

A numerical study of interactions and stellar bars

Inma Martínez-Valpuesta,^{1,2★} J. Alfonso L. Aguerri,^{1,2★} A. César González-García,³
Claudio Dalla Vecchia^{1,2} and Martin Stringer^{1,2}

¹*Instituto de Astrofísica de Canarias, E-38205 La Laguna, Tenerife, Spain*

²*Universidad de La Laguna, Dpto. Astrofísica, E-38206 La Laguna, Tenerife, Spain*

³*Instituto de Ciencias del Patrimonio, CSIC, Santiago de Compostela, E-15704 A Coruña, Spain*

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ABSTRACT

For several decades, it has been known that stellar bars in disc galaxies can be triggered by interactions, or by internal processes such as dynamical instabilities. In this work, we explore the differences between these two mechanisms using numerical simulations. We perform two groups of simulations based on isolated galaxies, one group in which a bar develops naturally, and another group in which the bar could not develop in isolation. The rest of the simulations recreate 1:1 coplanar fly-by interactions computed with the impulse approximation. The orbits we use for the interactions represent the fly-bys in groups or clusters of different masses accordingly to the velocity of the encounter. In the analysis, we focus on bars' amplitude, size, pattern speed and their rotation parameter, $\mathcal{R} = R_{\text{CR}}/R_{\text{bar}}$. The latter is used to define fast ($\mathcal{R} < 1.4$) and slow rotation ($\mathcal{R} > 1.4$). Compared with equivalent isolated galaxies, we find that bars affected or triggered by interactions: (i) remain in the slow regime for longer, (ii) are more boxy in face-on views and (iii) they host kinematically hotter discs. Within this set of simulations, we do not see strong differences between retrograde or prograde fly-bys. We also show that slow interactions can trigger bar formation.

Key words: methods: numerical – galaxies: evolution – galaxies: interactions – galaxies: kinematics and dynamics – galaxies: structure.

1 INTRODUCTION

Bars are ellipsoidal-like features present in a large fraction of discs galaxies. About 40–50 per cent of the galactic discs in the local Universe observed in the optical show a bar structure (see e.g. Marinova & Jogee 2007; Aguerri, Méndez-Abreu & Corsini 2009; Díaz-García et al. 2016). This fraction increases up to ~ 60 –70 per cent when observing in the near-infrared (see Eskridge et al. 2000; Menéndez-Delmestre et al. 2007). The fraction of barred galaxies depends on several integrated properties such as: galaxy stellar mass, star formation history, and colour (see Nair & Abraham 2010; Masters et al. 2011; Méndez-Abreu et al. 2012). The fraction is decreasing with increasing redshift (see Melvin et al. 2014), though this variation depends strongly on other internal galaxy properties such as mass, colour or bulge prominence (see e.g. Sheth et al. 2008).

Bars have a strong influence on the dynamics of disc galaxies. In particular, the presence of bars highly influences the exchange of angular momentum between the different galaxy components, mainly, halo and disc (see Lynden-Bell & Kalnajs 1972; Tremaine & Weinberg 1984; Weinberg 1985; Debattista & Sellwood 1998,

2000; Athanassoula 2002; Martínez-Valpuesta, Shlosman & Heller 2006; Saha, Martínez-Valpuesta & Gerhard 2012). They are also related to gas inflow and star formation events (see e.g. Hernquist & Mihos 1995; Martinet & Friedli 1997; Aguerri 1999). The growth and feeding of central supermassive black holes in galaxies can also be driven by bars (see Shlosman, Begelman & Frank 1990; Corsini, Debattista & Aguerri 2003).

Three main observational parameters characterize bars in galaxies: the length, the strength and the pattern speed. The bar length determines the extension in the disc of the orbits building the bar (Contopoulos 1981). The length of bars has been determined observationally with different methods: optical visual inspection (see e.g. Kormendy 1979; Martin 1995), locating the maximum of the isophotal ellipticity (see Wozniak et al. 1995; Márquez et al. 1999; Laine et al. 2002; Marinova & Jogee 2007; Aguerri et al. 2009; Díaz-García et al. 2016), or structural decompositions of the galaxy surface brightness (see Prieto et al. 1997, 2001; Aguerri et al. 2001; Aguerri, Debattista & Corsini 2003; Aguerri et al. 2005; Gadotti 2008; Laurikainen et al. 2009; Weinzirl et al. 2009).

The bar strength measures non-axisymmetric forces produced by the bar potential. It is determined with several methods: measuring the torques of the bar from photometry (see Combes & Sanders 1981; Quillen, Frogel & Gonzalez 1994; Buta & Block 2001; Salo

* E-mail: imv@iac.es (IM-V); jalfonso@iac.es (JALA)

et al. 2010; Díaz-García et al. 2016), or from kinematics (Seidel et al. 2015), measuring the bar ellipticity (see Martinet & Friedli 1997; Aguerri 1999; Whyte et al. 2002), or with Fourier decomposition of the galaxy light (see Ohta, Hamabe & Wakamatsu 1990; Marquez, Moles & Masegosa 1996; Aguerri et al. 2000; Laurikainen, Salo & Buta 2005; Díaz-García et al. 2016).

The bar pattern speed is defined as the rotational frequency of the bar. This dynamical parameter has been determined in the literature through several methods, among them: hydrodynamical simulations of barred galaxies (see e.g. Lindblad, Lindblad & Athanassoula 1996; Laine & Heller 1999; Aguerri et al. 2001; Weiner, Sellwood & Williams 2001; Pérez, Fux & Freeman 2004; Treuhardt et al. 2008), identifying galaxy structures with Lindblad resonances (see Buta & Combes 1996; Muñoz-Tuñón, Caon & Aguerri 2004; Pérez, Aguerri & Méndez-Abreu 2012), changes in the morphology or phase of spiral arms with radius (see Puerari & Dottori 1997; Aguerri et al. 2000; Sierra et al. 2014), the so-called Tremaine–Weinberg method (see Kent 1987; Merrifield & Kuijken 1995; Gerßen, Kuijken & Merrifield 1999; Debattista, Corsini & Aguerri 2002; Aguerri et al. 2003; Corsini et al. 2003; Debattista & Williams 2004; Corsini et al. 2007; Treuhardt et al. 2007; Aguerri et al. 2015), or studying the morphology of the residual gas velocity field after the rotation velocity subtraction (Sempere et al. 1995; Font et al. 2011, 2014).

Observationally, it has been shown that bar parameters depend on morphological galaxy properties. Thus, length and strength depend on the galaxy Hubble type. In particular, S0 galaxies show larger bars than late-type ones (see Elmegreen & Elmegreen 1985; Erwin 2005; Menéndez-Delmestre et al. 2007; Aguerri et al. 2009), but see also Masters et al. (2011) for a different perspective. In addition, S0 galaxies show weaker bars than late-type ones (see Laurikainen et al. 2007; Aguerri et al. 2009; Buta et al. 2010). The dependence of the bar pattern speed on the morphological type is not so evident (see Aguerri et al. 2015).

