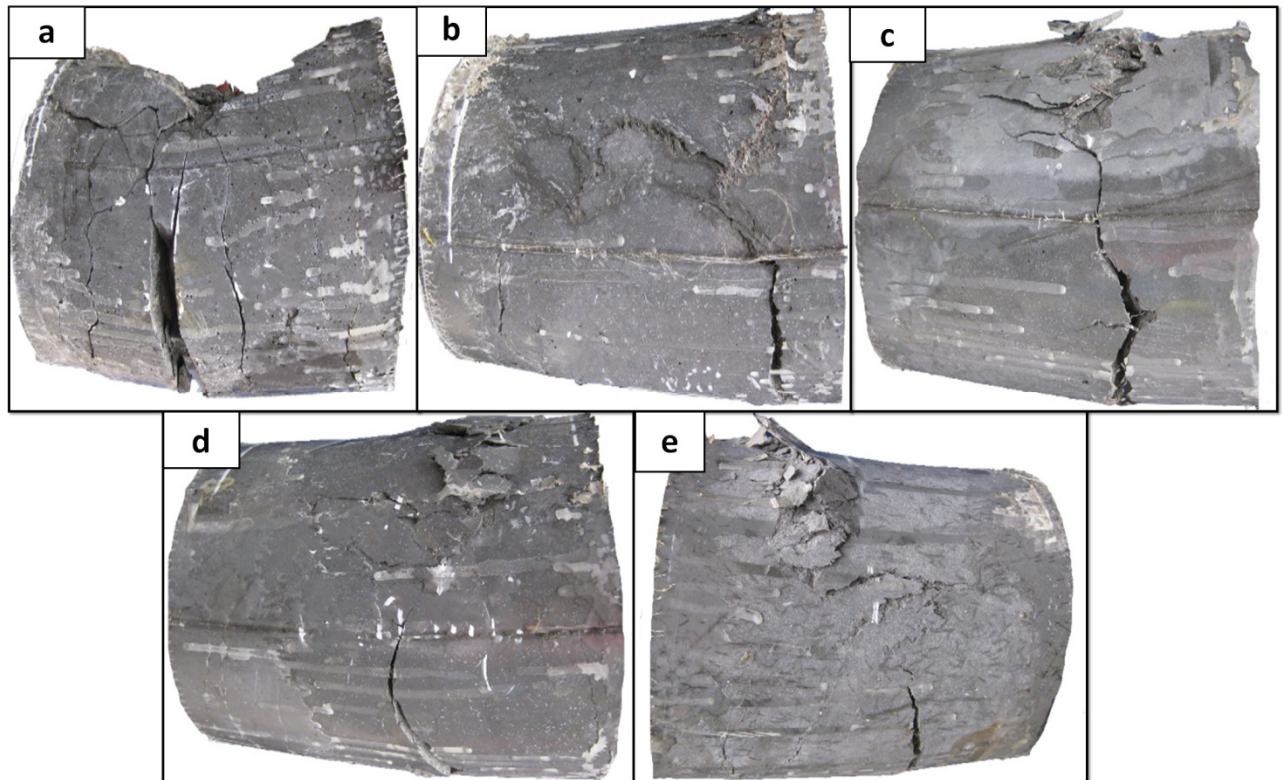
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**Figure 7.** Modes of failure of the tested specimens.

