

INTERSTELLAR SOLID HYDROGEN

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ABSTRACT

We consider the possibility that solid molecular hydrogen is present in interstellar space. If so cosmic-rays and energetic photons cause ionization in the solid leading to the formation of H_6^+ . This ion is not produced by gas-phase reactions and its radiative transitions therefore provide a signature of solid H_2 in the astrophysical context. The vibrational transitions of H_6^+ are yet to be observed in the laboratory, but we have characterized them in a quantum-theoretical treatment of the molecule; our calculations include anharmonic corrections, which are large. Here we report on those calculations and compare our results with astronomical data. In addition to the H_6^+ isotopomer, we focus on the deuterated species $(\text{HD})_3^+$ which is expected to dominate at low ionization rates as a result of isotopic condensation reactions. We can reliably predict the frequencies of the fundamental bands for five modes of vibration. For $(\text{HD})_3^+$ all of these are found to lie close to some of the strongest of the pervasive mid-infrared astronomical emission bands, making it difficult to exclude hydrogen precipitates on observational grounds. By the same token these results suggest that $(\text{HD})_3^+$ could be the carrier of the observed bands. We consider this possibility within the broader picture of interstellar medium photo-processes and we conclude that solid hydrogen may indeed be abundant in astrophysical environments.

Key words: dust, extinction – ISM: lines and bands – line: identification – molecular processes

Online-only material: color figures

1. INTRODUCTION

Astronomers observe matter in a great variety of physical conditions and, correspondingly, hydrogen exists in a variety of states in different astronomical contexts. Liquid metallic hydrogen is inferred to be present in a degenerate core in the planets Jupiter and Saturn (Hubbard et al. 2002), and in the interstellar context there are known to be three phases of hydrogen in rough pressure equilibrium: hot, ionized, low-density plasma; atomic gas; and molecular hydrogen in cold, dense, interstellar clouds. Might there also be solid molecular hydrogen?

That question was first addressed in the late 1960s when it was suggested that thick mantles of solid H_2 might be deposited onto the surfaces of graphite grains—see, for example, Wickramasinghe & Reddish (1968), Hoyle et al. (1968), and Wickramasinghe & Krishna Swamy (1969). But these early papers employed a poor description of the H_2 -saturated vapor pressure and in fact solid H_2 mantle formation is not expected under the conditions known to exist in the diffuse interstellar medium (ISM; Greenberg & de Jong 1969; Field 1969). The difficulty is simply that the pressure in the diffuse ISM is much smaller than the saturated vapor pressure of H_2 , even for temperatures as low as that of the microwave background.

The argument just given may, however, be misleading because the phase equilibrium of H_2 in astrophysical environments may differ significantly from that of pure H_2 . In particular the electrostatic binding energy contributed by ions in the lattice may substantially increase the total binding energy of the solid, even at very low ion concentrations. Astrophysical H_2 ice may thus be more robust than is commonly supposed.

It also remains a possibility that there exists gas which is so cold and dense that pure hydrogen precipitates can form. But that gas cannot be part of the diffuse ISM and must, instead, form distinct, self-gravitating entities. Clouds of this

type—cold, dense, mostly transparent, and having very little thermal emission—were postulated by Pfenninger and Combes (1994) and Pfenninger et al. (1994) to be a significant component of the Galaxy’s dark matter. That picture was subsequently considered by many other authors (e.g., Gerhard and Silk 1996; Walker & Wardle 1998; Draine 1998; Sciamia 2000; Walker 2007). It was argued by Wardle & Walker (1999) that small amounts of solid H_2 can confer thermal stability on these clouds.

Irrespective of these theoretical deliberations, observation provides the final arbiter of whether solid H_2 is present in the Galaxy. To that end we must first ask how solid H_2 might be detected if it were present? That is the question addressed in this paper. It is not a trivial matter because solid H_2 , like the gas from which it forms, is cold, dense, and very nearly transparent in the optical. We make no attempt at a comprehensive assessment of the detection problem; instead we focus on the properties of a particular molecule, H_6^+ , which is known to form in solid H_2 exposed to ionizing radiation (see Section 2). Cosmic-rays and energetic photons pervade interstellar space and we therefore expect H_6^+ to be present at some level in solid, interstellar H_2 . Furthermore, this molecular ion does not form in any significant quantities in the gas-phase chemistry of H_2 , so it is a good tracer of solid H_2 .

Currently H_6^+ is not well characterized experimentally so in order to predict its astrophysical manifestations we are first obliged to confront problems in quantum chemistry. To tackle these we have utilized the Q-Chem³ software package (Shao et al. 2006), with some bespoke extensions, for our calculations. For the most part we have concentrated on the bare H_6^+ molecule, whereas in solid H_2 it is expected that the ion forms many weak bonds with surrounding H_2 molecules, leading to a much larger complex. Our focus on bare H_6^+ is motivated by the fact that solvation does not greatly disturb the structure of the H_6^+ —see

³ <http://q-chem.com>

Kurosaki & Takayanagi (1998b)—and thus the high-frequency vibrational transitions of the solvated forms should closely resemble those of the bare molecule. Moreover, we do not yet know exactly what form the solvation takes. We do, however, give some consideration to how the properties of the solvated forms differ from those of the bare molecule, and where possible we estimate the size of these effects. This has been done by reference to the properties of $H_{14}^+ = H_6^+(H_2)_4$ —a cluster which is much smaller than those which are likely to occur in practice.

We have neglected any other interactions between H_6^+ and the host lattice. This is a reasonable assumption for an initial exploration as the intermolecular forces in solid hydrogen are very feeble. Indeed solid *para*- H_2 is commonly used for matrix isolation spectroscopy of small molecules (see, e.g., Oka 1993; Anderson et al. 2002), and this is precisely because it permits nearly free vibration and rotation of the impurity species. In the astronomical context there is plenty of time for *ortho*–*para* conversion to take place, so any cold H_2 is expected to be predominantly in the rotational ground state and is thus in the “*para*” form.

This paper is structured as follows. In the next section we discuss relevant laboratory results on irradiated solid hydrogens and their interpretation. In Section 3 we present our theoretical model of the H_6^+ molecule and its isotopic variant $(HD)_3^+$. The latter is expected to be the most abundant isotopomer at low ionization rates whereas the former dominates at high ionization rates. Section 4 compares the computed vibrational transitions of H_6^+ and $(HD)_3^+$ with mid-IR astronomical observations. The properties of 10 other isotopomers, which may be of interest in laboratory studies, are tabulated in the Appendix. Similarities between computed and observed spectra prompt us to suggest that $(HD)_3^+$ may actually be responsible for the observed mid-IR astronomical emission bands; the implications of this suggestion are discussed in Section 5 and we offer our conclusions in Section 6.

2. LABORATORY STUDIES OF H_6^+ IN IRRADIATED, SOLID H_2

At temperatures less than the triple-point (13.8 K), hydrogen is able to form a low-density solid ($\rho \simeq 0.086 \text{ g cm}^{-3}$). It is a “quantum solid,” meaning that the zero-point motion of the molecules is a large fraction of the intermolecular separation. Solid hydrogens have been extensively studied in the laboratory; see Silvera (1980) and Souers (1986) for reviews of their properties; Van Kranendonk (1983) provides theoretical models for some of these properties.

Although the natural abundance of tritium is negligible, its importance in fusion research led to studies of solid hydrogens in which tritium is incorporated. These solids naturally exhibit the effects of irradiation because tritium undergoes beta decay to ^3He with a half-life of approximately 12 years. The energetic electrons which result from beta decay cause ionization and dissociation of the H_2 . Various radiation-induced phenomena have received attention in the literature, as described below.

2.1. Radiation-induced Absorption Lines

In the first studies of irradiated solid hydrogens it was discovered that some extra lines were present in the absorption spectrum near the fundamental vibrational band of the solid (Souers et al. 1980, 1981). These lines were attributed to the presence of ions in the matrix which induce a Stark-shift in the quantum states of neighboring molecules.

Detailed studies of these spectral features were made by Brooks et al. (1983, 1985) using proton-beam irradiation of tritium-free solid D_2 —an approach which allows complete control over the magnitude and timing of the radiation doses. The radiation-induced lines were seen to persist for many hours after irradiation ceased, implying that the ions involved have very low mobilities. Brooks et al. (1985) identified the immobile anion as an “electron bubble” (i.e., an electron trapped in a lattice defect) but did not claim to have identified the immobile cation; they suggested D_3^+ , or the solvated form $D_0^+ = D_3^+(D_2)_3$.

Later studies of electron-beam and gamma-ray irradiated solids by Oka and collaborators (Oka 1993; Chan et al. 2000; Momose et al. 2001) emphasized the use of *para*- H_2 (i.e., $J = 0$) enriched solids to achieve intrinsically very narrow spectral lines; again the cations were interpreted as H_3^+ and its solvated forms.

2.2. Broad Spectral Features

In parallel with the investigations of radiation-induced absorption lines there were studies of broad band absorption in irradiated solid hydrogens. Again these studies commenced with solids containing tritium (Richardson et al. 1981; Poll et al. 1983) and later utilized external sources of ionizing radiation (Selen et al. 1984; Forrest et al. 1990). Broad infrared/optical absorptions were reported and interpreted in terms of bound–bound transitions of electron bubbles (Richardson et al. 1981; Poll et al. 1983; Selen et al. 1984), and a continuum UV absorption was reported and interpreted as the bound–free transitions of electron bubbles (Forrest et al. 1990).

Surprisingly, irradiated solid hydrogens were also observed to emit optical/near-infrared continua in a broadband peaking around 825 nm (Forrest et al. 1992; Magnotta et al. 1994; Forrest & Brooks 1997). Both steady emission and short flashes were seen to occur with essentially the same spectrum. Emission from solid deuterium was observed to be much stronger than that from solid H_2 . It was also observed that the optical emission increased in response to UV exposure, indicating a close connection with the UV continuum absorption process (Magnotta et al. 1994), but the actual emission process was not securely identified. One possibility is that the emission is due to radiative attachment of e^- and hydrogen atoms (Forrest et al. 1992; Forrest & Brooks 1997). In gas-phase the H^- bound–free opacity (e.g., Doughty et al. 1966) has a spectral peak in a similar location to the observed emission from solid D_2 , but the H^- opacity peak is much broader than that of the observed emission.

2.3. Paramagnetic Signals

By virtue of having no unpaired electrons H_2 molecules themselves have no electron spin resonance (ESR) signal. But the irradiated solid exhibits several features (e.g., Kumada et al. 2008). First there is a strong signal from atomic hydrogen, produced by dissociation of the molecules. Second there is a signal from free electrons in the solid, produced by ionization of the molecules. Third there is a quartet of lines (Miyazaki et al. 1995), initially suggested to be due to H_2^- (Symons 1995), but later recognized as the signature of H_6^+ (Symons & Woolley 2000; Suter et al. 2001; Kumada et al. 2005). Further ESR investigations of irradiated solid hydrogens conclusively demonstrated that H_6^+ is indeed the source of the quartet lines by studying solid mixtures of H_2 and HD or D_2 , for which a variety of isotopomers of H_6^+ arise, each with its own unique ESR signature (Kumada et al. 2006; Kumagai et al. 2007).

