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Theoretical Analysis of Double Logistic Distributed Activation Energy Model for Thermal Decomposition Kinetics of Solid Fuels

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Abstract

The distributed activation energy model (DAEM) has been widely used to analyze the thermal decomposition of solid fuels such as lignocellulosic biomass and its components, coal, microalgae, oil shale, waste plastics, and polymer etc. The DAEM with a single distribution of activation energies cannot describe those reactions well since the thermal decomposition normally involves multiple sub-processes of various components. The double DAEM employs a double distribution to represent the activation energies. The Gaussian distribution is usually used to represent the activation energies. However, it is not sufficiently accurate for addressing the activation energies in the initial and final stages of the thermal decomposition

1 reactions of solid fuels. Compared to the Gaussian distribution, the logistic distribution is
2 slightly thicker at the curve tail and suits better to describe the activation energy distribution.
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4 In this work, a theoretical analysis of the double logistic DAEM for the thermal
5 decomposition kinetics of solid fuels has been systematically investigated. After the
6 derivation of the double logistic DAEM, its numerical calculation method and the physical
7 meanings of the model parameters have been presented. Three typical types of simulated
8 double logistic DAEM processes have been obtained according to the overlapped situation of
9 two derivative conversion peaks, namely separated, overlapped and partially overlapped
10 processes. It is found that, for the partially overlapped process, the form of the minor peak
11 (overlapped peak or peak shoulder) depends on the values of the frequency factor and heating
12 rate. Considering the simulated processes and related examples from literature, the double
13 logistic DAEM has been remarked as a more reliable tool with abundant flexibility to explain
14 the thermal decomposition of various solid fuels. More accurate results are expected if the
15 double logistic DAEM is coupled with the computational fluid dynamics (CFD) simulation
16 for those reactions mentioned above.
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34 **Key words:** Distributed activation energy model (DAEM); Solid fuels; Thermal
35 decomposition; Kinetics; Simulation; Logistic distribution
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41 **1 Introduction**

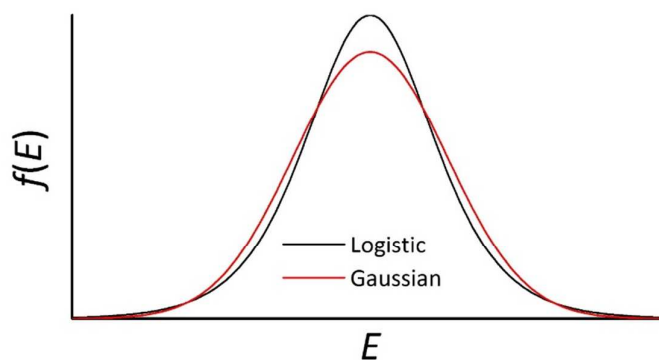
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43 When solid fuels undergo thermal processing, they decompose and produce gases and
44 volatiles.^{1,2} Depending on the processing temperature and atmosphere, these processes can be
45 classified as pyrolysis, gasification and combustion.^{3,4} Pyrolysis is the thermal decomposition
46 in non-oxidizing environment, resulting in the production of a liquid, solid and gases,^{5,6} and
47 the yields of these products rely on the feedstock and processing conditions.^{7, 8} The
48 combustion of solid fuels first undergo endothermic pyrolysis to produce combustible gases,
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1 which are subsequently combusted to supply heat required to produce further gases.⁹
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3 Gasification is the transformation of solid fuels into a gaseous fuel, which hinges on the
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5 gasifying medium on the solid fuels, the temperature and pressure.¹⁰
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8 A comprehensive understanding of the thermal decomposition kinetics of solid fuels
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10 plays an important role in the computational fluid dynamics (CFD) simulation,¹¹⁻¹⁴ which is a
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12 useful tool in reactor design and process optimization.¹⁵⁻²⁰ Many kinetic models have been
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14 proposed to describe the thermal decomposition kinetics of solid fuels.²¹⁻²³ The basic model
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16 used to describe the thermal decomposition kinetics of biomass components is the single first
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18 order reaction (SFOR) model.²⁴ However, the SFOR model is an empirical model, which is
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20 limited to a single reaction process occurring with a single activation energy.²⁵
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23 The conventional complex model applied to describe the thermal decomposition kinetics
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25 of solid fuels is the distributed activation energy model (DAEM).^{13, 26-28} In this model, it is
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27 assumed that the thermal decomposition of different components in the solid fuels occurs
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29 through a series of reactions with their own activation energies which are described by a
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31 continuous distribution function.^{29, 30} In general, the activation energy distribution is presented
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33 by the Gaussian distribution function. However, it is not sufficiently accurate for addressing
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35 the activation energies in the initial and final stages of the thermal decomposition reactions of
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37 solid fuels.³¹ Cai and co-workers³² originally proposed to use the logistic distribution to
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39 represent the activation energy distribution and successfully applied it for describing cellulose
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41 pyrolysis kinetics.³³ The differences between logistic and Gaussian distributions with the
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43 same distribution parameters values are presented in Figure 1, which shows that the logistic
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45 distribution has slightly thicker tails than the Gaussian distribution, thus offering improved
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47 accuracy for describing the thermal decomposition kinetics of solid fuels. Fiori and
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49 co-workers³⁴ found that the logistic DAEM gave a better fitting than the Gaussian DAEM for
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51 the pyrolysis kinetics of grape residues. Jain and co-workers³⁵ concluded that the logistic
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53 DAEM matched well with the experimental kinetic curves of coal pyrolysis at different
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1 heating rates. Xiong and co-workers³⁶ simulated the fast pyrolysis of biomass in fluidized bed
2 reactors with a coupled logistic DAEM and CFD model and found that the kinetics with
3 distributed activation energies could affect the predicted average value of the exit vapor-phase
4 tar flux and its statistical distribution, compared to the single-valued activation-energy
5 kinetics. Concerning the chemical kinetic analysis by using the logistic function, Burnham³⁷
6 also gave the examples of use and misuse of the logistic function for modeling chemical
7 kinetics and pointed out that some works, such as making comparisons to kinetic parameters
8 derived only with using a single heating rate experiment to fit models, might not qualify as
9 kinetic analysis methods.
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Figure 1. Differences between the logistic and Gaussian distributions with same distribution parameter values

