# DRENCH: A Semi-Distributed Resource Management Framework for NFV based Service Function Chaining

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Abstract—As networks grow in scale and complexity, the use of Network Function Virtualization (NFV) and the ability to dynamically instantiate network function instances (NFI) allow us to scale out the network's capabilities in response to demand. At the same time, an increasing number of computing resources, deployed *closer* to users, as well as network equipment are now capable of performing general-purpose computation for NFV. However, NFV management in the presence of Service Function Chaining (SFC) for arbitrary topologies is a challenging task.

In this work we argue for the necessity of an *algorithmic* resource management framework that captures the involved tradeoffs of NFIs minimum workload, load balancing, and flow path stretch. We introduce DRENCH as a low complexity NFV and flow steering management framework. In DRENCH a NFV market is considered where a centralised SDN controller acts as market orchestrator of NFV nodes. Through competition, NFV nodes make flow steering and NFI instantiation/consolidation decisions. DRENCH design enables third party NFV nodes participation while it can coexist with other NFV management solutions. DRENCH orchestrator parameterisation strikes the right balance between path stretch and NFI load balancing, resulting in significantly lower Flow Completion Times, up to  $10 \times$  less, in some cases.

#### I. INTRODUCTION

Middleboxes (MBs) are becoming ubiquitous in today's networks. MBs have typically been constructed from purposebuilt hardware, customized to perform specific tasks. Once setup, a network of MBs cannot alter its structure (e.g., topology) or (service) functionality (e.g., morph from one service to another). Network Function Virtualisation (NFV) [1] has been proposed to increase flexibility in the network, evolving MB architectures to virtual, or software-based services on top of commercial off-the-shelf (COTS) hardware. NFV promises to increase flexibility and achieve efficiency in using network resources, since both the structure and the (service) functionality of NFV nodes can be adjusted dynamically in response to service demand. Finally, Service Function Chaining (SFC), which determines the chain of NFV-based MB services a flow has to pass through, is gaining momentum as a necessary network process.

In order to exploit the full potential of virtualised Network Function Instances (NFIs), we argue that: *i*) NFIs have to be dynamically placed, replicated, instantiated and terminated (or consolidated), *ii*) new incoming flows have to be dynamically steered to the least-expensive NFI (in terms of current network and computation load), and *iii*) active, existing flows have to be redirected (if and when needed) to other instances of the same service in order to balance the load between NFIs of this service. Following this line of argument, we introduce and make the case for a resource management framework that dynamically handles NFIs and flow traffic, in order to load-balance i) network load in links and ii) computation load in NFV boxes. In designing such a resource management framework, we consider all potential options, that is, from centralized, software-based control plane approaches to decentralized, hardware-oriented data plane approaches. We find that a centralized controller can become the bottleneck when assigned with the task of making *real-time decisions* on service placement, instantiation, termination and flow steering/redirection. On the other hand, a purely distributed approach suffers from increased latency and overhead in order to exchange information between decision-making nodes, a process that also raises stability issues.

We argue for the need of a hybrid solution, where the (*log-ically*) centralised SDN controller performs lightweight tasks, related to the NFV environment coordination and flow settingup of state; while the *distributed network of NFIs* makes more frequent decisions, that impact flow latency. Despite the multiple SDN-NFV architectures proposed in recent years (*e.g.*, E2 [2], Stratos [3], Slick [4], SDNFV [5]), the problem of resource allocation and management in such environments has not received as much of attention.

In this paper, we propose a semi-<u>D</u>ist<u>R</u>ibut<u>E</u>d resource management framework for <u>NFV</u> based service function <u>CHaining</u> (**DRENCH**). DRENCH incorporates a traffic load-balancing algorithm that utilises dynamic estimation of NFI loads with each NFV node independently directing flows to an appropriate least-loaded service instance; DRENCH utilises a realtime service instantiation capability and redirects existing flows as necessary; DRENCH is applicable for an NFI based Service Function Chaining environment by using a centralised SDN controller to disseminate information among the NFV nodes in the network. DRENCH as a resource management framework can fit into most of the existing architectures, albeit with some modifications.

We realise DRENCH in the context of SDN-NFV architectures by defining a NFV nodes market environment. In particular, an SDN controller acts as the market orchestrator/regulator, assigning *prices* to NFIs which are indicative of their workload. At the same time, NFV nodes aim the increase of their 'income'; meaning, that NFV nodes aim to host popular NFIs that result in higher prices. In more detail, when the demand for a service increases (declines) the price of the service NFIs rises (decreases) accordingly, which in turn may drive NFV nodes to instantiate (consolidate the) NFIs of the corresponding service. In addition to NFIs instantiation/consolidation, each NFV node is also responsible for taking flow steering and redirection decisions.

In DRENCH the market orchestrator is setting the control parameters of *i*) *minimum NFI price* and *ii*) *off path penalty factor*. The minimum NFI price defines a threshold for consolidating NFIs whose prices are below the minimum one. Since NFIs' prices are representative of their workload, the minimum NFI price indicates the threshold below which an NFI is considered being under-utilised thereby controlling the number of active NFIs. On the other hand, the off path penalty factor controls the path-stretch of a flow in the context of SFC thereby penalising the choice of NFI that force the flow to deviate from its shortest path towards the destination. Considering Flow Completion Time (FCT) as an index of flow performance, DRENCH minimum NFI price (off path penalty factor) defines the tradeoff between under-utilised instances (flow path stretch) and FCT.

