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The role of pore-fluid pressure on the failure of magma reservoirs: insights from Indonesian and Aleutian arc volcanoes

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Abstract. We use numerical models to study the mechanical stability of magma reservoirs embedded in elastic host rock. We quantify the overpressure required to open tensile fractures (the failure overpressure), as a function of the depth and the size of the reservoir, the loading by the volcanic edifice and the pore-fluid pressure in the crust. We show that the pore-fluid pressure is the most important parameter controlling the magnitude of the failure overpressure rather than the reservoir depth and the edifice load. Under lithostatic pore-fluid pressure conditions, the failure overpressure is on the order of the rock tensile strength (a few tens MPa). Under zero pore-fluid pressure conditions, the failure overpressure increases linearly with depth (a few hundreds MPa at 5 km depth). We use our models to forecast the failure displacement (the cumulative surface displacement just before an eruption) on volcanoes showing unrest: Sinabung and Agung (Indonesia) and Okmok and Westdahl (Aleutian). By comparison between our forecast and the observation, we provide valuable constrain on the pore-fluid pressure conditions on the volcanic system. At Okmok, the occurrence of the 2008 eruption can be explained with a 1000 m reservoir embedded in high pore-fluid pressure, whereas the absence of eruption at Westdahl better suggests that the porefluid pressure is much lower than lithostatic. Our finding suggests that the pore-fluid pressure conditions around the reservoir may play an important role in the triggering of an eruption by encouraging or discouraging the failure of the reservoir.

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1. Introduction

The past decades have provided a wealth of observations of ground surface deformation 1 before, during and after volcanic eruptions using GPS, tiltmeters, strainmeters or satellite 2 radar interferometry (InSAR). Observed pre-eruption inflation ranges from a few cm prior 3 to the 2006 Augustine eruption, Alaska [Cervelli et al., 2006] to several meters at Sierra Negra volcano, Galapagos Islands [Geist et al., 2008]. An important question for hazard 5 assessment is whether detected inflation is a precursor for an eruption [Dzurisin, 2003; 6 Moran et al., 2011; Chaussard et al., 2013; Biggs et al., 2014]. There are many observations 7 of pre-eruptive inflation at basaltic volcanoes, e.g. at Krafla and Grimsvötn in Iceland 8 Björnsson et al., 1979; Ewart et al., 1991; Sturkell et al., 2006; Lengliné et al., 2008; 9 Reverso et al., 2014], Kilauea in Hawaii [Dvorak and Dzurisin, 1993], Fernandina in the 10 Galapagos Islands [Bagnardi and Amelung, 2012], Axial Seamount in the Pacific ridge 11 [Nooner and Chadwick, 2009] and Okmok in Alaska [Lu et al., 1998, 2010]. For several 12 andesitic and dacitic volcanoes arc-wide, InSAR surveys have documented pre-eruptive 13 inflation [Pritchard and Simons, 2002, 2004; Chaussard and Amelung, 2012; Chaussard 14 et al., 2013; Lu and Dzurisin, 2014]. In contrast, other volcanic systems can show unrest in 15 form of ground deformation, earthquakes swarms, large heat and gas emissions for months 16 to decades without eruption [Newhall and Dzurisin, 1988; Lowenstern et al., 2006; López 17 et al., 2012; Martí et al., 2013; Acocella et al., 2015]. This is the case of many silicic caldera 18 volcanoes such as Long Valley [Hill, 1984; Newman et al., 2006], Santorini [Newman et al., 19 2012; Parks et al., 2012], Yellowstone [Wicks et al., 2006; Chang et al., 2007], Campi 20 Flegrei [Orsi et al., 1999; Di Vito et al., 1999; Lundgren et al., 2001; Beauducel et al., 21

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²² 2004; Gottsmann et al., 2006; Troise et al., 2007; Amoruso et al., 2007; Trasatti et al.,
²³ 2008; Vilardo et al., 2009; Samsonov et al., 2014] or Laguna del Maule [Feigl et al., 2014;
²⁴ Le Mével et al., 2015].

The inflation of the ground surface in volcanic areas results from stress changes in the 25 crust due to the accumulation of magma or the exsolution of gas inside reservoirs or due to 26 the propagation of magma through intrusions or conduits. Such surface displacements are 27 often modeled at first order by analytical solutions such as point pressure sources [Mogi, 28 1958, finite spherical sources [McTique, 1987] or dislocations [Okada, 1985] embedded in 29 an elastic half-space. In a case by case approach, more realistic models based on numerical 30 techniques have been also developed to better explain volcanic ground deformation. Such 31 models can take into account the rheology of the crust, the heterogeneities of the rock 32 properties and the topography of the volcano [De Natale et al., 1997; Del Negro et al., 33 2009; Currenti et al., 2010; Geyer and Gottsmann, 2010; Ronchin et al., 2015]. 34

In a simplified view, the magma injection from a reservoir is "inflation predictable" 35 [Segall, 2013], which means that an intrusion can be considered when the ground inflation reaches a critical value. Such value is related to the mechanism of failure of the magma 37 reservoir [Tait et al., 1989; Burt et al., 1994; Gudmundsson, 1988; Pinel and Jaupart, 2000; 38 *Grosfils*, 2007] and therefore will be referred to as the failure displacement in this paper. 39 The magma reservoir, modeled as a pressurized cavity, remains intact as long as the sum 40 of the tangential stresses affecting the reservoir's wall does not exceed the strength of 41 the host rocks. When the magma overpressure reaches a threshold, referred to as the 42 failure overpressure in this paper, a tensile fracture is initiated from the reservoir and 43 the magma can propagate as a hydrofracture [Rubin, 1995; Gudmundsson and Brenner. 44

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⁴⁵ 2001; *Gudmundsson*, 2002]. Then, the propagation of the intrusion continues as long as ⁴⁶ the strain energy release rate exceeds the fracture toughness of the material [*Kilburn*, ⁴⁷ 2003; *Gudmundsson*, 2012; *Rivalta et al.*, 2015].

With knowledge on the elastic properties of the overlying host rock, failure models of 48 magma reservoirs therefore provide constraints on failure overpressure and the associated 49 failure displacement. The influence of various parameters of the volcanic system on the 50 tensile failure of the reservoir has been already investigated, such as the depth and the 51 shape of the reservoir [Grosfils, 2007; Martí and Geyer, 2009; Albino et al., 2010], the 52 mechanical properties of the host rocks [Gudmundsson, 2006; Long and Grosfils, 2009], 53 thermal effects and host rock rheologies [Gerbault, 2012; Gregg et al., 2012; Currenti 54 and Williams, 2014], the presence of existing structures [De Natale et al., 1997; Geyer 55 and Martí, 2009] and surface stress perturbations induced by edifice loading [Pinel and 56 Jaupart, 2003; Hurwitz et al., 2009; Chestler and Grosfils, 2013], flank collapse [Manconi 57 et al., 2009; Pinel and Albino, 2013] or ice cap melting [Albino et al., 2010; Geyer and 58 Bindeman, 2011]. Moreover, depending on the pore-fluid pressure [Gudmundsson, 2012; 59 Gerbault, 2012; Grosfils et al., 2015], the failure overpressure can be of the same magnitude 60 as the tensile strength of rock (a few to ten MPa) [Gudmundsson, 2002, 2006; Pinel and 61 Jaupart, 2005; Parfitt and Wilson, 2009] or be as high to exceed the confining pressure 62 (a few tens to hundreds of MPa) as reservoir depth increases [Sammis and Julian, 1987; 63 Grosfils, 2007; Hurwitz et al., 2009]. During a volcanic unrest, it is therefore crucial to 64 characterize the pore-fluid pressure around the magma reservoir before quantifying the 65 failure conditions. However, the magnitude of the pore-fluid pressure in volcanic systems 66 is usually unknown [Fournier, 2007]. 67