The thermal decomposition of some solid fuels, such as biomass and coal, usually involves multiple decomposition processes due to varying kinetic behaviors of their components.^{38, 39} The DAEM can successfully describe a single process, but difficult to fit multiple sub-processes.⁴⁰ Burnham and co-workers^{25, 31} developed the kinetics software LLNL (currently Kinetics2015) and proposed some comprehensive models with parallel Gaussian activation energy distributions or combination of the one sigmoidal model and the other Gaussian DAEM for the decomposition of polymers and oil shale. Recently, de Filippis and

1 co-workers⁴¹ proposed the double DAEM, which uses a double distribution function to
2 represent the activation energy distribution. As presented in Supporting Information Table S1,
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4 this model was confirmed later as a suitable tool for explaining the pyrolysis kinetic behaviors
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6 of microalgae,^{40, 42} coal,^{35, 40} poly-vinyl chloride (PVC) and poly-methyl methacrylate
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8 (PMMA),⁴³ olive residues,⁴⁴ plant oil asphalt⁴⁵ and raw and torrefied beech wood xylan
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10 samples⁴⁶.

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14 The aim of this study is to perform a comprehensive theoretical analysis to the thermal
15 decomposition processes of solid fuels that can be described by the double logistic DAEM.
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17 The structure of the paper is arranged as follows. Section 1 provides the background and aim
18 of this work; Section 2 introduces the theory of the double logistic DAEM; Section 3 presents
19 the numerical calculation method for the double logistic DAEM, followed by an investigation
20 of physical meanings of the model parameters in Section 4; Section 5 gives the possible
21 processes related to the thermal decomposition of solid fuels, with discussions on some
22 representative examples in publications; Conclusions of the present work are given in Section
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2 Double Logistic DAEM

The DAEM can be deduced based on the following assumptions: (1) the decomposition of complex solid fuels contains a large number of independent and parallel first order reactions; (2) each reaction has its own activation energy and all reactions share the same frequency factor; (3) the activation energies of all reactions can be described by a continuous distribution.^{26, 31, 32, 47} The equation of the DAEM in the form of conversion can be obtained:

$$\alpha(t) = \int_0^{\infty} \left\{ 1 - \exp \left[- \int_0^t A \exp \left(- \frac{E}{RT} \right) dt \right] \right\} f(E) dE \quad (1)$$

where α is conversion degree (dimensionless), A is the frequency factor (s^{-1}), E is the activation energy ($J mol^{-1}$), R is the universal gas constant ($8.3145 J K^{-1} mol^{-1}$), t is the time (s), T is the temperature (K), and $f(E)$ is the activation energy distribution ($mol J^{-1}$).

The equation of the DAEM in the form of the conversion rate can be obtained by differentiating Equation (1) with respect to t :

$$\frac{d\alpha}{dt}(t) = \int_0^{\infty} A \exp \left[- \frac{E}{RT} - \int_0^t A \exp \left(- \frac{E}{RT} \right) dt \right] f(E) dE \quad (2)$$

The experimental kinetic data is usually obtained under linear heating programs where the temperature increases with time by a constant heating rate.

$$\beta = \frac{dT}{dt} \quad (3)$$

where β is the heating rate ($K s^{-1}$).

The equations of the DAEM under the linear heating program can be expressed by the following equations (Equations (4) and (5)):

$$\alpha(T) = \int_0^{\infty} \left\{ 1 - \exp \left[- \frac{A}{\beta} \int_0^T \exp \left(- \frac{E}{RT} \right) dT \right] \right\} f(E) dE \quad (4)$$

$$\frac{d\alpha}{dT}(T) = \int_0^{\infty} \frac{A}{\beta} \exp \left[- \frac{E}{RT} - \frac{A}{\beta} \int_0^T \exp \left(- \frac{E}{RT} \right) dT \right] f(E) dE \quad (5)$$

The Gaussian distribution function is widely used to represent the activation energy distribution.^{26, 48, 49} Whereas it is inappropriate to address the initial and final stages of thermal decomposition of solid fuels. In this regard, the logistic distribution has slightly thicker tails⁵⁰ and is reported to be more suitable to describe the thermal decomposition kinetics of solid fuels.^{34, 35} Therefore, the logistic distribution for the representation of the activation energies is considered in this work.

