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Whispering-gallery mode resonators for highly unidirectional laser action

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Optical microcavities can be designed to take advantage of total internal reflection, which results in resonators supporting whispering-gallery modes (WGMs) with a high-quality factor (Q factor). One of the crucial problems of these devices for practical applications such as designing microcavity lasers, however, is that their emission is nondirectional due to their radial symmetry, in addition to their inefficient power output coupling. Here we report the design of elliptical resonators with a wavelength-size notch at the boundary, which support in-plane highly unidirectional laser emission from WGMs. The notch acts as a small scatterer such that the Q factor of the WGMs is still very high. Using midinfrared ($\lambda \sim 10 \mu\text{m}$) injection quantum cascade lasers as a model system, an in-plane beam divergence as small as 6 deg with a peak optical power of $\sim 5 \text{ mW}$ at room temperature has been demonstrated. The beam divergence is insensitive to the pumping current and to the notch geometry, demonstrating the robustness of this resonator design. The latter is scalable to the visible and the near infrared, thus opening the door to very low-threshold, highly unidirectional microcavity diode lasers.

Following the first description of the whispering-gallery mode (WGM) phenomenon in the acoustic regime by Lord Rayleigh in London's St Paul's Cathedral (1) and its subsequent analysis in terms of guided surface waves by Raman and Sutherland (2), its study was later extended to the radiofrequency (3) and optical domains (4) through the investigation of the ionosphere and solid spheres, respectively. WGMs were later investigated in liquid droplets (5) and microdisk diode lasers (6), opening a previously undescribed direction in photonics technology. WGM resonators offer great promise for investigation in the physical sciences (6–8), and applications of these devices have spanned a wide range from unique laser sources (9) and dynamic filters in communications (10) to sensors (11). One drawback, however, is that, in rotationally symmetric cavities (6, 12), WGMs can only be coupled out inefficiently and isotropically through scattering of evanescent waves by surface roughness or diffraction losses when the radius of curvature is comparable to the wavelength (9).

Previously, this problem was addressed through evanescent coupling using prisms (13), in-plane waveguide (14), or tapered fibers (15). The technique of using tapered waveguide (16) for coupling high Q WGMs out of cavities is quite successful for the study of fundamental cavity physics; however, it requires careful alignment and the devices are relatively sensitive to mechanical vibrations or other variations in the surrounding environment, which limit its usage for practical applications such as achieving microcavity lasers with directional emission. Another approach is to break the rotational symmetry by using deformed optical microcavities to increase the directionality of emission and power collection efficiency (17, 18), which has the advantage of easy and robust fabrication. The most successful designs include quadrupolar shaped lasers (19, 20) and spiral-shaped lasers (21, 22). However, all deformed microcavities studied in the literature have the problem that the Q factor degrades significantly as the deformation increases (23); in most of the cases WGMs are no longer supported in the cavity. Recently,

a Limaçon-shaped microcavity (24) was proposed to improve directionality and was soon demonstrated experimentally in the midinfrared (25, 26) and near-infrared spectral regions (27, 28). The far-field divergence angle of the main lobe of these devices, however, is about 30 or more degrees and side lobes persist. Here, we demonstrate highly unidirectional laser action, with FWHM beam divergence angle of $\sim 6 \text{ deg}$, from WGMs in elliptical-shaped quantum cascade laser (QCL) microcavities with a wavelength-size notch at the boundary. For resonator aspect ratios near the optimum for low beam divergence, the latter is insensitive to variations in notch size and in pumping current, proving the robustness of the design.