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Several studies have examined the relationship between volcanic activity and pore-68 fluid pressure. On the one hand, the strain changes caused by magma pressurization 69 during a volcanic unrest affect the groundwater level. Such intuitive effect has been 70 observed and modelled on several volcanoes such as Krafla (Iceland), Usu (Japan) and 71 Kilauea (Hawaii) [Stefansson, 1981; Shibata and Akita, 2001; Hurwitz and Johnston, 2003; 72 Strehlow et al., 2015]. On the other hand, the change in pore-fluid pressure modifies the 73 mechanical properties of the host rocks and could therefore influence the behavior of the 74 volcanic system. For example, Farguharson et al. [2016] conducted triaxial laboratory 75 experiments on rock samples to show that unrest-related pore-fluid pressure increase can 76 lead to the development of fracture networks around volcanic conduits, known as pore 77 pressure-induced embrittlement. In addition, Gressier et al. [2010] used analogue models 78 to examine how pore fluid pressure controls the emplacement of magma intrusions in 79 sedimentary basins. They showed that an increase of pore pressure prevents the vertical 80 propagation of magma and favours the emplacement of deep horizontal intrusions. Both 81 works show that the pore pressure conditions can influence both the initiation and the 82 propagation of magma intrusions. 83

In this paper, we investigate the failure overpressure conditions around magma reservoirs using finite element modeling. First, we perform a sensitivity study to understand the effect of pore-fluid pressure and compare it to the effect of other parameters such as the depth and the radius of the reservoir or the morphology of the volcanic edifice. Then, we apply our modeling to Sinabung and Agung in Indonesia and Okmok and Westdahl in the Aleutian Islands. All these volcanic systems exhibited periods of prolonged ground inflation which at Sinabung and Okmok led to eruptions, but at Agung and Westdahl

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did not, highlighting the limitations of ground inflation as eruption precursor. The main objective of this study is to understand why for similar ground inflation, some magmatic systems fail and initiate an eruption while some others remain stable without erupting. Stress threshold at which an intrusion is initiated from the magma reservoir varies between volcanoes. We will calculate for each volcano and for different pore-fluid pressure conditions this failure threshold taking into account the radius and the depth of the magma reservoir and the size of the volcanic edifice.

2. Method

2.1. Failure criterion

The failure conditions of magma reservoirs have been investigated from the analogy of hydro-fractures occurring around boreholes or tunnels [*Jaeger*, 1979]. The approach consists to calculate stress at the wall of the cavity. Assuming that magma and host rock have the same density, the internal magma pressure P_m is equal to:

$$P_m = -\rho_r g z + \Delta P_m \tag{1}$$

where ρ_r is the host rock density, g the gravitational acceleration and z the depth from the surface (negative values). Here, and in the entire study, we adopt by convention compressive stress as positive and tensile stress as negative. The first term in the equation counters the lithostatic load of the rock, creating a state of equilibrium with no deformation in the surrounding host rock. The second term, ΔP_m is an excess uniform pressure in comparison with lithostatic pressure (also referred to as overpressure), which induces host rock deformation.

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For 2D plane-strain geometry, analytical solutions of this problem have been given by *Jeffery* [1921] and been firstly used to quantify the pressure required to initiate a dyke intrusion from a cylindrical reservoir [*Gudmundsson*, 1988, 2006], considering that the dyke initiates from tensile fractures (mode I). The general formulation for the tensile criterion around a sphere is given by *Timoshenko et al.* [1951]. As we consider compressive stress as positive values, the failure criterion can be written as:

$$-\sigma_t \ge (P_L - P_p + T_s) \tag{2}$$

with σ_t the tangential stress at the wall, P_L the lithostatic pressure (equal to $-\rho_r gz$), P_p the pore-fluid pressure and T_s the tensile strength of the rocks. As the medium is elastic, the tangential stress is proportional to the magma overpressure so we can introduce the ratio k, with $k = -\frac{\Delta P_m}{\sigma_t}$. Therefore, the tensile failure will be initiated when the overpressure reaches a critical value referred to as the failure overpressure, ΔP_f , and defined as:

$$\Delta P_f = k(P_L - P_p + T_s) \tag{3}$$

The value of ΔP_f is dependent on tensile strength of the rock, the pore-fluid pressure conditions and the lithostatic pressure. The tensile strength of rocks can be measured by uniaxial tensile testing of natural samples. From such experiments, *Touloukian et al.* [1981] report tensile strengths of 13.8 ± 2.1 MPa for granite and 8.6 ± 1.4 MPa for pristine basalt. However, these values have to be considered as upper limits because crustal processes such as faulting, fracturing or hydrothermal activity reduces the tensile strength [*Schultz*, 1995]. For example, in-situ measurements in Iceland provide strength values of

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¹²⁸ 1-6 MPa [*Haimson and Rummel*, 1982]. Through the paper, we will use a constant value ¹²⁹ of 10 MPa for T_s and we will be aware that the failure overpressure calculated would ¹³⁰ correspond to an upper bound.

There are different approaches to include the pore-fluid pressure conditions in models 131 for reservoir failure [Gudmundsson, 2012; Gerbault, 2012; Grosfils et al., 2015]. A common 132 approach considers that some fluids are present in the rock adjacent to the reservoir *Lister* 133 and Kerr, 1991; Rubin, 1995; McLeod and Tait, 1999]. In that case, the pore-fluid pressure 134 equals the lithostatic pressure $(P_p = P_L)$ and the failure overpressure is of the magnitude 135 of the tensile strength, $\Delta P_f = kT_s$ [e.g., Gudmundsson, 2002, 2006; Pinel and Jaupart, 136 2005; Parfitt and Wilson, 2009]. An alternative approach considers that pre-existing fluids 137 are negligible at the contact between the reservoir and the host rock. In that way, there is 138 zero pore-fluid pressure $(P_p = 0)$ and the failure overpressure becomes strongly dependent 139 on the lithostatic stress $\Delta P_f = k(P_L + T_s)$ [Sammis and Julian, 1987; Grosfils, 2007]. For 140 zero pore-fluid pressure, the failure overpressure for a reservoir at 10 km depth will be 141 almost twice larger than for a reservoir at 5 km depth. 142

The solution of ΔP_f is well-known for a spherical reservoir embedded in an infinite space, in which the ratio k is constant along the wall and equal to 2 [Jaeger, 1979; Tait *et al.*, 1989]. However, for more complex geometries and/or non-lithostatic stress field, the ratio k can not be easily determined and numerical models are therefore required to assess the failure conditions.

2.2. Finite Element Modeling

¹⁴⁸ Stress and strain are numerically calculated solving the equations for linear elastic-¹⁴⁹ ity with the Finite Element Method, using the software COMSOL MULTIPHYSICS

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(https://www.comsol.com). The geometry of the mechanical model is a 2D axi-150 symmetrical box of 100 x 100 km, with a mesh of about 10 000 triangular elements 151 that is refined around the volcanic edifice and the magma reservoir. The width and the 152 height of the box are located far enough from the magma reservoir to limit the influence 153 of boundaries on the stress calculation. A condition of no-displacement in the normal 154 direction is fixed to the right and bottom boundaries. The top boundary corresponds to 155 the surface and is free to move and the left boundary is the axis of symmetry (Figure 156 1). We consider homogeneous and isotropic elastic host rock, characterized by its shear 157 modulus G and its Poisson's ratio ν . 158

In the absence of tectonic stress, the initial state in numerical models is assumed to 159 be either a lithostatic stress field $(\sigma_r = \sigma_{\phi} = \sigma_z = P_L)$ or a vertical uni-axial strain 160 $(\sigma_r = \sigma_\phi = \frac{\nu}{1-\nu}\sigma_z)$ [e.g., Sartoris et al., 1990; Grosfils, 2007; Currenti and Williams, 161 2014]. In our study, we assume the initial stress as lithostatic (e.g. no deviatoric stress), 162 which is considered as the most likely state of stress [e.g., McGarr, 1988], especially for 163 mature portion of the crust where different processes such as deformation, faulting or 164 fracturing tend to reduce deviatoric stresses. To model this state of stress, we therefore 165 impose on each element of the host rock an internal body load per volume, $\rho_r g$ and a 166 pre-existing lithostatic stress. 167

The first set of models reproduces the simplest case of a magma reservoir embedded in a lithostatic stress field (Figure 1a). The magma reservoir is modeled as a half spherical cavity with a radius R and a top depth H_t (depth considered as negative values). Total pressure inside the magma reservoir, P_m , is applied as a normal stress at the reservoir wall. It is composed of a depth-dependent component, $-\rho_r gz$, which compensates the weight

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¹⁷³ of the surrounding rock and an uniform overpressure, ΔP_m , which could be induced by ¹⁷⁴ different processes such as magma replenishment, volatile exsolution or fractional crystal-¹⁷⁵ lization. When ΔP_m is set to zero, the magmatic reservoir is in a stress equilibrium with ¹⁷⁶ the surrounding medium and no deformation is generated.

