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1 **Title: Dynamic model of basic oxygen steelmaking process based on multi-zone reaction**
2 **kinetics: Modelling of manganese removal**

3 **Author 1 (corresponding author)**

4 **Name:** Bapin Kumar Rout

5 **Affiliation:** Faculty of Science, Engineering and Technology, Swinburne University of Technology

6 **Mailing Address:** Hawthorn, Victoria, 3122, Australia, Email: brout@swin.edu.au

7 **Phone:** +61 3 9214 2837

8 **Author 2**

9 **Name:** Geoffrey Brooks

10 **Affiliation:** Faculty of Science, Engineering and Technology, Swinburne University of Technology

11 **Mailing Address:** Hawthorn, Victoria, 3122, Australia.

12 **Phone:** +61 3 9214 5672

13 **Author 3**

14 **Name:** M. Akbar Rhamdhani

15 **Affiliation:** Faculty of Science, Engineering and Technology, Swinburne University of Technology

16 **Mailing Address:** Hawthorn, Victoria, 3122, Australia.

17 **Phone:** +61 3 9214 8528

18 **Author 4**

19 **Name:** Zushu Li

20 **Affiliation:** WMG, University of Warwick

21 **Mailing Address:** WMG, University of Warwick, Coventry, CV4 7AL United Kingdom

22 **Author 5**

23 **Name:** Frank N.H. Schrama

24 **Affiliation:** Tata Steel, Netherlands

25 **Mailing Address:** Building 4H16, PO Box 10000, 1970 CA IJmuiden, NL

26 **Author 6**

27 **Name:** Willem van der Knoop

28 **Affiliation:** Tata Steel, Netherlands

29 **Mailing Address:** Building 4H16, PO Box 10000, 1970 CA IJmuiden, NL

30

31 **Abstract**

32 In the earlier work, a dynamic model for the BOF process based on the multi-zone reaction
33 kinetics has been developed. In the preceding part, the mechanism of manganese transfer in
34 three reactive zones of the converter has been analyzed. This study identifies that temperature
35 at the slag-metal reaction interface plays a major role in the Mn reaction kinetics and thus a
36 mathematical treatment to evaluate temperature at each reaction interface has been successfully
37 employed in the rate calculation. The Mn removal rate obtained from different zones of the
38 converter predicts that the first stage of the blow is dominated by the oxidation of Mn at the jet
39 impact zone, albeit some additional Mn refining has been observed as a result of the oxidation
40 of metal droplets in emulsion phase. The mathematical model predicts that the reversion of Mn
41 from slag to metal primarily takes place at the metal droplet in the emulsion due to an excessive
42 increase in slag-metal interface temperature during the middle stage of blowing. In the final
43 stage of the blow, the competition between simultaneous reactions in jet impact and emulsion
44 zone controls the direction of mass flow of manganese. Further, the model prediction shows
45 that the Mn refining in the emulsion is a strong function of droplet diameter and the residence
46 time. Smaller sized droplets approach equilibrium quickly and thus contribute to a significant
47 Mn conversion between slag and metal compared to the larger sized ones. The overall model
48 prediction for Mn in the hot metal has been found to be in good agreement with two sets of
49 different size top blowing converter data reported in the literature.

50 **Key words:** BOF, Mn refining, multi-zone kinetics, slag-metal emulsion, jet impact

51 1. Introduction

52 Manganese serves as an important alloying element in almost all commercial grades of steel.
53 The presence of Mn can influence several critical properties of steel. High Mn can improve
54 mechanical properties of steel, such as hardenability, toughness, and strength.^[1] On the other
55 hand, low Mn is required for ULC (ultra-low carbon) steels that require deep drawing
56 applications. In many steel plants, manganese ore has been added to achieve high Mn at the
57 end blow. This technique improves the process economics by reducing the addition of
58 ferromanganese (FeMn) in the subsequent secondary steelmaking process.^[1] On the other
59 hand, some steel plants face the problem of high Mn (>1 wt pct) hot metal due to the use of
60 lean iron ore having a high percentage of MnO in the blast furnace.^[2] Processing of high Mn
61 in BOF (basic oxygen furnace) is challenging as it causes problems such as slopping, refractory
62 lining consumption, and yield losses. The manganese in such converters is refined by either
63 overblowing oxygen or deslagging at the intermediate blow period. Therefore, it is very
64 important to understand the manganese refining behaviour under blowing conditions in order
65 to precisely control and improve the yield of Mn in a BOF process.

66 Several theoretical and experimental studies on the thermodynamics of manganese equilibrium
67 between the metal and slag have been reported in the literature.^[1, 3-7] As a result, numerous
68 semi-empirical correlations describing the partitioning ratio of Mn (L_{Mn}) between the metal
69 and slag containing manganese oxide are available in the literature.^[1,3-11] Owing to the
70 difficulty in measuring the Mn distribution ratio between the carbon saturated Fe and FeO
71 bearing slag (due to CO gas bubbling), researchers often applied indirect experimental
72 techniques to obtain the equilibrium data. Suito *et al.*^[3-5], Jung^[7], Kim *et al.*^[8] and Morales *et*
73 *al.*^[1] developed equilibrium distribution models based on experimentally obtained data
74 between liquid iron (Fe- Mn alloy) and slag. Another group of researchers used the equilibrium
75 data between liquid Cu or Ag with slag to establish Mn distribution model for carbon saturated

76 iron melts.^[7,9] The above studies agree that the equilibrium Mn distribution between slag and
77 metal increases with increase in total iron (T. Fe) in slag and decreases with increase in basicity
78 (%CaO/%SiO₂).^[3-11] Due to exothermic nature of Mn oxidation reaction, the negative effect
79 of temperature on demanganisation has been reported.^[3-6,11] It was further suggested that the
80 Mn oxidation in a BOF operation is controlled by the oxygen potential determined by Fe/Fe₂O
81 equilibrium.^[1,5] However, the above mentioned equilibrium distribution correlations are
82 limited to specific slag systems and no universal model has been established.

83 Meanwhile, due to increasing demand for improving high manganese yield, the reduction
84 mechanism of MnO by dissolved carbon in liquid iron has been investigated by several
85 researchers.^[12, 13, 14,15,16] According to proposed mechanism, MnO in the slag is reduced by Fe
86 at slag/metal interface producing Mn and FeO. The iron oxide is further reduced by CO at
87 slag/gas bubble interface to form CO₂ which subsequently reacts with the dissolved carbon at
88 gas bubble/metal interface to regenerate CO.^[13,14] Xu *et al.*^[14] reported that the rate of MnO
89 reduction in carbon saturated iron melt is limited by interfacial reaction (MnO +Fe = Mn +FeO)
90 and proposed a second order kinetic equation to describe the reaction rate.

91

92 Shibata *et al.*^[15] developed a kinetic model describing the simultaneous reaction between slag
93 and multi component iron alloy by using two film theory and reported that the reduction of
94 MnO is controlled by the transport process in slag phase. The study was focused on the
95 evaluation of rate parameters such as slag-metal interfacial concentration and discussed the
96 possible rate controlling steps for the reduction of MnO with the aid of the kinetic model.
97 Similarly, Marissa *et al.*^[16] applied the coupled reaction model to analyse the reduction rate of
98 MnO in slag in terms of the slag basicity, initial Si and C in the liquid iron. The rate of MnO
99 reduction was reported to increase with increasing the initial C concentration. The above

100 mentioned studies are limited to laboratory studies and did not include the kinetics of Mn
101 oxidation under oxygen blowing. Further, no validation of this kinetic model was attempted
102 with the industrial scale furnaces.

103 A few researchers attempted to establish a kinetic model for Mn refining in industrial scale
104 furnaces (BOF and EAF) by considering both the oxidation and reduction kinetics. [6, 17]
105 Takaoka *et al.* [17] analysed the equilibrium driving force for the reactions and concluded that
106 the competition between oxidation of Mn by gaseous oxygen and reduction of MnO by C
107 decides the kinetics of Mn refining in combined blowing converter. The authors were able to
108 establish a semi-empirical kinetic model that incorporates reduction and oxidation reaction.
109 However, the role of slag FeO on manganese transfer was completely ignored in this study and
110 the kinetic parameters were derived from fitting the plant data, which limits the model for
111 applying in different converters.

112 The present kinetic model for Mn refining reaction is based on a multi-zone kinetic model
113 proposed by the authors in the previous publication. [18] The details of the development of the
114 dynamic model which includes the reaction kinetics of C, Si, Mn and P coupled with flux
115 dissolution and FeO generation model has been already discussed in the paper. In the present
116 model, the three reactive zones of the converter, e.g. jet impact zone, slag-bulk metal zone, and
117 slag-metal emulsion zone have been considered for the refining of manganese. The
118 simultaneous occurrence of oxidation and reduction reaction kinetics has been analysed in each
119 zone. The rate of Mn refining in the emulsion zone has been simulated by using the previously
120 developed mathematical model for residence time [19], droplet generation [20] and
121 decarburisation model [21]. Using the rate model the relative contribution of different zones on
122 refining of Mn was quantified. Using this Mn refining kinetic model, the dynamic evolution of
123 Mn in the hot metal was estimated and the effect of process parameters on manganese refining

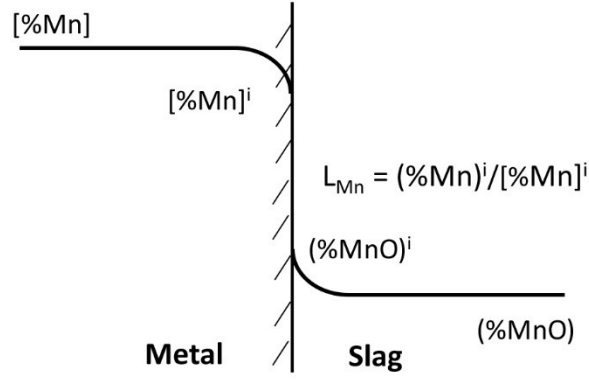
124 kinetics has been evaluated. The overall rate model for Mn prediction has been validated by
125 using two sets of industrial data obtained from a 200 t and a 55 t top blowing converters.

126 **2. Manganese reaction kinetics in BOF**

127 The behaviour of manganese refining profile commonly observed in basic oxygen furnace
128 (BOF) shows rapid oxidation at the beginning followed by back reduction of Mn from slag to
129 metal during the middle stage and finally some further oxidation at the end stage of the blow.
130 ^[22-24] Several researchers reported that the transfer of Mn between hot metal and slag is
131 controlled by the oxygen potential, determined by Fe/Fe₂O equilibrium according to the
132 following reaction: ^[1, 3, 9,13,14]



133 Under the condition of mass transport control, it is assumed that the chemical reactions are fast
134 and achieve equilibrium all the time at the slag-metal interface. Kawai *et al.*^[25] and Shinozaki
135 *et al.*^[26] reported that the resistance to the mass transport of Mn in metal and slag phases are of
136 similar order; suggesting that a mixed controlled mass transport can be suitable to describe the
137 Mn refining kinetics at liquid iron and slag interface. **Figure 1** shows a schematic of the
138 mechanism of mixed transport controlled Mn transfer across the metal–slag interface (e.g.
139 metal droplet-slag or bulk metal- slag).



