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# The Impact of Solar Irradiance on Visible Light Communications

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**Abstract**—This paper aims to address the perception that visible light communication (VLC) systems cannot work under the presence of sunlight. A complete framework is presented to evaluate the performance of VLC systems in the presence of solar irradiance at any given location and time. The effect of solar irradiance is investigated in terms of degradations in signal to noise ratio, data rate, and bit error rate. Direct current (DC) optical orthogonal frequency division multiplexing is used with adaptive bit and energy loading to mitigate DC wander interference and low-frequency ambient light noise. It was found that reliable communication can be achieved under the effect of solar irradiance at high-speed data rates. An optical bandpass blue filter is shown to compensate for half of the reduced data rate in the presence of sunlight. This work demonstrates data rates above 1 Gb/s of a VLC link under strong solar illuminance measured at 50350 lux in clear weather conditions.

**Index Terms**—Light fidelity (LiFi), OFDM, solar irradiance, visible light communication (VLC).

## I. INTRODUCTION

TRAFFIC from wireless and mobile devices will account for two-thirds of the total internet traffic by 2020 [1]. The radio frequency (RF) bandwidth is a scarce resource costing above \$1.28m per 1 MHz in the 2.4 GHz frequency band in the UK [2]. Visible light communication (VLC) offers a much larger frequency bandwidth that is unlicensed and safe to use. VLC has the potential to reuse the existing lighting infrastructure based on light emitting diode (LED) for communications purposes [3]. Light fidelity (LiFi) is the network solution for VLC that is proposed to work seamlessly beside other RF access technologies [3]. A record data rate of 7.91 Gb/s was reported

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for orthogonal frequency division multiplexing (OFDM)-based VLC using single violet micro-scale GaN led (micro-LED) [4]. Data rates above 100 Gb/s can be achieved when the complete visible spectrum is utilized [5].

The effect of solar irradiance is considered to be one of the main misconceptions surrounding VLC [6]. It is generally assumed that it could halt the operation of the communication system entirely due to interference. However, the effect of solar irradiance is more apparent as a strong shot noise source rather than an interference source as the sunlight intensity does not vary greatly over short periods of time. This allows multicarrier schemes such as OFDM to allocate the symbols over the usable frequency subcarriers of the deployed bandwidth [7].

The effect of solar irradiance on the performance of optical wireless communications (OWC) and VLC has been investigated in a limited number of works in the literature [8]–[12]. A simplified model was adopted in some of these works by approximating the solar irradiance to a black body radiation [8]. Other works adopted a standardized solar irradiance model [13] that is being used as a reference model in the research on solar energy harvesting [9]. However, the location and time of the studied system play important roles in characterizing the solar irradiance effect on VLC system performance. These important parameters were considered using computer simulation in [10]. However, the direct solar irradiance was not used to characterize the system performance. The solar irradiance was assumed to be incident from a window and reflected on multiple walls before it is collected by the photoreceivers. The impact of solar irradiance on the performance of underwater OWC links was investigated for positive-intrinsic-negative (PIN), avalanche photodiode (APD) and photomultiplier tube (PMT) using Monte Carlo simulation in [9]. It was shown that sunlight degrades the system performance at relatively low depths below 80 meters.

The use of optical filters with a light control film to mitigate the effects of sunlight was proposed in [8], [11]. A filter with a light control film called microlouver is used to restrict the field of view (FOV) and to reduce the background light collected at the photoreceiver. However, the light control film can not adapt to the changes of the photoreceiver orientation and location which limits the solution to fixed point-to-point systems. The objective of this paper is to provide a theoretical and experimental characterization of the solar irradiance effect on high-speed OFDM-based VLC systems. The investigation compares the use of a bandpass optical blue filter to the case where

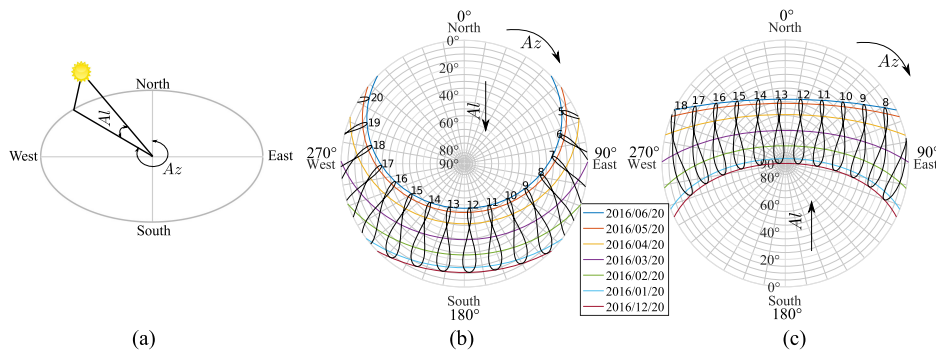


Fig. 1. (a) Solar position described by altitude and azimuth. (b) and (c) Solar position at Edinburgh and Antofagasta, respectively, for each 20th day of each considered month. The time of the day is listed above the elliptical shapes representing the Analemma diagrams.

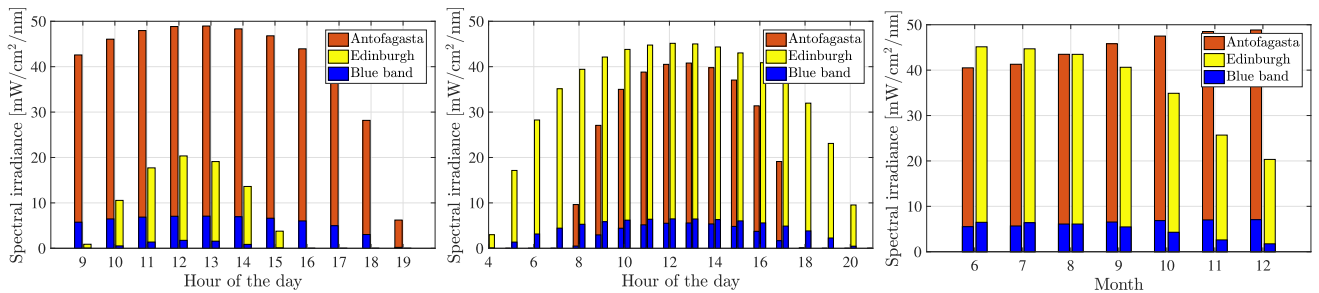


Fig. 2. Total solar irradiance estimated at Antofagasta and Edinburgh on the 20th of December 2016 (left) and on the 20th of June 2016 (center); and at the noon of each 20th day of the second half of the year (right). The blue spectral component of the solar irradiance is shown in blue.

80 a filter is not considered in front of the photoreceiver. The per-  
81 formance is compared to a benchmark scenario of a dark room  
82 where background light does not reach the photoreceiver.

83 In our previous work [14], we investigated the solar irradiance  
84 effect on VLC in Antofagasta, Chile based on worst-case  
85 scenarios in terms of location, link orientation and choice of  
86 photoreceiver. In this paper, we present a complete framework  
87 to investigate the sunlight effect on VLC at any given location  
88 and time. The previous literature were manily based on pulsed  
89 modulation techniques [11], [12]. However, an outdoor under-  
90 water VLC demonstration achieving a data rate of 58 Mb/s was  
91 considered using discrete multi-tone (DMT) [15]. In this work,  
92 we demonstrate our results by an experimental proof of concept  
93 of a high speed OFDM-based VLC system in Edinburgh,  
94 UK achieving data rate above 1 Gbps in the presence of solar  
95 irradiance without any optical filtering. The simulation and ex-  
96 perimental results show that the solar irradiance affects VLC  
97 link performance, but the effects are gradual and depend on a  
98 number of other parameters such as link margin. The simulation  
99 results show that at least half of the losses in data rate per-  
100 formance can be recovered using an inexpensive commercially  
101 available bandpass blue filter.