The second set of models takes into account the effect of the load of the volcanic edifice. 177 The edifice is modeled as a cone, characterized by a radius R_e and a height H_e (Figure 178 1b). In that model, the top depth of the reservoir H_t is now calculated from the base 179 of the edifice. The edifice is imposed as a body loaded volume without initial pre-stress. 180 Below the edifice, the initial conditions (pre-stress and loading) are set the same as in 181 the previous model. The edifice load will modify the initial lithostatic stress field and 182 induce deformation in the crust beneath. This configuration simulates the case where 183 the construction of an edifice is more rapid than the time-scale required to reach stress 184 equilibrium. Parameters and variables used in our modeling are reported in Table 1. 185

Failure overpressures are calculated numerically using the tensile failure criterion described in the section 2.1. As the failure conditions now vary along the wall of the reservoir, the equation (3) can be re-written as:

$$\Delta P(\theta) = k(\theta)(P_L(\theta) - P_p(\theta) + T_s) \tag{4}$$

¹⁸⁹ where θ is the angle between the location at the wall and the vertical axis (Figure 1), ¹⁹⁰ and the function $k(\theta)$, the ratio between the magma overpressure applied in the model ¹⁹¹ and the induced tangential stress at the reservoir's wall. Because the crust rheology is ¹⁹² elastic, only one model run is needed to calculate numerically the function $k(\theta)$. This ¹⁹³ function is minimum at the location $\theta = \theta_f$, where θ_f corresponds to the failure location.

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¹⁹⁴ By using θ_f in the equation (4), we can estimate the magma overpressure required to ¹⁹⁵ cause the reservoir failure $\Delta P_f = \Delta P(\theta_f)$.

For the case with edifice loading, we require two models runs: (1) a model without edifice loading but with reservoir overpressure (previous case) and (2) a model with edifice loading but without reservoir overpressure ($P_m = P_L$). Based on the superposition principle previously used in *Pinel and Jaupart* [2003] and *Albino et al.* [2010], we are able to calculate the overpressure required for failure below an edifice through the function:

$$\Delta P(\theta) = k(\theta)(\sigma_{t_e}(\theta) - P_p(\theta) + T_s) \tag{5}$$

where σ_{t_e} is the total tangential stress at the reservoir wall, which is composed of the pre-201 edifice lithostatic stress P_L and the stress induced by the edifice loading. For each model, 202 we take into account the two different pore-fluid pressure conditions discussed previously: 203 zero pore pressure where $P_p(\theta) = 0$ and lithostatic pore pressure where $P_p(\theta) = P_L(\theta)$. For 204 simplicity, we assume that pore-pressure conditions are not affected by the edifice. This 205 assumption is valid considering that (1) pore-fluid pressure changes induced by the elastic 206 load are fully dissipated at present time and (2) the water table does not significantly 207 change during the construction of the edifice. 208

Figure 2 details how the failure overpressure is calculated at the reservoir's wall for the two pore-fluid pressure cases. Solid and dashed color lines correspond to the case without edifice and with edifice, respectively. For each case, the minimum of the function $\Delta P(\theta)$ is shown by a dot, which indicates the failure overpressure, ΔP_f , and the angle of failure, θ_f . For the zero pore-fluid pressure without edifice, the failure occurs at $\theta_f=5^\circ$ with $\Delta P_f=132.3$ MPa. This is in good accordance with *Grosfils* [2007], who found that for his

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corresponding case, the failure occurs at the top (equivalent to $\theta_f=0^\circ$) for a normalized overpressure of 2 (equivalent to $\Delta P_f=2(P_L+T_s)=129.9$ MPa) (see their Fig. 7b and 10b for details).

For the lithostatic pore-fluid pressure without edifice, the failure occurs at $\theta_f = 69^\circ$ with $\Delta P_f = 18.6$ MPa. The failure location found is in accordance with the value of 70.5° deduced from the analytical solution $acos(\frac{R}{|H_c|})$ given by *Jeffery* [1921] and *McTigue* [1987] (H_c being the center depth of the reservoir). This location corresponds to the point of tangency where the line must be tangent to the reservoir's wall and intersects the free surface at the vertical axis.

For the edifice model, $\Delta P_f = 114.7$ MPa and $\theta_f = 0^\circ$ in the case of zero-fluid pore pressure, and $\Delta P_f = 4.8$ MPa and $\theta_f = 0^\circ$ if pore-fluid pressure is considered lithostatic. The loading of the edifice focus the failure at the top of the spherical reservoir, as already suggested by *Pinel and Jaupart* [2003], *Grosfils* [2007] and *Hurwitz et al.* [2009]. Moreover, it is interesting to notice that for both pore pressure conditions, the decrease of the failure overpressure induced by the edifice load is identical and about 15 MPa.

Based on this approach, we perform a parametric study by using three different model configurations. For the first configuration, the magma reservoir is embedded in an elastic half-space with lithostatic stress field (Figure 3). The second model configuration (topographic loading model, Figure 4) includes the loading stress induced by a conical volcanic edifice. For these two configurations, the radius and the top depth of the reservoir vary. In the third model configuration (Figure 5), the radius and the top depth of the reservoir are kept constant but the edifice size varies.

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3.1. Effect of the radius and the depth of the reservoir

To compare the results between the two pore-fluid pressure conditions, the failure overpressures are normalized by the term $(P_L(\theta_f) - P_p(\theta_f) + T_s)$. From the equation (4), the normalized failure overpressure correspond to the value $k(\theta_f)$. Figure 3 shows $k(\theta_f)$ and θ_f obtained in a lithostatic stress field for lithostatic pore-fluid pressure (Figure 3a,b) and zero pore-fluid pressure (Figure 3c,d). The reservoir radius and the reservoir top depth range from 100 to 2000 m and from -200 to -5000 m, respectively. Using step sizes of 100 m and 200 m, respectively, we conduct 500 model runs.

In both cases, the normalized failure overpressure increases with increasing reservoir 244 depth and with decreasing reservoir radius. For the lithostatic case, normalized values 245 range from 0.4 for large and shallow reservoirs (R=2000 m, $H_t=-200 \text{ m}$) to 2 for small and 246 deep reservoirs (R=100 m, $H_t = -5000$ m). For a reservoir radius of 1000 m, the failure 247 overpressure increases from 16.9 MPa at 1 km depth to 19.9 MPa at 5 km depth, using 248 $T_s = 10$ MPa (Figure 3a). For the zero pore-fluid pressure case, normalized values range 249 in the same order of magnitude from 0.25 to 2, according to reservoir depth. However, 250 in that case, the failure overpressures are much higher than in the lithostatic pore-fluid 251 pressure case. For the reservoir radius of 1000 m, the failure overpressure changes from 252 70.8 MPa to 295.3 MPa from 1 to 5 km depth, using $\rho_r = 2800 \text{ kg.m}^{-3}$ (Figure 3c). The 253 failure overpressure increases with depth by only 15% in the lithostatic case and by 75% in 254 the zero pore-fluid pressure case. With zero pore-fluid pressure around the reservoir, the 255 conditions of failure are strongly depth dependent and would require large overpressures 256 to initiate an eruption. 257

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Another difference between the two pore-fluid pressure assumptions is the location of 258 the failure (Figure 3b,d). For lithostatic pore-fluid pressure, the location of the failure for 259 a spherical reservoir is a function of the radius and the depth of the reservoir, with $\theta_f =$ 260 $acos(\frac{R}{|H_t|+R})$. For top depth deeper than 1 km, the failure will occur at the periphery 261 of the reservoir $\theta_f > 45^{\circ}$ (Figure 3b). At the failure point, the direction of propagation 262 is given by the maximum compressive stress, which is radial from the reservoir's wall. 263 Under lithostatic pore pressure, the failure will favor the emplacement of sub-horizontal 264 intrusions. Under zero pore-fluid pressure, the failure occurs at the top of the reservoir for 265 most of the cases ($\theta_f=0$) and deviates of only 30-40° from the pole for shallow reservoirs 266 (Figure 3d). Such pore pressure conditions will therefore favor the initiation of sub-vertical 267 intrusions. 268

3.2. Effect of the edifice loading

Figure 4 shows the failure overpressure for the two pore-fluid pressure assumptions 269 in the second model configuration, taking into account the load of the volcanic edifice 270 (Figure 1b). As we consider elastic rheology, the failure overpressure below a volcanic 271 edifice (Figure 4a,d) is the sum of the failure pressure in a lithostatic stress field (Figure 272 4b,e) and a term, δP , reflecting the effect of the loading stress due to the edifice (Figure 273 4c,f). Positive (negative) δP indicates that the edifice loading prevents (enhances) failure. 274 For the lithostatic pore-fluid pressure case, the failure overpressure is highest for small 275 reservoirs located at shallow depth (Figure 4a). For increasing reservoir depth, ΔP_f 276 decreases until a minimum is reached at intermediate depth between -2000 m and -3000 277 m below the base of the cone (white line on Figure 4a). For the zero pore-fluid pressure 278

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case, the failure overpressure is still largely dependent on the depth of the reservoir (Figure4d).