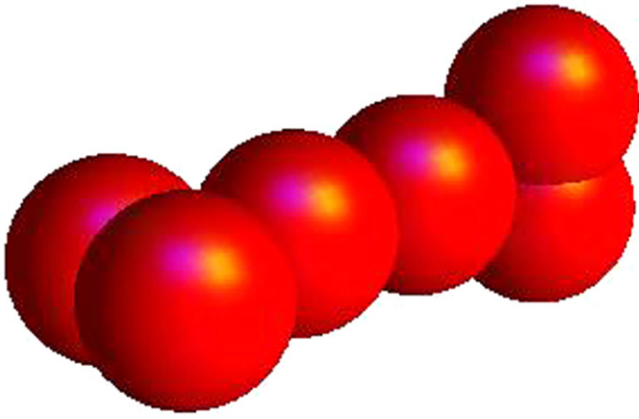


Figure 1. D_{2d} configuration of H_6^+ , which is the structure corresponding to the global minimum of potential energy for this molecule (Kurosaki & Takayanagi 1998b).

(A color version of this figure is available in the online journal.)

2.4. Molecular Hydrogen Ion Clusters

All of the literature cited in Sections 2.1 and 2.2 implicitly assumes that molecular hydrogen ion chemistry in the condensed phase resembles that of the gas phase, for which it is well established that clusters H_n^+ with odd- n occur in much greater abundance than those with even- n (Clampitt & Gowland 1969; Hiraoka 1987; Ekinici et al. 2006). The subsequent discovery of H_6^+ in the ESR experiments on irradiated solid hydrogens (Section 2.3) challenges that assumption. There seems to be no experimental data which point specifically to the presence of H_3^+ , or its solvated forms, in irradiated solid hydrogens: it is possible that the dominant cations are H_6^+ isotopomers and their solvated forms.

The existence of even- n clusters was predicted on the basis of ab initio calculations which showed them to have comparable binding energies to the odd- n clusters (Wright & Borkman 1982). The even- n clusters were then discovered in gas phase via mass spectroscopy (Kirchner & Bowers 1987), albeit at abundances very much lower than those of odd- n . H_6^+ was seen in these experiments to have much higher abundance than H_4^+ , H_8^+ , or H_{10}^+ and this result prompted further theoretical investigations of H_6^+ and the other even- n clusters (Montgomery & Michels 1987; Kurosaki & Takayanagi 1998a, 1998b). In particular Kurosaki & Takayanagi (1998a) confirmed the stability of H_6^+ and identified its most stable configuration as D_{2d} symmetry—a structure which is *not* based on the H_3^+ moiety, as can be seen in Figure 1.

Naïvely H_6^+ can be thought of as a central H_2^+ with an H_2 molecule bonded perpendicularly at each end, the axes of the three moieties being mutually orthogonal. In fact each atom in the molecule carries a similar fraction of the total charge (Kurosaki & Takayanagi 1998b). These authors also demonstrated the stability of larger clusters up to H_{14}^+ . The structure of the clusters was shown to correspond to solvation of H_6^+ by H_2 , with the solvating molecules being loosely bound and carrying very little charge, and the central H_6^+ moiety only slightly perturbed in its charge distribution and bond lengths.

The existence of very large even- n clusters has been demonstrated experimentally by Jaksch et al. (2008): molecular hydrogen ion clusters as large as $n = 120$ were observed via mass spectroscopy of ionic species formed inside ultra-cold (0.4 K) helium nanodroplets. Odd- n species were also produced and the ratio of even:odd clusters was observed to be small. Jaksch et al.

(2008) argued that their high yield of even- n clusters indicated that cluster ionization dynamics are affected by a helium matrix. The ionization dynamics of hydrogen clusters have been studied theoretically by Tachikawa (2000).

2.5. Summary of Impurities in Solid H_2

The ESR studies described in Section 2.3 demonstrate explicitly that irradiated solid hydrogens contain free electrons, atomic hydrogen, and H_6^+ . Free electrons and H-atoms can combine to yield H^- , and this reaction is strongly favored by the large ratio of the electron affinity of hydrogen (755 meV) to the temperature ($T < 14$ K, so $kT \lesssim 1$ meV). In a low temperature bath of H_2 , solvation of this anion and the H_6^+ cation are both expected. Icosahedral solvation shells have been suggested for both species (Wang & Andrews 2004; Jaksch et al. 2008). But it is not clear whether this remains a preferred geometry for solvation in the context of a solid H_2 matrix, where the interface between the solvation shells and the H_2 lattice presumably plays a significant role in determining the form of solvation.

In the astrophysical context hydrogen is not expected to occur as a pure element, but mixed with helium and trace amounts of metals. It appears that helium does not alloy with solid hydrogen (Leventhal & Mills 1991), but it is possible that a solid hydrogen matrix might contain metal impurities. In this paper we ignore that possibility and confine our attention to the hydrogen alone as there is plenty to occupy us even in this restricted case. We further assume that the deuterium abundance is $X_D \sim 10^{-5}$ by number, i.e., comparable to the deuterium abundances measured in diffuse Galactic gas (e.g., Sembach 2010). We expect this to manifest itself as an abundance of HD: H_2 that is X_D by number.

A solid hydrogen of this composition, when subject to ionizing radiation, will usually yield H_6^+ that is free of deuterium at the time of formation. However, the zero-point vibration energy (ZPVE) of singly deuterated H_6^+ (plus H_2) is about 13 meV lower than that of the undeuterated isotopomer (plus HD)—see the Appendix—so at low temperatures condensation of HD onto the H_6^+ proceeds. And the net ZPVE is further lowered by a similar amount for each of two subsequent deuterations, with the result that at temperatures less than about 12 K condensation proceeds all the way to $(HD)_3^+$.

We use the shorthand $(HD)_3^+$ to denote the specific isotopomer $[HD(HD)HD]^+$, where the central- and two end-moieties are encoded in the notation as $[End(End)End]^+$.

If the ionization rate in the solid is sufficiently high that the concentration of H_6^+ is of order $X_D/3 \sim 3 \times 10^{-6}$, then there is insufficient HD in the lattice to fully deuterate the H_6^+ and at these concentrations the singly and doubly deuterated isotopomers listed in the Appendix will constitute a significant fraction of the H_6^+ . At still higher ionization rates even these lightly deuterated isotopomers are in the minority and the H_6^+ isotopomer dominates. For simplicity we consider here only very high and very low ionization rates, for which the H_6^+ is essentially all in the form of the H_6^+ and $(HD)_3^+$ isotopomers, respectively.

The first two HD condensations on H_6^+ were observed by Kumagai et al. (2007) in ESR studies of irradiated solid hydrogens at 4 K, but these authors did not report a detection of $(HD)_3^+$. As each of the deuteration reactions involves lowering the ZPVE by a similar amount there is an expectation that if condensation starts it will go all the way to $(HD)_3^+$. We therefore assume that $(HD)_3^+$ was not detected by Kumagai et al. (2007) because its ESR spectrum is very complex and/or the lines are broad. We note that Kumagai et al. (2007) did not report

any isotopomer of H_6^+ containing D_2 or D_2^+ moieties except when the solid itself was made from a mixture including D_2 . This demonstrates that the condensation process is one where diatomic hydrogen molecules are preserved as units which are substituted in or out of the H_6^+ —a situation which is unsurprising considering the large energy (4.5 eV) that is required to break up H_2 .

3. THEORETICAL MODEL OF H_6^+

Before tackling H_6^+ itself we performed preliminary theoretical studies on H_2 and H_2^+ . We used various ab initio electronic structure methods, all available within the Q-Chem software package (Shao et al. 2006), to calculate the bond length and fundamental harmonic frequency for each molecule. From these calculations it was determined that the most suitable level of theory for our calculations is coupled cluster with single and double excitations (CCSD), combined with cc-pVTZ basis functions (correlation-consistent polarized Valence-only Triple Zeta-function). We found that the CCSD/cc-pVTZ combination gave a good compromise between accuracy and computational cost, for both H_2 and H_2^+ , with deviations of less than 0.001 Å and 5 cm^{-1} from our most accurate method, CCSD/cc-pVQZ, which utilizes a Quadruple Zeta-function basis set. Henceforth all the results we quote in this paper were obtained by using the CCSD/cc-pVTZ level of theory, unless stated otherwise.

To determine the importance of augmenting our basis function set with additional diffuse functions, we performed calculations of the energy required to break H_6^+ into $2\text{H}_2 + \text{H}_2^+$. The binding energy at the CCSD/cc-pVTZ level is $235.57 \text{ kJ mol}^{-1}$, whereas the CCSD/aug-cc-pVTZ energy is $236.35 \text{ kJ mol}^{-1}$. The effect of augmenting our chosen basis is thus one-third of 1%, from which we conclude that diffuse functions are not required.

After our calculations on H_6^+ were completed we became aware of a comprehensive ab initio study of the properties of H_6^+ (Hao et al. 2009), which had been published shortly after we completed our initial survey of the literature. The study of Hao et al. (2009) took in six different possible structures for H_6^+ and utilized various levels of theory: both restricted and unrestricted Hartree–Fock theory and CCSD with extension to perturbative and full triple-excitations. They used the basis sets cc-pVTZ and cc-pVQZ and their augmented counterparts aug-cc-pVTZ and aug-cc-pVQZ. In all 26 different combinations of basis-function sets and levels of theory were utilized by Hao et al. (2009).

In Section 3.2 we compare our results with those of Hao et al. (2009). However, in this paper our emphasis differs greatly from theirs in that we have concerned ourselves with treating the large anharmonic corrections to the vibration frequencies of H_6^+ , and our study takes in isotopic variations for the reasons given earlier. We undertook detailed modeling of only the lowest energy configuration of the molecule, namely, the D_{2d} structure. We have, however, modeled the D_{2h} transition structure at the harmonic level in order to gauge the effects of rotational delocalization of the end-groups of the molecule (see Section 3.2.1).

3.1. Electronic Excitations

Excited electronic states of H_6^+ were investigated using the equations of motion formalism (Krylov 2008). In addition to the CCSD/cc-pVTZ level of theory we utilized CCSD/aug-cc-pVTZ (i.e., augmented by additional diffuse basis functions) for this study. At the cc-pVTZ level we found the lowest two excited states to be 2^2A_1 at 7.44 eV and 1^2E at 8.79 eV. With

the augmented basis these levels shifted to 7.43 eV and 8.35 eV, respectively. The 2^2A_1 state is reached by a valence transition and is unaffected by the additional diffuse functions in the aug-cc-pVTZ basis. The degenerate 1^2E state is stabilized by 0.44 eV in the larger aug-cc-pVTZ basis, indicating that it is more diffuse. Not surprisingly, given that the binding energy of the ground state of H_6^+ is only 2.1 eV (Kurosaki & Takayanagi 1998b), the potential energy surfaces (PESs) of both these states are repulsive, so the molecule would dissociate if excited into either.

