

## ORIGINAL ARTICLE

# Assessing Pharmacodynamic Interactions in Mice Using the Multistate Tuberculosis Pharmacometric and General Pharmacodynamic Interaction Models

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The aim of this study was to investigate pharmacodynamic (PD) interactions in mice infected with *Mycobacterium tuberculosis* using population pharmacokinetics (PKs), the Multistate Tuberculosis Pharmacometric (MTP) model, and the General Pharmacodynamic Interaction (GPDI) model. Rifampicin, isoniazid, ethambutol, or pyrazinamide were administered in monotherapy for 4 weeks. Rifampicin and isoniazid showed effects in monotherapy, whereas the animals became moribund after 7 days with ethambutol or pyrazinamide alone. No PD interactions were observed against fast-multiplying bacteria. Interactions between rifampicin and isoniazid on killing slow and non-multiplying bacteria were identified, which led to an increase of 0.86 log<sub>10</sub> colony-forming unit (CFU)/lungs at 28 days after treatment compared to expected additivity (i.e., antagonism). An interaction between rifampicin and ethambutol on killing non-multiplying bacteria was quantified, which led to a decrease of 2.84 log<sub>10</sub> CFU/lungs at 28 days after treatment (i.e., synergism). These results show the value of pharmacometrics to quantitatively assess PD interactions in preclinical tuberculosis drug development.

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## Study Highlights

### WHAT IS THE CURRENT KNOWLEDGE ON THE TOPIC?

☑ There is limited knowledge on the PD interactions between standard TB drugs due to a lack of a quantitative framework for their assessment.

### WHAT QUESTION DID THIS STUDY ADDRESS?

☑ It addressed how to quantitatively assess drug-drug PD interactions between two drugs in more than two-drug combination therapies using sparse mice data.

### WHAT THIS STUDY ADDS TO OUR KNOWLEDGE

☑ The application of the MTP model together with the GPDI model in TB-infected BALB/c mice could describe untreated mice or mice treated with rifampicin, isonia-

zid, ethambutol, and pyrazinamide mono therapy, as well as an assessment of antagonistic interactions (less than expected additivity) between rifampicin and isoniazid and synergistic interactions (more than expected additivity) between rifampicin and ethambutol in combination therapies using a model-based approach.

### HOW MIGHT THIS CHANGE DRUG DISCOVERY, DEVELOPMENT, AND/OR THERAPEUTICS?

☑ Even with sparse animal data, PK-PD relationships with PD interactions using the MTP-GPDI model could be assessed, which provides information for phase II and phase III trials for translational development of novel combination therapies in TB drug development.

In 2015, approximately 1.8 million people died from *Mycobacterium tuberculosis* (*M. tuberculosis*) and 10.4 million new cases were reported worldwide.<sup>1</sup> No regimen has yet proven to be superior to the standard regimen for drug-susceptible tuberculosis (TB), which consists of a 2-month initial phase of rifampicin, isoniazid, pyrazinamide, and ethambutol followed by a 4-month continuation phase of rifampicin and isoniazid. Due to the development of drug resistance, long treatment periods cause a high risk of low patient adherence as well as disease relapse in patients. New drugs or combinations are highly needed to overcome these obstacles. Potential pharmacodynamic (PD) drug-drug interactions (i.e., a lower (antagonism) or higher effect

(synergism) compared to expected additivity, such as adding each drug effect in monotherapy), present a difficulty arising from combination therapies. The PD interactions are difficult to assess in a clinical setting, especially in the field of antitubercular drug development in which regimens contain two or more drugs. Hence, preclinical systems have to fill this knowledge gap, but evaluation of PD interactions has been methodologically challenging.<sup>2</sup>

The General Pharmacodynamic Interaction (GPDI) model provides a model-based assessment of PD interactions given as fractional changes of PD parameters of monotherapy effects, which was originally developed and presented by Wicha *et al.*<sup>3</sup> In contrast to other approaches, the GPDI

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model is applicable for more than two potentially interacting drugs, which is of key importance in TB drug development. A key feature of the GPDI approach is that interactions are quantified on the level of PD parameters and not on the pure effect level. Thereby, the GPDI approach is capable, in addition to determine pure synergistic or antagonistic interactions, to detect asymmetric interactions (i.e., in which both synergism and antagonism occur between two drugs over a concentration range or study time period). In addition, an advantage of the GPDI model compared with other traditional approaches is that it can estimate the interaction between an inactive perpetrator and an active victim drug. Moreover, the GPDI approach can be parameterized in different complexity and, hence, be used for both sparse and rich data.

The Multistate Tuberculosis Pharmacometric (MTP) model, predicting the change in bacterial numbers of fast, slow, and non-multiplying bacteria, with and without drug effects, is a semimechanistic pharmacokinetic (PK) and PD model for studying antitubercular drug effects and was developed using *in vitro* data.<sup>4</sup> The MTP model has successfully been used to describe rifampicin efficacy in an acute C57BL/6 mouse model using differences in colony-forming units (CFUs) over time,<sup>5</sup> and has also been applied to clinical data in order to estimate the drug efficacy of human early bacterial activity and to perform clinical trial simulations.<sup>6</sup>

The aim of this work was to use the MTP model approach to describe the drug effects of rifampicin, isoniazid, ethambutol, and pyrazinamide in the monotherapy in a BALB/c mouse model using biomarker CFU data. In addition, we aimed to link the MTP model to the GPDI model in order to assess PD interactions in combination therapies.

## MATERIALS AND METHODS

### Chemicals

Ethambutol and pyrazinamide were obtained from Sigma-Aldrich (Zwijndrecht, The Netherlands) and isoniazid was obtained from the hospital pharmacy (Rotterdam, The Netherlands). Compounds were dissolved in distilled water. Rifampicin was obtained from Sanofi-Aventis (Gouda, The Netherlands), dissolved in the supplemented solvent, and further diluted in water.

### Animals

Specified pathogen-free female BALB/c mice (13–15 weeks old, weighing 20–25 g) were obtained from Charles River (Les Oncins, France). Experimental protocols adhered to the rules specified in the Dutch Animal Experimentation Act and were in concordance with the European Union (EU) animal directive 2010/63/EU. The Institutional Animal Care and Use Committee of the Erasmus Medical Center approved the present protocols (117-12-08 and 117-12-13).

