1	Air-Water Flow Properties in Stepped Chutes with Modified Step and
2	<b>Cavity Geometries</b>
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9

## 10 Abstract

11 Skimming air-water flow properties were investigated in a stepped chute 12 configured with triangular steps, chamfered steps, and partially blocked step cavities. 13 The turbulent interactions between air and water were examined using a synchronised 14 system consisting of a dual-tip phase-detection probe and a pressure transducer mounted 15 side-by-side. In comparison to uniform triangular steps, the chamfered steps were found 16 to cause a reduction in air entrainment and an increase in mean velocity gradient next to the pseudo-bottom. Partial cavity blockages appeared to have little effect on air 17 18 entrainment, but were linked to an increased presence of large-scale structures in the 19 overflow, which likely resulted from a reduction in mutual sheltering between adjacent 20 step elements. The results indicated that modifications of step and cavity geometries 21 might have significant implications on stepped chute design.

22

### 23 Keywords

Multiphase flow; air entrainment; turbulence; stepped spillway; macro roughness; chamfer; physical modelling.

## 27 1. INTRODUCTION

28 Naturally occurring gas-liquid flows are one of the most challenging hydraulic problems 29 in consequence of the involvement of deformable interfaces and gas compressibility. 30 One classic example is the self-aerated skimming flow in a stepped chute, occurring due 31 to interactions between turbulent boundary layer and free-surface (e.g. Rao and Kobus 1971, Wood 1991, Chanson 1997). The air-water mixture downstream of the inception 32 33 point of aeration is characterised by highly complicated three-dimensional turbulent 34 processes. An example of prototype stepped chute skimming flow is illustrated in 35 Figure 1.

36 The properties and structures of aerated skimming flows were examined by many past

37 studies (e.g. Chanson 1997, Chanson and Toombes 2002a, Felder and Chanson 2014a,

38 2016). To date, most experimental observations are limited to flat steps within prismatic

39 rectangular channels. Several experiments performed for modified bottom geometries

40 have demonstrated modifications of energy dissipation and aeration performance to

41 different extents (e.g. Stephenson (1988) on varying step sizes, Gonzalez and Chanson

42 (2008) on steps with vanes, Felder and Chanson (2014b) on pooled steps, Wuthrich and

43 Chanson (2015) and Zhang and Chanson (2016a) on gabion steps). It is of interest to

44 investigate how modified bottom geometries would affect the air-water flow properties

45 in a stepped chute.

46 The goal of the present study is to investigate the effects of modified step edge and

47 cavity shapes on the two-phase flow properties in aerated skimming flows over stepped

48 chutes. Detailed air-water measurements were performed in stepped chutes configured

49 with triangular steps, chamfered steps, and partially blocked step cavities. The complex

50 two-phase interactions were characterised using a synchronised setup consisting of a

51 dual-tip phase-detection probe mounted abreast of a total pressure transducer. The

52 results revealed some effects of step edge and cavity geometries on air-entrainment and

flow structures, which underlined the complexity of stepped chute flows.



54

Figure 1 – Hinze dam (Gold Coast, Australia) spillway in operation on 31 Mar 2017 –  $q_w \approx 27 \text{ m}^2/\text{s}, d_c/h \approx 3.5, Re \approx 1.0 \times 10^8$ 

# 57 2. EXPERIMENTAL FACILITIES AND INSTRUMENTATION

## 58 2.1 INFLOW CONDITIONS

59 Present investigations were conducted in a large-size stepped spillway model at the 60 University of Queensland (UQ) with very-calm inflow conditions. A smooth and stable 61 discharge was delivered by three pumps driven by adjustable frequency AC motors. 62 Water was fed into a 1.7 m deep, 5 m wide intake basin with a surface area of 63  $2.7 \times 5 \text{ m}^2$ , leading to a 2.8 m long side-wall convergent with a contraction ratio of 64 5.08:1, which resulted in a smooth and waveless inflow. The chute inflow was controlled by an upstream broad crested weir. The weir consists of a 1.2 m high, 0.6 m 65 66 long and 0.985 m wide crest with a vertical upstream wall, an upstream rounded nose (0.058 m radius), and a downstream rounded edge (0.012 m radius). The crest was made 67 68 of smooth, painted marine ply. The discharge was deduced from integration of velocity 69 profiles measured on the crest (Zhang and Chanson 2016b).