We have also investigated the influence of solvation on electronic excitations by computing the energies of the two lowest-lying states for $\text{H}_6^+(\text{H}_2)_4$. We found them to be substantially lower at 6.52 and 7.01 eV (EOM-CCSD/cc-pVTZ), but still repulsive. In practice we expect much higher levels of solvation. For example, Jaksch et al. (2008) found evidence for closed icosahedral solvation shells—the first closed shell corresponding to $\text{H}_6^+(\text{H}_2)_{12}$ and the second to $\text{H}_6^+(\text{H}_2)_{12}(\text{H}_2)_{42}$ —when studying very cold (0.4 K) solvated clusters. We therefore expect that the lowest-lying electronic excitations of the actual solvated form will be much lower than those of $\text{H}_6^+(\text{H}_2)_4$ and we assume that some of these states will be bound states. This assumption, and the change in the electronic spectrum, on solvation, is important in the context of excitation of the vibrational modes of H_6^+ (see Section 3.2.2).

Because we are dealing with a cation, we expect the energy required for any further ionization to be large. We have confirmed this by direct calculation: the energy required for photoionization (“vertical ionization”) of bare H_6^+ is 19.2 eV and that of $\text{H}_6^+(\text{H}_2)_4$ is 18.3 eV.

3.2. Vibrational Model

When computing the vibrational properties of a molecule the harmonic approximation is usually employed. Such calculations are routine with the Q-Chem software package and yield both the frequencies of the normal modes and the electric-dipole intensities of $|\Delta v| = 1$ vibrational transitions. In the harmonic approximation the PES is taken to be quadratic about the equilibrium geometry. But H_6^+ is a weakly bound system (Kurosaki & Takayanagi 1998b), for which the higher-order terms in the PES are expected to be relatively large. And furthermore the molecule is composed entirely of hydrogens, which are the lightest nuclei and thus have the largest vibration amplitude in any given potential, so the higher-order terms in the PES are of particular importance.

Our model of the effective PES, which we denote U_{eff} , is a Taylor expansion in the normal mode coordinates, q_i , of the system, around the potential minimum. For $N = 6$ atoms there are $3N - 6 = 12$ such coordinates (the other six degrees of freedom are taken up by rigid body rotations and translations). Our model includes the usual quadratic terms, plus contributions that are cubic and quartic in the normal mode coordinates. In terms of the potential derivatives, η (the number of subscripts indicating the order of the derivative), we thus have

$$U_{\text{eff}}(\mathbf{q}) = \frac{1}{2!} \sum_i \eta_{ii} q_i q_i + \frac{1}{3!} \sum_{ijk} \eta_{ijk} q_i q_j q_k + \frac{1}{4!} \sum_{ijkl} \eta_{ijkl} q_i q_j q_k q_l. \quad (1)$$

At the CCSD level only analytic gradients are available, so all the η terms in Equation (1) had to be computed using

Table 1
Normal Modes of the D_{2d} Structure of H_6^+ and $(\text{HD})_3^+$

Species	Mode No.	Symmetry	I_o (km mol^{-1})	ω_o (cm^{-1})	ν (cm^{-1})
H_6^+	12	A_1	0.0	3858.1	3596.0
	11	B_2	953.3	3779.1	3347.6
	10	A_1	0.0	2087.4	1816.0
	9*	E	6.9	1189.5	1104.8
	8*	E	6.9	1189.4	1104.7
	7	B_2	2418.6	1018.1	1042.1
	6	A_1	0.0	906.9	884.9
	5*	E	13.6	726.0	795.0
	4*	E	13.6	726.0	794.6
	3*	E	0.3	356.2	794.6
	2*	E	0.3	356.2	795.0
	1*	B_1	0.0	99.2	201.3
$(\text{HD})_3^+$	12		6.4	3343.3	3070.2
	11		714.3	3275.3	2947.7
	10		274.7	1827.3	1574.2
	9*		5.4	1073.1	962.9
	8*		47.6	999.1	908.6
	7		1142.1	865.1	832.5
	6		299.2	800.7	738.1
	5*		72.9	616.8	626.6
	4*		25.0	557.4	613.8
	3*		2.9	297.8	225.3
	2*		1.2	291.0	184.6
	1*		4.4	84.7	120.5

Notes. Wavenumbers are given both with (ν) and without (ω_o) anharmonic corrections. Changes in rotational state of the molecule shift the lines away from these wave numbers. Modes marked with an asterisk are strongly affected by rotation of the end-groups, so these modes are not good approximations to the eigenmodes of the real molecule (Section 3.2.1).

finite difference methods to evaluate curvatures and higher-order derivatives of U_{eff} . We used a step size, h , of 0.1 Bohr and accurate finite difference expressions that give truncation errors of $O(h^4)$.

Anharmonic corrections to the vibration frequencies were computed using the vibrational configuration interaction (VCI) method (Whitehead & Handy 1975; Lin et al. 2008) in which up to five quanta were included. For computational reasons only two-mode coupling was considered. That is η_{ijj} terms were considered, but η_{ijk} terms, where $i \neq j \neq k$, were not. We also excluded all couplings to vibration mode 1 because, as discussed later (Section 3.2.1), this mode is better characterized as an internal rotation than a vibration.

Table 1 shows our results for the normal vibrational modes of H_6^+ . There we list the harmonic frequency, the electric-dipole intensity (derived in the harmonic approximation), and the anharmonic frequency for each mode. The four intensities listed as zero are, in the harmonic approximation, precisely zero in consequence of the symmetry of the mode (A_1 or B_1). Of the remaining eight modes, all six of E symmetry are fairly quiet while the two B_2 modes are both strong. These two modes acquire their intensity as a result of displacing the central H_2^+ moiety along its axis. Indeed mode 7 can be thought of as the central H_2^+ moiety bouncing back and forth along the main axis of the molecule and this mode is by far the most intense. Modes 12 and 11 both involve stretching of the two H_2 end-moieties and axial displacement of the central atoms. The two modes differ in that mode 12 is a symmetric manifestation of these motions whereas mode 11 is antisymmetric. Consequently

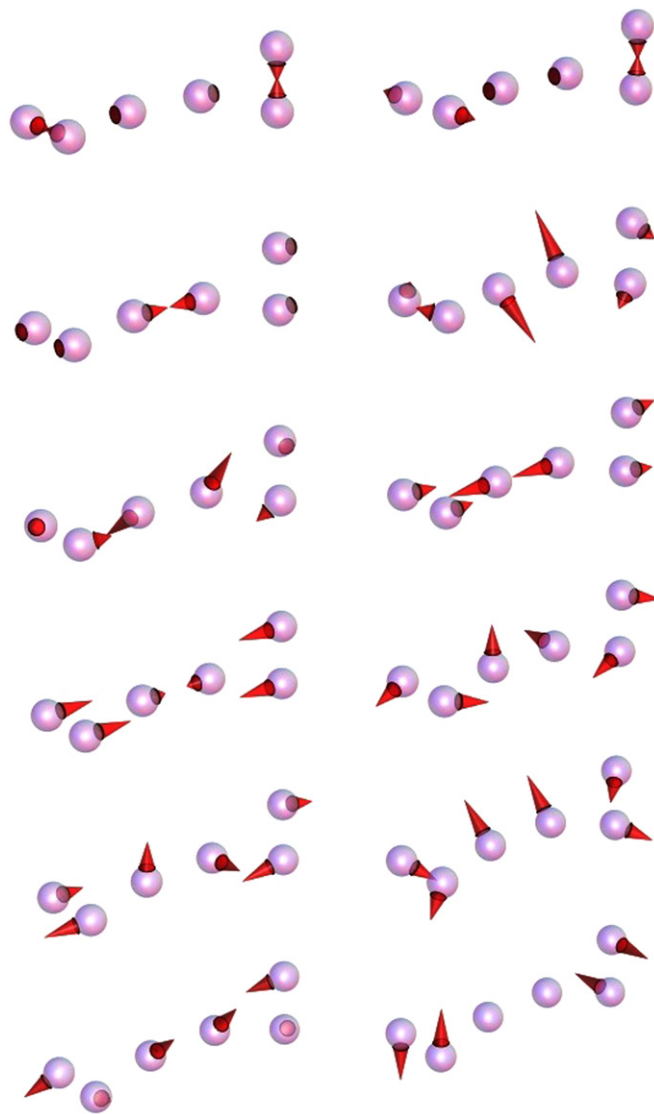


Figure 2. Normal modes of vibration of H_6^+ . The left column shows the even-numbered modes, in descending order starting from mode 12 at the top. The right column shows the odd-numbered modes, in descending order starting from mode 11 at the top. Spheres show the locations of the atoms at rest and red cones show the amplitude and direction of motion for each atom.

(A color version of this figure is available in the online journal.)

the latter involves a displacement of the central H_2^+ moiety and thus acquires a large intensity, whereas mode 12 simply stretches this moiety. Figure 2 shows the motions involved in each of the normal modes of H_6^+ .

Comparing the frequencies in the two rightmost columns of Table 1 shows clearly the high degree of anharmonicity in this molecule, exceeding 400 cm^{-1} for some modes.

Having obtained the PES model as per Equation (1) most of the computational work associated with the vibrational calculations is done and it is straightforward to investigate the isotopic variants of H_6^+ . In Section 2.5, we noted that condensation of HD onto H_6^+ is expected to proceed; so in Table 1 we also present the normal modes of $(\text{HD})_3^+$. For this isotopomer the vibrational symmetries of H_6^+ are broken and thus there are no silent modes. Indeed modes 10 and 6 acquire large intensities. Because the effective oscillating mass is greater for $(\text{HD})_3^+$ than for H_6^+ , each of the normal modes of $(\text{HD})_3^+$ has a lower frequency

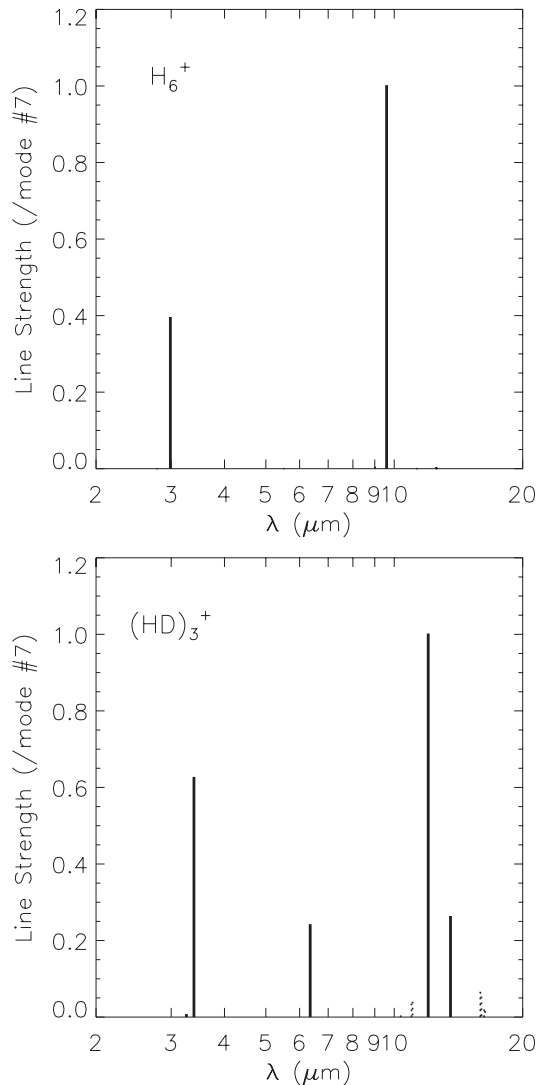


Figure 3. Stick diagram of the mid-IR lines of H_6^+ (upper panel) and $(HD)_3^+$ (lower panel). The line strengths are normalized to that of mode 7 for each molecule. The E -type modes of the D_{2d} structure are not good approximations to the actual eigenmodes of the molecules (see Section 3.2.1) and they are therefore plotted with dotted lines.

than the corresponding mode for H_6^+ . Whereas H_6^+ shows only two strong lines (in the harmonic approximation), there are at least four strong lines for $(HD)_3^+$. The lines for both isotopomers are shown in Figure 3.