Results and Discussion

We chose an elliptical resonator because it possesses WGMs with very high Q factors (29) for shapes with various long-to-short aspect ratio Y/X . A notch of size comparable to the wavelength in the material, suitably defined on the boundary, will diffract light toward the opposite boundary. Fig. 1*A* illustrates how the aspect ratio Y/X of the elliptical resonator (blue curve) was optimized to achieve maximum collimation. The notch is located at the intersection of the short axis and the boundary (point O). In order to achieve collimation of the majority of the light scattered by the notch, we exploit a well-known property of the ellipse: For any given refractive index $n > 1$, one can find an ellipse (auxiliary ellipse) such that all incoming parallel rays are collected into one of its foci (30); conversely in the reciprocal process light emerging from the left focus of the auxiliary ellipse in Fig. 1*A* is refracted by its *right half-side* into parallel rays. Note that the notch is located at one of the foci of the auxiliary ellipse (red dashed curve), but not at the focus of the elliptical resonator. The Y/X ratio of the elliptical resonator is now chosen such that its boundary best (i.e., over the largest possible angle 2θ) approximates that of the auxiliary ellipse.

In quantitative terms, let $r(\theta)$ be the distance between some point on the resonator boundary and point O, and $R(\theta)$ the distance between a corresponding point on the auxiliary ellipse and point O. Maximizing the range of angles θ where $R(\theta)-r(\theta)$ is negligible (here we set $|R(\theta)-r(\theta)|/R(\theta) \approx 1\%$ corresponding to the accuracy of fabrication), we find $\varepsilon \equiv Y/X$ is ~ 1.2 for a refractive index $n_{\text{eff}} = 3.2$ for the laser material we used in the experiment

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The authors declare no conflict of interest.

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out of the cavity through the notch. The two weak side peaks at positions b and c in Fig. 2B (corresponding to the two far-field peaks near ± 120 deg in Fig. 2D), respectively, originate from a certain amount of light reflected toward b and c from different directions than from the notch, similar to the origin of the side peaks in TM Limaçon microcavity (see figure 3 in ref. 24 for elaboration). Higher-radial-order, lower Q factor, WG-like modes are also present (*SI Text*). Although the proposed scheme is demonstrated in a regime where the ratio of cavity size to wavelength in material $X/\lambda_{\text{eff}} \sim 26$ is relatively high, simulations show that the smallest notched-elliptical resonators with directional emission correspond to $X/\lambda_{\text{eff}} \sim 3$.

Simulations (*SI Text*) demonstrate that the far-field profile of transverse electric (TE) polarized modes is also highly directional, implying that the proposed concept is broadly applicable also to diode lasers operating in the near infrared and visible. The Q factor of the whispering-gallery modes is still very high in these structures for the same wavelength-to-size ratio. At relatively short wavelengths, e.g., $\lambda \sim 1 \mu\text{m}$, free carrier absorption is negligible and optical losses are small (33) ($\sim 0.5 \text{ cm}^{-1}$), limited by sidewall roughness of the cavity, and material absorption. This will lead to a much smaller Q-factor degradation than that at mid-IR wavelengths (optical loss is $\sim 15.6 \text{ cm}^{-1}$ for our QCLs). Thus we expect notched-elliptical resonators to be excellent for low-threshold, highly directional microcavity diode lasers. In support of this also note that for the same high Q ($\sim 1 \times 10^6$) Limaçon-shaped microcavity design (24), a Q factor of $\sim 2 \times 10^4$ was experimentally obtained for diode lasers emitting at $\lambda \sim 1 \mu\text{m}$ (28) as compared to $\sim 1,000$ of mid-IR QCLs (26).

Note that an optical mode with a calculated very high Q factor of $> 5 \times 10^6$ does exist in the cavity (*SI Text*). It resembles the mode in Figs. 2A–C but with odd parity with respect to the short axis of the notched-elliptical resonator. However, due to its strongly reduced overlap with the notch, it has a much smaller output coupling than the even parity mode of Figs. 2A–C. In addition, due to the existence of unavoidable material optical losses, both odd and even parity modes start to lase at almost the same pumping current in experiments. Therefore, the odd parity mode is not observed in the far-field profile measurement but is visible in the measured spectra (as seen in Fig. 3D) because

the spectrometer helps discriminate this weak signal from the background at low pumping currents.