102 The rest of this paper is organized as follows. In Section II,  
103 we review the solar position and irradiance calculations based  
104 on location and time and present the results of two geographical  
105 locations. The assumptions of the theoretical study are specified  
106 in Section III-A. The signal-to-noise ratio (SNR), the maximum  
107 theoretical limit to the data rate and bit error rate (BER) of the  
108 system are derived and the system modelling is discussed in  
109 Section III-B. An experimental proof-of-concept is presented in

Section IV. The system performance is analyzed and the results  
110 are shown in Sections III-C and IV-B. Section V concludes the  
111 paper.  
112

## 113 II. SOLAR IRRADIANCE AND POSITION 114

115 The solar constant flux density  $P_{SC}$  is given as  $1366.1 \text{ W/m}^2$   
116 outside the Earth's atmosphere by the American society for  
117 testing and materials (ASTM) standard (ASTM E-490) [16].  
118 The solar irradiance is not limited to the visible spectrum as  
119 it spans the wavelengths from 250 nm to 2500 nm. The solar  
120 irradiance at different wavelengths is non-equally attenuated as  
121 it travels through the atmosphere due to the different absorption  
122 and scattering effects of the air molecules and aerosols. The  
123 shortest path for the sunlight exists when the Sun is located at  
124 the zenith point (imaginary point above the head of the observer).  
125 The optical air mass (AM) is approximated as the ratio of the  
126 actual sunlight path to the minimum path at the zenith point.  
127 It is given as AM0 for the extraterrestrial irradiance. When the  
128 Sun is at angle  $\theta_Z$  relative to the zenith, the optical AM is  
129 approximated as:

$$AM \simeq \frac{1}{\cos \theta_Z}. \quad (1)$$

129 The solar irradiance at  $\theta_Z = 48.2^\circ$  is given at an AM1.5 by the  
130 standard (ASTM E-490) [13] as a reference to help the solar  
131 energy community in testing and comparing the performance of  
132 various solar cells. However, the solar irradiance varies based  
133 on the geographical location; seasonal and diurnal variations  
134 arising from the rotation of the Earth around the Sun; and the

TABLE I  
MODELLING ASSUMPTIONS

Locations	Edinburgh, UK, 55°55'20.4"N 3°10'23.3"W Antofagasta, Ch, 23°27'16.1"S 70°26'21.4"W
Dates	Every 20 <sup>th</sup> of each considered month
APD model	Hamamatsu S8664-50K
APD detection area, $A$	19.6 mm <sup>2</sup>
Bandwidth, $B$	60 MHz
APD gain, $M$	100
Dark current, $I_d$	3 nA
Blue filter FWHM	50 nm
Maximum transmitted optical power, $P_{Max}^L$	8 mW
Transmission distance, $d$	63.85 cm
Half-power semi-angle of the transmitter, $\Phi_{1/2}$	25°

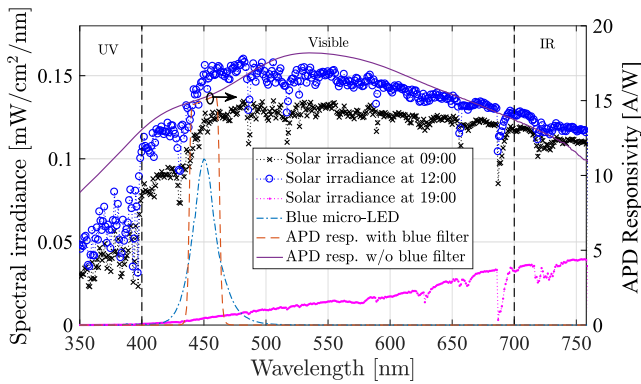


Fig. 3. The predicted solar irradiance in Antofagasta at 9 AM, 12 PM and 19 PM (local time) of the 20th on December 2016 (left), alongside the spectral irradiance of the modeled micro-LED centred at 450 nm (left) and response of the APD with and without considering the transmittance of the blue filter (right).

135 rotation of the Earth around its own axis. The effect of solar irradiance on VLC varies based on the location and time. Therefore, 136 it is essential to calculate the position of the Sun in the sky in order for the solar irradiance at a particular location and time 137 to be estimated. Various algorithms with different complexities and accuracies for calculating the solar position exist in the as- 138 trophysics literature [17]. In Appendix A, we review a simple algorithm based on the ecliptic coordinates with an accuracy 139 of  $(1/60)^\circ$  presented in [18] and proposed by the astronomical applications department of the U.S. naval observatory [19]. 140

141 The horizontal coordinate system is usually used for solar energy applications where the horizon of the observer is considered 142 to be the fundamental plane. The solar position can be described using two angles: altitude  $Al$  and azimuth  $Az$ . The solar altitude  $Al \in [0^\circ, 90^\circ]$  is given as the elevation of the Sun 143 above the horizon. A solar altitude of  $Al = 90^\circ$  means that the Sun is at the zenith point. The solar altitude can also be given as 144  $Al = 90^\circ - \theta_z$ . The solar azimuth  $Az \in [0^\circ, 360^\circ]$  is given as the angle between the north and the horizontal projection of the 145 line-of-sight (LoS) between the Sun and the observer. Both angles are illustrated in Fig. 1(a) and demonstrated in Fig. 1(b) and 146 (c) for Edinburgh, UK and Antofagasta, Chile on the 20<sup>th</sup> of each considered month, respectively. The solar altitude is shown to 147 reach the zenith  $Al = 90^\circ$  around 13:00 on the 20th of December 148

2016 for Antofagasta in Fig. 1(c). The time of the day is shown 159 above the analemma diagrams in Fig. 1(b) and (c), which depict 160 the Sun's motion throughout the year when observed at the same 161 location and the same hour of day. 162

163 Direct solar irradiance is the sunlight that is directly reaching 164 the surface of the Earth. Global solar irradiance is the combina- 165 tion of the direct and diffused solar irradiance. The simple model 166 of the atmospheric radiative transfer of sunshine (SMARTS) is 167 a transmittance model to evaluate the direct solar irradiance at 168 any particular location and time [20], [21]. The model is used 169 in generating the ASTM standard (ASTM E-490) with a resolu- 170 tion of 0.5–1 nm [16]. The direct solar irradiance is typically 171 stronger than the signal of interest when the total solar irradiance 172 is taken into account. Fortunately, VLC is realized using mono- 173 chromatic or multi-chromatic optical sources that has fixed and 174 pre-defined spectral irradiance. This allows inexpensive commer- 175 cially available optical filters to be a practical solution for the 176 degradations caused by solar irradiance. The total predicted 177 solar irradiance is shown in Fig. 2(a) and (b) for Antofagasta 178 and Edinburgh at the noon of December and June solstices, re- 179 spectively. Monthly comparisons for the total solar irradiance 180 are shown in Fig. 2(c). The total spectral irradiance is calculated 181 for the visible spectrum between 400 nm and 760 nm. The blue 182 component of the solar irradiance for the wavelengths between 183 425 nm and 475 nm shows the importance of optical filtering 184 in improving the VLC communications performance. Optical 185 filtering is also beneficial for other objectives in VLC. White il- 186 lumination is generally achieved by coating the blue LED with 187 a yellow phosphor which introduces a slow component into the 188 frequency response of the LED. Blue filters are required to 189 eliminate the slow response component of the yellow phosphor. 190 Monochromatic light sources with narrowband spectral 191 distributions can guarantee a robust VLC system against solar 192 irradiance with the potential of achieving data rates in the orders 193 of multiple Gb/s.