The main technical contributions of this paper involve:

- A feasible NFV management approach: in DRENCH resource management decisions are taken locally by NFV nodes while the market orchestrator solves lightweight problems, addressing a complex problem in an computationally feasible way with respect to *i*) path-stretch, *ii*) number of active NFIs per service, *iii*) load on each NFI and *iv*) flow completion time.
- A decoupled NFV resource management framework: in DRENCH NFV nodes do not have to be owned by the same entity, contributing in the incremental adaptation of NFV in arbitrary network topologies.
- Implementation and large scale evaluations: We prototyped DRENCH in Cloudlab testbed and Mininet to demonstrate that DRENCH is immediately deployable in an SDN environment. With Mininet, we compare DRENCH to a centralized approach Slick [4] on a 4K-Fat tree topology. Additionally, we compared DRENCH in a simulation environment consisting of a Rocketfuel topology (87 switches) to a custom centralized approach: Simplefying [6] on top of a E2 SDN framework [2]. Our results show that DRENCH is robust to: *i*) asymmetries caused by dynamics of arrival/departure of *elastic* flows with different service needs, and, *ii*) the instantiation/removal/failure of service instances (see Section VI).

## II. RELATED WORK

In the case of purely centralized solutions, the complexity (NP-hard in many cases) involved in the decision making for service instantiation and flow redirection results in a much coarser granularity of decision making. Solutions can only be based on heuristic-based approaches [7], or act on a perflow basis [8]. SIMPLE [6] relies on an offline Integer Linear Programming (ILP) solver to optimise the number of flow rules on the switches and an online Linear Programming (LP) solver for load balancing. However, SIMPLE [6] assumes that the NFIs and middleboxes are statically placed and any dynamic instantiation of NFIs requires the re-run of the expensive offline ILP solver. Slick [4] provides a programming model abstraction for service chaining and supports heuristic based function placement and flow steering schemes. Slick [4] also supports dynamic scaling of NFIs. However, it does not redirect the existing flows from the overloaded instances, but only steers the new flows to the scaled-out instances.

By and large, related works in this area have targeted only newly-arriving flows, while works such as Split/Merge [9] that address flow-redirection need to pause the existing flows for transferring VNF internal and forwarding states. On the other hand, purely distributed approaches for load balancing (e.g., TeXCP [10], CONGA [11]) face a different set of issues, such as: i) high overhead and latency: a large amount of information has to be exchanged among decision making nodes to synchronise their view of network state, with the consequent latency as the network scales; ii) complexity: achieving a stable synchronised view at every decision making node is complex; and iii) inefficiency and stability: since each node makes its decision based on its local view of the network state, packet loss, frequent rerouting, and transient loops are likely. In [12], authors employ the concept of shadow-prices to trade-off performance, QoS, and complexity, but they limit their scope only to address the flow steering in SFC.

**Framework:** OpenNF [13] provides the framework for control plane to make the decisions and migrate flows from NFI. It requires the events to be generated by NFIs and buffered at the controller for the interval of state migration. Stratos [3] provides an orchestration framework that employs rack-aware NFI placement strategy with horizontal scaling and migration of NFIs. The load/flow distributions are computed by an ILP formulation where only new flows are steered to the new instances while the existing flows continue to get processed at the same NFI, without alleviating the load on the already bottle-necked instance. E2 [2] is an NFV scheduling framework that supports affinity based NFI placement and dynamic scaling of NFIs. The framework tries to minimise the traffic across switches and load balance the traffic across NFIs, however it avoids flow redirections across hardware switches.

To the best of our knowledge, DRENCH is the first work that tackles both NFI placement and flow steering problems in arbitrary topologies; providing a computationally feasible algorithmic resource management framework inspired by the principles of market competition.

## **III. DESIGN OVERVIEW**

## A. Desired Properties

DRENCH is an in-network, congestion-aware, load balancing algorithmic framework for handling SFCs and dynamic NFIs in arbitrary network topologies. In designing DRENCH, we focus on providing the following key properties:

- **P1** Efficiency: As an NFI placement mechanism, DRENCH should neither under-utilise nor over-utilise the resources available in NFV nodes.
- P2 Cost awareness: DRENCH should instantiate the minimum NFIs to meet the requirements of the SFCs for

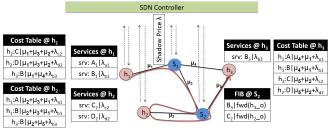


Fig. 1: DRENCH High-Level Operation

the flows through the network at any point in time, and balance the utilization across the active NFIs.

- *P3* Fine-grained flow handling: DRENCH must meet each flows' SFC functional requirements and meet end-to-end latency and minimum throughput requirements.
- *P4* **Responsiveness:** DRENCH should react to SFC traffic requirements, especially when traffic is volatile and bursty[14], [15], for arbitrary network topologies.
- **P5** Incremental deployability: DRENCH should require the minimum possible changes in terms of protocols and network infrastructure. It should also be applicable to any of the existing SDN architectures [2], [13], [5] with minimal changes. Further, it should be possible to directly apply DRENCH to a subset of available switches and of incoming traffic when necessary.

#### **B.** DRENCH Solution Overview

Our framework is designed to leverage the benefits of the centralised as well as the distributed networking paradigms. We use the **centralized approach**, *i.e.*, an SDN controller, to perform tasks with less computation load, but those that need to be carried out in a coordinated fashion across multiple nodes. These tasks include: i) gather, compute and disseminate NFI load information periodically to all the decision making entities; and *ii*) set up paths towards instances and egress nodes in case they do not already exist. Additionally, the SDN controller is used to decide which services are applicable to a flow (based on policies and/or flow characteristics). This design choice reduces the complexity of the controller and also overcomes the issues faced by a purely distributed approach, where the decision making entities might not have up to date information, thereby impacting performance. On the other hand, a distributed approach is used for decision making at individual NFV nodes. Based on the information provided by the controller, each node independently decides to i) steer flows towards the next required service; ii) redirect flows to the least loaded instance; and *iii*) instantiate/terminate service instances in order to adapt to demand. The high-level operation of the proposed mechanism is shown in Fig. 1.

#### **IV. DRENCH COMPONENTS**

DRENCH consists of the following components:

• Market Orchestrator: It associates every NFI and link resource to a *shadow price* (*i.e.*, cost) produced by utilising global information available at the controller. The orchestrator regulates the market by allowing the existence of instances above a certain minimum price.