Numerical simulations show that bar parameters evolve with time in isolated discs. These simulations show that evolution proceeds through three main phases. The first phase corresponds to the bar formation and extends ~ 2 Gyr. During this period, the bar strength and bar length grows rapidly. The bar is formed and clearly visible in the disc. During the second phase, the bar buckles (Combes & Sanders 1981; Raha et al. 1991). The time extension of this phase is about 1 Gyr, and the bar becomes shorter and weaker (Martinez-Valpuesta & Shlosman 2004). The third phase of the bar formation extends for several gigayears and is generally called secular evolution epoch. During this phase, bar grows slowly by increasing its length and strength. In contrast, its pattern speed continuously decreases through all these phases (see Martinez-Valpuesta et al. 2006). The rate at which bar parameters change during the three phases depends on several properties of the galaxy: dark matter content (Debattista & Sellwood 1998, 2000), gas content (Athanassoula, Machado & Rodionov 2013), the disc kinematics (see Athanassoula 1996), and even the shape of the dark matter halo (see Athanassoula 2003).

The general evolution described above is all based on simulations of isolated galaxies. But we know that galaxies interact. Are there any external influences in the formation and evolution of bars? What is the ‘nature’ versus ‘nurture’ of bars? Which is the role played by the environment in the bar formation and evolution? There are examples in the Universe of isolated galaxy pairs showing prominent bar features (see e.g. Fuentes-Carrera et al. 2004). These cases point towards the influence of the environment on the bar formation that is also studied in other galaxy samples. The pioneering work of Thompson (1981) showed an increased fraction of barred galaxies

in the central region of the Coma cluster indicating that tidal interactions trigger bar formation. Similar results were also found in other samples, especially for early-type galaxies (see Giuricin et al. 1993; Andersen 1996; Eskridge et al. 2000; Barazza et al. 2009; Lansbury, Lucey & Smith 2014; Lin et al. 2014). More recently, Méndez-Abreu et al. (2012) showed that the effect of the environment on the bar formation depends on the mass of the galaxy. They proposed that interactions trigger bar formation in massive galaxies, which are stable enough to keep their cold discs even in galaxy clusters. In contrast, the discs of low-mass haloes are heated by interactions inhibiting the bar formation.

N -body simulations have shown that interactions trigger bar formation in discs stable against their development in isolation (see Noguchi 1987; Aguerri & González-García 2009; Lang, Holley-Bockelmann & Sinha 2014). The strengths and the angular velocities of the bars change due to resonant transfer of angular momentum or mass-loss from the end of the bar produced by interactions (see e.g. Gerin, Combes & Athanassoula 1990; Sundin, Donner & Sundelius 1993; Miwa & Noguchi 1998). The variation of the bar parameters produced by tidal effects depends on the mass of the perturber and/or the relative phase of the bar and the companion at pericentre (see Gerin et al. 1990; Sundin et al. 1993). Miwa & Noguchi (1998) found that bars induced by simulations are confined to the Inner Lindblad Resonant, producing slow bars.

Simulations including gravity and hydrodynamics have shown that the gas phase plays an important role in bars formed by tidal events. In this case, depending on the orbital parameters of the perturber, interactions tend to speed up the transition from a galaxy with a strong bar to one with a weak or even without a bar (see Berentzen et al. 2003). Moreover, cosmological simulations show that bars can be formed and destroyed several times during a galaxy’s lifetime depending on the accretion history (see Romano-Díaz et al. 2008). The mass ratio between the main galaxy and the perturber creating the interaction determines bar formation in the main galaxy, in the perturber, or even in both (see e.g. Kazantzidis et al. 2011; Lang et al. 2014; Łokas et al. 2014).

In this work, we revisit the case of the influence of interactions on bar formation. The aim of this paper is to analyse the change produced by interactions on the observable bar parameters. Several high-resolution N -body simulations have been run to achieve this goal.

This paper is organized as follows. Section 2 shows the description of the simulations. The main results are given in Sections 3–5. The discussion and conclusions are shown in Sections 6 and 7, respectively.

2 DESCRIPTION OF SIMULATIONS

Our main goal is to determine dynamical differences between galactic bars that are self-generated and those that are purely induced by tidal interactions. Our approach uses N -body numerical simulations. The simulations have been run with an improved version of FTM4-4 (Heller & Shlosman 1994), using the potential solver falcON (Dehnen 2002). We have run two fiducial simulations in isolation. The simulation is initiated with: 5×10^5 particles describing the exponential disc and the same number for the dark matter halo. This number of particles assures that we achieve the necessary resolution to resolve resonances and therefore properly follow the formation and evolution of the bar (see e.g. Weinberg & Katz 2007a,b; Dubinski, Berentzen & Shlosman 2009). The halo distribution is generated following Fall & Efstathiou (1980). The rotating exponential disc is set with Toomre $Q = 1.5$, scalelength

of 2.85 kpc. The gravitational softening is 160 pc for all particles and the haloes extend out to ~ 30 kpc. The only difference between these two simulations is the fraction of baryonic matter. For SIMIO, 30 per cent of the total mass within a radius of 7 kpc is in the disc. In the case of SIMI1, 50 per cent of the total mass within 7 kpc is in the disc. The mass of these galaxies is $3.99 \times 10^{11} M_{\odot}$ for SIMIO and $2.17 \times 10^{11} M_{\odot}$ for SIMI1. At the edge of the disc, the stars are rotating at $\sim 200 \text{ km s}^{-1}$. With these settings, we have two types of isolated galaxies: one that does not develop a bar in isolation (SIMIO) and one that develops a strong bar (SIMI1).

We are interested in fast fly-by interactions, where there is insufficient time for the systems to react during the encounter, and all the effects develop after the interaction have taken place (González-García, Aguerri & Balcells 2005). In order to speed up the numerical calculations, we have modelled the interaction with the impulse approximation (IA). The modified model is then run in isolation for ~ 5 Gyr in order to see the effects of such interaction.

2.1 Impulse approximation

By applying the IA, we assume that the galaxy has no time to reorganize during the encounter, so that all the energy is injected as kinetic energy. Reorganization within the potential of the host halo occurs after the encounter has finished. We also make use of formulas based on the tidal approximation (Binney & Tremaine 1987, section 7.2d), in which the tidal field has been expanded to first order.

In the tidal approximation, after a fast interaction with a perturber of mass M_1 , the change of velocity of the stars of the perturbed galaxy, ΔV_2 , scales linearly with the galactocentric radius, R . The standard tidal approximation considers the perturber as a point mass. Following Gnedin, Hernquist & Ostriker (1999), González-García et al. (2005) generalized the approximation equations in order to take into account not only the extended nature of the perturber, but also the rotation of the perturbed galaxy and the duration of the encounter. From their equation (4), which gives the variation of kinetic energy, the absolute value of the velocity perturbation is

$$|\Delta V_2(R)| \sim 2 \frac{GM_1}{b^2 V} \frac{R_{\text{peri}}}{R_{\text{max}}} R (1 - \omega\tau)^{-1.25}, \quad (1)$$

where R_{peri} is the pericentre distance, b is the orbital impact parameter, V is the relative velocity at the pericentre passage, and $R_{\text{max}} = 15 \text{ kpc}$ the perturber's cut-off radius. The rightmost term includes the rotation frequency of the perturbed galaxy, ω , and the encounter's duration, τ .