The normal modes of vibration are not the whole story. In the harmonic approximation the normal modes are the only modes and they are non-interacting. The intensities are the same for all $|\Delta v| = 1$ transitions of a given mode and zero for $|\Delta v| \geq 2$, but we have seen that the anharmonicity is large for H_6^+ and we therefore expect that there may be significant intensities associated with some of the overtones ($|\Delta v| \geq 2$) and combination bands (which result from coupling between the normal modes). Although we have calculated the frequency shifts due to anharmonicity, we are unable to compute the intensities of overtones or combinations.

3.2.1. Errors and Uncertainties

There are various sources of error in our vibrational model of H_6^+ ; although we cannot remove these errors it is useful to know roughly how large they are. The easiest check to make

is whether or not the predicted harmonic properties of H_6^+ vary significantly with the level of electronic structure theory which is utilized. That test can be made by examining the results of Hao et al. (2009), either in isolation or by comparison with our own results. The highest levels of theory utilized by Hao et al. (2009) are cc-pVTZ UCCSDT and aug-cc-pVQZ UCCSD(T) and at these levels the harmonic frequencies typically differ by amounts (mean absolute difference) of order 11 cm^{-1} and 17 cm^{-1} , respectively, compared to our own results. These differences constitute a small fractional error for most of the vibrational modes.

Our level of theory corresponds precisely to the cc-pVTZ UCCSD case of Hao et al. (2009). In this case the mean absolute frequency difference between the two sets of results is only 6 cm^{-1} (or 4 cm^{-1} if mode 1 is excluded from the comparison). We attribute these differences to the fact that Hao et al. (2009) use analytic derivatives whereas we employ numerical derivatives.

In respect of the predicted (non-zero) intensities of the various modes there is, however, a substantial difference between our results and those of Hao et al. (2009). Comparing our results to the highest levels of theory employed by Hao et al. (2009) we see good agreement only for mode 11 (difference less than 10%), whereas for mode 7 their predicted intensity is less than half of ours and for modes 8 and 9 it is larger by a factor of 10. The disagreement is larger still for the four remaining modes, their intensities being more than 20 times larger for modes 4 and 5, and more than 1000 times larger for modes 2 and 3. However, these discrepancies parallel those which are evident amongst the various levels of theory of Hao et al. (2009) for each of the modes, to wit: discrepancies of order 10% for mode 11; a range spanning a factor of 3 for modes 7, 8, and 9; a factor of 30 for modes 4 and 5; and a factor of 100 for modes 2 and 3.

Given the huge variation in intensities reported by Hao et al. (2009), for the same mode with different levels of theory, we have no cause to doubt our own estimates of the mode intensities.

By comparing our calculations to observed vibrational characteristics we are also able to gauge errors beyond just the harmonic level. These checks cannot be made against H_6^+ itself, because the vibrational frequencies of that molecule have not yet been measured, but we have checked the accuracy of the quartic approximation in Equation (1) for the case of the H_2 molecule: we find that the computed vibration frequency is 61 cm^{-1} above the measured value for that molecule. Employing a sextic approximation to the PES reduces this error to only 2 cm^{-1} , so the error associated with the quartic approximation of Equation (1) appears to be roughly 60 cm^{-1} (at 4159 cm^{-1}). Another major source of error in our calculations of vibrational frequencies stems from our use of only two-mode coupling in the VCI method. By modeling H_3^+ we find that the errors introduced by restricting our calculations to two-mode coupling could be as large as 50 cm^{-1} (at $2,521 \text{ cm}^{-1}$).

All of our results here pertain to the isolated H_6^+ molecule, and its isotopomers, whereas we expect that H_6^+ inside a matrix of solid H_2 would be in the solvated form, which will have slightly different vibrational properties. In Section 3.4 we give quantitative estimates of the effects of solvation on the vibration frequencies of H_6^+ by noting the shifts which occur at the harmonic level between H_6^+ and $H_6^+(H_2)_4$.

Finally we draw attention to a fundamental source of uncertainty in our modeling of the vibrations of H_6^+ . Although the D_{2d} structure is the minimum energy configuration of H_6^+ , the D_{2h} structure, in which the two end-groups lie in the same plane



Figure 4. D_{2h} transition structure of H_6^+ differs from the D_{2d} structure of Figure 1 only in respect of the dihedral angle between the end-groups. This structure is a saddle point of the PES and it lies only 12 cm^{-1} above the D_{2d} minimum (Kakizaki et al. 2007).

(A color version of this figure is available in the online journal.)

(see Figure 4), is a transition structure which lies only 1.5 meV (12 cm^{-1}) above the minimum (Kakizaki et al. 2007). This transition structure can be reached simply by counter-rotation of the end-groups of H_6^+ , i.e., the degree of freedom manifest in vibration mode 1 (see Figure 2). But the vibration frequency for mode 1 is larger than the barrier height and even the ZPVE is sufficient to completely delocalize the structure in this coordinate. The resulting probability distribution functions have been computed by Kakizaki et al. (2007) for the isotopomers H_6^+ and D_6^+ and in both cases they are almost uniform in the dihedral angle. The situation is more complicated in the case of $(HD)_3^+$, because the center of mass of the HD end-groups does not coincide with the mid-point of the bond, around which the groups rotate. For small amplitude vibrations (in mode 1) the result is simply that the H atom oscillates with twice the amplitude of the D atom. But that cannot be the case for large amplitude motions: if one atom performs a complete rotation, so must the other. Rather we anticipate that the atoms of the central HD^+ group will move in response to the rotation of the end-groups. The $(HD)_3^+$ isotopomer was not modeled by Kakizaki et al. (2007) but we assume that, like H_6^+ and D_6^+ , the end groups of the molecule are delocalized in the dihedral angle.

Delocalization affects the vibrational characteristics of the molecule. Strictly speaking it means that none of our analysis is valid, because U_{eff} is a sinusoidal function of q_1 which, over its full range, is very poorly represented by Equation (1). And to the extent that the properties of a vibration mode depend on the dihedral angle that mode is necessarily coupled to mode 1. All couplings involving mode 1 are explicitly excluded from our model because mode 1 has more the character of an internal rotation than a vibration.

To gauge the size of these effects we can compute the harmonic vibration frequencies for the D_{2h} structure and compare them to those of the D_{2d} structure. We have done this and in Table 2 we show our results as the quantity $\Delta_{dh} = \omega_o(D_{2h}) - \omega_o(D_{2d})$.

For mode 1 the D_{2h} structure has an imaginary vibration frequency because it is a maximum of the PES traversed along the coordinate q_1 . For modes 6, 7, 10, 11, and 12 we find that the frequencies are the same as those of the D_{2d} structure to within 10 cm^{-1} and the mean absolute difference is only 6.4 cm^{-1} . These shifts are very small and that tells us that those modes are good approximations to the eigenmodes of the actual system, with its rotationally delocalized end-groups. We can therefore

Table 2
Vibrational Frequency Shifts for D_{2h} Structure and Solvated Form of D_{2d}

Mode No.	Symmetry	Δ_{dh} (cm^{-1})	Δ_s (cm^{-1})
12	A_1	6	-50
11	B_2	3	-68
10	A_1	10	-23
9	E	55	5
8	E	-115	5
7	B_2	-10	25
6	A_1	-3	27
5	E	120	34
4	E	-112	34
3	E	39	56
2	E	-17	56
1	B_1

Notes. The symmetry designation refers to the isotopomer H_6^+ in the D_{2d} structure. Frequencies appropriate to the D_{2h} structure are given by adding Δ_{dh} to the values in Table 1. Frequencies appropriate to the solvated species are given by adding Δ_s to the values in Table 1.

be confident that we have a reliable estimate of the frequencies of the corresponding lines.

For the remaining six modes, all of which have E-type symmetry, the shifts are an order of magnitude greater. Degeneracy of the three pairs of E-modes of H_6^+ in the D_{2d} structure is lifted in D_{2h} with splittings of 56 cm^{-1} (modes 2, 3), 232 cm^{-1} (modes 4, 5), and 170 cm^{-1} (modes 8, 9). Thus, the E-modes are strongly influenced by the nearly free rotation of the end-groups of the H_6^+ molecule.

The reason for this striking difference between the E-modes and the modes of A and B symmetry is that the E-modes all involve displacements of the central two atoms perpendicular to the z -axis (i.e., the long axis of the molecule), whereas the other modes only displace these atoms along the z -axis (see Figure 2). Thus E-mode vibrations are affected by the orientation of the end-groups, but the other modes are not.

The large frequency shifts of the E-type modes between D_{2d} and D_{2h} structures indicate that the corresponding vibrational eigenstates which we have characterized for the D_{2d} structure are poor approximations of the actual eigenstates of the rotationally delocalized molecule. We therefore place correspondingly little weight on these modes when comparing our results to observational data.

3.2.2. Excitation of Vibrations

In solid H_2 the temperature is necessarily below the triple-point of hydrogen so we have $kT < 10\text{ cm}^{-1}$, whereas the smallest vibrational quantum of H_6^+ exceeds 100 cm^{-1} , thus all of its excited vibrational states lie too far above the ground state to have any significant thermal population. There will thus be no thermal emission of vibrational quanta from H_6^+ in solid H_2 . But the vibrational modes of H_6^+ can be excited by non-thermal interactions. The most important non-thermal process is likely to be absorption of ambient starlight, for which the energy density peaks at a wavelength of approximately $1\text{ }\mu\text{m}$ (Mathis et al. 1983), corresponding to photon energies $\sim 1\text{ eV}$.