However, the variation of failure overpressure due to edifice loading, δP , is similar in 281 both cases (Figure 4c,f). The edifice loading discourages the failure for reservoirs shallower 282 than 1000 m and encourages failure of reservoirs at greater depth. For H_t =-200 m, the 283 failure overpressure increases by about 22 MPa for both pore-fluid pressure cases. In 284 contrast, for H_t =-3000 m, the failure overpressure decreases by 15 MPa in both cases. 285 The change is due to the transition of the horizontal normal stress induced by the edifice 286 loading to the reservoir's wall from compressive regime at shallow depth to tensile regime 287 at deep depth [*Pinel and Jaupart*, 2003, 2004]. For both pore-fluid pressure conditions, 288 the largest decrease in failure overpressure occurs for reservoirs located around 3000 m 289 depth (white line in Figure 4c, f). 290

In the third model configuration, the size and the depth of the reservoir are kept con-291 stant, but the edifice size varies. Edifice radius R_e ranges from 500 to 10000 m, with a 292 step size of 500 m and edifice slope θ_e from 2 to 30°, with a step size of 2°. The normalized 293 failure overpressures are shown in Figure 5a,b as a function of the radius and height of the 294 edifice, for the two pore-fluid pressure assumptions. In both cases, the failure overpres-295 sure increases with increasing edifice radius and decreases with increasing edifice height. 296 With the load of the edifice, the failure occurs at the top of the reservoir for both pore-297 fluid pressure conditions, which will favor the initiation of sub-vertical intrusions leading 298 eventually to summit eruptions. In the case of lithostatic pore-fluid pressure, there are 299 negative failure overpressures for large edifice heights (Figure 5a), which mean that the 300 reservoir is not mechanically viable under such edifices. Although the amplitude of the 301

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failure overpressure is different between the two pore-fluid conditions, we notice that the patterns are the same (Figure 5c-d). Variations are mostly linear with +2.5 MPa/km for the radius (Figure 5c) and -12 MPa/km for the height (Figure 5d). These results underline that the failure overpressure changes due to stress perturbations are independent of the conditions of pore-fluid pressure around the reservoir.

4. Application of failure models to Sinabung, Agung, Westdahl and Okmok volcanoes

In this section, we apply our failure models to real volcanoes. We select two pairs of volcanoes: Sinabung and Agung in Indonesia and Okmok and Westdahl in the Aleutian. The pair selection is based on the following characteristics: (1) both volcanoes showed sign of unrest, at one volcano the unrest is followed by an eruption but not at the other one. (2) eruptions are initiated by magma intrusions from a reservoir as a result of rock fracturing, and our mechanical models apply. (3) volcanoes are close enough in space to have similar geological and tectonic settings.

We calculate the failure overpressure, taking into account the reservoir depth and the 314 loading stress of the edifice. We investigate the failure overpressure considering lithostatic 315 pore-fluid pressure $(P_p = P_L)$ and zero pore-fluid pressure $(P_p = 0)$. With assumptions 316 on the shear modulus, we then convert the failure overpressure to failure displacement. 317 which corresponds to the maximum vertical surface displacement expected before the 318 failure of the reservoir. The total ground displacements in our FEM model are the sum 319 of two components: (i) subsidence by a few meters related to the implementation of the 320 surface load (ii) inflation caused by the pressurization of the reservoir. With an elastic 321 assumption, the subsidence occurs immediately or over a short period of time after the 322

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³²³ occurrence of the surface load. For the calculation of our failure displacements, we do not ³²⁴ consider this subsidence but only displacements related to the reservoir pressurization.

4.1. Eruptions and ground deformation

4.1.1. Example 1: Sinabung and Agung

Sinabung and Agung are located in the Indonesian subduction arc and are both associ-326 ated with a strike-slip setting [Hughes and Mahood, 2011; Acocella and Funiciello, 2010; 327 Chaussard and Amelung, 2014]. Sinabung is a 2460-m-high and esitic-dacitic stratovolcano 328 in northern Sumatra (Indonesia), 25 km north of Toba caldera (Figure 6a-top). Edifice 329 flanks are composed of successive lava flows (Global Volcanism Program, 2013), which 330 indicate past non-explosive eruption episodes. On August 27th 2010, Sinabung erupted 331 after a period of steady inflation, producing a 5 km high Plinian ash cloud above the 332 summit. A cumulative displacement of about 10 cm in line-of-sight (LOS) direction was 333 detected by InSAR during 3.5 years preceding the eruption [Chaussard and Amelung, 334 2012; Chaussard et al., 2013]. The 2010 phreatic episode was the first eruption in modern 335 times, except possibly an unconfirmed eruption in 1881 [Sutawidjaja et al., 2013]. 336

The 3000-m-high Agung stratovolcano in Bali is built on the caldera rim of neighbor-337 ing Batur volcano (Figure 6a-top). Three eruptions were reported during the last two 338 centuries, in 1808, 1843 and 1963-1964. The latter was one of the largest eruptions of 339 the 20th century and produced voluminous ashfall, pyroclastic flows and lahars, killing a 340 total of 1138 people [Witham, 2005]. Between mid-2007 and 2009, Agung inflated by more 341 than 13 cm in LOS direction but did not erupt [Chaussard and Amelung, 2012; Chaus-342 sard et al., 2013]. Quiescence over decades to centuries indicates the lack of permanent 343 conduits to transport the magma to the surface at Sinabung and Agung in contrast to 344

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³⁴⁵ persistently active volcanoes (e.g. Soufriere Hills, Popocatepetl or Merapi). An eruption
³⁴⁶ would be initiated by fracturing a new path into the crust.

³⁴⁷ 4.1.2. Example 2: Okmok and Westdahl

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The two volcanoes are located at 260 km distance in the Aleutian subduction arc in sim-348 ilar tectonic settings [Zellmer, 2008; Hughes and Mahood, 2011; Acocella and Funiciello, 349 2010; Chaussard and Amelung, 2014]. Okmok, a basaltic shield volcano (500 m) located 350 on Umnak Island in the Aleutian arc (Figure 6a-bottom), is one of the most active Aleu-351 tian volcanoes with 11 known eruptions since 1900 [Global Volcanism Program, 2013]. 352 The summit is composed of two overlapping 10-km-wide calderas formed about 12,000 353 and 2050 years ago [Larsen et al., 2007]. Subsequently, numerous small satellite cones 354 and lava domes have developed on the caldera floor [Byers, 1959]. The more recent cones 355 are basaltic and formed after the disappearance of a caldera lake. Intense hydrothermal 356 activity with fumaroles and hot springs is often observed within the caldera. Historical 357 eruptions have produced lava flows from the edge of the caldera rim. Between the last 358 two eruptions in 1997 and 2008, the caldera floor inflated by almost 1 m, which was mod-359 elled by an inflated source with a cumulative change of 0.05 km^3 [Lu et al., 2010; Lu and 360 Dzurisin, 2014].361

Westdahl, a basaltic shield (1654 m) located on Unimak island (Figure 6a-bottom), is one of the largest volcanoes in the Aleutians. Westdahl had only 3 eruptions since 1900 [*Global Volcanism Program*, 2013]. The last eruption in 1991 produced explosions and lava flows from a 8-km fissure. In January 2004, the Alaska Volcano Observatory (AVO) detected a strong seismic swarm associated with long-period events beneath the volcano, which could represent a failed eruption [*Neal et al.*, 2005]. Westdahl volcano inflated

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around 20-30 cm between the 1991-92 eruption and 2010 [*Lu et al.*, 2000, 2003], but no eruption has yet occurred. Both volcanoes show that historical eruptions are associated with lava flows originate from different fissures. This implies that eruptions at Okmok and Westdahl are not fed by a permanent conduit but rather by successive emplacement of magma intrusions from the reservoir.