Mice were infected, as previously described.<sup>7</sup> In brief, mice under anesthesia were infected through intratracheal instillation of a suspension (40  $\mu$ L) containing  $9.5 \times 10^4$  CFU of the Beijing VN 2002-1585 genotype strain, followed by proper inhalation to ensure the formation of a bilateral TB infection.<sup>8</sup>

### Anti-TB treatment

In this study, the doses were chosen based on the human-equivalent dose of each antitubercular compound. There

were three dose levels chosen for each drug,  $0.5 \times$  human-equivalent dose,  $1 \times$  human-equivalent dose, and  $2 \times$  human-equivalent dose. All treatments started 14 days after infection. Monotherapy of rifampicin at dose levels at 5, 10, and 20 mg/kg ( $R_5$ ,  $R_{10}$ , and  $R_{20}$ , respectively), isoniazid at 12.5, 25, and 50 mg/kg ( $H_{12.5}$ ,  $H_{25}$ , and  $H_{50}$ , respectively), ethambutol at 50, 100, and 200 mg/kg ( $E_{50}$ ,  $E_{100}$ , and  $E_{200}$ , respectively) or pyrazinamide at 75, 150, and 300 mg/kg ( $Z_{75}$ ,  $Z_{150}$ , and  $Z_{300}$ , respectively) were orally administered daily for 5 days per week via oral gavage, lasting for 4 weeks.<sup>8</sup> The CFU counts were assessed in monotherapy after 1, 2, and 4 weeks of treatment with isoniazid or rifampicin, using 9 mice per time point, including 3 mice per dose level. The CFU counts were only obtained from 6 mice after 1 week of treatment with pyrazinamide and ethambutol, because the mice did not survive beyond 1 week with treatments of pyrazinamide or ethambutol. Fixed doses were used in combination therapies, including  $R_{10}$ ,  $H_{25}$ ,  $E_{100}$ , and  $Z_{150}$ . Combination therapies ( $R_{10}H_{25}$ ,  $R_{10}H_{25}Z_{150}$ , and  $R_{10}H_{25}Z_{150}E_{100}$ ) lasted up to 24 weeks. The CFU counts were assessed in drug combinations after 1, 2, 4, 8, 12, and 24 weeks of treatment with 3 mice at each occasion. Bacterial natural growth (i.e., no treatment), was collected at 1, 3, 7, 14, and 21 days after infection.

### Population pharmacokinetic study and modeling

The PK information was obtained from TB-infected mice and was used for assessing PD in monotherapy. One blood sample per mouse was drawn from infected mice ( $n = 49$ ) after 4 weeks of treatment with rifampicin ( $R_5$ ,  $R_{10}$ , or  $R_{20}$ ), isoniazid ( $H_{12.5}$ ,  $H_{25}$ , or  $H_{50}$ ), and after 1 week of treatment with ethambutol ( $E_{50}$ ,  $E_{100}$ , or  $E_{200}$ ) or pyrazinamide ( $Z_{75}$ ,  $Z_{150}$ , or  $Z_{300}$ ) at 1, 4, and 8 hours after dose with 3 mice per time point. Mice receiving  $Z_{75}$  in monotherapy only contributed CFU data and not PK data. The PK sampling was different for mice treated with pyrazinamide or ethambutol, as the treatment results in no survival beyond 1 week with treatments. Drug plasma samples from infected mice were frozen at  $-80^\circ\text{C}$  and processed by protein precipitation with organic solvents plus filtration. Samples were then analyzed by ultraperformance liquid chromatography tandem mass-spectrometry for quantification of each drug at GlaxoSmithKline. To support the population pharmacokinetic (PopPK) model development for rifampicin, drug concentrations from the sparsely sampled TB-infected mice were combined with a second PK study in healthy mice ( $n = 18$ ).<sup>8</sup> Healthy mice were administered  $R_{10}$  or  $R_{160}$  for 5 days a week for 3 weeks and the PK was obtained at 0.08, 0.25, 0.5, 0.75, 1.5, 3, and 6 hours after the last dose (one sample per mouse). Rifampicin, quantified in plasma samples from healthy mice, was measured by protein precipitation, followed by high-performance liquid chromatography with ultraviolet detection.<sup>9</sup>

All plasma concentrations of each drug were pooled and modeled simultaneously. One and two compartment distribution models with first-order absorption and elimination were evaluated. Because of lack of data in the absorption phase, the absorption rate constant ( $k_a$ ) of isoniazid, ethambutol, and pyrazinamide was fixed to values from a previous study.<sup>10</sup> Differences in PK between healthy and

infected mice were evaluated. Similarly, concentration-dependencies or time-dependencies in all PK parameters were evaluated. Because only one sample was taken from each mouse, interindividual variability in PK was not quantified. A PopPK parameter approach was used as input and linked to the MTP model.<sup>11</sup>

### Evaluation of drug effects in monotherapy

The MTP model, consisting of fast-multiplying (F), slow-multiplying (S), and non-multiplying (N) bacteria was used for the PD modeling of CFU data from each drug. The differential equation system for F (Eq. 1), S (Eq. 2), and N (Eq. 3) was as follows:

$$\frac{dF}{dt} = k_G \cdot F + k_{SF} \cdot S - k_{FS} \cdot F - k_{FN} \cdot F \quad (1)$$

$$\frac{dS}{dt} = k_{FS} \cdot F + k_{NS} \cdot N - k_{SF} \cdot S - k_{SN} \cdot S \quad (2)$$

$$\frac{dN}{dt} = k_{SN} \cdot S - k_{NS} \cdot N + k_{FN} \cdot F \quad (3)$$

where  $k_G$  is the growth rate of F,  $k_{FS}$ ,  $k_{SF}$ ,  $k_{FN}$ ,  $k_{SN}$ , and  $k_{NS}$  are transfer rates between each bacterial state and F, S, and N represent fast, slow, and non-multiplying bacteria, respectively.

Initially, only CFU data without treatment were evaluated. The first-order transfer rates from S to F ( $k_{SF}$ ), from S to N ( $k_{SN}$ ), from N to S ( $k_{NS}$ ), and from F to N ( $k_{FN}$ ) were fixed according to the original *in vitro* study.<sup>4</sup> The transfer of F to S ( $k_{FS}$ ) increased linearly with time in the MTP model applied to *in vitro* data and was re-evaluated using maximum effect ( $E_{max}$ ) and linear functions with respect to time in this study. A re-estimation of  $k_{FS}$  as well as the other transfer rates, one at a time, was compared to fixing the parameter to the *in vitro* estimates.<sup>4</sup> Gompertz,  $E_{max}$ , and linear growth functions were evaluated to describe the growth rate ( $k_G$ ) of F in this mouse model.

