

Extensive study of electron acceleration by relativistic surface plasmons

G. Cantono, A. Sgattoni, L. Fedeli, D. Garzella, F. Réau, C. Riconda, A. Macchi, and T. Ceccotti

Citation: *Physics of Plasmas* **25**, 031907 (2018); doi: 10.1063/1.5017706

View online: <https://doi.org/10.1063/1.5017706>

View Table of Contents: <http://aip.scitation.org/toc/php/25/3>

Published by the [American Institute of Physics](http://www.aip.org)

Articles you may be interested in

[Surface plasmons in superintense laser-solid interactions](#)

Physics of Plasmas **25**, 031906 (2018); 10.1063/1.5013321

[Plasmon resonances, anomalous transparency, and reflectionless absorption in overdense plasmas](#)

Physics of Plasmas **25**, 031904 (2018); 10.1063/1.5023140

[Theoretical foundations of quantum hydrodynamics for plasmas](#)

Physics of Plasmas **25**, 031903 (2018); 10.1063/1.5003910

[Wave propagation in and around negative-dielectric-constant discharge plasma](#)

Physics of Plasmas **25**, 031901 (2018); 10.1063/1.5009413

[Preface to Special Topic: Plasmonics and solid state plasmas](#)

Physics of Plasmas **25**, 031701 (2018); 10.1063/1.5026653

[The impact of dissipation on plasmonic versus non-collective excitation](#)

Physics of Plasmas **25**, 031905 (2018); 10.1063/1.5018404

PHYSICS TODAY

WHITEPAPERS

ADVANCES IN PRECISION
MOTION CONTROL

Piezo Flexure Mechanisms
and Air Bearings

READ NOW

PRESENTED BY

PI

Extensive study of electron acceleration by relativistic surface plasmons

G. Cantono,^{1,2,3,4,a)} A. Sgattoni,^{3,5,6} L. Fedeli,⁷ D. Garzella,¹ F. Réau,¹ C. Riconda,⁵
 A. Macchi,^{3,4} and T. Ceccotti¹

¹LIDYL, CEA, CNRS, Université Paris-Saclay, CEA Saclay, 91191 Gif-sur-Yvette, France

²Université Paris Sud, Paris, 91400 Orsay, France

³National Institute of Optics, National Research Council (CNR/INO) A. Gozzini unit, 56124 Pisa, Italy

⁴Enrico Fermi Department of Physics, University of Pisa, 56127 Pisa, Italy

⁵LULI-UPMC: Sorbonne Universités, CNRS, École Polytechnique, CEA, 75005 Paris, France

⁶LESIA, Observatoire de Paris, CNRS, UPMC: Sorbonne Universités, 92195 Meudon, France

⁷Department of Energy, Politecnico di Milano, 20133 Milano, Italy

(Received 29 November 2017; accepted 14 February 2018; published online 30 March 2018)

The excitation of surface plasmons with ultra-intense ($I \sim 5 \times 10^{19} \text{ W/cm}^2$), high contrast ($\sim 10^{12}$) laser pulses on periodically modulated solid targets has been recently demonstrated to produce collimated bunches of energetic electrons along the target surface [Fedeli *et al.*, Phys. Rev. Lett. **116**, 015001 (2016)]. Here, we report an extensive experimental and numerical study aimed to a complete characterization of the acceleration mechanism, demonstrating its robustness and promising characteristics for an electron source. By comparing different grating structures, we identify the relevant parameters to optimize the acceleration and obtain bunches of $\sim 650 \text{ pC}$ of charge at several MeV of energy with blazed gratings. *Published by AIP Publishing.* <https://doi.org/10.1063/1.5017706>

I. INTRODUCTION

Plasmonics in the relativistic regime is a daring but largely unexplored domain. Exploiting the unique properties of light confinement^{1,2} and field concentration³ achieved with the excitation of surface plasmons (SPs) on metallic nanostructures could open new schemes of laser-plasma interaction at high field intensity and the possibility to improve laser-based radiation sources, which would notably profit from enhancing the laser-target coupling.

Indeed, SPs have been studied for the last few decades to efficiently increase the absorption of the laser energy by an overdense plasma. Exciting SPs at high laser intensities^{4,5} can generate very strong fields close to the surface and, in turn, produce a numerous population of highly energetic electrons and enhance the emission of both protons^{6,7} and extreme ultraviolet (XUV) harmonics from the target.⁸

Although promising, there is no decisive theory of SP excitation by ultra-intense laser pulses at the interface of a solid plasma, whose strongly non-linear response cannot be described by a univocal dielectric function because of the relativistic effects.⁹ Nevertheless, numerical simulations^{10,11} soon encouraged the possibility to excite SPs on grating targets irradiated at relativistic intensities at the proper resonant angle predicted by the linear, non-relativistic theory.¹² Yet, the first experiments on this topic^{13–15} were limited to intensities far below 10^{18} W/cm^2 , because the poor temporal contrast inherent to powerful chirped pulse amplification (CPA) laser systems did not ensure the survival of the grating surface, irradiated by the pulse pedestal before the arrival on target of the main intensity peak. The successful development of pulse cleaning techniques, such as the plasma mirror,¹⁶ recently enabled the experimental study of plasmonic effects at relativistic laser intensities.

In this context, recent experiments reported not only SP-enhanced proton acceleration⁷ but also the remarkable acceleration of electron bunches along the target surface directly driven by the SP electric field.^{17,18} This process, which had been only partly investigated by previous numerical simulations,^{10,11} has been thoroughly addressed in a series of experiments performed at CEA Saclay.¹⁹

In this paper, we report the exhaustive description of both experimental and numerical results, aiming to demonstrate the peculiar features of the electron emission and its dependence on some of the target and laser parameters. These results emphasize the robustness of the acceleration mechanism and encourage the development of a compact electron source at few MeV of energy, with potential applications for ultra-fast electron diffraction,^{20,21} photo-neutron generation,²² or enhanced emission of THz radiation.²³

II. SURFACE PLASMONS FOR ELECTRON ACCELERATION

SPs are normal modes of the electronic oscillations at a sharp metal-dielectric interface. They can be excited by an external laser pulse on a periodically modulated target that achieves phase-matching with the incoming electromagnetic (EM) wave.^{12,18} In the relativistic regime, the solid target is ionized within a laser cycle, allowing the rest of the laser pulse to interact with an overdense plasma. A short pulse duration (\sim tens of fs) and high contrast are required to avoid both the early smoothing and the following hydrodynamic expansion that otherwise would destroy the modulated surface of the target. If this one consists in a diffraction grating, resonance occurs when the laser pulse irradiates the grating at a specific incidence angle ϕ_R , related to the grating period Λ by the condition:

^{a)}Electronic mail: giada.cantono@cea.fr

$$\sin(\phi_R) = \pm \sqrt{\frac{1 - \omega_p^2/\omega^2}{2 - \omega_p^2/\omega^2}} + n \frac{\lambda}{\Lambda}. \quad (1)$$

In this expression, ω_p is the plasma frequency, ω and λ are the frequency and wavelength of the laser pulse, and n is an integer ($0, \pm 1, \dots$). The first term on the right-hand side represents the SP dispersion relation ck_{SP}/ω for a cold, collisionless plasma²⁴ derived from the linear theory. However, Eq. (1) can be reduced to $\sin(\phi_R) = \pm 1 + n\lambda/\Lambda$ in the limit of solid targets, since $\omega_p \gg \omega$ holds due to the high electron density. Measuring the angles from the target normal as indicated in Fig. 1(a), this expression reminds of the well-known grating equation, relating the incidence at ϕ_R of a monochromatic beam to the propagation of the n -th diffraction order along the grating surface. Indeed, SPs are particular solutions of the EM field diffracted by a grating, characterized by the field confinement in the direction perpendicular to the interface.²⁵

Electrons can be accelerated along the grating by the component of the SP electric field that is parallel to the surface, E_{\parallel} . Efficient acceleration occurs on the vacuum side of plasma-vacuum interface, since the SP field is rapidly evanescent inside the plasma: electrons are pulled into the vacuum region by the transverse component of the electric field, E_{\perp} , then self-injected in the SP field thanks to the $\mathbf{J} \times \mathbf{B}$ force directed along the surface.^{17,26} An example of electron trajectory super-imposed on the temporal evolution of electric field during the SP excitation is given in the [supplementary material](#).

