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1	BEHAVIOR OF FRP-STRENGTHENED RC ELEMENTS
2	SUBJECTED TO PURE SHEAR
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11	
12	ABSTRACT

The shear behavior of fiber reinforced polymer strengthened reinforce concrete (FRP 13 14 strengthened RC) has been the focus of extensive research studies. However, the mechanism of 15 this complex phenomenon has not been fully clarified. Recent analytical models which were 16 developed for predicting the shear capacity of FRP strengthened RC girders were based on test 17 results of simply supported beam specimens with various shear span-to-depth ratios. In such 18 tests no region of the specimen is subjected to uniform stress conditions, Therefore, 19 the results of such tests cannot predict the true pure shear behavior due to non-uniformity of stresses, the presence of flexural and other non-shear related effects such as a/d ratio that 20 21 cannot be filtered out. Therefore, proper design of shear strengthening using FRP requires testing 22 of elements that are subjected to pure shear case primary before adding other governing effects. This allows a careful investigation and full understanding of the behavior at the element level. In 23 24 order to accomplish this task, panel testing of representative RC specimens strengthened with FRP sheets were needed. This paper reports the testing of 10 FRP strengthened RC panels 25 subjected to pure shear stress field. The tests were carried out to evaluate the effects of three 26

variables: FRP stiffness, FRP wrapping scheme, and transverse steel reinforcement ratio. The test results showed that these three variables greatly affected the shear behavior due to various types of failure modes associated with FRP strengthening. In addition, it was observed that the magnitude of increased shear capacity associated with the application of FRP sheets depends not only upon the stiffness of FRP, but also on the stiffness of internal shear reinforcement. With the increase of internal steel shear reinforcement, the effectiveness of shear gain due to externally bonded FRP decreases.

34 Keywords: Shear behavior; FRP strengthened RC members; Failure modes; Wrapping Scheme

35

36 INTRODUCTION

37 As a response to corrosion problems in reinforcing steel, and to increase the efficiency of strengthening systems in terms of time and ease of application, FRP composites have been 38 39 increasingly used in rehabilitation and strengthening of RC structures [1]. The complex behavior 40 of FRP-strengthened RC structures with predominant shear behavior has been previously studied through extensive experimental and analytical investigations [2-4]. Research related to the 41 42 flexural behavior of FRP-strengthened elements has reached an advanced stage, and well established analytical models are available for analyzing and designing FRP-strengthened beams 43 and columns under flexural and axial-confinement actions [1, 5]. However, the experimental and 44 analytical research related to FRP strengthened RC under shear load are limited and has not been 45 fully developed [6-10] 46

To predict the behavior of FRP-strengthened RC elements in shear, the truss model approach is commonly utilized by researchers [8, 11-12]. In the truss model analogy, constitutive laws of each component, namely concrete, steel, and FRP external reinforcement are crucial for

50 acceptable predictions. The results presented in this paper are part of a research work which aimed at developing a modified softening membrane model (SMM) for FRP-strengthened RC 51 elements subjected to shear stress field. The SMM is based on a truss model and has been 52 53 developed and was used to predict the entire shear stress-strain curve of the RC element under inplane shear stress field [13]. The materials laws utilized is SMM was a work carried out by 54 55 Belarbi et al. [14] and are widely accepted and used in several versions of the Softened truss models [13,15]. While adding external reinforcement such as FRP sheets, the behavior of 56 elements such as concrete, steel and FRP are typically altered due to several effects such as the 57 58 crack pattern, softened concrete struts, and Poison's ratio. The smeared stress-strain behavior of the constituents of strengthened member including concrete and reinforcing steel will be 59 fundamentally different than their corresponding values for un-strengthened specimens. 60 Consequently, different failure modes exist, and in turn affects the shear strength. In addition to 61 the failure modes related to concrete in RC members such as diagonal tension failure in the 62 web, shear compression failure in compression zone and flexure failure, FRP 63 debonding and FRP rupture are common failure modes in FRP strengthened RC 64 members [4, 11]. The problem is further complicated due to the presence of several additional 65 66 parameters that might influence the behavior; parameters such as the properties of the FRP material, the angle of fiber direction, the characteristics of the fiber-resin interface and FRP-67 concrete interface, the presence of mechanical anchors, and the use of FRP strips as opposed to 68 69 continuous sheets. These additional parameters modify the crack patterns, failure modes, and in turn influence the constitutive behavior of concrete [6,8,16]. Recent analytical models that were 70 developed for predicting the shear capacity of FRP-strengthened RC beams are based on test 71 72 results of simply supported beam specimens with various shear span-to-depth ratios. Results of 73 such tests cannot represent the true pure shear behavior due to the presence of flexural and other 74 non-shear related effects that cannot be filtered out. As a result, a rational shear design cannot be accurately developed. An efficient method to evaluate the overall shear response of a member is 75 76 to identify the characteristic behavior and the contribution of each element and material constituting the structure [17]. Reinforced concrete structures, such as shells and nuclear 77 78 containment vessels, resist applied loads primarily through in-plane stresses. Each structure can be characterized as an assembly of elements, each subjected to two in-plane normal stresses and 79 one in-plane shear stress [18]. To perform a rational analysis and thoroughly understand the 80 81 behavior of FRP-strengthened RC structures, elements (panels) are isolated from the structure. Once a rational model is developed to predict the shear behavior in element level, the model can 82 then be incorporated into a finite element program to predict the behavior of the whole structure. 83

The first step in the research was to experimentally investigate the shear constitutive behavior of 84 FRP-strengthened RC elements subjected to pure shear. To evaluate such behavior, a series of 85 full scale FRP-strengthened RC panels were constructed and tested using the Universal Panel 86 Tester housed at the University of Houston [17]. Pure shear loading condition was simulated 87 88 through proportionally applied biaxial tension-compression load. The test results of 10 elements 89 (panels) subjected to pure shear loading are reported in this paper. The second step of the research was to develop an analytical model to predict the behavior of FRP-strengthened RC 90 91 membrane elements subjected to pure shear. This new model, so-called the Softened Membrane 92 Model for FRP-strengthened RC members (SMM-FRP), is described elsewhere [16,19].

93 The shear behavior of FRP-strengthened RC members is influenced by various factors. This94 study focuses on parameters that have been recognized by other researchers to have the most

95 influence on the behavior [6,8,20]. These parameters are (1) FRP reinforcement ratio (FRP
96 stiffness), (2) wrapping scheme, and (3) transverse steel reinforcement ratio.

97 FRP Sheet Stiffness

FRP sheet stiffness $(E_f t_f)$ affects the contribution of FRP reinforcement to the overall 98 shear strength of FRP strengthened RC members. Previous research studies have indicated that 99 100 there exists a limit with respect to axial rigidity of the applied materials beyond which no 101 increase in shear capacity is expected [20]. When the thickness of the FRP sheets applied to RC 102 beam increases, the ultimate shear strength gain is limited by premature debonding from the 103 concrete substrate [21]. Also, the disproportionate strength gain when the FRP thickness (FRP stiffness) increases is due to the fact that the ultimate failure is primarily governed by the 104 105 concrete cracking, splitting and loss of aggregate interlock [4]. Furthermore, as the FRP axial 106 stiffness increases, the effective strains in the sheets decrease [6], therefore, the FRP materials 107 will not reach their expected capacity before failure. In this case, the failure mode of the member will be either concrete crushing or FRP debonding instead of FRP rupture. 108

Design guidelines such as ACI 440.2R-08 [1], CAN/CSA S806-12 [22] and *fib*-TG9.3 Bulletin 14 [23] fail to incorporate such behavior for strengthened beams when the thickness of FRP sheets (and hence the stiffness) is high. These design guidelines are based on Triantafillou's [24] statement that contribution to shear strength will increase with low values of axial stiffness. Therefore, only when FRP sheets with low thickness is applied, the current design guidelines are satisfactory [2].

115 Wrapping Scheme

The wrapping scheme affects the confinement due to the FRP sheets, and the potential for
debonding. Common wrapping schemes in shear strengthening are fully wrap, side bond, UWrap, and U-wrap with FRP anchor.

The FRP anchor provides an effective way of anchoring the FRP composite to the RC substrate. There have been several studies regarding the design and implementation of FRP anchors [25-28]. The main parameters considered in designing the FRP anchors include the anchor diameter, number of anchors needed and anchor length. The FRP anchor used in this research had a diameter of 12.7 mm and a length of 610 mm as shown in Fig. 3. A contact length of 216 mm was used to cover the whole width of the FRP sheets with 6.5 mm extra on both sides, which satisfies the recommended length suggested by Kobayashi et al. [29].