4.2. Depth and volume change of the magma reservoirs

For the four cases, the volume change and the depth of the magma reservoir have been 373 already deduced by the inversion of InSAR time series, using point source model [Mogi, 374 [1958] or pressurized finite sphere embedded in elastic half-space [McTique, 1987]. The 375 Mogi analytical solution for vertical displacements at the surface is defined as $U_z(r) =$ 376 $\frac{(1-\nu)\Delta V \mid H_c \mid}{\pi (r^2 + H_c^2)^{\frac{3}{2}}}$, where ΔV is the volume change of the source, H_c the center depth of 377 the source and r the radial distance from the source. In detail, the volume change is a 378 function of the source radius R, the magma overpressure ΔP_m and the shear modulus of 379 the host rock G through: $\Delta V = \pi R^3 \frac{\Delta P_m}{G}$. This means that to convert displacement to 380 overpressure and vice versa, R and G have to be known. However, geodetic inversions 381 only constrain H_c and ΔV . 382

At Sinabung and Agung, the ground inflation has been attributed to pressurized spheres at 0.9 and 1.9 km depth below the average elevation of 0.7 and 0.5 km, respectively [*Chaussard and Amelung*, 2012; *Chaussard et al.*, 2013]. The authors also suggested that the volume changes of the Agung and Sinabung reservoir were around 1 km³ and 0.1 km³, respectively. The time series of LOS displacements of these two volcanoes given by *Chaussard et al.* [2013] are converted into vertical displacements assuming that the magma reservoir axes are located below the summits so that summit displacements are

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³⁹⁰ purely vertical (Figure 7a,b). The corresponding maximum vertical displacements for ³⁹¹ Sinabung and Agung are 13 and 16 cm, respectively. At Sinabung and Agung, as we do ³⁹² not have ground deformation data before the year 2007, these values should be therefore ³⁹³ considered as low bounds.

At Okmok, the ground inflation can be explained by a point source at 2.6-3.2 km below 394 sea level [Lu et al., 2003; Miyaqi et al., 2004; Fournier et al., 2009]. A more realistic Earth 395 model, taking into account the variability of elastic parameters in the crust, gave a source 396 depth of 3.5 km below sea level [Masterlark et al., 2016]. At Westdahl, the point source 397 is located deeper at 6 km below sea level [Lu and Dzurisin, 2014]. For both Aleutian 398 volcanoes, the inferred cumulative volume change is 50.10^6 m³ [Lu and Dzurisin, 2014]. 399 The time series of volume change at Aleutian volcanoes given by Lu and Dzurisin [2014] 400 are converted into vertical displacements at the center of the volcano (Figure 7c,d), using 401 the approximation $U_z(r=0) = \frac{3\Delta V}{4\pi H_c^2}$. The maximal vertical displacements found are 88 402 cm and 25 cm at Okmok and Westdahl, which, for Okmok, is the total inflation between 403 the 1997 and 2008 eruptions. 404

⁴⁰⁵ As we do not have constraints on the reservoir size, the radius will be considered as a ⁴⁰⁶ free parameter. The parameters used in the modeling are summarized in Table 2.

4.3. Morphological characteristics of the volcanic edifices

Elevation profiles show that the volcanic edifices are almost symmetrical, so that they can be approximated by 2D axis-symmetrical models (Figure 6b). The edifices of Sinabung, Agung and Westdahl are represented as cones defined by its radius and its height. The morphology of Okmok volcano is different than others as the edifice was destroyed by successive collapses. We model it as a cone truncated at 500 m above sea level

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(Figure 6b). The edifice radius is deduced from the analysis of slope maps and shaded relief images and the edifice height is derived by averaging elevation profiles with different azimuth (Table 2). The average height is measured between the centred summit and the base .

For the Indonesian volcanoes, the base of the edifice is taken as the regional average 416 elevation masking the edifice area, which is respectively 0.7 km for Sinabung and 0.5 km 417 for Agung. For the Aleutian islands, the choice of this base line is more questionable. The 418 reference can be either the sea level or the bottom of the ocean, which strongly depends 419 on which proportion of the volcano is under the sea. Based on the bathymetry map of the 420 Aleutian islands [Zimmermann et al., 2013], volcanic centers are built on top of a 50 km 421 width plateau, located at shallow depth (e.g. 100-500 m below sea level). It means that 422 the basement of Okmok and Westdahl is close to the sea level and it is therefore more 423 suitable to consider the sea level as reference rather than the bottom of the ocean.

4.4. Shear modulus around the volcanic system

The elastic parameters of the rocks in volcanic environment are poorly constrained. 425 Depending on the volcanic context, authors used in their models different values for the 426 shear modulus, from 2 GPa at Piton de la Fournaise (Reunion island) and Nyamulagira 427 (D.R. of Congo) [Fukushima et al., 2005; Peltier et al., 2008; Wauthier et al., 2013] to 428 12-30 GPa at Icelandic volcanoes [Pagli et al., 2006; Pinel et al., 2007]. Furthermore, the 429 elastic parameters vary vertically and laterally [Geyer and Gottsmann, 2008; Long and 430 Grosfils, 2009; Masterlark et al., 2010; Auriac et al., 2014] and are temperature-dependent 431 [e.g., Bakker et al., 2016]. Authors pointed out that high temperature may induce inelastic 432 behavior around the magma reservoir associated with low shear modulus [Dragoni and 433

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Magnanensi, 1989; Del Negro et al., 2009; Currenti et al., 2010; Currenti and Williams, 434 2014]. According to the values taken, the modeled displacements may change by an order 435 of magnitude. In addition, values for the poisson's ratio vary with the rock lithology 436 and range from 0.24 to 0.32 for igneous rocks [e.g., Christensen, 1996]. However, the 437 influence of the Poisson's ratio in our model results will be much smaller than the effect 438 of the shear modulus and it therefore can be neglected. For each volcano, the Poisson's 439 ratio, ν , is fixed at 0.25 and the shear modulus, G_s , is derived from seismic wave speed 440 measurements: 441

$$G_s = \frac{(1-2\nu)}{2(1-\nu)}\rho_r V_p^2$$
(6)

with ρ_r the rock density, and V_p the P-wave velocity.

At Agung and Sinabung, because there is no local seismic tomography we use results from Toba and Merapi volcanoes. The measured P-wave speeds are 3 km.s⁻¹ around the Toba magma chamber [*Stankiewicz et al.*, 2010] and 3-4 km.s⁻¹ for Merapi [*Wagner et al.*, 2007]. Taking a homogeneous rock density of 2800 kg.m⁻³, the seismic shear modulus ranges from 8.4 to 14.9 GPa with a mean of 11.6 GPa.

⁴⁴⁸ Using seismic tomography at Okmok, *Masterlark et al.* [2010] found P-wave velocities ⁴⁴⁹ of 2.5 km.s⁻¹ in the caldera structure and around the reservoir and 5.7 km.s⁻¹ in the ⁴⁵⁰ surrounding basement. Moreover, they suggested that there is a large contrast of rock ⁴⁵¹ density between the caldera (ρ_r =1800 kg.m⁻³) and the basement (ρ_r =2800 kg.m⁻³). The ⁴⁵² seismic shear moduli G_s calculated from Equation 6 are therefore 3.8 GPa below the ⁴⁵³ caldera and 30.3 GPa for the basement.

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At Westdahl, the velocity model of *McNutt and Jacob* [1986] used by the Alaska Volcano Observatory (AVO) is composed of four layers with velocities of 3.05, 3.44, 5.56 and 6.06km.s⁻¹ for the [3000, 0], [0, -1790], [-1790, -3650] and [-3650 -6000] meters depth ranges. The corresponding shear moduli are 8.7, 11.0, 28.9 and 34.2 GPa, respectively.