Condition for Mn mass transfer from metal to slag : $([\%Mn] - [\%Mn]^i) > 0$

140

141 Figure 1: Schematic of mixed controlled Mn transfer across slag-metal interface

142 Accordingly, the rate equation for the mass transfer of manganese across the slag-metal

143 interface can be written as:

$$-\frac{d[\%Mn]}{dt} = \frac{A}{W_m} k_m \rho_m ([\%Mn] - [\%Mn]^i) \quad (2)$$

$$-\frac{d[\%Mn]}{dt} = \frac{A}{W_m} k_s \rho_s ((\%Mn)^i - (\%Mn)) \quad (3)$$

144 and

$$-\frac{d[\%Mn]}{dt} = \frac{A}{W_m} k_o \rho_m \left([\%Mn] - \frac{(\%Mn)}{L_{Mn}} \right) \quad (4)$$

145 Where

$$k_o = \frac{k_m k_s \rho_s L_{Mn}}{k_m \rho_m + k_s \rho_s L_{Mn}} \quad (5)$$

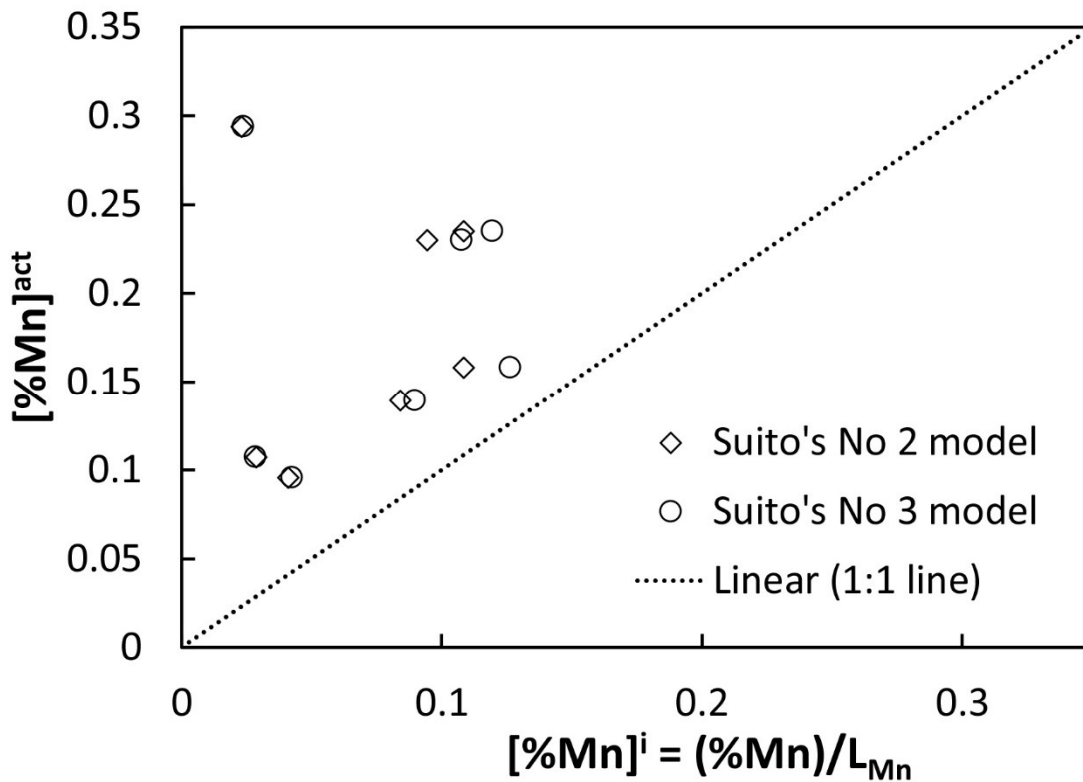
146 Where k_o is the overall mass transfer coefficient, k denotes the mass transfer coefficient, A is
147 the area of the slag-metal interface, ρ is the density, L_{Mn} is the equilibrium distribution ratio,
148 m and s denote metal and slag respectively.

149 As can be seen from Eq. 4, the thermodynamic driving force for the reaction,
150 $\left([\%Mn] - \frac{(\%Mn)}{L_{Mn}}\right)$ is the only parameter that decides the direction manganese transfer i.e.
151 whether Mn oxidises to slag or MnO reduces back to metal phase is primarily determined by
152 the equilibrium distribution ratio, manganese oxide concentration in slag and Mn content in the
153 hot metal.

154 Owing to the importance of evaluating manganese distribution between the metal and slag
155 during steelmaking operations, several empirical correlations for the equilibrium partitioning
156 ratio (L_{Mn}) and apparent equilibrium constant, $k'_{Mn} = \%MnO / (\%FeO \times [\%Mn])$ as a function of
157 slag composition and temperature have been developed by many researchers. Morales and
158 Fruehan^[1] indicated that k'_{Mn} has greater practical use than L_{Mn} since the expression
159 incorporates the wt pct of FeO and thus can be used to evaluate the distribution of manganese
160 at various oxygen potentials. For a known slag composition and temperature, $[wt\ pct\ Mn]^i$ can
161 be evaluated from the empirical correlation of either L_{Mn} or k'_{Mn} and may be compared with
162 the bath Mn concentration to estimate the reaction direction.

163 In order to examine the nature of Mn reaction, the authors compared the interfacial Mn
164 concentration, $[wt\ pct\ Mn]^i$ calculated by the empirical correlations of L_{Mn} with the actual $[wt$
165 $pct\ Mn]$ in the steel of a 200 t top blowing converter reported by Cicutti *et al.*^[24] Suito's No.
166 2^[4] and No. 3^[3] model has been applied to estimate L_{Mn} . **Figure 2** shows the comparison of
167 $[\%Mn]^i$ obtained from Suito's correlations with the bulk Mn concentration ($[\%Mn]^{act}$) during
168 different stages of oxygen blowing. The analysis shows that, the interfacial Mn concentration

169 is always lower than the measured Mn in the hot metal, indicating that the reaction at slag-
 170 metal interface has a positive thermodynamic driving force for forward direction and the flow
 171 of Mn takes place from bulk metal to slag throughout the blowing period. However, in the real
 172 process, the hot metal Mn profile shows the back reduction of manganese into the hot metal
 173 during the middle stage (4 min to 12 min) of the blow as observed by Cicutti *et al.*^[24] Similar
 174 observation of Mn reaction and its deviation from equilibrium value has been reported by
 175 several authors.^[17, 27] In the present work, the parameters responsible for this deviation have
 176 been subjected to investigation and discussed in the following sections.



177

178 Figure 2: Comparison of actual Mn in the metal and the interfacial Mn calculated from
 179 Suito's equilibrium distribution models: Slag and hot metal composition data were taken
 180 from a top blowing process

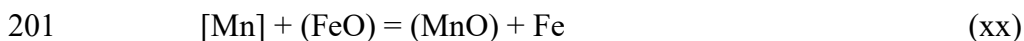
181 2.1. Temperature at the reaction interface

182 The oxidation of manganese in the hot metal is an exothermic reaction and therefore L_{Mn} is
 183 expected to decrease with increase in temperature. Zhu *et al.*^[9] and Jung *et al.*^[10] reported that

184 the equilibrium distribution ratio of Mn decreases linearly with increase in metal bath
185 temperature. The laboratory experiments studied for evaluation of L_{Mn} are often performed in
186 a crucible without oxygen blowing. Thus, the extraction and the extractive phases in the
187 crucible experiments can be assumed to be in permanent contact with each other. Thermal
188 gradient between the slag/metal interface and the bulk metal temperature can be thought to be
189 negligible in those experiments. However, in a real BOF process, marked thermal gradient
190 exists in the bath, the difference between the temperature of the top surface and bottom of the
191 vessel can vary from 200 to 400 °C depending on the blowing type (soft or hard blowing).^[28]
192 A significant variation of temperature at the reaction interface (slag/metal) can make a potential
193 change in the equilibrium concentration from the value obtained in laboratory scale L_{Mn}
194 correlations. Also, in a real BOF process, the reactions can take place in several reactive
195 interfaces with different thermal conditions and phases. The slag/metal equilibrium alone may
196 not accurately represent the overall thermodynamic driving conditions for the refining reactions
197 in a BOF.

198 **2.2.Competition between the reactions involving Mn**

199 The mass transfer of manganese between metal and slag proceeds via several reactions i.e.



203 It is entirely possible that the oxidation and reduction reaction of Mn takes place
204 simultaneously in different zones and the balance between those rates decides the direction of

205 overall manganese flow in the converter. A multiple zone reaction kinetics analysis may be
206 appropriate to represent the overall process of Mn conversion between the metal and the slag.

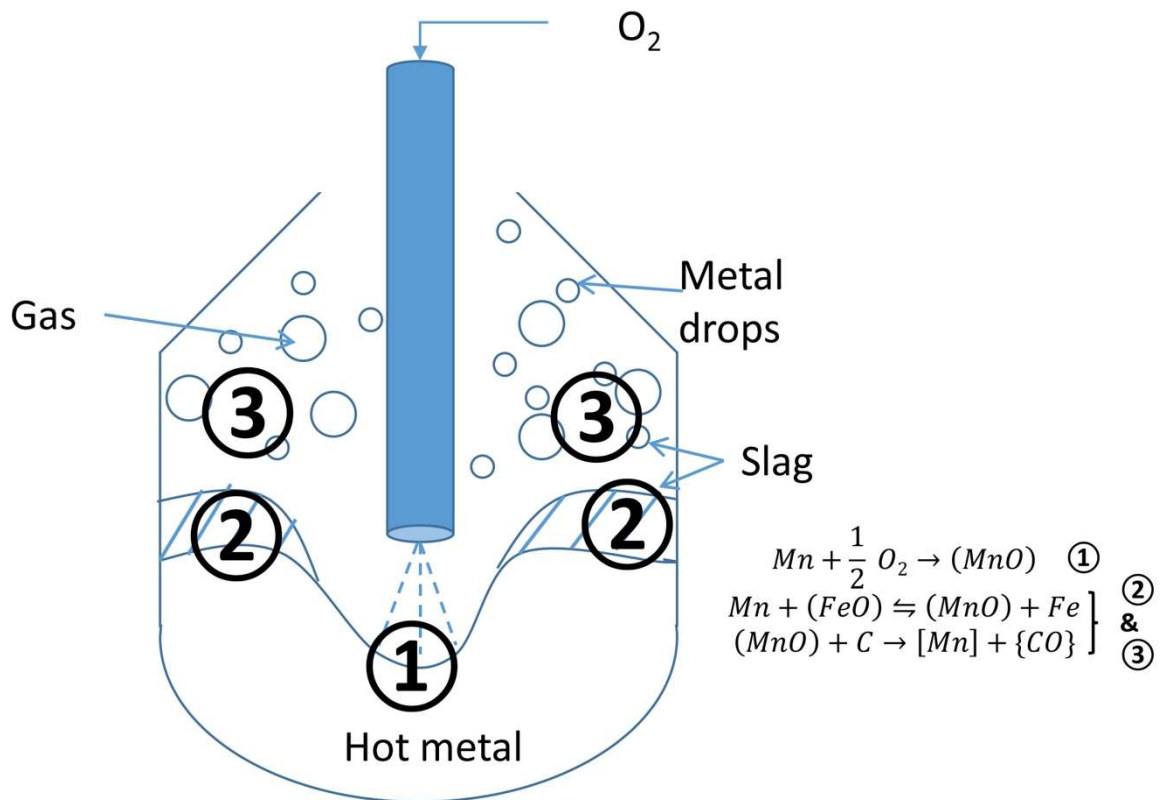
207 **2.3.Manganese reaction due to transitory phase contact in the slag-metal gas emulsion**

208 The reactions occurring in the slag-metal emulsion are thought to take place at several
209 interfaces with dynamic change in thermodynamic equilibrium and mass transfer conditions.
210 [23, 29,30] As the droplets eject from the melt, a large number of distinct interfaces are created
211 and the refining reaction in the emulsion proceeds via the reaction between the droplet and
212 slag. It is observed that the kinetics of the refining reactions are a strong function of interfacial
213 area, residence time, physicochemical condition of slag and droplet generation rate. Unlike the
214 reactions occurring at a permanent phase boundary, only the equilibrium interfacial
215 concentration cannot determine the direction of the mass conversion process between the hot
216 metal and emulsion. The rate difference between the mass concentration of ejected and the
217 refined droplets over the entire population of recirculated droplets would likely to determine
218 the direction of mass transfer of Mn between hot metal and slag.

219 The discussion mentioned above, indicates that in a multi-zone reactor like BOF, caution must
220 be taken in determining the transient rate parameters associated with Mn refining kinetics. In
221 the present work, the mathematical treatments to the multi-zone reaction kinetics have been
222 developed to simulate the time-variant rate parameters and overall Mn refining in the hot metal.
223 Three reaction interfaces, i.e. (i) jet impact where the oxygen gas directly reacts with the hot
224 metal bath, (ii) slag/ bulk metal interface where Mn in the hot metal reacts with the slag lying
225 on the top, and (iii) in emulsion where the Mn reaction takes place due to transitory phase
226 contact of the metal droplet with the slag, were considered for the formulation of the
227 mathematical model. The effect of temperature on manganese equilibrium at each reaction
228 interface was evaluated in the present work.