All parameters associated with natural growth ( $k_G$ ,  $k_{FS}$ ,  $k_{SF}$ ,  $k_{FN}$ ,  $k_{SN}$ , and  $k_{NS}$ ) were fixed during the estimation of drug effects. The effect of each drug was first evaluated using only monotherapy data. The effects of monotherapy were evaluated as inhibition of the growth of F, and/or stimulation of the death on each of the three bacterial states using an on/off effect, a linear function (Eq. 4), an ordinary  $E_{max}$  function (Eq. 5), or a sigmoidal  $E_{max}$  function (Eq. 6).

$$E_{drug} = k \cdot C_{drug} \quad (4)$$

$$E_{drug} = \frac{E_{max} \cdot C_{drug}}{EC_{50} + C_{drug}} \quad (5)$$

$$E_{drug} = \frac{E_{max} \cdot C_{drug}^\gamma}{EC_{50}^\gamma + C_{drug}^\gamma} \quad (6)$$

where  $C_{drug}$  represents drug concentration;  $k$  is the kill rate for each drug in monotherapy;  $E_{max}$  is the maximal achievable drug effect for each drug;  $EC_{50}$  is the drug concentration at 50% of  $E_{max}$  for each drug;  $\gamma$  is a sigmoidicity parameter, and  $E_{drug}$  expresses the drug effect in monotherapy. In the following step, all identified drug effects from

monotherapy were combined and evaluated for statistical significance ( $P < 0.05$ ). A final backward evaluation step ( $P < 0.01$ ) was also done where the effect functions were reduced to their simpler forms to identify the best model for each drug in monotherapy.

### Evaluation of pharmacodynamic interactions

During the evaluation of PD interactions, data from combination regimens were pooled with data from natural growth and data from monotherapy. The MTP model parameters ( $k_G$ ,  $k_{FS}$ ,  $k_{SF}$ ,  $k_{FN}$ ,  $k_{SN}$ , and  $k_{NS}$ ) and parameters of the monotherapy final exposure-response relationships were fixed during the PD interaction assessment. If no drug effect was identified using only monotherapy, a re-evaluation using the combination dataset was done with a similar modeling strategy as for monotherapy data. This step was required due to the different treatment lengths. The PD interactions were assessed at each effect site, including inhibition of the growth of F, and/or stimulation of the death of F, S, or N.

The Bliss Independence (BI)<sup>12</sup> (i.e.,  $E_{AB} = E_A + E_B - E_A \times E_B$ ) was used as an additivity criterion for the GPDI model,<sup>3</sup> as the Loewe Additivity<sup>13</sup> cannot handle differences in  $E_{max}$ . As BI was derived from probability theory, all effects were scaled between 0 and 1 relative to the highest  $E_{max}$  for BI calculation and then rescaled by the highest  $E_{max}$ , as described by Wicha *et al.*<sup>14</sup> For slope models, the BI was simplified to  $E_{AB} = E_A + E_B$  due to the minor contribution of  $E_A \cdot E_B$  at concentrations well below the  $EC_{50}$  when linear models are identified. Hence, the drug effects of two drugs A and B can be expressed as in Eq. 7 and Eq. 8. In three and four-drug combinations, interaction parameters identified in previous combinations were fixed. In the final MTP-GPDI model, all parameters were estimated simultaneously.

$$E_A = \frac{E_{max,A} \times C_A^{H_A}}{\left( EC_{50,A} \times \left( 1 + \frac{INT_{AB} \times C_B^{H_{INT,B}}}{EC_{50,INT,AB} \times C_B^{H_{INT,B}} + C_B^{H_{INT,B}}} \right) \right)^{H_A} + C_A^{H_A}} \quad (7)$$

$$E_B = \frac{E_{max,B} \times C_B^{H_B}}{\left( EC_{50,B} \times \left( 1 + \frac{INT_{BA} \times C_A^{H_{INT,A}}}{EC_{50,INT,BA} \times C_A^{H_{INT,A}} + C_A^{H_{INT,A}}} \right) \right)^{H_B} + C_B^{H_B}} \quad (8)$$

where  $INT_{AB}$  and  $INT_{BA}$  characterize the maximum fractional change of the respective PD parameters. An estimated value of zero of  $INT_{AB}$  or  $INT_{BA}$  suggested no interaction. A positive value suggested decreased drug potency, whereas a value between  $-1$  and  $0$  suggested increased drug potency caused by interaction between the two drugs.  $EC_{50,INT,AB}$  and  $EC_{50,INT,BA}$  represent the interaction potencies.  $H_{INT,A}$  and  $H_{INT,B}$  represent the interaction sigmoidicities.

Due to the fact that few exposure levels were included in the combination therapy data in this study, a joint  $INT_{AB}$  was estimated ( $INT_{AB} = INT_{BA}$ ) and  $EC_{50,INT}$  was set to a very low value of  $1 \times 10^{-8}$ , which reduced the  $E_{max}$  function to an on/off effect, which was used in evaluating the PD interaction. Equation 9 shows an example of a reduced GPDI model for the evaluation of a joint effect of drugs A

and B when the exposure-response relationship was defined using a slope model, and on/off interaction with a joint interaction term  $INT_{AB}$ :

$$E_{AB} = C_A \cdot \frac{k_A}{1 + INT_{AB}} + C_B \cdot \frac{k_B}{1 + INT_{AB}} \quad (9)$$

where  $k_A$  and  $k_B$  are linear effects of drug A and drug B identified in monotherapy.

### Model evaluation and selection

All modeling was done using the software NONMEM version 7.3 (Icon Development Solutions (<http://www.iconplc.com/technology/products/nonmem>), Ellicott City, MD) using the first-order conditional estimation method.<sup>15</sup> Model evaluation and selection were based on the objective function value (OFV) with a decrease of 3.84 considered statistically significant ( $P < 0.05$ ,  $\chi^2$  distribution) for nested models and one degree of freedom. In addition, goodness-of-fit plots, parameter precision, predictive performance assessed using visual predictive check (VPC),<sup>16</sup> prediction-corrected visual predictive checks (pcVPC),<sup>17</sup> and scientific plausibility were used for model selection. In both pcVPC and VPC, 1,000 replicates were simulated based on the model and fifth, median, and 95th percentiles were used in conjunction with the corresponding data to assess model performance using Perl-speaks-NONMEM (PsN) version 4.2.0 (<http://psn.sourceforge.net>), Department of Pharmaceutical Biosciences, Uppsala University, Sweden).<sup>16</sup> The R package Xpose version 4.4.1 (<http://xpose.sourceforge.net>), Department of Pharmaceutical Biosciences, Uppsala University, Sweden) was used for visualization of results and data management.<sup>16</sup> The run record was produced with Pirana software version 2.7 (Pirana Software and Consulting (<http://www.pirana-software.com>), San Francisco, CA).<sup>18</sup> The M3 method in NONMEM was used to handle data below the lower limit of quantification (LLOQ),<sup>19</sup> which was 10 CFU/lungs for PD data (5.7% of the dataset) and 10 ng/mL, 100 ng/mL, 10 ng/mL, and 60 ng/mL of rifampicin (8.9%), isoniazid (27.8%), ethambutol (0%), and pyrazinamide PK data (0%), respectively. Proportional, combined proportional, and additive error models for PK data and an additive error model on log scale for PD data were evaluated to describe residual unexplained variability.