126 Transverse Steel Reinforcement Ratio

Previous studies have revealed that the magnitude of increased shear capacity associated with the application of FRP materials depend not only upon the type of FRP that is being used, but also on the amount of internal shear reinforcement [8,21,30]. Researchers have indicated that the contribution of FRP in shear gain reduces when the beam is heavily reinforced in shear. This is because the maximum shear contributions of steel stirrups and FRP material may not be reached simultaneously. Also, with the increase of steel shear reinforcement, the measured effective strain reduces [6].

134 EXPERIMENTAL PROGRAM

In order to evaluate the shear behavior of FRP-strengthened RC members and to
investigate the main factors that influence the behavior of such members, full-scale tests of 8
FRP-strengthened RC panels and 2 un-strengthened RC control panels were conducted.

138 The test panels were 1397×1397×178 mm (55×55×7 inches) in size, as shown in Fig. 1. The 139 longitudinal and transverse steel reinforcements were arranged at a 45 degree angle with respect to the principal directions of the applied loads (1-2 coordinates) along l and t directions and the 140 141 external FRP reinforcement was applied along transverse (t) direction. The steel reinforcement was grade 60 deformed bars with cross-sectional areas of 71 mm² (#3 rebar) and 129 mm² (#4 142 rebar) spaced at 188 mm in both longitudinal and transverse directions. The FRP sheets utilized 143 in the experimental program which are typically used for shear strengthening in practice, consist 144 of unidirectional carbon fibers attached on the two opposite surfaces of the panel specimens. The 145 146 overall FRP sheet layout of the specimens is shown in Fig. 2a. The FRP strips had a width of 144 147 mm, and 188 mm center to center distance. The nominal strength of concrete was 52 MPa. The rebar was welded onto a pre-embedded connector inserts that were connected to the loading 148 149 actuators by high-strength bolts. The steel reinforcement ratios and FRP sheet thicknesses were chosen carefully in order to study the effect of FRP stiffness on the shear behavior and also the 150 effect of the ratio of FRP reinforcement to steel reinforcement. Three common wrapping 151 152 schemes in shear strengthening are adopted, namely, 1) fully wrap, (2) side bond, and (3) U-wrap with FRP anchor. The fully wrap is to ensure that debonding is eliminated and the FRP will 153 154 reach its ultimate strength, while the side bonding scheme is to evaluate the behavior up to FRP debonding occurs. The U-wrap with FRP anchor is to simulate the real case of shear 155 strengthening with FRP in T-beams, where fully wrap method is infeasible due to the flanges. 156 Fully wrap and side bonding wrapping scheme of the panels are shown in Fig. 2b and Fig.2c, 157 respectively. Details of the U-wrap with FRP anchor are given in Fig. 3. 158

159 The test matrix in the experimental program is shown in Table 1. The specimens are identified 160 using transverse rebar size (No.3 and 4), FRP thickness [0.6, 1 mm, and 2 mm (0.025, 0.040 and

0.080 inch)] and wrapping schemes, namely, Fully Wrap (FW) (Fig. 2b), Side Bond (SB) (Fig.
2c), and U-wrap with FRP Anchor (FA) (Fig. 3). As an example, P4-025-SB stands for the
specimen with #4 transverse rebar, 0.6 mm (0.025 in.) thick FRP sheets and side bond (SB)
wrapping scheme. REF-P3 and REF-P4, stand for RC reference specimens with No. 3 and 4
transverse rebar, respectively.

166 Standard material tests were conducted to obtain the material properties. Type III cement was used for concrete casting. Standard 152 mm \times 305 mm (6 x 12 inch) cylinders were tested to 167 obtain the compressive strength of concrete f_c as per ASTM C39 [31]. The FRP sheets were 168 made of unidirectional carbon fibers with the material properties determined from coupon tests 169 per ASTM D3039 [32]. The wet lay-up system was used for installation of FRP sheets. The 170 specimen was ground, sandblasted, and power-washed to provide the proper concrete surface 171 conditions that would develop the necessary bond strength between the concrete and FRP sheets. 172 Putty and primer were first applied on the surface; the sheets were then impregnated with epoxy 173 resin and applied in-situ. Specimens were then cured for a minimum of 72 hours before testing. . 174 Along with preparing each specimen, a concrete beam was cast and FRP was applied to test the 175 pull-off strength of the FRP-concrete interface. To have a quality control of the bond strength of 176 177 the FRP-concrete interface, the standard pull-off tests were carried out by using the Dyna Z16 pull-off tester. The test follows the requirements of ASTM D7522 [33]. Before the pull-off test, 178 179 several 2 in. diameter cores were cut by a core drill, then the 2 in. diameter aluminum disks were 180 attached onto the FRP sheets by high strength epoxy, with manufacture tested strength of 1500 psi. When testing, the disk was attached to the pull-off tester and the pull-off load was applied by 181 the manual crank. The ultimate load was captured by the load indicator and used to calculate the 182 pull-off strength. The pull-off strength, σ_p shall be at least 1.4 MPa [1]. Details of the respective 183

material properties of steel and FRP are presented in Table 1, where E_{ls} and E_{ts} are the steel modulus of Elasticity in *l* and *t* directions, respectively; and E_f are the modulus of elasticity of steel and FRP, respectively; ρ_t and ρ_l are the steel reinforcement ratios in *l* and *t* directions, respectively; and f_v is the yielding strength of steel.

188 Loading Method and Instrumentation

189 Proportionally applied tensile load (horizontal σ_1) and compressive forces (vertical σ_2) were used to simulate a pure shear loading condition in the experimental test. As shown in Fig. 4, 190 191 the reference *l-t* coordinate system represents the directions of longitudinal and transversal 192 reinforcements. The reference 1-2 coordinate system represents the directions of the principal 193 compressive stress (2-axis) and tensile stress (1-axis). Testing initially started using load control 194 with increments of 1 kN/min. up to first cracking and then switched to displacement control with the increment of strain in the horizontal direction set to 0.0001 (mm/mm)/min until the 195 196 specimen failed.

197 The average (smeared) strains in the horizontal, vertical, and diagonal directions were measured by a total of 14 Linear Variable Differential Transformers (LVDTs) attached on both sides of the 198 199 panel specimen. With the stable reading from LVDTs, the stress-strain curves of concrete panels in the post peak branches were reliably monitored. On the North side, the panel specimen was 200 instrumented symmetrically by 10 LVDTs. Four of the LVDTs were aligned horizontally, and 201 another set of 4 LVDTs were aligned vertically, and each one of the remaining two was aligned 202 along a diagonal direction as shown in Fig. 5a. On the south side of the specimen, four LVDTs 203 were used: two in horizontal direction and two in vertical direction (Fig. 5b). The gage length for 204 205 horizontal and vertical LVDTs was 800 mm, and gage length for diagonal LVDTs was 1,130 206 mm.

The local strains on steel rebar and FRP sheets for each panel specimen were measured by a total of 10 strain gauges. The position of strain gauges on steel rebar and FRP sheets are shown in Fig. 6 and Fig. 7, respectively. It should be noted that the strain gauges on steel and FRP were located at the same location.

A digital image correlation (DIC) system was used to obtain the displacement and deformation field on the south side of the specimen. Through this DIC-based non-contact measurement system, the crack spacing and crack width of the specimens were captured in real time. Load was measured by the load cells installed on each hydraulic actuator.

215

216 GENERAL BEHAVIOR OF TEST PANELS

The specimens were subjected to pure shear loads in the *l-t* coordinates, as shown previously in Fig. 4. The peak stresses and strains for all the test panels are listed in Table 2. The subscript "m" indicates the load stresses at the peak shear stress and the subscript "0" indicates the strains that are measured at the peak shear stress.

The shear stress, τ_{lt} , can be calculated in terms of the principle stress from Eq. (1) and the shear strain, γ_{lt} , is determined form Eq. (2) as follows:

223
$$\tau_{lt} = \frac{1}{2} \left(\sigma_1 - \sigma_2 \right) \tag{1}$$

$$224 \qquad \gamma_{lt} = \varepsilon_1 - \varepsilon_2 \tag{2}$$

where σ_1 and σ_2 are the average horizontal tensile and vertical compressive stresses, respectively; ε_1 and ε_2 are the average strains measured from LVDTs in horizontal and vertical directions, respectively.