70 2.2 Stepped spillway models

71 Detailed two-phase flow studies were conducted in a 45° stepped chute configured with

- vulturing triangular steps and with several modifications to step shape and cavity
- 73 geometries. The chute details are sketched in Figure 2 and summarised in Table 1.
- 74 Initial experiments were performed with twelve identical triangular steps  $(0.1 \times 0.1 \times 1)$

- 75 m, Fig. 2, top-left). Additional studies were undertaken for three cases of modified
- cavity geometries, where the step cavities were blocked to 33%, 50%, and 66% of the
- step height, corresponding to roughness densities  $\lambda/k = 3, 4, 6$  (Fig. 2, top-right), with  $\lambda$
- the streamwise separation between adjacent step edges and *k* the step roughness height.
- 79 Finally, the effects of step edge modification were examined by replacing step edges 2 –
- 80 12 with 20 mm chamfers (Fig. 2, bottom-right).
  - Model  $\overline{k}(\mathbf{m})$ *h* (m) l(m) $\lambda$  (m)  $\lambda/k$  $\theta$ Modification (°) Ι 0.1 0.1 2 0.14 0.071 45 Smooth triangular cavities (i.e. no modification) IIa 0.1 0.1 0.14 0.047 45 Partially filled cavities 3 IIb 0.035 4 IIc 0.024 6 III 0.1 0.1 0.14 0.061 2.33 45 Chamfered step edges
- 81 Table 1 Experimental channel details

- 82 Notes: h vertical step height; l step length;  $\lambda$  roughness wavelength; k roughness height;  $\theta$  chute
- 83 slope



85 Figure 2 – Definition sketch of experimental configurations (units: mm).

- 86 2.3 INSTRUMENTATION AND EXPERIMENTAL FLOW CONDITIONS
- 87 The present experiments were performed with water discharges ranging between Q =
- 0.083 and  $0.216 \text{ m}^3/\text{s}$ , with a focus on the skimming flow regime. The corresponding
- 89 Reynolds number range was  $3.4 8.8 \times 10^5$ . For all models, the air-water flow
- 90 properties were recorded with dual-tip phase-detection probes with an inner tip diameter
- 91 of 0.25 mm and longitudinal tip separations  $\Delta x$  between 4.3 and 8 mm. For models I
- 92 and *IIa*, additional data were obtained by simultaneously sampling a dual-tip phase-
- 93 detection probe mounted abreast of a total pressure transducer (inner diameter: 1 mm;
- 94 outer diameter: 4 mm) to further characterise the turbulent air-water interactions. The
- 95 pressure transducer was calibrated to measure relative pressures between 0 and 0.15
- 96 bars at a precision of 0.5% full scale (FS). The details of the experimental flow
- 97 conditions and sampling parameters are summarised in Table 2.
- 98 Table 2 Experimental flow conditions for detailed clear-water and air-water flow

99 measurements

Model	θ (°)	h (m)	W (m)	$\lambda/k$	Location	$\begin{array}{c} Q\\ (m^3/s) \end{array}$	$d_{c}/h$	Re	Instrumentation <sup>*1</sup>
Ι	45	0.1	1.0	2	Step edges 5 – 12	0.057 - 0.216	0.70 – 1.70	2.3 - 8.8×10 <sup>5</sup>	DPP: 20 kHz / 45 s
					Step edges 5 – 12	0.083 - 0.216	0.90 – 1.70	$3.4 - 8.8 \times 10^5$	DPP / TPT: 5 kHz / 180 s
Па	45	0.1	1.0	3	Step edges 4 – 12	0.083 - 0.216	0.90 – 1.70	3.4 – 8.8×10 <sup>5</sup>	DPP: 20 kHz / 45 s
					Step edges 3 – 12	0.083 - 0.182	0.94 – 1.75	3.6 – 9.1×10 <sup>5</sup>	DPP / TPT: 5 kHz / 180 s
IIb	45	0.1	1.0	4	Step edges 4 – 12	0.083 - 0.216	0.90 – 1.70	3.4 – 8.8×10 <sup>5</sup>	DPP: 20 kHz / 45 s
IIc	45	0.1	1.0	6	Step edges 4 – 12	0.083 - 0.216	0.90 – 1.70	3.4 – 8.8×10 <sup>5</sup>	DPP: 20 kHz / 45 s
III	45	0.1	1.0	2.33	Step edges 5 – 12	0.083 - 0.182	0.90 – 1.50	$3.4 - 7.3 \times 10^5$	DPP: 20 kHz / 45 s DPP / TPT: 5 kHz / 180 s



Notes: \*1 – DPP: Dual-tip Phase-detection probe; TPT: Total pressure transducer.

## 101 3. AIR-WATER FLOW PROPERTIES

#### 102 3.1 BASIC AIR-WATER FLOW PROPERTIES

103 Basic air-water properties at step edges were investigated for all step roughness types for skimming flow discharges ranging between  $d_c/h = 0.9 - 1.5$ , where  $d_c$  is the critical 104 105 flow depth, and h the step height. For all models, the aerated flow was divided into an 106 initial rapidly varied flow (RVF) region immediately downstream of the inception point 107 of free-surface aeration, followed by a gradually varied flow region (GVF). In the RVF 108 region, advective transport is negligible compared with turbulent diffusion, and the void 109 fraction profiles may be modelled with a theoretical solution (Zhang and Chanson 110 2017):

111 
$$C = \frac{1}{2} \operatorname{erfc}\left(\frac{Y_{50} - y}{2\sqrt{D_{a}t}}\right)$$
(1)

112 where C is the void fraction, y is the normal distance measured from the pseudo-bottom,

113  $Y_{50}$  the elevation where C = 0.5, t is the diffusion time, and  $D_a$  is an average diffusivity:

114 
$$D_{\rm a} = \frac{1}{t} \int_0^t D_{\rm t} dt \tag{2}$$

where  $D_t$  is a turbulent diffusivity. The similarity between Equation (1) and a Gaussian cumulative distribution function (CDF) with a mean of  $Y_{50}$  and standard deviation of  $\sqrt{2D_a t}$  emphasises the random nature of the initial diffusion process.