G	Network Topology		
$\mathcal{V}$	Set of Switches		
ε	Set of Links		
$\mathcal{H}$	Set of NFV Nodes		
S	Set of Services		
$\mathcal{H}_s$	Set of NFV Nodes executing service s		
$\mathcal{F}$	Set of ENUM Flows		
$x_f$	Rate of Flow f		
$U_f(x_f)$	Utility Function of Flow $f$		
$b_e$	Bandwidth Capacity of Link e		
$a_{e,f}$	Coefficient = 1, if flow $f$ traverses link $e$		
$b_s^h$	Computational Resources of NFI $s$ at $h$		
$\begin{array}{c} b^h_s \\ \hline d^h_{s,f} \\ \hline d_s \end{array}$	Coefficient = $d_s$ if f is processed by NFI s at h		
$d_s$	Computational Power Required by NFI s		
	for processing a single bit of traffic		
$w_f$	Weight of flow f		
$\lambda_s^h$	Service Cost of NFI $s$ at NFV node $h$		
$\underline{\lambda}, \overline{\lambda}$	Minimum and Maximum shadow prices		
	defining the efficiency of an instance		
$p_{v_i,v_j}$	Shortest path from $v_i$ to $v_j$		
$\mu_{v_i,v_j}$	Communication Cost from $v_i$ to $v_j$		
$\begin{array}{c c} \mu_{v_i,v_j} \\ \hline \mathcal{C}_{v_i,h}(s) \end{array}$	Communication and service cost from switch $v_i$		
	to a NFI executing service $s$ an NFV node $h$		
$ p_{v_i,v_j} $	Number of Hops from $v_i$ to $v_j$		
$\begin{array}{c c}  p_{v_i,v_j}  \\ \hline \Delta p^f_{v_i,h} \end{array}$	Shortest path deviation overhead		
ρ	Off Path Penalty Factor		
$\frac{\rho}{\mathcal{C}^f_{v_i,h}(s)}$	Estimated $C_{v_i,h}(s)$ cost of flow $f$ including $\rho$		
$\theta_{rid}$	Redirection threshold		
$P_h$	Profit of NFV $h$ in terms of shadow prices		
$\widetilde{\lambda}_{on}, \widetilde{\lambda}_{off}, \widetilde{\lambda}$	On-/Off- path and expected competitive price		

TABLE I: DRENCH Notation Description

- Flow Steering and Redirection: This component steers each flow through a valid sequence of NFIs (according to its SFC) determined by the SDN controller. Steering and redirection takes into account latency, NFI and link costs.
- NFI Instantiation/Consolidation: This component instantiates and consolidates NFIs in a distributed way through the market competition between NFV nodes.

Below, we describe each of these components in detail.

## A. Market Orchestrator

DRENCH, as any market-based approach, requires the association of each network resource (commodity), in terms of NFIs and link bandwidth, to an offered price, which is imposed on a given set of incoming flows (demand) that utilise this resource. In particular, when the quantity of demanded resources equals the quantity supplied for a set of prices, we refer to them as *market-clearing prices*. DRENCH market-clearing prices should A1) be representative of each NFI's workload, A2) achieve the minimum possible convergence time, A3) not require additional in-network signalling given the existence of an SDN controller [16], [11]. Every price derivation violating requirement (A2) and (A3) would be in stark contrast with DRENCH desired properties *wrt* responsiveness (P4) and incremental deployability (P5), respectively.

DRENCH deploys a *Market Orchestrator/Regulator* component, which, by utilising only flow path information, already available at the SDN controller, efficiently derives

market-clearing prices that comply to requirements (A1)-(A3). Inspired by [17], where the authors formulate a Network Utilisation Maximisation problem (NUM) based on market principles to allocate bandwidth resources to a set of flows, we extend their model to include NFI computational resources. We achieve this by solving the Extended Network Utilisation Maximisation problem (ENUM) at the Market Orchestrator as we describe next.

We denote the network topology by  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ , of  $\mathcal{V}$ switches and  $\mathcal{E}$  links, where a set of NFV nodes,  $\mathcal{H}$ , is placed at a subset of switches  $\mathcal{H} \subseteq \mathcal{V}$ . Then, given a set of NFIs executing the set of S services, and a set of flows  $f \in \mathcal{F}$ , we associate each link,  $\forall e \in \mathcal{E}$ , with a bandwidth capacity  $b_e$ , and each NFI s at NFV node h with  $b_s^h$  computational resources, in order to form the ENUM problem that maximises the total utility of the system. Similar to NUM, we associate each flow rate,  $x_f \ge 0$ , with a utility that is a weighted logarithmic function,  $U_f(x_f) = w_f \log(x_f)$ , of weight  $w_f$ , capturing a decreasing marginal gain as the flow rate increases (i.e., lower rate flows cause bigger increase of the utility). In turn, we maximise the total system utility,  $\sum_{f \in \mathcal{F}} U_f(x_f)$ , subject to link capacity constraints,  $\sum_{f \in \mathcal{F}} a_{e,f} x_f \leq b_e$ ,  $\forall e \in \mathcal{E}$ , and computational resource constraints,  $\sum_{f \in \mathcal{F}} d_{s,f}^h x_f \leq b_s^h$ ,  $\forall s \in \mathcal{S}, \forall h \in \mathcal{H}$ ; where  $a_{e,f}$  is a coefficient equal to 1 if flow f traverses link e and 0 otherwise, while  $d_{s,f}^h$  equals the computational power required by service s for processing a single bit of traffic,  $d_s$ , if f is executed at NFI s of NFV node h, and 0 otherwise. Parameters  $a_{e,f}$  and  $d_{s,f}^h$  describe the path of each flow and therefore they are known to the SDN controller which provides them to the Market Orchestrator.