There are two mechanisms by which H_6^+ may absorb ambient starlight: via electronic excitation and through vibrational combination bands. Ordinarily one would expect the former to be by far the more important of these two processes, as combination bands are usually very weak. However, there are

three aspects of H_6^+ which suggest that combination bands may not be completely negligible. First is that the energy of the lowest excited electronic state is very high at 7.44 eV, where the energy density of the ambient radiation field is only one-fifth to one-tenth of its value at the peak (Mathis et al. 1983). By contrast there are many vibrational combination bands of H_6^+ distributed right across the broad spectral peak of the ambient starlight. Second, even the lowest excited electronic state lies well above the vibrational continuum of the electronic ground state of H_6^+ , which has a binding energy of only 49 kcal mol⁻¹, or 2.1 eV per molecule (Kurosaki & Takayanagi 1998b). This means that the bulk of the photon energy cannot go into exciting the vibrational modes of H_6^+ . Indeed we expect that there will be essentially no excitation of vibrations as the two lowest excited electronic states are repulsive and dissociation should occur promptly. Thus electronic excitation is an inefficient way of powering vibrational emission from H_6^+ . This is in stark contrast with excitation through vibrational combination bands—a process which is 100% efficient. Finally we note that H_6^+ is an unusually floppy, anharmonic molecule and hence we expect it to have unusually strong combination bands.

Solvated forms of H_6^+ are also floppy and thus are also expected to have unusually strong combination bands. However, we have found (Section 3.1) that solvation to $\text{H}_6^+(\text{H}_2)_4$ lowers the minimum electronic excitation energy significantly. And for greater degrees of solvation we expect the energy to decrease further; we assume that this gives rise to excited electronic states which are bound. Lowering the energy of the excited state increases the efficiency of excitation of the vibrational degrees of freedom and it brings the electronic excitations into the spectral peak of the ambient starlight. We therefore anticipate that for highly solvated forms of H_6^+ , which are prevalent at low temperatures, electronic excitation is the dominant process.

Unfortunately we cannot sensibly model the electronic excitation of vibrations, because the excited electronic states are sensitive to the form of solvation of the molecule. Consequently we are currently unable to model the optical absorption spectrum of H_6^+ or the vibrational level population subsequent to such absorption. It is the latter which determines the strength of any vibrational emission because the cascade of emitted quanta will be dominated by $\Delta v = -1$ transitions in the various modes which have been excited. Thus we are unable to model the intensities of the mid-IR emission lines from H_6^+ .

We now consider the band structure which arises from rotational transitions of the molecule during emission of a vibrational quantum.

3.3. Rotational Band Structure

In the rigid-body approximation the rotational properties of H_6^+ are characterized by its moments of inertia or, equivalently, its rotational constants. For H_6^+ these are $B_x, B_y = 1.38 \text{ cm}^{-1}$ and $B_z = 26.8 \text{ cm}^{-1}$ and for $(\text{HD})_3^+$ $B_x, B_y = 0.92 \text{ cm}^{-1}$ and $B_z = 18.5 \text{ cm}^{-1}$. Thus both isotomers resemble a prolate symmetric top. Because $B_x, B_y \ll kT < B_z$ in both cases, rotation about the x - and y -axes may be thermally excited, whereas there will be little thermal excitation of rotation around z .

As emphasized in Section 3.2.1, H_6^+ is actually a floppy molecule and rigid-body rotation results are therefore not a good guide to its rotational properties.

Solvated species of H_6^+ will also be floppy because the H_6^+ itself is only slightly perturbed by solvation and the bonds between the solvent and solvated molecules are themselves

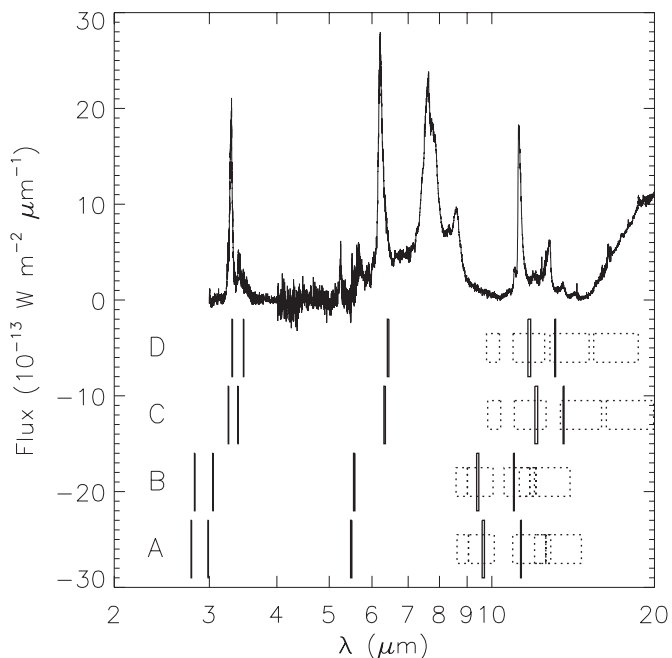


Figure 5. *Infrared Space Observatory* spectrum of the Orion Bar (Peeters et al. 2004). A background flux $\propto \lambda^{3.2}$ has been subtracted from the data so that the broad emission bands can be seen more easily. Also plotted here, in the lower half of the figure, are the locations of the predicted fundamental vibration lines for H_6^+ and $(\text{HD})_3^+$ isotomers in bare and solvated forms. Each line is stretched into a band whose spectral width spans the predictions for D_{2d} and D_{2h} structures in the case of the bare isotomers. Reliable predictions are shown with solid lines whereas the E -type modes are indicated with dotted lines. Predictions are coded thus: A $\leftarrow \text{H}_6^+$, B $\leftarrow \text{H}_6^+(\text{H}_2)_4$, C $\leftarrow (\text{HD})_3^+$, and D $\leftarrow (\text{HD})_3^+(\text{H}_2)_4$.

weak. The impediment to calculation therefore exists also in this case. A further uncertainty for the solvated species is whether or not such a large complex is able to rotate at all inside a matrix of solid hydrogen. Alternatively, internal rotation of the H_6^+ might occur relative to the solvating shells.

In view of the difficulties just described we are not able to undertake sensible calculations of the rotational band structure for H_6^+ .

3.4. Model Spectra

As we are unable to model either the strength of the vibrational emission or the band structure appropriate to the various lines, the only real information contained in our model spectra is the line frequencies. We therefore present the results of our modeling simply by marking the wavelengths of the vibration modes in Figure 5. Results are shown for both H_6^+ and $(\text{HD})_3^+$.

We remind readers that modes of E symmetry are not good approximations to the eigenmodes of the real molecule; they are therefore shown with dotted lines, to draw attention to the unreliable nature of the prediction. We further emphasize the effect of the rotation of the end-groups by plotting each mode as a box whose spectral width spans the frequencies predicted for the D_{2d} and D_{2h} structures (see Table 2). For the five well characterized modes these boxes are sufficiently narrow that they resemble vertical lines in Figure 5.

3.4.1. Effects of Solvation

Following Kurosaki & Takayanagi (1998b) we have characterized the harmonic vibration frequencies of the solvated

molecule $\text{H}_{14}^+ = \text{H}_6^+(\text{H}_2)_4$ in D_{2d} symmetry. Because of the much larger number of atoms, H_{14}^+ inevitably has many more modes of vibration—24 more than H_6^+ in fact. Of these the highest four frequencies are associated with stretching of the four solvent molecules, and most of the lowest frequencies are associated with vibrations which involve the weak bonds between these molecules and the core H_6^+ . In between there are modes which can be readily identified as perturbed modes 2–12 of the core H_6^+ . Comparing the frequencies of these modes with the harmonic frequencies for bare H_6^+ (Table 1) gives us an indication of the likely shifts associated with solvation. Our results are given as the quantity Δ_s in Table 2—a frequency shift which should be added to the predictions for the bare molecule in order to obtain the vibration frequencies of the solvated form.

We now apply these shifts to our anharmonic frequency predictions for H_6^+ and $(\text{HD})_3^+$ in order to estimate the vibration frequencies for the solvated forms of these molecules. The results of this procedure are shown in Figure 5.

4. H_6^+ SPECTRA VERSUS ASTRONOMICAL DATA

In addition to our theoretical predictions, we have shown in Figure 5 the *Infrared Space Observatory* mid-IR spectrum of the Orion Bar (Peeters et al. 2004). This spectrum was chosen because the data are of high quality and the band strengths and profiles are representative of the sort of spectrum which is most commonly seen, i.e., the “Type A” spectrum (Geballe 1997; Tokunaga 1997; Peeters et al. 2002; van Diedenhoven et al. 2004).

For clarity of presentation we have eliminated from this plot sixteen narrow lines arising from atomic or molecular hydrogen, neon, sulphur, or argon. The lines are (van Dishoeck 2004): H, Brackett- α ; four lines from the Pfund series of H; five pure rotational lines from H_2 ; [Ar II] 7.0 μm ; [Ar III] 9.0 μm ; [S IV] 10.5 μm ; [Ne II] 12.8 μm ; [Ne III] 15.6 μm ; and [S III] 18.7 μm . We thus concentrate on the broad bands of observed emission (Gillett et al. 1973); these are often referred to as the unidentified infrared (UIR) bands and we use that term henceforth.

It has been proposed that the UIR bands are vibrations of polycyclic aromatic hydrocarbons (PAHs; Duley & Williams 1981; Léger & Puget 1984; Allamandola et al. 1985) and this suggestion has been examined in considerable detail—see the review by Tielens (2008). However, the identification with PAHs is not completely secure. In part that is because there is no predictive theory for the shapes or relative strengths of the observed bands. This means that if the emission from H_6^+ lies within these bands then it will be difficult to place tight constraints on the abundance of the isotopomer in question.

First we compare the Orion spectrum with our results for the H_6^+ isotopomer, restricting attention to the five lines whose frequencies we can predict with confidence. Overall we see no clear correlation between the data and our predictions for H_6^+ , in either bare or solvated forms. For bare H_6^+ mode 6 lies right on the strong 11.3 μm (885 cm^{-1}) band and for the solvated molecule this mode is less than 30 cm^{-1} from the band, so within the possible errors (see Section 3.2.1) both species yield a coincidence. It is more difficult to claim a coincidence with any of the other modes, either for solvated or bare H_6^+ . Unfortunately the data shown here do not extend shortward of 3 μm ; however, we are not aware of any strong emission bands in this region. The closest feature to modes 11 and 12 is thus the 3.3 μm emission band seen in the plot and this is so far removed from

the predicted lines that it is plainly not attributable to the H_6^+ isotopomer in either bare or solvated forms. Similarly, mode 10 is almost 200 cm^{-1} away from the nearest strong emission band at 6.2 μm .

Translating the lack of spectral coincidences into limits on the H_6^+ abundance requires information which we do not yet have. However, it is fair to say that the data in Figure 5 give no reason to think that the H_6^+ isotopomer is abundant in interstellar space. Although the data shown in that figure are an example of a “Type A” spectrum, we would have reached the same conclusion if we had compared our results to a Type B or Type C spectrum as these differ from Type A mainly in respect of the relative strengths and shapes of the various bands, rather than in their placement (Peeters et al. 2002; van Diedenhoven et al. 2004). It remains possible that spectral coincidences could be found in other sorts of data—see the discussion of absorption spectra in Section 5.3.