### 194 III. THEORETICAL STUDY

#### 195 A. Modelling Assumptions

196 An OFDM-based VLC system is assumed due to its robustness 197 against background illumination flickering. The OFDM 198 waveform is required to be both unipolar and real valued. Her- 199 mitian symmetry is imposed on the  $M$ -ary quadrature amplitude 200 modulation ( $M$ -QAM) symbols, to enforce the OFDM time do- 201 main signal output into the real domain. This can be written as: 202  $X[k] = X^*[N_{FFT} - k]$ , where  $N_{FFT}$  is the OFDM frame size. 203 The subcarriers  $X[0]$  and  $X[N_{FFT}/2]$  are both set to zero. A 204 real-valued OFDM waveform with a direct current (DC) bias is 205 used to modulated the intensity of the LED in what is known 206 as DC-biased optical OFDM (DCO-OFDM). Binary inputs are 207 encoded into multiple  $M$ -QAM symbols which are allocated 208 into  $N_{FFT}$  subcarriers over a single-sided bandwidth of  $B$ . DC 209 bias is used to shift the negative signal samples into positive 210 values. Three scenarios are considered:

- *Dark room (Scenario 1)*: assumes an optimal case where 211 no background illumination is reaching the photoreceiver. 212

213 This is an ideal scenario as the dominant noise source is  
214 the thermal noise.

- 215 • *With blue filter (Scenario II)*: assumes that the solar irra-  
216 diance is collected with a bandpass blue filter in front of  
217 the photoreceiver. This is a practical scenario as the useful  
218 transmitted signal is passed and any out-of-band signal is  
219 filtered. Part of the solar irradiance is passed since it covers  
220 a wide wavelength band.
- 221 • *Without blue filter (Scenario III)*: assumes a worst case  
222 scenario where the solar irradiance is collected without  
223 any optical filtering in front of the photoreceiver.

224 The modeling assumptions are presented in Table I. The sys-  
225 tem uses a blue micro-LED with a pixel size of  $100 \times 100 \mu\text{m}^2$   
226 and a maximum optical power of 8 mW. Due to the reduced  
227 emission area of micro-LEDs, the capacitance decreases and  
228 current density increases allowing for higher 3-dB bandwidths  
229 compared to off-the-shelf LEDs [22]. The transmission distance  
230 is specified at  $d = 63.85$  cm to match with the distance that  
231 we have used to measure the spectral irradiance of the micro-  
232 LED. The system performance is also investigated at longer  
233 distances up to 3 meters in Section III-C. A focusing aspheric  
234 condenser optical lens (Thorlabs, ACL4532U-A) is used at the  
235 transmitter side, which allows for a small half-power semi-angle  
236 at the transmitter  $\Phi_{1/2} = 25^\circ$ . An optical bandpass blue filter  
237 from Edmund Optics is assumed in Scenario II with a center  
238 wavelength of 450 nm, a transmittance higher than 90%  
239 and a full width at half maximum (FWHM) of 50 nm. The  
240 photoreceiver is an APD (Hamamatsu, S8664-50K) where it is  
241 assumed to be aligned with the micro-LED. APDs operate at  
242 high reverse bias to create an amplification effect that allows  
243 incident photons to create an avalanche of electrons. APDs are  
244 more sensitive to background noise compared to other photo-  
245 diodes. However, APDs are used as a worst case choice in this  
246 investigation as they are shot-noise limited [23]. The APD will  
247 not always be collecting the solar irradiance due to the orienta-  
248 tion of the communication link in practical situations. However,  
249 the APD is always assumed to be collecting the sunlight in this  
250 investigation.

251 The locations considered are  $55^\circ 55' 20.4''\text{N}$   $3^\circ 10' 23.3''\text{W}$  in  
252 Edinburgh, UK and  $23^\circ 27' 16.1''\text{S}$   $70^\circ 26' 21.4''\text{W}$  in Antofa-  
253 gasta, Chile. The former location is used to compare with the  
254 experimental results and the latter is claimed to have the highest  
255 solar radiation on Earth [24]. The model considers two dates:  
256 summer solstice and winter solstice where the solar position  
257 is calculated and used in SMARTS [20], [21] to estimate the  
258 hourly solar irradiance data. The model assumes a clear sky  
259 scenario due to the irregular variations in the local weather con-  
260 ditions which influence the solar irradiance. This allows us to  
261 consider the maximum possible solar irradiance in a pessimistic  
262 approach. As the considered locations lies in the north and south  
263 hemispheres, the summer solstice at Edinburgh would be winter  
264 solstice at Antofagasta and similarly the opposite is true.

## 265 B. System Modeling

266 The OFDM waveform  $x(t)$  is transmitted over the VLC chan-  
267 nel  $h(t)$ , before it is distorted with noise  $n(t)$  at the receiver.

The received signal  $r(t)$  is then sampled at  $1/T$  with an analog-  
268 to-digital converter (ADC), where  $T$  is the sampling period. Fast  
269 Fourier transform (FFT) is then applied on the samples after  
270 serial to parallel (S/P) conversion. Assuming that the OFDM  
271 frame size is large ( $N_{\text{FFT}} > 64$ ) [25], central limit theorem  
272 (CLT) can be applied on the combination of noise generated at  
273 the receiver. This can be modeled as zero mean additive white  
274 Gaussian noise (AWGN) with variance  $\sigma_n^2$ . The received OFDM  
275 waveform  $r(t)$  can be given as: 276

$$r(t) = h(t) * x(t) + n(t). \quad (2)$$

The average photocurrent generated at the APD due to the  
277 average optical power received from sunlight is given as: 278

$$I_b = A_d \int_{350}^{750} P_D^S(\lambda) R(\lambda) T_{\text{bf}}(\lambda) d\lambda, \quad (3)$$

where  $A_d$  is the APD detection area,  $P_D^S(\lambda)$  is the direct solar  
279 irradiance given in  $\text{W}/\text{m}^2/\text{nm}$ ,  $T_{\text{bf}}(\lambda)$  is the transmittance of the  
280 bandpass optical blue filter,  $R(\lambda)$  is the intrinsic responsivity of  
281 the APD given in  $\text{A}/\text{W}$  and  $\lambda$  is the wavelength considered for  
282 the visible light spectrum mainly from 350 nm to 750 nm. 283

284 Similarly, the average photocurrent generated at the APD due  
285 to the average optical power received from the micro-LED is  
286 given as:

$$I_x = \frac{(m+1)A_d}{2\pi d^2} \int_{350}^{750} P_T^L(\lambda) R(\lambda) T_{\text{bf}}(\lambda) d\lambda, \quad (4)$$

where  $m = -1/\log_2(\cos(\Phi_{1/2}))$  is the Lambertian order of the  
287 micro-LED;  $d$  is the Euclidean distance between the micro-LED  
288 and the APD; and  $P_T^L(\lambda)$  is the transmitted optical irradiance  
289 from the micro-LED, which is given as: 290

$$P_T^L(\lambda) = P_{\text{Max}}^L \frac{P_{\text{Measured}}^L(\lambda)}{\int_{350}^{750} P_{\text{Measured}}^L(\lambda) d\lambda}, \quad (5)$$

where  $P_{\text{Max}}^L$  is the maximum transmitted optical power of the  
291 micro-LED and  $P_{\text{Measured}}^L(\lambda)$  is the measured optical irradiance  
292 of the micro-LED given in  $\text{W}/\text{m}^2/\text{nm}$ . This was measured at a  
293 distance of  $d = 63.85$  cm using a Labsphere spectral irradiance  
294 head (E1000). 295

