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## **Spatiotemporal Models of an Estuarine Fish Species to Identify Patterns and Factors Impacting Their Distribution and Abundance**

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# Estuaries and Coasts

## Spatiotemporal models of an estuarine fish species to identify patterns and factors impacting their distribution and abundance

--Manuscript Draft--

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<b>Abstract:</b>	<p>Understanding the distribution and abundance of organisms can be exceedingly difficult for pelagic fish species that live in estuarine environments. This is particularly so for fish that cannot be readily marked and released or otherwise tracked, such as the diminutive delta smelt, <i>Hypomesus transpacificus</i>, endemic to the San Francisco Estuary. The environmental factors that influence distribution operate at multiple scales, from daily tidal cycles and local perceptual fields to seasonal and annual changes in dominant environmental gradients spanning the entire San Francisco Estuary. To quantify scale specific patterns and factors shaping the spatiotemporal abundance dynamics of adult delta smelt, we fit a suite of models to an extensive, spatially resolved, catch survey time series from 13 annual cohorts. The best model included cohort-specific abundance indicators and daily mortality rates, a regional spatial adjustment, and haul-specific environmental conditions. The regional adjustment identified several density hotspots that were persistent across cohorts. While this model did include local environmental conditions, the gain in explained variation was relatively slight compared to that explained by the regional adjustment. Total abundance estimates were derived by multiplying habitat volume by catch density (design-based) and modeled density (model-based), with both showing severe declines in the population over the time period studied. The design-based approaches had lower uncertainty but potentially higher bias. We discuss the implications of our results for advancing the science and improving management of delta smelt, and future data collection needs.</p>

1       Spatiotemporal models of an estuarine fish species to identify patterns and factors impacting  
2                                their distribution and abundance

3

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12

13    Running page head: Distribution and abundance of delta smelt

14 ABSTRACT: Understanding the distribution and abundance of organisms can be exceedingly  
15 difficult for pelagic fish species that live in estuarine environments. This is particularly so for  
16 fish that cannot be readily marked and released or otherwise tracked, such as the diminutive delta  
17 smelt, *Hypomesus transpacificus*, endemic to the San Francisco Estuary. The environmental  
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20 the entire San Francisco Estuary. To quantify scale specific patterns and factors shaping the  
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22 spatially resolved, catch survey time series from 13 annual cohorts. The best model included  
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24 haul-specific environmental conditions. The regional adjustment identified several density  
25 hotspots that were persistent across cohorts. While this model did include local environmental  
26 conditions, the gain in explained variation was relatively slight compared to that explained by the  
27 regional adjustment. Total abundance estimates were derived by multiplying habitat volume by  
28 catch density (design-based) and modeled density (model-based), with both showing severe  
29 declines in the population over the time period studied. The design-based approaches had lower  
30 uncertainty but potentially higher bias. We discuss the implications of our results for advancing  
31 the science and improving management of delta smelt, and future data collection needs.

32

33 KEY WORDS: delta smelt; geostatistical models; population ecology; soap film smoothers; San  
34 Francisco Estuary

## 35 INTRODUCTION

36 Determining how and why an organism's population is distributed in space and time is a  
37 fundamental organizing problem in population ecology (Krebs 1994). For small pelagic species  
38 in tidal river estuaries, drawing inference about their distribution and abundance is especially  
39 challenging because they cannot be tagged and tend to aggregate in schools that are small  
40 relative to the size of their open-water habitats. Tidal river estuaries are ecotones characterized  
41 by almost continuous multi-scale changes in environmental factors, from tidal to annual time  
42 scales and with spatial scale changes ranging from the perceptual field of the organism up to the  
43 entire span of the estuary (Odum 1988). In general, we can expect to need to apply models that  
44 can disentangle the relative effects of processes acting at different spatiotemporal scales.

45  
46 Multi-scale environmental variability can be especially important for small resident pelagic  
47 species (Peebles et al. 2007; Reum et al. 2011). For example, tidal currents can influence vertical  
48 and horizontal distributions so that organisms can maintain or change geographic position within  
49 the estuary (Kimmerer and McKinnon 1987; Bennett and Burau 2015). Also, pelagic species will  
50 move in response to temperature, turbidity, salinity and prey density gradients, all of which can  
51 directly influence vital rates (Peebles et al. 2007; Reum et al. 2011; Rose et al. 2013) and shape  
52 estuary wide and regional distributions. A practical consequence for model-based analysis of  
53 distribution and abundance is that care must be taken to appropriately match the spatiotemporal  
54 resolution of the data and the model. Models must include factors, and allow for predictions,  
55 across multiple spatial and temporal scales simultaneously in order to provide useful insight into  
56 spatiotemporal variability in abundance.

57

58 The San Francisco Estuary (SFE, Fig. 1) is a tidal river estuary ecotone with habitat composition  
59 and structure that changes at multiple temporal and spatial scales (Cloern and Jassby 2012). One  
60 of the largest tidal river estuaries on the west coast of the Americas, the SFE provides habitat for  
61 delta smelt (*Hypomesus transpacificus*), an endemic annual pelagic fish species that inhabits the  
62 low salinity and freshwater portions of the estuary upstream of San Pablo Bay (Fig. 1).

63 Substantial declines in the cohort abundance of delta smelt during the 1980s and early 1990s led  
64 to protection under both the U.S. and California Endangered Species Acts in 1993, and new fish  
65 monitoring programs, including one for the adult life stage. In addition to these spatially and  
66 temporally extensive fish surveys, measurements of several salient environmental metrics have  
67 also been collected in the SFE.

68

69 Delta smelt habitat preferences are relatively well understood (Moyle et al. 2016). The species  
70 distribution is constrained down-estuary by salinity while up-estuary a variety of life stage  
71 specific factors operate, including landward extent of tides, water clarity, salinity, temperature,  
72 and risk of entrainment into water diversions (Sweetnam 1999; Bennett 2005; Kimmerer 2008;  
73 Kimmerer 2008; Nobriga et al. 2008; Feyrer et al. 2011). Nevertheless, more precisely  
74 understanding the spatiotemporal changes (or lack of changes) in abundance within the broader  
75 range limits has been a focal point of conservation discussions (Brown et al. 2009; Feyrer et al.  
76 2011), highlighting the need for statistical analysis at finer spatial and temporal scales than has  
77 been typically carried out.

78

79 Our primary motivation was to gain insight into patterns of the distribution and abundance of  
80 adult delta smelt. Specifically, we addressed three questions: Where do adult delta smelt

81 distribute themselves during their spawning season, and how variable is this distribution across  
82 time (both within and between cohorts)? What factors operating at what scales most strongly  
83 influence the spatial distributions? What are the year-over-year population growth rates?  
84

85 To answer these questions, we constructed spatiotemporal models of catch density with three  
86 different levels of spatiotemporal scale that we label global, regional, and local. Year of the  
87 survey and cohort-specific mortality rates were global-level (i.e. population wide) components to  
88 the model that described overall cohort specific trends in time. Regional (approximately 5 km  
89 and larger) spatial variation is apparent from exploratory data analyses (Fig. 2) of catch per unit  
90 volume (CPUV), the sum of all fish caught at given survey location divided by the sum of all  
91 water sampled at that location, and this spatial variation was modeled using nonparametric  
92 techniques. The importance of both within- and across-cohort changes in the regional spatial  
93 distribution patterns were tested. At the local (individual sample) level, we estimated how much  
94 of the variability in catch density was explained by three environmental covariates: water clarity,  
95 salinity, and tide. Increased turbidity and decreased salinity are expected to have positive effects  
96 on catch density based on *in situ* studies of earlier life stages (Nobriga et al. 2008; Feyrer et al.  
97 2011). Flood relative to ebb tide was expected to increase catch densities as fish position  
98 themselves within the water column and channel to either move upstream or to otherwise  
99 maintain position (Feyrer et al. 2013; Bennett and Burau 2015). We also compared design-based  
100 and model-based estimates of abundance for February of each year (definitions of design-based  
101 and model-based inference are given in the supplementary material [SM] Section 4). Here the  
102 aim was to quantify inter-annual changes and long-term trends, to assess how different

103 abundance estimates would be when standardizing effort for tide and to evaluate whether the two  
104 approaches have any qualitative differences.

105

## 106 **METHODS**

### 107 *Data*

108 The California Department of Fish and Wildlife established the Spring Kodiak Trawl (SKT) in  
109 2002 to collect data on the distribution and reproductive stage of spawning delta smelt. The SKT  
110 survey usually visits 40 locations monthly from January through May (Fig. 1) over a several day  
111 period. During each location visit a 10 minute surface trawl of the approximately top 2m of  
112 water is taken. Three quarters of all trawls were made before noon. All delta smelt retained by  
113 the gear are counted and measured, and the volume of water sampled (*Vol*, m<sup>3</sup>) is estimated. We  
114 used data from 2002-2014. Of the 2396 records used here, 1706 (71%) had zero catch. Of the  
115 690 samples with positive catch, 227 recorded a single adult delta smelt, with a maximum catch  
116 of 375.

117

118 The local tow-specific environmental covariate data included Secchi disk depth (*Sec*, cm), a  
119 proxy for water clarity; specific conductance (*Cond*, microSiemens per centimeter,  $\mu\text{S cm}^{-1}$ ), a  
120 proxy for salinity; and tide stage (*Tide*) which is categorically recorded as ebb (1500  
121 observations), low slack (68 observations), high slack (97 observations), flood (731  
122 observations). Although water temperature is also recorded, for this analysis we did not include it  
123 in the models because the range of observed temperatures (min=6.6°C, max=23.6°C,  
124 mean=12.9°C) were well within the tolerance of spawning and post-spawn adult delta smelt  
125 (Swanson et al. 2000; Komoroske et al. 2014). Earlier versions of the model that did include



126 temperature never identified it as statistically significant. In contrast, measures of salinity up to  
127 21ppt, high enough to constrain distribution and affect survival (Komoroske et al. 2014; Lisa M.  
128 Komoroske et al. 2016), have been recorded in the SKT survey.

129

### 130 *Spatiotemporal catch density models*

131 The catch  $y_{t,c,l}$  on Julian day  $t$  of cohort  $c$  at location  $l$  was modeled using a negative binomial  
132 distribution  $y_{t,c,l} \sim \text{NegBin}(\mu_{t,c,l}, \theta)$  parameterized to have expected value  $\mu$  and variance  $\mu + \mu^2/\theta$   
133 (Venables and Ripley 2002). The negative binomial was selected given evidence for  
134 overdispersion relative to a Poisson distribution and from model residual diagnostics. The  
135 different models for  $\mu_{t,c,l}$  are described next and summarized in Table 1.

136

137 Most generally, the expected catches  $\mu_{t,c,l}$  were modeled using a semi-parametric,  
138 spatiotemporally explicit model within a generalized additive model (GAM) framework (Hastie  
139 and Tibshirani 1986; Wood 2006; Augustin et al. 2013). The expected catch is the product of the  
140 volume of water sampled,  $Vol_{t,c,l}$ , the true density  $\delta_{t,c,l}$  in a spatially local region around  $l$ , and the  
141 catchability  $q_{t,c,l}$ ,

$$142 \quad \mu_{t,c,l} = q_{t,c,l} \delta_{t,c,l} Vol_{t,c,l}. \quad (1)$$

143 Catchability  $q_{t,c,l}$  has recently (Maunder et al. 2014) been conceptualized as a function of  
144 availability (i.e. whether fish are in the tow path in the first place) and contact selectivity (the  
145 probability that the net will catch and retain the fish given availability) (see Arreguín-Sánchez  
146 1996 for other classic definitions). The catchability parameter  $q_{t,c,l}$  is confounded with the overall  
147 density, so it is assumed equal to 1 for all the models. Further discussion of  $q_{t,c,l}$  in the context of  
148 adult delta smelt surveying is provided in the Discussion.

149

150 Modifications to Eqn. (1) were made to study different sources of variability in  $\delta_{i,c,l}$ . The first,  
151 which is labeled global scale effects, and was included in all models and intended to capture  
152 temporal trends in the overall density (total fish over total water volume), was to rewrite Eqn. (1)  
153 as

154 
$$\mu_{t,c,l} = \delta_{0,c} \exp(\beta_c t) Vol_{t,c,l} \quad (2)$$

155 Eqn. (2) describes an exponential decline (assuming  $\beta_c < 0$ ) in density from an overall initial  
156 density  $\delta_{0,c}$ , and the expected catch is simply this density times the volume sampled on a given  
157 tow.

158

159 An extension of the global density model of Eqn. (2) was to add a regional scale factor, namely a  
160 dependency on space to the predictions,

161 
$$\mu_{t,c,l} = \delta_{0,c} \exp(\beta_c t + s_{m,c}) Vol_{t,c,l} \quad (3)$$

162 where  $s_{m,c} = s_{m,c}(UTMX_l, UTM Y_l)$  is a nonparametric spatial smooth. A total of four different  
163 hypotheses about how  $s_{m,c}$  changed through time were considered: (1) it did not change in time,  
164  $s_{m,c} = s$ ; (2) it depended only on the month of the survey,  $s_{m,c} = s_m$ ; (3) it depended only on the  
165 year of the survey,  $s_{m,c} = s_c$ ; and (4) it depended on both the month and the year of the survey.

166 Because the spatial adjustments to the density vary at scales larger than the water surveyed in a  
167 single trawl, these adjustments can be thought of as capturing spatially regional changes in  
168 density.