229 **3. Kinetic modeling of manganese reaction**

230 The primary regions for Mn reaction in BOF have been illustrated in **Fig. 3**. As can be seen
 231 from the figure, jet impact, slag- bulk metal and emulsion zones were considered to be the main
 232 zones for manganese refining.



233

234 Figure 3: Schematic representation of oxidation/reduction reactions of Mn across various
 235 interfaces in a BOF

236 The reactive zones of manganese Mn refining are:

- 237 1. Jet impact zone

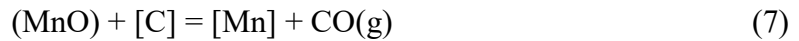
238 The direct oxidation of Mn by O_2 jet at the gas-metal interface can be given by the following
 239 reaction:



240

241 2. Slag-bulk metal zone

242 In this reaction zone, a permanent phase contact between the slag and the metal can be assumed.
243 Mn in the bulk metal reacts with FeO in the slag according to Eq. 1. This reaction can proceed
244 either in the forward direction or backward direction depending on equilibrium value of Mn at
245 the interface set by the temperature and slag compositions. A certain amount of MnO in the
246 slag is expected to reduce by dissolved C in the melt at slag-metal interface according to the
247 Eq. 7.



248 Since it is evident that the Mn equilibrium at the slag/metal is governed by Fe/Fe_tO oxygen
249 potential, the reduction of MnO by C has been ignored in the present work. ^[1, 5]

250 3. Slag-metal emulsion zone

251 In the emulsion zone, the ejected metal droplets are brought in contact with the slag and the
252 reactions presented in Eq. 1 can be applied to evaluate the Mn reaction rate. The kinetic
253 parameters of the total number, size evolution of metal droplets and time of residence in the
254 emulsion are important parameters to be considered in order to determine the overall Mn
255 refining by emulsion zone.

256 4. Mathematical modelling of overall Mn refining rate

257 The overall mass balance has been performed over the reacting zones to estimate the total Mn
 258 refining during the blowing process. The mathematical expression for the overall manganese
 259 refining rate can be written as:

$$\left(\frac{dW_{Mn}}{dt}\right)_{total} = \left(\frac{dW_{Mn}}{dt}\right)_{em} + \left(\frac{dW_{Mn}}{dt}\right)_{iz} + \left(\frac{dW_{Mn}}{dt}\right)_{sm} \quad (8)$$

260 Here, $\left(\frac{dW_{Mn}}{dt}\right)_{em}$, $\left(\frac{dW_{Mn}}{dt}\right)_{iz}$ and $\left(\frac{dW_{Mn}}{dt}\right)_{sm}$ are the rate of Mn removed from the emulsion, jet
 261 impact and slag-bulk metal zones respectively (kg/s) . $\left(\frac{dW_{Mn}}{dt}\right)_{total}$ is the total rate of Mn
 262 refining at each time of blowing (kg/s).

263 The concentration of manganese in the bulk metal was calculated by the following mass
 264 balance equation:

$$W_b^{t+\Delta t} \times [wt \ pct \ Mn_b]^{t+\Delta t} = W_b^t \times [wt \ pct \ Mn_b]^t - \left(\frac{dW_{Mn}}{dt}\right)_{em} \times \Delta t - \left(\frac{dW_{Mn}}{dt}\right)_{iz} \times \Delta t - \left(\frac{dW_{Mn}}{dt}\right)_{sm} \times \Delta t + \left(\frac{dW_{Mn}}{dt}\right)_{sc} \times \Delta t \quad (9)$$

265 Where Δt is the numerical time step, W_b^t is the weight of the hot metal (kg) at time t, $W_b^{t+\Delta t}$ is
 266 the weight of the hot metal at previous time step ($t + \Delta t$), [wt pct Mn_b] is the weight percentage
 267 of Mn in the bulk metal, dW_{Mn}/dt is the rate of Mn refining (kg/s) and the subscripts em, iz, sm
 268 and sc represents emulsion, jet impact, slag-metal bulk interface and scrap respectively.

269 The change in mass of the bulk metal has been estimated using the calculated mass of scrap,
 270 droplet generation and return to bath, slag and gas formation during time Δt . The mathematical
 271 expression can be written as:

$$W_b^{t+\Delta t} = W_b^t + \Delta W_{sc}^{m,t} - \Delta W_m^{sl,t} - \sum \left(\frac{dW_i}{dt} \right)_{em} \times \Delta t - \sum \left(\frac{dW_i}{dt} \right)_{iz} \times \Delta t \quad (10)$$

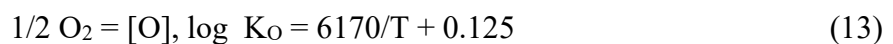
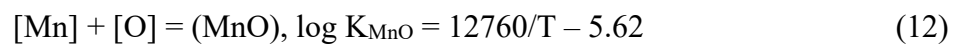
272 Here $W_b^{t+\Delta t}$ is the weight of the bulk metal at time $t + \Delta t$, W_b^t is the weight of the bulk metal
 273 at time step t , $\Delta W_m^{sl,t}$ is the weight of the elements in hot metal converts into slag (at slag-bulk
 274 metal interface) and $W_{sc}^{m,t}$ is the weight of the melted scrap during time step Δt .
 275 droplets $\left(\frac{dW_i}{dt} \right)_{em}$ and $\left(\frac{dW_i}{dt} \right)_{iz}$ are the rate of refining of hot metal impurities (kg/s) through
 276 emulsion and jet impact zone respectively.

277 4.1. Modeling of Mn reaction kinetics at jet impact area

278 The rate of Mn oxidation at jet impact area can be expressed as a first order rate law assuming
 279 the reaction to be controlled by mass transfer in the hot metal. It is due to the rapid dissolution
 280 of oxygen in the hot metal as a result of high temperature exhibiting at jet impact area. Also,
 281 the mass transfer coefficient in the gas phase is higher of a few orders of magnitude than in
 282 metal phase and a fast chemical reaction can always be expected at high temperatures. The
 283 liquid phase mass transfer controlled Mn refining rate equation in jet impact area can be written
 284 as:

$$\left(\frac{dW_{Mn}}{dt} \right)_{iz} = -k_m \times \frac{A_{iz}}{100} \times \rho_m ([wt \ pct \ Mn] - [wt \ pct \ Mn]_{iz}^{eq}) \quad (11)$$

285 Here k_m is the mass transfer coefficient in hot metal, A_{iz} is the area of the jet impact and ρ_m is
 286 density of steel. The value of $[wt \ pct \ Mn]_{iz}^{eq}$ was estimated from the following chemical
 287 reactions:



288 The overall equilibrium constant for the Mn oxidation reaction according to Eq. 6 is given by:

$$\log K = \log K_{\text{MnO}} + \log K_o \quad (14)$$

289 Oxygen partial pressure, P_{O_2} is assumed to be 1 atm (1.013×10^5 Pa) and activity of MnO, a_{MnO}
290 has been calculated by regular solution model introduced by Ban-Ya. [31] In a real BOF process
291 the value of P_{O_2} will be much lower than the atmospheric pressure as the jet entrains a large
292 amount of CO and CO₂. The assumption is initially undertaken to qualitatively analyse the
293 behaviour of equilibrium driving force of Mn reaction at gas/metal interface. The measured
294 thermal profile of hot spot reported by Chiba *et al.* [32] has been used to simulate the temperature
295 in the jet impact area. It was assumed that temperature in the jet impact linearly increases from
296 2273K to 2573K during the first 25 pct of the blow. During the main blow period (25 pct to 80
297 pct of blow), it remains constant with a value of 2573K. Finally after 80 pct of oxygen blowing,
298 the temperature was assumed to decrease linearly and equals the hot metal temperature at the
299 end of refining. The calculated value of $[\text{wt pct Mn}]_{iz}^{eq}$ was found to be in the order of 10^{-4} to
300 10^{-5} for a 200 t converter (Cicutti *et al.* [24]). In a BOF process the Mn content in the hot metal
301 usually varies from 0.3 to 0.6 wt pct, and the estimated equilibrium value was found to be 1,000
302 to 10,000 times lower than the actual manganese concentration. This ratio will further increase
303 in an actual BOF process due to entrainment of CO₂ and CO gas ($P_{\text{O}_2} < 1$) and our assumption
304 of P_{O_2} may not have large influence on the rate calculation. This low value of equilibrium
305 concentration shows that the Mn oxidation reaction in jet impact area has a strong positive
306 thermodynamic driving force for Mn refining from bulk metal.

307 Mass transfer in the metal phase has been assumed to be the rate controlling step for the Mn
308 oxidation kinetics in the jet impact area. It is due to the rapid dissolution of O in the hot metal
309 under extremely high temperature generated in the hot spot region. The mass transfer
310 coefficient in the metal phase was assumed to be a function of the amount of stirring in the

311 bath. Ishikawa^[33] investigated the reaction kinetics in a top blowing test converter and reported
312 that the kinetics of Si and Mn are a strong function of agitation in the bath and proposed a
313 correlation for k_m as a function of stirring energy, bath diameter and temperature. In the present
314 work, the relationship proposed by Kitamura *et al.*^[34], has been used to determine the mass
315 transfer coefficient of Mn in the melt phase.

$$\log k_m = 1.98 + 0.5 \log \left(\frac{\varepsilon H^2}{100L} \right) - \frac{125000}{2.3RT} \quad (15)$$

316 where k_m is the mass transfer coefficient in metal phase (cm/s), ε is the stirring energy (W/t),
317 H and L are the bath depth (cm) and diameter of the furnace respectively and T is the
318 temperature in the impact zone (K). The total stirring energy was calculated (see appendix A.1.
319 for details) from the combined effect of the top and bottom gas injection in the BOF.^[35]

320 One important parameter which controls the rate of Mn oxidation is the evolution of interfacial
321 area available for gas-metal reaction at jet impact region. The gas-metal interfacial area was
322 assumed to be the surface area of the cavity generated due to the impinging gas jet on the liquid
323 metal. The calculation of jet cavity area as a function of blow parameters has already been
324 discussed in the first part of the work.^[18] For multi-head nozzles, the cavity coalescence was
325 ignored and the overall cavity area was calculated by just adding the individual cavity formed
326 by each nozzle.

327 **4.2. Modelling of Mn reaction kinetics at slag-metal interface**

328 The rate of Mn transfer across the slag-bulk metal interface as a result of the reaction between
329 [Mn] in the bulk metal and (FeO) in the slag is assumed to be controlled by the transport of
330 both [Mn] in metal and (MnO) in the slag. Several past studies reported that the resistance to
331 mass transport of Mn in hot metal and slag are roughly at the same order of magnitude. [25,26]

332 In the present work, therefore, both resistance have been taken into account in the rate model
 333 of Mn at the slag-metal interface.

$$\left(\frac{dW_{Mn}}{dt}\right)_{sm} = -k_o^{sm} \times \frac{A_{sm}}{100} \times \rho_m \left\{ [wt \ pct \ Mn] - \frac{(wt \ pct \ Mn)}{L_{Mn}} \right\} \quad (16)$$

334 Where A_{sm} is the surface area at slag-bulk metal interface, k_o^{sm} is the overall mass transfer
 335 coefficient. The overall mass transfer coefficient was evaluated by applying Eq. 5. k_m was
 336 calculated from Eq. 15. The slag phase mass transfer coefficient was given by:^[36]

$$k_s = a \exp\left(-\frac{37000}{RT}\right) \cdot \varepsilon^b \quad (17)$$

337 Where k_s is the mass transfer coefficient in slag phase (cm/s), R: gas constant ($J \cdot mol^{-1} K^{-1}$), ε is
 338 the stirring energy (W/t), a and b are the empirical parameters, assumed to be 1.7 and 0.25
 339 respectively.^[36] Industrial measurement shows that the slag is about 20 to 100 K hotter than the
 340 hot metal.^[37] For simplicity, a uniform slag temperature which is 100 K higher than the hot
 341 metal temperatuer has been assumed in the rate calculation at slag-bulk metal interface.