228 Effect of FRP Stiffness on the Shear Behavior

To study the shear behavior of FRP-strengthened RC members and to investigate the 229 230 effect of FRP stiffness, panels with same steel reinforcements in l and t directions, but different FRP reinforcement ratios are tested. The application of FRP in the *t*-direction results in an 231 increase of effective reinforcement ratio in that direction. The effective reinforcement ratio is 232 defined as the contribution of transverse steel and FRP reinforcement ratio in the shear gain in t 233 234 direction. Therefore, a different behavior is expected to be observed. To compare the behavior of panels, the shear stress-strain curves of panels series P4-FW, with the same steel reinforcement 235 ratio in l and t directions ($\rho_l = \rho_t = 0.76\%$) and different FRP reinforcement ratios (FRP 236 Stiffness) fully wrapped, are shown in Fig. 8. It can be observed that with the increase of FRP 237 238 stiffness, the shear strength of panels increases. The maximum shear strength of test panels P4-025-FW, P4-040-FW, and P4-080-FW were 4.2 MPa, 5.6 MPa, and 6.3 MPa, respectively. With 239 240 the increase of FRP stiffness, the stiffness of strengthening system increases and the contribution of FRP reinforcement to shear capacity will increase; therefore, the shear strength of panels 241 increases. The presence of FRP sheets along the transverse direction delays the yielding of steel 242 243 rebar in the *t*-direction. Therefore, the rebar in the longitudinal direction will yield sooner compared to the rebar in the transverse direction. In other words, the rebar in l and t directions 244 will not yield at the same time as in panel REF-P4. 245

In order to compare the behavior of panels, the relationships between the shear stress and average strain in longitudinal and transverse directions of panels series P4-FW are shown in Fig. 8. Panel REF-P4 is reinforced with equal amount of steel in *l* and *t* directions. Due to symmetry of the loading and the reinforcements, the average strain in the *l*-direction, ε_l , equals the average strain in the *t*-direction, ε_l . Therefore, the steel in both directions approximately yielded at the same time. Also, the inclination of cracks in this case coincides with the direction 252 of principal compressive stress. Therefore, the interlocking action of aggregates between concrete struts vanishes. As shown in Fig. 9, the measured strains in the two directions 253 for panel REF-P4 are very close to each other from the beginning of testing up to failure of the 254 panel. Panels in series P4-FW were reinforced with equal amount of steel in l and t directions 255 $(\rho_l = \rho_t = 0.76\%)$. However, they were strengthened with different FRP reinforcement ratios 256 along the t-direction. Therefore, the presence of FRP sheets resulted in the increase of the 257 effective reinforcement ratio in transverse (t) direction and the steel in *l*-direction yielded sooner 258 than the steel in *t*-direction (Fig. 9). After steel yielded in both l and t directions, the average 259 260 strain in longitudinal direction ε_l increased rapidly compared to the average strain in transverse 261 direction ε_t . The FRP sheets aligned in the *t*-direction prevented the rapid increase of strain along the transverse direction. It is observed from Fig. 9 that with the increase of FRP stiffness, the 262 263 difference in steel strains in l and t directions increases. For instance, in panel P4-025-FW, ε_l at failure is 20% more than ε_t . With the increase of FRP reinforcement ratio this difference 264 increases. In panels P4-040-FW ($\rho_f = 0.87\%$) and P4-080-FW ($\rho_f = 1.74\%$), ε_l at failure is greater 265 266 than ε_t by 53% and 60%, respectively. With the increase of FRP reinforcement ratio (FRP stiffness) in the transverse direction, the effective reinforcement ratio in the *t*-direction increases. 267 268 This will result in increase of deformation in the *l*-direction which is less reinforced.

269 Effect of Wrapping Scheme on the Shear Behavior

Wrapping scheme affects the confinement effect of the FRP sheets and the potential for debonding. The effect of wrapping scheme on the shear stress-strain curves of the panels are shown in Fig. 10 and Fig. 11. Test results of panels with the same steel and FRP reinforcement ratios ($\rho_s = 0.76\%$, $\rho_f = 0.87\%$), but different wrapping schemes are shown in Fig. 10. The behavior of panel P4-040-SB was similar to panel P4-040-FA up to failure. However, the shear

capacity of panel P4-040-FA was 22% greater than panel P4-040-SB. Panel P4-040-SB failed 275 276 due to premature debonding of FRP sheets. Panel P4-040-FW showed a different behavior compared to the other two panels. The stiffness of the panel P4-040-FW after cracking was much 277 278 higher compared to P4-040-FA and P4-040-SB panels, which showed the same post cracking behavior. This was due to a better bond between the FRP sheets and concrete substrate after 279 280 cracking of concrete in panel P4-040-FW, which resulted in the increase of the overall stiffness. The shear capacity of panel P4-040-FW was 6% and 30% higher than panels P4-040-FA and P4-281 040-SB, respectively. In Fig. 11, test results of panels with the same steel and FRP reinforcement 282 ratios ($\rho_s = 0.76\%$, $\rho_f = 0.43\%$), but different wrapping schemes are compared. Although it was 283 expected that the two panels show a similar behavior up to failure, the shear capacity of panel 284 P4-025-FA was 15% higher than panel P4-025-FW. This difference was due to a lower concrete 285 compressive strength, f_c' , of panel P4-025-FW (45 MPa) compared to panel P4-025-FA (52 286 MPa). The contributions of steel and FRP on the overall shear capacity of the two members were 287 288 similar. However, the lower concrete compressive strength resulted in a lower contribution of concrete on the overall shear capacity of panel P4-025-FW therefore, a lower overall shear 289 capacity was observed compared to panel P4-025-FA. 290

For design purposes, the strengthening scheme is selected based on factors such as the accessibility of the member and the required amount of increase in shear capacity. The recommended wrapping scheme is fully wrap for shear strengthening of the member whenever it is possible. However, in most situations, a U-wrap with FRP anchor is the only economical and practical economical and practical wrapping scheme.

296 Effect of Transverse Steel Reinforcement on the Shear Behavior

297 The panels were reinforced with two levels of transverse steel reinforcement ratios, $\rho_t = 0.43\%$ and 0.76%. A low transverse reinforcement ratio (using No. 3 rebar) was chosen to 298 simulate a beam which is lightly reinforced, and a high transverse reinforcement was chosen to 299 300 simulate a beam which is heavily reinforced. The shear stress-strain curves of panels with the same FRP reinforcement ratio and wrappings scheme, but different transverse reinforcement 301 302 ratios are compared in Figs. 12 and 13. The shear stress-strain curves of panels P3-040-FW and P4-040-FW are compared in Fig. 12. The panels are reinforced with the same FRP reinforcement 303 ratio ($\rho_f = 0.87\%$) and the wrapping scheme is fully wrap. It can be observed that panel P4-040-304 305 FW had 25% higher shear strength compared to panel P3-040-FW, due to a higher transverse reinforcement ratio. 306

In Fig. 13, the shear stress-strain curves of panels P3-025-FW and P4-025-FW are compared. The panels are reinforced with the same FRP reinforcement ratio ($\rho_f = 0.54\%$) and the wrapping scheme is fully wrap. The two panels showed similar behavior in terms of maximum shear stress. It was expected that panel P4-025-FW show higher shear strength compared to panel P3-025-FW. Although, panel P4-025-FW had a lower concrete compressive strength ($f_c' = 45$ MPa) compared to panel P3-025-FW ($f_c' = 51$ MPa), panel P3-025-FW reached its peak strength at a lower shear stress and strain compared to panel P4-025-FW.