The phase velocity of the SP $v_{\phi} = \omega/k_{SP}$ does not depend on the SP intensity, and for $\omega_p \gg \omega$, it is $v_{\phi} \sim c$. Therefore, relativistic laser intensities are required to accelerate the electrons close to v_{ϕ} . Then, depending on the initial conditions,^{17,26} an electron can attain a kinetic energy $W \simeq m_e c^2 \gamma_{\phi} a_{SP} \gg m_e c^2$, where $\gamma_{\phi} = (\omega_p^2/\omega^2 - 1)^{1/2}$ is the relativistic factor associated with the phase velocity of the SP and $a_{SP} = eE_{\perp}/(m_e \omega c)$ is the normalized electron momentum in the transverse electric field of the SP (knowing that $E_{\perp} = \gamma_{\phi} E_{\parallel}$). Since $v_{\phi} \sim c$ and the evanescence length on the vacuum side $L_{e,v} = (k_{SP}^2 - \omega^2/c^2)^{-1/2}$ exceeds the laser wavelength λ , the electron can remain in phase with the SP for a long time, despite being steered away from the surface by E_{\perp} . Consequently, acceleration lengths $L_{acc} = W/(eE_{\parallel}) = \gamma_{\phi}^2/k$ can be achieved.¹⁹

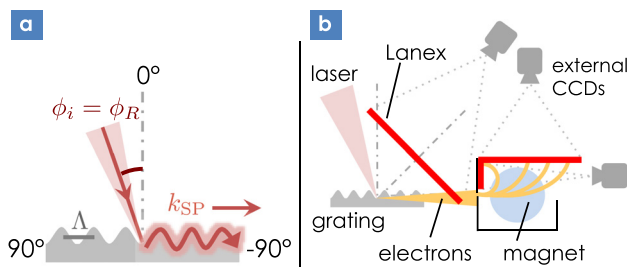


FIG. 1. (a) Scheme of the SP excitation on a grating, with the sign convention used in the text. The incidence angle ϕ_i corresponds to the resonant angle fixed by Eq. (1). (b) Layout of the experiments performed at CEA Saclay. In the spectrometer, the electron trajectory describing half a circle corresponds to 1.4 MeV of energy. The Lanex inside the yoke, reserved for electrons below this value, never produced a detectable signal.

Notice that because of self-injection, a large amount of charge can be synchronized to the accelerating field of the SP and reach high energies. In this way, this acceleration mechanism quite differs from the dielectric laser acceleration²⁷ or from the inverse Smith-Purcell effect,²⁸ where an external electron beam injected at grazing incidence on a periodic structure can be accelerated by the field induced on the micro-structure by a low-intensity, ps laser pulse. These processes do not involve the excitation of a SP and acceleration is achieved only if the electron beam is carefully synchronized to laser field. In the inverse Smith-Purcell effect, such synchronous condition should not be mistaken with the resonant condition Eq. (1), which derives from the phase-matching of the SP and the laser pulse and does not relate to the velocity of the accelerated electrons. Moreover, the inverse Smith-Purcell acceleration requires the laser beam to hit the grating at skew incidence,²⁹ whereas tilting the grating lines or varying the incidence angle spoils the electron acceleration in our case.

For a comparison with the experimental measurements reported in the following, we can derive E_{\perp} by assuming that the laser energy deposited in the focal spot is entirely yielded to the SP. Despite leading to an overestimation of a_{SP} , this choice is supported by the previous measurements of the target absorption, where values near 100% were reported.^{7,13} In this way, a_{SP} becomes ~ 3 for the peak intensity of the laser system UHI-100 described in Sec. III. Assuming a solid target density of $n_e \sim 400n_c$, the theoretical model predicts a γ_{ϕ} factor of ~ 20 , hence a maximum kinetic energy of $W \sim 30$ MeV. The emission angle, measured on the incidence plane from the grating normal, is expressed¹⁷ by $\tan(\phi) = \gamma_{\phi} \beta_{\phi}$, resulting here in $\sim 87^\circ$. The threshold value $a_{SP} \sim 1$, which was also recovered from 2D simulations,¹⁷ still leads to a maximum electron energy $W \sim 10$ MeV $\gg m_e c^2$.

III. EXPERIMENTAL RESULTS

Experiments were carried out at the Saclay Laser-matter Interaction Center Facility (SLIC) of CEA Saclay (Gif sur Yvette, France). The UHI-100 Ti:Sa laser system delivers 25 fs pulses with ~ 2.5 J of energy before compression. The spectrum is centered at $\lambda \simeq 800$ nm with 80 nm of FWHM bandwidth. A double plasma mirror increases the temporal contrast to 10^{12} and 10^{10} within, respectively, ~ 20 and 5 ps before the pulse peak.³⁰ Wavefront correction is performed by a deformable mirror, allowing the P-polarized beam to be focused on target at $\sim 4.6 \mu\text{m}$ FWHM with a $f/3.75$ off-axis parabola. The energy on the target is estimated to be ~ 700 mJ, corresponding to a peak intensity ranging from 3.4 to 1.7×10^{19} W/cm² depending on the incidence angle ϕ_i , which was varied between 10° and 60° by properly rotating the target along its vertical axis.

We used different types of gratings in order to explore the SP-driven electron acceleration under various conditions. Thin gratings, with a sinusoidal profile, were produced by heat-embossing 13 μm thick MylarTM foils with a metallic master. The grating periods Λ were $1.35\lambda - 2\lambda - 3.41\lambda$ for a resonant angle of, respectively, $15^\circ - 30^\circ - 45^\circ$ according to Eq. (1); these targets are hence referred to as G15, G30, and G45. The groove depth d was, respectively, 170–290–390 nm.

Depending on the grating type and incidence angle, the number of grating periods irradiated at resonance within the focal spot (at $1/e^2$) was, respectively, 7.5–5.5–4. For the resonance at 30° of incidence (i.e., $\Lambda = 2\lambda$), we also employed blazed gratings, (Edmund Optics). They were produced by depositing float glass on a sawtooth master coated with a $\sim 1\ \mu\text{m}$ thick Aluminum layer. The whole thickness of the target was 9.5 mm and five different blaze angles were tested: 4° – 6° – 13° – 22° – 28° with, consequently, a groove depth d of 120–180–365–580 and 700 nm. These targets will be indicated with the acronym BG, followed by the blaze angle (e.g., BG13). In order to clarify the role of the Aluminum coating on the target efficiency, also a thin sinusoidal grating with a period of 2λ was produced on a $12\ \mu\text{m}$ thick Aluminized Mylar foil (i.e., G30_{Alu}). Finally, we irradiated flat Mylar foils of $13\ \mu\text{m}$ thickness for comparison.