169

170 The global and regional effects model given by Eqn. (3) was further extended to include local  
171 scale effects. For each assumption about  $s_{m,c}$ , the effects of local environmental conditions on  
172  $\delta_{t,c,l}$  were estimated with the model

$$173 \quad \mu_{t,c,l} = \delta_{0,c} \exp(\beta_{ct} + s_{m,c} + \beta_{Sec} Sec_{t,c,l} + \beta_{Cond} Cond_{t,c,l} + \beta_{Tide(t,c),t,c,l} Tide_{t,c,l}) Vol_{t,c,l}. \quad (4)$$

174 The importance of Secchi and conductivity was also considered in the absence of a regional  
175 spatial adjustment component, i.e. extending Eqn. (2) with these covariates.

176

177 In total fifteen different models were fit and evaluated (Table 1). Model fitting was done in the R  
178 environment (R Core Team 2016) primarily using the `glm.nb` (Venables and Ripley 2002) and  
179 `gam` (Wood 2004; Wood 2011) functions. Other functions and packages used are documented in  
180 the model code provided in the SM. Soap film smoothers (Wood 2008) were used to make  
181 spatial smooths  $s_{m,c}$  follow large-scale habitat boundary features (SM Fig. S1). The boundaries  
182 were set up in particular to avoid an influence of catch between Montezuma Slough and either  
183 Cache Slough or Suisun Bay. Smoothing parameter estimation was done using maximum  
184 likelihood (Wood 2011), but other criteria used for estimating the smooth parameter such as  
185 generalized cross-validation did not qualitatively change the results. Secchi and conductivity  
186 measurements were standardized to their z-scores prior to model fitting. A wide range of smooth  
187 basis dimensions were considered to ensure results were not predicated on this choice, and  
188 standard model residual diagnostics were investigated, including semivariograms (Clark 2007) of  
189 residuals by month and year. Model comparison was done by assessing residual diagnostics,  
190 Akaike's information criterion AIC (Burnham and Anderson 2002), fitted negative log-marginal-  
191 likelihoods (NLML, see Eqn. 5 in Wood 2011).

192

193 Model evaluation of the effects of the locally measured covariates Secchi and conductivity was  
194 partly complicated because of their global spatial structure. On average, more easterly (upstream)  
195 regions of the delta smelt habitat are clearer and less saline (SM Fig. S2), leading to the  
196 possibility that local environmental covariates will be confounded with the spatial terms in the  
197 model. To approximate an upper bound on the most variability that local environmental  
198 conditions might explain in the absence of spatial terms in the model, we computed the  
199 proportion of null deviance explained by models of the form of Eqn. (2) but including each of  
200 these covariates one at a time (Table 1 models 2-4). The proportion of the deviance explained by  
201 each locally measured covariate when fitting the full model in Eqn. (4) (Table 1 models 13-15)  
202 was also calculated by dropping each term individually and refitting the model while fixing the  
203 smoothing parameters at the values estimated in model 9. This helped ensure that no changes in  
204 the smoothing penalty upon refitting resulted in a “mopping up” of variation previously  
205 accounted for by the removed covariate, thereby diminishing the estimated proportion of  
206 deviance explained by the dropped covariate under consideration.

207

#### 208 *Abundance estimation*

209 Total abundance estimates for the month of February for each year were made using both design-  
210 based and model-based approaches (SM Sec. 4). Both approaches rely on volumetric expansions  
211 of density estimates. The volumes were calculated by multiplying the area of water with at least  
212 2 meters depth (provided by the United States Geological Survey) by 2 to compute the volume of  
213 habitat  $V_{tot}$  over which the density estimates might reasonably be extrapolated. This volume  
214 excludes water deeper than 2 meters as well as shoal habitats. Thus our estimates are likely  
215 underestimating the total population size depending on unknown densities in these unsampled

216 water volumes. However, this approach avoids extrapolating catch density information into  
217 habitats that are not sampled by the SKT survey.

218

219 The design-based approach stratified the waterways most commonly occupied by delta smelt into  
220 27 subregions (SM Fig. S3). The subregion, year and month specific catch densities were  
221 expanded by subregion-specific water volumes and summed to obtain year and month-specific  
222 abundance estimates. Assuming the abundance estimates were lognormally distributed, the 2.5  
223 and 97.5 percentiles of this distribution were used to construct design-based prediction intervals.  
224 Section 4.1 of the SM provides details on obtaining the parameters for these cohort specific  
225 distributions.

226

227 In contrast to the design-based approach, the model-based approach does not require spatial  
228 stratification of the habitat and allows predictions to be contingent on specific environmental  
229 conditions thought to affect catchability. Based on model selection results, model 9 was used to  
230 make model-based total abundance estimates as follows. We used 984 points distributed within  
231 the spatial limits of the survey and the areas of water with at least 2 meters depth (SM. Fig S1) as  
232 the spatial locations for predictions. At each one of these locations, the density per 10000m<sup>3</sup> of  
233 water was predicted on February 15<sup>th</sup> (specifying a day is necessary for the Julian day effect) of  
234 each year, the tide set equal to the flood factor level, and the Secchi and conductivity values  
235 fixed at a month, year, and location specific value (described below). These densities were  
236 averaged within each subregion, multiplied by the subregion water volume down to 2m, and  
237 summed to produce overall abundance estimates (see SM Sec. 4.2 for details). Because direct  
238 observations on Secchi depth and conductivity at the point locations used in making predictions

239 were not always available, spatially smoothed GAMs were used to predict both of these variables  
240 during the February survey periods of each year. The GAMs were fit using the available survey  
241 data on Secchi depth and conductivity and had the form  $y_{t,c,l} \sim \text{Normal}(\mu = \beta_{m,c} + s_{m,c}, \sigma)$ , where  
242  $y_{t,c,l}$  was either the z-transformed Secchi depth or conductivity measurements from the SKT  
243 survey. The fits were generally quite good: the models of Secchi depth and conductivity  
244 described at least 88% and 94% of the null deviance for 80% of the months, respectively.  
245 Abundance prediction intervals were estimated using a parametric bootstrapping approach that  
246 included uncertainty in model parameters, covariate predictions, and observations (see SM Sec.  
247 4.2).

248

## 249 **RESULTS**

250 Table 1 shows model summary statistics. There was clear support for including both a regional  
251 spatial adjustment and local environmental conditions in the expected catch models. The best  
252 model identified by AIC included a separate spatial distribution for each month (model 10),  
253 while the negative log-marginal-likelihood identified a model with a constant spatial smooth  
254 over time as the best (model 9). Residual diagnostics for models without a regional smooth  
255 adjustment term were poor as measured by distributional checks of residuals. In contrast, models  
256 including a regional spatial term had residual qq-plots and semivariograms that suggested no  
257 systematic bias in predictions due to the spatial variability in the distribution. Simpler models  
258 had higher dispersion parameters, reflecting larger prediction error when the mean structure was  
259 less flexible.

260

261 Models including a smooth term to capture regional variation in catch identified several density  
262 hotspots (Figs. 3 and S4; see also Fig. 2 for empirical densities): the waterways surrounding  
263 Grizzly Island, channels at the confluence of the Sacramento and San Joaquin rivers, the Cache  
264 Slough complex, and the Sacramento deep water shipping channel. These density hotspots were  
265 fairly consistent between cohorts, with the Cache Slough complex and Sacramento deep water  
266 shipping channel the most persistently high. We focused on model 9 for making predictions  
267 because the differences in month-specific predictions in model 10 are dominated by  
268 disappearance of density hotspots in April and May (likely reflecting post-spawning mortality)  
269 rather than a spatial shift in the locations of hotspots (SM Fig. S4).

270

271 The local environmental covariates tide and conductivity explained very little (<2%) of the null  
272 deviance beyond that of model 1, but Secchi depth explained an additional 21.3% of the null  
273 deviance when no regional spatial adjustment was made (Table 1, models 2-4 and 13-15). The  
274 effect size on the linear scale of Secchi was approximately double that of conductivity, but both  
275 local covariates could translate into substantially larger expected changes in density predictions  
276 over the range of observed turbidity and salinity indices (Table 2). Catch density was higher on  
277 flood and low slack tide levels in comparison with ebb tide (the increase on low slack tide was  
278 the highest, but surveys during this tide stage account for <3% of samples), and not significantly  
279 different for high slack tide conditions (Table 2).

280

281 Figure 4 shows the total abundance estimates and prediction uncertainty for February 15<sup>th</sup> of  
282 each year (see SM Table S1 for values) for the design- and model-based estimates. The  
283 geometric mean annual growth rate over the 13 years was 0.88 and 0.87 for the design- and

284 model-based approaches, respectively, and the percentage decline from 2002 to 2014 was 82%  
285 and 79% for the design- and model-based approaches, respectively. Note that the results about  
286 declines do not depend on the tide factor level choice used in making total abundance estimates.  
287 Despite the general agreement between design- and model-based estimates of trend, the two  
288 approaches showed the same annual growth rate in only 6 of the 13 years, and differed in  
289 magnitude especially in 2003 and 2012 (Fig. 4 and SM Table 1). The differences in abundance  
290 magnitude did depend on the model chosen, with the most complicated model showing  
291 predictions very similar to the design-based approach (SM Fig. S5).

292

## 293 **DISCUSSION**

294 For small, elusive, and rare pelagic fish species such as delta smelt, often the only source of  
295 information from the wild is catch density from trawls or other types of nets (e.g., beach seining),  
296 along with additional measurements of local environmental conditions. Given such data, at a  
297 minimum we would like to quantify the variability in distribution and abundance. Ideally, we  
298 could go further to identify causal factors that explain the variability at different scales, or rule  
299 out those that do not, and to assess the extent to which findings from theoretical and laboratory  
300 work are identifiable in the wild.

301

302 The spatial distributions quantified here are similar to the descriptive reports by Merz et al.  
303 (2011) and Murphy and Hamilton (2013) in their general depiction. By constructing statistical  
304 models, we were able to test hypotheses about the variability of this spatial structure. At a  
305 regional scale, our models indicated that the distribution of adult delta smelt was fairly consistent  
306 across months and years, with the dominant within-year change being disappearance of hotspots



307 likely due to post-spawn mortality as the spawning season progresses for this annual species.  
308 This suggests that the majority of regional movement from juvenile and sub-adult rearing  
309 locations to spawning areas has already happened by the time the SKT survey is conducted, that  
310 spawning habitat locations are relatively constant within and between years, and that no  
311 substantial further restructuring of the population at regional scales occurs afterwards.

312

313 What leads to the emergence of density hotspots remains to be determined. A recent pairing of  
314 the sub-adult delta smelt catch data used by Feyrer et al. (2011) with a three-dimensional  
315 hydrodynamic model suggests that density hotspots may reflect the interplay of local water  
316 quality conditions with tidal velocity differences that exist between shoals and deeper shipping  
317 channels (Bever et al. 2016). Other possible explanations for adult and spawning delta smelt  
318 spatial variation include distributions of prey or spawning habitats, or areas more suited for  
319 survival during spawning. Why no density hotspots emerge and persist upstream of the Jersey  
320 Point (located near the arrow tip showing the San Joaquin River in Fig. 1) area remains to be  
321 determined, but likely factors include inhospitable habitat and advection of fish into water export  
322 facilities (Kimmerer 2008; Kimmerer 2011).

323

324 At local spatial scales there continues to be high variability in the spatial distribution (which  
325 necessitated the use of a negative binomial catch distribution model), some of which is likely  
326 related to spawning-related aggregations of delta smelt and some of which is related to changes  
327 in local salinity (movement away from) and turbidity (movement towards) conditions. Our view  
328 is that the best interpretation of the categorical covariate tide is that it affects changes in fish  
329 availability to the gear, a component of catchability  $q_{t,c,l}$ , with the direction of the effects found

330 here being consistent with Feyrer et al. (2013). In general it appears that, due to its relatively  
331 coarse spatial and temporal resolution, the SKT survey cannot distinguish between very local,  
332 site level movement, up to movement between adjacent locations, and changes in catchability  
333 related to local environmental conditions. The infrequent yet extremely large catches point to  
334 highly localized and ephemeral aggregations of fish but, similar to questions about the existence  
335 of regional density hotspots, the relative contributions of social cues vs. habitat cues vs.  
336 hydrodynamics leading to the formation of these aggregations remains to be determined.

337

338 Previous analyses of the sub-adult life-stage have found local environmental covariates to be  
339 statistically significant predictors of delta smelt distribution, with Feyrer et al. (2011) remarking  
340 that “specific conductance and Secchi depth accounted for a meaningful reduction of null  
341 deviance.” In contrast, we found that these covariates explained very little of the variation in  
342 adult catch when a regional spatial adjustment to density was included. The comparatively large  
343 amount of deviance explained by Secchi depth when no spatial smooths were included in the  
344 model (model 2) suggests that water clarity has some influence on both local and regional  
345 distributions, although from a statistical perspective any models not containing a spatial  
346 adjustment beyond what is made by the local environmental covariates were very inferior. While  
347 suitable local environmental conditions are necessary to explain the distribution and abundance  
348 of delta smelt, they are far from sufficient. We suggest that to better understand both the regional  
349 and local changes in densities, an understanding of the characteristics leading to ideal spawning  
350 habitat features is needed, along with assessments of the variability of these characteristics in  
351 space and time.

352

353 At the decadal time scale delta smelt are currently in a severe state of population decline, with  
354 suspected causes including removal of water from the system and alien species (Moyle et al.  
355 2016). Here we used the best available survey data to quantify this decline more precisely.  
356 Design- and model-based approaches closely agreed in the rate and amount of overall decline  
357 from 2003 to 2014.