In Fig. 14, the strain of FRP sheets and transverse steel, measured using strain gauges, for panels P4-040-FW and P3-040-FW are compared at same load levels. It is observed that both the external FRP reinforcement and the transverse steel reinforcement did not contribute to the loadcarrying capacity in the initial stage of loading. This contribution initiated and became effective after the first cracking occurred. In panel P4-040-FW it can be observed that before reaching the tensile strength of concrete, the strains in FRP and steel were very small and less than the 320 maximum tensile strain of concrete. Once cracking occurred, strains on both steel and FRP 321 increased suddenly. Before yielding of the steel, FRP strain was higher than the steel strain at the same load level. After steel yielded, the steel strain rapidly increased compared to FRP strain. 322 323 The same behavior was observed for panel P3-040-FW. In panel P3-040-FW immediately after the steel yielded, since the transverse steel reinforcement ratio was low, the steel strain increased 324 325 rapidly and became higher than FRP strain at the same shear stress level. In panel P4-040-FW, immediately after steel yielded, the transverse steel strain did not get bigger than the strain of 326 FRP. This was due to a larger steel reinforcement ratio compared to panel P3-040-FW, and due 327 328 to the different yield behavior of rebar Nos. 3 and 4 compared to each other. The strains in the FRP and the transverse steel are different, even at the same locations, because the strain on the 329 fiber sheets increases drastically near the crack, due to the bond between the FRP and the 330 concrete substrate. Also, the crack widths are smaller at the rebar location and increase at the 331 surface. Addition of the FRP sheets delayed the contribution of transverse steel to the load 332 carrying capacity of the specimen. The results clearly show that the effect of externally bonded 333 334 FRP sheets preserves the integrity of internal transverse steel reinforcements. The effectiveness of the contribution of FRP sheets to the shear gain highly depends on the amount of internal 335 336 shear steel reinforcement. However, the design guidelines have not yet considered the effect of transverse steel reinforcement and the contribution of FRP on the overall shear response (V_f) in 337 their formulations. 338

339 Failure Modes Associated with FRP-Strengthened RC Panels

In RC members subjected to compression-tension biaxial stresses, various types of shear failure
occur; such as diagonal cracking, splitting, shear-compression failure, and web crushing[15].
These all involve cracking and crushing of concrete in a biaxial stress state. In FRP-strengthened

RC members, additional failure modes were observed. The two main failure modes related to the 343 FRP strengthening which were observed in test panels are FRP rupture and FRP debonding. In 344 the case of FRP rupture, the fibers reached their ultimate strain value and fracture at the point of 345 346 maximum stress. In the FRP debonding failure mode, the strain of FRP at ultimate stage were considerably lower than the rupture strain. The failure mode of FRP rupture is similar to shear 347 348 tension failure in conventional RC beams where vertical flexural cracks originates from the tension face. Widening of the diagonal crack eventually leads to failure involving tearing of the 349 FRP along a line corresponding to the diagonal shear crack in the concrete. Available 350 351 experimental data in literature shows that all of the test specimens with FRP sheets bonded on sides only, and many bonded with U-wrap, failed by debonding of the FRP from the concrete 352 353 substrate.

354 The main failure modes associated to panel specimens are shown in Table 3. Fig. 15 shows the main failure modes observed in panel specimens. In panels P3-FW and P4-FW series, which 355 were strengthened with fully wrap scheme, the main observed failure modes were FRP rupture 356 followed by crushing of concrete (Fig. 15a), except for panel P4-080-FW which failed by 357 concrete crushing prior to FRP failure (Fig. 15b). Concrete crushing occurred due to high 358 359 principal compressive stresses in the region between induced cracks. This failure mode is normally associated with high amounts of transverse reinforcement but may also be critical in 360 beam members with thin webs. Panel P4-080-FW, which was strengthened with a higher FRP 361 362 reinforcement ratio compared to other panels ($\rho_f = 1.74\%$), had a different failure mode. The governing failure mode in this panel was concrete crushing. The increase in amount of FRP 363 reinforcement (increase in thickness of FRP sheets) resulted in decrease of active bond length, 364 365 that is the length which the majority of bond is maintained. Therefore, the effective strain in the

FRP sheets decreases and ultimately, FRP sheets did not reach their expected capacity up to theirtensile strength before rupture and the panel failed due to concrete crushing.

368 In panels P4-FA series, which were strengthened using U-wrap with FRP anchor wrapping 369 scheme, a mixed failure mode was observed. In panel P4-025-FA, anchorage failure was observed on the south side of the panel while on the north side FRP rupture of FRP sheets was 370 371 seen (Fig. 15c). In panel, P4-040-FA, FRP anchors did not show any sign of failure and the 372 failure mode of the panel was governed by rupture of FRP sheets. This could be associated with 373 different bond between FRP and concrete substrate on both sides of the panel. On the south side 374 of the panel, the FRP anchors engaged in the shear resistance once the FRP sheets debonded from the concrete surface and failed at their ultimate load carrying capacity. 375

376 Panel P4-040-SB, was strengthened with the side bond wrapping scheme. Once the concrete cracked, local debonding of FRP sheets initiated from the concrete substrate and the panel 377 ultimately failed by debonding of all FRP sheets at a lower load level compared to other 378 379 strengthened panels (Fig. 15d). In this panel, the FRP was not able to utilize its full tensile capacity and therefore, debonding of FRP sheets at lower strain levels occurred, which lowered 380 the efficiency of the strengthening system. In this mode of failure, once the FRP starts to peel 381 382 off, the beam will fail very quickly in a brittle process. The bond strength between FRP and concrete thus plays the key role in this mode. 383

It should be noted that the strain distribution in the FRP along a shear crack is non-uniform because the width of the critical shear crack changes from the lower end to the upper crack tip [34]. This leads to a non-uniform strain distribution in the FRP because the strain anywhere in the FRP intersected by the crack is closely related to the width of the crack at that location. Since the FRP sheets are linear elastic material up to their rupture, the stress in the FRP is also nonuniform along the shear crack. Combined with the brittle behavior of FRP, this means that at any instant in the failure process, only the most highly stressed part of the FRP is at its full tensile capacity.

392 In practice, for design of FRP strengthened RC members, the primary failure modes are selected for each element. Each failure mode is classified in terms of the type of failure it 393 394 represents and the seriousness of damage it causes [35]. A primary failure mode should be 395 considered followed by other failure modes and their degree of undesirability. For instance, in an RC beam strengthened with FRP, the most desirable failure mode is flexural concrete crushing 396 397 and the least desirable is debonding. For shear strengthening, the failure modes and bond of FRP to concrete substrate remain the focus of many research work. There are several verities in 398 failure modes in FRP strengthened systems which can govern the strength [1]. While most of the 399 400 failure modes have been identified by researchers, more accurate methods are still required. Throughout the design procedures, significant limitations on the strain and stress level achieved 401 in the FRP material are imposed to conservatively account for debonding failure modes. More 402 thorough design guidelines should be incorporated in codes for predicting debonding and other 403 404 failure modes.

405

406 CRACK CHARACTERISTICS

The evolution of strains and deformations on FRP and concrete have been measured with a DIC system and its tracking method. This method has been widely used for measurements in RC and masonry members [36-38]. In order to study the crack characteristics on panel specimens, the DIC system was used on the south side of the specimen. The DIC system will generate contour plots of the axial and lateral surface deformations of the panels, which will help determine theexact pattern around and in between the FRP sheets [19].

413 The crack characteristics including crack width, spacing, and amount were measured by the DIC 414 system and are presented in the following sections. In Fig. 16, the strain field in the direction of applied horizontal load ε_x of a specimen at a specific load level is shown using color gradient. 415 416 The cracks are identified at locations with sudden increase in strain. The crack widths are measured by assigning two points near the cracks and continuously measuring their distances. It 417 should be mentioned that due to accessibility issue, the DIC system was not used for specimen 418 P4-025-FW, P4-040-FA, and P4-040-SB. The integrity of a structure is affected by the crack 419 420 characteristics and therefore careful considerations should be made [39].

421 Crack Spacing

422 The stabilized cracking phase is reached when the crack spacing between two existing cracks are too small for a new crack to develop in between. The crack spacing was determined at 423 424 the last phase of the testing, since it is closest to the stabilized cracking stage. In Table 4, 425 experimental measurements of the average crack spacing, S_{rm} , maximum crack spacing, $S_{r,max}$, and minimum crack spacing, $S_{r,min}$, in panel specimens subjected to shear are presented. The 426 427 experimental average crack spacing is defined by the measurement of the spacing between the adjacent cracks on the panel at different heights and averaging for the entire specimen at the 428 429 stabilized cracking stage. The maximum and minimum crack spacing is defined based on the maximum and minimum measured crack spacing at the stabilized cracking stage throughout the 430 specimen, respectively. In Fig. 17, ratios of maximum and minimum to average crack spacing 431 versus average crack spacing in shear tests of panel specimens are presented. The mean value of 432 433 the ratio $S_{r,max}/S_{rm}$ and $S_{r,min}/S_{rm}$ are shown with horizontal dashed lines. In EC2-04 [40] a value

of 1.7 is assumed for the ratio of the maximum to average crack spacing for RC structures; which is observed to be higher compared to the experimental value of $S_{r,max}/S_{rm}$ that equals 1.47 for FRP-strengthened RC panels.