All simulations were performed assuming that the encounters are between galaxies of the same size and mass. In addition, the disc of the galaxy and the orbit of the perturber are co-planar. Therefore, encounters are either prograde or retrograde. Initial conditions were generated for prograde and retrograde encounters, the latter by keeping the same orbital configuration and inverting the spin of the perturbed galaxy by flipping the particle distribution. The orbit has pericentre at distance $R_{\text{peri}} = 30 \text{ kpc}$ from the centre of the galaxy. The relative velocity at the pericentre passage is 500, 1000, and 2000 km s^{-1} to ensure that the orbit is hyperbolic, and that we are comfortably in the regime of non-merging initial conditions (González-García & van Albada 2005). The parameters of the simulations are summarized in Table 1.

For model SIMI1, which develops a bar and experiences a buckling instability, we would like to see the impact of the interaction at the two different evolutionary stages, before and after the buckling. We introduce the IA at different times (see Table 1), one before the

Table 1. Orbital parameters of the simulated interactions. All simulations where run with hyperbolic orbits and for three different velocities 500, 1000, 2000 km s^{-1} .

NAME	R_{peri} (kpc)	Spin	Time
I0_d_2000	30	P	$t_{01} = 1.45 \text{ Gyr}$
I0_d_1000			
I0_d_500			
I0_i_2000	30	R	$t_{01} = 1.45 \text{ Gyr}$
I0_i_1000			
I0_i_500			
I1_d_2000	30	P	$t_{11} = 1.45 \text{ Gyr}$
I1_d_1000			
I1_d_500			
I1_i_2000	30	R	$t_{11} = 1.45 \text{ Gyr}$
I1_i_1000			
I1_i_500			
I1.00.30.d.t12.h	30	P	$t_{12} = 4.80 \text{ Gyr}$
I1.00.30.i.t12.h	30	R	$t_{12} = 4.80 \text{ Gyr}$

buckling (t_{11}) and one after the buckling (t_{12}) when the bar has already resumed its evolution.

3 EFFECTS OF THE INTERACTION ON BAR PARAMETERS

In this section, we describe the main results obtained from the simulations. As we stated above, we focus on interactions with pericentres at 30 kpc. We have also studied those with 15 kpc, but consider the end product not to be as reliable in this case; we would be using the IA for an interaction where the discs of both galaxies are overlapping.

We approach the effect of the interaction by analysing some of the main parameters used in the literature to classify and describe stellar bars and their evolution. These are the bar amplitude, bar length, pattern speed, and the rotation parameter, $\mathcal{R} = R_{\text{CR}}/R_{\text{bar}}$, related to how fast or slow the bar is, and to the mass distribution of the different components, mainly, the halo and the disc (e.g. Aguerri et al. 2003, 2015; Pérez et al. 2012).

The bar amplitude is computed as the amplitude of the second coefficient of Fourier density decomposition. In detail, this can be computed by

$$A_{m,r}(R) = \frac{1}{N_s} \left| \sum_j^{N_s} e^{im\theta_j} \right|, \quad m = 1, 2, \dots, \quad (2)$$

where θ_j is the azimuthal angle of particle j and N_s is the number of particles included in the summation. Here, the summation is over all particles with a cylindrical radius within a range around a given R value, giving a measure of the bar strength at that radius. From the same density distribution, the bar pattern speed is calculated from the phase angle of the bar.

The bar length is taken at the radius where the ellipticity is 10 per cent lower than the maximum (Martínez-Valpuesta et al. 2006). Finally, R_{CR} is the radius where the angular velocity equals the pattern speed.

3.1 SIMI1: bar in isolation

Simulation SIMI1 was already presented in Martínez-Valpuesta & Gerhard (2011), where it was scaled to match the Milky Way bar length and solar velocity. Here with a different scaling, the disc

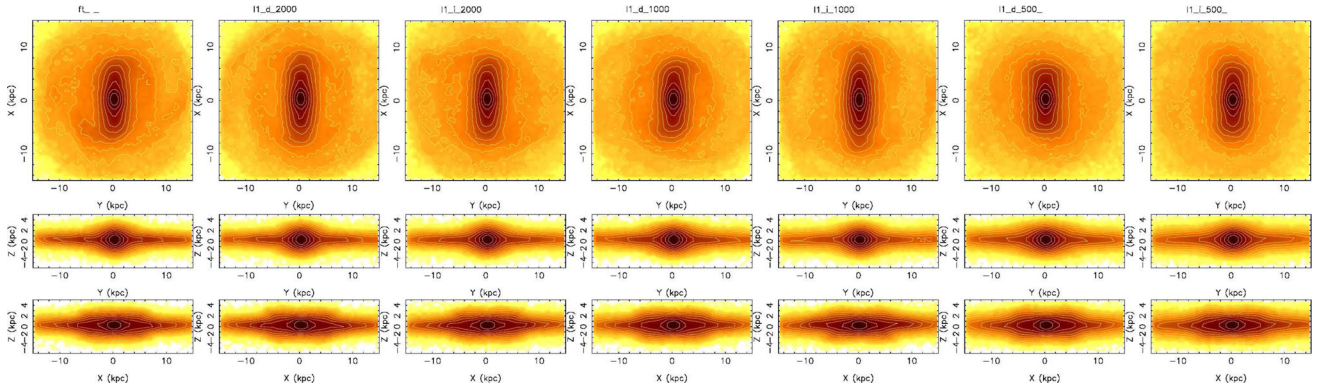


Figure 1. Density maps in three projections. The original simulation SIM11 is plotted on the left and then from fast to slow interaction. These are plotted at time $\tau = 4.18$ Gyr, sometime after the big drop in bar strength to give the bar time to resume its evolution.