358

359 Despite the general agreement in long-term trends between the two approaches for abundance  
360 estimation, there were also differences. In 2003 the design-based estimates showed a decline in  
361 abundance compared to 2002, while model-based estimates showed an increase. During this year  
362 the frequency of sampling on the flood tide was only 8%, and this may have led to the qualitative  
363 mismatch in year-over-year abundance change between the design- and model-based methods. It  
364 seems likely that the design-based approach is negatively biased when compared with the model-  
365 based approaches due to the failure to account for the effect of tide cycle on catchability  $q_{t,c,l}$ .

366 Another difference was in prediction intervals, with model-based ones being notably wider likely  
367 related to the more complete inclusion of the different sources of uncertainty in the model-based  
368 approach which is accounting for spatial and tow-specific sources of uncertainty. Finally, the  
369 magnitude of the estimates also differed, with model-based estimates generally being  
370 substantially higher, although models with more complicated smooths had estimates that  
371 increasingly approached the design-based ones (SM Fig. S5). This closer agreement of the  
372 models with the most complicated smooths and the design-based approach is likely due in part to  
373 overfitting, whereby the expected model predictions are able to more closely track zero catch  
374 data. Other surveys making multiple tows per site visit have found that although the frequency of  
375 zero catch was similarly high on any given tow, nonzero catch usually occurred at least once

376 (Polansky et al. 2014). Thus, we suspect that the models with simpler spatial smooth terms are  
377 more reflective of actual distributions because they are drawing on information across time, and  
378 hence less informed by zero catch when in fact fish may be locally in the area. Whether using  
379 design- or model-based approaches to construct abundance estimates, information about false  
380 zero catches as well as abundances in shoal habitats as well as the vertical density gradients in  
381 channel and open-water habitats are needed to reduce abundance estimate bias and uncertainty.

382

383 Pinpointing the relative contributions of anthropogenic vs. natural sources to the population  
384 decline will continue to be challenging, and will likely best be done in a complete life-cycle  
385 analysis framework that integrates survey data from all life stages. Absolute abundance estimates  
386 will first be needed from each source in order to integrate information from different life stages,  
387 and catch level models such as applied here can help achieve this. The importance of tide, found  
388 here and elsewhere (Bennett et al. 2002; Feyrer et al. 2013; Bennett and Bureau 2015),  
389 emphasizes a need to consider accounting for this covariate analyses where organism detection  
390 might be driven by tidal conditions (see also Arreguín-Sánchez 1996) to control for its effect on  
391 catch density. None of the previous population dynamics models using annual abundance indices  
392 (Mac Nally et al. 2010; Thomson et al. 2010; Maunder and Deriso 2011) attempted to  
393 standardize catch data when making these indices, which could mean that abundance and  
394 covariate relationships have not been described accurately.

395

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399 the authors and do not necessarily reflect the opinions of the U.S. Department of the Interior or  
400 the U.S. Fish and Wildlife Service.

401

## 402 **Supplementary Material**

403 Supplementary material with additional details, figures and code is provided. Data and code are  
404 available from the U.S. Fish and Wildlife Service.

405

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521 **Tables**

522 Table 1- Overview of catch models showing the (effective) degrees of freedom (df), information theoretic measures of model  
 523 goodness of fit (AIC and  $\Delta$ AIC), the negative log-marginal-likelihood (NLML- smaller values are better), and percent of the null  
 524 deviance explained (% dev. expl.). Global is defined by Eqn. (2) and Global + regional is defined by Eqn. (3), while local terms are  
 525 Secchi (Sec), conductivity (Cond), and Tide- see Eqn. (4). Regional spatial smooth terms were either constant across months and years  
 526 (single), different by month but not year (monthly), different by year but not month (yearly), or different for each month and year.  
 527 Models 13-15 had fixed smooth term parameters using the estimates from model 9 and were used for estimating the % dev. expl. by  
 528 each of the three individual local terms in model 9.

Model	Density model	df	AIC	$\Delta$ AIC	NLML	% dev. expl.	$\theta$
1	Global	27	6717.2	1178.2	-	12.9	0.1
2	Global + Sec	28	6337.8	798.9	-	34.2	0.2
3	Global + Cond	28	6692.8	1153.8	-	14.5	0.1
4	Global + Tide	30	6701.4	1162.5	-	14.2	0.1
5	Global + regional (single)	49.9	5643.0	104.0	2821.8	63.6	0.4
6	Global + regional (monthly)	118.1	5638.3	99.3	2853.3	67.4	0.4
7	Global + regional (yearly)	199.0	5603.3	64.4	2831.6	72.2	0.5
8	Global + regional (month and year)	632.5	5888.7	349.7	2933.1	83.8	0.8
9	Global + regional (single) + Sec + Cond + Tide	54.7	5548.2	9.3	2769.2	66.9	0.4
10	Global + regional (monthly) + Sec + Cond + Tide	128.1	5538.9	0.0	2789.3	70.6	0.5
11	Global + regional (yearly) + Sec + Cond + Tide	198.6	5572.3	33.4	2798.6	72.9	0.5
12	Global + regional (month and year) + Sec + Cond + Tide	506.3	5726.6	187.7	2819.6	82.4	0.7
13	Global + regional (single, fixed) + Cond + Tide	52.7	5606.3	67.4	2801.1	65.0	0.4
14	Global + regional (single, fixed) + Sec + Tide	52.7	5566.9	28.0	2780.2	66.1	0.4
15	Global + regional (single, fixed) + Sec + Cond	50.7	5557.9	18.9	2778.0	66.4	0.4

529 Table 2- Parameter estimates and bootstrapped estimates of uncertainty for the parameters  
 530 associated with the local environmental covariates for model 9 (see Table 1) on the  $\log_e$  scale.  
 531 Lower and upper columns show the 2.5 and 97.5 percentiles from 1000 samples from a  
 532 multivariate normal distribution parameterized by the mean and covariance matrix from the fitted  
 533 model 9. The final columns show density prediction differences on the response scale given the  
 534 described local environmental change, where the changes are based on changing from the 2.5 to  
 535 the 97.5 percentile for the continuous covariate observations, and in comparison with an ebb tide.

Covariate	Estimate	Lower	Upper	Density factor change on response scale	
Secchi depth	-0.880	-1.112	-0.670	Decrease in turbidity	0.415
Conductivity	-0.403	-0.583	-0.232	Increase in salinity	0.669
Flood	0.338	0.113	0.552	From ebb to flood	1.398
High slack	-0.093	-0.658	0.476	From ebb to high slack	0.910
Low slack	0.962	0.389	1.571	From ebb to low slack	2.622

536

537 **Figures**

538 Figure 1- Overview of the inland portion of the San Francisco Estuary where adult delta smelt  
539 are most commonly found. Black x's denote the regular monthly Spring Kodiak Trawl survey  
540 locations.

541

542 Figure 2- Mean catch per unit volume at each sampling location for each month (averaged over  
543 2002-2014). Units are per 10000m<sup>3</sup> of water.

544

545 Figure 3- Density predictions at a flood tide per 10000m<sup>3</sup> of water based on model 9 on February  
546 15<sup>th</sup> 2004 using the mean Secchi and conductivity values. By fixing the local covariates the  
547 figure emphasizes density variation due to intrinsic variability. For clarity catch densities above  
548 10 fish/10000m<sup>3</sup> of water are colored the same. See SM Fig. S4 for month specific predictions  
549 using model 10.

550

551 Figure 4- Abundance estimates on February 15<sup>th</sup> of each year. Design-based abundance estimates  
552 are shown by the line with filled circles with vertical lines extending to the 2.5 and 97.5  
553 percentiles of the lognormal distributions. Model-based predictions from model 9 are shown as a  
554 solid line with dashed lines drawn at the 2.5 and 97.5 prediction percentiles based on 1000  
555 bootstrapped samples. Inset numbers show the percentage of samples in each February that were  
556 done on a flood tide to illustrate the variability in sample conditions, which the model-based  
557 estimates account for. See SM Fig. S5 predictions using models 8 and 12.