437 Crack Width

Using the DIC system the crack widths were measured continuously during the test. It was 438 observed that in FRP-strengthened RC members; average crack widths were generally smaller 439 440 than for un-strengthened members at the same shear strain level (Fig. 18), due to the additional bond action developing at the FRP-concrete interface. Although, the number of cracks did not 441 increase significantly in strengthened members as shown in Table 4., the crack widths decreased 442 443 compared to RC panels. The thicker FRP (1.0 mm) provided better crack control compared to the thinner FRP (0.6 mm). Similar results were observed for P4-FW and P4-FA series. As shown in 444 Fig. 19, in panels strengthened with FRP, average crack widths were generally smaller than un-445 strengthened RC panels at the same shear strain level. For panels P4-FW series, with the increase 446 of FRP reinforcement ratio, the crack widths did not change significantly at lower shear strains. 447 In general. specimens strengthened with FRP exhibited a greater tension stiffening effect 448 compared to RC specimens. The contribution of the concrete in shear affects the overall stiffness 449 450 of the FRP strengthened RC members after cracking. Therefore, the crack spacing and crack 451 width are affected at service load level. Wrapping scheme and FRP reinforcement ratio affect the bond behavior of steel-concrete and, FRP-concrete interface in FRP strengthened RC members. 452 453 This will result in a different crack pattern in such members compared to RC members.

454 MATHEMATICAL MODELING OF SMEARED STRESS-STRAIN CURVES OF FRP 455 STRENGTHENED RC IN COMPRESSION

The softening coefficient is the most important parameter affecting the smeared 456 stress-strain relationships of concrete in compression. Several researchers have 457 investigated the softening coefficient in RC members and determined that the most 458 effective parameters are: concrete compressive strength, f'_c , the uniaxial tensile 459 strain, $\bar{\varepsilon}_1$, and the deviation angle, β [13,14]. In case of FRP strengthened RC 460 members, the FRP sheets also have significant effect on the softening of concrete 461 [16]. The smeared constitutive relationship of concrete compressive stress, σ_2^c , 462 versus the uniaxial compressive strain, $\overline{\varepsilon_2}$, in the Softened Membrane Model, shown 463 464 in Fig. 20, is given as:

465
$$\sigma_2^c = \zeta f_c' \left[2 \left(\frac{\overline{\varepsilon}_2}{\zeta \varepsilon_0} \right) - \left(\frac{\overline{\varepsilon}_2}{\zeta \varepsilon_0} \right)^2 \right] \quad \text{when } \frac{\overline{\varepsilon}_2}{\zeta \varepsilon_0} \le 1 \text{ and}$$
 (2)

466
$$\sigma_{2}^{c} = \zeta f_{c}^{\prime} \left[1 - \left(\frac{\left(\frac{\overline{\varepsilon}_{2}}{\zeta \varepsilon_{0}} \right) - 1}{\left(\frac{4}{\zeta} \right) - 1} \right)^{2} \right] \quad \text{when } \frac{\overline{\varepsilon}_{2}}{\zeta \varepsilon_{0}} > 1$$
(3)

467 The softening coefficient in Eq. 2 and 3 is expressed as the product of the function of concrete 468 compressive strength, f_c' , uniaxial tensile strain, $\bar{\varepsilon}_1$, and deviation angle, β , as

469

470
$$\zeta = f(f_c)f(\bar{\varepsilon}_1)f(\beta)$$
, where (4)

471
$$f(f_c) = \frac{5.8}{\sqrt{f_c}} \le 0.9$$
 (5)

$$472 \qquad f(\overline{\varepsilon}_1) = \frac{1}{\sqrt{1 + 400\overline{\varepsilon}_1}},\tag{6}$$

$$473 \qquad f(\beta) = 1 - \frac{|\beta|}{24^{\circ}} \tag{7}$$

474 Previous researches showed that in FRP strengthened RC members, FRP reinforcement has

475 significant effect on the softening coefficient [9,16]. Therefore, in FRP strengthened members476 the softening coefficient is expressed as

477
$$\zeta_{FRP} = f(f_c')f(\bar{\varepsilon}_1)f(\beta)f(FRP)$$
(8)

where, the first three terms on the right-hand side of Eq. (8) are the same as the
softening coefficient for RC, Eq`ns. (5) to (7), proposed by other researchers at
University of Houston [14, 18,41]. The fourth term is proposed by Yang [9] as

481
$$f(FRP) = 1 + 0.0076\sqrt{\rho_f E_f}$$
 (9)

In the proposed equation, $\rho_f E_f$ were adopted to account for the area of the concrete. It should be noticed that the proposed equation converges to the result of RC when $\rho_f E_f$ equals to zero, in which case f (FRP) equals to 1 and the expression will be the same as for RC.

To express the smeared stress-strain curves of the concrete in compression in FRP strengthened RC members, the same parabolic equation, Eq. (2) and (3), is used. The softening coefficient is derived from Eq. (8). The experimental results of FRP strengthened RC panels subjected to shear will be used to validate the function of deviation angle, β , in the softening equation of RC members for FRP strengthened RC members.

492 The angle β is the deviation angle between *r*-*d* coordinate and 1-2 coordinate, 493 equal to α_r - α_1 (Fig. 21). β is a function of the strain state, and can be expressed in 494 terms of the three strains, ε_1 , ε_2 , and γ_{12} using the compatibility equations as

495
$$\beta = \frac{1}{2} \tan^{-1} \left[\frac{\gamma_{12}}{\varepsilon_1 - \varepsilon_2} \right]$$
(10)

496

The deviation angle, β , is equal to zero if the element is reinforced with the 497 same amounts of steel bars in *l* and *t* directions and subjected to pure shear loading, 498 e.g., REF-P4. The values of β and $f(\beta)$ from FRP strengthened RC panel tests are 499 listed in Table 5. The concrete compressive strength, f'_c , and the uniaxial tensile 500 strain, $\bar{\epsilon_1}$, of the concrete in the 1-direction at the peak point of the shear stress-501 strain curve for each panel are listed in Table 5. The values of $f(f_c)$, $f(\bar{\epsilon}_1)$ and 502 f(FRP) are calculated using Eqns. (5, 6, and 9), respectively. Dividing the 503 experimental value of the softening coefficient, ζ_{exp} , by $f(f_c)$, $f(\bar{\varepsilon}_1)$, and f(FRP) the 504 experimental $f(\beta)$ for each panel is obtained and listed in Table 5. The value of β 505 for each panel is calculated using Eq. (10). 506

According to the data in Table 5, the $f(\beta)_{exp}$ versus β relationships for the FRP strengthened RC panels is plotted in Fig. 20 along with the data for the reinforced concrete panel tests [18, 41]. Also, the straight line defined by Eq. (7) is plotted in Fig. 20.

The $f(\beta)_{exp}$ versus β relationships for FRP strengthened RC panels show a different trend than that for RC panels. Therefore, Eq. (7) should be modified before it can be applied to FRP strengthened RC members. Similar to RC members, the relationship between β and $f(\beta)$ is approximately linear. A regression analysis of the FRP strengthened RC data is performed to develop the new function of the deviation angle, β , in the softening coefficient of FRP strengthened RC members as

517
$$f_{FRP}\left(\beta\right) = \left(1 - \frac{|\beta|}{16^{\circ}}\right)$$
(11)

The effect of deviation angle, β , on the softening coefficient in FRP strengthened RC members is more complicated than that in RC members. The presence of FRP along the transversal direction increases the stiffness in that direction and therefore, increases the difference in the stiffness in the *l* and *t* directions. Thus, the deviation angle increases followed by a decrease in the softening coefficient. The new function of the deviation angle, $f_{FRP}(\beta)$, has been used for the softening equation of the new softened membrane model for FRP strengthened RC members presented elsewhere [42].

525

526 CONCLUSIONS

In order to evaluate the shear behavior of FRP-strengthened RC members and investigate 527 the main factors which influence its behavior, panel testing was carried out. Other testing 528 529 techniques such as testing beam with various a/d ratios cannot predict the true pure shear behavior due to the presence of flexural and other non-shear related effects that cannot be filtered 530 out. For this purpose, full-scale tests on 8 FRP-strengthened RC panels and 2 RC panels were 531 conducted. It should be noted that in this research the initial stresses existing in members prior to 532 strengthening have been considered. The effects of different parameters on the true shear 533 534 behavior of FRP-strengthened RC members were investigated. The following conclusions can be made: 535

1) It was found that the application of FRP sheets enhanced the overall shear behavior of RC
panels. However, ductility of the specimens was reduced due to the failure modes associated
with the strengthening system such as FRP rupture and FRP debonding.