## RESULTS

### Population pharmacokinetic models

The final PopPK models of rifampicin, isoniazid, and pyrazinamide were one-compartment models, whereas a two-compartment model described the ethambutol data well. All data were well-described using the final PopPK models (Figure 1) and all PK parameters are shown in Table 1. The pcVPCs of the final PopPK models are available as Supplementary Material S1.

The final PopPK model for rifampicin included a separate apparent clearance ( $CL/F$ ) in TB-infected mice receiving 4 weeks of rifampicin treatment, which was 3 times higher than  $CL/F$  in healthy mice treated for 3 weeks. In addition, the  $CL/F$  at  $R_{160}$  was 2.5 times lower than for mice that

received lower doses of rifampicin. Apparent volume of distribution of the central compartment ( $V/F$ ) after  $R_{160}$  was 1,700 mL·kg<sup>-1</sup>, which was larger than  $V/F$  at other dose levels (706 mL·kg<sup>-1</sup>). Isoniazid  $CL/F$  decreased from 612 mL·h<sup>-1</sup>·kg<sup>-1</sup> at lowest dose of 12.5 mg/kg to 440 mL·h<sup>-1</sup>·kg<sup>-1</sup>. Isoniazid  $V/F$  was estimated to 811 mL·kg<sup>-1</sup>. Apparent clearance ( $CL/F$ ) of ethambutol was estimated to 3,400 mL·h<sup>-1</sup>·kg<sup>-1</sup>. Ethambutol  $V/F$  and apparent volume of distribution of the peripheral compartment ( $V_2/F$ ) were estimated to 1,500 and 4,690 mL·kg<sup>-1</sup>, respectively. Pyrazinamide PK was linear with respect to dose with  $CL/F$  estimated to 273 mL·h<sup>-1</sup>·kg<sup>-1</sup> and  $V/F$  to 525 mL·kg<sup>-1</sup>.

### Multistate tuberculosis pharmacometric model

The final model structure of the MTP model describing changes in CFU over time after treatment with rifampicin, isoniazid, pyrazinamide, or ethambutol is shown in Figure 1. The data supported estimation of initial bacterial numbers of fast-multiplying ( $F_0$ ) and slow-multiplying ( $S_0$ ) bacteria, but no inoculum of non-multiplying bacteria, which was, therefore, set to zero in the final model. Re-estimating the transfer rate from F to S ( $k_{FS}$ ) as a linear function with time produced a decrease in OFV of 22 points compared to fixing the parameter to the *in vitro* estimate.<sup>4</sup> Re-estimation of the other transfer rates between the states did not provide a reduction in OFV and was, therefore, fixed to *in vitro* estimates.<sup>4</sup> An exponential growth function was used to describe the natural growth rate of F ( $k_G$ ).

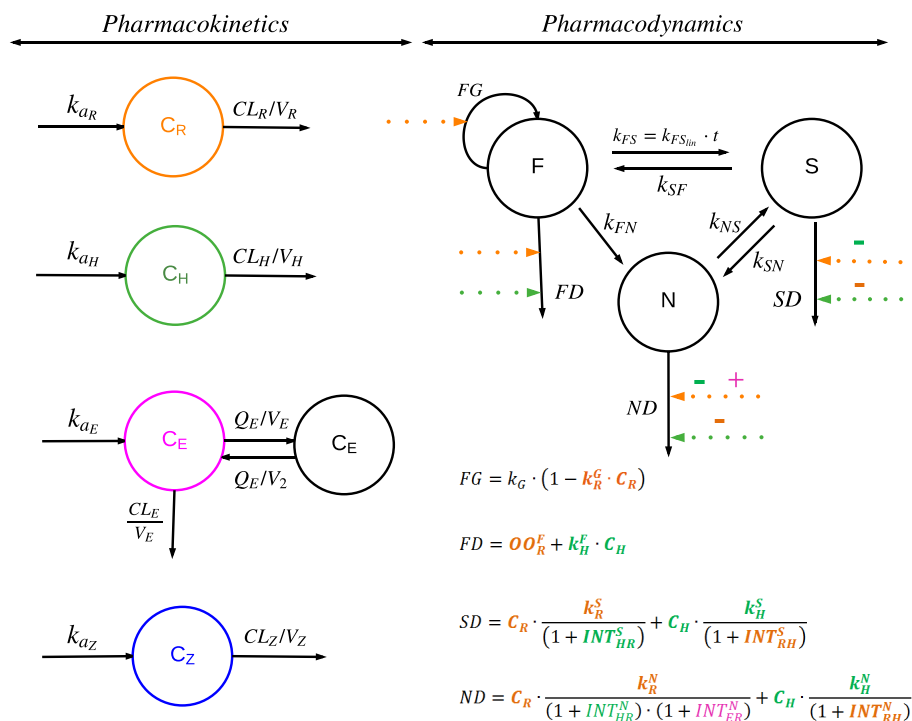
### Exposure-response relationships for mono drug therapy

The final MTP model included rifampicin mono drug effects on inhibition of the growth of F, and stimulation of the death of F, S, and N, as well as isoniazid mono drug exposure-response relationships as linear death rates of both F and S. Isoniazid effect on stimulation of the death of N was identified in  $R_{10}H_{25}Z_{150}$  using a linear function, which was not identifiable in isoniazid monotherapy and  $R_{10}H_{25}$  combination. All equations of mono drug effects are shown in Figure 1.

Due to a lack of longitudinal CFU data on ethambutol and pyrazinamide during monotherapy, the mono drug effects of these drugs could not be quantified.