Figure 1

Figure 1

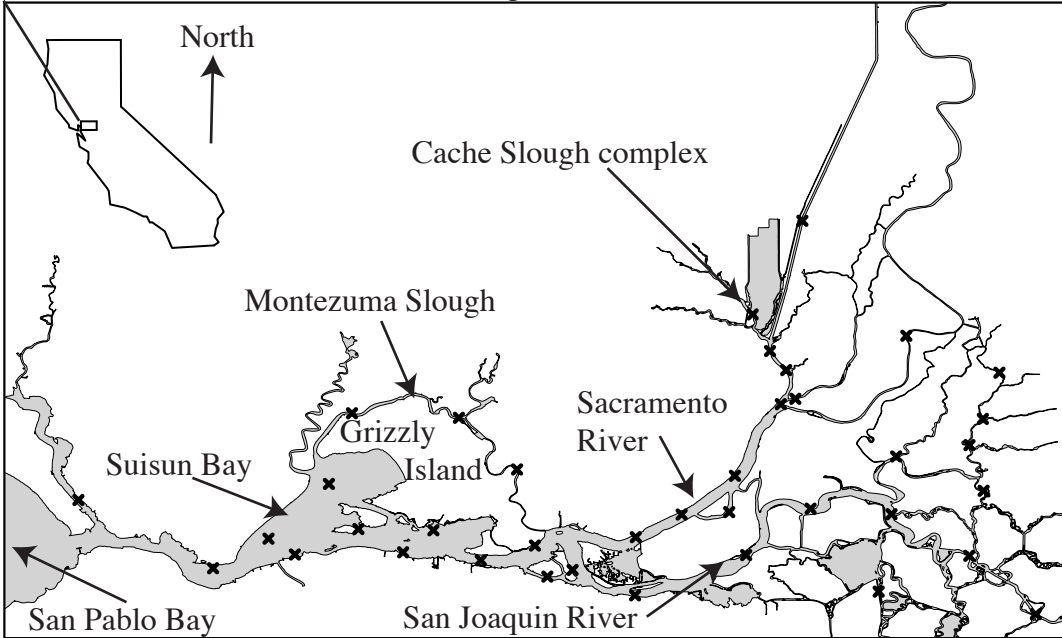


Figure 2

Figure 2

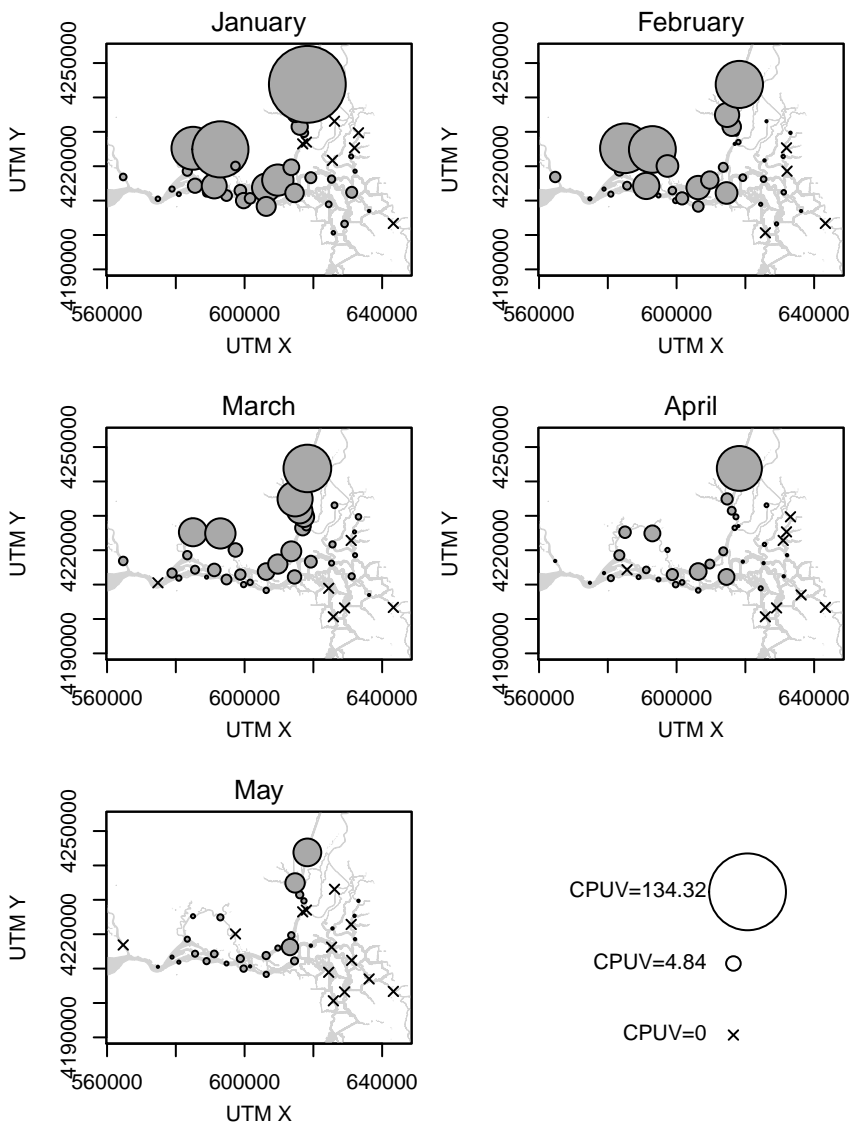


Figure 3

Figure 3

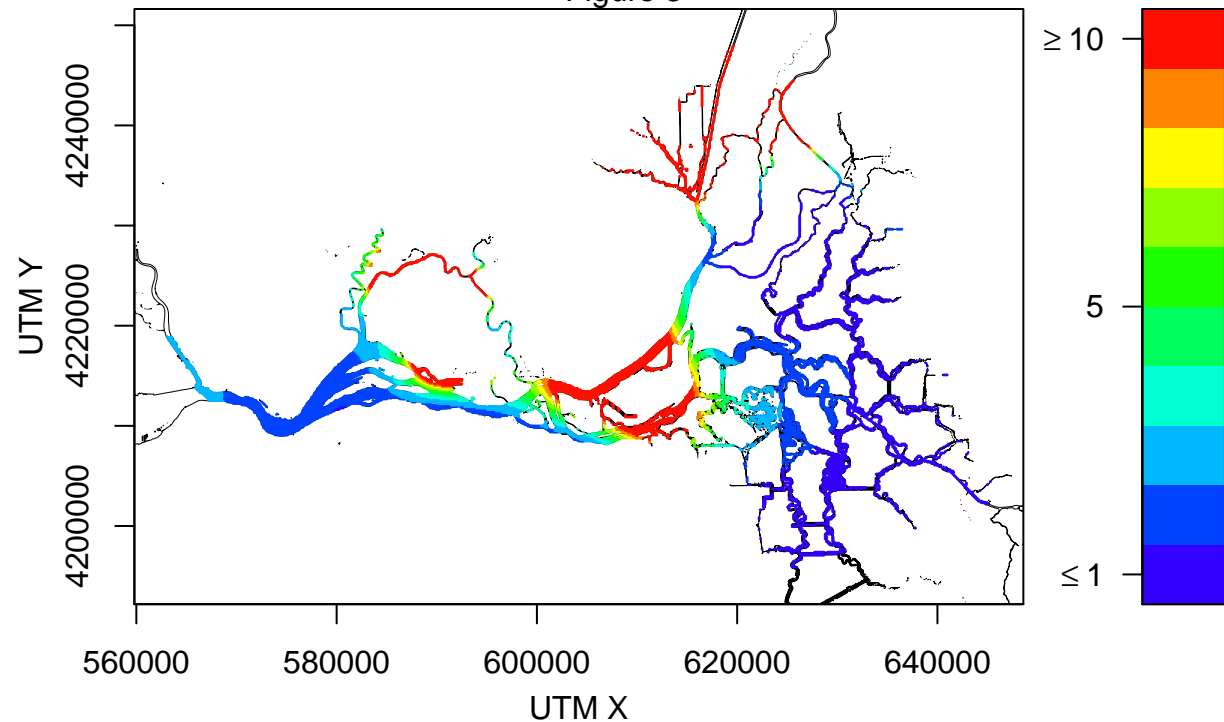
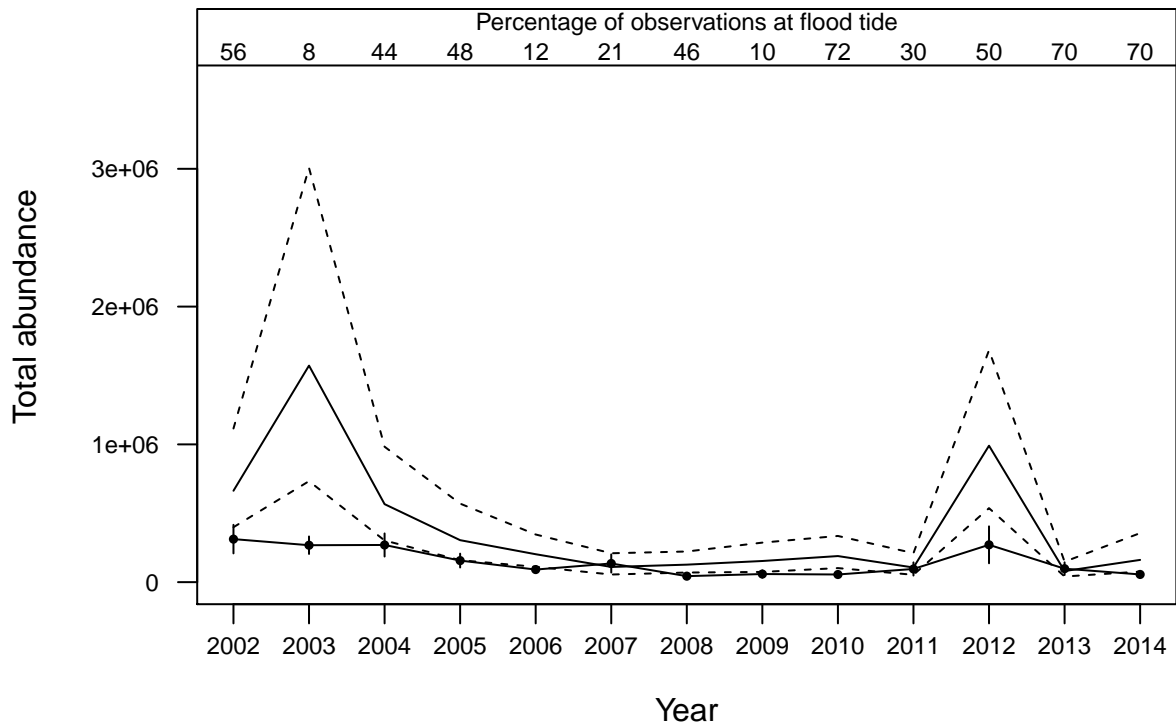




Figure 4

Figure 4



1 **Spatiotemporal models of an estuarine fish species to identify patterns and**  
2 **factors impacting their distribution and abundance**

3 Leo Polansky, Ken B. Newman, Matthew L. Nobriga, Lara Mitchell

4 Supplementary Material

5 **1 Survey locations, knots for smoothing basis, boundaries, and density pre-**  
6 **dition locations**

Figure S1: Model smooth boundaries, knot locations, and prediction locations used in the analysis.

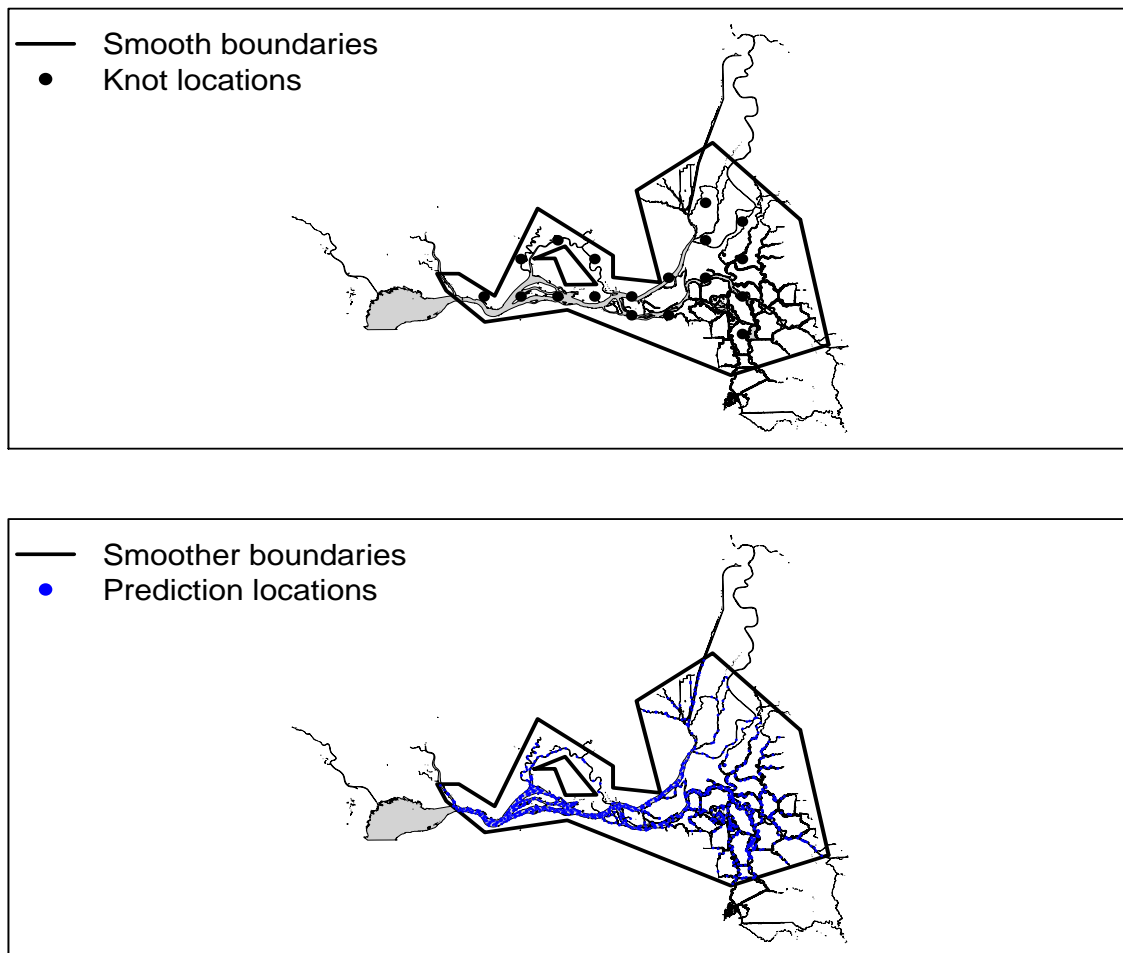
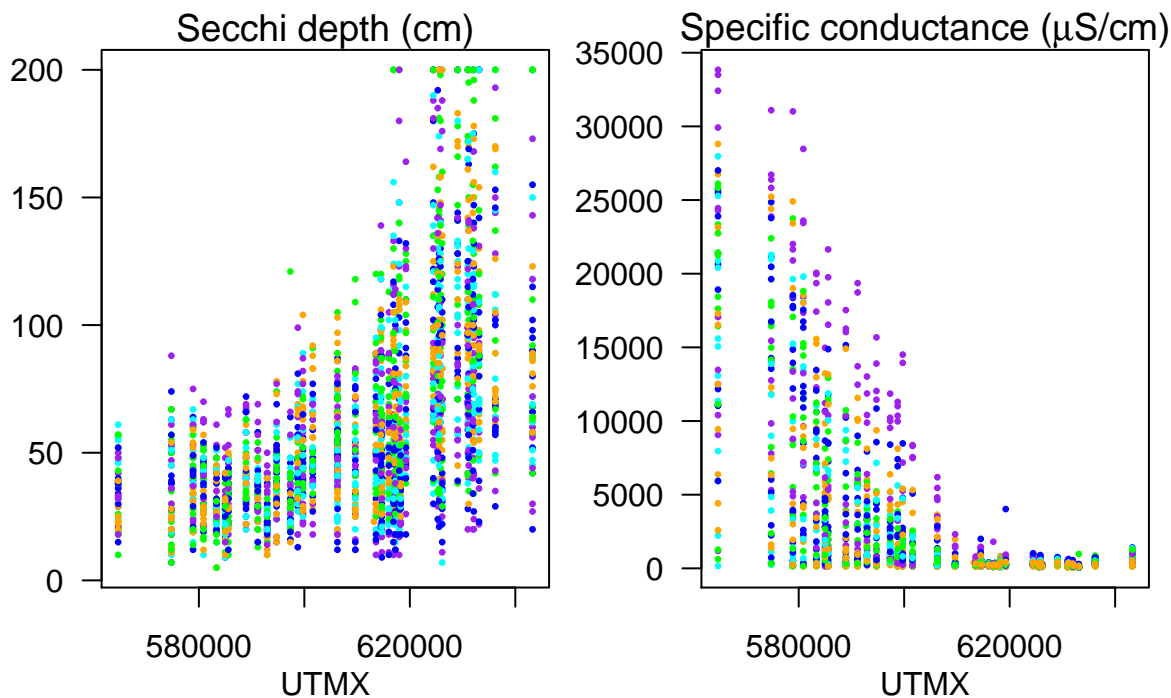


Figure S2: Tow specific values of Secchi and electrical conductance vs. UTMX. Points are colored by the month during which they were recorded: purple-January; blue-February; cyan-March; April-green; May-orange.



## 7 2 Locally measured covariates

8 A visual display of how turbidity and salinity vary in the UTMX direction, which corre-  
9 sponds approximately to an up and down estuary change, is shown in Figure S2.