The random arrival of incident photons results in shot noise  
296 which can be modeled by a Poisson distribution. However, when  
297 the number of incident photons increases, the shot noise is  
298 approximated by a Gaussian distribution [26]. The shot noise  
299 variance is given by [27]: 300

$$\sigma_s^2 = 2qM^2 F(I_b + I_x) B, \quad (6)$$

where  $M$  is the average gain of the APD,  $q$  is the electron charge,  
301  $B$  is the bandwidth of the APD and  $F$  is the excess noise given  
302 as [28]: 303

$$F = \kappa M + (2 - 1/M)(1 - \kappa), \quad (7)$$

where  $\kappa$  is the holes/electrons ionization rate. The SNR at sub-  
304 carrier  $k$  can be given by: 305

$$\gamma_k = \frac{M^2 I_x^2}{\sigma_n^2 / |H(k)|^2}, \quad (8)$$

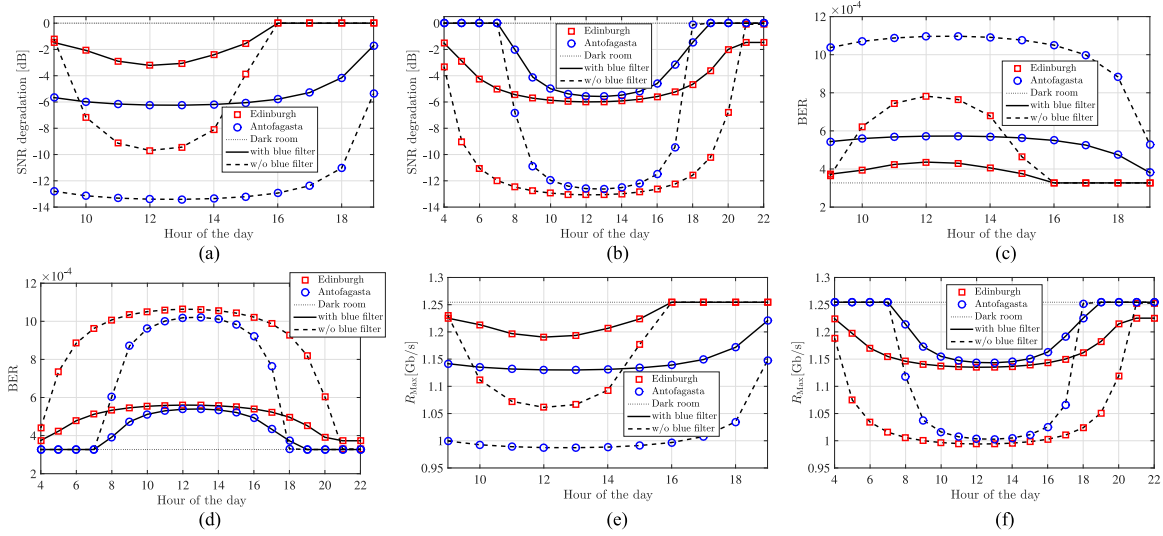


Fig. 4. (a and b) SNR; (c and d) BER; (e and f) maximum theoretical limit to the data rate. All results are presented for the three considered scenarios in Antofagasta and Edinburgh versus time at the 20th of December 2016 (a, c, e) and 20th of June 2016 (b, d, f).

306 where  $H(k)$  is the frequency domain realization of the VLC  
 307 channel,  $\sigma_n^2 = \sigma_s^2 + \sigma_t^2 + \sigma_d^2$  and  $\sigma_d^2$  is the variance of the dark  
 308 noise which is given as [27]:

$$\sigma_d^2 = 2qM^2FI_{dg}B + 2qI_{ds}B, \quad (9)$$

309 where  $I_{ds}$  is the surface dark current and  $I_{dg}$  is the bulk dark  
 310 current that experience the avalanche effect of the APD and  
 311 where  $I_d = I_{ds} + MI_{dg}$ . The variance of the thermal noise  $\sigma_T^2$   
 312 is given by [29]:

$$\sigma_T^2 = 4 \left( \frac{K_B T}{R_L} \right) F_n B, \quad (10)$$

313 where  $K_B$  is Boltzmann constant,  $T$  is the temperature in  
 314 Kelvin,  $R_L$  is the load resistance given as  $50\Omega$  and  $F_n$  is the  
 315 photodiode noise figure.

316 Adaptive bit and energy loading algorithms such as the Levin-  
 317 Campello algorithm [30] can be used to maximize the data rate  
 318 by assigning larger constellation sizes on the subcarriers that  
 319 have higher SNR. The maximum theoretical limit to the data  
 320 rate of DCO-OFDM can be calculated using the channel capac-  
 321 ity defined by Shannon-Hartley theorem [31] when neglecting  
 322 the DC bias and the optical source nonlinearity [32]. This is  
 323 given as:

$$R_{\text{Max}} = B \sum_{\substack{k=1 \\ M'_k > 0}}^{N_{\text{FFT}}/2-1} \log_2(1 + \gamma_k), \quad (11)$$

324 where  $M'_k$  is the constellation order of  $M'_k$ -QAM used at sub-  
 325 carrier  $k$ .

326 The system performance in terms of BER can be calculated  
 327 using the theoretical BER of real-valued OFDM given for fre-  
 328 quency selective channels [33]. The BER at subcarrier  $k$  can be

given as:

$$\text{BER}(M'_k, \gamma_k) \cong \frac{4}{\log_2(M'_k)} \left( 1 - \frac{1}{\sqrt{M'_k}} \right) \times \sum_{l=1}^R Q \left( (2l-1) \sqrt{\frac{3\gamma_k}{2(M'_k - 1)}} \right), \quad (12)$$

330 where  $Q(\cdot)$  is the complementary cumulative distribution  
 331 function (CCDF) for the standard normal distribution and  
 332  $R = \min(2, \sqrt{M'_k})$ . The overall system BER can be given as:

$$\text{BER} = \frac{\sum_{\substack{k=1 \\ M'_k > 0}}^{N_{\text{FFT}}/2-1} \text{BER}(M'_k, \gamma_k) \log_2(M'_k)}{\sum_{\substack{k=1 \\ M'_k > 0}}^{N_{\text{FFT}}/2-1} \log_2(M'_k)} \quad (13)$$

### C. Results and Discussions

333 The spectral irradiance of the micro-LED and the amplified  
 334 responsivity of the APD  $MR(\lambda)$  are shown in Fig. 3 with the  
 335 presence and absence of the optical bandpass blue filter. In addition,  
 336 the predicted spectral irradiance of the sunlight at Antofa-  
 337 gasta is shown at three different times of the summer solstice.  
 338 It is shown that the solar irradiance is high at the ultra-violet  
 339 (UV) and blue spectrum bands at sunrise. At sunset it becomes  
 340 higher at the red and infra-red (IR) spectrum bands. The blue  
 341 filter captures 70% of the micro-LED irradiance.  
 342

343 The system performance is presented in Fig. 4(a) and (b) as  
 344 a function of the SNR degradation against the time of the day  
 345 for both December and June solstice, respectively. The degrada-  
 346 tion is calculated with reference to the benchmark case of  
 347 the dark room in Scenario I. It is shown that the SNR degrades  
 348 by a maximum of  $-13.4$  dB and  $-9.69$  dB at the noon of De-  
 349 cember solstice in Scenario III at Antofagasta and Edinburgh,  
 350 respectively. However, when a blue filter is used in front of the