### General pharmacodynamic interaction model

The GPDI model was linked to the MTP model for the evaluation of PD interactions using combination therapies. Rifampicin and isoniazid decreased their respective potencies on jointly killing S ( $INT_{RH}^S$ ) and N ( $INT_{RH}^N$ ).  $INT_{RH}^S$  and  $INT_{RH}^N$  were estimated to 4.49 and 0.32, respectively, which can be interpreted as a 4.49-fold or 0.32-fold decrease in the efficacy slope of rifampicin and isoniazid, respectively (Supplementary Material S2). This potency shift leads to 0.86 log<sub>10</sub> CFU/lungs higher CFU at 28 days after treatment compared to the expected additivity of the two drugs based on monotherapy alone (i.e., PD antagonism was observed on the biomarker level (Figure 2)). Figure 3 illustrates simulations from the final MTP-GPDI model and revealed that antagonistic interactions between rifampicin and isoniazid were more relevant in the lower dose range



**Figure 1** Schematic illustration of the final population pharmacokinetic (PK) models and the final Multistate Tuberculosis Pharmacometric model consisting of fast (F), slow (S), and non-multiplying (N) bacterial states linked to the General Pharmacodynamic Interaction model. The bacterial system was described with a growth rate of F ( $k_G^F$ ), a time-dependent linear rate parameter describing transfer rate from fast to slow-multiplying bacteria ( $k_{FS}$ ), first-order transfer rate from slow to fast-multiplying state ( $k_{SF}$ ), first-order transfer rate from fast to non-multiplying state ( $k_{FN}$ ), first-order transfer rate from slow to non-multiplying state ( $k_{SN}$ ), and first-order transfer rate from non to slow-multiplying state ( $k_{NS}$ ). The final PK models of rifampicin (R; in orange), isoniazid (H; in green), ethambutol (E; in purple) and pyrazinamide (Z; in blue) are shown where the absorption rate constant ( $k_a$ ), clearance (CL), volume of distribution of the central and peripheral compartment (V and V<sub>2</sub>) and intercompartmental clearance (Q) are specified for different drugs with subscription. The monotherapy drug effects are shown as dashed lines for rifampicin (in orange), isoniazid (in green), ethambutol (in purple), and pyrazinamide (in blue) affecting the inhibition of the growth of fast-multiplying bacteria (FG) and stimulation of the death of fast-multiplying bacteria (FD), slow-multiplying bacteria (SD), or non-multiplying bacteria (ND). The  $k_R^F$  is the linear rifampicin-induced inhibition of fast-multiplying bacteria growth rate in monotherapy. The  $OO_R^F$  is the rifampicin-induced on/off stimulation of fast-multiplying bacteria death rate in monotherapy. The  $k_R^S$  and  $k_R^N$  are rifampicin-induced second-order slow and non-multiplying bacteria death rates, respectively, in monotherapy. The  $k_H^F$ ,  $k_H^S$ , and  $k_H^N$  are isoniazid-induced second-order fast, slow, and non-multiplying bacteria death rates, respectively, in monotherapy. The pharmacodynamic (PD) interactions of rifampicin (R; in orange), isoniazid (H; in green), ethambutol (E; in purple) and pyrazinamide (Z; in blue) are shown as + (synergism) or – (antagonism) on the respective dashed drug effect line.  $INT_{RH}^S$  and  $INT_{RH}^N$  are the PD interactions on stimulation of the death of slow and non-multiplying bacteria, respectively, observed between rifampicin and isoniazid in the combination. The  $INT_{RE}^N$  is the PD interaction on stimulation of the death of non-multiplying bacteria, observed between rifampicin and ethambutol in the combination.

of rifampicin and higher dose range of isoniazid at 28 days after treatment.

Rifampicin and ethambutol increased their potencies ( $INT_{RE}^N = -0.15$ ), as estimated by the GPDI model (**Supplementary Material S2**). The data did not support any PD interaction between ethambutol and pyrazinamide. These PD interactions led to 2.84 log<sub>10</sub> CFU/lungs lower CFU compared to expected additivity between four drugs. PD parameters are shown in **Table 2**. An additive residual error on log scale was used in the final MTP-GPDI model to describe the residual variability using log transformation of both sides.

The differential equation system for F (Eq. 10), S (Eq. 11), and N (Eq. 12) for the final MTP-GPDI model was as follows:

$$\frac{dF}{dt} = FG \cdot F + k_{SF} \cdot S - k_{FS} \cdot F - k_{FN} \cdot F - FD \cdot F \quad (10)$$

$$\frac{dS}{dt} = k_{FS} \cdot F + k_{NS} \cdot N - k_{SF} \cdot S - k_{SN} \cdot S - SD \cdot S \quad (11)$$

$$\frac{dN}{dt} = k_{SN} \cdot S - k_{NS} \cdot N + k_{FN} \cdot F - ND \cdot N \quad (12)$$

where FG and FD are the inhibition of the growth and stimulation of the death of F, and SD and ND are the stimulation of the death of S and N. Detailed equations of FG, FD, SD, and ND are shown in **Figure 1**. The VPCs for no treatment, monotherapies, and combination therapies based on the final models are shown in **Figure 4**. The final model code is available in the **Supplementary Material S3**.

**Table 1** Final population pharmacokinetic parameter estimates for rifampicin, isoniazid, ethambutol, and pyrazinamide in mice

Parameters	Rifampicin		Isoniazid		Ethambutol		Pyrazinamide	
	Typical value	RSE, %	Typical value	RSE, %	Typical value	RSE, %	Typical value	RSE, %
$k_a$ ( $h^{-1}$ )	6.23	21.0	12.6 FIX <sup>a</sup>	-	0.87 FIX <sup>a</sup>	-	2.84 FIX <sup>a</sup>	-
CL/F ( $mL \cdot h^{-1} \cdot kg^{-1}$ )	234	22.4	612 <sup>b</sup>	5.4	3,400	11.0	273.71	15.9
V/F ( $mL \cdot kg^{-1}$ )	706	32.4	811	8.0	1,500	22.3	525.1	22.1
Q/F ( $mL \cdot h^{-1} \cdot kg^{-1}$ )	-	-	-	-	2,530	42.7	-	-
$V_2/F$ ( $mL \cdot kg^{-1}$ )	-	-	-	-	4,690	27.3	-	-
$V_{highest\ dose}/F$ ( $mL \cdot kg^{-1}$ )	1,700	11.6	-	-	-	-	-	-
$CL_{highest\ dose}/F$ ( $mL \cdot h^{-1} \cdot kg^{-1}$ )	94.6	6.3	-	-	-	-	-	-
Slope <sup>s</sup>	-	-	7.50E-03	16.8	-	-	-	-
CL/F ( $mL \cdot h^{-1} \cdot kg^{-1}$ )	54.9	35.3	-	-	-	-	-	-
Proportional residual error	0.0419	13.0	0.0174	23.1	0.135	12.0	0.264	13.2
Additive residual error	7.77	35.0	0.232	25.0	0.0239	38.1		

CL/F, apparent clearance;  $CL_{highest\ dose}/F$ , apparent clearance at the highest dose level of 160 mg/kg of rifampicin; CL/F, apparent clearance of rifampicin in healthy mice;  $k_a$ , absorption rate constant; V/F, apparent volume of distribution in the central compartment;  $V_{highest\ dose}/F$ , apparent volume of distribution at the highest dose of 160 mg/kg of rifampicin;  $V_2/F$ , apparent volume of distribution in the peripheral compartment; Q/F, apparent intercompartmental clearance; RSE, relative standard error reported on the approximate SD scale.