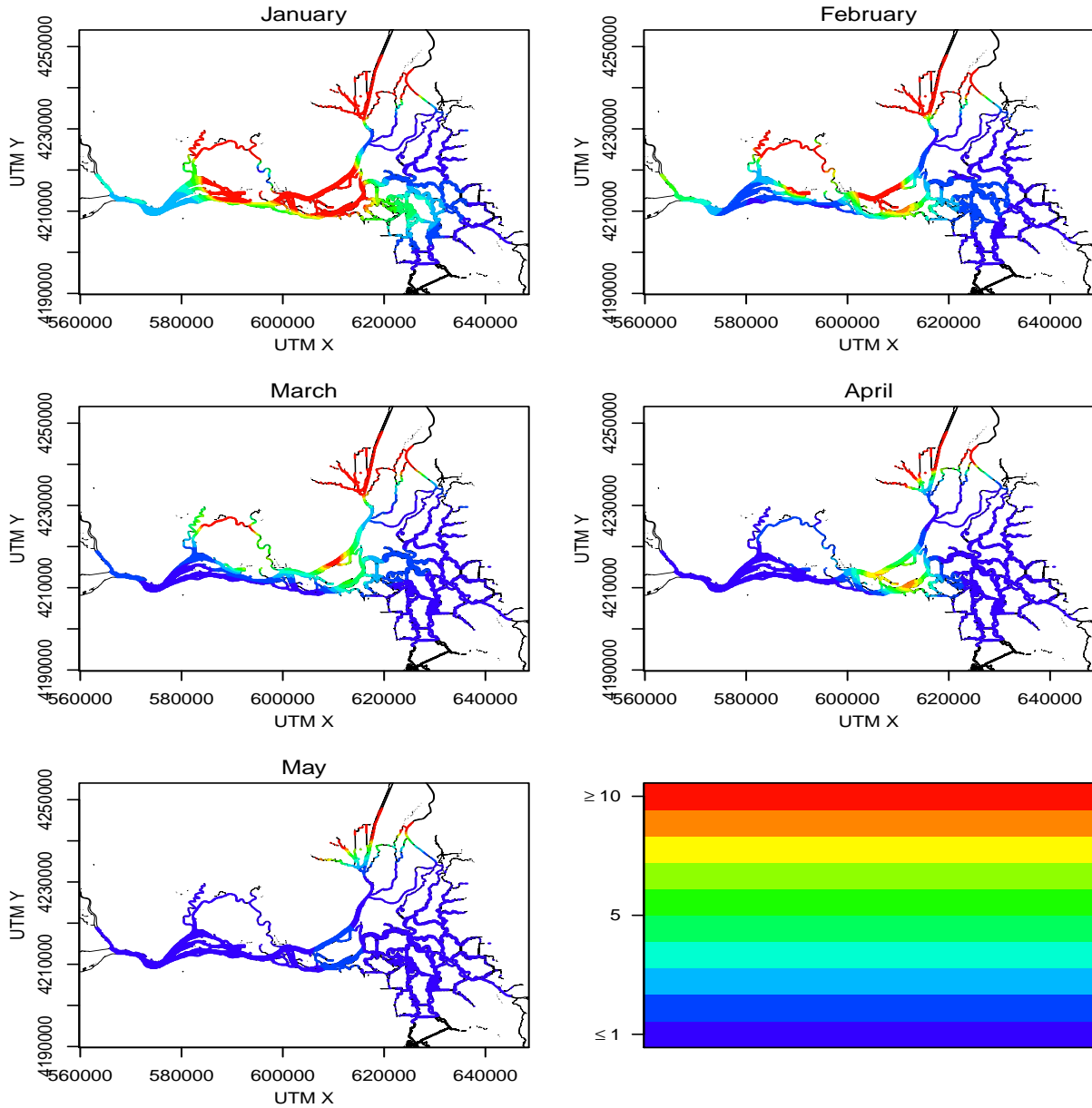
## 10 3 Intra-cohort distribution changes

11 Figure S3 shows density predictions using model 10 of the main text, which has a different  
12 spatial smooth for each month.

## 13 4 Total abundance estimates

14 Two distinctly different perspectives in sampling theory on making inferences from sam-  
15 ples to populations are design-based inference and model-based inference (Thompson  
16 2002). Design-based inference views the values on sampling units as fixed, non-random  
17 quantities, and the only randomness present is that induced by the sample selection pro-

Figure S3: Month specific density predictions based on model 10 (Table 1 of the main text) at a flood tide per 10000m<sup>3</sup> using the mean Secchi and conductivity values; compare with figure 3 of the main text. Turbidity and salinity at each prediction point are set at their mean value, the Julian day is 15, 45, 74, 105, and 135 for the months of January, February, March, April, and May, respectively. As such these density maps emphasize the changes in density due to spatial and temporal changes. Color value map is shown in figure 3 of the main text.



18 cess. For example, assume in a body of water there are  $N$  cubic meter water volumes  
 19 “plots”, with plot  $i$  having  $y_i$  individual fish,  $i = 1, \dots, N$ , and the inference objective is  
 20 to estimate total population,  $\tau_y = \sum_{i=1}^N y_i$ . A simple random sample of size  $n < N$  is  
 21 drawn without replacement and  $\tau_y$  is estimated by multiplying the sample average of  $y$  by  
 22  $N$ . The total population estimate is thus a random variable where the randomness arises  
 23 solely from the random selection process.

24 In contrast, model-based inference views the values on sample units as realizations from  
 25 some underlying random natural process. When the sample units are partitions of a spatial  
 26 domain the random process often induces spatial correlation in the attributes defined on  
 27 the units, e.g., adjacent plots are more likely to have similar values than more spatially  
 28 separated plots. Inference is directed at estimating parameters that characterize the  
 29 underlying random natural process, e.g., a mean value ( $\mu$ ), variance ( $\sigma^2$ ), and covariance  
 30 between plots  $i$  and  $j$  ( $\sigma_{i,j}$ ). Realized population characteristics, e.g.,  $\tau_y$ , can still be  
 31 estimated using estimates of the parameters of the random process, e.g.  $\hat{\tau} = N\hat{\mu}$ .

32 We note that strictly speaking, from a model-based inference perspective, the sample  
 33 units do not need to be randomly selected for inference. However, it is our view that such  
 34 additional human-induced randomization is advisable as it allows for comparison between  
 35 model-based and design-based inference, and assessment of the sensitivity of assumptions  
 36 made about the random process.

#### 37 4.1 Design-based total abundance estimates

Design-based estimates of total monthly abundance  $N_{tot}$  (indices for month and year are suppressed for clarity) were calculated with historical SKT data by dividing the delta into 27 subregions (see Fig. S5) and carrying out volume expansions of average delta smelt catch densities at the subregion level. The average density in each subregion was calculated as the total catch divided by the total water volume sampled

$$\hat{\delta}_h = \frac{\sum_{j=1}^{m_h} Catch_{h,j}}{\sum_{j=1}^{m_h} Vol_{h,j}}$$

is the average density calculated over the  $m_h$  sampling locations in the subregion,  $Catch_{h,j}$  is the catch in a single tow  $j$  in subregion  $h$ , and  $Vol_{h,j}$  is the associated tow volume. The total abundance was calculated by expanding the subregion specific catch densities by the water volume in areas at least 2 meters deep down to 2 meters depth in subregion  $h$ ,  $Vol_h$ , and then summing across all subregions the subregion specific totals  $\hat{N}_h$ ,

$$\hat{N}_{tot} = \sum_{h=1}^{27} \hat{N}_h = \sum_{h=1}^{27} \hat{\delta}_h Vol_h$$

38 In some months not all 27 subregions were sampled by the SKT. In cases where subregion  
 39 density estimates were missing due to lack of sampling, an estimate from a neighboring  
 40 subregion was used for imputation.

For a given year, variance estimates for the total abundances are given by

$$Var(\hat{N}_{tot}) = \sum_{h=1}^{h=29} \left( \frac{Vol_h^2 s_h^2}{\left(\frac{1}{m_h} \sum_{j=1}^{n_h} Vol_{h,j}\right)^2 m_h} \right)$$

where

$$s_h^2 = \frac{\sum_{j=1}^{m_h} (Catch_{h,j} - \hat{\delta}_h Vol_{h,j})^2}{m_h - 1}$$

41 is the variance contribution from each subregion. Some values of  $s_h^2$  were missing because  
 42 no sampling was done in a subregion or because a single site was sampled (in which case  
 43  $m_h = 1$ ). In these cases, the median value of  $s_h^2$ , calculated over all available values, was  
 44 used in place of missing values.

Suppressing time specific indices, confidence intervals were calculated for these abundance estimates by assuming the abundances  $\hat{N}_{tot}$  were log-normally distributed. For a sample point estimate  $\hat{N}_{tot}$  and variance of  $Var(\hat{N}_{tot})$ , an estimate of the coefficient of variation is

$$CV = \frac{\sqrt{Var(\hat{N}_{tot})}}{\hat{N}_{tot}}$$

the location and scale parameters are

$$\mu = \log_e \left( \frac{\hat{N}_{tot}}{\sqrt{1 + CV^2}} \right)$$

and

$$\sigma = \sqrt{\log_e(1 + CV^2)}$$

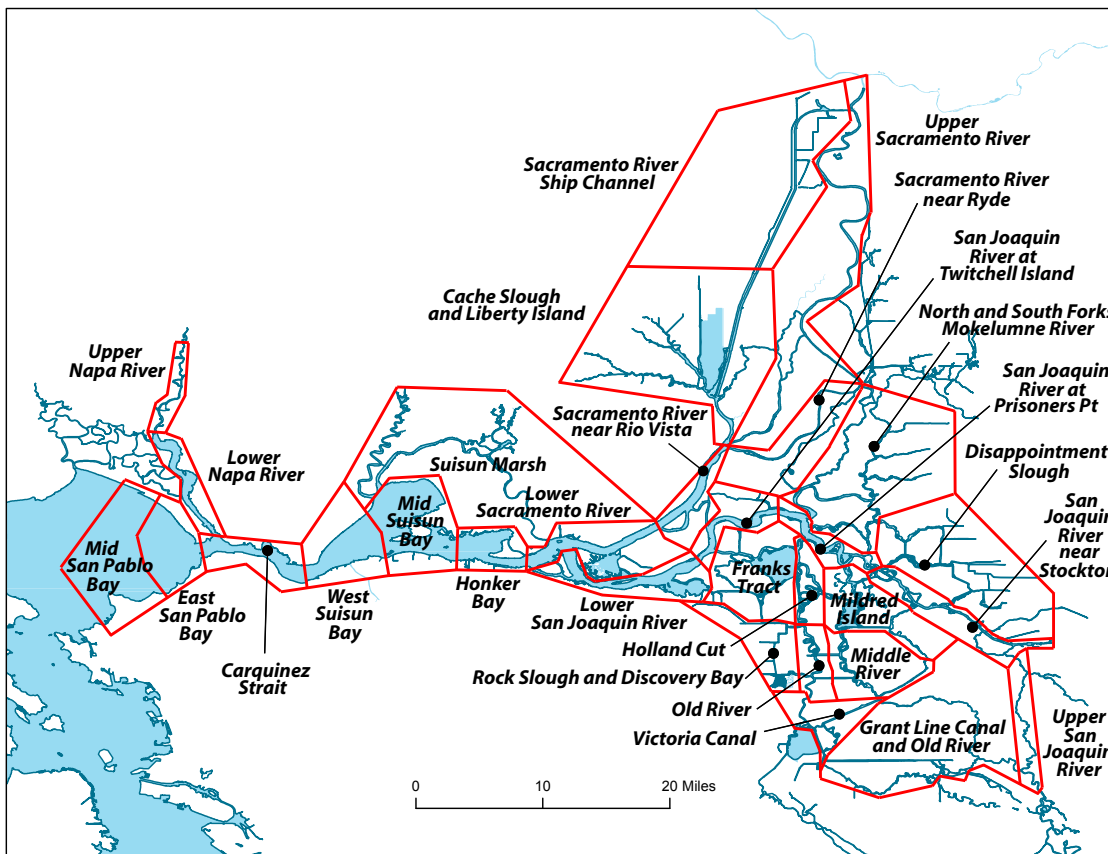
45 respectively. The natural log transformed abundance  $z = \log_e(\hat{N}_{tot})$  is normally dis-  
 46 tributed with mean  $\mu - \sigma^2/2$  and variance  $\sigma^2$ , where the mean is bias corrected so that  
 47 the expected value of  $\exp(z)$  is  $\hat{N}_{tot}$ . The 2.5 and 97.5 percentiles of  $z$  were exponentiated  
 48 to estimate a 95% confidence interval for  $\hat{N}_{tot}$ .

## 49 4.2 Model-based total abundance estimates

Similar to the design-based approach using subregion specific average catch densities as the starting point for constructing a total abundance estimate, the model-based approach uses a model averaged density estimate per subregion to expand by subregion specific water volumes en route to obtaining a total abundance estimate. The month and year indices are suppressed for clarity. Denote the parameter vector of coefficients (including the coefficients for the smooth terms) from the fitted model by

$$\hat{\beta} = [\hat{\beta}_0, \dots, \hat{\beta}_n]^\top$$

Figure S4: Spatial stratification of the Delta used for subregion based density expansions in the design-based estimates of abundance. The Mid and East San Pablo Bay subregions, along with Franks Tract, were excluded in total abundance calculations because these areas are not surveyed by the SKT.



and denote by  $\mathbf{X}_i$  the design vector of values at location  $i$  from one of the locations shown in Fig S1. The model estimated abundance on the log scale at location  $i$  is

$$\hat{Y}_i = \mathbf{X}_i \hat{\boldsymbol{\beta}} + \log_e (Vol_p)$$

where  $Vol_p$  is the prediction volume. The estimated number of fish  $\hat{y}_i$  (per  $Vol_p \text{m}^3$  of water) at location  $i$  on the response scale is

$$\hat{y}_i = \exp(\hat{Y}_i)$$

The mean density in subregion  $h$  is

$$\hat{\delta}_h = \frac{\sum_{k=1}^{K_h} \hat{y}_i}{K_h Vol_p}$$

where the sum is over the  $K_h$  locations in subregion  $h$ . The estimate of the total abundance in subregion  $h$  is

$$\hat{N}_h = \hat{\delta}_h Vol_h$$

where  $Vol_h$  is the total water volume in areas at least 2 meters deep down to 2 meters depth in subregion  $h$ . Again the total abundance estimate is simply the sum of these subregion level estimates over all subregions

$$\hat{N}_{tot} = \sum_{h=1}^{27} \hat{N}_h$$

50 Prediction intervals for total abundance were obtained by parametric bootstrap and  
 51 posterior simulation of GAM model coefficients, conditional on the smoothing parameter  
 52 (Sections 4.8 and 5.4.2 in Wood (2006) and the scale parameters (the  $\hat{\theta}$  from the catch  
 53 model GAM and the  $\hat{\sigma}$ 's from the Secchi and conductivity GAMs). (Obtaining posterior  
 54 distributions unconditional on the smoothing parameter, as outlined in Section 4.9.3 in  
 55 Wood (2006) which involves wrapping the entire steps described next into a simulation-  
 56 refitting process was not possible due to computational time.) Because estimates of total  
 57 abundance are based on predicted values of Secchi depth and conductivity at each point  
 58 location  $i$ , the first step is to simulate predictions of these covariate values at each location,  
 59 and then, given these values, simulate location specific observations from the catch model.  
 60 For  $b = 1, \dots, B$ , compute a bootstrapped predicted total abundance  $N_{tot}^{(b)}$  by adding up  
 61 the predicted catches  $y_k^{(b)}$  at each location  $k = 1, \dots, K$  as follows