342 The manganese partitioning ratio at the interface between the slag and the metal can be defined
 343 as the ratio between the wt pct of Mn in slag to wt pct of Mn in the hot metal as:

$$L_{Mn} = \frac{(wt \ pct \ Mn)^i}{[wt \ pct \ Mn]^i} \quad (18)$$

344 The subscript i in Eq. 18 denotes the concentration at the slag-metal interface. Since the
 345 chemical reaction is fast at high temperature, the reaction species were assumed to attain
 346 equilibrium all the time at the interface. The interfacial concentrations described in Eq. 18 can
 347 be replaced by the equilibrium concentration for the calculation of L_{Mn} . Some studies have

348 been performed in the past to investigate the thermodynamics of Mn equilibrium and several
 349 correlations for Mn partition ratio has been reported in the literature. [3-5] In the present work,
 350 Suito's model [3] has been chosen for the calculation of manganese equilibrium concentration.
 351 The empirical correlation of k'_{Mn} proposed by Suito has been developed between liquid iron
 352 and CaO-SiO₂-Fe_tO slag with MnO concentration varying up to 16 wt pct. Since in Cicutti's
 353 slag data the wt pct of MnO falls in the same range, the correlation can be suitable in evaluation
 354 of interfacial Mn concentration. The following empirical relationship was suggested by Suito
 355 *et al.* [3] to determine the apparent equilibrium constant and [%Mn]^{eq} at the interface between
 356 slag and bulk metal.

$$\begin{aligned} \log k'_{Mn} = & -0.0180[(wt\ pct\ CaO) + 0.23(wt\ pct\ MgO) \\ & + 0.28(wt\ pct\ Fe_tO) - 0.98(wt\ pct\ SiO_2) \\ & - 0.08(wt\ pct\ P_2O_5)] + \frac{7300}{T} - 2.697 \end{aligned} \quad (19)$$

357 Where the apparent equilibrium constant k'_{Mn} is defined as:

$$k'_{Mn} = \frac{(wt\ pct\ MnO)}{(wt\ pct\ T.Fe) \times [wt\ pct\ Mn]} \quad (20)$$

358 The interfacial area between slag and bulk metal (A_{sm}) was calculated by subtracting the cavity
 359 area resulted by top jet from the geometrical area of the bath surface. For non-coalescence
 360 cavity the area of slag metal can be expressed by the following equation:

$$A_{sm} = \pi \left(\frac{D_b^2}{4} - n_n \times r_{cav}^2 \right) \quad (21)$$

361 Here D_b is the diameter of the bath surface (m), n_n is the number of nozzles in the lance tip and
 362 r_{cav} (m) is the radius of a single jet cavity. The cavity geometry was calculated by using the
 363 dimensionless relationships suggested by Korla and Lange. [38] In the above calculation, for

364 simplicity, the surface area of the slag-bulk metal interface was assumed to be flat and the bath
365 oscillation was neglected.

366 4.3. Modelling of Mn reaction kinetics in slag-metal emulsion

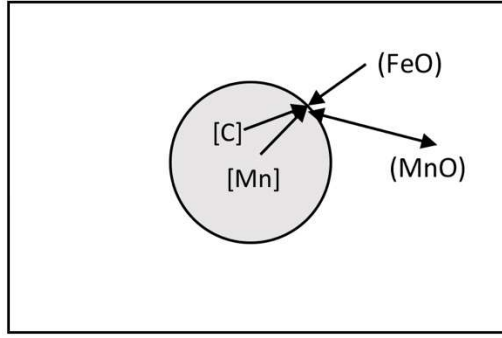
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368 4.3.1. Microkinetics: Evaluation of Mn refining rate in a droplet

369 Similar to slag-bulk metal zone, the reaction of Mn at metal droplet and slag interface was
370 considered to be controlled by the transport of Mn inside the metal drop and MnO in the slag.
371 [39] Thus, a mixed controlled kinetic equation has been applied for evaluating the rate of reaction
372 of metal droplets in the slag-metal emulsion. **Figure 4** illustrates the schematic of exchange of
373 Mn between metal-drop and slag inside the emulsion phase. The rate of Mn removal by a single
374 droplet can be expressed as:

$$\left. \frac{d[\text{wt pct Mn}]^{em}}{dt} \right|_{drop} = -\frac{A_{drop}}{V_{drop}} \times k_o^{em} \times \left\{ [\text{wt pct Mn}] - \frac{(\text{wt pct Mn})}{L_{Mn}} \right\} \quad (22)$$

375 A_{drop} and V_{drop} are the area and volume associated with the single droplet in the emulsion and
376 L_{Mn} is the equilibrium partition ratio of Mn between slag and metal droplet. Similar to the slag-
377 bulk metal interface, L_{Mn} was calculated by applying Eq. 18 at slag- metal droplet phase
378 boundary. Instantaneous surface area of the droplet due to bloating behaviour resulted by
379 decarburization reaction has been estimated from the empirical correlation of density change
380 of droplet as a function of decarburization rate and FeO wt pct in slag proposed by Brooks *et*
381 *al.* [19]



382

383 Figure 4: Transport process of Mn at metal droplet and slag containing iron oxide interface in
384 the emulsion zone

385 The overall mass transfer coefficient, k_o^{em} was calculated by applying mixed controlled
386 kinetics as mentioned in Eq. 5. It should be noted that the reaction at slag-metal droplet
387 interface undergoes a transitory phase contact during the emulsion where as a permanent phase
388 contact can be assumed between metal and bulk slag. The mass transfer coefficient of Mn
389 transport in the metal for a translating droplet was determined by employing surface renewal
390 model as

$$k_m^{drop} = 2 \times \sqrt{\frac{D_{Mn}}{\pi t_c}} = 2 \times \sqrt{\frac{D_{Mn} u}{\pi d_p}} \quad (23)$$

391 Here d_p is the average droplet diameter (m) corresponding to the same size class and u is the
392 velocity (m/s) of the metal droplet in the emulsion. D_{Mn} is the diffusion coefficient of Mn in
393 molten metal (m^2/s). The temperature and viscosity effect on mass diffusivity was taken into
394 account by applying the Stokes-Einstein equation.

$$D_T^{Mn} = D_{1873}^{Mn} \left(\frac{T}{1873} \right) \times \left(\frac{\mu_{m,1873}}{\mu_{m,T}} \right) \quad (24)$$

395 Where D_T^{Mn} is the diffusivity of Mn in hot the metal of temperature T (m^2/s), D_{1873}^{Mn} is the
396 diffusivity of species at $T=1873K$ (m^2/s), T is the temperature (K), $\mu_{m,1873}$ and $\mu_{m,T}$ are the
397 viscosity of hot metal at 1873K and T respectively. In the present work, the effect of
398 temperature on viscosity has been neglected.

399 On the slag side, the mass transfer coefficient can be calculated assuming the metal droplet to
400 be a rigid sphere with a stream of slag surrounding it. Due to high Schmidt number prevailing
401 in steelmaking slag (in the range of 10^5 and 10^6 in slag as compared to $\sim 10^3$ in steel melt) , the
402 boundary layer is considered to be laminar and the effect of turbulence on mass transfer
403 coefficient can be neglected.^[39] The mass transfer coefficient in slag phase was determined by
404 the following relationship^[39]:

$$Sh = 2 + 0.6Re^{1/2}Sc^{1/3} \quad (25)$$

405 Where Sh is the Sherwood number, Re is the Reynolds number and Sc is the Schmidt
406 number. The diffusion of MnO in slag D_{slag} was taken to be $5 \times 10^{-10} \text{ m}^2/\text{s}$.^[39]

407 As different sizes of metal droplets are ejected from the melt, the size distribution and time of
408 residence are important parameters to estimate the kinetics of refining of Mn. The authors in
409 their previous publications^[18,20] have developed mathematical models to predict the amount of
410 ejected droplets, size distribution and residence time as a function of the furnace operating
411 parameters, hot metal and slag compositions. The size distribution of the entire population of
412 ejected droplets was divided into different groups by using Rosin-Rammler-Sperling (RRS)
413 distribution function.^[40] The mathematical model for the residence time of the metal droplets
414 was based on the principle of ballistic motion, proposed by Brooks *et al.*^[19] The trajectory of a
415 droplet in both vertical and horizontal direction was calculated by the force balance method
416 with taking into account the dynamic change in density due to bloating caused by the nucleation
417 of CO gas bubbles. The details of the development of residence time submodels can be found
418 elsewhere.^[18] The residence time model calculates the concentration change of Mn (also C, Si
419 and P) in the droplet for a particular size class at each time of its trajectory inside emulsion. At
420 each numerical time steps, the Mn concentration of each size group of the droplets at the time
421 of their re-entry to the bath was evaluated.

422 4.3.2. Temperature at metal drop-slag interface

423 As described in the previous work [18] the temperature at metal droplet-slag interface was
424 estimated by assuming the ejected droplets to be rigid spheres and initially carry the
425 temperature of the hot spot. The droplets gradually decrease the temperature as they pass
426 through the emulsion phase which is expected to be a lower temperature than the hot spot. A
427 homogeneous temperature in the emulsion, same as of the slag has been assumed in the
428 calculation. The following equation has been applied to determine the droplet interface
429 temperature:[41]

$$T_{drop} = T_0 + \frac{T_0 - T_\infty}{1 + \beta} \quad (26)$$

430

$$\beta = \left(\frac{\lambda_m C_{p,m} \rho_m}{\lambda_s C_{p,s} \rho_s} \right)^{1/2} \quad (27)$$

431 where λ is the conductivity (W/mK), C_p is the heat capacity (J/kg). The subscript m, s
432 corresponds to hot metal and slag. T_{drop} , T_0 , T_∞ represents the temperature at the droplet
433 interface in the emulsion, temperature of the droplet at the time of ejection and the emulsion
434 temperature respectively. Here $T_0 = T_{iz}$ and $T_\infty = T_s$, are assumed for the calculation of the
435 temperature at the droplet interface. The details about the calculation of heat capacity in metal
436 ($C_{p,m}$) and slag ($C_{p,s}$) phases can be found in an earlier publication.[18]

437 4.3.3. Macrokinetics: Evaluation of overall Mn refining rate by emulsion phase

438 The overall Mn removal rate by emulsion at each time of blowing was calculated by the
439 difference between the total mass of droplet ejected and returning droplets at a predefined
440 numerical time step.

$$\left(\frac{dW_{Mn}}{dt}\right)_{em} = \frac{W_{Mn}^{eject,t} - W_{Mn}^{return,t}}{\Delta t} \quad (28)$$

441 The total mass of manganese (kg) ejected into the emulsion was estimated from the
 442 previously developed droplet generation model. [20]

$$W_{Mn}^{eject,t} = \left(\sum_{p=1}^P (R_{B,T})_p^t \times \Delta t \right) \times \frac{[wt\ pct\ Mn]_m^t}{100} \quad (29)$$

443 Where P is the total number of divisions of the ejected droplet size spectrum, $(R_{B,T})_p^t$ is the
 444 rate of droplet generated (kg/s) for a given size class p at time t and $[wt\ pct\ Mn]_m^t$ is the
 445 concentration (wt pct) of Mn in the hot metal. The value of total division in the size spectrum,
 446 P was taken to be 6 in the present model calculations.

447 Micro-kinetic model estimates the manganese concentration of an individual droplet at each
 448 time of its trajectory inside the emulsion phase. For each size group, the final Mn concentration
 449 at the time of their return to the bath and the total time of residence in the emulsion was
 450 calculated. The total number of returning droplets having the final manganese concentration at
 451 the time of their re-entry to the hot metal has been estimated and the total weight of Mn entering
 452 into the bath was calculated.

$$W_{Mn}^{return,t} = \sum_{p=1}^P N_p^{return,t} \times \frac{[wt\ pct\ Mn]_{d,p}^{t_{res}} \times w_{d,p}^{t_{res}}}{100} \quad (30)$$

453 Here, $N_p^{return,t}$ is the number of returning metal droplets, $[wt\ pct\ Mn]_{d,p}^{t_{res}}$ and $w_{d,p}^{t_{res}}$ are the
454 concentration of Mn and the weight (kg) of a droplet for a given size class at the time of its re-
455 entry to the molten bath at a given blowing time, t.