In order to better describe the thermal decomposition of solid fuels, which involves two sub-processes, the double logistic distribution is used to represent the activation energy distribution:

$$f(E) = wf_1(E) + (1-w)f_2(E) \quad (6)$$

$$f_1(E) = \frac{\pi}{\sqrt{3}\sigma_1} \frac{\exp\left[-\pi(E-\mu_1)/(\sqrt{3}\sigma_1)\right]}{\left\{1 + \exp\left[-\pi(E-\mu_1)/(\sqrt{3}\sigma_1)\right]\right\}^2} \quad (7)$$

$$f_2(E) = \frac{\pi}{\sqrt{3}\sigma_2} \frac{\exp\left[-\pi(E-\mu_2)/(\sqrt{3}\sigma_2)\right]}{\left\{1 + \exp\left[-\pi(E-\mu_2)/(\sqrt{3}\sigma_2)\right]\right\}^2} \quad (8)$$

where w is a constant, $0 < w < 1$, μ is the mean value (J mol^{-1}) and σ is the standard deviation (J mol^{-1}) of the activation energy distribution, the subscripts 1 and 2 represent the values related to the first and second sub-processes.

3 Numerical calculation

There are an inner dT integral and an outer dE integral in Equations (4) or (5), which result in difficulties in solving them. For this reason, a numerical approach for calculating the DAEM is developed in this section.

In fact, the inner dT integral is the temperature integral,⁵¹⁻⁵³ which can be expressed in the following form:

$$\int_0^T \exp\left(-\frac{E}{RT}\right) dT = \frac{E}{R} \int_{E/(RT)}^{\infty} \frac{\exp(-x)}{x^2} dx = \frac{E}{R} P\left(\frac{E}{RT}\right) \quad (9)$$

$$P\left(\frac{E}{RT}\right) = \frac{\exp[-E/(RT)]}{E/(RT)} - \int_{E/(RT)}^{\infty} \frac{\exp(-x)}{x} dx \quad (10)$$

In mathematics, there is a special integral named the exponential integral:

$$\text{Ei}(x) = -\int_{-x}^{\infty} \frac{e^{-t}}{t} dt \quad (11)$$

The exponential integral can be easily solved by using a specific function “ExpIntegralEi” in the Mathematica software system.⁵⁴ Substituting Equations (10) and (11) into Equation (9) results in

$$\int_0^T \exp\left(-\frac{E}{RT}\right) dT = T \exp\left(-\frac{E}{RT}\right) + \frac{E}{R} \text{Ei}\left(-\frac{E}{RT}\right) \quad (12)$$

As for the outer dE integral, the upper integration limit is ∞ . According to Güneş and Güneş,⁵⁵ if the upper integration limit is replaced by a value high enough, there is almost no deviation from the real value. The effect of different upper integration limits ($\mu+3\sigma$, $\mu+10\sigma$ and $\mu+30\sigma$, where μ is the greater one of μ_1 and μ_2 , σ is the greater one of σ_1 and σ_2) on the numerical results of the double logistic DAEM was investigated and shown in **Figure 2**. It can be observed that the $d\alpha/dT - T$ curves would converge into a curve with increasing of upper integration limit values. Since there was almost no deviation from the final converge curve when the upper integration limit increased to $\mu+10\sigma$, $\mu+10\sigma$ is selected as the upper integration limit of the outer dE integral for further calculation of the double logistic DAEM. Then, the outer dE integral can be converted to a normal definite integral, as shown in Equations (13) and (14).

$$\begin{aligned} \alpha(T) &= \int_0^{\infty} \left\{ 1 - \exp\left[-\frac{A E}{\beta R} P\left(\frac{E}{RT}\right)\right] \right\} f(E) dE \\ &\approx \int_0^{\mu+10\sigma} \left\{ 1 - \exp\left[-\frac{A E}{\beta R} P\left(\frac{E}{RT}\right)\right] \right\} f(E) dE \end{aligned} \quad (13)$$

$$\begin{aligned} \frac{d\alpha}{dT}(T) &= \int_0^{\infty} \frac{A}{\beta} \exp\left[-\frac{E}{RT} - \frac{A E}{\beta R} P\left(\frac{E}{RT}\right)\right] f(E) dE \\ &\approx \int_0^{\mu+10\sigma} \frac{A}{\beta} \exp\left[-\frac{E}{RT} - \frac{A E}{\beta R} P\left(\frac{E}{RT}\right)\right] f(E) dE \end{aligned} \quad (14)$$

For numerical calculations of Equations (13) and (14), Simpson's rule,⁵⁶ a common method for numerical integration, was used. **Figure 3** shows the numerical calculation flowchart of the double logistic DAEM.