Devices with different dimensions and notch sizes were fabricated and tested in pulsed mode operation at room temperature (*Materials and Methods*). Fig. 3A and B show, respectively, scanning electron microscope (SEM) images of a representative device and its vertical sidewall. Fig. 3C presents the light output power versus current (L-I) characteristics of this device. The measured Q factor of our devices is $\sim 1,260$, deduced from threshold current density and the gain coefficient measurements (32), which agrees well with the simulation value when the relatively high optical losses at the midinfrared wavelengths (32) ($\sim 15.6 \text{ cm}^{-1}$ for our devices, deduced from the measurements of threshold current densities versus cavity lengths of ridge laser devices) are included in the simulation. Thus for the QCL case, the threshold current density and Q factor of the notched-elliptical lasers are similar to those of Limaçon-shaped QCLs (25, 26), respectively, due to the high optical losses.

Fig. 3D presents the emission spectra of the notched-elliptical QCLs measured at different pumping currents. The laser operates in single mode at $\lambda \sim 10 \mu\text{m}$ near the threshold current (520 mA), corresponding to the mode with the highest Q factor ($> 5 \times 10^6$) with odd parity. At a pumping current of 750 mA, two sets of optical modes appear, indicated by blue and red arrows, corresponding respectively to the first two highest Q factor WGMs with even and odd parities. The average mode spacing of each set is approximately 5.80 cm^{-1} , which agrees very well with the calculated value of 5.85 cm^{-1} for both odd parity and even parity modes. At a higher pumping current several additional modes appear, indicated by green arrows, corresponding to lower Q factor type of modes as the one described in the *SI Text* (Fig. S1A).

The schematic and the 2D far field of the device are displayed in Fig. 4A and B, respectively. A much narrower beam divergence angle of 6 deg in the plane of the laser cavity than previously reported in microcavity (26) and Fabry–Perot ridge QC lasers is demonstrated. As the vertical far-field emission distribution (due to diffraction at the small light-emitting aperture in the vertical direction of the resonator) does not affect the characteristics of WGM in the plane of the resonator, such as the mode intensity