2) The presence of FRP sheets resulted in the increase of the effective reinforcement ratio in transverse direction, and the steel in the *l*-direction yielded sooner than the steel in the *t*direction. After the steel yielded in both *l* and *t* directions, the strain in the longitudinal direction, ε_l , increased rapidly compared to the strain in the transverse direction, ε_t . The FRP sheets aligned in the *t*-direction prevented the rapid increase of strain along the transverse direction. Also, with the increase of FRP reinforcement ratio, the difference in steel strains in *l* and *t* directions increased.

546

547 3) In this research, many failure modes of FRP strengthened RC members have been identified. While some of these failure modes are similar to those of RC members, others are unique to FRP 548 549 strengthened members. The transfer of stresses from concrete to FRP sheets is a critical parameter in FRP strengthening since it is likely to cause undesirable premature and brittle 550 failures. The two main failure modes observed in the tests were rupture of FRP sheets at the 551 552 ultimate strain following the yielding of internal steel reinforcement and debonding of FRP 553 sheets in a brittle manner with a thin layer of concrete residue attached to the delaminated FRP sheet. It was observed that wrapping schemes played a critical role in determining the failure 554 mode of the strengthened member. While all specimen with side bond wrapping scheme failed 555 by premature FRP debonding, most specimens with U-wrap plus FRP anchor and fully wrap 556 557 failed by concrete crushing followed by rupture of FRP.

4) It was observed that the magnitude of increased shear capacity associated with the application of FRP sheets depend not only upon the amount of FRP reinforcement that is being used, but also on the amount of internal shear reinforcement. The increase in transverse steel reinforcement resulted in a significant decrease in the shear gain due to FRP strengthening. There exists a high

562 interaction between the components of the strengthening system, specifically steel and FRP 563 reinforcement, when subjected to shear. The strains in the FRP sheets and the internal transverse steel reinforcement were observed to be different at the same locations in the test region. This 564 was due to the strain on the fiber sheets increasing drastically near the cracks, due to the bond 565 between the FRP and the concrete substrate. With increase in the internal shear reinforcement 566 567 ratio, the crack pattern becomes relevantly more distributed along the member and therefore, the available effective bond length decreases. This ultimately leads to decrease in the bond force and 568 decrease in the effectiveness of the FRP strengthening scheme. It should be noted that the 569 570 external FRP reinforcement does not prevent the internal transverse steel reinforcement from yielding rather delays it. 571

572 5) Test results showed that applying FRP reinforcement significantly changed the crack width 573 and spacing of the RC member. The contribution of the concrete in shear affects the overall stiffness of the FRP strengthened RC members after cracking. Therefore, the crack spacing, and 574 crack width are affected at service load level. Different wrapping schemes and external FRP 575 reinforcement ratio affects the bond behavior of steel-concrete and also FRP-concrete interface 576 577 in FRP strengthened members. This will result in different crack patter in in such members 578 compared to RC members. Average crack widths were generally smaller than for unstrengthened RC members at the same smeared strain level due to the additional bond action 579 developing at the FRP-concrete interface which further reduced the crack spacing. 580

6) The softening coefficient is the most important parameter affecting the smeared stress-strain relationships of concrete in compression. Previous research studies showed that in addition to effective parameters in the softening coefficient of RC members, FRP sheets also have significant effect on the softening of concrete in FRP strengthened RC members. In this paper, a

new softening coefficient for FRP strengthened reinforced concrete in compression is proposed based on panel tests. The new softening coefficient includes the modified deviation angle factor in terms of the deviation angle β . The presence of FRP along the transversal direction increases the stiffness in that direction and therefore, increases the difference in the stiffness in the *l* and *t* directions. Thus, the deviation angle increases followed by a decrease in the softening coefficient. The new function of the deviation angle was implemented in the softening equation of the new softened membrane model for FRP strengthened RC members presented elsewhere.

592

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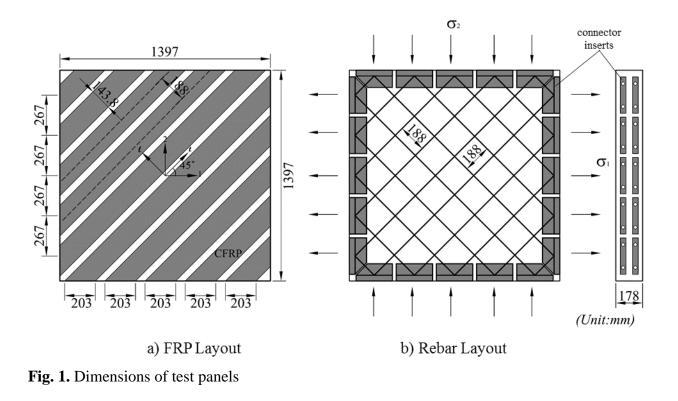
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- behavior of FRP-strengthened RC members. Eng. Struct., 153(2017) 239-253.
- 698 **Figure Captions**
- **Fig. 1.** Dimensions of test panels

- Fig. 2. Layout and wrapping method of FRP sheets, a) FRP layout, b) Fully wrap, and c) Sidebond wrapping scheme cross sections
- **Fig. 3.** U-Wrap with FRP anchor details
- **Fig. 4.** Proportional loading of panel in 1-2 directions
- **Fig. 5.** LVDT arrangement for the panel specimens
- **Fig. 6.** Strain gauge layout on steel rebar of panel specimens
- **Fig. 7.** Strain gauge layout on FRP sheets of panel specimens
- **Fig. 8.** Effect of FRP stiffness on shear stress-shear strain curves of panels P4-FW series
- **Fig. 9.** Effect of FRP stiffness on $\tau_{lt} \varepsilon_l$ and $\tau_{lt} \varepsilon_t$ relationships of panels P4-FW series
- 709 Fig. 10. Shear stress-strain curves for specimens with different wrapping schemes (panels P4-
- 710 040 series)
- **Fig. 11.** Shear stress-strain comparison of wrapping scheme in panels P4-025 series
- **Fig. 12.** Shear stress-strain comparison of transverse steel reinforcement in panels 040-FW series
- **Fig.13.** Shear stress-strain comparison of transverse steel reinforcement in panels 025-FW series
- Fig. 14. Comparison of transverse steel strain and FRP of panels P4-040-FW and P3-040-FW
- **Fig. 15.** Different failure modes of panel specimens, a) FRP debonding, b) Concrete crushing, c)
- 716 FRP anchor failure, d) FRP rupture
- **Fig. 16.** Full strain field in the direction of applied load of specimen at a specific load level
- Fig. 17. Ratios of maximum and minimum to average crack spacing vs. average crack spacing inshear tests
- 720 Fig. 18. Crack width comparison of panel series P3-FW and REF-P3
- **Fig. 19.** Crack width comparison of panel series P4-FW and P4-FA



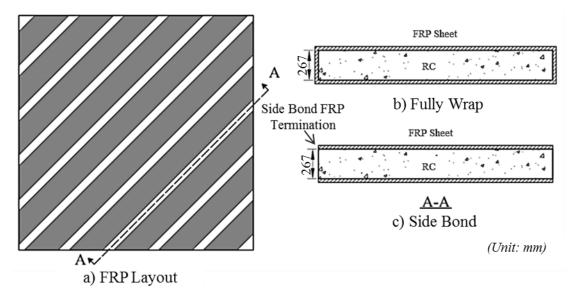


Fig. 2. Layout and wrapping method of FRP sheets, a) FRP layout, b) Fully wrap, and c) Side bond wrapping scheme cross sections