The experimental arrangement is illustrated in Fig. 1(b). Electron diagnostics consisted of a scintillating Lanex screen and an electron spectrometer and were designed to record both the spatial and energetic distribution of the electrons emitted in the half-space in front of the target. The Lanex screen ($15 \times 7\ \text{cm}^2$) was tilted by 45° to intercept the electron emission from the tangent to the normal of the target; the distance between the screen and the tangent was 8 cm. A $200\ \mu\text{m}$ thick Aluminum slab was placed in front of the screen to filter out X-rays and electrons below $\sim 150\ \text{keV}$. In the following, the angular directions along the Lanex screen will be indicated as ϕ on the incidence plane and θ in the vertical direction (the azimuthal and polar angle, respectively). The electron spectrometer was aligned 3 cm behind a 2 mm diameter hole drilled in the tangent direction of the Lanex screen. It was formed by a pair of round magnets (0.9 T of magnetic field) and a collimating slit of 1.5 mm, which determined a spectral resolution of $\sim 500\ \text{keV}$ for electron energies of $\sim 10\ \text{MeV}$. The trajectories of electrons above 1.4 MeV of energy were bent by 90° before reaching another Lanex screen protected by $100\ \mu\text{m}$ of Aluminum. Electrons with lower energy were curved back towards a third small Lanex placed inside the yoke, right next to the entrance slit. Throughout the experimental campaign, this third screen never produced a detectable signal, suggesting a negligible amount of electrons below 1.4 MeV. This allowed us to relate the intensity of the signal emitted by the tilted Lanex to the amount of charge reaching its surface, since the energy deposited by electrons in the active layer of the scintillator is independent of their initial energy above 1.5 MeV.³¹ To this end, we calibrated both the Lanex and its optical system with a stable electron source provided by the laser-triggered radio-frequency electron accelerator ELYSE (Orsay, France).

Finally, all diagnostics were mounted on a powered platform which rotated around the chamber center; this allowed us to keep the alignment with the target whenever varying the incidence angle. The signal from the Lanex and electron spectrometer was imaged by 12-bit CCD cameras equipped with 546 nm band-pass filters and fixed outside of the interaction chamber. This implied a non-negligible dependence of the measured signal on the distance and the angle between the CCDs and the detectors. Therefore, a correction factor

was calculated starting from the reference pictures of every position of the rotating platform, to allow for a legitimate comparison between the data acquired on the same points of the Lanex when diagnostics were set at different positions.

A. Electron acceleration for different grating periods

All the gratings irradiated at the expected angle for SP excitation produce an intense, low-divergence electron bunch in the tangent direction, with energies up to $\sim 20\ \text{MeV}$. Combined with the diameter of the focal spot, these energies suggest that accelerating gradients of $\sim \text{TV/m}$ are achieved during the interaction.

Figure 2 presents the electron distribution recorded by the Lanex screen from a G30 irradiated at various incidence angles. The strongest and narrowest emission is found at $\phi_i = \phi_R = 30^\circ$; it extends over $\sim 10^\circ$ from the tangent along ϕ , and over less than $\sim 5^\circ$ along θ . Also, two round regions with a weaker signal are observed in the directions corresponding to the specular reflection of the laser pulse ($\phi = -30^\circ$) and to the first diffraction order of this grating ($\phi = 0^\circ$, i.e., the target normal).¹⁷ Similar holes in the specular direction have been reported in other measurements of laser-driven electrons from solid targets^{32,33} and attributed to the isotropic scattering exerted by the ponderomotive force of the laser pulse. According to this, the hole at the first diffraction order is a convincing evidence of the grating survival to the pulse pedestal, thanks to the high contrast achieved on UHI-100.^{7,17} It is worth mentioning that the flat foil irradiated at the same incidence angle resulted in a ~ 20 times weaker signal, with electrons mainly distributed around the specular direction.¹⁷

For all the other incidence angles, the electron signal is weaker and spread on a larger area. Notice from Fig. 1(b) that large incidence angles require the platform with the diagnostics to rotate farther away from the CCDs; as a consequence, the same portion of the Lanex screen subtends a wider

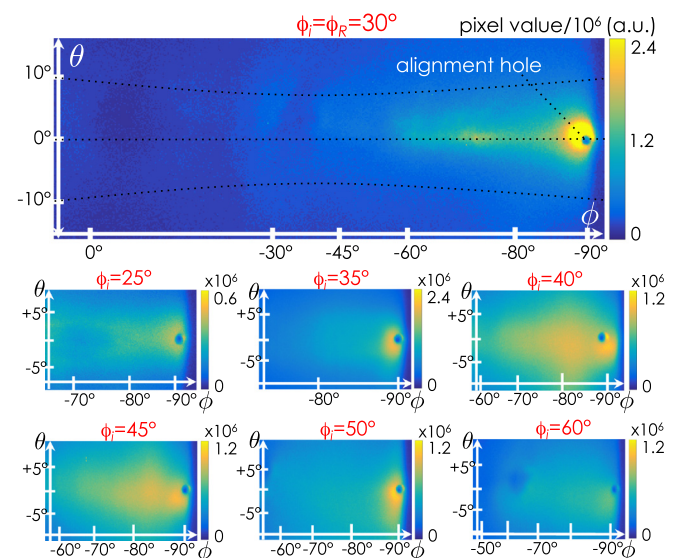


FIG. 2. Electron spatial distribution from a G30 irradiated at different incidence angles. The largest panel shows the emission at the resonant angle $\phi_R = 30^\circ$, over the entire range of ϕ and θ . The angular range is reduced to, respectively, $\sim 30^\circ$ and $\sim 15^\circ$ in the other images. Color bars indicate the signal intensity.

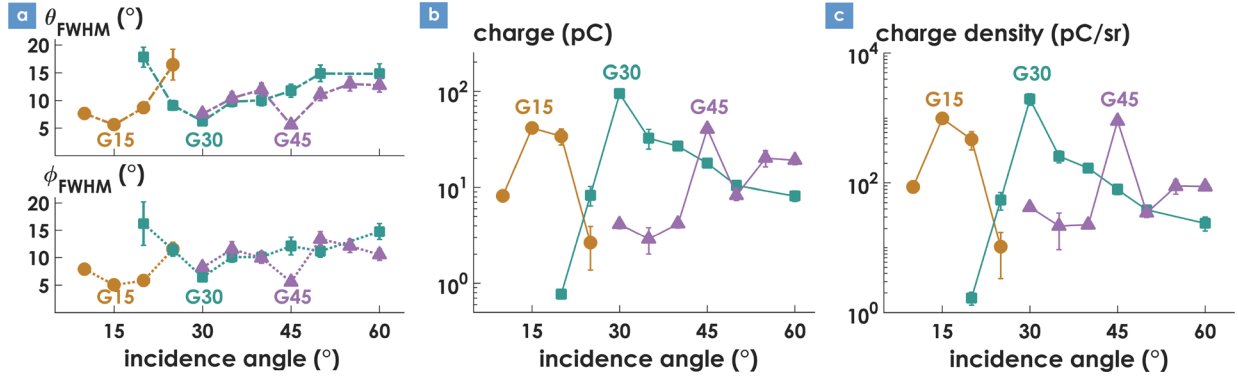


FIG. 3. Properties of the electron bunch measured along the surface of all thin gratings for different incidence angles: (a) divergence along θ and ϕ ; (b) charge; (c) charge density. The most intense and collimated bunch is observed at the resonant angle for SP excitation.

angular range, especially over ϕ , and this partially explains why the signal intensity increases around the tangent at large incidence angles. In principle, this effect could also result from a more efficient vacuum heating absorption;⁴ however, this is in contradiction with the fact that both the measured energetic spectra (compare Fig. 4) and the numerical simulations (presented in Sec. IV) indicate that only low energy electrons (below ~ 5 MeV) are emitted in these cases.