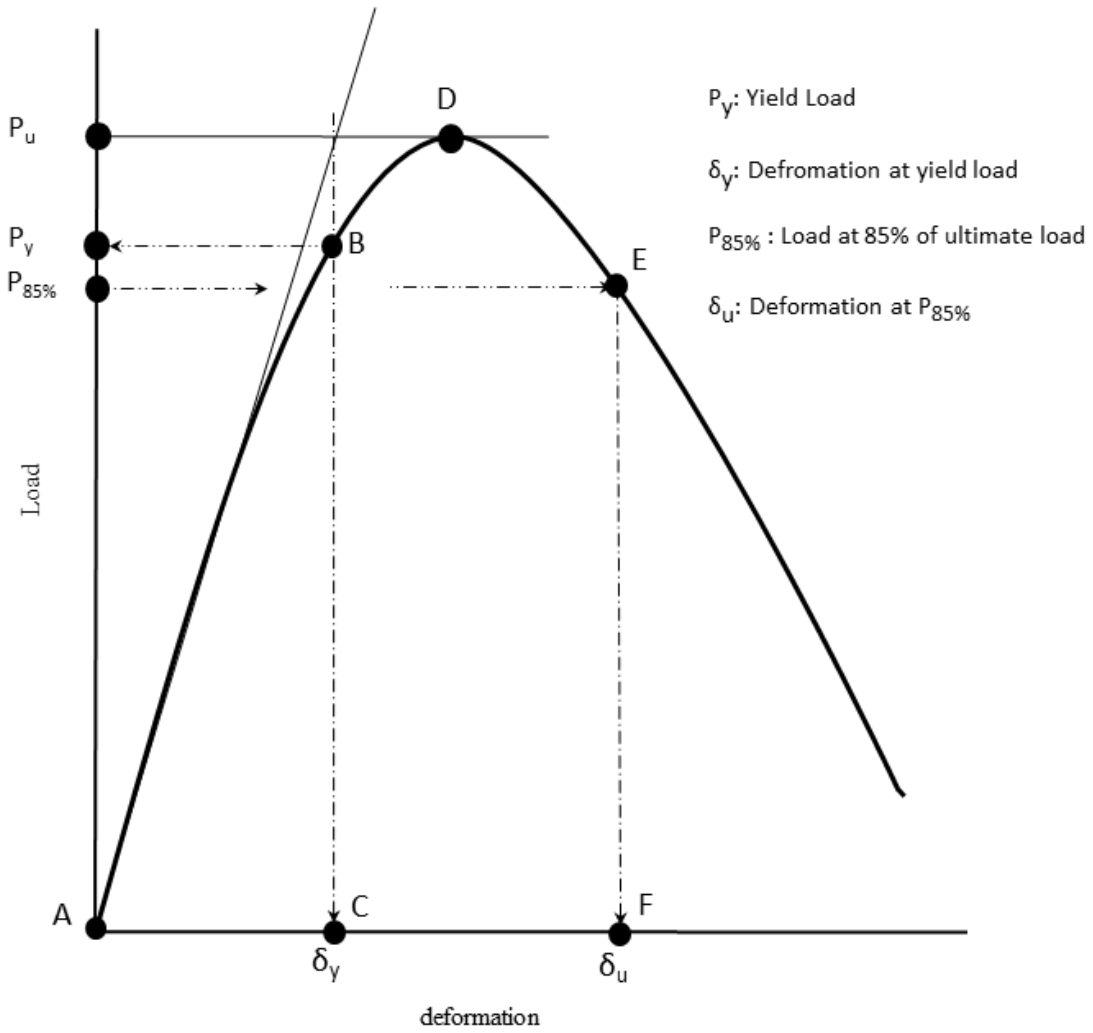
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**Figure 8.** Close-view of the specimens tested under flexural loading: a) Specimens NF-PB, b) Specimens MF-PB, c) Specimens DF-PB, d) Specimens WF-PB and e) Specimens WHF-PB.

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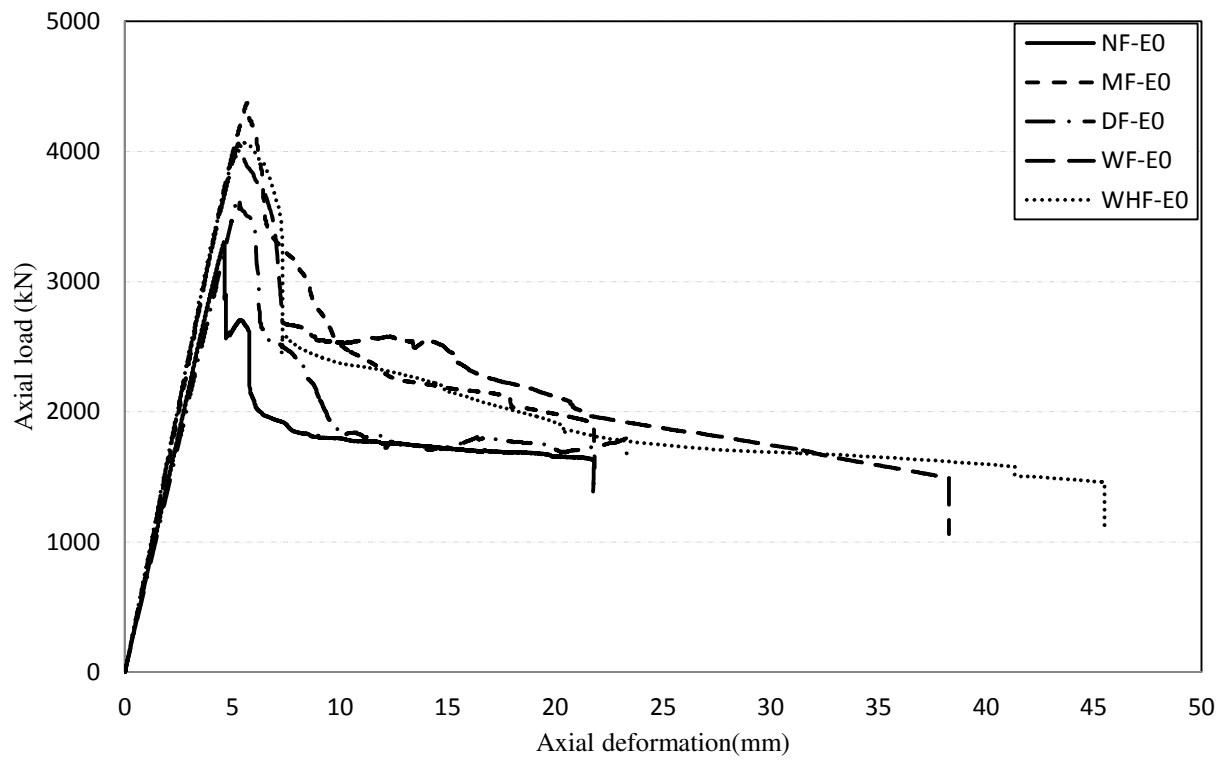


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**Figure 9.** Calculation of energy absorpion the tested specimens.