The situation is quite different for $(\text{HD})_3^+$: Figure 5 shows a striking coincidence between the data and our predictions, especially for the solvated form. Coincidences are seen in the case of the emission bands at 3.3 μm (mode 12), 3.4 μm (mode 11), 6.2 μm (mode 10), 11.3 μm (mode 7), and 12.7 μm (mode 6). We emphasize that this accounts for all of the reliable mode predictions for $(\text{HD})_3^+$. There is no predicted mode coincident with the strong emission bands at 7.7 and 8.6 μm , but this is of no immediate significance since the remaining vibration modes, the *E*-type modes, are not good approximations to the eigenmodes of the actual $(\text{HD})_3^+$ molecule (Section 3.2.1). Notwithstanding the uncertain identification of the 7.7 and 8.6 μm emission bands, the excellent agreement between the data and the well characterized modes of $(\text{HD})_3^+$ prompts us to suggest that this molecule is responsible for the ubiquitous UIR bands.

5. DISCUSSION

Having suggested that $(\text{HD})_3^+$ is the carrier of the UIR bands we now need to consider the broader implications of that suggestion. For example, the UIR bands typically carry a significant fraction ($\sim 10\%$) of the total intensity seen on various lines of sight through our Galaxy (Onaka 2004), so their carrier must be contributing substantially to the extinction on these lines of sight. In this section we consider $(\text{HD})_3^+$ in the broader picture of ISM photo-processes. Readers who are unfamiliar with current models of interstellar dust may wish to consult Draine (2003) and the many papers in Witt et al. (2004). The following discussion is couched entirely in terms of $(\text{HD})_3^+$, even though the same physics would in most cases apply to the H_6^+ isotopomer.

5.1. Excitation Mechanism

In Section 3.2.2, we argued that excitation of the vibrational modes of $(\text{HD})_3^+$ is expected to occur as a result of absorption of ambient starlight. The two contributing processes were identified as electronic excitation and absorption in combination bands, with electronic excitation expected to dominate for highly solvated forms. Some insight into the excitation process is available from the data in Figure 5 where we see that there are peaks at both 3.3 and 3.4 μm with the former being by far the stronger of the two. Our model of $(\text{HD})_3^+$ does indeed predict lines at approximately these locations – modes 11 and 12, respectively – but the ratio of calculated transition strengths is the opposite of that observed: mode 11 is more than 100 times stronger than mode 12. This suggests that if the observed

bands arise from $(\text{HD})_3^+$ then the excitation process is probably electronic. The reason is that the strength of a combination band in part reflects the strength of the individual transitions involved in that combination, so if these modes were excited by absorption in combination bands then we would expect that mode 11 would be the stronger of the two lines. By contrast, if the excitation is electronic then the population of the excited vibrational levels is determined by the Franck–Condon factors and is unrelated to the transition strengths of the modes. It seems probable that the Franck–Condon factors would favor excitation of mode 12. The reason is that mode 12 is a symmetric vibration mode, whereas mode 11 is antisymmetric. The Franck–Condon factors reflect the distortion in the molecular PES which occurs as a result of the electronic excitation, and for the low-lying electronic excitations those distortions will be predominantly symmetric.

5.2. Relationship to FIR

In this paper we have concentrated on the vibration modes of $(\text{HD})_3^+$ itself. But the solvated form has in addition a large number of vibration modes which we have thus far ignored. For example, in the case of icosahedral solvation with a single shell, i.e., $(\text{HD})_3^+(\text{H}_2)_{12}$, we would expect a total of 84 modes, whereas $(\text{HD})_3^+$ has only 12. Extrapolating from the behavior seen for low degrees of solvation (Kurosaki & Takayanagi 1998b) we expect that a complex with a single icosahedral shell would exhibit 12 high-frequency modes, close to the vibration frequency of unperturbed H_2 , and 60 low-frequency modes, in addition to the modes common to bare $(\text{HD})_3^+$. If solvation extends to a second complete icosahedral shell, i.e., $(\text{HD})_3^+(\text{H}_2)_{12}(\text{H}_2)_{42}$, then we expect there to be 270 low-frequency vibration modes attributable to the solvation.

Following electronic excitation of the solvated complex, courtesy of an absorbed photon, it is probable that many of the low-frequency modes will be excited because the lowest-lying electronic excitations are likely to be spread over the whole complex. Thus if $(\text{HD})_3^+$ is responsible for the UIR bands then we expect that far infrared (FIR) emission will accompany them. Because of the large number of modes crammed into a relatively small emission bandwidth, the FIR emission may appear as a quasi-continuum if the degree of solvation is high.

FIR emission is indeed observed to accompany UIR band emission and in fact there is generally observed to be far more power in the FIR than in the UIR bands (e.g., Onaka 2004). In a model which seeks to attribute the observed FIR power to solvated $(\text{HD})_3^+$ that would imply that the majority of the observed interstellar extinction must be attributed to absorption by $(\text{HD})_3^+$.

5.3. Absorption Spectra

If $(\text{HD})_3^+$ is present in interstellar space then it should manifest itself in absorption as well as emission. The relative strengths of the infrared vibrational lines may differ greatly between these two processes. Absorption-line strengths just reflect the oscillator strengths of the transitions (assuming the molecule is in the vibrational ground state). These mode intensities are given in Table 1 and plotted in Figure 3. Thus we see, for example, that in absorption the $3.4 \mu\text{m}$ line of $(\text{HD})_3^+$ is expected to be much stronger than the $3.3 \mu\text{m}$ line, whereas in emission

the $3.3 \mu\text{m}$ band is observed to be more intense. In practice it is unusual to see any of the UIR bands in absorption, so there is not much data to compare our results with. However, there is sometimes an absorption band seen at $3.4 \mu\text{m}$ with no detectable $3.3 \mu\text{m}$ absorption accompanying it (Pendleton 2004). Conventionally this band is interpreted in terms of aliphatics—long-chain hydrocarbon molecules, very different to the polycyclic species which are usually invoked to explain the other UIR bands.

We are not aware of any other interstellar absorption bands coincident with our mode predictions for $(\text{HD})_3^+$. However, as our predictions match the locations of the observed UIR emission bands it seems unlikely that this situation presents any particular difficulty for interpreting the UIR emission in terms of $(\text{HD})_3^+$.

Looking again at Figure 3, but this time at the predictions for the H_6^+ isotopomer, we see that the only strong absorption lines expected for that molecule are at $9.6 \mu\text{m}$ and $3.0 \mu\text{m}$ —coincident with known bands of strong interstellar absorption. These bands are usually attributed to amorphous silicates and to water ice, respectively (Draine 2003; van Dishoeck 2004). It is beyond the scope of this paper to construct an astrophysical model in which these absorption bands are interpreted in terms of H_6^+ ; here we simply note the spectral coincidences.

We have already noted that the optical absorption spectrum of solvated H_6^+ is probably dominated by electronic excitations (Section 3.2.2) and that this expectation is reinforced by the data in Figure 5 (Section 5.1). We are unable to calculate the electronic absorption spectrum, but we can give a qualitative description as follows.

The large number of vibrational modes possessed by a single solvated molecule means that we can expect to see a very large number of absorption lines. Taking the bare molecule, for example, there are 12 modes of vibration. Assuming the Franck–Condon factors favor only two different quantum states for each mode gives us $2^{12} \sim 4000$ different vibrational states and the same number of absorption lines. For the solvated species this number is, of course, vastly greater: for a single icosahedral shell, i.e., $(\text{HD})_3^+(\text{H}_2)_{12}$, it is $\sim 10^{25}$. Given that the binding energy of the clusters is only about 2.2 eV in the ground electronic state (Kurosaki & Takayanagi 1998b), the spacing between individual lines is expected to be typically very small so that they create, in effect, a continuum absorption.

Individual absorption lines should nevertheless be detectable because the large number of vibration modes also leads to a large dynamic range in line strength. For example, if we assume, as before, that the Franck–Condon factors favor only two different quantum states in each mode, but that one of these states has typically twice the Franck–Condon factor of the other, then the intensity ratio between the strongest and weakest lines is of order the total number of lines.

All of the foregoing arguments apply equally well to any bound, excited electronic states. It is likely that there will be a number of such states and this correspondingly multiplies the number of possible absorption lines.

An unusual aspect of $(\text{HD})_3^+$ is its high levels of anharmonicity. One result of this is that in any vibrational sequence the level spacings are not uniform. Thus, even in cases where the Franck–Condon factor is large over a broad range of one vibrational quantum number, there will be no regular spacing in the corresponding sequence of absorption lines.

If we try to make a connection to the astronomical data then we are looking for correlated optical continuum and line

absorption phenomena in which the optical lines are unidentified. We therefore consider the possibility of a connection to the diffuse interstellar bands (DIBs). The properties of DIBs have been reviewed by Herbig (1995) and Sarre (2006), for example. Their phenomenology is rich and we do not attempt a detailed assessment vis-à-vis $(\text{HD})_3^+$ absorption; instead we confine ourselves to the following points. First, DIBs are known to correlate well with optical continuum absorption, as gauged by reddening. Second, DIBs are concentrated in the optical band, consistent with a carrier that has a small binding energy. Third, although there have been suggestions of regularities in DIB spacings (notably, Herbig 1988), with the best available data it appears that there are no statistically significant regularities in line spacing for intervals smaller than 400 cm^{-1} (Hobbs et al. 2008, 2009). This is consistent with absorption by a floppy molecule.

Finally, the lack of very strong correlations among the various DIB strengths, measured on different lines of sight (McCall et al. 2010; Friedman et al. 2011), is a puzzling feature of the data, but it can be understood in the context of an absorption spectrum in which any individual absorption line represents a minuscule fraction of all the absorptions, as we expect for solvated $(\text{HD})_3^+$. This is because that fraction will depend on the smallest details of the wave functions of the ground- and excited-states and the dependencies will be different for each absorption line. Branching ratios may therefore exhibit a strong environmental dependence.

We also note that DIB strength is known to correlate with the column density of atomic hydrogen, not molecular hydrogen (Herbig 1993; Friedman et al. 2011). At first sight this might seem to argue against $(\text{HD})_3^+$ being the carrier, given its intimate association with solid molecular hydrogen. However, the correlations are determined using measurements that are sensitive to diffuse gas and insensitive to precipitates. Furthermore it is possible that the diffuse atomic hydrogen could actually arise from photodissociation of H_2 which is itself undetected (Allen & Diaz-Miller 2004).

Finally we recall that $(\text{HD})_3^+$ resides in a matrix of solid H_2 , which contributes absorption, as do the H^- ions which we expect are also present (Section 2.5). The electronic transitions which make up the Lyman and Werner bands of H_2 are very strong and they are expected to introduce high levels of absorption in the far ultraviolet (FUV). This is qualitatively consistent with the observed rapid rise in extinction toward the FUV (e.g., Fitzpatrick 2004). Although the properties of the Lyman and Werner transitions have been well studied in the gas phase of H_2 (Abgrall et al. 1993a, 1993b), we are not aware of any studies of their appearance in the condensed phase. Similarly, we are not aware of any studies of the properties of H^- in a solid hydrogen matrix. Quantitative estimates of their contributions must therefore be deferred.