Figure 3 describes the spatial extent and the charge of the electron bunch inferred from the images of the Lanex screen. The emission along the tangent is analyzed for all thin gratings as a function of the incidence angle. Each point represents the average of all shots acquired in the same configuration, with error bars given by the standard error (i.e., the standard deviation normalized by the square root of the number of shots). When necessary, the standard error is replaced by the systematical error performed during the analysis ($\sim 10\%$ of the average); still, in some cases the error bars are hidden by the size of the points shown in the plot.

The angular widths along ϕ and θ are measured on the two orthogonal profiles of the bunch which exhibit the maximum signal. The graph in Fig. 3(a) clearly shows how the electron emission is the less divergent at resonance, with similar FWHM ($\simeq 5^\circ$) for all gratings; the size significantly increases even within $\pm 5^\circ$ of the resonant angle. The charge values reported in Fig. 3(b) are estimated inside the area identified for each incidence angle by the FWHM along ϕ and θ . The role of the SP is remarkable even in a logarithmic

scale, as shown in the graph. Gratings at resonance emit up to 100 pC of charge, at least 3 times more than at other incidence angles. Finally, Fig. 3(c) shows the charge density resulting from the combination of both the size and charge of the electron bunch.

Figure 4(a) compares the energetic spectra obtained from all thin gratings at resonance: no electrons above the noise level are detected below ~ 2 MeV and the largest population is centered around a peak energy E_{peak} ; the maximum energy, E_{max} , is measured where the signal $dN^2/(d\Omega dE)$ is equal to 10% of its value at the peak. Non-Maxwellian distributions are also found when the gratings are irradiated at non-resonant angles, as in Fig. 4(b) for a G30, yet they show fewer electrons and lower energies. The energetic dispersion $\Delta E/E_{\text{peak}} \simeq 1.1$ is constant within 5° around the resonant angle for all gratings (where ΔE is the FWHM around E_{peak}).

The resonant effect is once again visible in Fig. 4(c), where E_{peak} and E_{max} are plotted as a function of the incidence angle. Both the G30 and the G45 exhibit similar values, with the maximum energy at resonance around 18 MeV. The measurements on the G15 at resonance, instead, are supposed to have suffered from an accidental misplacement of the electron spectrometer. In fact, the reference pictures of the diagnostics show that the shots at 15° of incidence were acquired when the rotating platform was not properly aligned to the target surface. Further support of this hypothesis is given by the simulations, where the maximum electron energy does not appear to depend on the grating type.

For comparison, flat foils were irradiated at the incidence angles corresponding to the grating resonances. In this case, there is no electron acceleration in the tangent direction and

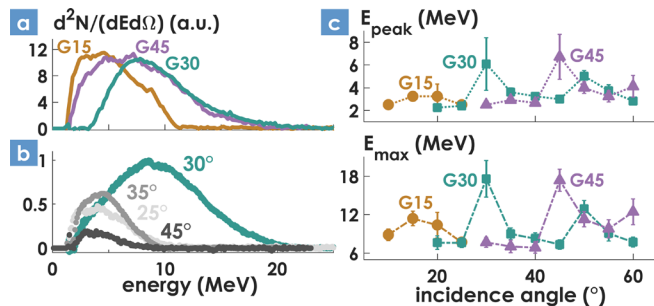


FIG. 4. Energetic distributions of the electrons accelerated along the surface of thin gratings: (a) energetic spectra collected at the resonant angles; (b) energetic spectra from a G30 irradiated at various incidence angles (the spectra are normalized to the peak value of the signal at 30°); and (c) peak and maximum energy for all thin gratings as a function of the incidence angle, emphasizing the effect of the SP excitation at the resonant angles.

TABLE I. Charge and position of the electron bunch emitted from a flat foil (F) around the specular and from a grating (G) along the tangent. The incidence angles correspond to the resonant angles for the gratings. The fluctuations $\Delta\phi$ and $\Delta\theta$ are the standard error of the bunch positions (ϕ , θ) on the dataset.

ϕ_i (deg)	Charge (pC)		$\Delta\theta$ (deg)		$\Delta\phi$ (deg)	
	F	G	F	G	F	G
15	3 ± 1	41 ± 4	2.1	0.7	2.2	0.2
30	4 ± 1	95 ± 5	1.8	0.2	2.8	0.05
45	5 ± 1	40 ± 4	2.3	0.3	2.1	0.1

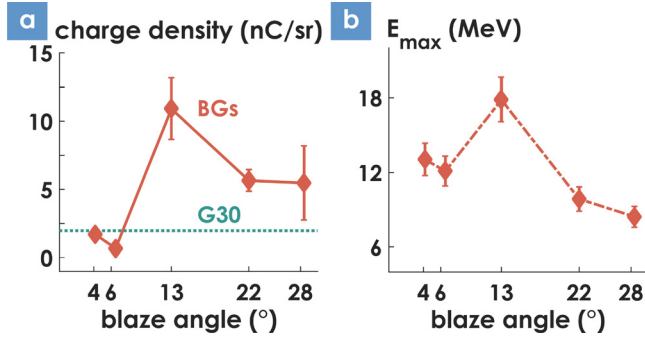


FIG. 5. Charge density (a) and maximum energy (b) of the surface electrons emitted by BGs at resonance. 13° is the optimal blaze angle for the laser wavelength. In (a), the value of charge density obtained with the sinusoidal G30 is added for comparison.

electron bunches of variable size are observed in random positions around the specular reflection of the laser beam. For these bunches, Table I presents the charge values inferred from the images of the Lanex screen, together with the fluctuations of their position in both θ and ϕ directions. These results are compared to the gratings at resonance, which visibly produce ~ 10 times more charge and far more directional electron beams.

Because of the poor reproducibility of the electron emission from flat foils, we did not measure the energetic spectra in the specular direction. Experiments performed with other configurations, involving either very large incidence angles³⁴ or requiring a pre-formed density gradient at the foil surface,³³ have reported the acceleration of electrons in the tangent or specular direction from 2 to 15 MeV.

B. Blazed and aluminized gratings

Commonly used in low field plasmonics, blazed gratings (BGs) are designed to maximize the laser energy concentrated into a specific diffraction order (usually $n = 1$) for a specific wavelength (known as blaze wavelength).³⁵ Ideally, choosing the blaze angle so that the maximum energy is diffracted along the grating surface should maximize the coupling between the laser pulse and the SP. Indeed, with the most suitable BG, we found that the charge in the electron bunch increases by ~ 6 times with respect to the sinusoidal Mylar gratings.

From the efficiency curves reported by Edmund Optics for the BGs tested in the experiments, only the BG13 is

expected to have a high efficiency at the laser wavelength, since its blaze wavelength is close to 800 nm. Figure 5 shows the charge density and maximum energy measured from all the BGs irradiated at resonance (30°), confirming that the SP excitation is indeed optimized in correspondence of the BG13. In particular, the charge density is ~ 5 times higher than what is obtained with the G30, because ~ 660 pC are typically measured in the electron bunch. On the other side, the angular divergence along both θ and ϕ increases (compare Table II). The deterioration of the spatial distribution of the electron bunch is believed to depend of the Aluminum coating of the BGs. This layer could in fact suffer from early ionization by the residual laser pedestal,³² slightly altering the depth and profile of the grating during the interaction.