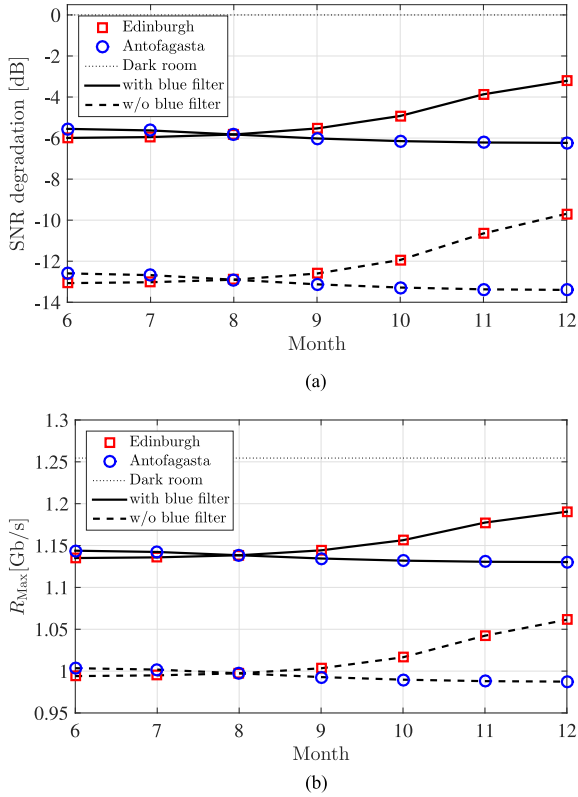


Fig. 5. The system performance presented on monthly basis at the noon of each 20th day of the considered months for the three considered scenarios in Antofagasta and Edinburgh. (a) SNR and (b) Maximum theoretical limit on data rate.

351 APD, this degradation is reduced to  $-6.23$  dB and  $-3.214$  dB  
 352 in Scenario II at Antofagasta and Edinburgh, respectively. The  
 353 high degradation in SNR at Antofagasta is expected due to the higher  
 354 solar irradiance in December solstice in comparison with  
 355 Edinburgh as shown in Fig. 2(a). The SNR degradations at Ed-  
 356 inburgh for June solstice increase in comparison with December  
 357 solstice by a maximum increase of 3.38 dB. The SNR degrada-  
 358 tion is 0.8 dB lower for June solstice compared with December  
 359 solstice at Antofagasta. A minimum of 6.47 dB improvement in  
 360 SNR is achieved when blue filters are used in Scenario II. The  
 361 SNR degradation at Edinburgh are witnessed for longer hours  
 362 during June solstice due to the longer daylight that is shown in  
 363 Fig. 1(b). The SNR degradation at Antofagasta and Edinburgh  
 364 at the 20th day of the noon of the last six months of 2016 is  
 365 presented in Fig. 5(a). The degradation decreases noticeably as  
 366 we approach December solstice at Edinburgh, while SNR  
 367 degradation variations are less noticeable for Antofagasta.

368 The system performance as a function of the BER against  
 369 the time of the day is shown in Fig. 4(c) and (d) for 128-QAM  
 370 DCO-OFDM at December and June solstices, respectively. The  
 371 results show the SNR degradation effect on the BER perfor-  
 372 mance for the OFDM-based VLC system. Both scenario II and  
 373 scenario III at Antofagasta and Edinburgh are shown to allow  
 374 the use of forward error correction (FEC) in both December and  
 375 June solstice, although a significant improvement is shown to be  
 376 achieved when the blue filter is used. The system performance

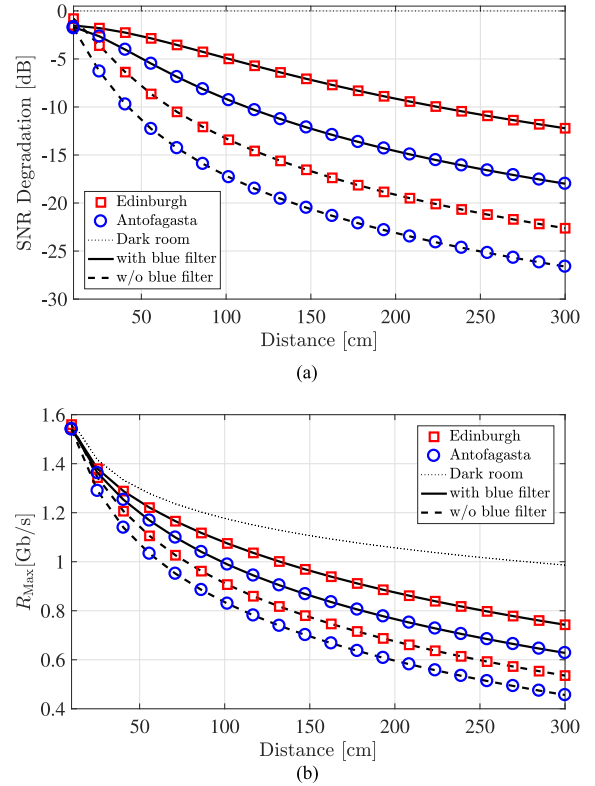


Fig. 6. System performance versus transmission distance  $d$  at the noon of the 20th of December 2016 for the three considered scenarios in Antofagasta and Edinburgh. (a) SNR and (b) Maximum theoretical limit on data rate.

is investigated as a function of the maximum theoretical limit to  
 the data rate versus the time of the day in Fig. 4(e) and (f) for  
 December and June solstices, respectively. The performance of  
 Scenario II and the performance of Scenario III are compared to  
 the benchmark performance recorded at 1.25 Gb/s of Scenario I  
 for Antofagasta and Edinburgh. It is shown that the data rate  
 degrades by 21.35% and by 15.49% at the noon of December  
 solstice when the blue filter is not used in Antofagasta and Ed-  
 inburgh, respectively. However, this degradation is reduced to 10%  
 and 5.22% for Scenario II at Antofagasta and Edinburgh, respec-  
 tively. This is equivalent to a significant 53.16% and 66.30%  
 improvement that is achieved by placing a blue filter in front  
 of the APD. A maximum theoretical limit to the data rate for  
 June solstice under the solar irradiance is estimated at 1.03 Gb/s  
 and 0.99 Gb/s for Scenario III at Antofagasta and Edinburgh,  
 respectively and at 1.14 Gb/s and 1.13 Gb/s for Scenario II at  
 Antofagasta and Edinburgh, respectively. A comparison of the  
 maximum data rate performance at both Antofagasta and Ed-  
 inburgh at noons of the last six months of 2016 is presented in  
 Fig. 5(b). The variations in data rates are more noticeable for  
 Edinburgh, where it increases to reach a maximum of 1.19 Gb/s  
 for Scenario II and 1.06 Gb/s for Scenario III in December.

The SNR degradation and the maximum theoretical limit on  
 the data rate are given in Fig. 6(a) and (b) as functions of the  
 transmission distance. The results in Fig. 6 are presented for  
 the three considered scenarios at Antofagasta and Edinburgh  
 at noon of the 20th of December 2016. The SNR degrades as  
 the transmission distance increases in all considered scenarios,

405 including the dark room scenario I, as expected. However, the  
 406 SNR degradation for Scenario II and III are calculated with  
 407 reference to the dark room in scenario I to highlight the solar  
 408 irradiance effect in comparison with the benchmark Scenario I.  
 409 It is shown that the SNR degradation reaches  $-26.61$  dB and  
 410  $-22.63$  dB when the blue filter is not used in Scenario III at a  
 411 transmission distance of 3 meters at Antofagasta and Edinburgh,  
 412 respectively. Although the SNR degradation appears to be high,  
 413 the SNR gain of using the blue filter in Scenario II reaches  
 414  $8.6$  dB and  $10.41$  dB at a transmission distance of 3 meters for  
 415 Antofagasta and Edinburgh, respectively. Similarly, the maxi-  
 416 mum theoretical limit on the data rate is shown to decrease as  
 417 the transmission distance increases. The maximum theoretical  
 418 limit on the data rate at a transmission distance of 3 meters for  
 419 the dark room in Scenario I is  $986.3$  Mb/s. This is degraded  
 420 by  $53.74\%$  for Antofagasta and  $45.71\%$  for Edinburgh in Scen-  
 421 ario III. However, it is shown that the degradation is reduced  
 422 to  $36.33\%$  and  $24.7\%$  in Antofagasta and Edinburgh when the  
 423 blue filter is used in Scenario II. Despite the degradation in  
 424 SNR, high-speed VLC can still be available at sufficiently long  
 425 distances.