The shear modulus applicable for static mechanical models is lower than the shear 458 modulus for seismic waves because of the presence of fluid-filled pores and cracks [e.g., 459 Gudmundsson, 1990; Wauthier et al., 2012; Zhao et al., 2016]. The frequency dependence 460 of the modulus decreases with depth and confining pressure [*Ciccotti and Mulargia*, 2004]. 461 Adelinet et al. [2010] have shown using laboratory measurements of Icelandic basalt that 462 in dry conditions the ratio between the low frequency and high frequency bulk moduli 463 is independent of depth and around $\frac{2}{3}$. In saturated conditions, the ratio increases from 464 0.25 at sea level to 1 at a confining pressure of 200 MPa. 465

For each volcano, we consider models with three different shear moduli, 0.25 G_s , 0.5 G_s 466 and G_s . For Agung and Sinabung, the models are homogeneous with three shear moduli: 467 2.9, 5.8 and 11.6 GPa. For Okmok, we use different shear moduli for the caldera and for 468 the surrounding basement. Following the study of Masterlark et al. [2010], the caldera 469 domain is modeled as a semi-ellipse below the surface with horizontal and vertical axis of 470 5 km and 2 km, respectively. For the caldera domain, the three values modeled are 0.9, 471 1.9 and 3.8 GPa and for the basement 7.6, 15.15 and 30.3 GPa. For Westdahl, we use the 472 four-layers model from the seismic tomography. 473

4.5. Observed displacements vs. Failure displacements

⁴⁷⁴ By applying the failure overpressure ΔP_f at the wall of the magma reservoir, we can ⁴⁷⁵ calculate the failure displacement Uz_f . This value depends on the shear modulus, the

depth and the size of the reservoir. We use the geodetic reservoir depths and consider the
reservoir size as a free parameter. Values for the reservoir radius range from 100 m to
2000 m for the Aleutian volcanoes. At Sinabung and Agung volcanoes, as their reservoirs
are located shallower than 2000 m (900 and 1900 m, respectively), the upper bound of
the radius will be fixed at 800 and 1800 m, respectively.

Figure 8 shows for the four volcanoes the failure displacement as a function of reservoir 481 radius, shear modulus and pore-fluid pressure conditions. Zero pore-fluid pressure is 482 indicated by green shadings and lithostatic pore-fluid pressure by red shadings. The figure 483 shows that zero pore-fluid conditions produce significantly higher failure displacements 484 than lithostatic pore fluid pressure conditions (independent of reservoir radius and shear 485 modulus). This means that for increasing reservoir radius the failure displacement can be 486 kept constant by increasing the pore-fluid pressure (to produce a decrease in overpressure). 487 The figure also shows that a decrease in shear moduli results in an increase of the failure 488 displacements (independent of reservoir radius and the pore-fluid pressure conditions). 489

We are aware that the reservoir depth given for each volcano is known with some 490 uncertainty, which may also influence the failure displacements calculated. Under zero 491 pore pressure, the overpressure increases with the reservoir depth. As a consequence, a 492 variation of 20% of the reservoir depth does not have significantly effect on the failure 493 displacements (Figure S1 - Supplementary material). On contrary, under lithostatic pore 494 pressure, the variations of the failure overpressure with depth are small, therefore the 495 failure displacement largely decreases with the increase of the reservoir depth. In this 496 case, an increase of 20% of the depth would have the same effect than an increase of the 497 shear modulus by a factor of two (Figure S1 - Supplementary material). Uncertainties of 498

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failure displacements due to reservoir depth are therefore very similar to the uncertainties
 already deduced from the shear modulus (Figure 8).

At Sinabung, the observed displacement of 13 cm (prior to the 2010 eruption) is reached 501 under zero pore-fluid pressure conditions for reservoirs with 350-640 m radius and under 502 lithostatic pore-fluid pressure conditions for reservoirs with 520-800 m radius. The same 503 failure displacement can be produced by a range of pore-fluid pressure conditions. This 504 shows that the interpretation of the observed inflation in terms of the fluid pressure 505 conditions (assuming that there was no inflation prior to 2007, i.e. that it equals the 506 failure displacement) would require information on the reservoir radius and the shear 507 modulus. 508

Agung inflated by 16 cm but there was no eruption, which suggests that inflation remained below the failure displacement. Using Figure 8b we obtain a lower bound of the reservoir radius. Assuming a shear modulus of 0.5 G_s , we find that Agung's reservoir radius must be larger than 560 and 1220 meter for zero and lithostatic pore-fluid pressure conditions, respectively.

Okmok inflated by 88 cm between the 1997 and 2008 eruptions. The models show that under zero pore-fluid pressure conditions such failure displacement can be reached for reservoirs with radii between 600 and 950 m and under lithostatic pore-fluid pressure conditions for radii between 1050 and 1550 m. *Fournier* [2008] used GPS data and thermodynamic models to constrain the radius of the reservoir to be between 1 and 2 km. Combined with our modeling results, this would suggest lithostatic pore-fluid pressure conditions for this volcano.

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Westdahl has inflated by 25 cm since the 1991-1992 eruption without any new eruption 521 at the surface. As for Agung, this observation may suggest a combination of pore-fluid 522 pressure conditions and reservoir radius so that the failure displacement is above this 523 value. Using Figure 8d, we find that the pore-fluid pressure conditions should be lower 524 than lithostatic and the reservoir radius must be larger than 700 m. However, the caveat 525 for this interpretation is a seismic swarm in January 2004 [Neal et al., 2005], which could 526 indicate that the system had reached a stress state sufficient to break rock after only 527 20 cm of inflation. The swarm could represent a failed eruption (tensile failure of the 528 reservoir wall without propagation of the intrusion to the surface). From Figure 8d, we 529 find that for $P_p=0$ and $G=0.5~G_s$, a 850 m radius reservoir can produce the observed 530 failure displacement of 20 cm. For lithostatic pore-fluid pressure conditions, the failure 531 displacements modeled are always less than 20 cm, which can not explain the failed 532 eruption. 533

To summarize, for shallow reservoirs (less than 1 km), such as Sinabung, it is impossible to discriminate between the two pore-fluid pressure assumptions as failure overpressures are similar. However, for deeper magma reservoirs, the difference between failure displacements becomes significant. At Agung, the absence of eruption indicates that the radius of the reservoir must be larger than 560 m. At Okmok, the 2008 eruption seems to be associated with high pore-fluid pressure conditions whereas the failed eruption at Westdahl would suggest pore-pressure conditions much lower than lithostatic.

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5. Discussion

5.1. Influence of magma reservoir, volcanic edifice and pore-fluid pressure on failure conditions

Table 3 summarizes the main results of the parametric study (section 3) on the failure overpressure. An initial model without edifice with a magma chamber with R=1000 m at $H_t=-2000$ m is given as a reference. As the depth of the reservoir decreases, the failure overpressure decreases, which promotes the initiation of magma intrusions. The effect is nearly negligible for lithostatic pore-fluid pressure (a few MPa), but is significant for zero pore-fluid pressure as a 1 km reduction in reservoir depth leads to a decrease of the failure overpressure by 60 MPa.

The load of the volcanic edifice also affects the failure conditions. A 1250 m high 548 edifice with 5000 m radius reduces the failure overpressure by about 15 MPa from the 549 reference model for both pore-fluid pressure conditions. Later, when the edifice widens, 550 the failure overpressure increases (by 5 MPa for a 8000 m radius). When the edifice 551 collapses and/or a caldera forms, the load of the edifice is suppressed and the failure 552 overpressure is similar to the reference model. The effect of stress perturbations, such as 553 the construction/destruction of an edifice, on failure overpressure is independent of the 554 value of the pore-fluid pressure. It means that the studies focussing on the influence of 555 external stress changes on reservoir failure do not need to take into account the pore-fluid 556 pressure conditions. 557

For lithostatic pore-fluid pressure, the failure overpressure is more sensitive to edifice loading than to reservoir depth. Indeed, the minimum failure overpressure is associated with the small edifice case (* in Table 3). In contrast, for zero pore-fluid pressure, the

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failure overpressure is more sensitive to reservoir depth than to edifice loading. The minimum failure overpressure is found for a reservoir depth of 1 km (* in Table 3).