118 Further downstream, the aerated flow approaches an approximate equilibrium, where

the effects of bubble buoyancy and droplet weight become relevant. Assuming a

homogeneous air-water mixture between C = 0 and 0.9 (Wood 1985, Chanson 1993), a

121 solution is obtained by balancing the turbulent diffusion and advection terms in the

122 advection-diffusion equation (Chanson and Toombes 2002a):

123 
$$C = 1 - \tanh^2 \left[ K - \frac{y'}{2D_0} + \frac{\left(y' - \frac{1}{3}\right)^3}{3D_0} \right]$$
(3)

- 124 where  $Y_{90}$  is the elevation where C = 0.9, K is an integration constant and  $D_0$  is a
- 125 function of *C*<sub>mean</sub>:

126 
$$C_{\text{mean}} = \frac{1}{Y_{90}} \int_{0}^{Y_{90}} C dy$$
 (4)

127 
$$K = \tanh^{-1}\left(\sqrt{0.1}\right) + \frac{1}{2D_0} - \frac{8}{81D_0}$$
(5)

128 
$$D_0 = -\frac{1}{3.614} \ln\left(1.0434 - \frac{C_{\text{mean}}}{0.7622}\right)$$
(6)

129 Figure 3 presents the dimensionless step edge void fraction distributions in all setups for 130 a skimming flow  $d_c/h = 0.9$ , where x is the streamwise distance measured from the first 131 step edge,  $x_i$  is the inception point location, and  $\lambda$  is the separation between adjacent step 132 edges (= 0.141 m). The theoretical solutions (Eqs. 1 and 3) were also plotted for ease of 133 reference. A good agreement between experimental data and theoretical models was observed for all models with sharp edges (i.e. models I, IIa, IIb, IIc). In model III (Figs. 134 3e-f), the no-flux boundary condition at the chamfer surface appeared to be associated 135 136 with the build-up of some air-concentration boundary layer. The observation was 137 consistent with those in chute and tunnel spillways, and might contribute to a reduction 138 in skin friction (Chanson 2004). The results suggested that the air concentration profiles 139 were more influenced by step edge profiles than by cavity shapes.



(a) model I

(b) model IIa

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(e) model *III*, upstream edge



- 140 Figure 3 Step edge void fraction distributions in chutes with various step roughness
- 141 types. Flow conditions:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ,  $\theta = 45^\circ$ .
- 142 The bubble count rate *F* is defined as half the number of air-water interfaces detected by
- 143 the probe sensor per second. For a given interfacial velocity, it is directly proportional
- 144 to the specific interfacial area (Chanson 2001b). Figure 4 presents typical skimming
- 145 flow bubble count rate distributions in all setups for a dimensionless discharge  $d_c/h =$
- 146 0.9. All data exhibited a characteristic bell shape with a marked maximum at  $y/Y_{50} \approx 1$
- 147 ( $C \approx 0.5$ ), consistent with previous studies (e.g. Chanson and Toombes 2002a, Toombes
- 148 and Chanson 2008). Furthermore, a continuous increase in maximum bubble count rate
- 149 with increasing distance downstream of the inception was observed in all setups,

- 150 implying that uniform equilibrium conditions were not achieved. Overall, the step edge
- and cavity modifications appear to have no significant influence on the bubble count
- 152 rate profiles.



(c) model *IIb* 

(d) model *IIc* 



(e) model *III*, upstream edge
(f) model *III*, downstream edge
153 Figure 4 – Step edge bubble count rate distributions in chutes with various step

154 roughness types. Flow conditions:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ,  $\theta = 45^\circ$ .

155 The interfacial velocity may be derived from the cross-correlation function between two

156 probe signals (Crowe et al. 1998, Chanson 2002, Chanson and Carosi 2007):

157 
$$U_{\rm aw} = \frac{\Delta x}{T_{\rm aw}}$$
(7)

158 where  $U_{aw}$  is the interfacial velocity,  $\Delta x$  is the streamwise tip separation and  $T_{aw}$  is the 159 time lag at which the cross-correlation function peaks. Figure 5 shows the step edge 160 interfacial velocity profiles for all models, where  $U_{50}$  is the interfacial velocity 161 corresponding to C = 0.5. All data followed a two-tier distribution:

162 
$$\frac{U_{\text{aw}}}{U_{50}} = \left(\frac{y}{Y_{50}}\right)^{\frac{1}{N_{50}}} \qquad \text{for } 0 \le y/Y_{50} < 1 \ (8)$$