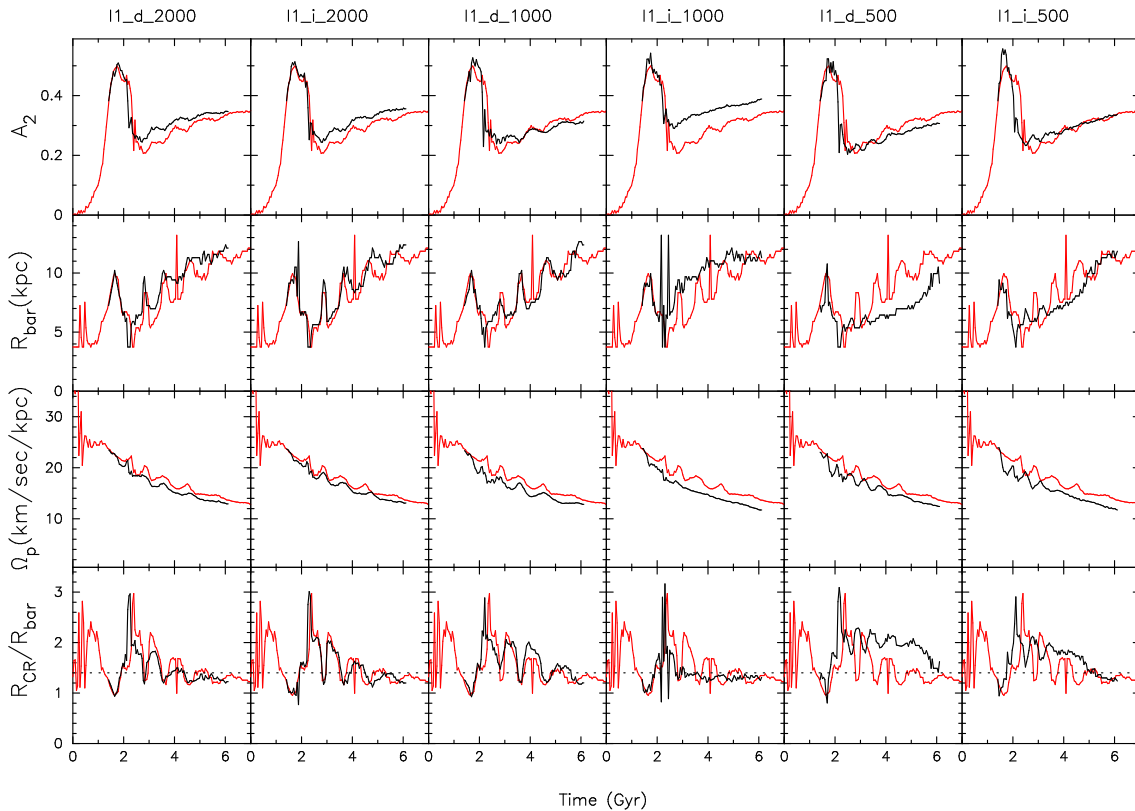


Figure 2. Time evolution of bar parameters for the model in isolation, SIM11 (red line) and for the simulations of interactions introduced at t_{11} . From top to bottom, we show bar amplitude, bar length, bar pattern speed, and \mathcal{R} .

develops a flat bar in less than 2 Gyr, and by 3 Gyr, it already buckles. Then, the bar weakens and resumes its evolution, changing its structure and slowly becoming longer, stronger and thicker, forming a peanut/boxy structure when seen edge-on. In Martinez-Valpuesta et al. (2006), there is a more detailed explanation of general bar dynamical and secular evolution, including details of the different buckling events. As a representative snapshot, we choose time $\tau = 4.18$ Gyr (Fig. 1, first column). The three panels show face-on, end-on, and side-on projection of SIM11. The general time evolution of the bar parameters for SIM11 can be seen in Fig. 2 (red line). We can see the amplitude of the bar increasing rapidly until the buckling event, then increasing slowly (secular phase). The size of the bar suffers similar evolution. The pattern speed decreases continuously, anticorrelating with the bar amplitude (e.g. Athanas-

soula 2003). The parameter \mathcal{R} fluctuates accordingly to the variations of R_{bar} but, in general, most of the time the bar is fast ($\mathcal{R} \lesssim 1.4$).

Our first experiment is based in a 1:1 fly-by with a perturbed galaxy (SIM11) that has already been able to form and evolve a bar. In order to quantify these characteristics and its effects, we measure the bar strength, the bar length, the pattern speed, and \mathcal{R} . In Fig. 2, we show the evolution of these measurements with time. The resulting bar after the interaction at early and late times (t_{11} and t_{12}) has very similar properties to those of the bar created in isolation. The most significant difference, for most of the evolution, is the bar becoming slower in terms of the pattern speed. This slowdown is even bigger when the maximum of the interaction occurs after the bar has already buckled (t_{12}). As expected, the

effect is always stronger when the interaction is slower (I1_i_500). Gerin et al. (1990) have shown that the angular frequency of the bar is not imposed by the perturber and no difference was found between the isolated and the perturbed experiment. This slowdown in angular frequency in our simulations is translated into a slowdown in terms of \mathcal{R} . After the bar buckles and regrows again, the bar becomes considerably shorter and slower, and for at least 4 Gyr, stays as slow as $\mathcal{R} > 1.8$. In the slow interactions, I1_i_500 and I1_d_500, this effect is very important, being up to ~ 30 per cent slower in \mathcal{R} than in the isolated case.

3.2 SIMI0: no-bar in isolation

This simulation, as mentioned previously in Section 2, was conceived to not form a bar in isolation. The main reason is the ratio of dark matter halo mass and disc mass within the inner 7 kpc. From previous theoretical works (Athanasoula 2003), and our own experience, we know that massive central concentration of mass in the inner part at the initial development of the bar (70 per cent of mass in the halo) and absence of mass to acquire angular momentum in the outer parts, at later times, are the main causes for non-developing a bar for more than 6 Gyr.

The interaction by IA is introduced at time $\tau = 1.5$ Gyr. At the time of the interaction, the halo and the disc lose angular momentum because of the tidal distortion. Later on, when the bar is forming, the disc loses angular momentum and the halo gains it, as in the standard angular momentum transfer scenario (Debattista & Sellwood 1998, 2000; Athanasoula 2003; Martínez-Valpuesta et al. 2006). As we showed before, the slower the interaction, the stronger the effect. For our first case, with $v = 2000 \text{ km s}^{-1}$, the effect is small but still noticeable. There is a weak bar developing (Fig. 3). We can also see how the bar becomes stronger when the velocity of the encounter decreases. Another clear feature of the galaxies affected by the interaction is the amount of structure developed in the disc, from spiral arms to rings (see Fig. 3).

Let us now describe in detail the evolution of I0_i_500 (Fig. 4). The big amplitude of the A_2 mode is initially due to the spiral arms induced by the interactions and then the strength is due to the recently created bar. The first big drop in bar amplitude at $\tau \sim 2.3$ Gyr (four top left panels) of the bar corresponds to a first buckling event. In the second weakening, the bar becomes rounder and therefore weaker. The bar length grows together with amplitude. And contrary to standard bar evolution, the pattern speed trend does not anticorrelate with amplitude and stays almost constant with time. Since the bar keeps on growing and the pattern speed is close to constant, the \mathcal{R} parameter decreases with time. As we show before for the interaction for SIMI1, most of the time, the bar is in the slow regime ($\mathcal{R} > 1.4$). Towards the end of the simulation, $\tau \sim 6$ Gyr, the bar becomes fast with $\mathcal{R} \sim 1.4$.

In this set of simulations (SIMI0), although some of them develop a bar, the standard bar evolution in simulations is not seen. For example, buckling event and secular growth are seen just in the slow interaction (strong). In the intermediate interaction (1000 km s^{-1} , I0_d_1000, I0_i_1000), the bar is weak, with $A_2 \sim 0.2$, and keeps on growing in length and strength but does not buckle. In this particular simulation, the growth of the bar in length and the constancy of the pattern speed, Ω_p , results in the bar being very slow with $\mathcal{R} \sim 2$.