Since the objective function is differentiable and strictly concave, while the feasible region of the constraints is compact, the optimal rates  $x_f \forall f \in \mathcal{F}$  exist, are unique, and can be found efficiently by Lagrangian methods. Based on [17], it can be shown that the dual problem of the ENUM is:

maximise 
$$\sum_{f \in \mathcal{F}} w_f \log \left( \sum_{e \in \mathcal{E}} \mu_e a_{e,f} + \sum_{h \in \mathcal{H}} \sum_{s \in \mathcal{S}} \lambda_s^h d_{s,f}^h \right) - \sum_{e \in \mathcal{E}} \mu_e b_e - \sum_{h \in \mathcal{H}} \sum_{s \in \mathcal{S}} \lambda_s^h b_s^h$$
(1)

subject to

$$\begin{split} \mu_{e} &\geq 0, \; \forall e \in \mathcal{E}, \\ \lambda_{s}^{h} &\geq 0, \; \forall s \in \mathcal{S}, \forall h \in \mathcal{H}, \end{split}$$

where  $\mu_e$  and  $\lambda_s^h$  are the Lagrange multipliers of link *e* and service instance *s* at NFV node *h* respectively. The Lagrange multipliers are also known as *shadow prices*, due to their association to the optimal rates of each flow:

$$x_f = \frac{w_f}{\sum\limits_{e \in \mathcal{E}} \mu_e a_{e,f} + \sum\limits_{h \in \mathcal{H}} \sum\limits_{s \in \mathcal{S}} \lambda_s^h d_{s,f}^h}$$
(2)

where weight  $w_f$  is perceived as the budget that flow f is willing to pay for its rate, while the denominator is the cost imposed to the flow in order to use the resources along its path.

In that sense, *each Lagrange multiplier can be considered as the price of a particular resource*, leading us to the following definition about communication and service cost.

Definition 1: The communication cost between two switches,  $v_i, v_j \in \mathcal{V}$ , is the sum of on-path link shadow prices  $\mu_{v_i,v_j} = \sum_{e \in p_{v_i,v_j}} \mu_e$ , where  $p_{v_i,v_j}$  is the shortest path between switches  $v_i$  and  $v_j$ ; while the service cost of an instance s at NFV node h is the shadow price  $\lambda_s^h$ .

Note that the service and communication costs are kept in the forwarding tables of the NFIs, *i.e.*, the decision making nodes, and are updated periodically by the SDN controller after being estimated by the Market Orchestrator (see Fig. 1).

Shadow prices are indicative of the workload at a particular resource, complying with (A1). In fact, from (2), we derive that the value of a shadow price,  $\lambda$ , defines the maximum possible rate that flows using that resource can achieve,  $w_f/\lambda$ .<sup>1</sup> Based on the maximum achievable flow rate we can define the efficiency of a NFI as a range of shadow prices.

Definition 2: The Market Orchestrator determines the load of a NFI by a shadow price range  $[\underline{\lambda}, \overline{\lambda}]$ , where if a service cost,  $\lambda_s^h$ , is less/more than  $\underline{\lambda}/\overline{\lambda}$  the NFI is considered under/over-utilised, respectively.

Given the shadow price range  $[\underline{\lambda}, \overline{\lambda}]$  the Market Orchestrator tries to maintain the minimum required number of instances per service type (**P2**) by: *i*) terminating instances that are underutilised and *ii*) allowing for more instances for services whose existing instances are over-utilised (see Section IV-C).

## B. Flow Steering and Redirection

1) Flow Steering: Given a placement of NFIs and their respective shadow-prices, as determined by the Market Orchestrator, DRENCH's flow steering component is responsible for steering each new incoming flow towards the chain of required services. The flow steering component tries to route the flow through the chain that imposes the lowest possible cost to the flow. Determining the optimal end-to-end path of a flow through the SFC is a NP-complete problem [18]. DRENCH works on a hop-by-hop heuristic basis, picking each time the best next-hop NFI choice, in an effort to achieve instantaneous and adaptive steering decisions (**P4**).

We illustrate DRENCH's flow steering component through the following example. Assume that flow f arrives at the network requiring the execution of service s (or service chain  $s_1/s_2/.../s_m$ ) before being delivered to destination  $v_f$ . Let  $v_i$  be the switch that has to make a steering decision about f and  $\mathcal{H}_s \subseteq \mathcal{H}$  the set of NFIs of service s. Then the combined communication and service s execution cost at  $h \in \mathcal{H}_s$  is  $C_{v_i,h}(s) = \mu_{v_i,h} + \lambda_s^h$ . The DRENCH flow steering component initially estimates the shortest path deviation overhead applied by steering flow f to instance h in terms of hops,  $\Delta p_{v_i,h}^f = |p_{v_i,h}| + |p_{h,v_f}| - |p_{v_i,v_f}|$ , weighted by an off-path penalty factor  $\rho$ . Therefore, the estimated cost

<sup>&</sup>lt;sup>1</sup>It follows that the shadow prices are positive when a resource is totally utilised and 0 otherwise. To introduce a minimum workload to the resources that are not saturated, we add a set of *dummy flows* into  $\mathcal{F}$  when solving (1).

applied to the flow for executing service s at NFI of h is  $C_{v_i,h}^f(s) = C_{v_i,h}(s) + \rho \Delta p_{v_i,h}^f$ . Then,  $v_i$  selects the next service instance s of f that minimises  $C_{v_i,h}^f(s)$ :

$$h^* = \operatorname*{argmin}_{h \in \mathcal{H}_s} \mathcal{C}^f_{v_i,h}(s) \tag{3}$$

In Eq. (3) the off-path penalty factor,  $\rho$ , dis-incentivises node  $v_i$  from sending flow f away from its shortest path towards  $v_f$ . Eq. (3) applies on a hop-by-hop basis, that is, it is calculated at each NFV node responsible for forwarding flow f towards the next instance in its chain.