#### 426 IV. EXPERIMENTAL STUDY

##### 427 A. Experimental Set-Up

428 The measurements were conducted between 11:00–17:00 (lo-  
 429 cal time) of the 6th and 9th of June 2016 under clear sky weather  
 430 conditions demonstrated by very good visibility estimated  
 431 above 21 km and a solar illuminance measured at 50350 lux.  
 432 The measurements were carried at  $55^{\circ}55'20.4''N$   $3^{\circ}10'23.3''W$   
 433 in Edinburgh, UK. The experimental setup is shown in  
 434 Fig. 7(a)–(b). The system elements used in the experiment  
 435 are the same components described in Section III-A. The  
 436 OFDM modulation waveform is generated and processed off-  
 437 line using MATLAB. The OFDM digital waveform is con-  
 438 verted into an analog waveform using the arbitrary waveform  
 439 generator Agilent 81180A, which sends the bipolar OFDM  
 440 waveform to the micro-LED using a Bias-Tee ZFBT-4R2GW.  
 441 The DC bias is selected after exhaustive tests at  $V_{DC} = 4.1$   
 442 Volts to minimize the clipping distortion. The optical power  
 443 of the micro-LED is  $4.5$  mW and the 3-dB bandwidth is  
 444  $30$  MHz, both measured at DC current  $I_{DC} = 50$  mA. An as-  
 445 pheric collimation lens ACL 4532 is used to focus the light  
 446 on the photoreceiver. Two Silicon APDs are used in this ex-  
 447 periment (Hamamatsu, S8664-05k) and (Hamamatsu, S8664-  
 448 50k), as shown in the top-right corner of Fig. 7(b). These  
 449 APDs are referred to as ‘small’ APD and ‘large’ APD, respec-  
 450 tively. The small APD has a smaller active area of  $0.19$  mm<sup>2</sup>  
 451 and therefore, has a lower capacitance that leads to a higher  
 452 3-dB bandwidth of  $680$  MHz. The large APD has a larger active  
 453 area of  $19.6$  mm<sup>2</sup> that leads to a higher capacitance and lower  
 454 3-dB bandwidth of  $60$  MHz.

455 The received signal at the APDs is filtered using a low  
 456 pass electrical filter (Mini-circuits, SLP-100+) with a cut-off  
 457 of  $98$  MHz for the large APD; and (Mini-circuits, SLP-250+)  
 458 with a cut-off of  $225$  MHz for the small APD. Both filters are  
 459 shown in Fig. 7(a). The system modulation bandwidth is used  
 460 at  $100$  MHz and  $250$  MHz for the large and small APDs, re-

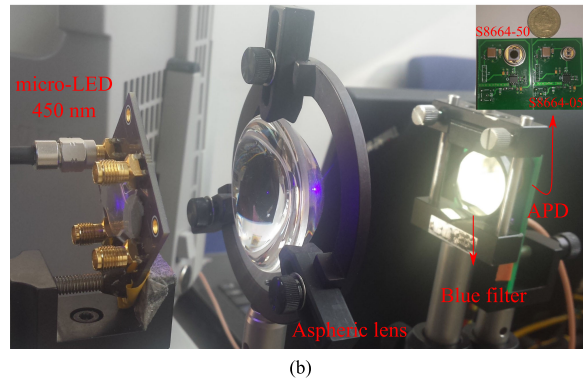
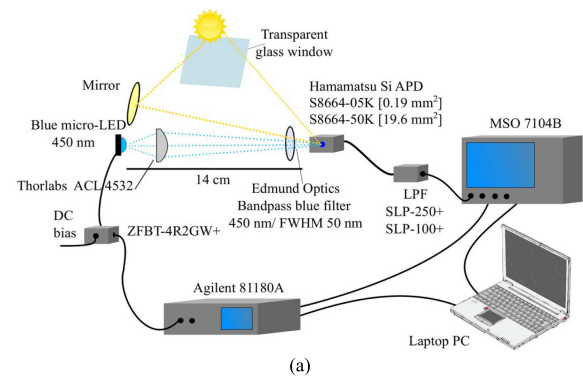


Fig. 7. The experimental set-up. (a) Schematic set-up of the experiment showing the optical system, arbitrary waveform function generator, oscilloscope, electrical and optical filters and Bias-T. (b) Photograph of the optical system showing the micro-LED, optical lenses system and the used APDs. In the top right corner (left): large APD s8664-50k; (right): small APD S8664-05k.

461 spectively. This is experimentally determined as the maximum  
 462 bandwidth that allows for a SNR higher than  $0$  dB to be achieved.  
 463 The electrical signal is then captured using an oscilloscope (Ag-  
 464 ilent, MSO7104B) and then processed using MATLAB. The  
 465 overall distance between the micro-LED and the photodetec-  
 466 tor is  $14$  cm. The received optical power from the micro-LED  
 467 would decrease at longer distances and consequently this would  
 468 degrade the SNR because the SNR diminishes as the desired  
 469 signal diminishes, but not because of noise due to sunlight. The  
 470 distance is limited by the optical power of the micro-LED and  
 471 it can be improved using more advanced collimation optics or  
 472 using micro-LEDs with multiple pixels in a ganging mode [22].  
 473 The three scenarios described in Section III-A are considered  
 474 in the experimental study. The SNR of the channel is first esti-  
 475 mated and then the constellation sizes and the associated power  
 476 of  $M$ -QAM symbols are adaptively allocated to each subcar-  
 477 rier based on the estimated SNR. The adaptive bit and energy  
 478 loading algorithm avoids the use of low-frequency subcarriers,  
 479 where the interference of ambient light can be strong. In addi-  
 480 tion, it avoids any other subcarrier, where the SNR is expected  
 481 to result in a BER below the FEC target.

##### 482 B. Results and Discussions

483 The measured solar irradiance is given in Fig. 8 for the wave-  
 484 lengths between  $350$  and  $750$  nm covering the visible spec-  
 485 trum and part of the infrared and ultraviolet spectra. Four cases  
 486 are presented: direct sunlight; reflected sunlight from a mirror,



TABLE II  
ACHIEVABLE SNR VALUES AND DATA RATES FOR THE SMALL AND LARGE APDs FOR THE THREE CONSIDERED SCENARIOS

	Dark room (Scenario I)		with blue filter (Scenario II)		w/o blue filter (Scenario III)	
	Large APD	Small APD	Large APD	Small APD	Large APD	Small APD
Average SNR [dB]	17.57	18.58	16.64	17.36	12.42	16.42
Data rate @ BER<3.8e-3 [Mb/s]	416.44	1139.26	396.71	1080	313.35	1015

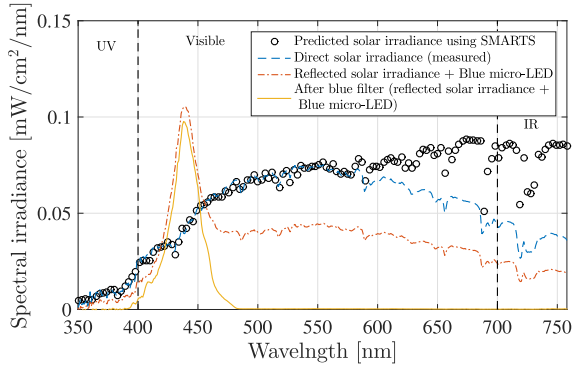


Fig. 8. The spectral distribution of the solar irradiance measured and predicted using SMARTS [20], [21] for Edinburgh (direct, reflected and filtered) in the presence and absence of the desired signal at 450 nm.