4 EFFECTS OF THE INTERACTION ON PHOTOMETRICAL PROPERTIES

Photometric signatures are, in general, observationally cheaper than kinematic measurements. Therefore, we start describing the pho-

tometical signatures for the different bars. First, we focus on the ellipticity for the set of simulations for SIMI1. Broadly speaking, the ellipticity of the bars varies from 0.7 before the buckling to $\epsilon \simeq 0.5$ after the buckling event and then slowly increases up to 0.6. The simulations where the ellipticity is smallest are I1_500, but note that the difference within this set is no more than $\delta\epsilon \leq 0.1$. For the set of simulations, SIMI0, the ellipticity in the strongest case, I0_500, is, on average, ~ 0.65 .

In general, we have noticed that certain bars influenced by the interaction are clearly more boxy, in face-on view, than those created in isolation (Fig. 1). We have analysed the boxiness parameter, $100(a_4/a)$, which is a clear indicator of boxy isophotes if negative and discy isophotes if positive (Bender 1988). We obtain negative values in the outer parts of the bars, with average value for the I1 series of $100(a_4/a) = -0.2$. At the end of the bar, the value reaches the minimum. The differences between those bars affected by the interactions are very small, $100(a_4/a) \sim 0.1$. For the slow prograde interaction, the boxiness parameter reaches $100(a_4/a) = -0.25$ for 20 per cent of the bar length. The set SIMI0 is not boxy at all and this is also reflected in a slightly higher ellipticity of the induced bar.

It is clear when looking at density maps (Fig. 1) that the bar structure has slightly changed in the 3D view. For example, in the fast interaction (2000 km s^{-1}), both prograde and retrograde, the bar has become longer and somehow ‘more pinched’ in the boxy bulge. For the very slow interaction (500 km s^{-1}), the bar becomes shorter and also pinched in the boxy bulge.

In general, bars created in isolation show a boxy-peanut region that extends up to two-third of the bar length (Athanasoula & Misiriotis 2002). In our study, the bars induced purely by the interactions show the thick vertical part reaching almost the extension of the whole bar. We also see how clearly the discs hosting bars triggered by the interaction have a higher number of structures, including rings and long-lived multispirals, as clearly seen in Fig. 3. As a result, the bar and the spiral arms merge sometimes making the bar stronger during those periods. The spiral arms then form a ring and the bar weakens considerably. These features are also related to how kinematically hot the different resulting discs are, as we show in the next section.

5 EFFECTS OF THE INTERACTION ON KINEMATIC PROPERTIES

We have seen that bars created or affected by interactions are slower for longer time (always in terms of $\mathcal{R} > 1.4$) than those created in isolation. In this section, we explore the kinematic imprints of this influence. We will compare each of the isolated galaxies, SIMI0 and SIMI1, with those in the corresponding series where the effect of the interaction is stronger, I0_i_500 and I1_i_500, respectively. In Figs 5 and 6, we show kinematic maps. The aim of these figures is to show general patterns found in those bars affected or created by interactions.

5.1 SIMI1 and I1_i_500

In terms of density distribution in any of the shown views (face-on, mildly inclined, and side-on), we cannot see major differences between bars influenced by an interaction and those in isolation (Fig. 5, top row). The same is true for velocity maps. We start seeing the effect of the interaction in the velocity dispersion of the disc, although not in the vertical direction σ_z . We can clearly see an effect in the mildly inclined frame, which shows a composition

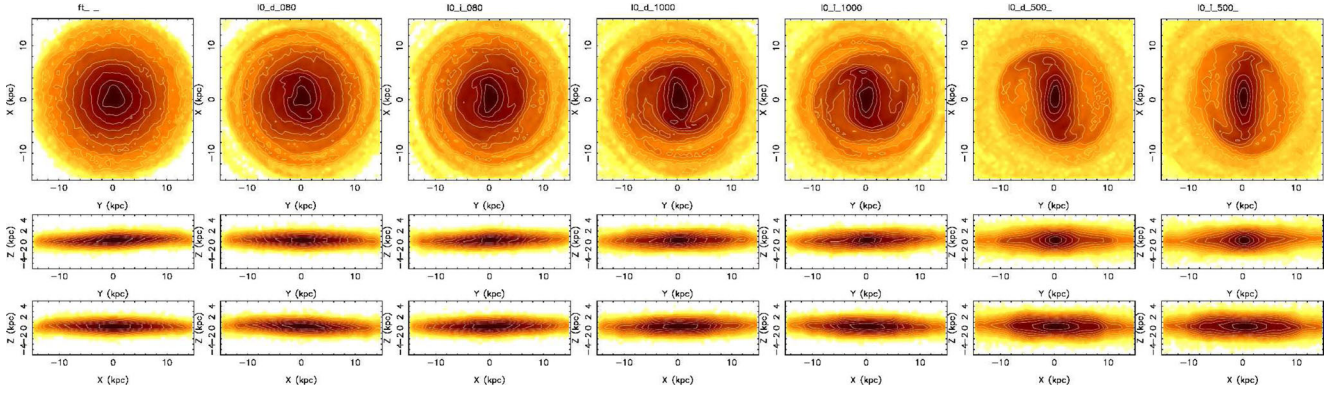


Figure 3. Density maps in three projections. The original simulation SIMIO is plotted on the left and then from fast to slow interaction. These plots correspond to time $\tau = 4.18$ Gyr.