Lastly, upon making a steering decision, switch  $v_i$  informs the SDN controller that flow f is forwarded towards  $h^*$  to execute service s. At the same time, the SDN controller is setting up paths towards NFIs and/or egress nodes as necessary.

2) Flow Redirection of Stateless and Stateful flows: The cost of a service instance might change dramatically throughout the duration of a flow, rendering previous flow steering decisions outdated. Therefore, redirection of existing flows is necessary in order to keep the expenditure of existing flows at low levels (**P3-P4**) and avoid routing through overutilised instances (**P1**). We realise flow redirection as follows: if the cost difference between two instances of s at h and h', as seen by switch  $v_i$ , is bigger than a redirection threshold,  $\theta_{rid}$ ,  $C_{v_i,h}(s) - C_{v_i,h'}(s) > \theta_{rid}$ , switch  $v_i$  repeats the flow steering process for a portion of flows that  $v_i$  currently forwards to h. The redirection threshold is set to  $\theta_{rid} = \overline{\lambda} - \underline{\lambda}$ .

Rerouting of stateful flows to dynamically instantiated services to achieve optimal load balancing is usually complex and costly. For instance, solutions such as Split/Merge [9], pause ongoing flows in order to transfer internal NF and forwarding states. For the purposes of DRENCH, we rely on work like OpenNF [13] and Split/Merge [9]. We leverage the approach in Split/Merge [9], to pause ongoing flows and transfer internal NF state. To identify the service instances, we make use of the Information Centric Networking (ICN) construct which is proven to be beneficial in terms of providing flexible routing, and reducing the routing states at the switches [19].

#### C. Instantiation

In DRENCH, NFV nodes autonomously provide services and try to maximise their profit, in terms of *shadow prices* (*i.e.*, the cost to execute some service). In particular, let  $S_h$  be the set of NFIs at some NFV node h, then the profit of h in terms of *shadow prices*,  $\lambda_s^h$ , can be estimated, as:

$$P_h = \sum_{s \in \mathcal{S}_h} \lambda_s^h \tag{4}$$

DRENCH NFI instantiation/consolidation scheme defines how service demand and NFI *shadow prices* affect the individual NFV node decisions to manage the number of service instances. Through competitiveness, NFV nodes achieve responsiveness to NF demand changes, while the market orchestrator ensures market efficiency, as we explain next. 1) NFV Node Competitiveness: Let the shadow price of an NFI s' at NFV node h' be  $\lambda'$ . We are interested in estimating the competitive price of a potential NFI s at an NFV node h,  $h \neq h'$ , with respect to  $\lambda'$ .

Definition 3: The competitive price of NFI s is defined as the shadow price that renders the flow steering scheme to consider s to be at least as good as s'.

Then, let  $\mu$  be the communication cost, between NFV node h' and h that are  $\Delta p$  hops away, and f be a new flow that is about to get steered at NFI s'. Then according to DRENCH's flow steering component, the smallest possible competitive price at s for flow f, would be equal to  $\lambda_{off} = [\lambda' - \mu - \rho \Delta p]^+$ , where  $\rho$  is the off-path penalty factor. The off-path penalty factor is taken into account as in the worst case flow f will have to traverse  $\Delta p$  additional hops to reach s from s'.<sup>2</sup> This acts as a disincentive for some node to forward traffic to nodes that are far off from the flow's shortest path. On the other hand, in the best case, flow f is forwarded to NFV node h' by NFV node h, meaning that s is already on the path of flow f and additional hops are not required<sup>3</sup>. Hence, in the best case, the competitive price at s for flow f would be  $\lambda_{on} = \lambda' + \mu$ .

The expected competitive price of NFI s with respect to NFI s' price  $\lambda'$  will be a value between  $(\tilde{\lambda}_{off}, \tilde{\lambda}_{on})$ . Let y be the total amount of traffic with competitive price  $\tilde{\lambda}_{on}$ . Then y can be considered as the local information of NFI s' demand at NFV h that accounts for the utilization percentage  $d_{s'}y/b_{s'}^{h'}$ . Here,  $d_{s'}$  is the computational power required by the service of NFI s' for processing a single bit of traffic and  $b_{s'}^{h'}$  is the fixed computational resources that are allocated to NFI s'. Then the expected competitive price is estimated as:

$$\widetilde{\lambda} = (d_{s'}y/b_{s'}^{h'})\widetilde{\lambda}_{on} + (1 - d_{s'}y/b_{s'}^{h'})\widetilde{\lambda}_{off}$$
(5)

2) NFI Instantiation: As long as a NFI shadow price,  $\lambda$ , executing a service at NFV node h, is lower that the maximum target price,  $\lambda < \overline{\lambda}$ , this service is not considered over-utilised and an instantiation of an additional NFI of the same service at h is prohibited (see also *Definition 2*). On the other hand, if  $\lambda > \overline{\lambda}$ , the Market Orchestrator limits the number of NFI that can be created by competing the NFI with service cost  $\lambda$  to  $\lfloor \lambda/\overline{\lambda} \rfloor$ . Therefore, given the set of allowed services for instantiation at each NFV node h, h estimates the expected competitive prices of every NFI. Then moving from the highest to the lowest competitive price, the NFV node instantiates the service associated with the price  $\overline{\lambda}$  as long as i) it is expected that the instance will not be under-utilised,  $\overline{\lambda} > \underline{\lambda}$ , and ii) the Market Orchestrator maximum number of instances allow it, respecting properties (*P1*), (*P2*), and (*P4*).

3) NFI Consolidation: If the price of an instance is below the minimum target shadow price,  $\underline{\lambda}$ , the NFV node consolidates this instance (**P2**). When there is a service availability requirement, the market orchestrator can hinder the consolidation of the last instance of that service.

 $<sup>{}^{2}[\</sup>cdot]^{+}$  denotes the projection onto nonnegative orthant.