Further evidence of this effect comes from the measurements on the Aluminized sinusoidal grating (G30_{Alu}), reported in Table II. In particular, electrons are less numerous and slightly more dispersed with respect to the bare G30 described in Sec. III A. Also, the maximum energy is reduced, in contrast with the theoretical model that predicts a growth of the maximum energy following the density increase ($W \propto \sqrt{n_e}$). The experimental results clearly suggest that despite providing a higher electron density, the Aluminum hampers the electron acceleration along the surface. However, this drawback might be mitigated on the BG13 because of both the deeper profile and the presence of the blaze, although the maximum electron energy remains of the same order of what is measured with the G30 and the G45.

The last column in Table II contains the bunch properties observed when the orientation of the BG13 was reversed (i.e., the blaze angle points to the same side of the incident laser beam). Since the sawtooth profile is asymmetric, this change does not displace the diffraction orders (and indeed a bunch is still emitted along the grating surface), but it affects the grating efficiency,³⁶ as clearly demonstrated by the poorer characteristics of the electrons observed in this case.

All these results indicate that the amount of charge and the final electron energy are strongly sensitive to the details of the grating structure, as blazed profiles achieve better results than sinusoidal gratings. Hence, engineering the target surface on a sub-micrometric scale can be exploited to optimize both the interaction and the secondary emissions also in the high intensity regime, even when the target is eventually heated to very high temperatures.

TABLE II. Properties of the electron emission obtained at resonance (30°) with the bare G30 and with the Aluminized gratings (G30_{Alu}, BG13, and BG13rev). The orientation for the BGs follows the sign convention as in Fig. 1(a). The results indicate that the Al coating spoils the electron acceleration, yet the optimal blaze profile in the right orientation accounts for a high amount of charge (bold value).





	G30	G30 _{Alu}	BG13	BG13rev
Al thickness	None	~ 100 nm	$1 \mu\text{m}$	$1 \mu\text{m}$
Profile				
θ_{FWHM} (deg)	6.0 ± 0.5	7.0 ± 0.3	9.3 ± 0.9	11.6 ± 0.2
ϕ_{FWHM} (deg)	6.5 ± 0.5	6.0 ± 0.2	5.4 ± 0.5	5.8 ± 0.1
Charge (pC)	95 ± 5	28 ± 3	660 ± 80	19 ± 1
E_{peak}	6 ± 2	4.2 ± 0.1	7.7 ± 0.8	3.8 ± 0.2
E_{max}	17 ± 3	10.5 ± 0.3	18 ± 2	7.6 ± 0.3

TABLE III. Setup of the 2D PIC simulations.

Parameter	Values
Box size (x, y)	$100\lambda \times 100\lambda$
Spatial resolution $\Delta x, \Delta y$	$\lambda/70, \lambda/40$
Boundaries	Periodic
Target density n_0	$50n_c$
Particles per cell	128 electrons, 25 ions
Target shape	Flat, sinusoidal/blazed grating
Target location (x, y limits)	$[0, \text{thickness}] \times [-50\lambda, 50\lambda]$
Grating depth d	Scan from 0.25λ to 2λ
Target thickness	Scan from 1λ to 5λ
Laser polarization	P
Laser a_0	5
Laser duration τ FWHM	$12\lambda/c$
Laser waist w_0	5λ

IV. NUMERICAL RESULTS

We tested and validated our experimental results with two-dimensional particle-in-cell (PIC) simulations performed with the open source code PICCANTE³⁷ on the HPC cluster CNAF (Bologna, Italy). The 2D geometry is adequate to assess the main features of a surface mechanism such as the SP excitation, since it includes all the fundamental elements of the interaction. Nevertheless, 3D simulations have shown to better reproduce the fine structure of the energetic spectra and to reveal a possible correlation between the electron energy and the emission angle.¹⁷

The relevant parameters of the 2D simulations are reported in Table III. The overdense target is placed at the center of the simulation box, with the irradiated surface at $x = 0$, and extending in the y direction over the whole range $-50\lambda \times 50\lambda$. To relieve the computational load, both the density and thickness of the target are smaller than their experimental values. However, few simulations were performed with $n_0 = 200n_c$ and thicker targets (up to 5λ). As a result of the increased density, the dispersion relation of the SP in Eq. (1) weakly depends on the plasma density, allowing to narrow the

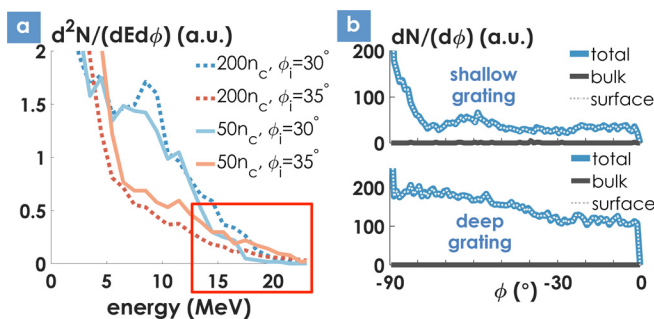


FIG. 6. Evaluation of the initial parameters of the 2D PIC simulations. (a) Energetic spectra of the electrons emitted along the tangent of a G30 irradiated at 30° (blue lines) or 35° (red lines) of incidence, for an initial target density of $50n_c$ (solid lines) or $200n_c$ (dashed lines). Electrons above 17 MeV (within the red box) are suppressed at 35° in case of high density. (b) Spatial distribution of electrons (with energy above 1 MeV) emitted from the surface and the bulk of a 5λ -thick G30 irradiated at resonance. The grooves are 0.25λ (top) and 2λ (bottom) deep; the surface layer includes the whole groove and a further 0.5λ of thickness. Visibly, no electrons come from the substrate.

range of incidence angles for which the electron acceleration takes place. In particular, it was possible to ascribe some energetic electrons, observed in the low density simulations for non-resonant angles, to the target heating rather than to the excitation of a SP, as shown in Fig. 6(a). Simulations with thick targets, instead, demonstrated that the electrons accelerated in the bunch come only from the surface layer of the target, while the electrons from the bulk do not contribute to the spatial emission over the entire ϕ range, as shown in Fig. 6(b).

At the end of the simulations ($t = 55\lambda/c$), the electron phase-space was analyzed to infer the energetic spectrum in the tangent direction (centered at $\phi = \arctan(y/x) = -88^\circ \pm 1^\circ$) and the angular distribution ($-90^\circ < \phi < 0^\circ$, with the same sign convention as in Fig. 1(a)). Only the electrons emitted in front of the target were considered ($-50 < x < d/2$, where d is the groove depth). Target absorption was estimated by comparing the fraction of energy possessed by all the particles in the box to the initial energy of the laser pulse.

A. Role of the grating depth

Due to manufacturing constraints, the thin gratings explored in Sec. III A had different groove depths. The resonance condition in Eq. (1) is valid under the assumption that the groove depth is smaller than the grating period, $d \ll \Lambda$. But even within this limit, the groove depth could have a significant influence on the coupling between the target and the laser pulse, as corrugated and micro-structured targets are generally known to increase the target absorption because of local field enhancement.^{38–40} Therefore, we tested the role of the grating depth by running several simulations, where first we varied the groove depth while keeping the grating period constant.