5.4. Red Fluorescence and the ERE

In Section 2.2, we noted that irradiated solid hydrogens are seen to fluoresce in the far red and near infrared. This fluorescence may be of interest in an astrophysical context as a possible explanation for the extended red emission (ERE) which has been observed from various types of nebulae and the broader ISM—see Witt & Vijh (2004) for a review of the ERE phenomenon. With reference to the requirements on the ERE carrier listed by Witt & Vijh (2004) we note the following points of similarity between the two phenomena: (1) the spectral peaks occur in similar places, (2) the spectra are similarly broad, unstructured and confined to similar wavelength ranges, (3) both

are photoluminescence phenomena, and (4) the ERE arises from an abundant element with Galaxy-wide distribution. There is no doubt that hydrogen is an abundant element with a Galaxy-wide distribution. We do not yet know if it is found in solid form in astrophysical contexts, but if it is then it would be a strong candidate for the carrier of the ERE.

6. CONCLUSIONS

It is remarkable that a single, small hydrogen molecule exhibits most of the strong mid-IR bands which pervade astronomical environments. This fact alone makes $(\text{HD})_3^+$ of interest to astronomers, even though we cannot yet place it in our theoretical picture of the ISM with any degree of confidence. The 7.7 and 8.6 μm astronomical bands, which are often the strongest of all the observed UIR features, are absent from our predictions for $(\text{HD})_3^+$, but there are several vibrational modes which we are unable to characterize, leaving open the prospect that some of those modes are responsible for the bands in question.

Inside a matrix of solid hydrogen, $(\text{HD})_3^+$ is solvated and the many weak bonds in the resulting cluster are expected to give rise to a large number of FIR vibrational transitions. Like the mid-IR bands, these cluster modes will be excited following electronic absorption of optical photons, and we expect a correspondingly close relationship between mid-IR and FIR emissions from the solvated $(\text{HD})_3^+$ molecule.

We are unable to compute the electronic absorption spectrum of solvated $(\text{HD})_3^+$ because it is sensitive to the details of the solvation, but the floppy nature of the molecule leads us to expect line properties which are broadly consistent with those observed for the DIBs. The multitude of weak lines yields an apparent continuum of optical absorption.

To these phenomena one can add FUV absorption contributed by the solid hydrogen matrix itself and a red fluorescence, possibly attributable to H^- . Thus, in an astronomical context, solid hydrogen is expected to manifest itself in a variety of ways, each of which seems to resemble one of the observed astronomical phenomena collectively attributed to “dust.” We conclude that serious consideration should be given to the possibility that solid H_2 is abundant in the ISM.

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APPENDIX

ISOTOPIC VARIANTS OF H_6^+

In Section 2, we noted that the dominant isotopomer of H_6^+ in astrophysical environments is usually either H_6^+ or $(\text{HD})_3^+$. In the laboratory, however, conditions may be chosen which favor different isotopomers. Here we tabulate properties of the ten

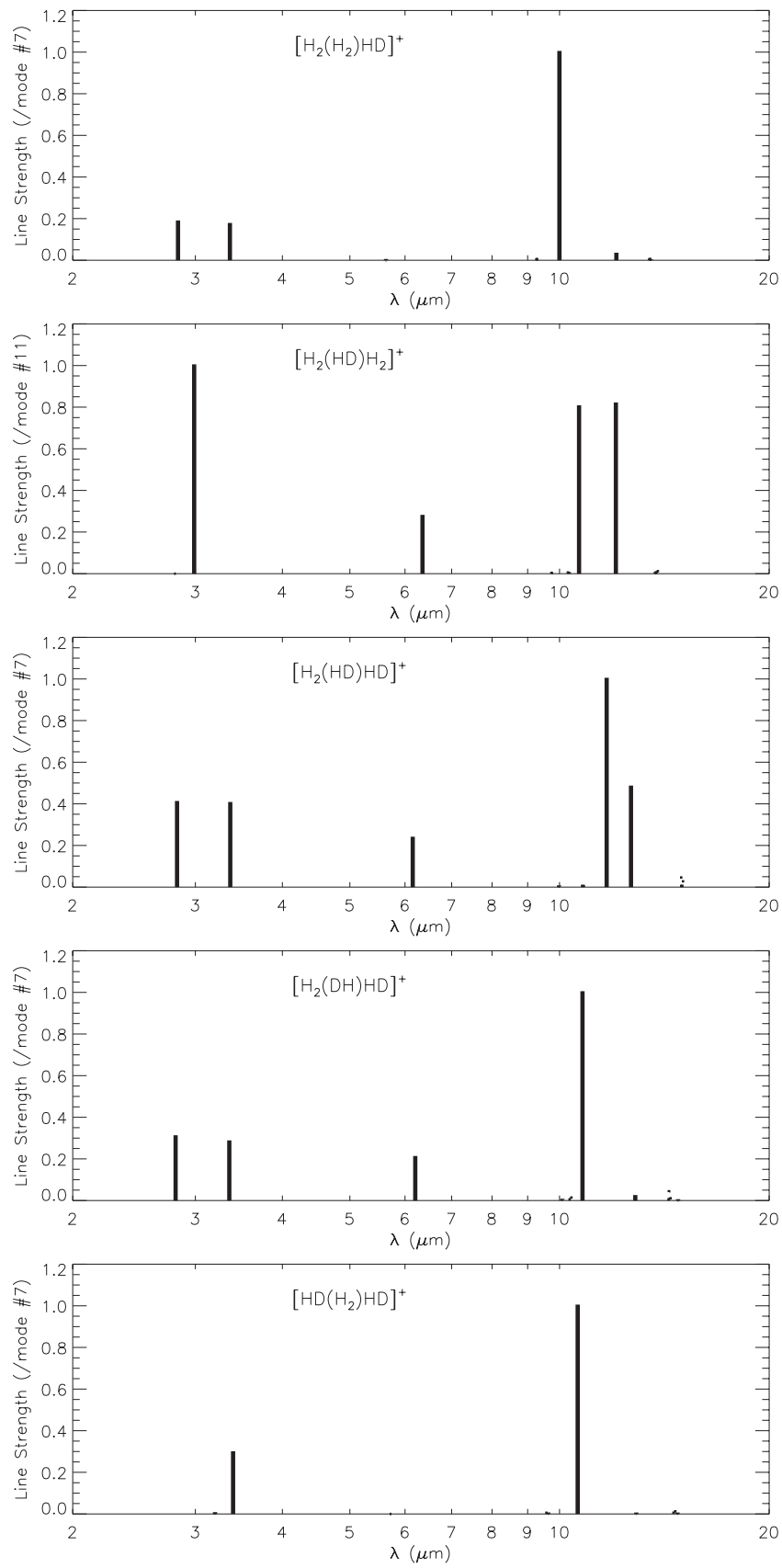


Figure A1. Stick diagram of the mid-IR lines of five isotopomers of H_6^+ . The line strengths are normalized to that of mode 7 or 11 for each molecule. The E -type modes of the D_{2d} structure are not good approximations to the actual eigenmodes of the molecules (see Section 3.2.1) and they are therefore plotted with dotted lines.

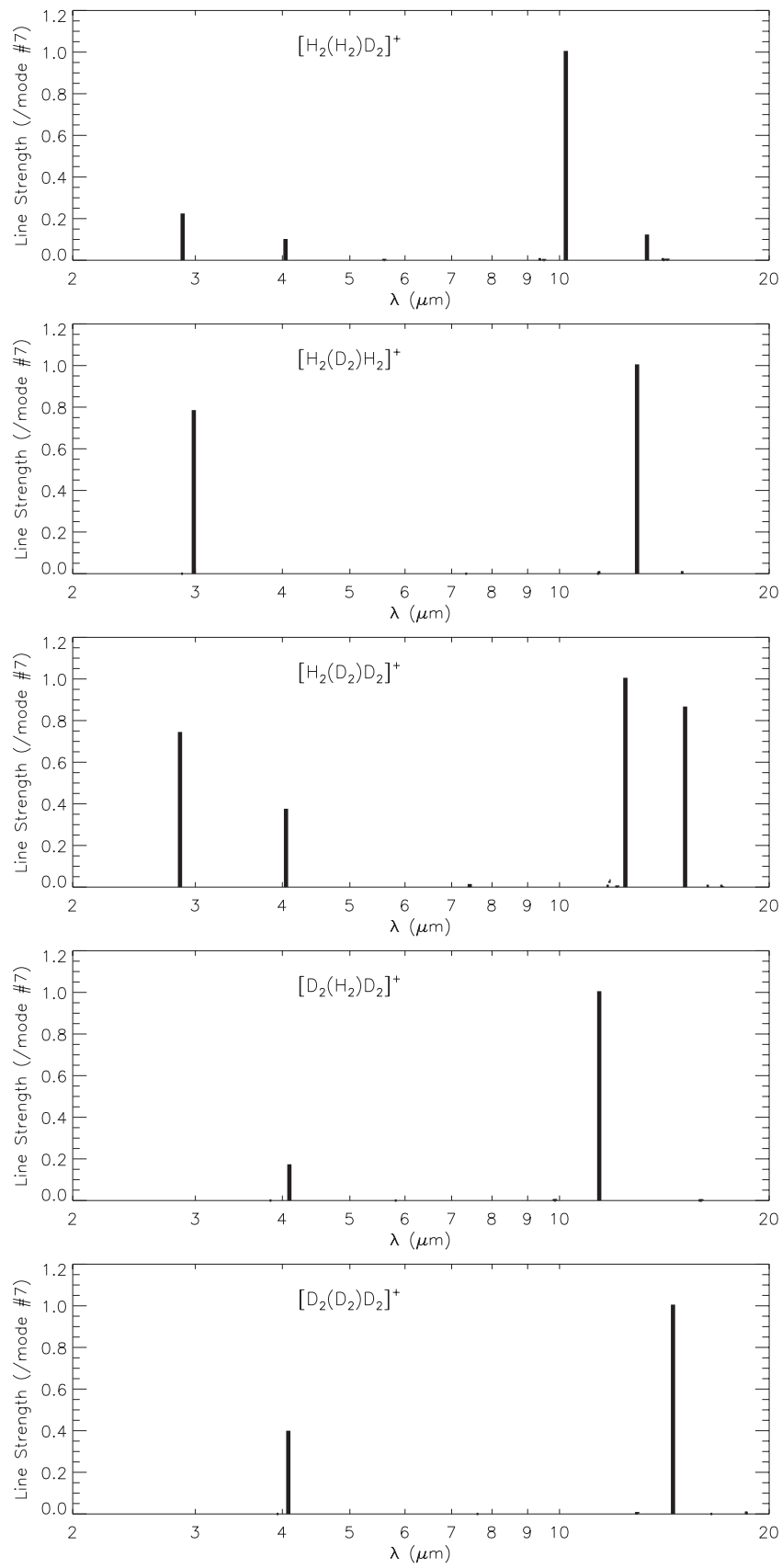


Figure A2. Stick diagram of the mid-IR lines of five isotopomers of H_6^+ . The line strengths are normalized to that of mode 7 for each molecule. The E -type modes of the D_{2d} structure are not good approximations to the actual eigenmodes of the molecules (see Section 3.2.1) and they are therefore plotted with dotted lines.