 $<sup>^{3}</sup>$ In fact it is not the NFV node that is aware of the forwarded traffic but the switch that the NFV node is attached to

## V. IMPLEMENTATION

The prototype implementation of DRENCH consists of SDN controller, Open vSwitches and custom virtual NFIs. Overall implementation including the extensions needed for the DRENCH controller and NFI support is  $\sim 1800 \text{ LOC}$ .

#### A. Control Plane: DRENCH Controller

We extended Pox<sup>4</sup> to serve as DRENCH's controller. Policy specification is provided as input to the controller.

Flow Classifier and Policy Enforcement: The DRENCH controller performs fine-grained flow classification, based on the standard IP 5-tuple. As per the mappings in policy specification, it applies the sequence of desired service functions. We dedicate the combination of IP-DS field and L4: destination port to represent the service chain ID and the sequence of functions in the service chain respectively.

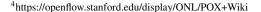
Flow Steering: In order to be more flexible, and readily deployable with NFIs, we rely on the switch-based service chain/network function ID mapping that can be supported by openflow switches, without the need for any modifications to the NFI. The controller sets the path from the Ingress/NFV node to the next NFV node/destination in the chain. For better granularity at each ingress or intermediate NFV node, the flow rules are setup based on the match obtained from flowclassification - this readily enables the capability to match and correlate the packets that enter/exit the NFIs, even when NFIs modify the packet headers, while the rest of the intermediate and egress switches are setup with a tunnel. For tunneling, we leverage the named instance source routing scheme [19] with an improvement for the tag, which is defined as follows:

VNF-ID = InstanceID | SVC-ID, where the InstanceID is defined by CoreID|SW-ID.

This enables the paths to be setup pro-actively on all the intermediate switches as soon as an NFI is discovered in the network. Our proposal of ID based tunnelling can be realized by using either the Multi-Protocol Label Switching (MPLS) or VLAN tags, underlay (unused IP/TCP header fields like DS/option fields) or with Network Servie Header (NSH) [20]. The choice of Layer-2.5 (MPLS) or Layer-2 (VLAN) tag makes it convenient to define the match in Openflow switches, *i.e.*, by being agnostic to L3/L4 fields allow any TCP/UDP flow to be matched with a same rule. This helps to significantly reduces the number of switch rules. As most MBs readily support VLAN as opposed to MPLS [21], we make use of Layer-2 tags to realize the NFI-based tunnels.

## B. Data Plane: Openflow Swithces and Network Functions

One of the key challenges we faced in the implementation of DRENCH in our prototype was the non-availability of a MB/NFV-capable switch in the Mininet environment. Therefore, we realized NFIs as hosts connected to the switch. However, this resulted in additional challenges since Open-Flow is designed with a Southbound API control channel between the controller and network switches, but not the hosts. Therefore, any information (e.g., estimated costs of



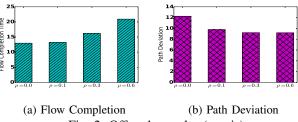


Fig. 2: Off-path penalty (x-axis)

other instances or shadow-price) that had to be exchanged between the controller and the NFV-hosts had to be performed either via the switch (e.g., we used LLDP packets to make the controller aware of the presence of NFV-hosts) or via a separate channel. In a real-world deployment, we believe that this would not be the case since NFV nodes will have a Southbound-API based channel from the controller through an in-built switch. Once the communication channel's established, the controller was able to both obtain and disseminate cost related information periodically. Additionally, to demonstrate that the NFI capability can be realized on Openflow switches, we implemented on each host a host-local Open vSwitch and controller. The host interface is setup as a port of the local vSwitch. This way, we leveraged the local Open vSwitch and Pox controller to implement the VNF specific functionality, *i.e.*, to monitor and disseminate NFI specific load information and communicate it to the global controller.

## VI. EVALUATION

Our goal is three-fold: i) study the effect of different DRENCH parameters, the resulting trade-offs and the impact on performance in order to fine-tune DRENCH; ii) highlight the benefits of DRENCH on a controlled topology (we perform these evaluations on a CloudLab<sup>5</sup> test-bed); and *iii*) compare the performance of DRENCH with other approaches in large scale scenarios (both data-center and Rocketfuel topologies). We make use of the DRENCH prototype on a data-center topology in a Mininet Cluster<sup>6</sup> to study the benefits of DRENCH in terms of FCT, delay, number of active NFIs, NFI utilization and the impact of redirection. We compare DRENCH against a centralized approach (Slick [4]) and against DRENCH without redirection (DwoR).

Moreover, we build a custom-based simulator to study the benefits of DRENCH in terms of path deviation, avg. throughput and FCT in comparison to the custom centralized approach: Simplefying [6] on top of a E2 SDN framework [2]. Unlike similar work that focuses on latency requirements in service chains, we also emphasize on FCT - arguably the most important metric for the user [22].

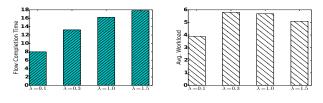
#### A. DRENCH Parameter design and study of tradeoffs

We implemented DRENCH on a python-based discrete event simulator using SimPy,<sup>7</sup> in order to be able to quickly fine-tune DRENCH's parameters and to perform large scale

<sup>&</sup>lt;sup>5</sup>https://cloudlab.us

<sup>&</sup>lt;sup>6</sup>http://mininet.org

<sup>&</sup>lt;sup>7</sup>http://simpy.readthedocs.io/en/latest/



(a) Flow Completion (b) Work Load (Throughput) Fig. 3: Shadow Price threshold (x-axis)

evaluation. For these experiments, we perform simulations on a Rocketfuel topology with 27 hosts that send/receive flows and 57 nodes that are capable of hosting NFIs. Unless stated otherwise, the default parameters are: off-path penalty,  $\rho$ , is 0.3 and length of SFC is 2. We then apply the results of the simulation study to setup the DRENCH prototype.