163 and

164 
$$\frac{U_{aw}}{U_{50}} = 1$$
 for  $y/Y_{50} \ge 1$  (9)

165 Equations (8) and (9) imply a physical demarcation in terms of the flow composition at 166 about  $y/Y_{50} = 1$ . A constant interfacial velocity profile for  $y/Y_{50} > 1$  implied lesser shear 167 stress in this region, despite the visually complex nature of the mixture. It also appeared

- 168 that the dynamics of air had little observable effect on the mean momentum of the water
- 169 droplets in the spray zone (C > 0.9). Table 3 summarises the best fit of power law
- 170 exponent N<sub>50</sub>, and corresponding correlation coefficients R. For all present data, N<sub>50</sub>
- 171 ranged between 3.1 7.6. Compared to the non-modified chute (*I*), those with modified
- 172 step cavities (IIa,b,c) recorded smaller  $N_{50}$  values, possibly linked to a downward shift
- 173 in the mean velocity profile. In the chamfered chute (III), the N<sub>50</sub> values were larger at
- the upstream edge than at the downstream chamfer edge, which could be linked to some
- 175 flow separation at the upstream edge. Furthermore, the cavity and step edge
- 176 modifications appeared to have respectively resulted in a decrease and an increase in the
- 177 correlation coefficient *R*. The observation was likely reflective of geometry-induced
- 178 changes in vortex shedding behaviours, which in turn lead to some streamwise
- 179 variations in the overflow.
- 180 Table 3 Interfacial velocity power law exponents in all present configurations
- 181 (average over all data)

Model	$N_{50}$	R	Remark
Ι	5.0	0.75	$\lambda/k = 2$ , triangular steps
Па	4.2	0.61	$\lambda/k = 3$ , partially blocked cavities
IIb	3.1	0.31	$\lambda/k = 4$ , partially blocked cavities
IIc	5.0	0.70	$\lambda/k = 6$ , partially blocked cavities
III (upstream edge)	7.6	0.89	$\lambda/k = 2.33$ , chamfered steps
III (downstream edge)	5.1	0.95	$\lambda/k = 2.33$ , chamfered steps



(a) model I

(b) model *IIa* 

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(e) model *III*, upstream edge(f) model *III*, downstream edgeFigure 5 – Interfacial velocity distributions at step edges in chutes with various step

Figure 5 – Interfacial velocity distributions at step edges in chutes with various step roughness types. Flow conditions:  $d_c/h = 0.9 - 1.7$ ,  $Re = 3.4 - 8.8 \times 10^5$ ,  $\theta = 45^\circ$ .

184 3.2 INTERFACIAL TURBULENCE CHARACTERISTICS

The fluctuations of interfacial velocity may be quantified by comparing the relative
widths between auto- and cross-correlation functions of the two tip signals (Chanson
and Toombes 2002a):

188 
$$Tu_{aw} = 0.85 \frac{\sqrt{\tau_{0.5}^2 - T_{0.5}^2}}{T_{aw}} = \frac{\sqrt{u_{aw}^{'2}}}{U_{aw}}$$
(10)

189 where  $Tu_{aw}$  is the interfacial turbulence intensity,  $\tau_{0.5}$  is the time lag where the

190 normalised cross-correlation function between two probe sensors equals 0.5,  $T_{0.5}$  is the

- 191 time lag for which the normalised auto-correlation function equals 0.5,  $T_{aw}$  is the time
- 192 lag corresponding to the peak of the cross-correlation function between two tips, and
- 193  $u'_{aw}$  is the interfacial velocity fluctuation. For a given probe tip separation, a large
- 194 relative width between auto- and cross-correlation functions must correspond to large
- 195 fluctuations of the air-water interfaces (Chanson and Carosi 2007). Implicitly, *Tu*<sub>aw</sub>

196 takes into account all forms of interfacial fluctuations whether they are turbulence-

- 197 induced rigid-body transformations (which preserve angles and line lengths) or
- 198 deformation of the interfaces (warping).

199 Figure 6 shows typical interfacial turbulence intensity distributions at step edges for a 200 skimming flow  $d_c/h = 0.9$ . For all models, the inception point data showed some large 201 scatter that reflected the unsteady nature of the region. Further downstream, the data 202 generally followed a characteristic shape, with local maxima next to the pseudo-bottom 203 and at about  $y/Y_{50} = 1$ . The observations were consistent with past studies in skimming 204 flows (e.g. Chanson and Carosi 2007, Felder and Chanson 2009). The two peaks in  $Tu_{aw}$ 205 were respectively associated with large turbulence levels in the step-induced wakes, and 206 a continuous breakdown of freshly entrained air coupled with a phase change process. 207 For  $y/Y_{50} > 1$  the data decreased monotonically with increasing elevation. At sufficiently 208 high elevations the flow was mainly composed of discrete droplets, and the strain field 209 of the surrounding air had little effect on the water because of the large density 210 difference. The non-trivial  $Tu_{aw}$  values (> 0.5) in this region most likely resulted from 211 inhomogeneous droplet shapes instead of turbulence. A comparison between the 212 different models revealed the largest  $Tu_{aw}$  for the modified cavities, followed by those 213 for the chamfered steps and for the unmodified chute. The observation suggested that 214 interfacial turbulence might be sensitive to additional length scales introduced by 215 modifications of step and cavity shapes.