62 1. Prediction of covariate values. The fitted covariate models for Secchi and conduc-  
 63 tivity are of the form  $z_k \sim N(\hat{\mu}_k, \hat{\sigma}^2)$ , where  $\hat{\mu}_k = \mathbf{W}_k \hat{\boldsymbol{\beta}}$ .  $\mathbf{W}_k$  is a  $1 \times J$  row vector of  
 64 the design matrix with values corresponding to the intercept and soap film smooth  
 65 basis of the latitude and longitude dimensions at location  $k$ ,  $\hat{\boldsymbol{\beta}}$  is a  $J \times 1$  column  
 66 vector of the estimated GAM parameter vector with  $J \times J$  covariance matrix  $\Sigma_{\hat{\boldsymbol{\beta}}}$ ,  
 67 and  $\hat{\sigma}^2$  is the estimated observation variance. For each covariate, obtain a  $K \times 1$   
 68 column vector  $\mathbf{z}_b$  of values as follows:

- 69 (a) Simulate a  $\boldsymbol{\beta}^{(b)} \sim N(\hat{\boldsymbol{\beta}}, \Sigma_{\hat{\boldsymbol{\beta}}})$ .  
 70 (b) Set  $\mu_k^{(b)} = \mathbf{W}_k \boldsymbol{\beta}^{(b)}$   
 71 (c) For  $k = 1, \dots, K$ , simulate  $z_k^{(b)} \sim N(\mu_k^{(b)}, \hat{\sigma}^2)$ .

72 2. Construct the simulated covariate based design matrix  $\mathbf{X}^{(b)}$  using the  $\mathbf{z}^{(b)}$  values  
 73 from step 1 for the Secchi and conductivity columns.

3. Prediction of catch given covariates. The catch model is of the form  $y_k \sim NB(\hat{\lambda}_k, \hat{\theta})$ ,  
 where  $\log_e(\hat{\lambda}_k) = \mathbf{X}_k \hat{\boldsymbol{\beta}} + \log_e(\text{Volume})$ ,  $Vol_p$  is the volume sampled,  $\hat{\theta}$  is the  
 estimated dispersion parameter of the negative binomial distribution,  $\mathbf{X}_k$  is the  
 design matrix,  $\hat{\boldsymbol{\beta}}$  is the estimated model parameter vector and  $\Sigma_{\hat{\boldsymbol{\beta}}}$  is its covari-  
 ance matrix. Given  $\mathbf{X}^{(b)}$ ,  $\log_e(\lambda_k, b)$  depends only on the value of a realization of  
 $\boldsymbol{\beta}^{(b)} \sim N(\hat{\boldsymbol{\beta}}, \Sigma_{\hat{\boldsymbol{\beta}}})$ . Viewed this way,  $\log_e(\lambda_k^{(b)})$  are iid normal random variables with  
 mean  $\mathbf{X}_k \hat{\boldsymbol{\beta}} + \log_e(\text{Volume})$  and variance

$$\tau_{\mu_k^{(b)}}^2 = \sum_{j=1}^J (x_{k,j}^{(b)})^2 \text{Var}(\hat{\beta}_j) + \sum_{1 \leq j < l \leq J} 2x_{k,j}^{(b)} x_{k,l}^{(b)} \text{Cov}(\hat{\beta}_j, \hat{\beta}_l)$$



74 where  $x_{k,j}^{(b)} = \mathbf{X}_{k,j}^{(b)}$ . To simulate catch values per  $Vol_p$  of water,

75 (a) Simulate  $\boldsymbol{\beta}^{(b)} \sim N(\hat{\boldsymbol{\beta}}, \Sigma_{\hat{\boldsymbol{\beta}}})$  and set  $\mu_k^{(b)} = \mathbf{X}_k^{(b)} \boldsymbol{\beta}^{(b)} + \log_e(Vol_p)$ .

76 (b) Compute the bias adjusted value  $\mu_k^{(b,adj)} = \exp(\log_e(\mu_k^{(b)}) - \tau_{\mu_k^{(b)}}^2/2)$ ,

77 (c) For  $k = 1, \dots, K$ , simulate  $y_k^{(b)} \sim NB(\mu_k^{(b,adj)}, \hat{\theta})$

78 4. Compute subregion mean density, subregion abundance, and total abundance as

(a) The mean catch density in subregion  $h$  is

$$\bar{\delta}_h^{(b)} = \frac{\sum_{k \in h} y_k^{(b)} / K_h}{Vol_p}$$

79 where  $K_h$  is the number of prediction locations in  $h$ .

80 (b) The total predicted number of fish per subregion is  $\hat{N}_h^{(b)} = \bar{\delta}_h^{(b)} Vol_h$

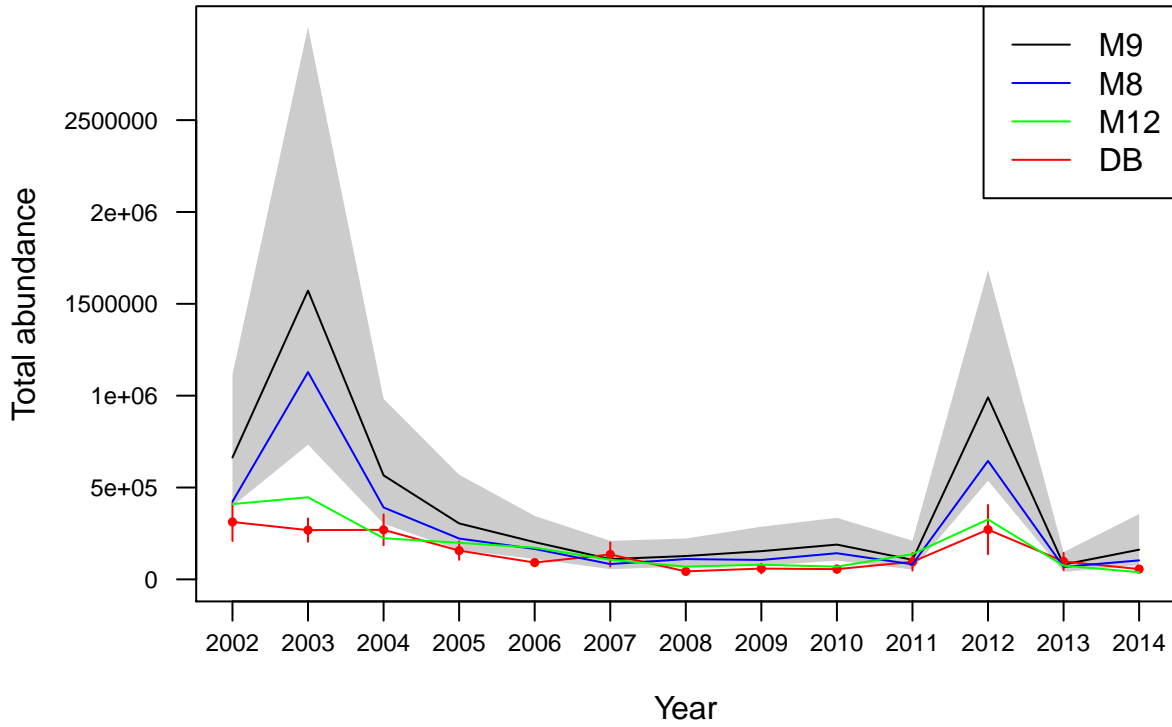
(c) The total predicted number of fish is

$$N_{tot}^{(b)} = \sum_{h=1}^{27} \hat{N}_h^{(b)}$$

Table S1: Abundance estimates and annual growth rates for February using design- and model-based approaches. Model based estimates are from Model 9 (Table 1 of the main text). Growth rates are year-over-year ratios.

Year	Model-based		Design-based	
	Abundance	Growth rate	Abundance	Growth rate
2002	312488		649028	
2003	268157	0.86	1479322	2.28
2004	269777	1.01	545347	0.37
2005	156633	0.58	291774	0.54
2006	91509	0.58	191509	0.66
2007	135563	1.48	100526	0.52
2008	43603	0.32	125398	1.25
2009	58877	1.35	142908	1.14
2010	55650	0.95	173163	1.21
2011	95682	1.72	86463	0.50
2012	271020	2.83	891304	10.31
2013	97707	0.36	74772	0.08
2014	56027	0.57	136596	1.83

Figure S5: Abundance estimates from model-based approaches using models M8, M9, and M12, and design-based. Grey shading shows the central 95% prediction interval for the M9 based predictions.



81 **References**

82 Thompson, Steven K. 2002. Sampling, Second Edition. John Wiley & Sons, Inc. New  
83 York, NY

84 Wood, Simon W. 2006. Generalized Additive Models: An Introduction with R. Chapman  
85 & Hall, Boca Raton, FL

## 86 Appendix

87 R code used to fit the models and compute predictions and prediction intervals. Complete  
88 R code and input data available on request.

```
89 rm(list=ls())
90 library(MASS)
91 library(mgcv)
92 library(maptools)
93 library(proj4)
94 library(rgdal)
95 library(xtable)
96 library(rgeos)
97 library(car)
98 library(ncf)
99 library(geoR)
100 if(Sys.info()['sysname'] == 'Darwin'){
101   library(parallel)
102 }else{library(parallelsugar)}
103
104
105 data.root <- '~/smelt/gam-analyses/SKT-gam-analyses/Data/'
106
107 load(paste0(data.root, 'SKT-2002-2014-gam-analysis-data-prep-v7.RData'))
108
109
110 # Time consuming model fits
111 load.M8.M12 <- TRUE
112 if(load(load.M8.M12)){
113   load(file=paste0(data.root, 'SKT-2002-2014-gam-analysis-soap-v9-M8.RData'))
114   load(file=paste0(data.root, 'SKT-2002-2014-gam-analysis-soap-v12-M8.RData'))
115 }
116
117 # M12
118 fit.M12 <- FALSE
119 if(fit.M12){
120   m.regional.local.by.month.year.formula <- as.formula("smelt~offset(logVol)+
121     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fCohort.year.month)
122     +Secchi.z+Cond.z+Tide")
123   m.regional.local.by.month.year <- gam(m.regional.local.by.month.year.formula,
124     family=nb(),
125     knots=knots,data=ds,method="ML")
126   save(list=ls(),
127     file=paste0(data.root, 'SKT-2002-2014-gam-analysis-soap-v9-M12.RData'))
```

```

128 }
129
130 # M8
131 fit.M8 <- FALSE
132 if(fit.M8){
133   m.regional.by.month.year.formula <- as.formula("smelt~offset(logVol)+
134     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fCohort.year.month)")
135   m.regional.by.month.year <- gam(m.regional.by.month.year.formula,family=nb(),
136     knots=knots,data=ds,method="ML")
137   save(list=ls(),
138     file=paste0(data.root,'SKT-2002-2014-gam-analysis-soap-v9-M8.RData')
139 }
140
141 # Remaining models
142 #VIF model
143 r.vif <- glm.nb(smelt~offset(logVol)+Secchi.z+Cond.z+Tide+Month+SubRegion,
144   data=ds)
145 vif(r.vif)
146
147 r.vif <- glm.nb(smelt~offset(logVol)+Secchi.z+Cond.z+Tide+Month+Lon.z+Lat.z,
148   data=ds)
149 vif(r.vif)
150
151 # 1) Global: no regional (smooth), no local
152 m.global <- glm.nb(smelt~offset(logVol)+fCohort.year*JD,data=ds)
153
154 # Global + one local to estimate the best a particular local covariate can do
155 m.global.plus.Secchi <- glm.nb(smelt~offset(logVol)+fCohort.year*JD+Secchi.z,data=ds)
156 m.global.plus.cond <- glm.nb(smelt~offset(logVol)+fCohort.year*JD+Cond.z,data=ds)
157 m.global.plus.tide <- glm.nb(smelt~offset(logVol)+fCohort.year*JD+Tide,data=ds)
158
159 # 2) Global x regional: no by in smooth
160 m.regional.formula <- as.formula("smelt~offset(logVol)+
161   fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb))")
162 t1 <- Sys.time()
163 m.regional <- gam(m.regional.formula,family=nb(),
164   knots=knots,data=ds,method="ML")
165 t2 <- Sys.time()
166 difftime(t2,t1)
167
168 # 3) Global x regional: by month
169 m.regional.by.month.formula <- as.formula("smelt~offset(logVol)+
170   fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fmonth)")
171
172 t1 <- Sys.time()