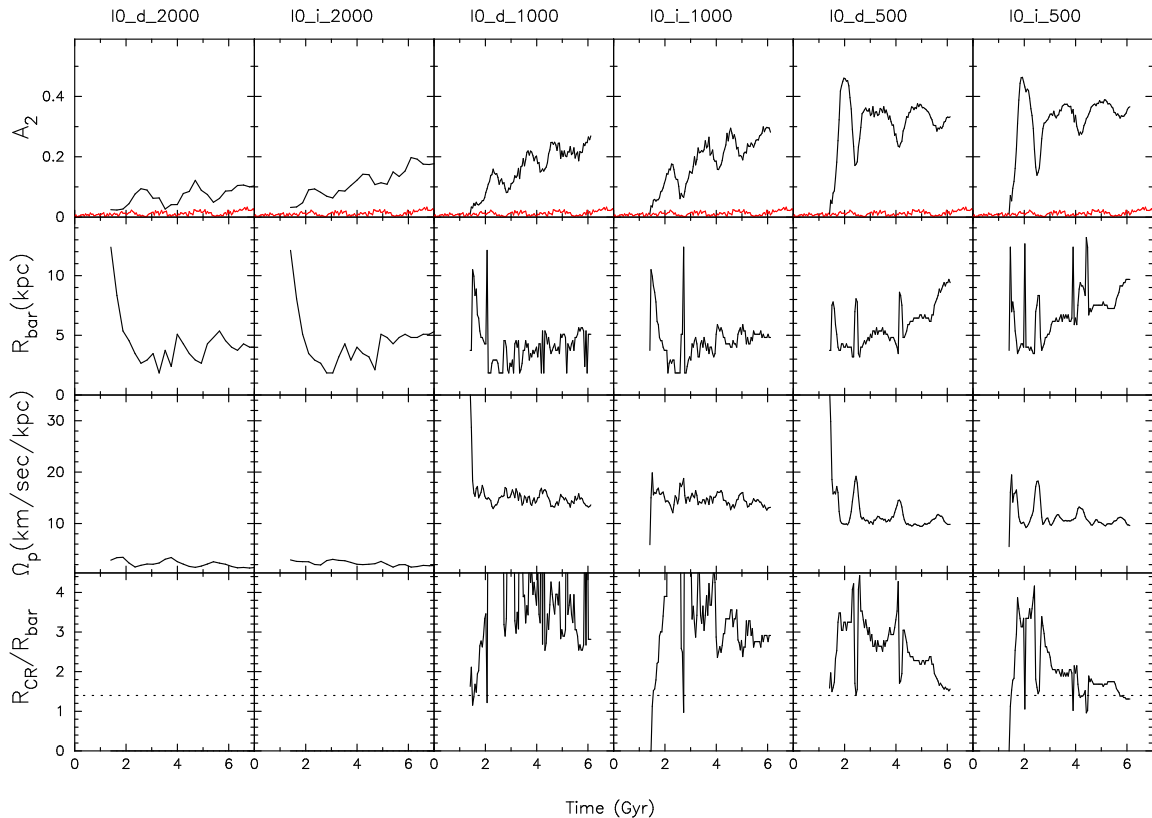


Figure 4. Time evolution of bar parameters for the model in isolation, SIMIO (red line), and for the simulations of interactions introduced at t_{11} . From top to bottom, we show bar amplitude, bar length, bar pattern speed, and \mathcal{R} .

of the three velocity components. On average, in the region $R_{\text{bar}} < r < 1.5R_{\text{bar}}$, and on the intermediate inclination ($inc = 60^\circ$), the velocity dispersion of the disc doubles from 15 km s^{-1} in isolation to 28.5 km s^{-1} with the interaction. But when we look at the edge-on view, we can see the increment in velocity dispersion much better. This is because the interaction increases the radial and the tangential composite velocity dispersion. In the outer parts, for $x > 10 \text{ kpc}$, the value for the isolated case corresponds to $\sim 21 \text{ km s}^{-1}$ and for the interaction to $\sim 42 \text{ km s}^{-1}$.

For high-velocity moments in the Gauss–Hermite decomposition, such as h_3 and h_4 , we see more enhanced structure than for velocity and velocity dispersion. The spiral structure is clearly seen in h_3 for the interacting case, in the mildly inclined orientation (Fig. 5,

fifth column). The surroundings of the bar also have higher absolute values for both h_3 and h_4 in comparison with the isolated case. The $v-h_3$ anticorrelation in this case is a clear indicator of disc kinematics. As already known, the opposite is true for barred kinematics, where the correlation is expected. For example, in the side-on view, in the boxy-dominated area, there is a clear correlation $v-h_3$ (for more information on these issues, see Bureau & Athanassoula 2005 and Iannuzzi & Athanassoula 2015).

5.2 SIMIO and IO_i_500

The general characteristics of the density and kinematics moments maps for SIMIO are standard for a normal non-barred disc galaxy.

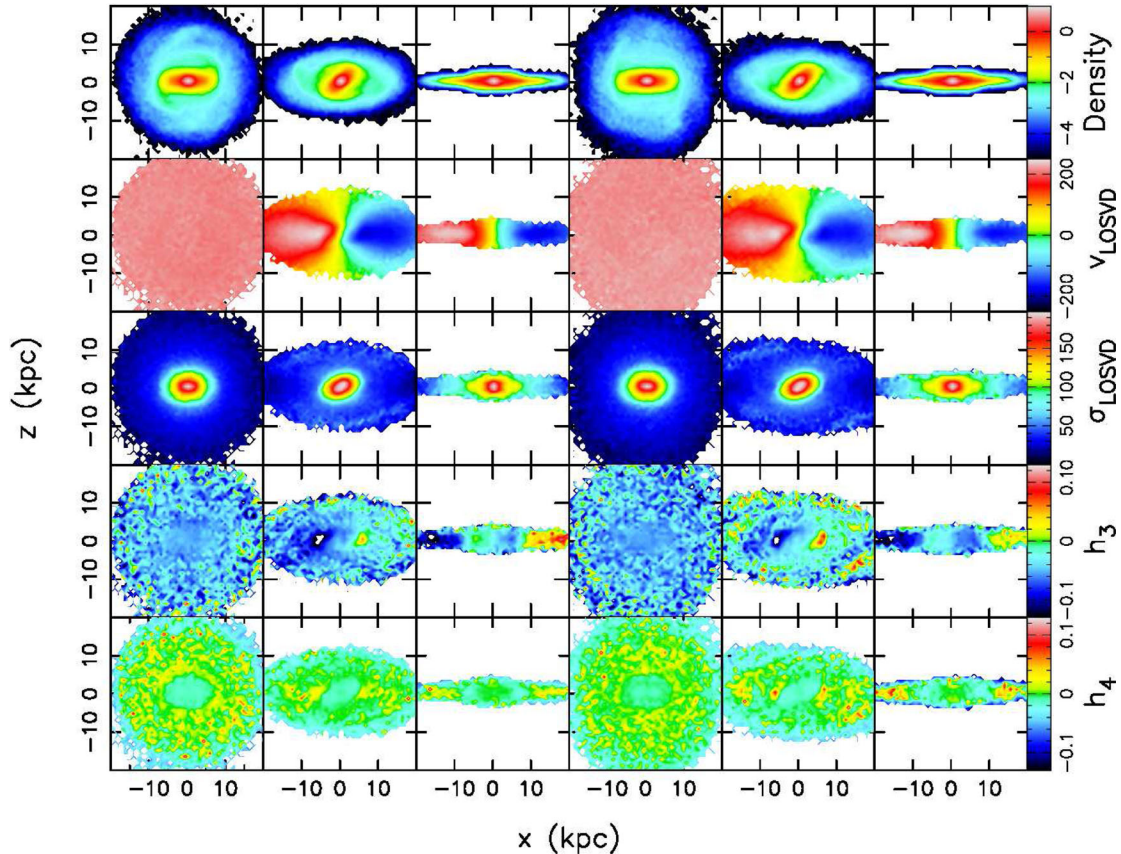


Figure 5. From top to bottom, density and kinematic moments maps. From left to right, the different simulations, SIMI1 simulation at $inc = 0^\circ$ and $PA_{\text{bar}} = 0^\circ$, $inc = 60^\circ$ and $PA_{\text{bar}} = 60^\circ$, and $inc = 90^\circ$ and $PA_{\text{bar}} = 0^\circ$ at $\tau = 4.18$ Gyr and for the same orientations for the interaction I1_i_500.