1) Off-path penalty,  $\rho$ : Traditionally, flows follow the shortest path towards their destination, deviating only for traffic engineering reasons and/or in response to link/node failures (e.g., fast-reroute in MPLS). When it comes to service chaining, flows deviate from their shortest path in order to be served by NFIs. In DRENCH the off-path penalty factor,  $\rho$ , enables the tradeoff between the shortest path deviation and FCT by trading path deviation overhead for less congested NFIs as Figs. 2 and 3 indicate. In more detail, the FCT increases as the off-path penalty,  $\rho$ , increases since the flows prefer to get served by a more congested NFI (e.g., with a higher service cost) than deviating from their shortest path. Hence, for our experimental purposes we choose a value of  $\rho$  in the range of 0.3-0.5. The exact setting of the  $\rho$  factor is up to the network operator. During low-demand periods (e.g., during nighttime), where links are generally less utilised, operators might choose a lower value to improve FCT (*i.e.*, given low link utilisation, extra path deviation should not cause problems). On the other hand, in high demand periods, path deviation should be kept to lower levels, even if this increases the individual flows' FCT, in order to avoid extensive path stretch.

2) Shadow price Threshold: Fig. 3 shows the results of varying the minimum shadow-price threshold,  $\underline{\lambda}$ , at which new instances are spawned. Fig. 3a shows that FCT increases with increasing threshold values. A very low  $\underline{\lambda}$  of 0.1 results in lower FCT compared to values in the range 0.3 to 1.5, but we can also observe that it results in a large number of underutilized NFIs as seen in Fig. 3b. Utilisation is depicted as the amount of traffic (in terms of throughput - see Fig. 3b) that an NFI can serve. The exact setting of  $\underline{\lambda}$  is up to the network operator. If the demand is low, then more instances can be allowed in order to result in lower FCTs, but larger number of under-utilised instances. In contrast, during high demand periods, the operator might have to compromise on individual flow FCT, in order to make full utilisation of the existing NFIs and eventually serve more flows overall.

## B. Testbed: Simple controlled experiments

We perform controlled experiments on a small topology, as shown in Fig. 4, in our CloudLab setup to illustrate the benefits of DRENCH components. Consider flows *Src1-Dst1*,

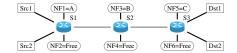
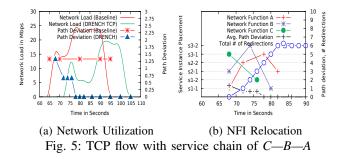


Fig. 4: Simple Topology with initial placement of NFIs.



requiring the service chain of C/B/A, which also comprises the ideal placement.

We study the performance and behavior of the system in the worst case scenario, where the services are initially placed in the reverse order as depicted in Fig. 4.<sup>8</sup> To prevent an increase in the flow's path length (by going back and forth in this topology), it is desirable to relocate the NFIs (from A - B - C to C - B - A in nodes S1-S2-S3, respectively) to minimize path stretch and FCT. In Fig. 5a, we observe

TABLE II: Avg. Bitrate and Delay

-	DRENCH	Baseline
Avg Bitrate (Mbps)	4.033227116	3.814941386
Avg Pkt Delay (ms)	18.982	23.207
Std. Dev of Pkt Delay (ms)	129.151	143.216

that, initially, due to the service instances being located in the wrong order (*i.e.*, A - B - C, instead of C - B - A) the flow suffers higher path-stretch, resulting in additional delay and higher network load. Later, as the switches gradually adapt towards the ideal placement, path stretch declines and network throughput increases (see Table II) compared to a non-reactive (Baseline) approach.

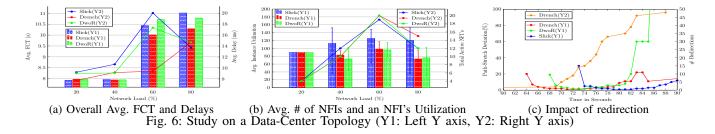
When all the instances individually seek to be competitive and maximise their utilisation, the switches with NFV capacity near the ingress switches end up hosting most of the services. From 5b, we see that DRENCH converges to this ideal case by instantiating and placing the services in the chain along the path towards the destination.

## C. Large scale Evaluation: Data-Center Topology

We setup a Mininet Cluster on Cloudlab to study the performance of DRENCH in a large network topology.

**Topology:** We use a 4K Fat-Tree topology to evaluate DRENCH in a data-center environment and compare it to Slick (used as an example of a centralized approach.) We consider that only aggregation-layer switches in the fat-tree topology have NFV capability and dedicate 2 cores per aggregate switch for instantiating the NFIs.

<sup>&</sup>lt;sup>8</sup>We set the NF capacity and the off-path penalty factors to just exceed the threshold required in order to allow for service instantiation.



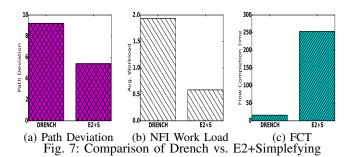
Workload: We model the traffic based on the available data center workload characteristics similar to the ones used in [11], [14]. The workload constitutes a mix of elephant flows (20% with flow size  $\geq 10$ MB) and mice flows (80% with flow size <2MB). Thus, elephant flows account for more than 80% of the traffic bytes. We use iperf<sup>9</sup> and D-ITG [23] to generate traffic with varying network loads. Flows originate from one of the servers connected to a leaf switch and terminate at another server connected to another leaf switch (in either the same or different pod). We use TCP flows in a client/server model with random flow arrival times. Based on the information on the service chaining policies in [24] and the details presented in earlier work (e.g., [6]), we setup a service function chain of 3 distinct Network Functions (NFs). We assume that there are a total of 6 NFs available in the network and that each flow requires exactly three of them. The service functions are chosen based on a zipf-distribution with exponent set to 0.3.