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(e) model *III*, upstream edge (f) model *III*, downstream edge Figure 6 – Interfacial turbulence intensity distributions at step edges in chutes with various step roughness types. Flow conditions:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ,  $\theta = 45^\circ$ .

- 219 Following Chanson and Carosi (2007), an integral air-water time scale may be
- 220 determined from the autocorrelation function of an air-water voltage signal:

221 
$$T_{xx,c} = \int_{0}^{\tau_{R_{xx,c}=0}} R_{xx,c}(\tau) d\tau$$
(11)

222 where  $R_{xx,c}$  is the normalised autocorrelation coefficient of the void fraction signal and  $\tau$ 223 is the time lag.  $T_{xx,c}$  is a time scale that characterises the longest streamwise air-water 224 connections (i.e. air-water 'memory' time). Figure 7 presents the  $T_{xx,c}$  distributions at 225 step edges for a skimming flow discharge  $d_c/h = 0.9$ . All data followed a bell shape with a maximum at  $y/Y_{50} \approx 1$ . In addition, a local maximum was sometimes observed next to 226 227 the pseudo-bottom, which could be linked to vortices shed from the step edge. Some 228 large data scatter was seen for the first 2-3 step edges downstream of the inception 229 point because of boundary layer fluctuations. Further downstream, the data tended to 230 become approximately self-similar, as previously observed (Carosi and Chanson 2006, 231 Felder 2013). The finding suggested that the air-diffusion layer could attain some local 232 equilibrium at sufficient distance downstream of the inception point. The step edge and 233 cavity modifications appeared to bear no significant effect on the air-water time scale 234 distributions.



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(e) model *III*, upstream edge (f) model *III*, downstream edge Figure 7 – Integral air-water time scale distributions at step edges in chutes with various step roughness types. Flow conditions:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ,  $\theta = 45^\circ$ .

# 238 4. TWO-PHASE INTERACTIONS

239 4.1 TOTAL PRESSURE FLUCTUATIONS

240 The total pressure fluctuations in the aerated flow region were examined for all models

- 241 with a total pressure transducer. The sensor responded to both turbulence-induced and
- 242 density-induced fluctuations, as shown in Figure 8. Next to the pseudo-bottom, the PDF
- 243 of the fluctuating total pressure  $p'_{t}$  was typically unimodal with a positive skew, likely
- associated with intermittent fluid ejections from the step cavity. With increasing
- 245 distance from the pseudo-bottom the PDF curves became distinctively bimodal because
- of density fluctuations, while some bias due to wetting and drying were also likely.

- 247 Importantly, Figure 8 implies that any second or higher order statistics of total pressure
- 248 fluctuations would be determined by the combined effects of density and isolated-phase
- 249 (air or water) fluctuations.





Figure 8 – Typical PDFs of total pressure fluctuations in the air-water flow region in skimming flows – Flow conditions:  $d_c/h = 0.9$ ,  $\theta = 45^\circ$ , model *I*, step edge 12.

253 An intensity of total pressure fluctuation may be defined as:

$$254 \qquad \frac{\sqrt{p_t^{\prime 2}}}{P_t} \tag{12}$$

where  $p_{t}$  and  $P_{t}$  are respectively the fluctuating and mean total pressure measured by the 255 256 total pressure sensor. Figure 9 presents typical distributions of total pressure fluctuation intensity at step edges for a skimming flow  $d_c/h = 0.9$ . For all models, the total pressure 257 258 fluctuation intensity exhibited a minimum at about  $y/Y_{50} = 0.6$ , where the void fraction C 259 was about 0.2 - 0.3. The total pressure fluctuations intensified next to the pseudo-bottom 260 and towards the free-surface, respectively on account of a high turbulence level and 261 density fluctuations coupled with a diminishing mean total pressure  $P_{\rm t}$ . Note that the 262 influence due to capillary effects might grow near the free-surface. Overall, the data highlighted the turbulent nature of the skimming stepped chute flow. No significant 263 264 difference was observed between the unmodified model and those with altered step and 265 cavity geometries.

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(c) model *III*, upstream edge(d) model *III*, downstream edge266Figure 9 – Total pressure fluctuation intensity distributions at step edges. Flow

267 conditions: model *I/III*:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ; model *IIa*:  $d_c/h = 0.94$ ,  $Re = 3.6 \times 10^5$ ;  $\theta = 45^\circ$ .