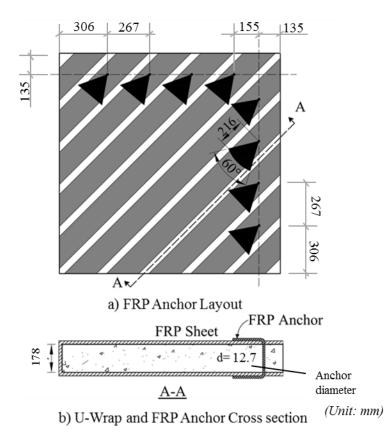


Fig. 3. U-Wrap with FRP anchor details

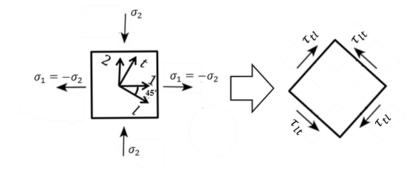


Fig. 4. Proportional loading of panel in 1-2 directions

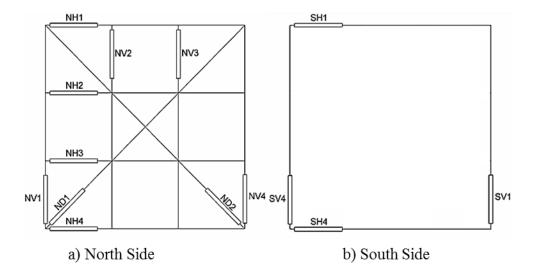
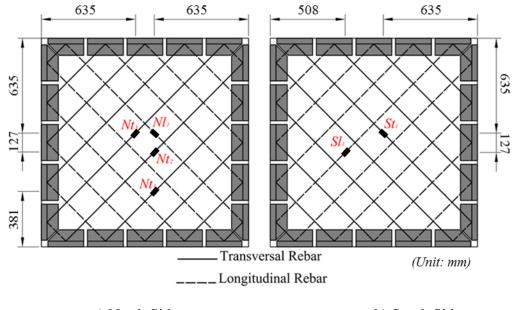


Fig. 5. LVDT arrangement for the panel specimens



a) North Side

b) South Side

Fig. 6. Strain gauge layout on steel rebar of panel specimens

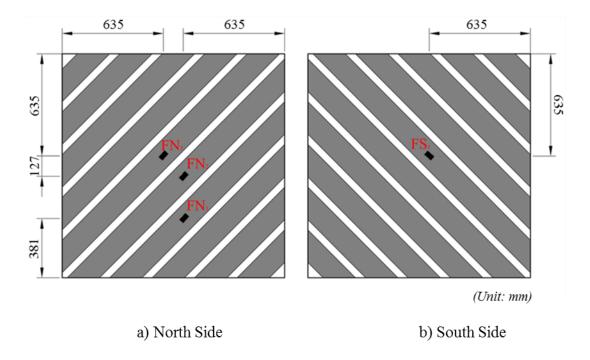


Fig. 7. Strain gauge layout on FRP sheets of panel specimens

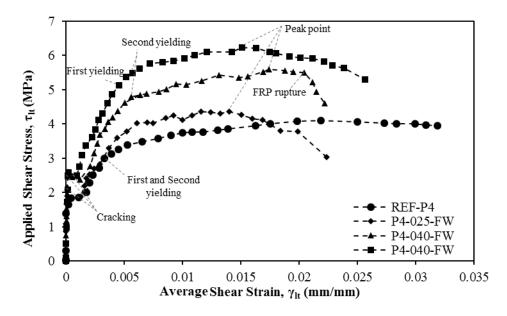


Fig. 8. Effect of FRP stiffness on shear stress-shear strain curves of panels P4-FW series

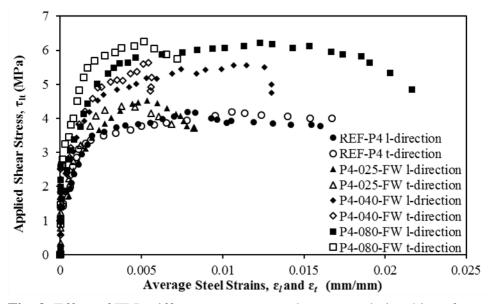


Fig. 9. Effect of FRP stiffness on $\tau_{lt} - \varepsilon_l$ and $\tau_{lt} - \varepsilon_t$ relationships of panels P4-FW series

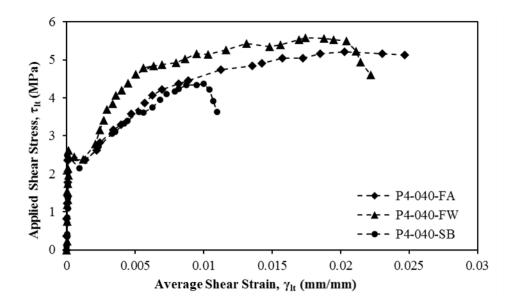


Fig. 10. Shear stress-strain curves for specimens with different wrapping schemes (panels P4-040 series)

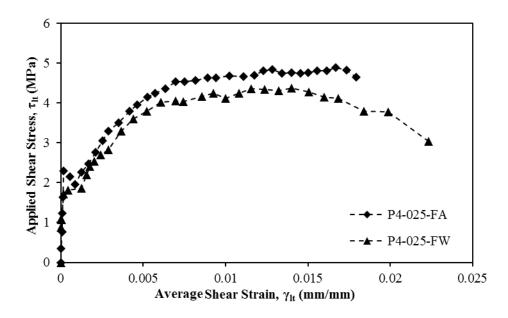


Fig. 11. Shear stress-strain comparison of wrapping scheme in panels P4-025 series

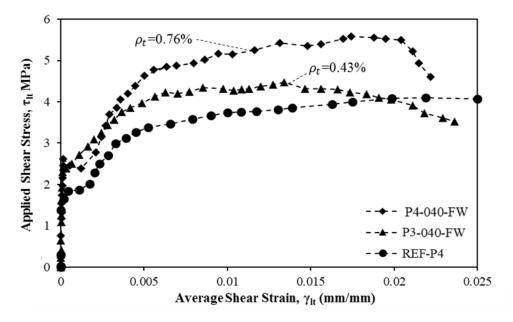


Fig. 12. Shear stress-strain comparison of transverse steel reinforcement in panels 040-FW series

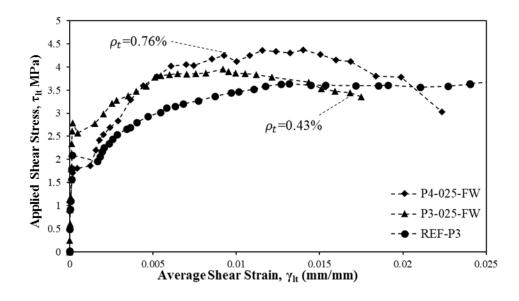


Fig.13. Shear stress-strain comparison of transverse steel reinforcement in panels 025-FW series

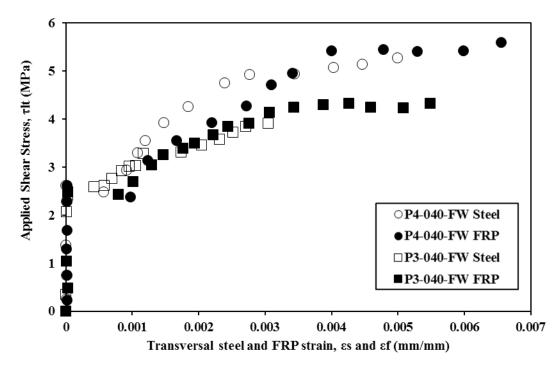


Fig. 14. Comparison of transverse steel strain and FRP of panels P4-040-FW and P3-040-FW

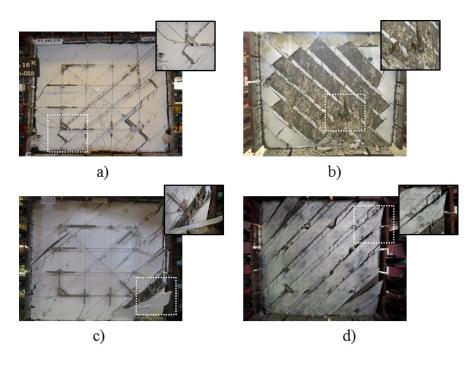


Fig. 15. Different failure modes of panel specimens, a) FRP debonding, b) Concrete crushing, c) FRP anchor failure, d) FRP rupture

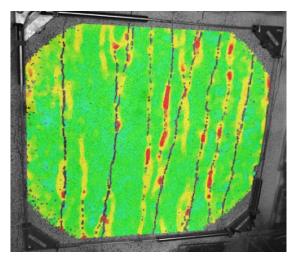


Fig. 16. Full strain field in the direction of applied load of specimen at a specific load level

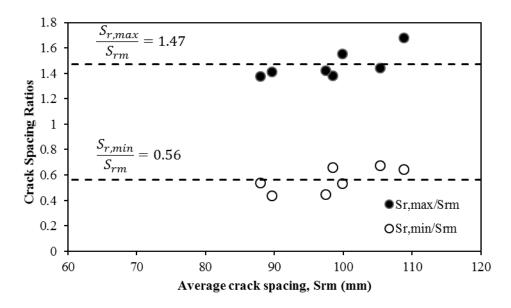


Fig. 17. Ratios of maximum and minimum to average crack spacing vs. average crack spacing in shear tests