```

```

173 m.regional.by.month <- gam(m.regional.by.month.formula,family=nb(),
174                             knots=knots,data=ds,method="ML")
175 t2 <- Sys.time()
176 difftime(t2,t1)
177
178
179 # 4) Global x regional: by year (cohort)
180 m.regional.by.year.formula <- as.formula("smelt~offset(logVol)+
181     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fCohort.year)")
182
183 t1 <- Sys.time()
184 m.regional.by.year <- gam(m.regional.by.year.formula,family=nb(),
185                             knots=knots,data=ds,method="ML")
186 t2 <- Sys.time()
187 difftime(t2,t1)
188
189 # 6) Global x regional x local: No by
190 m.regional.local.formula <- as.formula("smelt~offset(logVol)+
191     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb))+Secchi.z+Cond.z+Tide")
192
193 t1 <- Sys.time()
194 m.regional.local <- gam(m.regional.local.formula,family=nb(),
195                             knots=knots,data=ds,method="ML")
196 t2 <- Sys.time()
197 difftime(t2,t1)
198
199 # 7) Global x regional x local: by month
200 m.regional.local.by.month.formula <- as.formula("smelt~offset(logVol)+
201     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fmonth)
202     +Secchi.z+Cond.z+Tide")
203
204 t1 <- Sys.time()
205 m.regional.local.by.month <- gam(m.regional.local.by.month.formula,
206                                 family=nb(),knots=knots,data=ds,method="ML")
207 t2 <- Sys.time()
208 difftime(t2,t1)
209
210 # 8) Global x regional x local: by year (cohort)
211 m.regional.local.by.year.formula <- as.formula("smelt~offset(logVol)+
212     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb),by=fCohort.year)
213     +Secchi.z+Cond.z+Tide")
214
215 t1 <- Sys.time()
216 m.regional.local.by.year <- gam(m.regional.local.by.year.formula,family=nb(),
217                                 knots=knots,data=ds,method="ML")

```

```

218 t2 <- Sys.time()
219 difftime(t2,t1)
220
221
222 m <- m.regional.local
223
224 # Drop one local cov at a time to look at
225 # proportion deviance explained by adding this cov to a global X regional model
226 m.regional.local.minus.Secchi <- gam(smelt~offset(logVol)+
227                                     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb))+
228                                     Cond.z+Tide,family=nb(),
229                                     sp=m$sp,knots=knots,data=ds,method="ML")
230
231 m.regional.local.minus.cond <- gam(smelt~offset(logVol)+
232                                     fCohort.year*JD+s(x,y,bs='so',xt=list(bnd=fsb))+
233                                     Secchi.z+Tide,family=nb(),
234                                     sp=m$sp,knots=knots,data=ds,method="ML")
235
236 m.regional.local.minus.tide <- gam(smelt~offset(logVol)+fCohort.year*JD+
237                                     s(x,y,bs='so',xt=list(bnd=fsb))+
238                                     Secchi.z+Cond.z,family=nb(),
239                                     sp=m$sp,knots=knots,data=ds,method="ML")
240
241 #####----- Make predictions of abundance in Feb -----#####
242 # Make predictions at each grid location on Feb 15th
243 # for flood and ebb tides and bootstrap prediction intervals
244 ucym <- as.character(unique(ds$fCohort.year.month))
245 index.Feb <- which(as.numeric(unlist(lapply(as.character(ucym),
246                                     FUN=function(x){y=strsplit(x,split="-")[[1]][3]})))==2)
247 ucym.Feb <- ucym[index.Feb]
248
249 # Make predictions on grid-
250 # Why doesn't crs(DSLCM.SubRegions) or CRS(DSLCM.SubRegions) work here?
251 # Why does crs work on a Windows PC? Or does it?
252 spatial.grid.predict <- SpatialPoints(grid.predict,
253                                     proj4string=attributes(DSLCM.SubRegions)$proj4string)
254 grid.predict.with.subregions <- cbind(grid.predict,
255                                     over(spatial.grid.predict,DSLCM.SubRegions))
256
257 # Prediction volume
258 vol.p <- 10000
259
260 # Don't fix boundary at 0 for covariates
261 fsb.cov <- vector("list",1)
262 fsb.cov[[1]]$x <- region.boundary[,"x"]

```

```

263 fsb.cov[[1]]$y <- region.boundary[, "y"]
264
265 grid.cov.gam.func <- function(ucym, dat, cov){
266   # Get subregion averages of a given covariate for a dataset dt
267   dt <- subset(dat, fCohort.year.month==ucym)
268   names(dt)[which(names(dt)=="UTMX")] <- "x"
269   names(dt)[which(names(dt)=="UTMY")] <- "y"
270   cov.temp <- dt[, cov]
271   if(nrow(dt)>27){
272     cov.gam <- try(gam(cov.temp~s(x,y,bs="so",xt=list(bnd=fsb.cov)),
273                   knots=knots,data=dt,method="ML"))
274   }else{
275     cov.gam <- try(gam(cov.temp~s(x,y,k=25),data=dt,method="ML"))
276   }
277   return(cov.gam)
278 }
279
280 Secchi.z.models <- lapply(as.character(ucym),
281                          FUN=grid.cov.gam.func, dat=ds, cov='Secchi.z')
282 Cond.z.models <- lapply(as.character(ucym),
283                          FUN=grid.cov.gam.func, dat=ds, cov='Cond.z')
284
285 Secchi.z.gam.gof <- unlist(lapply(Secchi.z.models,
286                                  FUN=function(x){summary(x)$dev.expl}))
287 Cond.z.gam.gof <- unlist(lapply(Cond.z.models,
288                                  FUN=function(x){summary(x)$dev.expl}))
289
290 range(Secchi.z.gam.gof[index.Feb])
291 median(Secchi.z.gam.gof[index.Feb])
292 quantile(Secchi.z.gam.gof[index.Feb], probs=seq(.1, 1, by=.1))
293 range(Cond.z.gam.gof[index.Feb])
294 median(Cond.z.gam.gof[index.Feb])
295 quantile(Cond.z.gam.gof[index.Feb], probs=seq(.1, 1, by=.1))
296
297 grid.cov.gam.pred.func <- function(m, gcv.est=TRUE){
298   # Sample a prediction from a fitted GAM model m
299   # Returns a prediction at each location of the grid
300   # If gcv.est=F, prediction includes uncertainty in the
301   #   model coefficients and observation error
302   # Prediction does not include uncertainty in the smoothing paramter
303   data.new <- data.frame(x=grid.predict$x, y=grid.predict$y)
304   if(gcv.est){
305     y <- predict(m, newdata=data.new, type='response')
306   }else{
307     beta <- coef(m)

```

```

308     Vb <- m$Vc
309     Cv <- chol(Vb)
310     n.rep=1
311     nb <- length(beta)
312     br <- t(Cv) %*% matrix(rnorm(n.rep*nb),nb,n.rep) + beta
313     Xp <- predict(m,newdata=data.new,type="lpmatrix")
314     lp <- Xp %*% br
315     y <- rnorm(length(lp),mean=lp,sd=sqrt(m$sig2))
316   }
317   return(y)
318 }
319
320 cpue.newdata.grid.func <- function(fcym,tide.set,gcv.est){
321   index.temp <- which(ucym==fcym)
322   Secchi.z.temp <- grid.cov.gam.pred.func(m=Secchi.z.models[[index.temp]],
323                                           gcv.est=gcv.est)
324   Cond.z.temp <- grid.cov.gam.pred.func(m=Cond.z.models[[index.temp]],
325                                           gcv.est=gcv.est)
326
327   # Sets up a data frame of new data for making CPUE predictions
328   Month <- as.numeric(strsplit(as.character(fcym),split="-")[[1]][3])
329   if(Month==1){JD=15}
330   if(Month==2){JD=45}
331   if(Month==3){JD=74}
332   if(Month==4){JD=105}
333   if(Month==5){JD=135}
334
335   dn <- data.frame(
336     logVol=log(vol.p),
337     fCohort.year=factor(paste(
338       strsplit(as.character(fcym),split="-")[[1]][1:2],collapse="-"),
339       levels=levels(ds$fCohort.year)),
340     fCohort.year.month=factor(fcym,levels=levels(ds$fCohort.year.month)),
341     JD=JD,
342     fmonth=strsplit(fcym,split="-")[[1]][3],
343     Secchi.z=Secchi.z.temp,
344     Cond.z=Cond.z.temp,
345     Tide=tide.set,
346     x=grid.predict$x,
347     y=grid.predict$y
348   )
349   return(dn)
350 }
351
352 beta.param.vect.sample.from.gam <- function(m,b){

```



```

353 # m a fitted GAM, returns a J x b column vector of
354 # a samples of beta, J=length(beta)
355 beta <- coef(m)
356 Vb <- m$Vc
357 Cv <- chol(Vb)
358 n.rep <- b
359 nb <- length(beta)
360 br <- t(Cv) %*% matrix(rnorm(n.rep*nb),nb,n.rep) + beta
361 return(br)
362 }
363
364 var.sum.func <- function(a,x,Sigma){
365 # a, x- vectors of same length; Sigma- covariance matrix of x
366 # Let X=(a_1*x_1,...,a_n*x_n)
367 # Computes the variance of the of sum of the elements of X
368 # Var(sum(X))=sum_i a_i^2*Var(x_i)+2*sum_1<=i<j<=n a_i*a_j*Cov(x_i,x_j)
369
370 ai.aj <- combn(a,m=2,prod) # Get all a_i*a_j products for 1<=i<j<=n
371
372 # Get index of cov(x_i,x_j) values in same order as ai.aj vector
373 off.diag.index <- combn(1:ncol(Sigma),m=2) #All possible combinations of 1,...,n
374 off.diag.index <- cbind(off.diag.index[1,],off.diag.index[2,])
375
376 # Get the Cov(x_i,x_j) terms
377 off.diag.var.cov <- Sigma[off.diag.index]
378
379 # Compute variance of the sum
380 r <- sum(a^2*diag(Sigma))+sum(2*ai.aj*off.diag.var.cov)
381 return(r)
382 }
383
384 boot.pred.func <- function(m,fcym,tide.set,boot){
385 # ****Get covariance matrix of beta from m
386 # For bias correcting mu_k samples in the boot loop.
387 # See **** Do this here for speed.
388 # Actual variance will depend on Xp.boot so need to wait till boot
389 # loop to finish computing
390 off.diag.index <- combn(1:ncol(m$Vc),m=2) #All possible combinations of 1,...,n
391 off.diag.index <- cbind(off.diag.index[1,],off.diag.index[2,])
392 off.diag.var.cov <- m$Vc[off.diag.index]
393 v.m <- diag(m$Vc)
394
395 # Predictions at estimated parameters
396 data.new <- cpue.newdata.grid.func(fcym=fcym,tide.set=tide.set,gcv.est=T)
397 Xp <- predict(m,newdata=data.new,type="lpmatrix")

```

```

398 mu.pred.linear <- Xp %*% coef(m)+log(vol.p)
399 #GLM models don't bias correct when making prediction from log link models
400 mu.pred <- exp(mu.pred.linear)
401
402 mu.pred.mean.sr <- tapply(mu.pred,grid.predict.with.subregions$SubRegion,mean)
403
404 index.match <- match(wv$SubRegion,names(mu.pred.mean.sr))
405
406 tot.pop.size <- sum(mu.pred.mean.sr[index.match]*wv$twom,na.rm=T)/vol.p
407
408 if(boot==0){
409   return(list(
410     tot.pop.size=tot.pop.size,
411     mean.pop.boot=NA,
412     tot.pop.pred.boot.interval=NA
413   ))
414 }else{
415   boot.tot.pop.size <- rep(NA,boot)
416   theta.est <- m$family$getTheta(TRUE)
417   for(i in 1:boot){
418     # Step 1- simulate from covariate data models Xp_boot
419     boot.data.new <- cpue.newdata.grid.func(fcym=fcym,tide.set=tide.set,
420                                           gcv.est=F)
421     Xp.boot <- predict(m,newdata=boot.data.new,type="lpmatrix")
422
423     # Sample a beta_b from N(hat(beta),Sigma_hat(beta))
424     beta.samp <- beta.param.vect.sample.from.gam(m=m,b=1)
425
426     # Make linear predictor using sample beta and sample covariates
427     boot.mu.pred.linear <- Xp.boot %*% beta.samp+log(vol.p)
428
429     # View log(tau_b)=boot.mu.pred.linear as a normally distributed variable
430     # tau_b ~ LN(logmean=Xp.boot %*% hat(beta)+log(vol.p),
431     #   varlog= Var(Xp.boot %*% hat(beta)+log(vol.p))=Var(Xp.boot %*% hat(beta))
432     # Then bias correct exp(log(tau_b))
433     # Bias correct assuming boot.mu ~ LN with mean=boot.mu.pred,
434     #   variance=sigma^2
435     # mu_i=1*beta_0+Xp1[i,1]*beta1+...+Xp[i,n]*beta_n
436     # mu=beta_0+x1*beta_1+x2*beta_2+...+xn*beta_n
437     # Var(mu)=sum_over_i x_i^2*var(beta_i)+
438     #   sum_over_i*sum_over_j x_i*x_j*Cov(beta_i,beta_j) covariance of sums formula
439     # Var(mu)=
440     #   sum_over_i x_i^2*var(beta_i)+2*sum_1<=i<j<=N x_i*x_j*cov(beta_i,beta_j)
441     # ****Have covariance matrix of beta
442     sig2 <- rep(NA,length(boot.mu.pred.linear))