269 4.2 WATER-PHASE TURBULENCE

The stepped spillway flow is characterised by extremely complex interactions between the air and water phases. The lowest order descriptor of the water phase turbulence is the turbulence intensity, defined as:

273 
$$Tu_{\rm p} = \frac{\sqrt{u_{\rm w}^2}}{U_{\rm w}} \tag{13}$$

- where  $u'_{w}$  and  $U_{w}$  are the fluctuating and mean water velocities. The turbulence intensity
- 275 *Tu*<sub>p</sub> may be estimated from simultaneously sampled total pressure and phase-detection
- 276 probe signals (Zhang and Chanson 2016b):

277 
$$Tu_{p} = \sqrt{\frac{\frac{\overline{p_{t}^{'2}}}{\rho_{w}^{2}U_{w}^{4}} - \frac{1}{4}C(1-C)}{\left(1 + \frac{1}{2}C\right)(1-C)}}$$
(14)

where the total pressure fluctuation  $p'_{t}$  and the void fraction C are measured by the 278 279 pressure transducer and phase-detection probe, respectively. Note that the validity of 280 Equation (14) decreases for  $Tu_p$  greater than 0.4 - 0.5.  $Tu_p$  characterises the streamwise 281 velocity fluctuations of water particles and may be biased by: (a) instantaneous pressure 282 rise due to surface tension during interfacial processes; (b) wetting and drying time of 283 the sensor diaphragm; (c) bursting bubbles. Lastly, in high void fraction regions the 284 water-phase is no longer continuous, and Equation (14) essentially reflects the velocity 285 variations over a streamwise ensemble of water droplets.

286 Typical water phase turbulence intensity distributions at step edges are presented in 287 Figure 10 for a skimming flow  $d_c/h = 0.9$ . The data were shown up to  $y = Y_{50}$  because of 288 different flow structures in the upper region. Herein the mean water velocity  $U_{\rm w}$  was 289 calculated from the mean total pressure Pt assuming a hydrostatic pressure distribution 290 between  $0 \le y \le Y_{90}$ . All data typically ranged between 0.1 - 0.5, approximately an 291 order of magnitude smaller than the largest interfacial turbulence intensity  $Tu_{aw}$ . Hence 292 bubbles should not be used as accurate tracers of water-phase turbulence. Albeit some 293 scatter, the  $Tu_p$  levels was about 30% at the pseudo-bottom, and decreased to 10% -294 20% at  $v/Y_{50} = 0.7 - 0.8$ . These values were comparable to those obtained in the clear-295 water flow region in a stepped chute (Ohtsu and Yasuda 1997, Amador et al. 2006), and 296 in flows over transverse rib-roughness (Okamoto et al. 1993, Cui et al. 2003). At higher 297 elevations, the water-phase turbulence intensities were noticeably larger next to the 298 inception point than further downstream, highlighting the turbulent nature of the RVF 299 region. For the chamfered steps, slightly larger  $Tu_p$  values were identified at the 300 upstream edge than at the downstream edge. Overall, no significant cavity and step edge 301 effects were observed on the distributions of water-phase turbulence.

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(c) model *III*, upstream edge (d

(d) model III, downstream edge

Figure 10 – Water-phase turbulence intensity distributions at step edges in chutes with various step roughness types. Flow conditions: model *I/II*:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ;

304 model *IIb*:  $d_c/h = 0.94$ ,  $Re = 3.6 \times 10^5$ ;  $\theta = 45^\circ$ .

305 4.3 TOTAL PRESSURE TIME SCALES

The longest connections of total pressure fluctuations in the flow may be characterisedby the total pressure autocorrelation time scale:

308 
$$T_{xx,p} = \int_{0}^{\tau_{R_{xx,p=0}}} R_{xx,p}(\tau) d\tau$$
(15)

309 where  $R_{xx,p}$  is the normalised autocorrelation coefficient of the total pressure signal and  $\tau$ 

310 is the time lag.  $T_{xx,p}$  is a measure of the average longitudinal size of the energy-

311 containing eddies subject to effects of coherent density fluctuations.

- 312 Figure 11 shows typical distributions of dimensionless total pressure time scales at step
- 313 edges for the various configurations. All configurations, except for model *IIa*, exhibited
- the largest total pressure time scales close to the pseudo-bottom, reaching a
- dimensionless value of approximately 0.2. The more scattered  $T_{xx,p}$  data in model *IIa*
- 316 appeared to be associated with increased flow instabilities caused by the cavity
- 317 blockage. Significant time scales were sometimes observed next to the inception point,
- 318 highlighting the large-scale instabilities in that region. For model III, subtly larger  $T_{xx,p}$
- 319 values were identified at the upstream edge than at the downstream edge. The
- 320 observation could be linked to a reduction in turbulent production along the chamfer

321 edge because of smaller velocity gradients. At sufficient distance downstream of the

- inception point (i.e.  $(x-x_i)/\lambda > 2$ ), the data in both models *I* and *III* exhibited some self-
- 323 similarity. Hence the energy-containing structures might have reached a state of pseudo-
- 324 dynamic equilibrium, despite that uniform equilibrium flow conditions were not
- 325 achieved. Importantly, the findings demonstrated some large impact of cavity blockage

on the spatial homogeneity of the flow.