As before, in the perturbed galaxy, we identify more structure in the density map, such as spirals and rings outside the bar (Fig. 6, top row). In the velocity map for the inclined snapshot, we can see the strong twist of the kinematic axis due to the non-circular motions of the bar and the flares due to the spirals. On average, in the region within the range $R_{\text{bar}} < r < 1.5R_{\text{bar}}$, the velocity dispersion of the disc is higher by $\sim 20 \text{ km s}^{-1}$, from 3.6 km s^{-1} in isolation to 23.9 km s^{-1} with the interaction ($inc = 60^\circ$). In the edge-on view, the vertical parallel isoveLOCITIES are clearly associated with the cylindrical rotation of the bar's boxy part. In the dispersion map, as before, the influence of the interaction is clearly seen in the high values of dispersion outside the bar. In the outer parts, for $x > 10 \text{ kpc}$, the value in isolation corresponds to ~ 10 and $\sim 42 \text{ km s}^{-1}$ for the galaxy in interaction.

We would like to know if the heating comes directly from the bar itself or from the interaction. When the bar is much weaker due to the very fast interaction (I0_i_2000), we do not have such high dispersion in the disc. But at this point, we cannot distinguish whether the newly created bar or the interaction is responsible for the heating.

For the high-velocity moment h_3 , when the bar is seen edge-on, we should see correlation between h_3 and velocity. But in this particular case, I0_i_500, where the bar is created purely by interaction, we do not see it as clearly as before. The same is true for the inclined map (Fig. 6, fifth column), where high values for h_3 outside the bar are not so visible. For h_4 maps, in the face-on (Fig. 6, 4th column, bottom), the bar region shows high values, in negative, with the bar shape clearly outlined. Also, a ring shape can be seen in h_4 around the bar.

6 DISCUSSION

6.1 Results and comparison with observations

In early observational studies of interacting pairs and bars (Elmegreen, Elmegreen & Bellin 1990), the bars were clearly triggered by interactions, in particular, those of early type galaxies. This is in good agreement with some of our results, where interactions clearly trigger bars. Conversely, recent statistical analysis of observations (Casteels et al. 2013) suggests that bars are suppressed by close interactions between galaxies of similar masses.

In the detailed observational study of galaxy pairs by Couto da Silva & de Souza (2006), they found no significant change in bar ellipticity with pair separation. Their interpretation of this result was that bar ellipticity is probably governed by intrinsic factors such as velocity field, bulge/disc mass ratio, or mass distribution. This is in complete agreement with our results, since the bar ellipticity evolves depending on initial conditions, and in both simulations sets (SIMI1, SIMI0), we found an extended range of ellipticities from $\epsilon \sim 0.5$ to 0.7 .

Barazza et al. (2009) compared bars in fields and clusters, finding that bars of cluster galaxies tend to be slightly longer than those of field galaxies. Their sample had 925 galaxies at $z = 0.4$ – 0.8 . Based on our study, this result could be explained as the small effect that a fast interaction has over the galaxy's intrinsic fate. In our case, we find, in general, longer bars for those interactions with 2000 km s^{-1} (associated with clusters), where the bar growth is almost unaffected by the interaction. This effect is also similar and compatible with that one found by Li et al. (2009),

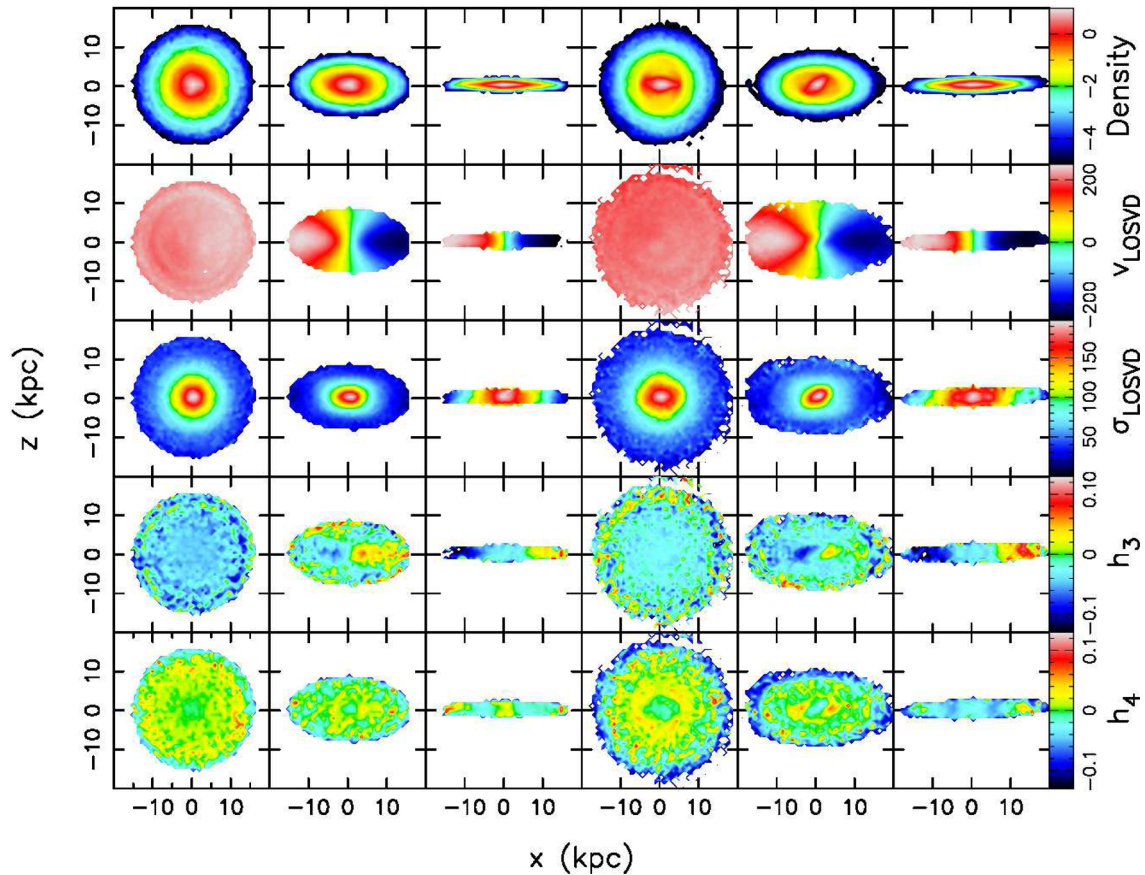


Figure 6. From top to bottom, density and kinematic moments maps. From left to right, the different simulations, SIMIO simulation at $inc = 0^\circ$ and $PA_{\text{bar}} = 0^\circ$, $inc = 60^\circ$ and $PA_{\text{bar}} = 60^\circ$, and $inc = 90^\circ$ and $PA_{\text{bar}} = 0^\circ$ at $\tau = 4.18$ Gyr and for the same orientations for the interaction I0_i_500.

where red bars (evolved) present higher ellipticity in clustered galaxies.

For at least a decade, the fate of bars has been related to intrinsic properties: to the mass ratios of the disc and dark matter halo and to the central mass concentration (Athanasoula 2003). Our study emphasises the need to recognize that a significant fraction of bars will have been triggered only by interactions, independently of the intrinsic properties of the hosting system.