<sup>a</sup> $k_a$  fixed according to Chen *et al.*<sup>10</sup>; <sup>b</sup>CL/F<sub>isoniazid</sub> for the lowest dose; CL/F<sub>isoniazid</sub>, CL/F<sub>lowest dose</sub> · (1 - Slope<sup>s</sup> (Dose - Dose<sub>lowest dose</sub>)).

## DISCUSSION

In this study, we describe the application of the MTP model together with the GPDI model using a BALB/c mouse model in order to describe untreated mice or mice treated with rifampicin, isoniazid, ethambutol, and pyrazinamide. The major focus of the work was the assessment of PD interactions using a model-based approach, which could be applied to both mono and combination therapies of antitubercular drugs and the biomarker CFU data.

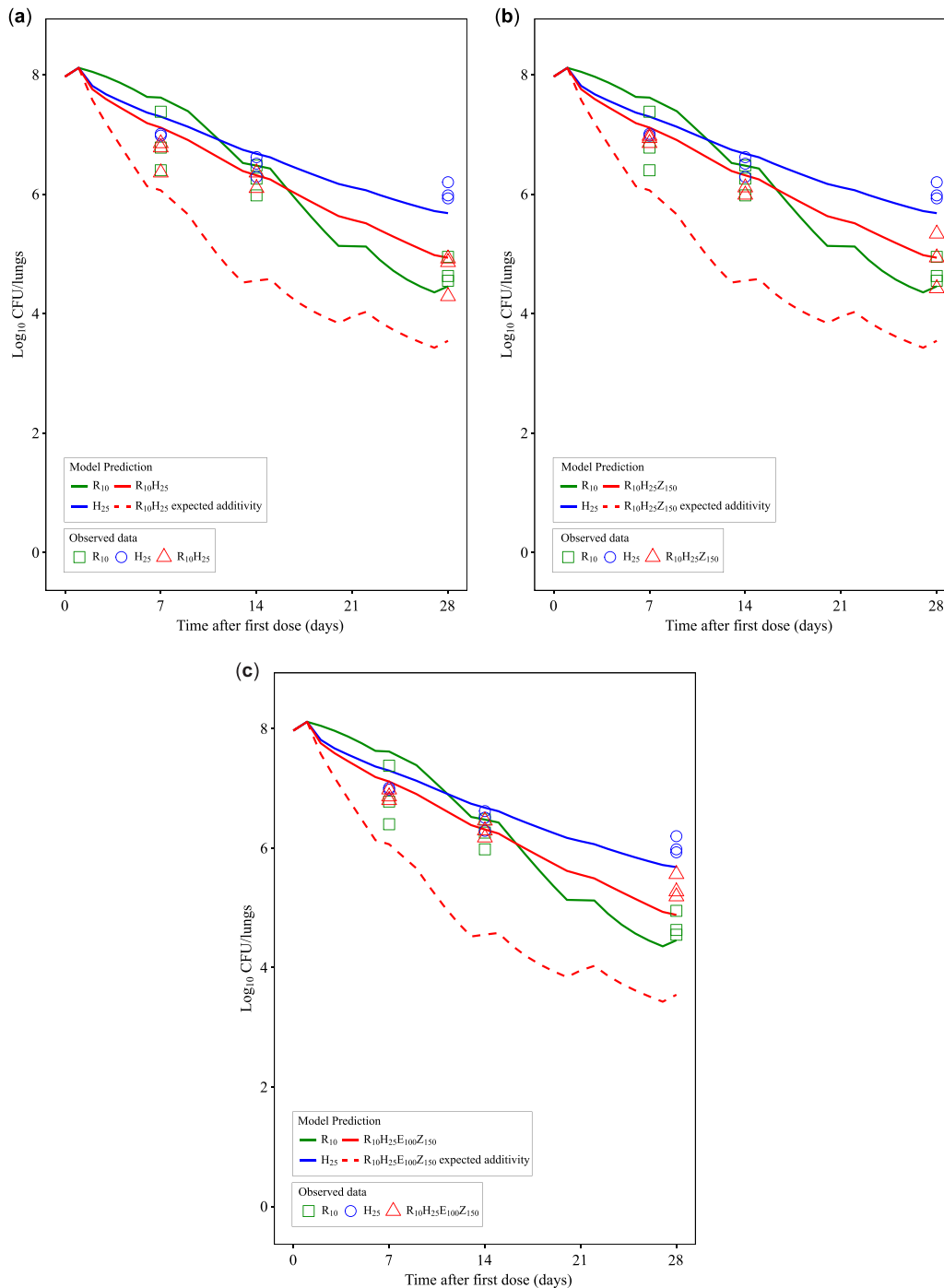
To go beyond simple dose-response characterization, we included PK information to characterize the (joint) exposure-response relationship of the antitubercular drugs studied. To our knowledge, for the first time, our modeling approach quantified that rifampicin CL/F in TB-infected mice treated for 4 weeks is three times higher than in healthy mice treated for 3 weeks. This difference is potentially due primarily to different disease status, but auto-induction of rifampicin may also contribute to some degree. The mechanism of action on dose-dependent V/F of rifampicin and isoniazid is unknown.

Exposure-response relationships were characterized in monotherapies by the MTP model. We fixed the transfer rate between each bacterial state according to an earlier *in vitro* study,<sup>4</sup> except  $k_{FS}$ , which was re-estimated as a linear function of time. This provided a significant drop in OFV whereas re-estimation of the other rate constants was not significant. The CFU data in this study did not contain enough information about transfer from the other bacterial states, which was evident in the *in vitro* data. It has been demonstrated that the decline in CFU after 60 days of *in vitro* incubation is not due to bacterial death. Instead, it is due to the fact that the bacilli entered into persistent stage *in vitro* and *in vivo*, which can only be woken up by resuscitation-promoting factors.<sup>20</sup> Natural growth rate ( $k_G$ ) of F was described by an exponential function, due to lack of plateau information on the bacterial burden. A similar approach to using (fixing) *in vitro* information about transfer

between bacterial states was used in a previous study in the acute C57BL/6 mouse model,<sup>5</sup> and in the other study as well.<sup>21</sup> To treat drug-susceptible TB, ethambutol is the last drug added in the combination of rifampicin, isoniazid, and pyrazinamide. The major role of ethambutol is to prevent drug resistance in the combination therapy.<sup>22</sup> Pyrazinamide is effective to the bacterial subpopulation in acid pH conditions in the lesions.<sup>23</sup> However, there is no lesion in BALB/c mouse model.<sup>24</sup> Therefore, no effects of ethambutol and pyrazinamide were observed in monotherapy in this study.