456 **5. Model assumptions and input data**

457 The following are the list of assumptions, which has been made in developing the kinetic model
458 for demanganisation in a BOF process.

- 459 1. The mass transfer of manganese only takes place at three reactive zones i.e. (i) jet
460 impact area, (ii) slag-bulk metal, and (iii) slag-metal-gas emulsion.
- 461 2. The manganese refining in the slag-metal emulsion and slag-metal bulk zone was
462 assumed to be proceeded by Mn and FeO reaction.
- 463 3. The equilibrium manganese distribution ratio (L_{Mn}) between the metal droplet and slag
464 was assumed to be the same as between bulk metal and slag. Suito's empirical
465 correlation of L_{Mn} was considered for the calculation of manganese equilibrium at metal
466 droplet -slag interface in the emulsion phase.
- 467 4. A linear hot metal temperature profile which varies between 1623-1923 K (1350-1650
468 °C) for Cicutti's heat data^[24] and between 1603-1973 K (1330-1700 °C) for Holappa's
469 data^[42] has been used in the model calculations. The authors acknowledge that a linear
470 temperature profile is a simplified assumption and type of additions (flux, iron ore) can
471 have a significant effect on the thermal profile of the melt and need to be taken into
472 account in the future dynamic model.
- 473 5. As reported by Cicutti *et al.*,^[24] the initial droplet size spectrum was assumed to vary
474 between 2.3×10^{-4} m to 3.35×10^{-3} m. The entire size range of droplets has been divided
475 into different sizes groups and an average weight of droplets corresponds to each group
476 was estimated by applying Rosin- Rammler- Sperling (RRS) distribution function.^[39]

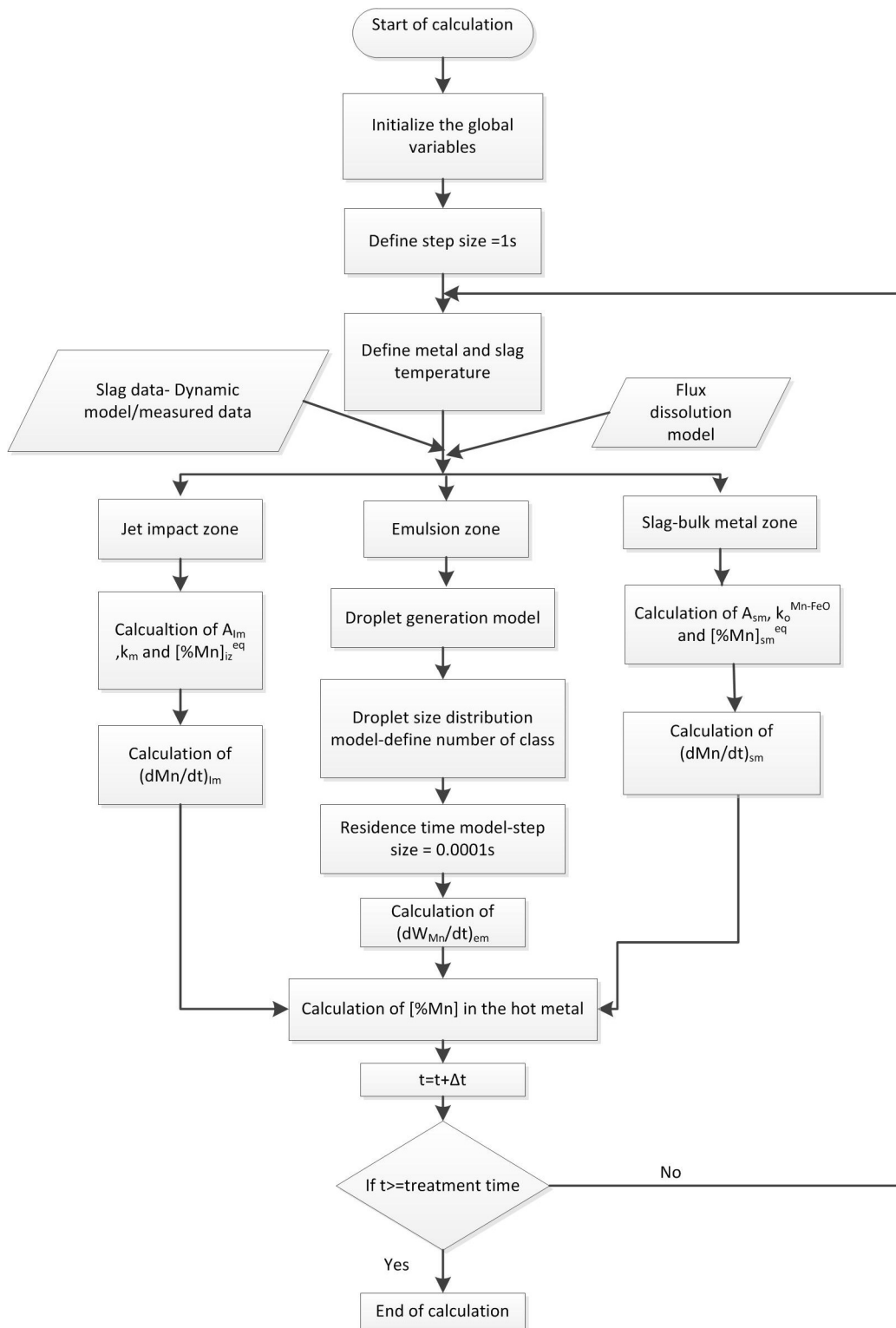
477 The details about the size distribution model of ejected droplets can be found in a
478 previous study by Rout *et al.* ^[18] Six size groups of different droplet size ranges have
479 been considered for the present model calculations.

480 The experimentally measured data from a 200 t combined blowing converter ^[24], and a 55 t top
481 blowing converter ^[42] was used for model validation. In both the furnaces, samples of metal
482 and slag are collected during seven different times of blowing from the start of the blow. For
483 the 55 t converter data reported by Holappa *et al.*, ^[42] the precise information about the time
484 and amount of flux addition during the converter operation was not found. Apart from the
485 addition of lime and converter dust, fluorspar, bauxite and calcium borate was reported to use
486 as a fluxing agent in the converter operation. Due to unavailability of the precise information
487 about the time of addition of these flux materials, a predictive slag model could not be possible
488 for Holappa's data.

489 Thus in the kinetics analysis of manganese refining for Holappa's data, the measured slag data
490 at different time intervals of blowing period have been used through an interpolation technique
491 as input in each step of model calculations. However, for the model used for Cicutti's data, a
492 dynamic slag generation model that includes the evolution of iron oxide in slag based on
493 oxygen mass balance and flux dissolution model have been incorporated. The model details
494 can be found in our earlier publication. ^[18].

495 **6. Computational strategy**

496



497

498

Figure 5: Calculation steps for Mn refinement model for a BOF process

499

The computational program uses finite difference method to compute the concentration of

500

manganese in the hot metal in the next time step by using the known data in the previous time

501

step. The simulation starts at blowing time of 2.2 minutes because only data is available at this

502 time. All the initial inputs are entered into the model at this time. An optimum time step of 1s
503 is chosen for calculation of bath Mn concentration. For the 55 t converter, the slag composition
504 at each time step of calculation was calculated by using interpolation between the measured
505 data points. These slag composition data were dynamically entered into the model as an input
506 at each time step. However, in the 200 t converter, a dynamic slag generation model ^[18] was
507 coupled with the model for the estimation of bulk Mn concentration at each computational time
508 step.

509 Figure 5 demonstrates the algorithm of the mathematical model used for computing the change
510 in manganese concentration in the bulk metal. Initially, the global input variables such as gas
511 constant, molecular weight, lance profile, top and bottom flow rate, hot metal weight were
512 entered into the central model. The scrap dissolution model, based on the previous model
513 results by Dogan *et al.*^[43], was assumed that 30 t of scrap in Cicutti's heat dissolve at a constant
514 rate within the first seven minutes of the blow. The temperature profiles in the hot metal, slag
515 and in the jet impact area were estimated based on predefined functions. The temperature at
516 the slag-droplet interface was calculated by applying Eqs. 26 and 27. The physical properties
517 such as density and viscosity of slag were estimated as a function of their composition and
518 temperature. The density of slag at each time step was calculated using partial volume
519 method^[44] and modified Urbain model^[45] was applied to estimate the slag viscosity.

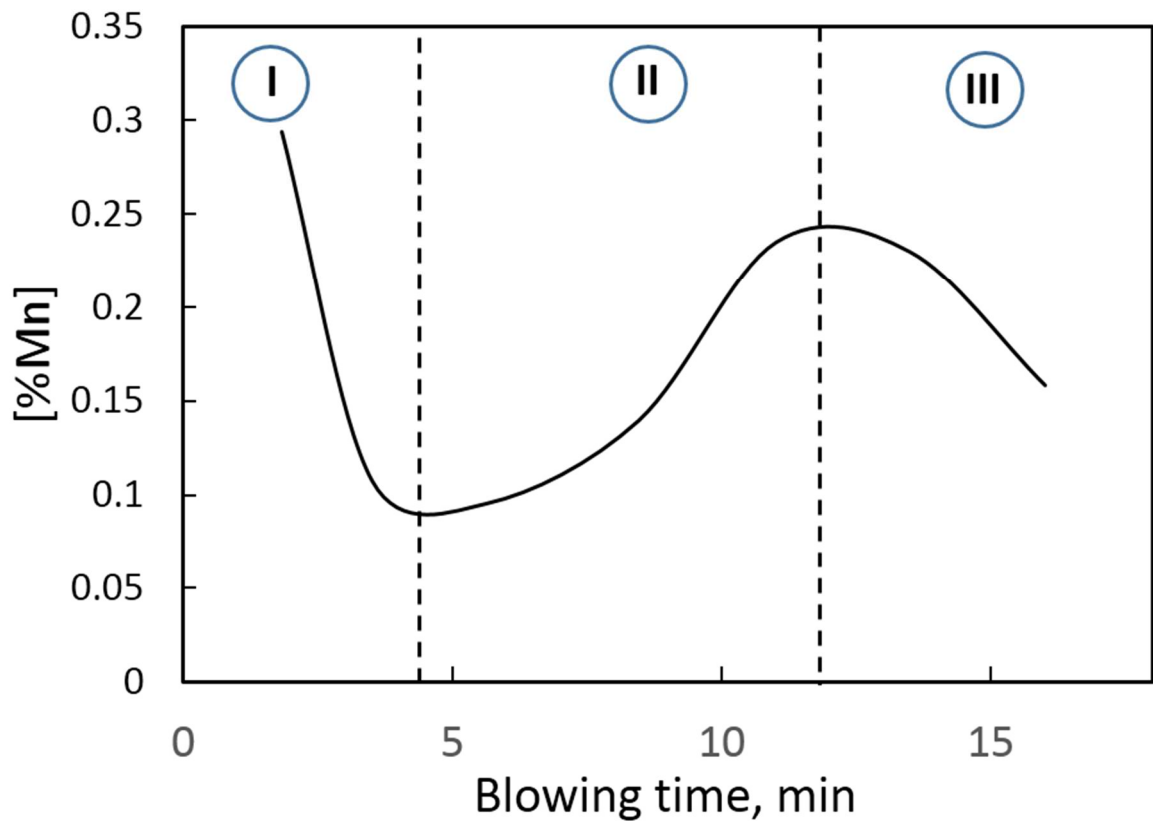
520 Flux dissolution (lime and dolomite) rate was calculated as a function of temperature and
521 physical properties of slag and metal. Previously developed flux dissolution model by Dogan
522 *et al.*^[46] was applied in the present work to determine the amount of dissolved flux in slag at
523 each numerical time step. In the calculation of manganese refining rate in emulsion zone, the
524 overall size spectrum of droplets has been divided into six classes, and the degree of manganese
525 refining was calculated individually for each class by use of microkinetics sub-model discussed

526 in section 4.3.1. An optimum numerical time step of 0.0001s, as already discussed in our
527 previous work^[18], has been chosen to calculate the residence time of the metal droplets in each
528 class of diameter. By use of the droplet-generation sub-model^[20], the total weight of the Mn in
529 the droplet ejects into the emulsion phase was estimated by using Eq. 29. The total amount of
530 manganese returning to the bulk metal after refining by the emulsion was determined by
531 summing the weight of Mn in the entire population of returning droplets (Eq. 30). The total Mn
532 refining rate through emulsion zone was estimated from the difference between the ejected
533 mass of Mn and their return to the emulsion, as shown in Eq. 28. Similarly, sub-models to
534 calculate the rate of Mn removal from slag-bulk metal and jet impact zone were developed by
535 applying Eq. 11 and Eq. 16. Through Eq. 8-10, the rate of Mn refined from all the zones were
536 combined, and mass balance has been performed to estimate the change in concentration of
537 manganese in the hot metal. All the numerical computation has been carried out by using
538 MATLAB® version 2016a. The model input parameters used in the calculation for the two
539 different converters are listed in Appendix A.2. (Table A1 and Table A2).