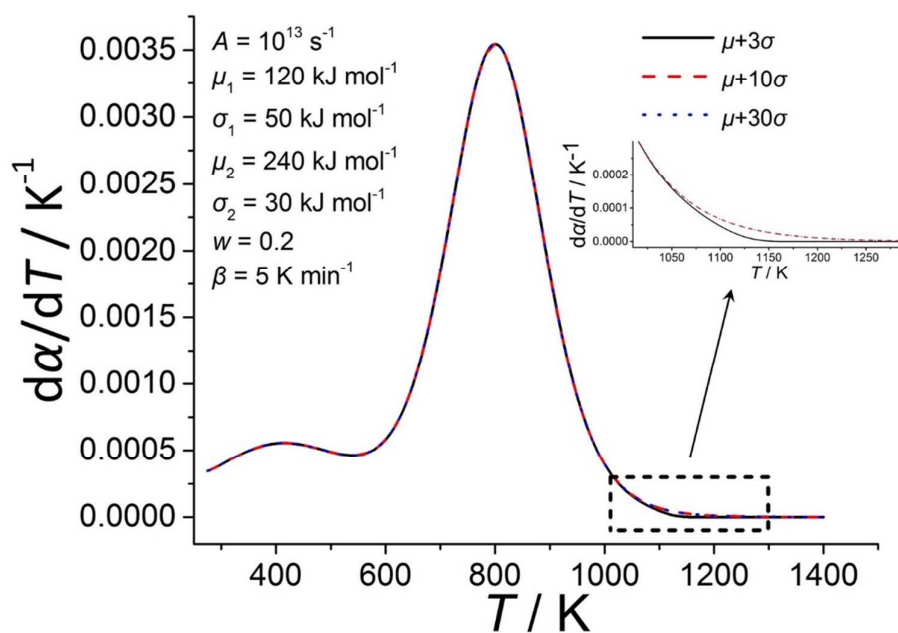
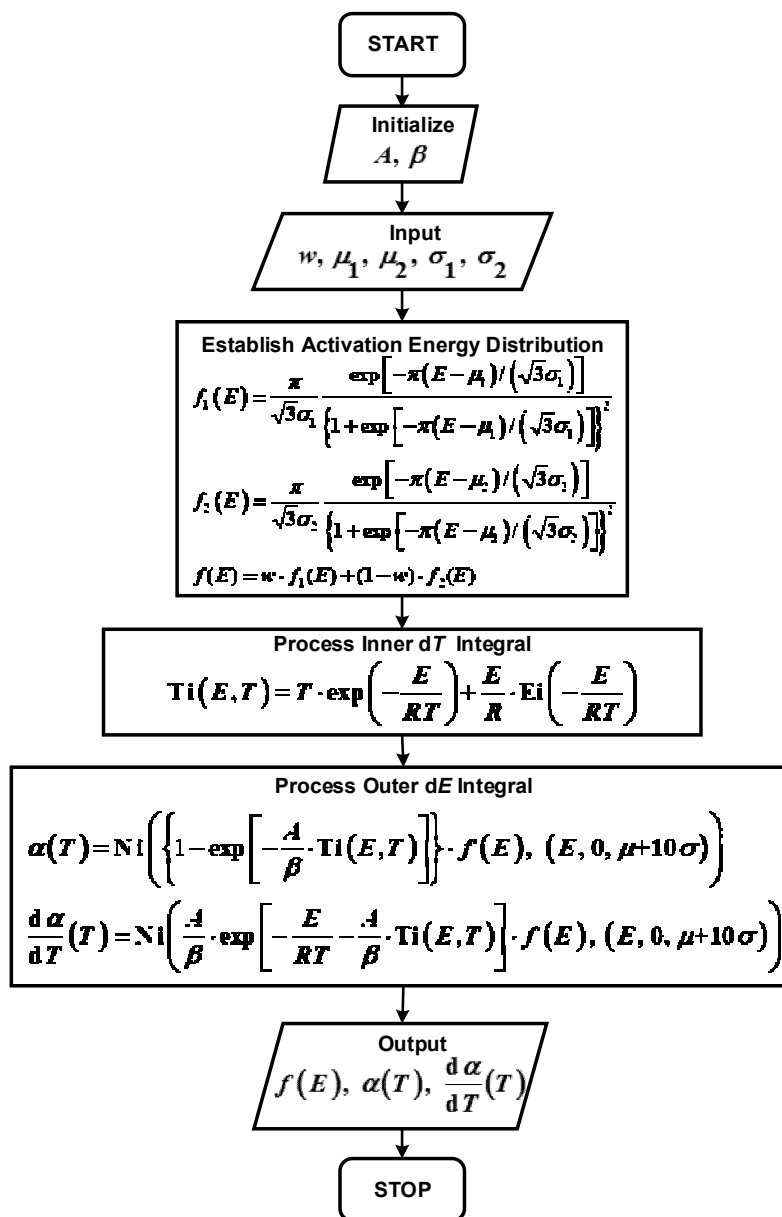


Figure 2. Effect of upper integration limit on numerical results of double logistic DAEM



42 **Figure 3.** Numeical calualtion flowchart of double logistic DAEM (Ei: Exponential integral;

43 Ti: Temperature integral; Ni: Numerical integration function)

44 4 Physical meaning of model parameters

45 The influences of various parameters on α for the Gaussian DAEM can be found in our
46 previous study.⁵⁷ In fact, the $d\alpha/dT$ data is more sensitive to reveal model details.^{58, 59}

47 Therefore, in this section, the influences of the model parameters on the $d\alpha/dT - T$ curve are

investigated and the physical meanings of model parameters are presented.

Substituting Equation (6) into Equations (4) and (5) leads to:

$$\begin{aligned} \alpha(T) &= w \cdot \int_0^\infty \left\{ 1 - \exp \left[-\frac{A}{\beta} \int_0^T \exp \left(-\frac{E}{RT} \right) dT \right] \right\} f_1(E) dE \\ &\quad + (1-w) \cdot \int_0^\infty \left\{ 1 - \exp \left[-\frac{A}{\beta} \int_0^T \exp \left(-\frac{E}{RT} \right) dT \right] \right\} f_2(E) dE \\ &= w \cdot \alpha_1(T) + (1-w) \cdot \alpha_2(T) \end{aligned} \quad (15)$$

$$\begin{aligned} \frac{d\alpha}{dT}(T) &= w \cdot \int_0^\infty \frac{A}{\beta} \exp \left[-\frac{E}{RT} - \frac{A}{\beta} \int_0^T \exp \left(-\frac{E}{RT} \right) dT \right] f_1(E) dE \\ &\quad + (1-w) \cdot \int_0^\infty \frac{A}{\beta} \exp \left[-\frac{E}{RT} - \frac{A}{\beta} \int_0^T \exp \left(-\frac{E}{RT} \right) dT \right] f_2(E) dE \\ &= w \cdot \frac{d\alpha_1}{dT}(T) + (1-w) \cdot \frac{d\alpha_2}{dT}(T) \end{aligned} \quad (16)$$

From Equations (15) and (16), it can be obtained that the double DAEM can be considered as the weighted sum of two single DAEMs and w is the weight parameter. **Figure 4** shows the influences of w on the numerical results of the double logistic distribution and the double logistic DAEM. It can be also elucidated that w can affect the height of each $d\alpha/dT$ peak from **Figure 4**.