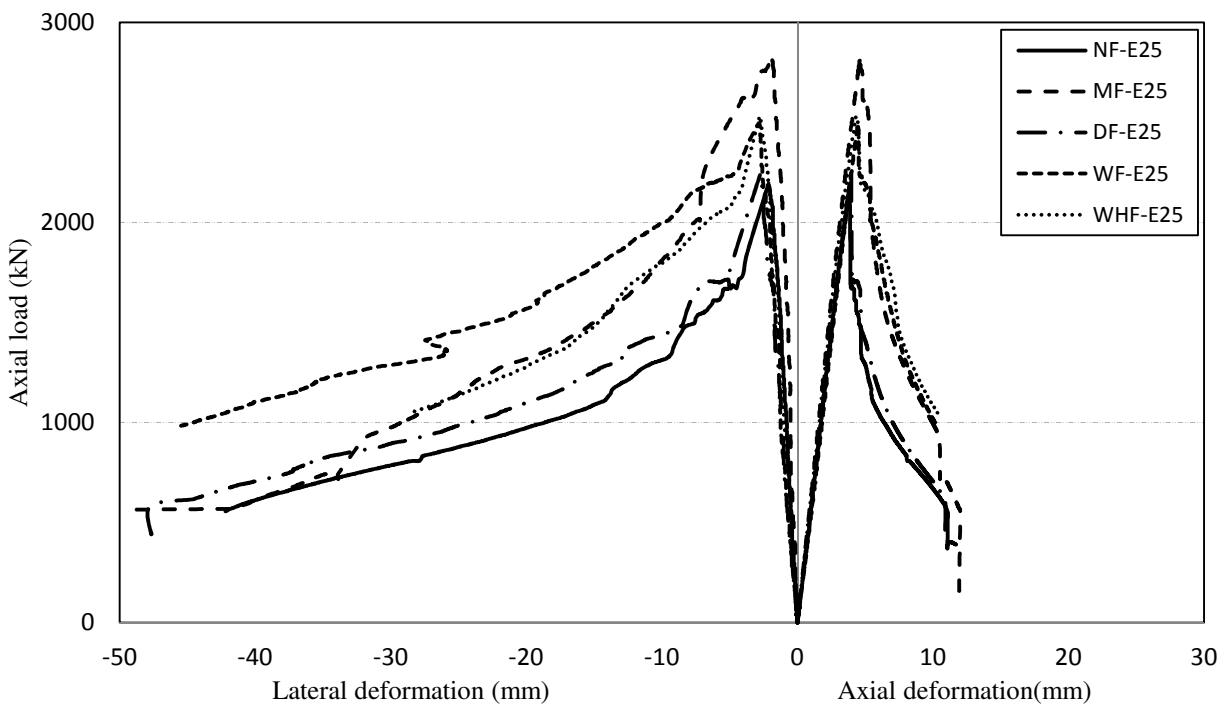


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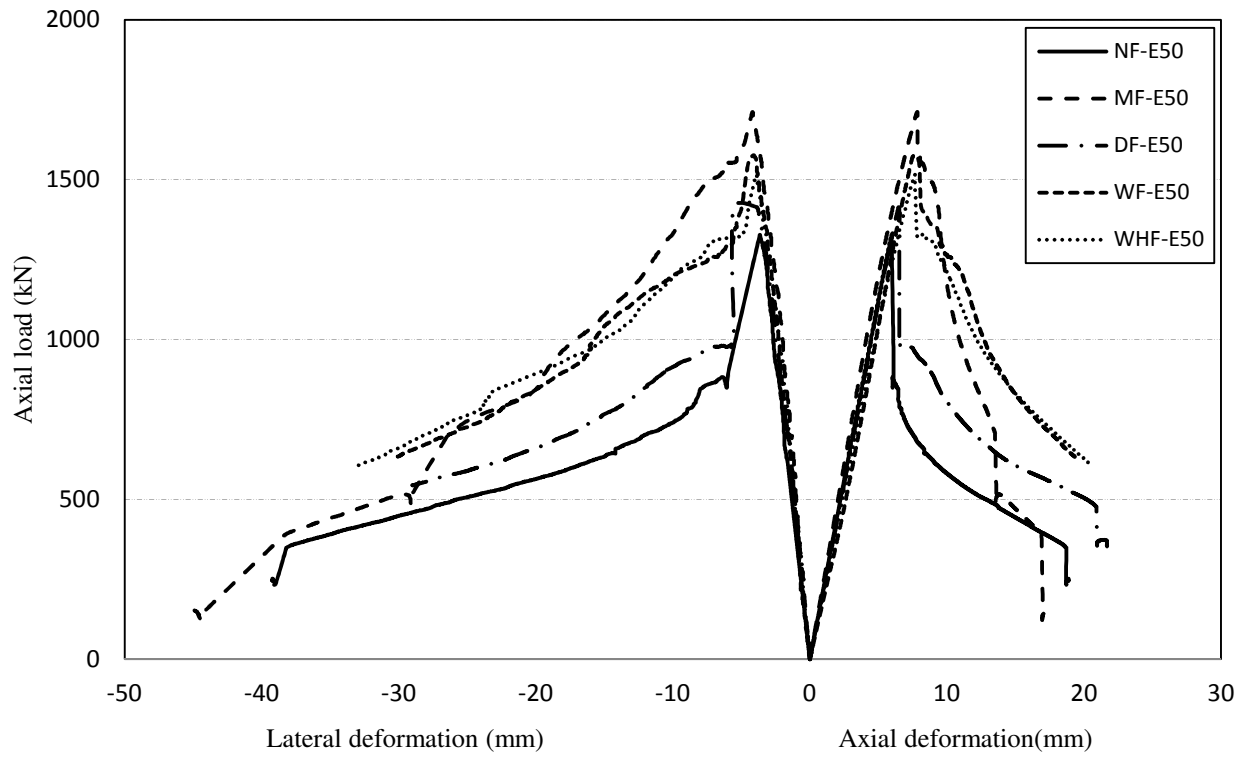


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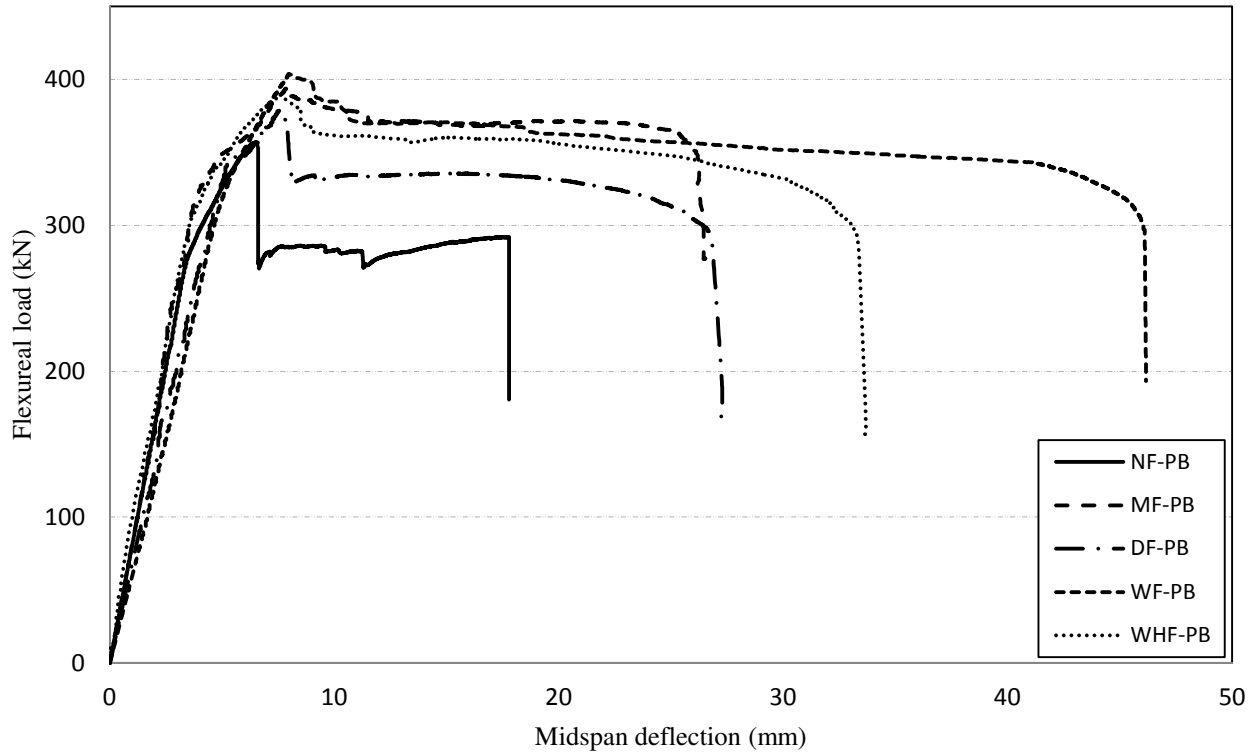