Pharmacological synergism and antagonism are usually defined as greater or less than additive effect (additivity) of combined drugs. Loewe Additivity and BI are two major competing definitions of additivity. Empirical parametric interaction approaches, for instance, by using a power function<sup>25</sup> or the Greco model,<sup>26</sup> have been used to quantify how PD interactions lead to differences from additivity. However, results from these models are more difficult to interpret, as their interaction parameters have no quantitative meaning and only assess monodimensional symmetric interaction with single interaction parameter, limited to two drugs in combination and a single underlying additivity criterion.

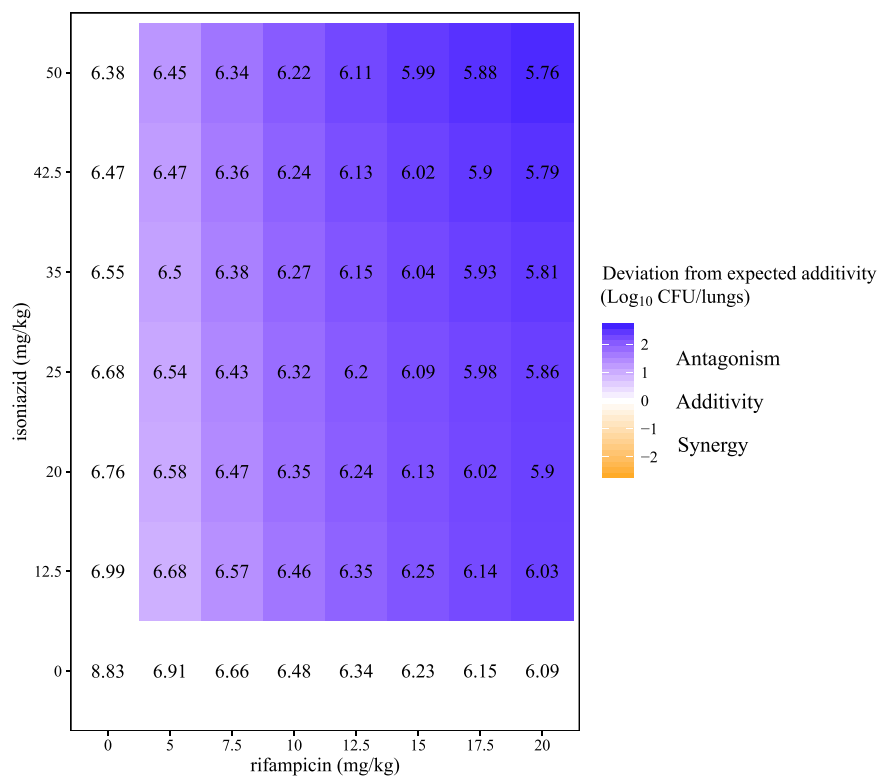
This study quantified, we believe for the first time, the observed *in vivo* PD interactions in combination therapies by using the GPDI model.<sup>3</sup> Both BI and Loewe Additivity are compatible with the GPDI model, which makes the GPDI model approach more flexible than previously described approaches. As our studies emphasize, the GPDI model based on BI is not limited to the two drugs in combination therapies. A property of the GPDI approach is that asymmetric interactions can be quantified (i.e., a different effect of drug A on drug B and vice versa), as shown in **Supplementary Material S4**. In our study, asymmetric interactions were not characterized, due to the single-dose level of each drug in the combination therapy, which led to the assumption of an on/off effect only estimating  $INT_{AB}$ , instead of an  $E_{max}$



**Figure 2** Predicted change from baseline of  $\log_{10}$  colony-forming unit (CFU)/lungs after mono and combination therapies based on the final Multistate Tuberculosis Pharmacometric-General Pharmacodynamic Interaction model (solid lines) compared to model-predicted expected additivity (dotted lines) after 10 mg/kg rifampicin monotherapy (R<sub>10</sub>), 25 mg/kg isoniazid monotherapy (H<sub>25</sub>), combination therapy of 10 mg/kg rifampicin and 25 mg/kg isoniazid (R<sub>10</sub>H<sub>25</sub>), combination therapy of 10 mg/kg rifampicin, 25 mg/kg isoniazid, and 150 mg/kg pyrazinamide (R<sub>10</sub>H<sub>25</sub>Z<sub>150</sub>), combination therapy of 10 mg/kg rifampicin, 25 mg/kg isoniazid, 150 mg/kg pyrazinamide, and 100 mg/kg ethambutol (R<sub>10</sub>H<sub>25</sub>Z<sub>150</sub>E<sub>100</sub>). Observed data are given as symbols. The data did not support any drug effect from pyrazinamide or ethambutol in monotherapy. The fluctuations in response are due to drug treatments in 5 of 7 days per week.

function, which represents a limitation of our study originating from the sparse experimental data. Scalability of the GPDI approach to different levels of complexity (i.e., using the full four-parameter model or a reduced single parameter

model) is a key advantage of this approach over the conventional approaches. Moreover, interaction parameters are interpretable in the GPDI approach as fractional changes of the PD parameter (i.e., change of the slope in the present



**Figure 3** Predicted log<sub>10</sub> colony-forming unit (CFU)/lungs in numbers and log<sub>10</sub> CFU/lungs deviation from expected additivity (in shaded areas) for rifampicin and isoniazid in different combinations at 28 days after treatment. White areas in the figure show expected additivity, whereas blue shaded areas show higher log<sub>10</sub> CFU/lungs (antagonism) than expected additivity, and orange shaded areas show lower log<sub>10</sub> CFU/lungs (synergism) than expected additivity.