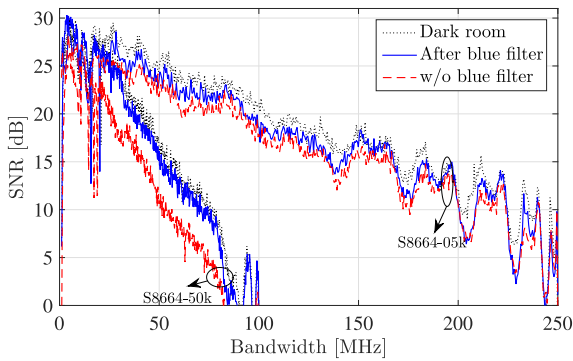


Fig. 9. Experimentally estimated SNR versus the system bandwidth when small and large APDs are used for the three considered scenarios.

487 reflected sunlight and blue micro-LED (Scenario III); and re-  
 488 flected sunlight and blue micro-LED with a blue optical filter  
 489 (Scenario II). The experiment was conducted inside a building  
 490 where the direct sunlight is passed through a transparent glass  
 491 window before it is collected at the photoreceiver. It was practi-  
 492 cally infeasible to realize the experimental setup while the direct  
 493 solar irradiance is always focused into the APD due to the vary-  
 494 ing solar position throughout the experiment duration. A mirror  
 495 was used to work around this issue at the expense of reduced solar  
 496 irradiance. This was shown to have little impact on the blue  
 497 band below 450 nm as it is shown in Fig. 8. The experimen-  
 498 tally measured direct solar irradiance is shown to be identical  
 499 to the simulated solar irradiance below 580 nm. The mismatch  
 500 at longer wavelengths is attributed to the high reflectance and  
 501 less transmittance characteristics of heat mirrors glazing in the  
 502 infrared band that aim to improve building heat insulation [34].  
 503 The experimentally estimated SNR is presented in Fig. 9  
 504 for the small and large APDs at all the considered scenarios.  
 505 All the performance comparisons are presented with reference  
 506 to the optimal dark room (Scenario I). It is shown that the  
 507 performance of the VLC system degrades in the presence of

508 direct sunlight for both APDs. The degradation in the average  
 509 SNR is estimated at 2.16 dB for the small APD and 5.15 dB  
 510 for the large APD in Scenario III. The photocurrents generated  
 511 by both signal and background noise generally increase as the  
 512 detection area of the APD increases. However, an optical source  
 513 with small emission area and an imaging lens are used in this  
 514 experiment to focus the light into the APD. The focused light  
 515 spot size at the APD can ideally be as small as the emission  
 516 area of the micro-LED (0.01 mm<sup>2</sup>) [35]. Therefore, The signal  
 517 photocurrent does not increase when the detection area becomes  
 518 larger than the focused light spot at the APD. This validates the  
 519 result that the SNR degradation is higher for the large APD,  
 520 because it collects more background light. When the blue filter  
 521 is used to restrict the unwanted irradiance, the degradation in  
 522 the average SNR is reduced to 1.22 dB for the small APD  
 523 and 0.93 dB for the large APD. Similar trends are presented in  
 524 Table II for the achieved data rates. All the presented data rates  
 525 are achieved below the FEC limit of  $3.8 \times 10^{-3}$ . The data rate  
 526 decreases in the presence of solar irradiance. However, most  
 527 of this reduction can be recovered using the blue filter. It is  
 528 shown that a data rate of 1.015 Gb/s can be achieved under the  
 529 presence of solar irradiance for the small APD in Scenario III.  
 530 This is equivalent to a 10.4% reduction in data rate compared  
 531 to Scenario I. This degradation can be reduced to 5.2% when  
 532 the blue filter is used. A reduction of 24.75% in the data rates  
 533 is witnessed in Scenario II for the large APD. This is improved  
 534 to 4.73% when using the blue filter in Scenario II.

## V. CONCLUSION

535  
 536 VLC system is feasible in the presence of solar irradiance.  
 537 Worst-case scenarios are considered in this study to prove the  
 538 concept that VLC systems can work under the influence of  
 539 strong solar irradiance. Shot noise caused by sunlight reduces  
 540 the data rate of VLC systems. However, optical bandpass blue  
 541 filters can limit the degradation caused by solar irradiance. Data  
 542 rates above 1 Gb/s were experimentally achieved in the presence  
 543 of solar irradiance without optical filtering. Simulation results  
 544 have shown that an improvement of at least 6.47 dB can be  
 545 achieved for SNR using off-the-shelf blue filters.

546 Saturation is a major drawback for photodiodes in the pres-  
 547 ence of strong background noise. Automatic gain controller  
 548 (AGC) can be used to reduce the likelihood of performance  
 549 outage due to APD saturation. However, this is not considered  
 550 in the current work and will be considered in future research.  
 551 Bandpass optical filtering was considered as a technique to miti-  
 552 gate solar irradiance noise. However, the results of this study  
 553 can be used to build upon and to develop new solar irradiance  
 554 noise mitigation techniques. An interesting solution could be  
 555 envisaged to use angle-diversity receiver with signal combining  
 556 techniques. However, the details of such investigation is out the  
 557 scope of this paper and will be considered in future research.

APPENDIX A  
 SOLAR POSITION

558

559 Three coordinate systems are used to calculate the position of  
 560 the Sun: ecliptic coordinates; equatorial coordinates; and hori-  
 561 zontal coordinates. These coordinate systems can be illustrated  
 562 on the celestial sphere shown in Fig. 10. The parameters cor-  
 563 responding to each coordinate system are mapped in Table III.  
 564 The arbitrary coordinates in Fig. 10 is defined by  $\Theta$  which is the  
 565 angle between the principle and the projection of the Sun at the  
 566 fundamental plane and by  $\Xi$  which is the angle between the Sun  
 567 and the fundamental plane. Celestial coordinate systems can be  
 568 converted into Cartesian coordinates using:

$$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix} = \begin{pmatrix} \cos \Xi \cos \Theta \\ \cos \Xi \sin \Theta \\ \sin \Xi \end{pmatrix}. \quad (14)$$

569 The horizontal coordinate system is usually used for solar  
 570 cell applications where the horizon of the observer is the funda-  
 571 mental plane. The solar position can be projected on a celestial  
 572 sphere using two angles: altitude  $Al$  and azimuth  $Az$ . The Earth  
 573 revolves around the Sun in an elliptic orbit in which a complete  
 574 revolution takes a year, a motion of around  $1^\circ$  per day. This mo-  
 575 tion can be best described using the ecliptic coordinates where  
 576 the principle is the position of the Sun during the spring equinox  
 577 (the date of the year when the Earth's equator is alligned with  
 578 the center of the Sun ecliptic). The angular ecliptic coordinates  
 579 are the ecliptic longitude,  $\lambda$  and ecliptic latitude,  $\beta$ , which is  
 580 given as  $\beta \approx 0$  [18]. The ecliptic longitude can be given as [18]:

$$\lambda = q + 1.915^\circ \sin q + 0.020^\circ \sin 2q, \quad (15)$$

581 where  $q$  is the mean longitude given as [18]:

$$q = 280.459^\circ + 0.98564736^\circ D, \quad (16)$$

582 and  $g$  is the mean anomaly of the Sun, which accounts for the  
 583 varying speeds of the Earth motion throughout the year. This is  
 584 given as [18]:

$$g = 357.529^\circ + 0.98560028^\circ D, \quad (17)$$

585 where  $D$  is the time elapsed since the Greenwich noon of the  
 586 1st of January 2000.