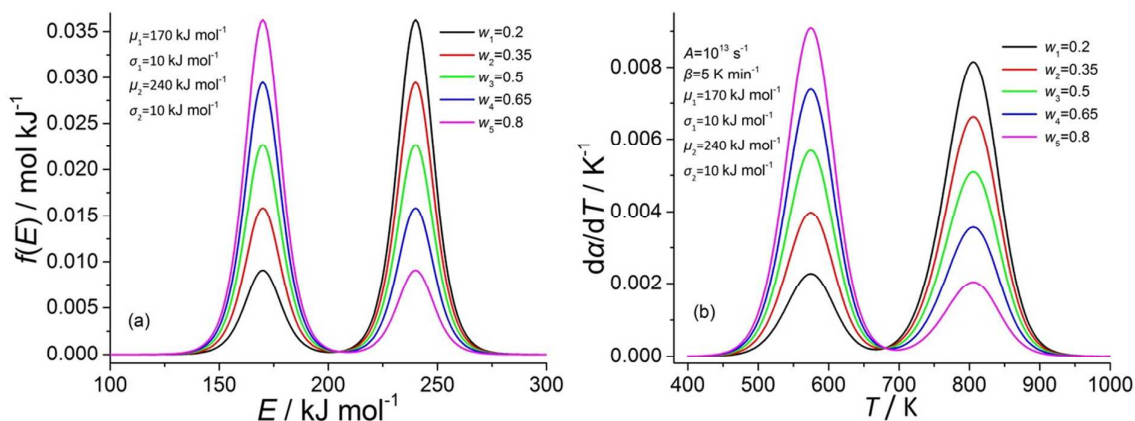


Figure 4. Effect of w on numerical results of (a) double logistic distribution and (b) double logistic DAEM

Since the double DAEM is considered as the weighted sum of two single DAEMs, the single DAEM can be used to investigate the physical meaning of μ and σ in the logistic DAEM. The study is carried out by changing each parameter, taking one parameter at a time and keeping the remaining parameters unchanged.

Figure 5 shows the effect of μ on the numerical results of the logistic distribution and the logistic DAEM. It can be observed that increasing μ can result in the change of the $d\alpha/dT$ peak location. Along with the increase of μ , the $d\alpha/dT - T$ curve is shifted to higher temperature. This is consistent with the kinetic theory that the higher activation energy needs higher temperature to trigger the reaction.^{60, 61} Therefore, μ can be considered as the location parameter in the logistic DAEM while increasing μ may cause a decrease in $d\alpha/dT$ peak height.

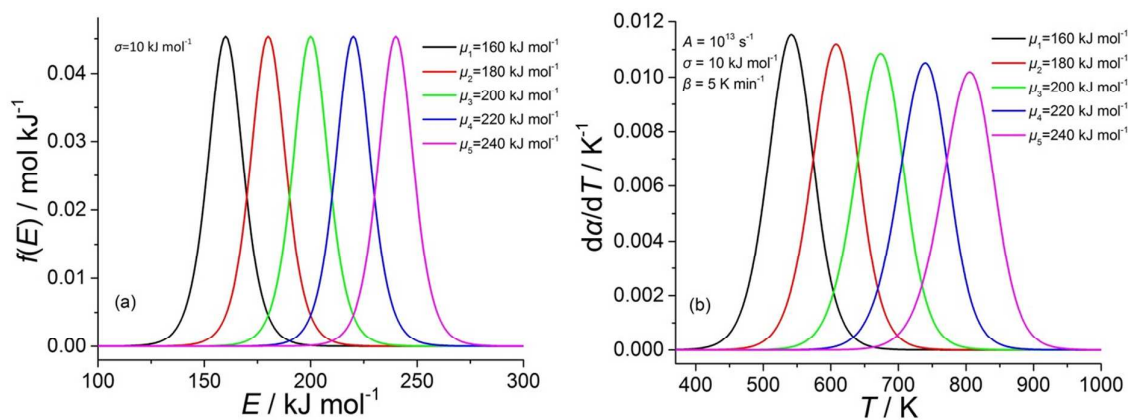


Figure 5. Effect of μ on numerical results of (a) logistic distribution and (b) logistic DAEM

Figure 6 shows the effect of σ on the numerical results of the logistic distribution and the logistic DAEM. It can be observed that increasing σ exerts significant effect on the $d\alpha/dT$ peak height while the $d\alpha/dT - T$ curve becomes broader and shallower with increasing σ . Therefore, σ can be suggested as the shape parameter of the logistic DAEM.