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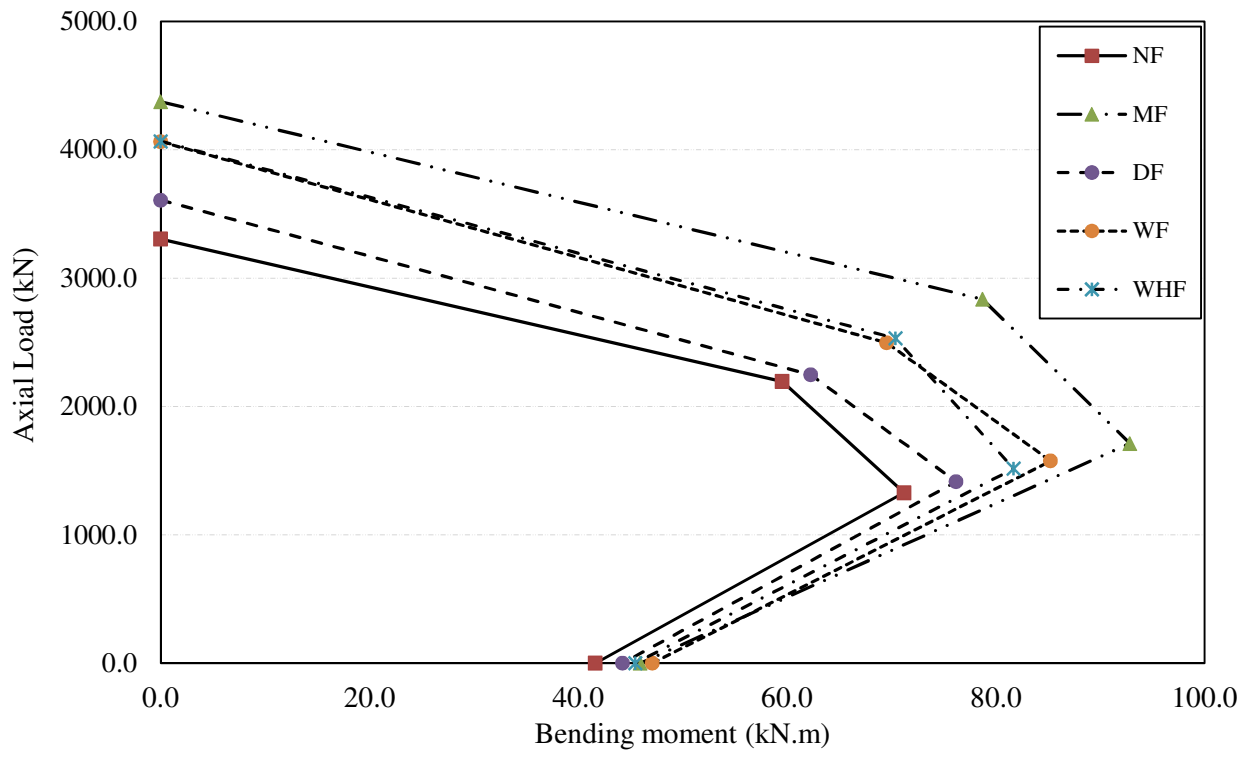


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**Figure 10.** The load-deformation curves of the specimens tested under: (a) concentric loading; (b) 25 mm eccentric loading; (c) 50 mm eccentric loading; (d) flexural loading.

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**Figure 11.** The experimental ( $P$ - $M$ ) interaction diagram of tested specimens.