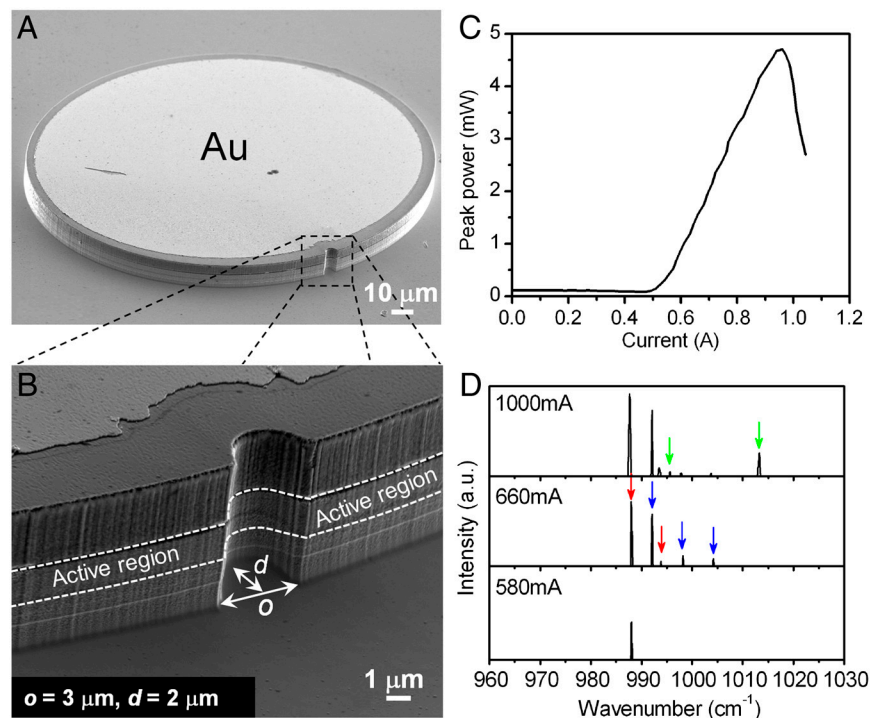


Fig. 3. Fabricated device and its electrical and optical characteristics. (A) Scanning electron microscope image of the notched-elliptical resonator with a minor radius $X = 80 \mu\text{m}$, a major radius $Y = 96 \mu\text{m}$, and notch dimensions $o = 3 \mu\text{m}$, and $d = 2 \mu\text{m}$. The top gold contact is deposited for electric pumping. (B) Zoom-in view of the device showing the smooth sidewall of the laser cavity. The two white lines indicate the boundaries of the active region. (C) Room temperature L-I characteristics of the device measured in pulsed mode operation with a duty cycle of 1%. A peak output power of $\sim 5 \text{ mW}$, a threshold current density $\sim 2.0 \text{ kA/cm}^2$, and a slope efficiency of $\sim 11 \text{ mW/A}$ were obtained. (D) The laser spectra of the device at different pumping currents. The threshold current of the laser is around 520 mA. At a pumping current of 750 mA, two sets of WGMs, indicated by the blue and red arrows, are present; at an even higher pumping current (1,000 mA), several additional modes appear, indicated by green arrows, corresponding to lower Q-factor modes.