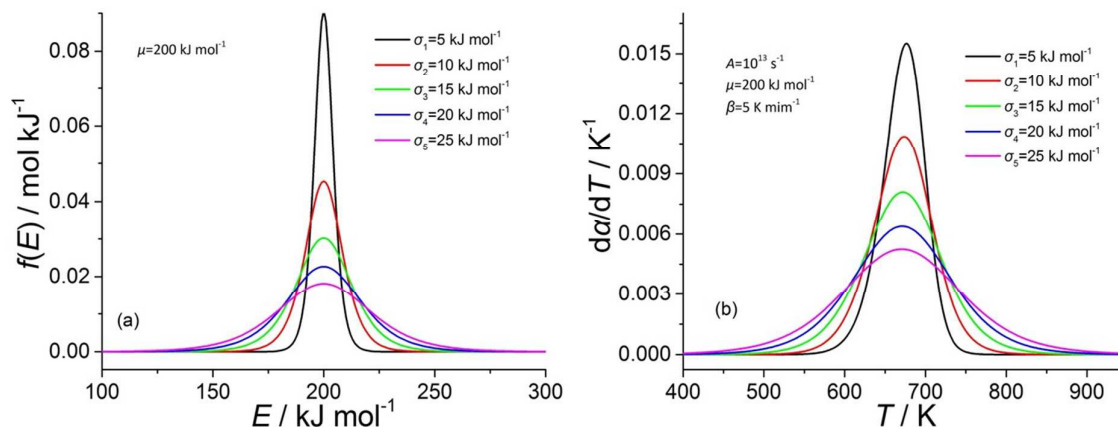


Figure 6. Effect of σ on numerical results of (a) logistic distribution and (b) logistic DAEM

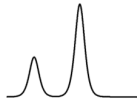

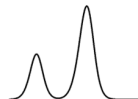
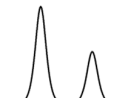

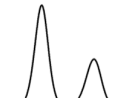


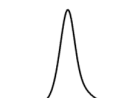
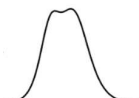

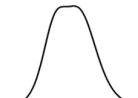
5 Typical double logistic DAEM processes

To present a wide range of thermal decomposition processes, some theoretical double logistic DAEM processes are simulated. All simulated $\alpha - T$ and $da/dT - T$ curves are calculated in 10,000 temperature points ($300 \text{ K} \leq T \leq 1300 \text{ K}$). According to a series of pre-calculations, it was found that the shape of the da/dT curve mainly depends on the shape of the corresponding double logistic distribution, like μ_1 , μ_2 , σ_1 , σ_2 and w . According to the results about the double distribution from Robertson and co-workers,⁶² the distribution shape depends on the values of the following three parameters: w , $r = \sigma_2/\sigma_1$ and $u = (\mu_2 - \mu_1)/\sigma_1$ when the modality of the distribution shape is unaffected by location and scale changes. Based on the above conclusion, without loss of generality, the parameters μ_2 and σ_2 are set as fixed values ($\mu_2 = 240 \text{ kJ mol}^{-1}$ and $\sigma_2 = 20 \text{ kJ mol}^{-1}$) for the simulation of the double logistic DAEM processes. The values of the other parameters were set as follows: μ_1 (from 120 to 240 kJ mol⁻¹ with an interval of 10 kJ mol⁻¹), σ_1 (from 1.0 to 50.0 kJ mol⁻¹ with an interval of 1.0 kJ mol⁻¹), A (from 10^{11} to 10^{21} s^{-1} with a ratio of 10), w (from 0.2 to 0.8 with an interval of 0.05)





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3 and β (from 0.125 to 128 K min⁻¹).
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5 According to the shapes of the simulated $d\alpha/dT$ curves, those simulated double logistic
6 DAEM processes can be divided into three types: (1) separated process; (2) overlapped
7 process; and (3) partially overlapped process. The corresponding $f(E)$, $\alpha - T$ and $d\alpha/dT - T$
8 curves are listed in **Table 1**. Some examples of the thermal decomposition of solid fuels
9 corresponding to the above typical processes are also presented in **Table 1**.
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Table 1. Typical processes described by double logistic DAEM

No.	Name	Typical curves			Characteristics	Examples from literature
		$f(E)$ curve	$\alpha - T$ curve	$d\alpha/dT - T$ curve		
1	Separated process				<ul style="list-style-type: none"> There are two significantly separate peaks in the $d\alpha/dT$ curve. The left peak value is lower than the right peak value. 	Pyrolysis of oil shale ⁴⁹
						
2	Overlapped process				<ul style="list-style-type: none"> There is one sharp peak in the $d\alpha/dT$ curve. There is one flat peak in the $d\alpha/dT$ curve. 	Combustion of coal and biomass char blends ⁶⁴
						

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3	Partially overlapped process		<ul style="list-style-type: none"> ● There are two partially overlapped peaks in the da/dT curve. ● The left peak value is lower than the right peak value. 	Pyrolysis of Russian coal (anthracite) ⁴¹
			<ul style="list-style-type: none"> ● There are two partially overlapped peaks in the da/dT curve. ● The left peak value is higher than the right peak value. 	Pyrolysis of Sulcis coal (Italian sub-bituminous coal) ⁴¹
			<ul style="list-style-type: none"> ● There is one peak in the da/dT curve. ● There is a peak shoulder in the left side of the peak. 	Pyrolysis of cotton stalk, pine wood and wheat straw (lignocellulosic biomass) ³⁰ Pyrolysis of plant oil asphalt ⁴⁵ Pyrolysis of poly-methyl methacrylate (PMMA) ⁴³
			<ul style="list-style-type: none"> ● There is one peak in the da/dT curve. ● There is a peak shoulder in the right side of the peak. 	Pyrolysis of microalgae ⁴²