```

```

443     for(k in 1:length(boot.mu.pred.linear)){
444         ai.aj <- combn(Xp.boot[k,],m=2,prod) #All a_i*a_j products for 1<=i<j<=n
445         sig2[k] <- sum(Xp.boot[k,]^2*v.m)+sum(2*ai.aj*off.diag.var.cov)
446         #sig2[k] <- var.sum.func(a=Xp.boot[k,],x=coef(m),Sigma=m$Vc)
447     }
448     # End bias correct
449
450     boot.mu.pred <- exp(boot.mu.pred.linear-sig2/2)
451     boot.pred <- rnegbin(boot.mu.pred,theta=theta.est)
452     boot.dens.pred <- boot.pred/vol.p
453
454     boot.mean.dens.sr <- tapply(
455         boot.pred,grid.predict.with.subregions$SubRegion,mean)
456
457     boot.tot.pop.size[i] <- sum(
458         boot.mean.dens.sr[index.match]*wv$twom,na.rm=T)/vol.p
459     }
460     return(list(
461         tot.pop.size=tot.pop.size,
462         mean.pop.boot=mean(boot.tot.pop.size),
463         tot.pop.pred.boot.interval=quantile(
464             boot.tot.pop.size,probs=c(.025,.25,.5,.75,.975))
465     ))
466 }
467 }
468
469 # t1 <- Sys.time()
470 # e=boot.pred.func(m=m,fcym=ucym[2],tide.set="Flood",boot=2)
471 # t2 <- Sys.time()
472 # difftime(t2,t1)
473
474 # Check on understanding p1 should equal p1.alt
475 # t1 <- Sys.time()
476 # i=1
477 # fcym.temp <- as.character(ucym[i])
478 # data.new <- cpue.newdata.grid.func(fcym=fcym,tide.set=tide.set,gcv.est=T)
479 # p1 <- predict(m,newdata=data.new,type="response")
480 # Xp.alt <- predict(m,newdata=data.new,type="lpmatrix")
481 # p1.alt <- exp(Xp.alt %*% (coef(m))+log(vol.p))
482 # max(abs(p1-as.numeric(p1.alt)))
483 # t2 <- Sys.time()
484 # difftime(t2,t1)
485
486 # Point estimates and uncertainty using model 9
487 pop.estimate.posterior.sim.feb.func <- function(X,tide,boot){

```

```

488   r <- boot.pred.func(m=m,fcym=X,tide.set=tide,boot=boot)
489   return(r)
490 }
491
492 boot.set <- 4 #1000
493 cor.set <- 4
494
495 t1 <- Sys.time()
496 p.store.list.ebb.feb <- mclapply(X=ucym.Feb,
497                                FUN=pop.estimate.posterior.sim.feb.func,
498                                tide="Ebb",boot=boot.set,mc.cores=cor.set)
499 t2 <- Sys.time()
500 difftime(t2,t1)
501
502 boot.set <- 1000
503 t1 <- Sys.time()
504 p.store.list.flood.feb <- mclapply(X=ucym.Feb,
505                                   FUN=pop.estimate.posterior.sim.feb.func,
506                                   tide="Flood",boot=boot.set,mc.cores=cor.set)
507 t2 <- Sys.time()
508 difftime(t2,t1)
509
510 save(list=ls(),file=paste0(data.root,'SKT-2002-2014-gam-analysis-soap-v10.RData'))
511
512 # Point estimates using model 10
513 pop.estimate.posterior.sim.feb.func.M10 <- function(X,tide,boot){
514   r <- boot.pred.func(m=m.regional.local.by.month,fcym=X,tide.set=tide,boot=boot)
515   return(r)
516 }
517 p.store.list.flood.feb.M10 <- lapply(X=ucym.Feb,
518                                     FUN=pop.estimate.posterior.sim.feb.func.M10,
519                                     tide="Flood",boot=0)
520
521 # Point estimates using model 12
522 pop.estimate.posterior.sim.feb.func.M12 <- function(X,tide,boot){
523   r <- boot.pred.func(m=m.regional.local.by.month.year,fcym=X,tide.set=tide,
524                       boot=boot)
525   return(r)
526 }
527 p.store.list.flood.feb.M12 <- lapply(X=ucym.Feb,
528                                     FUN=pop.estimate.posterior.sim.feb.func.M12,
529                                     tide="Flood",boot=0)
530
531 pop.est.ebb.feb <- data.frame(
532   est=unlist(lapply(p.store.list.ebb.feb,FUN=function(x){x$tot.pop.size})),

```

```

533 mean=unlist(lapply(p.store.list.ebb.feb,FUN=function(x){x$mean.pop.boot})),
534 median=unlist(lapply(p.store.list.ebb.feb,FUN=function(x){
535   x$tot.pop.pred.boot.interval['50%']})),
536 lower=unlist(lapply(p.store.list.ebb.feb,FUN=function(x){
537   x$tot.pop.pred.boot.interval['2.5%']})),
538 upper=unlist(lapply(p.store.list.ebb.feb,FUN=function(x){
539   x$tot.pop.pred.boot.interval['97.5%']})))
540 pop.est.flood.feb <- data.frame(
541   est=unlist(lapply(p.store.list.flood.feb,FUN=function(x){x$tot.pop.size})),
542   mean=unlist(lapply(p.store.list.flood.feb,FUN=function(x){x$mean.pop.boot})),
543   median=unlist(lapply(p.store.list.flood.feb,FUN=function(x){x$mean.pop.boot})),
544   lower=unlist(lapply(p.store.list.flood.feb,FUN=function(x){
545     x$tot.pop.pred.boot.interval['2.5%']})),
546   upper=unlist(lapply(p.store.list.flood.feb,FUN=function(x){
547     x$tot.pop.pred.boot.interval['97.5%']})))
548
549 pop.point.estimate.ebb.feb <- unlist(lapply(p.store.list.ebb.feb,
550                                           FUN=function(x){x$tot.pop.size}))
551 pop.point.estimate.flood.feb <- unlist(lapply(p.store.list.flood.feb,
552                                           FUN=function(x){x$tot.pop.size}))
553 pop.point.estimate.flood.feb.M10 <- unlist(lapply(p.store.list.flood.feb.M10,
554                                                  FUN=function(x){x$tot.pop.size}))
555 pop.point.estimate.flood.feb.M12 <- unlist(lapply(p.store.list.flood.feb.M12,
556                                                  FUN=function(x){x$tot.pop.size}))
557
558 plot(pop.point.estimate.flood.feb,
559       pop.point.estimate.flood.feb.M10,type='n',xlab='',ylab='')
560 abline(a=0,b=1)
561 title(xlab='Model 9 (single smooth for all months)',line=2.2)
562 title(ylab='Model 10 (month specific smooth)',line=2.2)
563 text(pop.point.estimate.flood.feb,pop.point.estimate.flood.feb.M10,
564       labels=sapply(uy,FUN=function(x){substr(x,start=3,stop=4)}))
565 cor(pop.point.estimate.flood.feb,pop.point.estimate.flood.feb.M10)
566 round(100*(pop.point.estimate.flood.feb.M10-pop.point.estimate.flood.feb)/
567       pop.point.estimate.flood.feb,2)
568
569 ab=data.frame(Year=uy,M9=pop.point.estimate.flood.feb,
570              M10=pop.point.estimate.flood.feb.M10,
571              M12=pop.point.estimate.flood.feb.M12)
572 print(ab,row.names=F)
573
574 ab=data.frame(
575   Coef=names(coef(m)[1:14]),
576   M9=coef(m)[1:14],
577   M10=coef(m.regional.local.by.month)[1:14],

```

```

578   M12=coef(m.regional.local.by.month.year)[1:14]
579 )
580 print(ab,row.names=F)
581
582 p.f <- function(x,p.t,col.set){
583   y.lim <- c(-10,3)
584   plot(x,type='n',ylim=y.lim,xaxt='n',xlab='',ylab='')
585   axis(side=1,at=x,labels=row.names(p.t),las=2,cex.axis=.85)
586
587   for(i in 1:nrow(p.t)){
588     points(x[i],p.t[i,'Estimate'],col=col.set,pch=20)
589     lines(rep(x[i],2),c(p.t[i,'Estimate']-p.t[i,'Std. Error'],
590                        p.t[i,'Estimate']+p.t[i,'Std. Error']),col=col.set)
591   }
592 }
593 p.f2 <- function(x,p.t,col.set){
594   for(i in 1:nrow(p.t)){
595     points(x[i],p.t[i,'Estimate'],col=col.set,pch=20)
596     lines(rep(x[i],2),c(p.t[i,'Estimate']-p.t[i,'Std. Error'],
597                        p.t[i,'Estimate']+p.t[i,'Std. Error']),col=col.set)
598   }
599 }
600
601 par(mar=c(10,3,2,1))
602 p.f(x=seq(1,31,by=1),p.t=summary(m.regional.local)$p.table,col.set='blue')
603 p.f2(x=seq(1.1,31.1,by=1),p.t=summary(m.regional.local.by.month)$p.table,
604      col.set='red')
605 p.f2(x=seq(1.2,31.2,by=1),p.t=summary(m.regional.local.by.month.year)$p.table,
606      col.set='green')
607 legend('bottomright',legend=c('M9','M10','M12'),
608      col=c('blue','red','green'),pch=20)
609
610 p.t.M9=summary(m)$p.table
611 p.t.M12=summary(m.regional.local.by.month.year)$p.table
612
613 delta0.M9 <- exp(c(p.t.M9[1,'Estimate'],
614                  p.t.M9[1,'Estimate']+p.t.M9[2:13,'Estimate']))
615 delta0.M12 <- exp(c(p.t.M12[1,'Estimate'],
616                   p.t.M12[1,'Estimate']+p.t.M12[2:13,'Estimate']))
617
618 print(data.frame(cohort=cohort,M9.delta0=delta0.M9,
619                M12.delta0=delta0.M12,ratio=delta0.M12/delta0.M9),row.names=F)
620
621 data.frame(cohort=cohort,M9.delta0=delta0.M9,
622           M12.delta0=delta0.M12,ratio=delta0.M12/delta0.M9)

```

```

623 s.t.M9=summary(m)$s.table
624 s.t.M12=summary(m.regional.local.by.month.year)$s.table
625
626 a=names(coef(m.regional.local.by.month.year))
627
628
629 # Summaries across models
630 # Theta estimates
631 theta.est <- c(m.global$theta,
632 m.global.plus.Secchi$theta,
633 m.global.plus.cond$theta,
634 m.global.plus.tide$theta,
635 unlist(lapply(list(m.regional,
636 m.regional.by.month,
637 m.regional.by.year,
638 m.regional.by.month.year,
639 m.regional.local,
640 m.regional.local.by.month,
641 m.regional.local.by.year,
642 m.regional.local.by.month.year,
643 m.regional.local.minus.Secchi,
644 m.regional.local.minus.cond,
645 m.regional.local.minus.tide),FUN=function(x){
646 return(x$family$getTheta(TRUE)}))
647 )
648 theta.est
649 range(theta.est)
650 m$family$getTheta(TRUE)
651
652 # Model comparison
653 prop.dev.func <- function(a){
654 return((a$null.deviance-a$deviance)/a$null.deviance)
655 }
656
657 AIC.set <- AIC(m.global,
658 m.global.plus.Secchi,
659 m.global.plus.cond,
660 m.global.plus.tide,
661 m.regional,
662 m.regional.by.month,
663 m.regional.by.year,
664 m.regional.by.month.year,
665 m.regional.local,
666 m.regional.local.by.month,
667 m.regional.local.by.year,

```

```

668         m.regional.local.by.month.year,
669         m.regional.local.minus.Secchi,
670         m.regional.local.minus.cond,
671         m.regional.local.minus.tide
672     )
673
674 index.temp <- which.min(AIC.set$AIC)
675 delta.AIC.set <- AIC.set$AIC-AIC.set$AIC[index.temp]
676
677 ML.score.set <- c(NA,NA,NA,NA,unlist(lapply(list(
678     m.regional,
679     m.regional.by.month,
680     m.regional.by.year,
681     m.regional.by.month.year,
682         m.regional.local,
683         m.regional.local.by.month,
684         m.regional.local.by.year,
685     m.regional.local.by.month.year,
686         m.regional.local.minus.Secchi,
687         m.regional.local.minus.cond,
688         m.regional.local.minus.tide),FUN=function(x){x$gcv.ubre})))
689
690 Percent.dev.exl.set <- unlist(lapply(list(
691     m.global,
692     m.global.plus.Secchi,
693     m.global.plus.cond,
694     m.global.plus.tide,
695     m.regional,
696     m.regional.by.month,
697     m.regional.by.year,
698     m.regional.by.month.year,
699         m.regional.local,
700         m.regional.local.by.month,
701         m.regional.local.by.year,
702     m.regional.local.by.month.year,
703         m.regional.local.minus.Secchi,
704         m.regional.local.minus.cond,
705         m.regional.local.minus.tide),FUN=function(x){prop.dev.func(x})))
706
707 dev.expl.table <- data.frame(
708 Model=c('Global',
709 'Global + Secchi',
710 'Global + cond',
711 'Global + tide',
712 'Global + regional (single)',

```



```

713 'Global + regional (month)',
714 'Global + regional (year)',
715 'Global + regional (month year)',
716     'Global + regional (single) + local',
717     'Global + regional (month) + local',
718     'Global + regional (year) + local',
719     'Global + regional (year) + local',
720     'Global + regional (single) + local - Secchi',
721     'Global + regional (single) + local - cond',
722     'Global + regional (single) + local - Tide'),
723 Df=AIC.set$df,
724 AIC=AIC.set$AIC,
725 delta.AIC=delta.AIC.set,
726 SSC=ML.score.set,
727 'Dev. exp.'=100*Percent.dev.expl.set,
728 'Theta'=theta.est
729 )
730 dev.expl.table <- data.frame(M=1:nrow(AIC.set),Model=dev.expl.table$Model,round(dev.expl
731 dev.expl.table
732 write.csv(dev.expl.table,
733           file='~/smelt/gam-analyses/SKT-gam-analyses/dev-explained-table-v10.csv',
734           row.names=F)
735 print.xtable(xtable(dev.expl.table,digits=1),include.rownames=F)

```