Although both reservoir depth and edifice loading have an effect on the failure over-563 pressure, the strongest effect is the pore-fluid pressure itself. For the reference model, 564 the failure overpressure decreases from 132 to 19 MPa for a pore-fluid pressure increases 565 from 0 to P_L . The effect would even be larger for deeper magma reservoirs. Our study 566 underlines that the effect of the pore-fluid pressure on the failure overpressure of spherical 567 reservoirs is an order of magnitude larger than stress perturbations due to loading. The 568 estimation of the overpressure to initiate an intrusion therefore requires knowledge about 569 the pore-fluid pressure conditions and the reservoir depth. 570

5.2. Model assumptions and limitations

In our study, we have neglected the anelastic effects associated with visco-elastic rheol-571 ogy, which describes the response of large and long-lived silicic magmatic systems [Jellinek 572 and DePaolo, 2003; Simakin and Ghassemi, 2010; Gregg et al., 2012; de Silva and Gregg, 573 2014]. Studies have been conducted for Campi Flegrei [Bonafede et al., 1986; Dragoni 574 and Magnanensi, 1989] and Long Valley [Newman et al., 2001, 2006]. Visco-elasticity 575 affects both ground deformation and the conditions for failure of the reservoir. A pressur-576 ized magma reservoir embedded in a visco-elastic medium will be associated with more 577 surface displacement than one embedded in an elastic medium due to the viscous relax-578 ation of the rocks. Following eruptions, visco-elasticity may lead to deflation, even if the 579 magma chamber is replenished [Segall, 2016]. In addition, heated rocks become ductile 580 and can support larger stress without fracturing [Jellinek and DePaolo, 2003; Greqq et al., 581 2012]. Gregg et al. [2012] demonstrate that visco-elasticity has little effect on the failure 582

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⁵⁸³ overpressure for small reservoirs with volume less than a hundred cubic kilometer (which ⁵⁸⁴ corresponds to a radius of almost 3 km). The reservoirs of Okmok, Sinabung and Agung ⁵⁸⁵ are located at depths shallower than 3 km. Westdahl has a deeper source (6 km), but ⁵⁸⁶ there is no evidence for a large magma reservoir. It is unlikely that the reservoir volumes ⁵⁸⁷ of the four volcanoes studied are larger than 100 km³, strongly suggesting that the elastic ⁵⁸⁸ assumption is valid. In such assumption, the conditions of failure discussed in our study ⁵⁸⁹ do not depend on the rate of ground deformation.

We have also neglected the effect of pore-fluid pressure on ground deformation estimation. In our modelling, host rock medium behaves elastically as pore pressure effect is only considered at the vicinity of the reservoir. This assumption is valid if we consider that the accumulation of fluid is localized around magma reservoirs. In this case, the poro-elastic medium will only be a ring around the magma reservoir.

Previous studies have already shown that ellipticity of the reservoir influences the failure conditions both in location [*Grosfils*, 2007] and amplitude [*Albino et al.*, 2010]. For example, for oblate ellipsoid, the failure overpressure is smaller compared to spherical reservoir, because tensile stress concentrates at the extremity of the horizontal axis, where the curvature is highest. As a consequence, the failure displacement would also be smaller. Only at Okmok, *Lu et al.* [2010] found from the inversion of InSAR data an ellipticity ratio of 1.04, which nearly corresponds to a sphere.

⁶⁰² Our failure models provide the overpressure for the failure of a magma reservoir. How-⁶⁰³ ever, reservoir failure does not necessarily produce an eruption, as new intrusions can be ⁶⁰⁴ stalled at depth due to a decrease in magma supply, magma freezing due to slow ascent, ⁶⁰⁵ viscosity increases by magma degassing and heat loss or density barriers in the crust [*Gud*-

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mundsson, 2002; Taisne et al., 2011; Moran et al., 2011]. As mentioned above, the 2004
Westdahl seismic swarm could represent a failed eruption for which the overpressure was
not sufficient to propagate the intrusions to the surface. Magma propagation is a complex
problem (see *Rivalta et al.* [2015] for a review) and is not yet considered in our models.

5.3. Pore-fluid pressure conditions around magma reservoirs

Experimental rock mechanics predict that the brittle frictional strength linearly in-610 creases with depth in the upper crust [Brace and Kohlstedt, 1980]. Such linear relation-611 ship is based on the assumption of hydrostatic pore-fluid pressure and implies that the 612 crust is close to a critical state of failure. This is in good accordance with stress data 613 from deep boreholes such as the KTB borehole in Germany [e.g., Townend and Zoback, 614 2000; Zoback, 2010]. The pore-fluid pressure is usually considered to be in a hydrostatic 615 equilibrium equal to the weight of a column of water, $P_H = \rho_H gz$ with ρ_H the density of 616 water. Zoback and Townend [2001] suggested that hydrostatic pore-fluid pressure could be 617 sustained to a depth of as much as 12 km. However, in particular contexts, the pore-fluid 618 pressure can be in excess of hydrostatic [e.g., Moos and Zoback, 1993]. Suprahydrostatic 619 pore-fluid pressure can be due to an under-compaction during rapid burial of sediments, 620 lateral compression, release of water from minerals, or expansion of the fluid volume 621 [Hantschel and Kauerauf, 2009]. Evidence for suprahydrostatic pore-fluid pressure was 622 also found around magmatic intrusions, mud volcanoes, hydrothermal vents, or faults, 623 showing that pore-fluid pressure is spatially heterogeneous [Jamtveit et al., 2004]. Under 624 undrained conditions, the pore-fluid pressure can be between hydrostatic and lithostatic. 625 Under drained conditions with the fluids escaping from the pores, the pore-fluid pressure 626 can be lower than hydrostatic. 627

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There is little information about the pore-fluid pressure surrounding magma reservoirs. 628 If fluids originating from the magma, the pore-fluid pressure in the rock adjacent would be 629 similar to the magma pressure. Over a narrow zone of a few meters to tens of meters the 630 fluid pressure decreases with a steep gradient to hydrostatic or sub-hydrostatic, depending 631 on depth and the confining pressure and whether a hydrothermal system exists. Ductile 632 flow near the brittle-plastic transition could act to reduce the permeability of the silicic 633 rock, potentially providing a self-sealing mechanism [Fournier, 2007]. For Long Valley 634 Caldera, the variability of the stress directions constrained by both borehole breakouts 635 and earthquake focal mechanisms suggest near-lithostatic pore-fluid pressure conditions 636 [Moos and Zoback, 1993]. 637

Therefore, the two approaches for the failure of magma reservoirs described in sec-638 tion 2.1 are both correct, but correspond to different drainage conditions [Grosfils et al., 639 2015; Gerbault, 2012; Gerbault et al., 2012]. The failure models discussed by Tait et al. 640 [1989], Gudmundsson [2002] and Pinel and Jaupart [2005] considered the host rock as 641 an undrained medium with lithostatic pore-fluid pressure. Grosfils [2007] considers a 642 drained medium with zero pore-fluid pressure where all the fluids have escaped from the 643 rock pores. These two approaches are end-members for the range of possible pore-fluid 644 pressure conditions. 645

At Okmok caldera, the inter-eruption displacement together with independent information about the size of the magma reservoir suggests near-lithostatic pore-fluid pressure whereas the inflation at Westdahl without eruption at the surface suggests pore-fluid pressures significantly lower than lithostatic. Knowing the failure pressure, we can derive the critical volume change required before an eruption. Considering lithostatic pore pressure,

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the total volume change at Okmok before an eruption is 13.5×10^6 m³. Under zero pore 651 pressure, the total volume change at Westdahl before an eruption is 52.3×10^6 m³. Due 652 to the difference of pore pressure conditions, the failure of Westdahl's reservoir requires 653 a volume change four times larger than the one required for the failure of Okmok's reser-654 voir. Under the assumption that both shallow reservoirs are supplied at the same magma 655 supply rate from a deeper source, it means that the frequency of failure should be four 656 times higher at Okmok in comparison with Westdahl. This is in accordance with the erup-657 tion records that reported 11 confirmed eruptions at Okmok and 3 eruptions at Westdahl 658 between 1900-2017. Pore pressure difference can be therefore an explanation for the dif-659 ference of eruption frequency between these two Aleutian volcanoes. The development of 660 high pore pressure at Okmok promotes the failure of the reservoir and the occurrence of 661 frequent intrusions of small volume (Figure 9a). Under low pore-fluid pressure conditions 662 such as at Westdahl, the failure of the reservoir requires a large volume change, which 663 could explain the low frequency of eruptions (Figure 9b). 664

The importance of pore-fluid pressure changes for earthquake generation is well-665 established [Bell and Nur, 1978; Talwani and Acree, 1984; Parotidis et al., 2003; Shapiro 666 et al., 2003; Zoback and Gorelick, 2012]. An increase of pore-fluid pressure in the crust 667 reduces the normal stress on faults, which favors Coulomb shear failure. It has been 668 shown that the increase of pore-fluid pressure produced by heavy rainfall events (mon-669 soons, typhoons or hurricanes) can trigger earthquakes (see *Costain and Bollinger* [2010]; 670 Hainzl et al. [2006]). Our study shows that the pore-fluid pressure also affects the mode 671 of transport of the magma by playing a role in the failure of magma reservoirs. In theory, 672 a pore-fluid pressure increase could trigger an eruption without any increase of the reser-673

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voir pressure, which may be an explanation why some eruptions occur without significant pre-eruptive inflation.