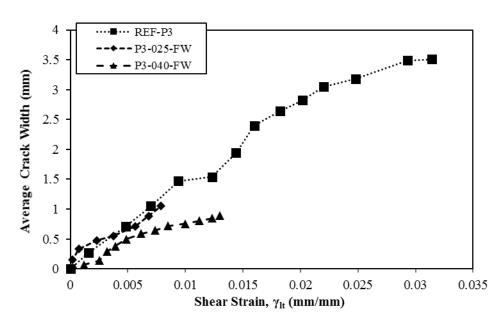


Fig. 18. Average crack width comparison of panel series P3-FW and REF-P3

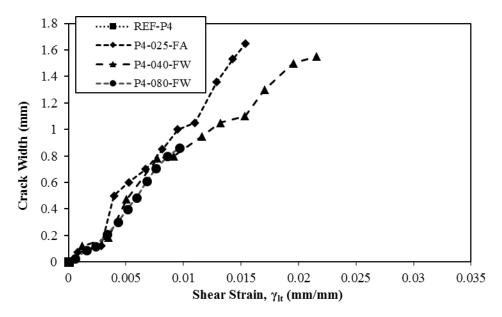
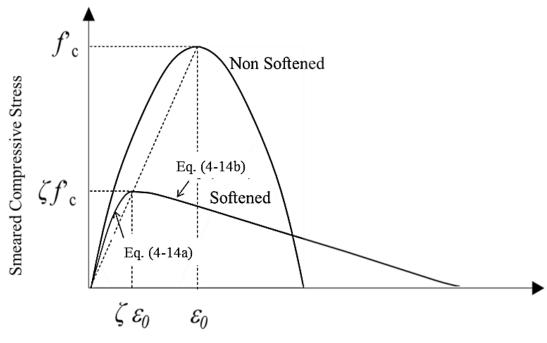


Fig. 19. Average crack width comparison of panel series P4-FW and P4-FA



Smeared Compressive Strain

Fig. 20. Monotonic Non-Softened and Softened Stress-Strain Curve [15]

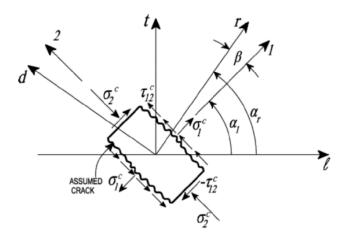


Fig. 21 Deviation Angle β [15]

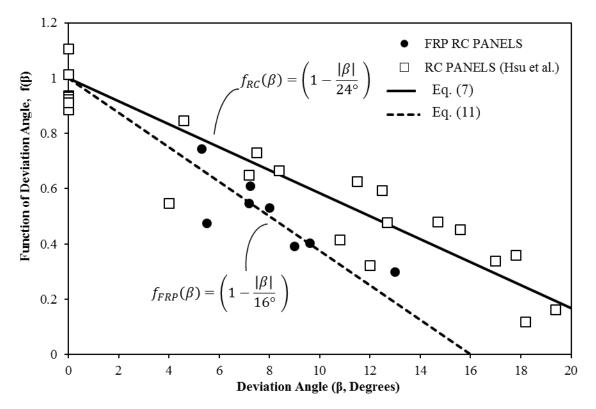


Fig. 22 $f(\beta)$ versus β Relationships for RC and FRP Strengthened RC Panels

Table 1. Principal variables of test panel and material properties

		Concrete	St	Steel in <i>l</i> direction			eel in <i>t</i> dire	FRP in t direction		
Series	Specimen Name	f'c (MPa)	ρ _l (%)	f _{ly} (MPa)	E _{ls} (MPa)	ρ _t (%)	f _{ty} (MPa)	E _{ts} (MPa)	ρ _f (%)	E _f (MPa)
	REF-P3	53	0.76	462	190000	0.43	459	188000	-	-
REF	REF-P4	52	0.76	462	190000	0.76	462	190000	-	-
	P3-025-FW	51	0.76	462	190000	0.43	459	188000	0.54	82700
P3-FW	P3-040-FW	50	0.76	462	190000	0.43	459	188000	0.87	72400
P4-FW	P4-025-FW	45	0.76	462	190000	0.76	462	190000	0.54	82700
	P4-040-FW	52	0.76	462	190000	0.76	462	190000	0.87	72400
	P4-080-FW	54	0.76	462	190000	0.76	462	190000	1.74	72400
P4-SB	P4-040-SB	44	0.76	462	190000	0.76	462	190000	0.87	72400
	P4-025-FA	52	0.76	462	190000	0.76	462	190000	0.54	82700
P4-FA	P4-040-FA	52	0.76	462	190000	0.76	462	190000	0.87	72400

Table 2. Applied stresses and corresponding measured strains at peak load stage

Series	Panel	σ _{2m} (MPa)	σ _{1m} (MPa)	τ _{ltm} (MPa)	ε ₂₀ (mm/mm)	E ₁₀ (mm/mm)	E _{l0} (mm/mm)	E _{t0} (mm/mm)	γ _{lt0} (mm/mm)
DEE	REF-P3	-3.6	3.3	3.5	-0.000113	0.0228	0.0073	0.0172	0.0229
REF	REF-P4	-4.1	4.1	4.1	-0.000147	0.0219	0.0085	0.0117	0.0220
D2 EW	P3-025-FW	-4.2	3.7	4.0	-0.000164	0.0108	0.00632	0.00429	0.1089
P3-FW	P3-040-FW	-4.7	4.1	4.4	-0.000241	0.0121	0.0059	0.0060	0.0122
	P4-025-FW	-4.0	4.4	4.2	-0.000265	0.0067	0.0037	0.0024	0.0070
P4-FW	P4-040-FW	-5.5	5.6	5.6	-0.000798	0.0166	0.0100	0.0050	0.0174
	P4-080-FW	-6.6	5.9	6.3	-0.000328	0.0165	0.0177	0.0065	0.0162
P4-SB	P4-040-SB	-3.9	4.7	4.3	-0.000114	0.0089	0.0047	0.0018	0.0091
	P4-025-FA	-5.1	4.8	4.9	-0.000233	0.0162	0.0098	0.0045	0.0164
P4-FA	P4-040-FA	-5.6	5.0	5.3	-0.000101	0.0187	0.0131	0.0042	0.0188

Table 3. Failure modes of test specimens

Panel	REF-P3	REF-P4	P3-025-FW	P3-040-FW	P4-025-FW	P4-040-FW	P4-080-FW	P4-040-SB	P4-025-FA	P4-040-FA
Failure Mode	Concrete crushing	Concrete crushing	FRP rupture	FRP rupture	FRP rupture	FRP rupture	Concrete crushing	FRP debonding	Anchor Failure/rupture	FRP rupture

Table 4. Experimental maximum, minimum and average crack spacing of panels at stabilized cracking stage

Specimen	No. of cracks	S _{r,max} (mm)	S _{r,min} (mm)	S _{rm} (mm)
REF-P3	10	151.89	71.37	105.35
REF-P4	8	121.16	47.49	87.95
P3-0250-FW	12	182.82	70.38	108.81
P3-040-FW	11	136.14	65.02	98.46
P4-025-FA	10	138.94	43.44	97.43
P4-040-FW	12	154.94	53.16	99.79
P4-080-FW	13	126.49	39.37	89.57

Table 5. Calculation of β and $f(\beta)$ for FRP Strengthened RC Panels

Specimen	ζ _{exp}	f ['] _c (Mpa)	$f(f_c^{\prime})$	$\bar{\epsilon}_1$	$f(\bar{\epsilon}_1)$	ρ _f E _f (Mpa)	f(FRP)	$f(\boldsymbol{\beta})_{exp}$	β°
P3-025-FW	0.184	51	0.812	0.017	0.367	463.3	1.164	0.529	8.0
P3-040-FW	0.158	50	0.820	0.012	0.413	651.6	1.193	0.390	9.0
P4-025-FW	0.198	45	0.864	0.012	0.415	463.3	1.164	0.473	5.5
P4-040-FW	0.204	52	0.804	0.018	0.349	651.6	1.193	0.608	7.3
P4-080-FW	0.110	54	0.789	0.016	0.367	1259.7	1.269	0.298	13.0
P4-040-SB	0.190	44	0.874	0.010	0.452	651.6	1.193	0.402	9.6
P4-025-FA	0.184	52	0.804	0.017	0.359	463.3	1.164	0.547	7.2
P4-040-FA	0.200	52	0.804	0.029	0.280	651.6	1.193	0.744	5.3