6.2 Robustness of impulsive approximation

By using the IA, we are only modelling the influence of the interaction at one particular time. We have checked whether an interaction lasting for a longer time would still give the same results, by running a simulation where the perturber is a set of particles representing the companion. The ‘companion’ follows the real orbit of the impulsive approximation. The orbit described by the companion is that of simulation II_d_500. The resulting main parameters of the bar are comparable with those from the impulsive approximation. The case of the bar amplitude and pattern speed can be seen in Fig. 7. The evolution of the bar is clearly similar to that from the IA. This gives the necessary support and independence to our results obtained with the IA. We have explored the $R_{\text{CR}}/R_{\text{bar}}$ evolution for this particular case and we find that it is higher because the bar is shorter. So, if anything, the IA underestimates the extent to which the bar strength can be reduced by the interaction.

We have performed the same analysis with a simulation very stable to bar formation with a hotter disc $Q = 3$. The IA is not able

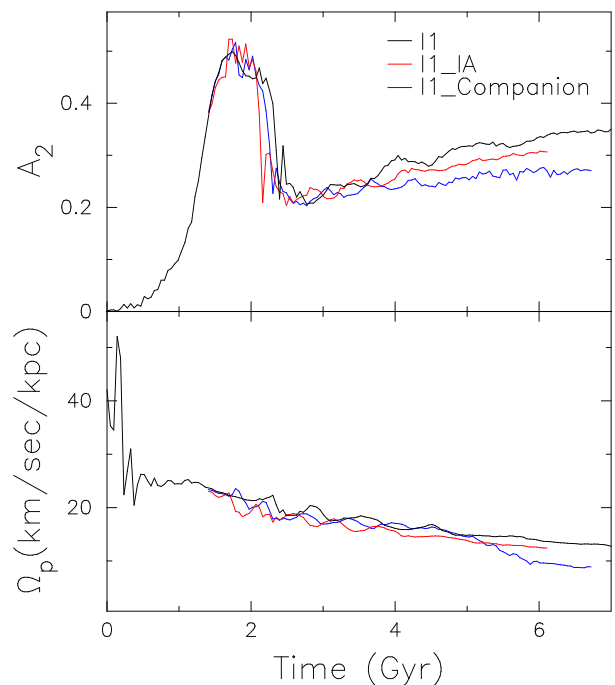


Figure 7. Time evolution of bar amplitude and pattern speed for the standard model in isolation (black line), the interacting model with IA (red line), and for the model interacting with a mock galaxy simulating a more lasting interaction (blue line).

to trigger the formation of the bar. With a long interaction performed in the same way as that described above, the galaxy is also not able to develop a bar.

6.3 Prograde versus retrograde orbits

The early study by Lang et al. (2014) shows that interactions produce stronger bars when the orbit of the encounter is prograde. In our study, we find indications of the opposite, although the difference between prograde and retrograde is quite small. For example, in case I0_d_500, the final bar is weaker than in case I0_i_500. For a clear effect, although for the case of simulations unstable to bar formation, see I1_d_1000 and I1_i_1000. In this particular case, there are several effects to be considered. First, if at the initial time, the prograde orbit makes the bar stronger, the buckling event will be stronger, and therefore the recovering and the later growth is somehow weaker. We have run the same interaction but at a different time (t_{12}), when the bar has already resumed its evolution and the boxy bulge is fully formed. In this case, the ending strength of the bar is similar for both orbits, prograde and retrograde.

The second possible explanation is the angle between the bar and the companion at the pericentre at the time of the interaction. Even after studying the simulations with the encounter at different time (t_{12}), where the bar angle is different to that at t_{11} , we cannot currently distinguish between these two possibilities.

6.4 Detecting slow bars

These simulations are scaled to be compared with galaxies with masses of few times $10^{11} M_{\odot}$. According to the COSMOS survey (Sheth et al. 2008), half of the galaxies in this mass range formed bars at $0.60 < z < 0.84$, much earlier than lower mass galaxies where just 20 per cent hosted bars at these redshifts. Most of the observational studies of pattern speeds of bars in nearby galaxies find most of the bars to be fast. This is in agreement with our study where, at some time after the interactions, bars seem to end up in the fast regime with $\mathcal{R} \leq 1.4$.

In the case of massive barred galaxies, we expect that bars created by interactions should be slow in terms of \mathcal{R} at intermediate redshift. Conversely, the first and only study of this found that bars are fast at $z \lesssim 0.5$ (Pérez et al. 2012). This study is purely based in photometry, the survey is not complete in any sense, and the selection is based on galaxies having outer rings, with the possible bias that this can induce.

A way to test our scenario (slow bars being those influenced by interactions) would be to look for pattern speeds of low-mass galaxies, since they are assumed to form their bar recently. We could then observe them within the ~ 4 Gyr slow-mode time interval that we have predicted with our fly-by simulations. At the moment, the only low-mass galaxy with a measured pattern speed is NGC 4431 (Corsini et al. 2007). The authors found that the probability of the bar being fast is twice that of being slow. Their study is based on long-slit data of just one galaxy, so we should take it with caution. We expect that this galaxy can be studied with 3D kinematic maps in more detail, in particular, by looking for signs of interactions in the kinematics.

7 CONCLUSIONS

In the last decades, bar formation has almost always been considered as having two causes: instability in isolated discs (self-generated) or triggered by interactions. In this work, we run a set of N -body

numerical simulations of coplanar 1:1 interactions and explore the differences between these two mechanisms, showing clear differences between them.

(i) For galaxies that would form a strong bar in isolation, the interaction was not able to prevent it. The interaction is also not able to strongly change the general evolution of bar parameters.

(ii) Conversely, for galaxies that would not form a bar in isolation, a slow interaction developed a strong bar in the galaxy.

(iii) Bars that were fully triggered or affected by interactions were slower than those created intrinsically by pure dynamical instabilities and stayed in the slow regime for 4 Gyr after the closest point of the encounter.

(iv) As these triggered or affected bars do ultimately speed up, to catch them in the slow phase, we should look for them either at high redshifts or in low-mass galaxies (where observations indicate that bar formation occurs later).

(v) Slow fly-bys, or stronger ones, had a greater effect on the galaxies. Therefore, we expect to find slower bars in low-mass groups where the velocity dispersion is lower.

(vi) We do not find any consistent differences between prograde or retrograde orbits.

(vii) The bar triggered purely by the slow fly-by developed a more radially extended boxy/peanut bulge than any of the isolated simulations.

(viii) The effect of fly-bys on the discs as a whole was always to kinematically heat them. This was particularly noticeable in the inclined systems.

(ix) In those bars triggered by the fly-bys, their discs show more structures such as spirals and rings. If this effect is shown in pure N -body simulations, we expect the effect in real galaxies, with gas and dust, to be even more pronounced.

In the future, we will extend our study by using more realistic simulations of full clusters and groups including gas, star formation, and feedback. We expect to confirm the results presented here and constrain better the bar and halo properties as well as the disc heating by the interactions.

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