- 327 The dimensionless  $T_{xx,p}$  profile displayed a marked change at about  $y/Y_{50} = 0.8 1$ . This
- 328 implied a physical demarcation in flow properties about this region, potentially
- 329 underpinned by structural changes in the two-phase turbulence patterns. In the lower
- region (i.e.  $y/Y_{50} < 0.8 1$ ), the  $T_{xx,p}$  values were dominantly of the order 0.1, which was
- 331 comparable to a roughness timescale  $T_k$  defined as:

332 
$$T_{\rm k} = \frac{k}{U_{\rm sl}}$$
 for  $0 \le y/Y_{50} < 0.8 - 1$  (16)

where *k* is the roughness height projection normal to the pseudo-bottom, and  $U_{sl}$  is the convection velocity in the shear layer. Since  $T_{xx,p} \sim k_T/\varepsilon$  (*k*<sub>T</sub>: turbulent kinetic energy;  $\varepsilon$ : dissipation) (Pope 2000), the observation highlighted the importance of the lower

aerated flow region for turbulent production, and the absence of roughness

337 characteristics for  $y/Y_{50} > 0.8 - 1$ .

338 Figure 12 examines the relationship between the dimensionless total pressure time scale

- 339  $T_{xx,p}$  and integral air-water time scale  $T_{xx,c}$  in stepped chutes I and IIa. The data revealed
- a strong correlation between the two variables for  $y/Y_{50} \ge 1$  (R = 0.79), and almost no
- 341 correlation for  $y/Y_{50} < 1$  (R = 0.13), where R is the normalised correlation coefficient. If
- 342 the total pressure signal is simply expressed as a sum of air and water components:

343 
$$f(t) = f_a(t) + f_w(t)$$
 (17)

344 and assuming that the air and water components are independent, it follows that:

345 
$$R_{xx,p}(\tau) = R_{xx,a}(\tau) + R_{xx,w}(\tau)$$
(18)

346 
$$T_{xx,p} = T_{xx,c} + T_{xx,w}$$
 (19)

347 where  $R_{xx,w}$  and  $T_{xx,w}$  are the water-phase contributions to the autocorrelation function 348 and integral time scale of the total pressure signal. For  $y/Y_{50} \ge 1$ , the high correlation 349 between  $T_{xx,p}$  and  $T_{xx,c}$  implies that  $T_{xx,w} \approx 0$ . Hence the water-phase contribution to the 350 total pressure signal in this region was approximately a white noise with a flat power 351 spectrum (i.e. the autocorrelation function of the water phase signal is a delta function). 352 The finding confirmed a lack of water-phase structure in the upper flow region. Note 353 that the data might be skewed in very low void fraction regions due to unreliability of 354 the phase-detection probe.



Zhang, G., and Chanson, H. (2018). "Air-water flow properties in stepped chutes with modified step and cavity geometries." *International Journal of Multiphase Flow*, Vol. 99, pp. 423-436 (DOI: 10.1016/j.ijmultiphaseflow.2017.11.009) (ISSN 0301-9322).



355 Figure 11 – Total pressure time scale distributions at step edges in chutes with various

356 step roughness types. Flow conditions: model *I/II*:  $d_c/h = 0.9$ ,  $Re = 3.4 \times 10^5$ ; model *IIb*:

357  $d_{\rm c}/h = 0.94, Re = 3.6 \times 10^5; \theta = 45^{\circ}.$ 



(a) model I



Figure 12 – Relationship between  $T_{xx,p}$  and  $T_{xx,c}$  at step edges in models *I* and *IIa*. Flow conditions: Model *I*:  $d_c/h = 0.9 - 1.7$ ,  $Re = 3.4 - 8.8 \times 10^5$ ; Model *IIa*:  $d_c/h = 0.94 -$ 

360 1.75,  $Re = 3.6 - 9.1 \times 10^5$ ;  $\theta = 45^\circ$ .

## 361 **5.** CONCLUSION

362 Skimming air-water flow properties were carefully examined in a stepped chute

363 configured with triangular steps, chamfered steps, and partially blocked step cavities.

364 Interactions between the air and water phases were investigated with a dual-tip phase-

detection probe mounted side-by-side with a total pressure transducer. The effects on
skimming flow air-water properties induced by step and cavity geometry modifications
were characterised.

368 Void fraction distributions in all models showed a reasonable agreement with analytical 369 solutions of the advection-diffusion equation. The no-flux boundary condition imposed 370 on the chamfer surface stipulated an air boundary layer growth, which could lead to a 371 reduction in skin friction. All bubble count rate data followed a characteristic shape with 372 a maximum occurring next to  $C \approx 0.5$ . The interfacial velocity data followed a two-tier 373 distribution with a demarcation at  $\nu/Y_{50} \approx 1$ . In comparison to the un-modified step 374 geometry, steeper and flatter step edge velocity profiles were respectively observed for 375 the chamfered steps and partially blocked cavities. Correlation analyses identified 376 significant interfacial fluctuations and large air-water structures at  $y/Y_{50} \approx 1$  as well as 377 next to the pseudo-bottom, which might be sensitive to step and cavity geometry 378 modifications. The data indicated that uniform equilibrium conditions were not 379 achieved in the present studies.