**Parameters:** Based on our findings from Section VI-A2, we set the parameter off-path penalty factor to 0.5, and the instance shadow-price that influences service consolidation and service instantiation decisions as follows. An instance is consolidated when the shadow-price reflects NFI utilisation of < 30% and flows serviced by that instance is < 5 flows. This is done in-order to mitigate the number of flow re-directions and the packet re-ordering impact of flow re-directions. A new NFI is instantiated when the shadow-price reflects NFI utilisation of > 85%.

**Comparison:** In order to perform a fair comparison, we also implemented a greedy heuristic-based flow steering approach as in Slick [4] - as a representative of a fully centralized state-of-the-art load balancing scheme <sup>10</sup>. We also compare against DwoR to study the effects of redirections and its impact on DRENCH. Our main goal is to evaluate the behaviour and performance of DRENCH wrt NFI placement, flow steering, and load balancing in terms of its efficiency in NF resource utilization and flow completion time (FCT).

Figure 6a shows the average FCT and packet delays for different schemes. We can observe that at lower load (20-40%) all the schemes have similar FCT, but DRENCH and DwoR schemes incur relatively lower packet delays. At larger network loads, DRENCH performs roughly  $10\sim20\%$  better than Slick and DwoR in terms of FCT. Furthermore, we also observe that DwoR provides better FCT than the centralized

<sup>9</sup>https://iperf.fr/



approach, while DRENCH outperforms both DwoR and Slick. Finally, we also see that the average delay in the case of DRENCH remains low in most cases and close to the other solutions when the network load is extremely high (80%).

In Figure 6b, the average number of NFIs utilized for all the schemes is almost the same However, DRENCH is able to balance the load more efficiently since the variation in the load among the NFIs and the NFI utilization is maintained at the optimum.

In Figure 6c, we present the specific case for 80% network load, where we observe that DRENCH is able to get close to Slick, which is optimal terms of path-stretch deviation. We can also observe the benefits of DRENCH redirections in order to correct path-deviation during traffic bursts (see 70-80secs) and also when a large number of flows terminate. In both cases we can see that DRENCH is more effective than DwoR, in terms of keeping path-stretch at a minimum, providing better load-balancing across NFIs and achieving better FCT.

Note: In DRENCH re-directions enable to reroute flows through lightly loaded links and NFIs, thus aid to lower packet delays. However, the FCT may still get impacted due to interim packet-reordering, which result in false congestion signals. We believe that a modified TCP stack as in [25] could help mitigate the packet-reordering issue.

## D. Large scale Evaluation: ISP Topology

To further examine the capability of DRENCH to efficiently use NFIs in a typical WAN ISP environment, we performed simulations with *SimPy*.<sup>11</sup>

**Experimental Setup:** We performed simulations on the Rocketfuel AS-1755 (Ebone in Europe) topology.<sup>12</sup> In order to perform a fair comparison, we implemented a greedy heuristic

<sup>&</sup>lt;sup>10</sup>We implemented the shortest weighted path-based flow routing scheme and not the entire Slick runtime [4]

<sup>&</sup>lt;sup>11</sup>We plan to make our simulator code publicly available in order for other members of the community to experiment and extend with the group of algorithms and protocols discussed here.

<sup>&</sup>lt;sup>12</sup>http://www.cs.washington.edu/research/projects/networking/www/rocketfuel/interactive/1755eur.html

for flow steering which we call E2+Simplefying that uses a combination of E2 [2] for service instantiation and servicechain path definition, and Simplefying [6] for flow steering. Note that in terms of performance, this combination of E2 and Simplefying performs much better than any of the E2 or Simplefying alone and therefore is the best choice for comparison.

DRENCH vs. E2+Simplefying: Fig. 7 compares DRENCH and E2+Simplefying (E2+S) approach. We observe that DRENCH presents higher path deviation (see Fig. 7a) since it deviates from the shortest path in search of a non-congested NFI. In doing so, DRENCH is able to make better use of the available NFI instances (see Fig. 7b) and performs instantiation or consolidation when necessary. This way, DRENCH ensures that all the available NFIs are running close to peak utilisation (in terms of throughput served by the NFV nodes) as seen in Fig. 7b. With these design choices, DRENCH achieves significantly lower FCT (see Fig. 7c). In summary, DRENCH provides up to  $10 \times$  improvement in FCT and is able to support roughly 4x times more workload, while incurring an average path deviation penalty of up to 2x in comparison to the E2+Simplefying approach. This extra path stretch though is compensated in terms of optimal node utilisation and in turn, very low FCT.

**Summary of Evaluation:** To summarize, our evaluation demonstrates that with its hybrid centralised-decentralised decision-making structure, DRENCH can optimally and dynamically load-balance traffic and allocate resources according to demand. DRENCH makes informed decisions on the load of NFIs and accordingly instantiates new or consolidates existing NFIs. In turn, traffic is load-balanced (through flow steering and redirection) to the appropriate instance achieving significantly lower FCT.

#### VII. CONCLUSION

We have developed a hybrid centralized-distributed algorithm framework for resource management and traffic load-balancing among virtual NFIs that elegantly combines distributed decision-making with centralized control for orchestration and coordination, while performing complex, dynamic service function chaining. DRENCH is designed to dynamically adapt and balance resource availability and traffic demand. It is based on a market-inspired, competition-based shadow-price and accordingly takes decisions on flow-steering, flow-redirection and service instantiation/consolidation in a distributed manner. A centralized SDN controller performs market orchestration, dissemination of price information and coordination.

Our novel semi-distributed approach for dynamic service instantiation and direction of new and existing flows to the least loaded NFV node increases the throughput from each NFV node and in turn reduces FCT significantly. With the help of a prototype implementation on CloudLab and extensive simulations, we illustrate the benefits of using DRENCH, namely that traffic is dynamically load-balanced among instances and the path deviation of flows across the NFIs is kept to a minimum. Resources are efficiently utilized by timely consolidation of NFIs when they are lightly loaded. Overall DRENCH results in almost a  $10 \times$  reduction in FCT in some of our experiments.

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