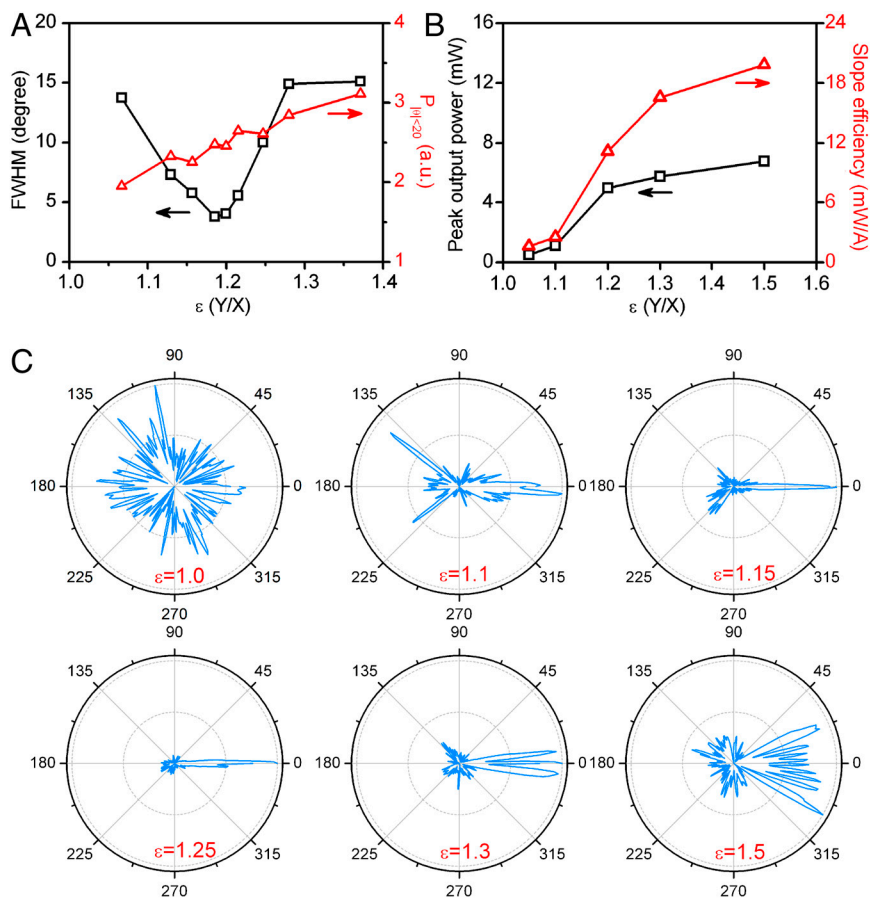


Fig. 5. Sensitivity of collimation. (A) Wave simulations of the directionality in terms of the FWHM and the optical output power within ± 20 deg $P_{|\theta|<20}$ versus ϵ of the devices for $X = 80 \mu\text{m}$, $o = 3 \mu\text{m}$, and $d = 2 \mu\text{m}$. When $\epsilon = 1.2$, the notched ellipse gives the best directionality while maintaining significant output power. The increase of the latter with larger ϵ is due to the fact that the effective lens aperture (right-hand-side boundary of the resonator) increases, collecting more light scattered from the notch. Simultaneously, the directionality of the far-field profile does not significantly increase for ϵ from 1.1 to 1.3. (B) Measured peak optical power and slope efficiency as a function of ϵ from various devices with the same $X = 80 \mu\text{m}$. The output power was collected with a power meter placed along the $\theta = 0$ direction with a collection angle of 100 deg. As expected, both the output power and the slope efficiency increase with increasing ϵ . (C) Experimental results of the far-field intensity profiles with ϵ in the range from 1.0 to 1.5.

Materials and Methods

Device Fabrication. We fabricated QCLs with different cavity sizes $X = 50, 80,$ and $110 \mu\text{m}$, and different axis ratio $\epsilon = 1.0, 1.1, 1.15, 1.2, 1.25, 1.3,$ and 1.5 . The QCL material is the same as the one used in ref. 26 designed at an emission wavelength $\lambda \sim 10 \mu\text{m}$. Devices with different notch sizes near the optimum and significantly away from the optimum were fabricated. Standard photolithography was used to define the contour of the laser cavity, shown in Fig. 3A, and the structure was etched through the gain medium using inductively coupled plasma reactive ion etching to obtain vertical and smooth sidewalls. Then, the top and back metal contacts (Ti/Au: 10 nm/200 nm) were deposited. A SEM image of the device sidewall (Fig. 3B) shows a roughness of about 300 nm, which gives minor scattering in the midinfrared wavelength range.

Simulations. Wave simulations for the cavities without considering gain were carried out by solving Maxwell's equations numerically using the boundary element method (24). Our simulations show that the shape of the notch does not play a significant role; therefore, a Gaussian shape was chosen as it is numerically convenient. In the simulations, the equation used to describe the boundary of the notched-elliptical resonator is $x = \{1/\epsilon - \delta \exp[-0.5(\phi - \pi)^2 / (0.25\theta^2)] \cos(\phi)\}$ and $y = \sin(\phi)$ in polar coordinates, where ϕ is the polar angle to the center of the notched ellipse; $\epsilon = Y/X$; $X = 80 \mu\text{m}$; δ and θ determine the depth d and width o of the notch. An effective refractive index $n_{\text{eff}} \approx 3.2$ for TM polarization is used in the simulations for $\lambda = 10 \mu\text{m}$ (λ is the

wavelength in free space), deduced from the measurement of the mode spacing of a Fabry–Perot-type ridge QCL fabricated from the same material that is used for the notched-elliptical resonators.

Measurements. The processed devices were electric pumped and tested in pulsed mode at room temperature with 125-ns current pulses at 80-kHz repetition rate. The far-field profiles of our devices were measured using a setup described in ref. 34. The tested device was mounted at the center of a motorized rotation stage with 0.5° resolution, and a midinfrared mercury–cadmium–telluride detector positioned 10 cm away from the devices was scanned the output of the laser. Power measurements were carried out with a calibrated power meter. Devices with a smaller size of $X = 50 \mu\text{m}$ exhibited continuous wave operation above cryogenic temperature (SI Text).

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