540 **7. Results and Discussions**

541 **7.1. Analysis of oxidation and reduction reaction of Mn in a BOF**

542



543

544 Figure 6: Typical manganese refining path in a top blowing converter.^[22,24] Region I: rapid
 545 manganese oxidation, Region II- manganese reversion from slag to metal, Region III:
 546 manganese oxidation

547 A typical variation of Mn concentration in the hot metal during the blow period is shown in

548 **Fig. 6.** ^[22, 24] The evolution of Mn in the molten bath can be broadly divided into three stages:

549 (1) rapid oxidation of Mn from the hot metal at early stage of blow, (2) reversion of Mn from

550 slag to metal during the middle stage of blowing, and (3) finally Mn oxidation towards the end

551 blow period. As discussed in the earlier sections, manganese reaction primary takes place either

552 by direct reaction with O₂ or with FeO in the slag. The competition between these reactions

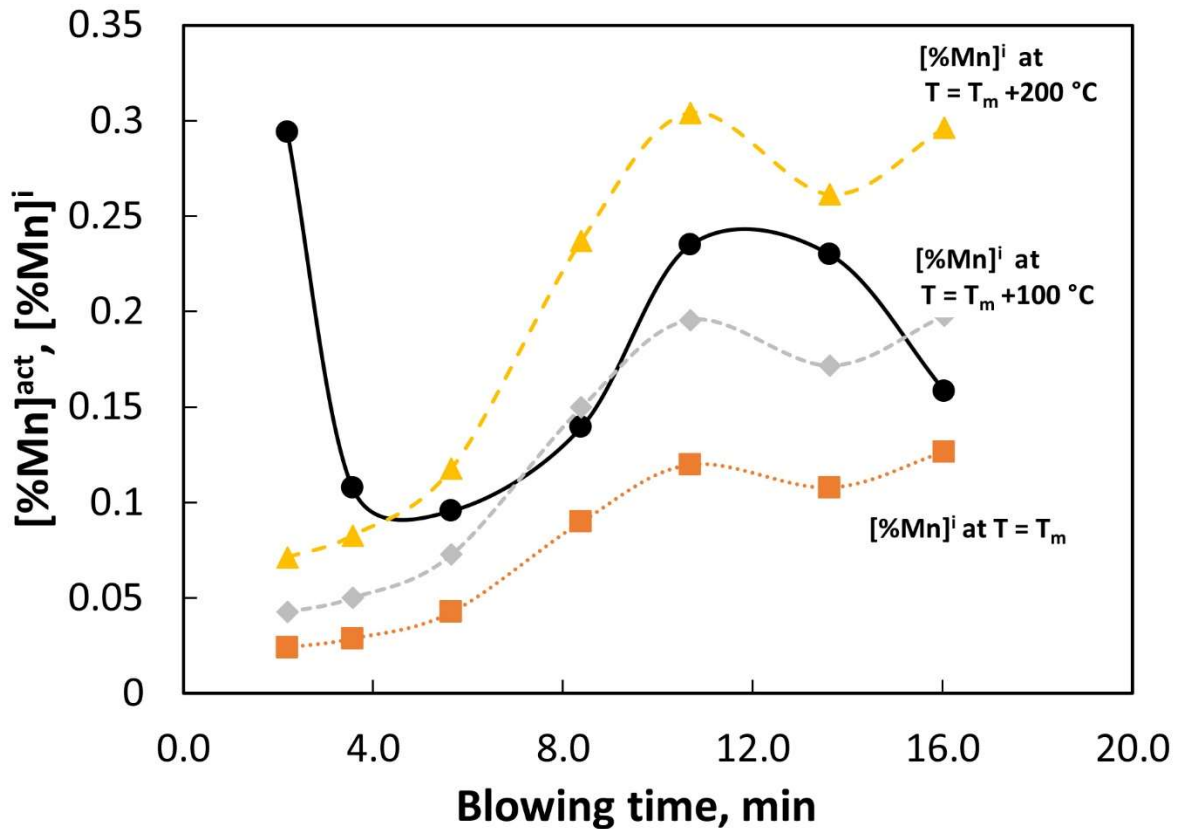
553 determines the overall rate and direction of Mn mass transfer.

554 The equilibrium Mn concentration at different interfaces has been calculated as a function of

555 slag composition and temperature. The estimated value of [wt pct Mn]ⁱ at the gas-metal

556 interface in jet impact zone was found in the order of 10⁻⁵, which implies that the reaction at

557 the jet impact region has a strong positive driving force for Mn oxidation.



558

559 Figure 7: Effect of temperature on the equilibrium manganese at slag-metal interface (solid
 560 line- actual Mn in bath, dotted line- interfacial Mn concentration estimated at different slag-
 561 metal interface temperatures, T_m- Hot metal temperature (as measured during blowing time)
 562 and T is the interface temperature

563 However, the value of the interfacial concentration of Mn calculated by considering Mn/MnO
 564 equilibrium at slag/metal interface was found to have values in the same order as the manganese
 565 concentration in the hot metal bath. Since the metal droplets are originated from the periphery
 566 of jet impact region, it is likely that the interface between the metal droplets and slag may
 567 experience higher temperature than the bulk metal. Similarly, as reported in previous studies,
 568 the bulk-metal and slag interface can exhibit higher temperature than the bulk melt; a difference
 569 of 200 to 400 °C between the surface and bottom of the vessel has been reported by Rote and
 570 Flinn.^[28] The effect of temperature on the equilibrium concentration of Mn at slag/metal
 571 interface has been illustrated in **Fig. 7**. It should be noted that the slag concentration is changing
 572 during the blow period according to the measured values in the Mn equilibrium calculation.

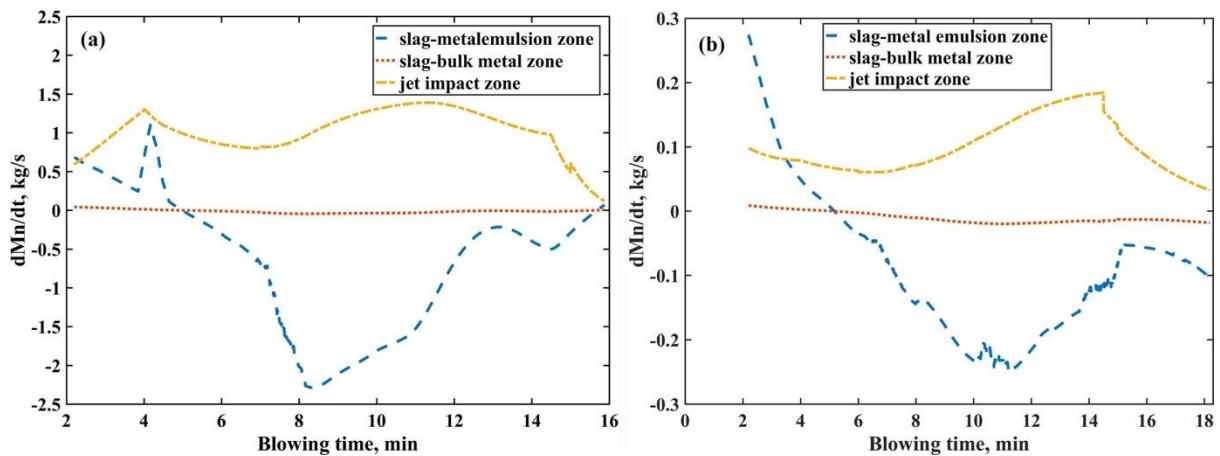
573 When the temperature of the interface was maintained as the bulk metal temperature the
574 equilibrium line was found to be always lower than the actual Mn in the metal. In spite of the
575 change in oxygen potential (slag composition) and hot metal temperature in the calculation, the
576 shape of the bulk Mn concentration was not explained by the predicted equilibrium
577 concentration. However, as the interface was raised to 100 °C above the bulk temperature the
578 value of [wt pct Mn]ⁱ was increased above the bulk Mn concentration and some reversion was
579 found during the intermediate stage of blowing. Further, the oxidation of Mn during the early
580 blow and reversion after 5 min of the blow was noticed when the temperature of the droplet/slag
581 interface was raised to 200 °C above the bulk metal temperature. The change in the direction
582 of equilibrium driving force was undoubtedly noticed when the temperature of the interface
583 increased. In the earlier publication, the authors have mapped the variation of the temperature
584 profile in different interfaces of the converter during the blowing period. [18] It was observed
585 that the droplet surface exhibits 90 to 200 K higher temperature than the hot metal. The droplet
586 surface temperature was predicted to increase linearly in most part of the blow, except towards
587 the end blow a decreasing trend is observed due to a reduction in hot spot temperature.
588 Therefore, it may be inferred that the high temperature prevailing at the reaction interface at
589 the droplet-slag interface is one of the significant factors that control the oxidation and
590 reduction behaviour of manganese in the top blowing process.

591 Based on our understanding of manganese equilibrium for the reactions described in Eq. 1 and
592 Eq. 6, the kinetics of manganese transfer can be qualitatively evaluated. Table 1 summarizes
593 the reactions involving Mn and their direction during the different stages of the BOF operation.

594 **7.2. Mn refining in different reactive zones in the converter**

595 The rate of manganese refined by the three distinct zones inside the BOF converter as a function
596 of blowing time has been shown in **Fig. 8**. In the jet impact region, the transfer of manganese

597 from metal to slag was found to be increasing in the initial part of the blow for 200 t converter
 598 data reported by Cicutti *et al.*^[24] However, a decreasing trend has been observed for the 55 t
 599 converter operation during the initial stage. The difference in the Mn refining profile by jet
 600 impact zone during the starting period may be due to the difference in lance practice adopted
 601 in the different converters. In Cicutti's heat data the lance position has started with high (2.5
 602 m) and then lowered to the low position (2.2 m) after 4 minutes of blowing. However, in
 603 Holappa's data, the lance position was started with low position (0.9 m) and then raises to a
 604 high position (1.1 m) after 5 minutes. Decreasing in lance height increases the cavity area and
 605 thus enhances the kinetics of Mn reaction at jet impact region, which was reflected in Cicutti's
 606 heat data. A similar trend of refining profile of Mn in jet impact area for the intermediate and
 607 final stage of converter operation has been observed for both the heats. The increase in Mn
 608 refining during the middle stage of the blow and finally decreasing towards the end blow period
 609 may be caused by the reduction in the jet impact temperature which exerts a substantial effect
 610 on the overall mass transfer coefficient (k_m) of Mn reaction kinetics.