587 The equatorial coordinate system is required as a translational  
 588 stage when transforming the ecliptic coordinates into horizontal  
 589 coordinates, as follows:

$$\begin{pmatrix} X_{Equ} \\ Y_{Equ} \\ Z_{Equ} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \epsilon & -\sin \epsilon \\ 0 & \sin \epsilon & \cos \epsilon \end{pmatrix} \begin{pmatrix} X_{Ecl} \\ Y_{Ecl} \\ Z_{Ecl} \end{pmatrix}, \quad (18)$$

590 where  $\epsilon$  is the axial tilt between the equatorial plane and the  
 591 ecliptic plane. The axial tilt is zero in March and September  
 592 equinox and takes its maximum value of  $\pm 23.429^\circ$  in June  
 593 and December solstices (the days when the maximum tilt is  
 594 expernced at the north and south hemisphere, respectively).  
 595 The axial tilt is given as [18]:

$$\epsilon = 23.429^\circ - 0.00000036^\circ D. \quad (19)$$

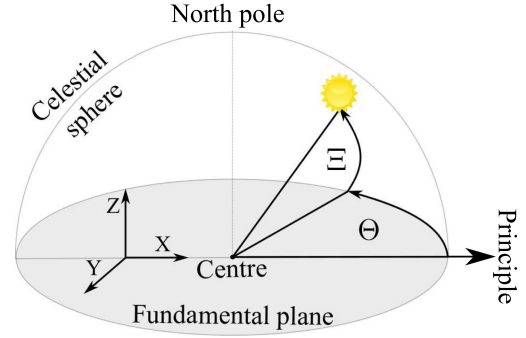


Fig. 10. An illustration of an arbitrary coordinate system on a celestial sphere.

TABLE III  
 COORDINATION SYSTEMS CORRESPONDING PARAMETERS

Arbitrary	Ecliptic	Equatorial	Horizontal
center	center of the Earth	center of the Earth	observer
north pole	north ecliptic pole	north celestial pole	zenith
fundamental plane	ecliptic	celestial equator	horizon
principle	March equinox	March equinox	geographic north pole
$\Theta$	ecliptic longitude ( $\lambda$ )	right ascension ( $\alpha$ )	azimuth ( $Az$ )
$\Xi$	ecliptic latitude ( $\beta$ )	declination ( $\delta$ )	altitude ( $Al$ )
$\begin{pmatrix} X \\ Y \\ Z \end{pmatrix}$	$\begin{pmatrix} X_{Ecl} \\ Y_{Ecl} \\ Z_{Ecl} \end{pmatrix}$	$\begin{pmatrix} X_{Equ} \\ Y_{Equ} \\ Z_{Equ} \end{pmatrix}$	$\begin{pmatrix} X_{Hor} \\ Y_{Hor} \\ Z_{Hor} \end{pmatrix}$

The equatorial coordinates are given by the right ascension  $\alpha$  596  
 which is the angle between the March equinox and the projection 597  
 of the Sun on the Earth's equator and by the declination  $\delta$  which 598  
 is the angle between the Sun and the Earth equator. The Sun 599  
 moves  $15^\circ$  of longitude per hour. The hour angle is defined as 600  
 the angle between the projection of the Sun on the fundamental 601  
 plane and the meridian given at longitude of  $0^\circ$  (an imaginary 602  
 circle passing through the north and south poles and the zenith 603  
 of an observer). The hour angle is given by: 604

$$h = \theta_L - \alpha, \quad (20)$$

where  $\theta_L$  is the angle between the meridian and the March 605  
 equinox. It can also be defined as the local mean sidereal time 606  
 (LMST). A sidereal day is the time that the Earth takes to com- 607  
 plete a  $360^\circ$  rotation on its own axis. It is slightly shorter than 608  
 the solar day mainly due to the rotation of the Earth around the 609  
 Sun. The LMST can be given as: 610

$$\theta_L = \text{GMST} \frac{15^\circ}{\text{hour}} + \lambda_0, \quad (21)$$

where  $\lambda_0$  is the longitude of the observer and GMST is the 611  
 Greenwich mean sidereal time (GMST), which is defined as 612  
 the hour angle between the March equinox and the meridian at 613  
 Greenwich. GMST is calculated as [18]: 614

$$\text{GMST} = 18.697374558h + 24.06570982441908hD, \quad (22)$$

where it is scaled to values between 0 and 24.

615

616 The principle of the coordinates can be transformed from the  
617 March equinox to the LMST using:

$$\begin{pmatrix} \cos \delta \cos h \\ \cos \delta \sin h \\ \sin \delta \end{pmatrix} = \begin{pmatrix} \cos \theta_L & \sin \theta_L & 0 \\ 3pt \sin \theta_L & -\cos \theta_L & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} X_{\text{Equ}} \\ Y_{\text{Equ}} \\ Z_{\text{Equ}} \end{pmatrix}, \quad (23)$$

618 In addition, the center of the coordinates can be transformed  
619 from the center of the Earth to the position of the observer using:

$$\begin{pmatrix} X'_{\text{Hor}} \\ Y'_{\text{Hor}} \\ Z'_{\text{Hor}} \end{pmatrix} = \begin{pmatrix} \sin \phi_0 & 0 & -\cos \phi_0 \\ 0 & 1 & 0 \\ \cos \phi_0 & 0 & \sin \phi_0 \end{pmatrix} \begin{pmatrix} \cos \delta \cos h \\ \cos \delta \sin h \\ \sin \delta \end{pmatrix} \quad (24)$$

620 Following the prior calculations, the directions of  $X'_{\text{Hor}}$  and  
621  $Y'_{\text{Hor}}$  are directed towards south and west, respectively. The  
622 following can be applied to adjust the reference direction to  
623 north and east [18]:

$$\begin{pmatrix} X_{\text{Hor}} \\ Y_{\text{Hor}} \\ Z_{\text{Hor}} \end{pmatrix} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} X'_{\text{Hor}} \\ Y'_{\text{Hor}} \\ Z'_{\text{Hor}} \end{pmatrix} \quad (25)$$

624 The horizontal coordinates can then be calculated using [18]:

$$\sin Al = \cos \phi_0 \cos \theta_L \cos \lambda_S + (\cos \phi_0 \sin \theta_L \cos \epsilon + \sin \phi_0 \sin \epsilon) \sin \lambda_S \quad (26)$$

$$\tan Az = \frac{\Gamma_1}{\Gamma_2 - \Gamma_3}, \quad (27)$$

625 where:

$$\Gamma_1 = -\sin \theta_L \cos \lambda_S + \cos \theta_L \cos \epsilon \sin \lambda_S, \quad (28)$$

$$\Gamma_2 = -\sin \phi_0 \cos \theta_L \cos \lambda_S, \quad (29)$$

$$\Gamma_3 = \sin \lambda_S (\sin \phi_0 \sin \theta_L \cos \epsilon - \cos \phi_0 \sin \epsilon), \quad (30)$$

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