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3 (1) Separated processes
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5 The main characteristic of the first type is that there are two separate peaks in the
6 $d\alpha/dT$ curve. In this type of process, there are two distinguishable sub-processes,
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8 which occur in completely different temperature ranges.
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11 There were several examples corresponding to this type of process in
12 publications. Tiwari and Deo⁴⁹ investigated the pyrolysis of oil shale, which involved
13 the organic and carbonate decomposition. The organic decomposition has been
14 reported between 250 and 500 °C while the carbonate decomposition commenced at
15 525 °C or above depending on the heating rate. In addition, the derivative conversion
16 curves of oil shale pyrolysis showed two separate peaks. Lai and co-workers⁶³
17 performed the gasification kinetics of municipal solid waste (MSW) under
18 80%N₂/20%CO₂ atmosphere. The derivative conversion curves showed two separate
19 peaks, which corresponded to the thermal decomposition of MSW from 200 to 650 °C,
20 and the reaction between CO₂ and the char production at above 700 °C. Following the
21 above conclusion, the derivative conversion curves of biomass gasification process
22 will generate two separate peaks, which corresponded to the thermal decomposition of
23 biomass (drying and pyrolysis, < 650 °C), and the reaction between fuel gas (syngas,
24 CO₂, steam) and hot reactive charcoal above 650 °C. Bhargava and co-workers⁴³
25 performed the pyrolysis of poly vinyl chloride (PVC). The resulting derivative
26 conversion curves at different heating rates showed two separate peaks, which were
27 mainly attributed to the release of hydrogen chloride and the formation of aliphatic,
28 olefinic and aromatic hydrocarbons and char, respectively.
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50 According to the simulation results obtained in this work, if the value of

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53 $\frac{|\mu_1 - \mu_2|}{\sqrt{\sigma_1^2 + \sigma_2^2}}$ is high enough (the critical value depends on the values of A and β), the
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3 double logistic DAEM shows two separate peaks, which is consistent with the
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5 results from Ashman and co-workers⁶⁵ for the double normal distribution.
6

7 (2) Overlapped processes 8

9 When the difference between the mean values of two distribution components,
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11 $|\mu_1 - \mu_2|$, is small, the double logistic DAEM shows one single peak in the $d\alpha/dT$
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13 curve. Researchers usually used certain single process kinetic models (such as the
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15 SFOR model or the single DAEM) to describe this type of process.
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18 Moyo⁶⁴ performed the combustion kinetic analysis of a blend of 50% biomass
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20 char and 50% coal char. The derivative conversion curves at different heating rates (8,
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22 12 and 15 K min⁻¹) showed a single peak, which was attributed to the fact that the
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24 combustion kinetic behaviors of biomass char and coal char were similar.
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26

27 (3) Partially overlapped processes 28

29 This type can describe the process which involves two partially overlapped
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31 sub-processes. The curve shows a main peak with a minor peak appearing as an
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33 overlapped peak or a peak shoulder.
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36 The form of overlapped peak or peak shoulder depends on the values of A and β ,
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38 except w , r and u . **Figure 7 (a)** shows an example of the effect of A on the $d\alpha/dT - T$
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40 curve of the double logistic DAEM. It can be observed that the form of the minor
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42 peak varies from the peak shoulder to the overlapped peak when the value of A
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44 increases from 10^{11} to 10^{21} s⁻¹. The increase of the frequency factor shifts the $d\alpha/dT -$
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46 T curve to the left side. An example of the effect of β on the $d\alpha/dT - T$ curve of the
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48 double logistic DAEM is presented in **Figure 7 (b)**, where the minor peak varies from
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50 the overlapped peak to the peak shoulder with an increasing value of β from 0.125 to
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52 128 K min⁻¹. As β increases, the $d\alpha/dT - T$ curve is shifted to higher temperatures, but
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54 the $d\alpha/dT$ peak height decreases.
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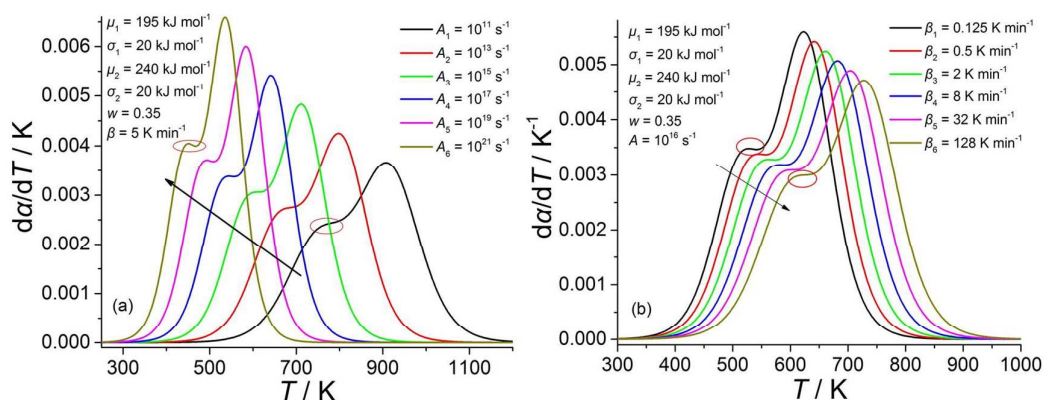


Figure 7. Examples of effects of (a) A and (b) β on the $d\alpha/dT - T$ curve of the double logistic DAEM

Many examples of the thermal decomposition of solid fuels from literature belongs to this type of process.