Table A1
Harmonic and Anharmonic Zero-point Vibration
Energies for Various H₆⁺ Isotopomers

Isotopomer	Harmonic ZPVE (meV)	Anharmonic ZPVE (meV)
[H ₂ (H ₂)H ₂] ⁺	1010.0	1000.9
[H ₂ (H ₂)HD] ⁺	964.5	955.3
[H ₂ (HD)H ₂] ⁺	962.3	952.7
[H ₂ (HD)HD] ⁺	916.6	906.2
[H ₂ (DH)HD] ⁺	915.9	907.5
[HD(H ₂)HD] ⁺	918.6	909.5
[HD(HD)HD] ⁺	869.9	860.7
[H ₂ (H ₂)D ₂] ⁺	913.6	905.8
[H ₂ (D ₂)H ₂] ⁺	912.3	903.2
[H ₂ (D ₂)D ₂] ⁺	813.9	807.3
[D ₂ (H ₂)D ₂] ⁺	815.9	810.2
[D ₂ (D ₂)D ₂] ⁺	714.4	709.8

Notes. Anharmonic corrections to the ZPVE were computed using Equation (A1) with Z_{kin} and ϕ_{ijk} terms neglected.

Table A2
Normal Modes of the D_{2d} Structure of H₆⁺ Isotopomers
Containing H₂ and HD Groups

Species	Mode No.	I_o (km mol ⁻¹)	ω_o (cm ⁻¹)	ν (cm ⁻¹)
[H ₂ (H ₂)HD] ⁺	12	422.7	3821.0	3530.2
	11	395.6	3307.9	2973.6
	10	0.6	2081.4	1774.8
	9*	8.2	1187.6	1076.4
	8*	13.7	1169.0	1074.3
	7	2282.6	1004.6	1000.3
	6	69.2	860.7	828.7
	5*	11.4	723.7	740.8
	4*	40.3	627.3	738.4
	3*	1.5	349.0	227.5
	2*	6.2	332.6	740.8
1*	2.2	92.9	170.6	
[H ₂ (HD)H ₂] ⁺	12	0.0	3858.0	3566.2
	11	992.2	3777.8	3346.5
	10	274.6	1842.6	1573.2
	9*	3.6	1104.6	1024.1
	8*	19.7	1020.9	970.0
	7	797.1	927.3	937.5
	6	810.5	862.1	830.0
	5*	14.9	725.7	724.6
	4*	24.8	660.7	724.6
	3*	2.9	325.0	727.5
	2*	3.0	320.2	211.2
1*	0.0	99.2	179.2	
[H ₂ (HD)HD] ⁺	12	431.3	3820.9	3541.4
	11	426.1	3306.2	2970.2
	10	249.8	1832.0	1624.8
	9*	2.8	1074.7	1001.6
	8*	22.5	1018.3	925.4
	7	1056.9	923.7	855.7
	6	509.2	805.4	789.5
	5*	12.4	723.5	664.3
	4*	56.1	566.8	666.8
	3*	1.0	313.4	202.9
	2*	3.2	307.5	175.4
	1*	1.8	92.8	145.8
	[H ₂ (DH)HD] ⁺	12	445.4	3819.9
11		409.7	3307.5	2979.5
10		301.1	1837.6	1611.3
9*		4.3	1103.3	990.7

Table A2
(Continued)

Species	Mode No.	I_o (km mol ⁻¹)	ω_o (cm ⁻¹)	ν (cm ⁻¹)	
[H ₂ (H ₂)H ₂] ⁺	8*	37.6	1002.3	964.4	
	7	1446.6	866.9	926.9	
	6	29.7	857.9	778.5	
	5*	21.6	658.1	694.7	
	4*	64.4	615.9	694.7	
	3*	0.8	314.6	675.7	
	2*	3.5	298.3	270.4	
	1*	1.4	92.7	163.0	
	[HD(H ₂)HD] ⁺	12	6.4	3343.6	3123.5
		11	677.2	3276.9	2942.5
		10	0.1	2075.5	1748.5
		9*	3.5	1167.6	1037.9
		8*	29.3	1166.3	1041.3
		7	2293.7	979.4	941.7
6		2.5	829.3	775.8	
5*		57.8	643.0	684.1	
4*		2.5	600.6	677.0	
3*		10.7	328.3	217.3	
2*		4.0	322.4	187.6	
1*		5.6	84.9	133.5	

Notes. Wavenumbers are given both with (ν) and without (ω_o) anharmonic corrections. Changes in rotational state of the molecule shift the lines away from these wave numbers. Modes marked with an asterisk are strongly affected by rotation of the end-groups, so these modes are not good approximations to the eigenmodes of the real molecule (Section 3.2.1).

Table A3
Normal Modes of the D_{2d} Structure of H₆⁺ Isotopomers
Containing H₂ and D₂ Groups

Species	Mode No.	I_o (km mol ⁻¹)	ω_o (cm ⁻¹)	ν (cm ⁻¹)
[H ₂ (H ₂)D ₂] ⁺	12	465.5	3819.2	3476.3
	11	205.2	2703.8	2474.5
	10	2.6	2075.0	1785.0
	9*	9.5	1185.8	1064.7
	8*	0.9	1153.5	1052.5
	7	2126.6	996.9	979.4
	6	250.3	760.0	749.0
	5*	9.5	721.4	708.7
	4*	2.2	581.4	708.7
	3*	4.2	341.2	699.7
	2*	2.2	310.5	248.2
1*	0.0	88.2	149.4	
[H ₂ (D ₂)H ₂] ⁺	12	0.0	3857.8	3483.6
	11	1039.1	3776.2	3350.8
	10	0.0	1521.4	1361.6
	9*	17.6	923.5	874.8
	8*	17.6	923.4	874.8
	7	1331.9	832.0	773.9
	6	0.0	880.3	880.7
	5*	16.1	648.1	665.0
	4*	16.1	648.0	664.6
	3*	9.4	303.4	182.9
	2*	9.4	303.4	184.0
1*	0.0	99.2	154.4	
[H ₂ (D ₂)D ₂] ⁺	12	504.5	3817.7	3506.9
	11	252.9	2700.8	2470.3
	10	6.1	1497.8	1345.7
	9*	21.7	920.8	850.3
	8*	1.5	846.7	826.1
	7	682.0	852.2	804.4

Table A3
(Continued)

Species	Mode No.	I_o (km mol ⁻¹)	ω_o (cm ⁻¹)	ν (cm ⁻¹)
	6	587.7	690.0	660.2
	5*	9.8	640.8	610.9
	4*	12.1	520.3	583.7
	3*	1.9	283.5	240.9
	2*	2.0	270.7	164.0
	1*	0.0	88.2	122.9
[D ₂ (H ₂)D ₂] ⁺	12	0.0	2730.1	2600.0
	11	390.6	2677.7	2443.0
	10	0.0	2063.6	1718.6
	9*	2.1	1149.0	1015.2
	8*	2.1	1149.0	1015.2
	7	2321.7	927.9	876.9
	6	0.0	648.7	629.2
	5*	0.5	574.9	626.2
	4*	0.5	574.8	625.9
	3*	9.6	297.5	223.9
	2*	9.6	297.4	224.5
	1*	0.0	70.1	98.5
[D ₂ (D ₂)D ₂] ⁺	12	0.0	2729.2	2540.4
	11	477.0	2673.3	2451.7
	10	0.0	1476.6	1311.5
	9*	3.5	841.4	773.7
	8*	3.5	841.4	773.7
	7	1210.3	720.2	687.2
	6	0.0	641.6	605.3
	5*	6.8	513.6	537.9
	4*	6.8	513.6	537.7
	3*	0.1	252.0	213.6
	2*	0.1	252.0	214.0
	1*	0.0	70.1	85.6

Notes. Wavenumbers are given both with (ν) and without (ω_o) anharmonic corrections. Changes in rotational state of the molecule shift the lines away from these wave numbers. Modes marked with an asterisk are strongly affected by rotation of the end-groups, so these modes are not good approximations to the eigenmodes of the real molecule (Section 3.2.1).

isotopomers which, in addition to H₆⁺ and (HD)₃⁺, arise in solids made from mixtures of H₂ with HD or D₂.

In Table A1, we list the zero-point vibration energies (ZPVEs) of all these isotopomers. These values for the ZPVE include anharmonic corrections, treated as a perturbation according to (Schuurman et al. 2005)

$$\begin{aligned} \text{ZPVE} = & \frac{1}{2} \sum_i^{3N-6} \omega_i - \frac{1}{32} \sum_{ijk}^{3N-6} \frac{\phi_{iik}\phi_{kjj}}{\omega_k} \\ & - \frac{1}{48} \sum_{ijk}^{3N-6} \frac{\phi_{ijk}^2}{\omega_i + \omega_j + \omega_k} + \frac{1}{32} \sum_{ij}^{3N-6} \phi_{iij} + Z_{kin}, \quad (\text{A1}) \end{aligned}$$

where the various ϕ 's are the mode-coupling constants, given by

$$\phi_{ijk} = \frac{\eta_{ijk}}{\sqrt{\omega_i \omega_j \omega_k}}, \quad (\text{A2})$$

and similarly for the quartic constants. We have not evaluated the three-mode coupling coefficients (ϕ_{ijk} , see Section 3.2) and so we ignore the third term on the right-hand side of Equation (A1). We also ignore the last term (Z_{kin}), associated with rotation, as here we are treating mode 1 as a vibration on a par with the other modes.

To determine whether or not isotopic condensation occurs it is also necessary to know the ZPVE for H₂ and HD or D₂. From Table 39 in the appendix of Herzberg (1950) we find ZPVE(H₂) = 268.8 meV, ZPVE(HD) = 233.7 meV, and ZPVE(D₂) = 191.4 meV.

In Tables A2 and A3, we list the wave numbers and intensities of the normal vibrational modes of 10 isotopomers to complement the results for H₆⁺ and (HD)₃⁺ given in Table 1. Likewise the plots in Figures A1 and A2 complement those in Figure 3. The theoretical modeling is as described in Section 3. We remind readers that the line intensities reported here are computed in the harmonic approximation, even though we have calculated anharmonic corrections for the frequencies of the lines. All transitions in Tables A2 and A3 are $\nu = 1 \leftrightarrow 0$, for the mode in question, and rotation is neglected. The notation for an isotopomer consisting of End₁, Center, and End₂ moieties is [End₁(Center)End₂]⁺.

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