Figure 7 illustrates how increasing the groove depth spoils the surface electron acceleration, despite increasing the target absorption. In these simulations, the target was a G30 (i.e., $\Lambda = 2\lambda$) irradiated at resonance; the target thickness is indicated next to the curves. Figure 7(a) shows that the number of electrons with energy above 5 MeV emitted along the grating surface drastically decreases when the groove depth is beyond 0.5λ , whereas the absorption, in Fig. 7(b), increases. Both results show that although deep grooves cause the shadow

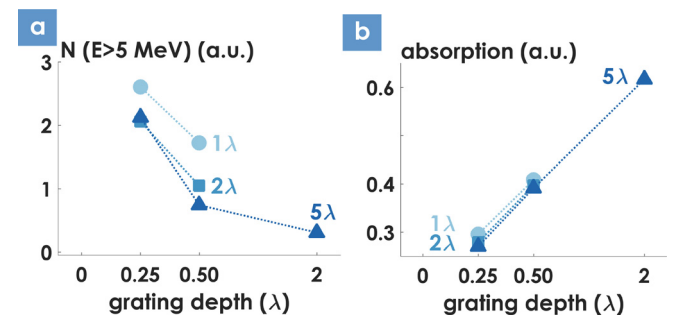


FIG. 7. Effect of increasing the groove depth in a G30 irradiated at 30° : (a) number of electrons beyond 5 MeV accelerated at tangent and (b) grating absorption. Markers, colors, and labels specify the target thickness. Deep grooves reduce the efficiency of the SP excitation, despite increasing the target absorption. Recirculation effects might account for the larger electron number observed with thinner gratings.

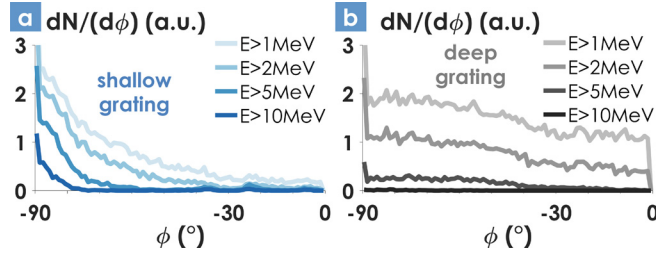


FIG. 8. Spatial distribution of the electron emission, for a G30 irradiated at resonance with different depth-thickness configurations, i.e., $0.25\lambda-1\lambda$ in (a) and $2\lambda-5\lambda$ in (b). The legends report the energy filters applied to the electron population. Only the shallow grating exhibits energetic electron along the surface ($\phi < -80^\circ$).

effect to hamper the SP excitation,¹⁰ geometrical effects are still able to increase the absorption.^{6,7,41}

However, it is worth noticing that the high absorption is largely due to low-energy electrons, as Fig. 8 shows. In fact, the full spatial distribution of the electrons emitted from the deep G30 (Fig. 8(b)) indicates that most electrons are below 5 MeV of energy; the shallow grating, on the contrary, exhibits a distinctive emission in the tangent direction ($\phi \simeq -90^\circ$) of electrons between 5 and 10 MeV (Fig. 8(a)). This allows to exclude that a SP is excited with deep grooves, as confirmed also by analyzing the electron distribution obtained with different incidence angles (not shown here, for brevity).

Since the shadow effect depends on both the grating depth and period, the groove depth where the SP excitation becomes inefficient is expected to be different for each resonant angle investigated in Sec. III A. Indeed, Fig. 9 confirms that each grating requires a specific groove depth to optimize the charge and energy of the SP-accelerated electrons. In these simulations, all gratings were irradiated at resonance, and the groove depth was varied for both the sinusoidal gratings (G15, G30, and G45) and the blazed gratings (in this case, the blaze angle automatically determines the groove depth). Both graphs show that increasing the resonant angle (i.e., the grating period) requires to increase the groove depth; however, the optimal performances of all sinusoidal gratings are comparable, as it was found in the experiment (compare the charge in Fig. 3(b) or the maximum energy in Fig. 4(c)). Moreover, the simulations where we modeled the depth of the sinusoidal gratings with the values as in the experiments confirm that there are no significant differences among the surface electron emission

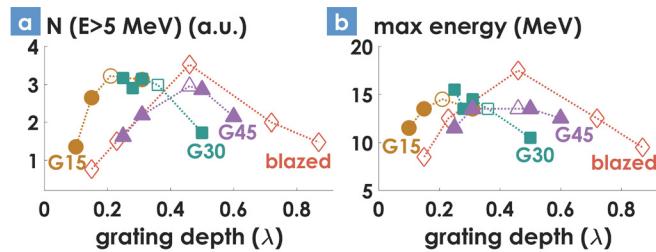


FIG. 9. Depth scan on gratings with different periods: Both the electrons at tangent beyond 5 MeV (a) and the maximum energy attained by the spectra (b) are optimized within a certain range of depth. Empty points represent the simulations where the groove depth corresponded to the experimental value (0.21λ for the G15, 0.36λ for the G30, 0.46λ for the G45, and the values fixed by the blaze angles for the BGs). The bulk thickness was 2λ in all these simulations.

obtained with these targets (neither in the energetic spectra nor in the spatial distributions, which are not shown here for brevity). Further improvement of the grating efficiency is once again obtained with the suitable blazed grating, the BG13.

In a final set of simulations, we investigated the role of the number of grating periods illuminated by the laser pulse, which depends on both the groove spacing and the incidence angle. Therefore, we tested a G45 irradiated at 45° of incidence, by a laser pulse whose focal spot was adapted to cover the same number of periods as the G30 irradiated at 30° (by a beam with waist 5λ). The peak intensity was kept at $a_0 = 5$. As a result, the two configurations produced equivalent electron emissions at the grating surface, provided that the depth of the G45 was larger with respect to the G30. This study pointed out that the number of grating periods is not a crucial parameter required to optimize the electron acceleration.

B. Scan of the laser conditions

With another set of numerical simulations, we covered the SP-driven electron acceleration with different laser parameters. The goal was both to evaluate the possible influence of some interaction conditions and to explore the scaling laws of the acceleration mechanism.

In the first case, we performed a scan of the grating position along the axis of the laser beam and of the grating phase with respect to the focal point (whether the center of the focal spot hits the sinusoidal profile on a peak, on a valley, or somewhere between them). The target implemented in all these simulations was a G30 irradiated at resonance, with a groove depth of 0.36λ and a substrate thickness of 2λ . As result, we found that the grating phase has no influence on the electron acceleration over the entire ϕ range. Figure 10(a), instead, shows that a $\sim \pm 50 \mu\text{m}$ shift of the focal position leads to $\sim 40\%$ fluctuations on the charge emitted along the tangent and, from the spectra, $\pm 2 \text{ MeV}$ on the maximum energy.

We also varied either the beam waist or the pulse duration, keeping the laser energy constant. The electron spatial distribution, illustrated in Fig. 10(b), indicates that the configurations at higher intensity (small focal spot or short pulse, solid lines) are the most favorable for the electron acceleration (note that fewer irradiated lines correspond here to a

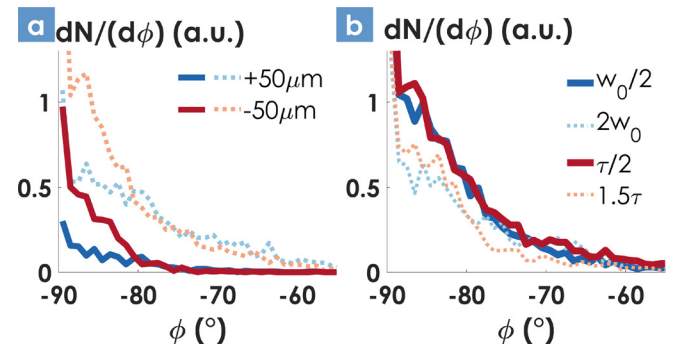


FIG. 10. Scan of the laser parameters on a G30 irradiated at resonance. The electron spatial distributions are shown for: (a) different grating positions along the focal axis, for electrons above 5 MeV (dashed lines) or 10 MeV (solid lines); and (b) different beam waists w_0 or pulse durations τ at fixed laser energy. In (b), the configurations at higher intensity are represented with solid lines.