380 Simultaneously acquired void fraction and total pressure signals permitted individual 381 examinations of the component phases. Significant total pressure fluctuations were 382 identified throughout the flow column, resulting from water-phase turbulent fluctuations 383 coupled with rapid phase changes. The water-phase turbulence levels were comparable 384 to those reported for the clear water flow region, and were substantially less than the 385 interfacial turbulence levels. The total pressure time scale distributions implied a 386 physical demarcation about  $v/Y_{50} = 0.8 - 1$ , where the upper region was characterised by 387 a lack of coherent water-phase structures. The partial cavity blockage also appeared to 388 result in increased instabilities in the aerated flow region.

The present investigation indicated some implications for stepped chute design due to step edge and cavity modifications. The chamfers led to some reduction in air entrainment, slightly raised interfacial turbulence levels, and a steeper mean velocity profile next to the pseudo-bottom. The partial cavity blockages were observed to cause flow instabilities and an increased presence of large-scale structures in the overflow, likely resulting from modifications to the vortex shedding dynamics. Importantly, the

395 results highlighted the turbulent nature and extremely complex air-water interactions in396 aerated skimming flows over stepped roughness.

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## 498 APPENDIX A. LIST OF SYMBOLS

- 499 C time-averaged void fraction (-);
- 500  $C_{\text{mean}}$  depth-averaged void fraction (-);
- 501  $D_a$  average diffusivity (m<sup>2</sup>/s);
- 502  $D_t$  turbulent diffusivity (m<sup>2</sup>/s);
- 503  $D_0$  dimensionless diffusivity (-);
- 504  $d_c$  critical depth (m);
- 505 F bubble count rate (Hz);

- 506 g gravity constant  $(m/s^2)$ ;
- h vertical step height (m);
- K integration constant (-);
- k step roughness height (m);
- $k_{\rm T}$  turbulent kinetic energy (m<sup>2</sup>/s<sup>2</sup>);
- *l* horizondal step length (m);
- 512 N<sub>50</sub> power law exponent (-);
- $P_t$  time-averaged total pressure (Pa);
- $p_{t}$  fluctuating total pressure (Pa);
- Q water discharge (m<sup>3</sup>/s)
- $q_w$  unit discharge of water (m<sup>2</sup>/s);
- *R* normalised correlation coefficient (-);
- $R_{xx,a}$  air-phase contribution to  $R_{xx,p}$  (-);
- $R_{xx,c}$  normalised autocorrelation coefficient of a void fraction signal (-);
- $R_{xx,p}$  normalised autocorrelation coefficient of a total pressure signal (-);
- $R_{xx,w}$  water-phase contribution to  $R_{xx,p}$  (-);
- *Re* Reynolds number (-);
- $T_{aw}$  average interfacial travel time between two probe tips (s);
- $T_k$  roughness time scale (s);
- $T_{xx,a}$  air-phase contribution to  $T_{xx,p}$  (s);
- $T_{xx,c}$  streamwise autocorrelation timescale based on a void fraction signal (s);
- $T_{xx,p}$  streamwise autocorrelation timescale based on a total pressure signal (s);
- $T_{xx,w}$  water-phase contribution to  $T_{xx,p}$  (s);

- $T_{0.5}$  time lag for which normalised autocorrelation of the leading tip equals 0.5 (s);
- $Tu_{aw}$  interfacial turbulence intensity (-);
- $Tu_p$  water-phase turbulence intensity estimated from synchronised total pressure and 532 void fraction signals (-);
- t time (s);
- $U_{aw}$  time-averaged interfacial velocity (m/s);
- $U_{\rm sl}$  convection velocity in shear layer (m/s);
- $U_{\rm w}$  time-averaged water velocity (m/s);
- $U_{50}$  time-averaged interfacial velocity corresponding to C = 0.5 (m/s);
- $u_{aw}$ , fluctuating interfacial velocity (m/s);
- x streamwise coordinate (m);
- $Y_{50}$  elevation normal to the pseudo-bottom where C = 0.5 (m);
- $Y_{90}$  elevation normal to the pseudo-bottom where C = 0.9 (m);
- y normal coordinate (m);
- *Greek symbols*
- $\Delta x$  streamwise separation between probe tips (m);
- $\varepsilon$  disspation rate (m<sup>2</sup>/s<sup>3</sup>);
- $\theta$  chute slope (°);
- $\lambda$  streamwise separation between adjacent steps (m);
- $\tau$  time lag between two signals (s);
- $\tau_{0.5}$  time lag for which the normalised cross-correlation between two probe tips 551 equals 0.5 (s);

- 553 Functions
- 554 erfc complementary error function;
- 555
- 556 Acronyms
- 557 CDF cumulative distribution function;
- 558 DPP dual-tip phase-detection probe;
- 559 FS full scale;
- 560 GVF gradually varied flow;
- 561 PDF probability density function;
- 562 RVF rapidly varied flow;
- 563 TPT total pressure transducer.