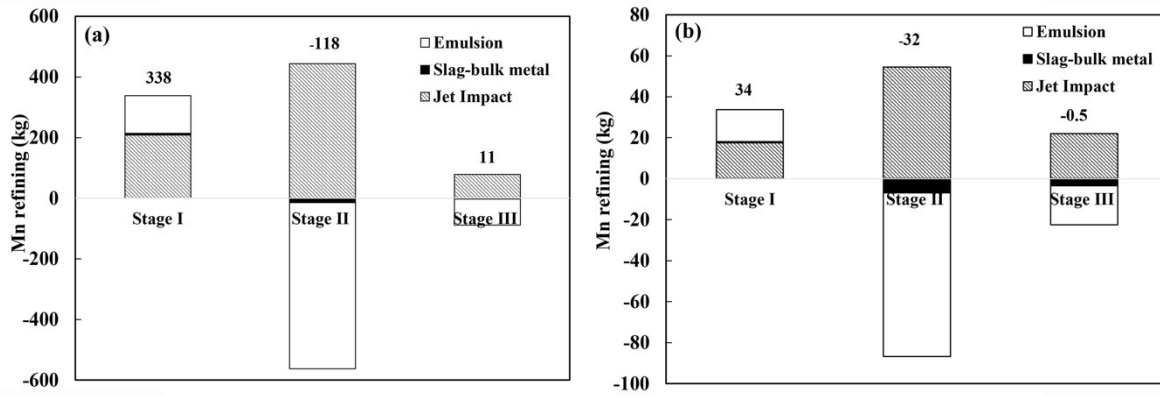


611

612 Figure 8: Mn removal rate calculated from different zones of the converter as a function of
 613 blowing time (a) 200 t converter (b) 55 t converter

614 The manganese removal rate by the circulating metal droplets in the emulsion has been
 615 computed for both cases and shown in Fig. 8. As seen from the figure, during the initial part,

616 up to 5 min after the start of blowing, the rate of manganese transfer was found to be positive,
617 which indicates the oxidation of manganese has been favored during this period. The transfer
618 of manganese from metal droplet to slag is possible due to the low value of [wt pct Mn]ⁱ as a
619 result of low temperature, high FeO, and low basicity during this period. However, as the blow
620 progresses, the droplet surface temperature raises, FeO in slag decreases due to rapid
621 decarburisation and as a result basicity increases, which initiates the conditions for the
622 reversion of MnO from slag to the metal droplets. A significant fraction of manganese has been
623 observed to be transferred from slag to metal by the emulsion phase during the middle stage of
624 the blow. The peak reversion has been found to take place during 50 to 60% of blowing time.
625 At the end stage of the blow, due to a small value of residence time of metal droplets in the
626 emulsion, the rate of manganese transfer by the droplets approaches to zero. Further, it has
627 been observed that the rate of manganese transfer in the slag-bulk metal zone is almost
628 negligible as compared to jet impact and emulsion zone refining during the entire blow period.
629 The reason may be due to the availability of a small area for the reaction that limits the kinetics
630 of Mn refining in this zone. In the heat data provided by Holappa et al. for the 55 t LD-
631 converter, the total iron oxide in the slag was observed to decrease (end blow Fe_tO ~12 wt pct)
632 during the last stage of the blow. Since the oxygen flow rate was held constant, the decreasing
633 of slag iron oxide may be resulted from the lowering in lance position (1.25 m to 1.1 m) during
634 14 to 18 min of blowing. However, in Cicutti's heat no variation in oxygen flow rate and lance
635 height was made during the last stage of the blowing and an increasing iron oxide trend was
636 reported (end blow Fe_tO ~22 wt pct). The variation in the iron oxide evolution in two different
637 converters may be the reason for the difference in Mn refining prediction during the last 2 min
638 of the blowing shown in Fig. 8. Due to low iron oxide in slag, the Mn refining prediction in
639 Holappa's heat shows a reversion during the final stage of the blowing.



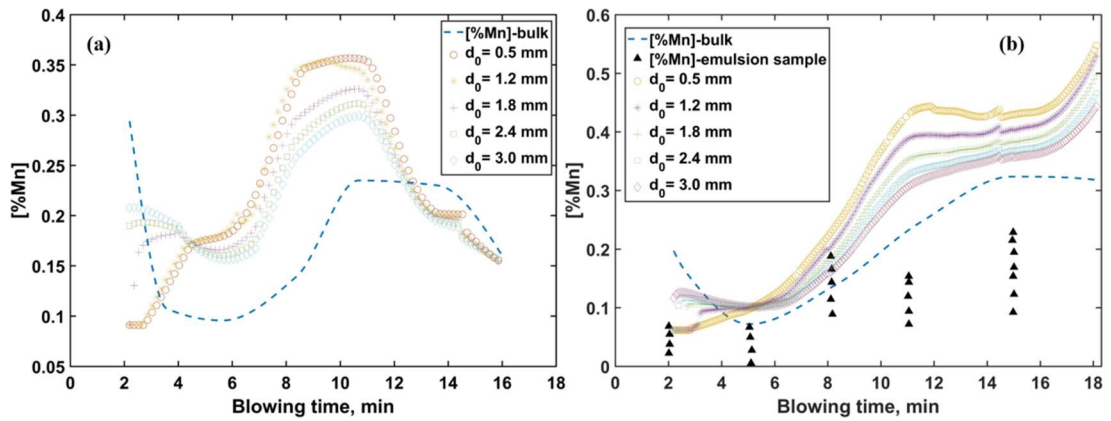
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641 Figure 9: Total Mn exchange between metal and slag at different stages of the blowing (a)
 642 200 t converter (b) 55 t converter

643 The total amount of manganese removed by each reaction zone during different stages of the
 644 blow has been computed by using the mathematical model. Based on the observed Mn profile,
 645 the entire blowing period has been divided into three stages: Stage I (0 to 30% of blow), Stage
 646 II (30 to 80% of blow), and stage III (80 to 100% of blow). Total Mn refining by each reaction
 647 zone has been obtained from the **Fig. 9** by computing the area under the curve in the three
 648 different regimes of blowing. The result shows that there is always a positive thermodynamic
 649 force for manganese oxidation during the initial stage of the blow. The enhanced manganese
 650 refining observed at the beginning of the blow is caused by oxidation of droplets in the
 651 emulsion in addition to the oxidation in jet impact region. The competition between the
 652 oxidation and reduction particularly in the jet impact zone and emulsion determines the
 653 direction of manganese transfer in second and end stage of the blow. In the middle stage of the
 654 blow, it has been observed that the reduction of MnO by the metal droplets dominates, which
 655 was found to be the main reason for a manganese reversion from slag to metal.

656 **7.3. Analysis of Mn reaction kinetics in emulsion**

657



658

659 Figure 10: Mn refining of a metal droplet inside the emulsion phase; the dotted line represents
 660 the bulk concentration (measured) and the other symbols represent the concentration of Mn in
 661 the droplet at the time of returning to the bath (simulated) (a) 200 t converter data (b) 55 t
 662 converter data; the solid symbol represents the measured Mn in emulsion

663

664 The kinetics of manganese transfer between metal droplets and the slag is dependent on the
 665 interfacial concentration, the size of initial droplets and their bloating behavior as a result of
 666 decarburization reaction. **Figure 10** shows the concentration of Mn in the refined droplets of
 667 different sizes as a function of blowing time. As can be seen from the figure, the manganese
 668 concentration of the droplets at the time of return to the bulk melt nearly follows the refining
 669 path of Mn in the bulk metal for both the converters under investigation. Further, it was
 670 observed that the rate of oxidation or reduction of smaller sized droplets is higher as compared
 671 to the larger ones. The reason for this may be due to longer residence time and high surface
 672 area/volume ratio associated with smaller sized droplets.^[21] As a result of which the reactions
 673 in small-sized droplets approaches the equilibrium concentration quickly. However, the big
 674 droplets having small residence time and surface area to volume ratio do not complete
 675 equilibrium and consequently contribute less towards the conversion process.^[21] The fast rate
 676 of decarburisation associated with the droplets of diameter of the range ~0.5 mm (predicted
 677 decarburisation efficiency is more than ~70% during the entire blowing period)^[21] accelerates
 678 the bloating process and thus results in increasing the reaction time between the droplet and
 679 slag to achieve the final equilibrium Mn concentration.

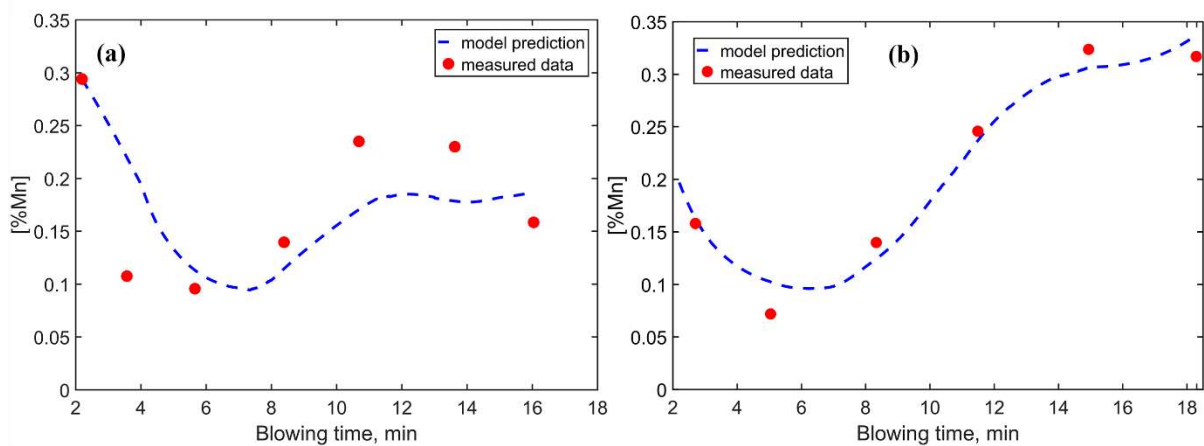
680 The present result agrees well with the observation made by Millman *et al.*^[47] in a 6 t pilot
681 scale converter experiments. The authors reported that during the middle blow period (after 10
682 min) the Mn pick up from the slag to droplet takes place for specific size range (1 to 3 mm) in
683 the emulsion layer. The present model calculation predicts that the Mn pick up by the droplets
684 in the lower region of the size spectrum makes a greater contribution to the reversion process.

685 Holappa *et al.* ^[42] measured the manganese concentration in the emulsion during the blowing
686 time which has been shown in **Fig. 10 (b)**. It can be seen that during the initial stage of the
687 blow the predicted value of droplet manganese concentration agrees reasonably well with the
688 measured concentration in the emulsion, whereas a difference between the predicted and the
689 measured value has been observed at an intermediate stage of blowing. The cause of this
690 deviation could not be explained by this study since a significant reversion of bulk Mn
691 concentration has been observed during middle and end stage of blowing, although the
692 emulsion Mn concentration shows a lower value than the bulk. It is noteworthy that the reported
693 manganese concentration in the emulsion represents the average concentration of the droplets
694 in the emulsion at a particular instance of blowing time, whereas the predicted Mn by the model
695 is the concentration of refining droplets (at the time of re-entry to the bath). This could be one
696 of the reasons for the difference between the model prediction and actual measurement.

697 **7.4 . Model validation with the measured hot metal composition**

698 The rate of manganese refining from three different zones are combined and mass balance has
699 been applied in the hot metal to compute the bath Mn concentration (in wt pct) at each time of
700 blowing. The model prediction of change in concentration of Mn in the bulk metal as a function
701 of blowing time is shown in **Fig. 11**. The model calculation of Mn has been compared with the
702 actual Mn value measured in the hot metal for two different converters. As can be seen from
703 the **Fig. 11. (a)**, in Cicutti's heat data, the predicted Mn matches well with the actual Mn

704 particularly during the early part of the blow. However, a small deviation has been observed
 705 towards the end of the blow. It may be due to the inaccurate calculation of manganese
 706 equilibrium at slag-metal droplet interface. Further experimental studies are needed to establish
 707 the manganese distribution between the slag and metal droplet in the emulsion. This model has
 708 also been applied to a different converter of 55 t capacity. As shown in **Fig. 11. (b)**, good
 709 agreement between the measured and predicted values was observed. It should be noteworthy
 710 to mention that in contrast to the difference between the emulsion sample measurement and the
 711 refined droplets (in **Fig 10. (b)**), Jalkanen *et al.*'s heat data^[48] of Mn refining of bulk metal
 712 profile shows a great consistency with the predicted values. Several authors indicated that the
 713 way the samples (in a blow, after blow stopping, height and time of sampling) are collected
 714 from the emulsion, can have a significant influence on droplet characteristics. ^[49, 50] However,
 715 the sampling procedure was not mentioned in Jalkanen's study and thus the substantial
 716 reversion observed in the bulk metal due to the cause of slag/metal droplet reversion as
 717 predicted by the model, was not conclusively verified. This needs a further experimental study
 718 to investigate the reversion mechanism of Mn to establish the current hypothesis.