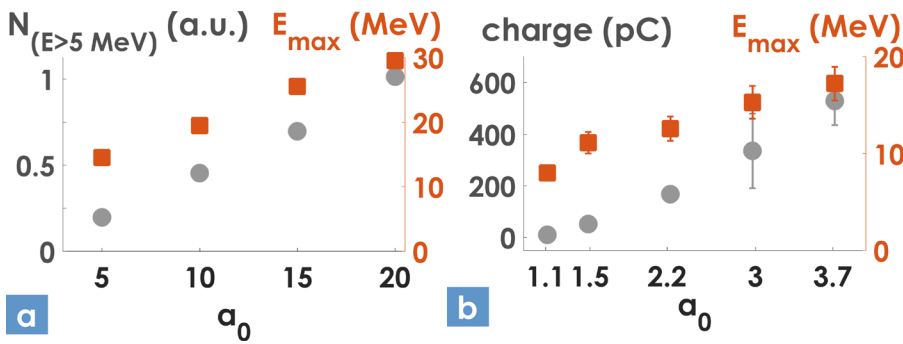


FIG. 11. (a) Number of electrons above 5 MeV emitted at tangent and maximum energy as a function of the laser peak intensity, from PIC simulations. (b) Charge amount and E_{max} measured on the electron bunch emitted from a BG13 at resonance, when varying the energy of the laser pulse on the UHI-100 facility.

higher laser intensity, whereas in the simulation described in Sec. IV A the peak intensity was fixed).

As a final consideration, the theoretical model²⁶ briefly presented in Sec. II predicts for the electron energy a scaling proportional to a_0 ($W \propto a_{\text{SP}} \sim a_0$) but makes no predictions with respect to the amount of charge emitted along the grating surface. Figure 11(a) illustrates that also this quantity exhibits a linear trend with increasing laser intensities. The results of the numerical simulations, in particular, are compared in Fig. 11(b) to the experimental measurements performed on UHI-100, for a_0 between 1.1 and 3.7. The target is a BG13, irradiated at resonance. Despite the necessary caution in comparing the signal emitted by the Lanex screens and the result of 2D PIC simulations, the linear scaling is also supported by the experimental points. Further accuracy would surely result from evaluating the dependence of the simulations on the target density and the 3D geometry. If confirmed, these trends would suggest that the total energy of the surface electrons scales linearly with the laser energy, implying a quasi-constant efficiency of the acceleration mechanism.

V. CONCLUSIONS

This article provides numerous evidence of SPs excitation in the relativistic regime, by analyzing its role in the acceleration of intense electron bunches along the target surface.

Gratings irradiated at the resonant angle for SP excitation predicted by the linear theory exhibit a bright and highly directional emission of energetic electrons, whose properties dramatically worsen when changing the incidence angle or spoiling the temporal contrast of the laser pulse. Flat foils rather produce a 20-time weaker electron cloud around the specular reflection of the laser beam. Varying the grating period, profile, and material has allowed us to demonstrate the robustness of the acceleration mechanism and to identify useful guidelines for its optimization. In particular, the most suitable blazed grating produces ~ 700 pC of charge with an energetic spectrum centered at ~ 10 MeV and reaching 18 MeV of cutoff. The experiments also indicate that dielectric materials give place to electron beams with higher charge and lower divergence with respect to metallic gratings.

With 2D PIC simulations, we have explored the role of various parameters of the laser-grating interaction on both the surface electron acceleration and the target absorption, such as the number and position of grating periods irradiated by the laser pulse, the characteristics of the laser pulse, and the grating depth. In particular, there exists an optimal groove depth,

which depends on the resonant angle, where the electron acceleration is most efficient; this agrees with the SP theory which requires shallow gratings to derive the resonance condition. Inversely, complex geometrical effects account for the high absorption achieved with deep grooves, although the electron emission is neither collimated nor energetic in this case.

The observation of SP-accelerated electron bunches demonstrates the feasibility of SP excitation in the relativistic regime, warming up both the theoretical and experimental investigation of high field Plasmonics.⁵ Moreover, the accurate characterization of the electron emission is the first step towards their promising application as a bright, laser-synchronized, ultra-short electron source at modest energies, potentially suitable for high-repetition rate schemes.⁴² Indeed, although the energetic spectra are far from being mono-chromatic, the peak energies belong to a range hardly attainable with the laser wakefield mechanism, the charge amounts are much higher, and the simple interaction geometry supports the integration of these electron sources in more complex target structures.

SUPPLEMENTARY MATERIAL

See [supplementary material](#) for an example of the electron trajectory and energy increase of a test electron during the temporal evolution of the electric field at the grating surface. The laser irradiates the grating at the resonance angle. The electron is dragged in the vacuum region and performs some oscillations before reaching the optimal velocity to phase-lock with the accelerating field.

ACKNOWLEDGMENTS

We acknowledge M. Květoň (HoloPlus, Prague, Czech Republic) for the prompt and accurate manufacturing of the thin gratings; Jean-Philippe Larbre (ELYSE, Université Paris Sud, Orsay, France) for his contribution during the calibration of the Lanex screen; the computational support from HPC Cluster CNAF (Bologna, Italy), with particular thanks to S. Sinigardi for his precious assistance; and F. Amiranoff (LULI, UPMC, Paris, France) for the invaluable discussions on the theory of SP excitation and electron acceleration. G.C. acknowledges financial support from the Université Franco-Italienne (Vinci program 2015, Grant No. C2–92).

¹W. L. Barnes, A. Dereux, and T. W. Ebbesen, *Nature* **424**, 824 (2003).

²J. A. Schuller, E. S. Barnard, W. Cai, Y. C. Jun, J. S. White, and M. L. Brongersma, *Nat. Mater.* **9**, 193 (2010).

³D. K. Gramotnev and S. I. Bozhevolnyi, *Nat. Photonics* **8**, 13 (2014).

⁴A. Macchi, e-print [arXiv:1711.05124](#) [physics.optics].