Cai and co-workers³⁰ conducted the pyrolysis of eight lignocellulosic feedstocks and presented the corresponding derivative conversion curves had a main peak and a peak shoulder on the left side of the main peak. The main peak corresponded to the pyrolysis of cellulose, while the peak shoulder on the left side of the main peak corresponded to the pyrolysis of hemicellulose.⁶⁶ Tang and co-workers⁴⁵ performed the pyrolysis kinetics of plant oil asphalt, a lipid-based residue biomass generated in biodiesel and fatty acid industries. The corresponding derivative conversion curves had a main peak with a left peak shoulder which corresponded to the pyrolysis of two pseudo-components, respectively. In contrast, de Filippis and co-workers^{40, 42} found that the derivative conversion curve presented a main peak with a peak shoulder on its right side during the pyrolysis of microalgae. The breakage of the weakest chemical bonds in microalgae has been reported during the primary pyrolysis sub-process, whereas the secondary pyrolysis sub-process favors the rupturing of stronger bonds

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3 and releases the hydrogen from the aromatic and aliphatic groups. Bhargava and
4 co-workers⁴³ investigated the pyrolysis of poly-methyl methacrylate (PMMA) and
5 found a main broad peak and a minor peak shoulder on the left side of the main peak,
6 which was attributed to the reactions occurring at the chain ends and random scission
7 process producing only monomers. In the kinetic study of coal pyrolysis from de
8 Caprariis and co-workers⁴¹, the derivative conversion curves at different heating rates
9 showed two partially overlapped peaks, which corresponded to a primary and
10 secondary pyrolysis sub-processes, respectively. Light volatiles and tar were released
11 in the primary pyrolysis sub-process while the repolymerization of coal molecules to
12 produce char took place in the secondary pyrolysis sub-process.⁴⁰

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24 According to aforementioned theoretical analyses, the double logistic DAEM can
25 be suggested as the most suitable tool for explaining the pyrolysis, combustion, or
26 gasification of various solid fuels which involve two thermal decomposition
27 sub-processes. When double logistic DAEM is applied to describe thermal
28 decomposition of solid fuels, the model parameters (A , μ_1 , μ_2 , σ_1 and σ_2) will provide
29 information about the activation energy distribution of each sub-process and weights
30 of both sub-processes. In the future work, these parameters will also be investigated
31 with optimization tools. It can be expected that the simulation results of the thermal
32 decomposition of solid fuels should fit the experimental data more accurately if the
33 double logistic DAEM would be coupled with the CFD simulation.

48 **6 Conclusions**

- 49 ● The equations of the double logistic DAEM were obtained and shown in
50 Equations (4)-(8).
- 51 ● The numerical calculation of the double logistic DAEM can be performed by the

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3 following method: the inner dT integral can be expressed in the form of the
4 exponential integral which can be easily processed in some mathematical
5 software systems, and the outer dE integral can be numerically solved by using
6 Simpson's rule.
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11 ● The double logistic DAEM is the weighted sum of two single logistic DAEMs
12 and the parameter w is the weight parameter. The parameters μ_1 and μ_2 are the
13 location parameters and mainly affect the locations of the $d\alpha/dT - T$ curve peaks.
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15 The parameters σ_1 and σ_2 are the shape parameters and mainly determine the
16 shape of the $d\alpha/dT - T$ curve.
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20 ● Three typical types of simulated double logistic DAEM processes were obtained:
21 separated, overlapped and partially overlapped processes.
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25 (1) When the value of $\frac{|\mu_1 - \mu_2|}{\sqrt{\sigma_1^2 + \sigma_2^2}}$ is high enough, the $d\alpha/dT - T$ curve of the
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30 double logistic DAEM shows two separate peaks.
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33 (2) If the difference between the mean values ($|\mu_1 - \mu_2|$) of two distribution
34 components is small, the double logistic DAEM shows one single peak in the
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39 $d\alpha/dT$ curve.

40 (3) As for the overlapped process, the form of the minor peak is the overlapped
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43 peak or peak shoulder depending on the values of A and β .

- 44 ● The double logistic DAEM is a suitable tool with abundant flexibility in
45 explaining the thermal decomposition of solid fuels, such as the pyrolysis,
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52 combustion or gasification of various solid fuels (e.g. lignocellulosic biomass,
53 coal, microalgae, plant oil asphalt, plastics).

- 53 ● The analysis of experimental kinetic data by using the double DAEM as well as
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60 the comparison between the logistic and Gaussian distributions in DAEM will be

our next work. It is hoped that our work can help to establish a comprehensive research framework for the double logistic DAEM.

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Supporting Information

Further details on the application of the double DAEM in thermal decomposition kinetics of solid fuels from literature.

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Nomenclature

Acronyms

DAEM	Distributed activation energy model
CFD	Computational fluid dynamics
SFOR	Single first order reaction
PVC	Poly-vinyl chloride
PMMA	Poly-methyl methacrylate
MSW	Municipal solid waste

TGA	Thermo-gravimetric analysis
Ei	Exponential integral
Ti	Temperature integral
Ni	Numerical integration function
Variables	
α	Conversion degree (dimensionless)
A	Frequency factor (s^{-1})
E	Activation energy ($J mol^{-1}$)
R	Universal gas constant ($8.3145 J K^{-1} mol^{-1}$)
t	Time (s)
T	Temperature (K)
$f(E)$	Activation energy distribution ($mol J^{-1}$)
β	Heating rate ($K s^{-1}$)
w	Constant, $0 < w < 1$
μ	Mean value of $f(E)$ ($J mol^{-1}$)
σ	Standard deviation of $f(E)$ ($J mol^{-1}$)

Subscript

1	Values related to the first sub-processes
2	Values related to the second sub-processes

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Graphical abstract