719

720 Figure 11: Model validation of Mn prediction in hot metal (a) Cicutti *et al.* data^[24] (b)
 721 Jalkanen *et al.* data^[46]

722 **8. Conclusions**

723 A kinetic model for Mn reaction in BOF has been developed. The computational model can
724 predict the change in manganese concentration in the bulk metal during the blow period by
725 estimating the rate of refining from different zones of the converter. The following conclusions
726 are made from this study:

- 727 1. The temperature at the slag–metal droplet interface plays a major role in deciding the
728 oxidation and reduction behaviour of Mn reaction. Higher interface temperatures lead to
729 decrease in thermodynamic driving force for the mass transfer from metal droplets to slag.
- 730 2. The kinetics of Mn refining in the first stage of the blow is controlled by the oxidation of
731 Mn by FeO in the emulsion and direct oxidation of Mn by O₂ in the jet impact zone.
- 732 3. Competition between the Mn oxidation in the jet impact zone and reduction of MnO by Fe
733 in the metal droplets in emulsion zone determines the direction of Mn transfer during
734 middle and end period of the blow.
- 735 4. In the middle stage of the blow, after 30 to 40 % of blowing, a significant fraction of Mn
736 reversion was observed to take place in the emulsion zone. Due to a large increase in
737 temperature of the droplet-slag interface, the reaction (Eq. 1) proceeds in the reverse
738 direction which was found to be the primary reason for manganese reversion.
- 739 5. During the last stage of the blow, the refining of Mn is a result of simultaneous reaction at
740 jet impact and emulsion zones. The reaction (Eq. 1) direction at slag-metal droplet interface
741 controls the conversion process in this period.
- 742 6. The rate of Mn oxidation in the emulsion is predicted to be a strong function of droplet
743 diameter and the residence time. Small sized droplets have high conversion capacity than
744 the large diameter ones.

745 **Acknowledgement**

746 The authors acknowledge their gratitude to Tata Steel for providing financial support for this
 747 work.

748 **Nomenclature**

- 749 A- Area of the reaction interface (m²)
 750 C_{p,m} – Heat capacity of bulk metal (J/kg)
 751 C_{p,s} – Heat capacity of slag (J/kg)
 752 d_p – Diameter of the droplet (m)
 753 $\left(\frac{dMn}{dt}\right)_{overall}$ – Overall manganese refining rate (kg/s)
 754 $\left(\frac{dMn}{dt}\right)_{iz}$ - Manganese refining rate in jet impact zone (kg/s)
 755 $\left(\frac{dMn}{dt}\right)_{sm}$ - Manganese refining rate in slag-bulk metal zone (kg/s)
 756 $\left(\frac{dMn}{dt}\right)_{em}$ - Manganese refining rate in emulsion zone (kg/s)
 757 J_{Mn} – Manganese reaction rate (kg/s)
 758 H- Bath height (cm)
 759 L- Bath diameter (cm)
 760 k_{overall}- Overall mass transfer coefficient (m/s)
 761 k_m – Mass transfer coefficient in metal phase (m/s)
 762 k_m^{drop} - Mass transfer coefficient of metal droplet (m/s)
 763 $k_{overall}^{em}$ - Overall mass transfer coefficient in emulsion (m/s)
 764 k_s – Mass transfer coefficient in slag phase (ms⁻¹)
 765 k'_{Mn} – Apparent equilibrium constant of Mn (-)
 766 K – Equilibrium constant (-)
 767 L_{Mn} – Equilibrium manganese partition ratio (-)
 768 [%Mn]^{eq} – Equilibrium manganese concentration (wt pct)
 769 [%Mn]ⁱ – Manganese concentration at slag metal interface (wt pct)
 770 P_{O₂} – partial pressure of oxygen inside the furnace (atm)
 771 $N_p^{eject,t}$ – Number of droplets of pth class size ejects to the bath at blowing time t (-)
 772 $N_p^{return,t}$ – Number of droplets of pth class size returns to the bath at blowing time t (-)
 773 P- Number of divisions in the droplet size spectrum (-)
 774 Re- Reynolds number (-)
 775 R_{B,T}- Droplet generation rate (kg/s)
 776 Sc- Schmidt number (-)
 777 Sh- Sherwood number (-)
 778 t_{res}- Residence time of droplet in emulsion (seconds)
 779 T_m- Temperature of the hot metal (K)
 780 T_{iz}- Temperature at the impact zone (K)
 781 T_{drop} -Interface temperature at slag–metal droplet (K)
 782 T_∞- Temperature in the emulsion medium (K)
 783 T₀ - Initial temperature of the metal drop at the time of ejection (K)
 784 u- Velocity of the droplet (m/s)
 785 W_b – Weight of bulk metal (kg)
 786 $W_{Mn}^{eject,t}$ - Mass of metal ejected into emulsion at time t (kg)
 787 $W_{Mn}^{return,t}$ - Mass of metal droplet returns to the bulk metal at time t (kg)

788

789 **Greek symbols**

790 ρ_m – Density of the bulk metal (kg/m³)

791 ρ_s – Density of slag (kg/m³)

792 λ_m - Thermal conductivity of liquid metal (W/m K)

793 λ_s - Thermal conductivity of slag (W/m K)

794 ε – Stirring energy (W/t)

795 μ - Viscosity (Pa.s)

796

797 **Subscripts and Superscripts**

798 **cav-** Cavity

799 eq- Equilibrium

800 em- Emulsion

801 gm- Gas/metal

802 i- Interface

803 iz- Impact zone

804 m- Hot metal

805 sc- Scrap

806 sm-Slag/metal

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883

884 **Appendix:**

885 **A1. Calculation of total stirring energy:**

886 The following equations have been applied to estimate the stirring power due to the combined
887 effect of both top and bottom blowing [⁴⁰]:

$$\epsilon = \epsilon_t + \epsilon_b \quad (\text{A1})$$

$$\epsilon_t = 6.32 \times 10^{-7} \cos(\alpha) \frac{Q_{O_2} M_{O_2}}{W_b n_n^2 d_t^3 L_h} \quad (\text{A2})$$

888

$$\epsilon_b = \frac{6.18 Q_b T_m}{W_b} \left(\ln \left(1 + \frac{\rho_m g H}{P_a} \right) + \left(1 - \frac{T_b}{T_m} \right) \right) \quad (\text{A3})$$

889 Where ϵ_t and ϵ_b are the specific mixing power (W/t) due to top and bottom gas injection
890 respectively. α is the angle of the lance with the vertical axis (rad), Q_{O_2} is the oxygen flow
891 rate (Nm³/min), n_n is the number of nozzles in the lance tip, d_t is the throat diameter (m), L_h
892 is the lance height from the bath level (m), Q_b is the bottom blowing rate (Nm³/min), P_a is the
893 atmospheric pressure (atm) and T_b is the temperature of the injected bottom gas.

894 **A.2. Input data used for model validations**

895 **Caption List**

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898 **Figure 2:** Comparison of actual Mn in the metal and the interfacial Mn calculated from
 899 Suito’s equilibrium distribution models: Slag and hot metal composition data were taken
 900 from a top blowing process

901 **Figure 3:** Schematic representation of oxidation/reduction reactions of Mn across various
 902 interfaces in a BOF **Figure 4:** Transport process of Mn at metal drop and slag containing iron
 903 oxide interface in the emulsion zone

904

905 **Figure 5:** Calculation steps for Mn refinement model for a BOF process

906 **Figure 6:** Typical manganese refining path in a top blowing converter. ^[22, 24] Region I: rapid
 907 manganese oxidation, Region II- manganese reversion from slag to metal, Region III:
 908 manganese oxidation

909 **Figure 7:** Effect of temperature on the equilibrium manganese at slag-metal interface (solid
 910 line- actual Mn in bath, dotted line- interfacial Mn concentration estimated at different slag-
 911 metal interface temperatures), T_m - Hot metal temperature (as measured during blowing time)
 912 and T is the interface temperature

913 **Figure 8:** Mn removal rate calculated from different zones of the converter as a function of
 914 blowing time (a) 200 t converter (b) 55 t converter

915 **Figure 9:** Total Mn exchange between metal and slag at different stages of the blowing (a)
 916 200 t converter (b) 55 t converter

917 **Figure 10:** Mn refining of a metal droplet inside the emulsion phase; the dotted line
 918 represents the bulk concentration (measured) and the other symbols represent the
 919 concentration of Mn in the droplet at the time of returning to the bath (simulated) (a) 200 t
 920 converter data (b) 55 t converter data; the solid symbol represents the measured Mn in
 921 emulsion

922 **Figure 11:** Model validation of Mn prediction in hot metal (a) Cicutti's data^[24] (b) Jalkanen
 923 and Holappa. data^[48]

924 **List of Tables**

925 Table 1: Possible reactions and their direction for Mn refining in BOF operation

Reaction/stages	Reaction 1 (Emulsion)	Reaction 3 (Jet impact zone)
Stage I (0 – 30%)	Forward (Mn flows from metal to slag)	Forward (Mn flows from metal to slag)
Stage II (30- 80%)	Forward/Backward – Depends on slag composition and T	Forward (Mn flows from metal to slag)

Stage III (80-100%)	Forward/Backward – Depends on slag composition and T	Forward (Mn flows from metal to slag)
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926

Table A1: Input data for model calculation: Cicutti *et al.* [24]

Input parameters	Value
Initial hot metal composition (Blowing time = 2.2 min)	170000 kg, wt pct C= 3.86, wt pct Si = 0.19, wt pct Mn = 0.29, wt pct P = 0.065
Scrap composition	30000 kg, wt pct C = 0.08, wt pct Si = 0.001, wt pct Mn = 0.52
Hot metal temperature	1623- 1923 K (1350- 1650 °C)
Initial slag composition and weight	Initial slag weight at 2.2 min = 5200 kg, total lime added = 7600 kg, Iron ore = 1900 kg, Quartzite = 800 kg Slag composition : wt pct CaO = 27, wt pct FeO = 33, wt pct SiO ₂ = 17, wt pct MnO = 13.5, wt pct MgO = 5, wt pct P ₂ O ₅ = 4.5
Oxygen blow	620 Nm ³ /min, six hole lance
Bottom blow (Ar/N ₂)	2.5 – 8.33 m ³ /min
Lance height	2.5, 2.2, 1.8 m
Steel density	7000 kg/m ³
Slag density	Partial molar volume method [44]
Surface tension of steel	1.7 N/m
Viscosity of slag	Modified Urbain model [45]
Diffusion coefficient in metal phase at 1873K (1600 °C)	C- 2.0×10^{-9} m ² /s, Si – 3.8×10^{-9} m ² /s, Mn - 7×10^{-9} m ² /s, P- 4.7×10^{-9} m ² /s
Gas fraction in emulsion	0.8
Droplet diameter	2.3×10^{-4} m to 3.35×10^{-3} m
Angle of droplet ejection	60 degree

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Table A2: Input data for model calculation: Holappa *et al.* [40]

Input parameters	Value
Initial hot metal composition (Blowing time = 2.2 min)	48000 kg, wt pct C= 3.88, wt pct Si = 0.073, wt pct Mn = 0.2, wt pct P = 0.026
Scrap composition	5000 kg, wt pct C = 0.08, wt pct Si = 0.001, wtpct Mn = 0.52
Hot metal temperature	1603- 1973 K (1330- 1700 °C)
Slag composition and weight	Initial slag weight at 2.2 min = 1376 kg, Iron ore = 900 kg (dust) Dynamic slag data
Oxygen blow	130 Nm ³ /min, three-hole lance, lance angle 15 degree
Bottom blow (Ar/N ₂)	0
Lance height	1.0m, 1.1m, 1.2m, 1.5m
Steel density	7000 kg/m ³
Slag density	Partial molar volume method [44]
Surface tension of steel	1.7 N/m
Viscosity of slag	Modified Urbain model [45]
Diffusion coefficients	C- 2.0×10^{-9} m ² /s, Si – 3.8×10^{-9} m ² /s, Mn - 7×10^{-9} m ² /s, P- 4.7×10^{-9} m ² /s
Gas fraction in emulsion	0.8
Droplet diameter	2.3×10^{-4} m to 3.35×10^{-3} m
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935