- ⁵L. Fedeli, “High field plasmonics,” Ph.D. thesis, Università di Pisa, Springer International Publishing, 2016.
- ⁶A. Bigongiari, M. Raynaud, C. Riconda, and A. Héron, *Phys. Plasmas* **20**, 052701 (2013).
- ⁷T. Ceccotti, V. Floquet, A. Sgattoni, A. Bigongiari, O. Klimo, M. Raynaud, C. Riconda, A. Heron, F. Baffigi, L. Labate, L. A. Gizzi, L. Vassura, J. Fuchs, M. Passoni, M. Květoň, F. Novotny, M. Possolt, J. Prokūpek, J. Proška, J. Pšikal, L. Štolcová, A. Velyhan, M. Bougeard, P. D’Oliveira, O. Tcherbakoff, F. Réau, P. Martin, and A. Macchi, *Phys. Rev. Lett.* **111**, 185001 (2013).
- ⁸L. Fedeli, A. Sgattoni, G. Cantono, and A. Macchi, *Appl. Phys. Lett.* **110**, 051103 (2017).
- ⁹S. M. Weng, P. Mulser, and Z. M. Sheng, *Phys. Plasmas* **19**, 022705 (2012).
- ¹⁰M. Raynaud, J. Kupersztynch, C. Riconda, J. C. Adam, and A. Héron, *Phys. Plasmas* **14**, 092702 (2007).
- ¹¹A. Bigongiari, M. Raynaud, C. Riconda, A. Héron, and A. Macchi, *Phys. Plasmas* **18**, 102701 (2011).
- ¹²S. A. Maier, *Plasmonics: Fundamentals and Applications*, 3rd ed. (Springer, 2007), ISBN: 9780387331508.
- ¹³S. Kahaly, S. K. Yadav, W. M. Wang, S. Sengupta, Z. M. Sheng, A. Das, P. K. Kaw, and G. R. Kumar, *Phys. Rev. Lett.* **101**, 145001 (2008).
- ¹⁴G.-y. Hu, A.-l. Lei, W.-t. Wang, X. Wang, L.-g. Huang, J.-w. Wang, Y. Xu, J.-s. Liu, W. Yu, B.-f. Shen, R.-x. Li, and Z.-z. Xu, *Phys. Plasmas* **17**, 033109 (2010).
- ¹⁵S. Bagchi, P. Prem Kiran, W.-M. Wang, Z. M. Sheng, M. K. Bhuyan, M. Krishnamurthy, and G. Ravindra Kumar, *Phys. Plasmas* **19**, 030703 (2012).
- ¹⁶C. Thauray, F. Quéré, J.-P. Geindre, A. Levy, T. Ceccotti, P. Monot, M. Bougeard, F. Réau, P. D’Oliveira, P. Audebert, R. Marjoribanks, and P. Martin, *Nat. Phys.* **3**, 424 (2007).
- ¹⁷L. Fedeli, A. Sgattoni, G. Cantono, D. Garzella, F. Réau, I. Prencipe, M. Passoni, M. Raynaud, M. Květoň, J. Proška, A. Macchi, and T. Ceccotti, *Phys. Rev. Lett.* **116**, 015001 (2016).
- ¹⁸A. Sgattoni, L. Fedeli, G. Cantono, T. Ceccotti, and A. Macchi, *Plasma Phys. Controlled Fusion* **58**, 014004 (2016).
- ¹⁹G. Cantono, “Relativistic plasmonics for ultra-short radiation sources,” Ph.D. thesis, Università di Pisa & Université Paris Saclay, 2017.
- ²⁰P. Zhu, Y. Zhu, Y. Hidaka, L. Wu, J. Cao, H. Berger, J. Geck, R. Kraus, S. Pjerov, Y. Shen, R. I. Tobey, J. P. Hill, and X. J. Wang, *New J. Phys.* **17**, 063004 (2015).
- ²¹S. Tokita, S. Inoue, S. Masuno, M. Hashida, and S. Sakabe, *Appl. Phys. Lett.* **95**, 111911 (2009).
- ²²I. Pomerantz, E. McCary, A. R. Meadows, A. Arefiev, A. C. Bernstein, C. Chester, J. Cortez, M. E. Donovan, G. Dyer, E. W. Gaul, D. Hamilton, D. Kuk, A. C. Lestrade, C. Wang, T. Ditmire, and B. M. Hegelich, *Phys. Rev. Lett.* **113**, 184801 (2014).
- ²³L. Fedeli, A. Formenti, L. Cialfi, A. Sgattoni, G. Cantono, and M. Passoni, *Plasma Phys. Controlled Fusion* **60**, 014013 (2018).
- ²⁴P. K. Kaw and J. McBride, *Phys. Fluids* **13**, 1784 (1970).
- ²⁵K. T. McDonald, e-print [arXiv:0003065](https://arxiv.org/abs/0003065) [physics].
- ²⁶C. Riconda, M. Raynaud, T. Vialis, and M. Grech, *Phys. Plasmas* **22**, 073103 (2015).
- ²⁷E. A. Peralta, K. Soong, R. J. England, E. R. Colby, Z. Wu, B. Montazeri, C. McGuinness, J. Mcneur, K. J. Leedle, D. Walz, E. B. Sozer, B. Cowan, B. Schwartz, G. Travish, and R. L. Byer, *Nature* **503**, 91 (2013).
- ²⁸K. Mizuno, S. Ono, and O. Shimoe, *Nature* **253**, 184 (1975).
- ²⁹R. B. Palmer, *11th International Conference On High-Energy Accelerators* (Birkhäuser Basel, 1980) ISBN: 9783034855426.
- ³⁰A. Lévy, T. Ceccotti, P. D’Oliveira, F. Réau, M. Perdrix, F. Quéré, P. Monot, M. Bougeard, H. Lagadec, and P. Martin, *Opt. Lett.* **32**, 310 (2007).
- ³¹Y. Glinec, J. Faure, A. Guemnie-Tafo, V. Malka, H. Monard, J. P. Larbre, V. De Waele, J. L. Marignier, and M. Mostafavi, *Rev. Sci. Instrum.* **77**, 103301 (2006).
- ³²A. G. Mordovanakis, J. Easter, N. Naumova, K. Popov, P.-E. Masson-Laborde, B. Hou, I. Sokolov, G. Mourou, I. V. Glazyrin, W. Rozmus, V. Bychenkov, J. Nees, and K. Krushelnick, *Phys. Rev. Lett.* **103**, 235001 (2009).
- ³³M. Thevenet, A. Leblanc, S. Kahaly, H. Vincenti, A. Vernier, F. Quere, and J. Faure, *Nat. Phys.* **12**, 355 (2016).
- ³⁴Y. T. Li, X. H. Yuan, M. H. Xu, Z. Y. Zheng, Z. M. Sheng, M. Chen, Y. Y. Ma, W. X. Liang, Q. Z. Yu, Y. Zhang, F. Liu, Z. H. Wang, Z. Y. Wei, W. Zhao, Z. Jin, and J. Zhang, *Phys. Rev. Lett.* **96**, 165003 (2006).
- ³⁵C. Palmer and E. Loewen, *Diffraction Grating Handbook*, 7th ed. (Newport Corporation, Rochester, 2014).
- ³⁶Newport Corporation, Richardson Gratings Technical Notes no. 7 and 11 (1997).
- ³⁷A. Sgattoni, L. Fedeli, S. Sinigardi, A. Marocchino, A. Macchi, V. Weinberg, and A. Karmakar, e-print [arXiv:1503.02464](https://arxiv.org/abs/1503.02464) [cs.DC].
- ³⁸O. Klimo, J. Pšikal, J. Limpouch, J. Proška, F. Novotny, T. Ceccotti, V. Floquet, and S. Kawata, *New J. Phys.* **13**, 053028 (2011).
- ³⁹A. Andreev, N. Kumar, K. Platonov, and A. Pukhov, *Phys. Plasmas* **18**, 103103 (2011).
- ⁴⁰S. Jiang, A. G. Krygier, D. W. Schumacher, K. U. Akli, and R. R. Freeman, *Phys. Rev. E* **89**, 013106 (2014).
- ⁴¹A. Bigongiari, “High intensity laser-plasma grating interaction: Surface wave excitation and particle acceleration,” Ph.D. thesis, Ecole Polytechnique X, 2012.
- ⁴²I. Prencipe, J. Fuchs, S. Pascarelli, D. W. Schumacher, R. B. Stephens, N. B. Alexander, R. Briggs, M. Büscher, M. O. Cernaianu, A. Choukourov, M. De Marco, A. Erbe, J. Fassbender, G. Fiquet, P. Fitzsimmons, C. Gheorghiu, J. Hund, L. G. Huang, M. Harmand, N. J. Hartley, A. Irman, T. Kluge, Z. Konopkova, S. Kraft, D. Kraus, V. Leca, D. Margarone, J. Metzkes, K. Nagai, W. Nazarov, P. Lutoslawski, D. Papp, M. Passoni, A. Pelka, J. P. Perin, J. Schulz, M. Smid, C. Spindloe, S. Steinke, R. Torchio, C. Vass, T. Wiste, R. Zaffino, K. Zeil, T. Tschentscher, U. Schramm, and T. E. Cowan, *High Power Laser Sci. Eng.* **5**, e17 (2017).