6. Conclusions

(1) We show that the two commonly used approaches to investigate the failure of magma reservoirs [*Gudmundsson*, 2012; *Grosfils et al.*, 2015] are end-members in a framework that accounts for the pore-fluid pressure conditions in the host rock. The pore-fluid pressure around the reservoir has a strong influence on the magma overpressure required for tensile failure of the reservoir wall. It is stronger than the influence of the depth of the reservoir or the loading stress of the volcanic edifice.

(2) Whereas the failure overpressure is dependent on the pore-fluid pressure conditions, the changes of the failure overpressure due to stress perturbations (e.g. growth of an edifice, caldera formation) are independent of the pore-fluid pressure conditions.

(3) The ground surface inflation due to reservoir pressurization depends on the reservoir location, geometry and elastic properties of the rock. The interpretation of geodeticallydetected inflation in terms of eruption potential thus requires knowledge about (i) the pore-fluid pressure conditions in the vicinity of a magma reservoir, (ii) the reservoir depth, (iii) the reservoir radius, and (iv) the shear modulus of the surrounding host rock.

⁶⁹⁰ (4) From the four volcanoes studied, the inferred pore-fluid pressure conditions are ⁶⁹¹ likely supra-hydrostatic for the two erupted volcanoes (Sinabung and Okmok) and sub-⁶⁹² hydrostatic for the non-erupted volcanoes (Agung and Westdahl). High pore-fluid pressure ⁶⁹³ conditions favor the initiation of intrusions whereas low pore-fluid pressure conditions ⁶⁹⁴ make the initiation of intrusions difficult and favor the growth of reservoirs.

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$\overline{\nu}$	Poisson's ratio	0.25
T_s	Tensile strength [MPa]	10
$ ho_r$	Rock density $[kg.m^{-3}]$	2800
<u>g</u>	Constant gravity $[m.s^{-2}]$	9.81

Table 1.Model parameters and variables.Parameters

Variables

\overline{R}	Reservoir radius [m]
H_t	Reservoir top depth [m]
H_c	Reservoir center depth [m]
R_e	Edifice radius [m]
H_e	Edifice height [m]
G	Shear modulus [GPa]
$ \begin{array}{c} \Pi_t \\ \Pi_c \\ R_e \\ \Pi_e \\ G \\ \end{array} $	Reservoir top depth [m] Reservoir center depth [m] Edifice radius [m] Edifice height [m] Shear modulus [GPa]

 Table 2.
 Model parameters used for studied cases (see Figure 6b)

Volcano name	${f Magma\ reservoir^a}$		Volcanic $edifice^{b}$			
	R [m]	H_c [m]	R_e [m]	H_e [m]		
Sinabung	100-800	900	2300	1250		
Agung	100-1800	1900	4700	1800		
Okmok	100-2000	3000	12500	500		
Westdahl	100-2000	6000	12500	1600		

^a Reservoir depths taken from *Chaussard et al.* [2013] and *Lu and Dzurisin* [2014]. Values

are relative to the base of the volcano, which is assumed to be 0.7 km for Sinabung, 0.5 km for

Agung, and 0 km for Okmok and Westdahl.

^b Calculated from the SRTM DEM.

Table 3. Summary of how failure overpressures of a spherical magma reservoir vary with reservoir depth, edifice loading and pore-fluid pressure. The initial model is without topography and given as a reference. In the loading models, the size and the depth of the reservoir are the same as the initial model. The symbol * indicates the minimum value for each pore-fluid pressure

conditions.					
Model configuration	Variables [m]	Failure overpressure [MPa]		N° Figure	
		$P_p = P_L$	$P_p = 0$		
Reference model	$R=1000 H_t=-2000$	19	132	4	
Reservoir depth decrease	$R=1000 H_t=-1000$	17	71^{*}	4	
Edifice loading					
Small edifice	$R_e = 3000 \ H_e = 1250$	5*	116	4	
Large edifice	$R_e = 8000 \ H_e = 1250$	11	122	5	
Caldera	$R_e = 8000 \ H_e = 500$	17	128	5	



Figure 1. Mechanical model used to calculate the failure overpressure required to initiate an intrusion: a) without edifice and b) with edifice. In a) the stress field is lithostatic with $\sigma_r = \sigma_{phi} = \sigma_z = P_L$. In b) the pre-lithostatic stress field is modified by the edifice loading. $\sigma_z > \sigma_r = \sigma_{phi}$ with $\sigma_z = P_L + (\rho_r g H_e) \frac{R_e - r}{H_e}$ below the edifice.

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Figure 2. Overpressure required to initiate tensile fractures as a function of the angle θ in the case of a spherical reservoir (R=1000 m, H_t =-2000 m) for zero pore-fluid pressure (green lines) and lithostatic pore-fluid pressure (red lines). Solid lines: without edifice; dashed lines: with conical edifice (R_e =3000 m, H_e =1250 m). Here we assume T_s =10 MPa and ρ_r =2800 kg.m⁻³; dotted black lines: analytical solutions 2($P_L + T_s$) and 2 T_s . For each model, the failure overpressure ΔP_f is the local minimum showed by the dots. The location of the angle of failure, θ_f , for the different cases are reported on the right sketch.

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Figure 3. Normalized failure overpressure $k(\theta_f)$ (left) and location of the failure at the wall θ_f (right), as function of the radius and the top depth of a spherical reservoir embedded in an elastic half-space subject to a lithostatic stress field (Figure 1a) for (a,b) lithostatic pore-fluid pressure and (c,d) zero pore-fluid pressure. Numbers are non-normalized overpressure values ΔP_f , for R=1000 m and $H_t=[-1000, -3000, -5000]$ m, using $T_s=10$ MPa and $\rho_r=2800$ kg.m⁻³.



Figure 4. Failure overpressure considering the topographic loading of a fixed edifice (R_e =5000 m and H_e =1250 m). The final ΔP_f is a summation of the previous failure overpressure without edifice (Figure 3) and a term δP . Calculation is done for lithostatic pore-fluid pressure (a,b,c) and for zero pore-fluid pressure (d,e,f). White lines indicate depths where ΔP_f and δP are minimum.



Figure 5. Normalized failure overpressure of the reservoir as a function of the radius and the height of the edifice for a spherical magma reservoir (R=1000 m, H_t =-2000 m) for a) lithostatic pore-fluid pressure and b) zero pore-fluid pressure. c-d) The profiles A-B and C-D show ΔP_f as a function of R_e (H_e =1500 m) and H_e (R_e =5000 m), respectively.



Figure 6. a) Geographical location of the four volcanoes studied. b) E-W profiles showing the topography of the edifices (deduced from the SRTM DEM) and the depth of the reservoirs (inferred from InSAR time series). In addition, the surface topography used in our model is shown by dashed lines.

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Figure 7. Time series of vertical displacement at Sinabung, Agung (modified from Fig. 5 and 7 of *Chaussard et al.* [2013]), Okmok and Westdahl (modified from Fig. 6.98 and 6.142 of *Lu and Dzurisin* [2014]). Red vertical lines underline eruptions and the blue vertical line corresponds to a seismic swarm. On each plot, the maximal displacements inferred from the time series are indicated.



Figure 8. Failure displacements calculated for a) Sinabung, b) Agung, c) Okmok and d) Westdahl volcanoes as a function of the reservoir radius and the shear modulus for zero porefluid pressure (green shaded area) and lithostatic pore-fluid pressure (red shaded area). The center line of each area corresponds to the displacements associated with 0.5 G_s . Lower bound and upper bound are respectively for G_s , and $0.25G_s$ as show in panel b). Horizontal lines indicate for each volcano the cumulative displacements obtained from the InSAR time series (Figure 7).



Figure 9. Sketch explaining the difference of eruptive behavior based on the pore-fluid pressure conditions of the host rock: a) a shallow magma reservoir embedded in a high pore-fluid pressure host rock promotes the initiation of a magma intrusion, which may lead to an eruption; b) a deep magma reservoir within a low pore-fluid pressure host rock favors the expansion of the reservoir rather than the initiation of an intrusion.