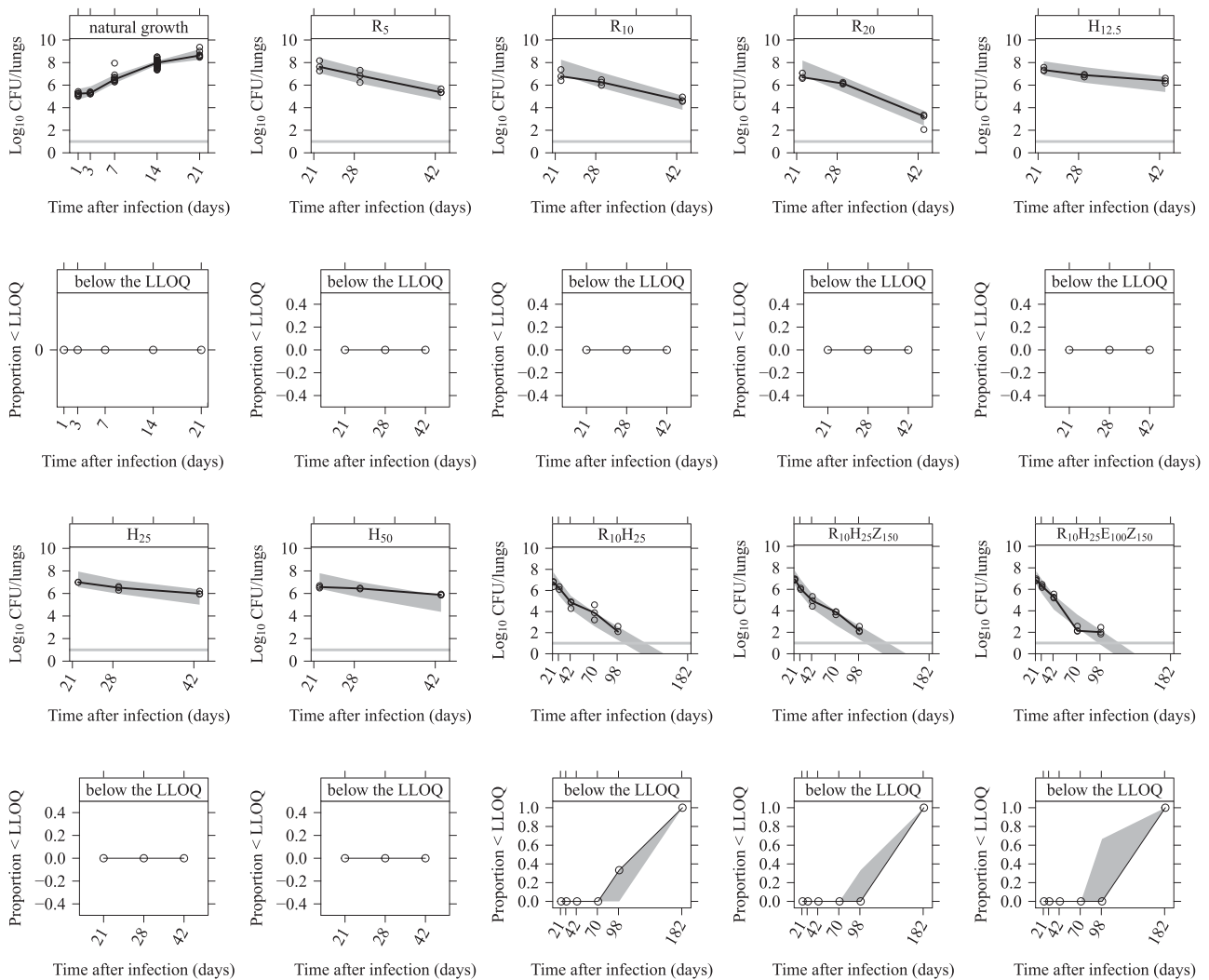
**Table 2** Pharmacodynamic parameter estimates of the final Multistate Tuberculosis Pharmacometric-General Pharmacodynamic Interaction model

Parameter	Description	Typical value	RSE, %
<b>The MTP model</b>			
$F_0$ (lungs <sup>-1</sup> )	Initial fast-multiplying bacterial number	20,100	59.2
$S_0$ (lungs <sup>-1</sup> )	Initial slow-multiplying bacterial number	119,000	31.0
$k_G$ (h <sup>-1</sup> )	Growth rate of the fast-multiplying bacteria	0.034	10.0
$k_{FS_{in}}$ (h <sup>-2</sup> )	Time-dependent transfer rate from fast-multiplying to slow-multiplying bacterial state	$6.65 \cdot 10^{-5}$	20.3
$k_{SF}$ (h <sup>-1</sup> )	First-order transfer rate from slow to fast-multiplying bacterial state	$6.03 \cdot 10^{-4}$ FIX <sup>a</sup>	
$k_{FN}$ (h <sup>-1</sup> )	First-order transfer rate from fast to non-multiplying bacterial state	$3.74 \cdot 10^{-8}$ FIX <sup>a</sup>	
$k_{SN}$ (h <sup>-1</sup> )	First-order transfer rate from slow to non-multiplying bacterial state	$7.73 \cdot 10^{-3}$ FIX <sup>a</sup>	
$k_{NS}$ (h <sup>-1</sup> )	First-order transfer rate from non to slow-multiplying bacterial state	$5.11 \cdot 10^{-5}$ FIX <sup>a</sup>	
$k_R^G$	Linear rifampicin-induced inhibition of fast-multiplying bacteria growth rate	0.0022	29.2
$OO_R^E$ (h <sup>-1</sup> )	Rifampicin-induced on/off stimulation of fast-multiplying bacteria death rate	0.019	4.2
$k_R^S$ (mL·h <sup>-1</sup> ·μg <sup>-1</sup> )	Rifampicin-induced second-order slow-multiplying bacteria death rate	0.0137	15.8
$k_R^N$ (mL·h <sup>-1</sup> ·μg <sup>-1</sup> )	Rifampicin-induced second-order non-multiplying bacteria death rate	0.0033	8.0
$k_H^F$ (mL·h <sup>-1</sup> ·μg <sup>-1</sup> )	Isoniazid-induced second-order fast-multiplying bacteria death rate	0.055	15.6
$k_H^S$ (mL·h <sup>-1</sup> ·μg <sup>-1</sup> )	Isoniazid-induced second-order slow-multiplying bacteria death rate	0.00047	53.6
$k_H^N$ (mL·h <sup>-1</sup> ·μg <sup>-1</sup> )	Isoniazid-induced second-order non-multiplying bacteria death rate	0.0012	5.0
<b>The GPDI model</b>			
$INT_{RH}^S$	Interaction between rifampicin and isoniazid on stimulation of the death of slow-multiplying bacteria	4.49	28.1
$INT_{RH}^N$	Interaction between rifampicin and isoniazid on stimulation of the death of non-multiplying bacteria	0.32	38.0
$INT_{RE}^N$	Interaction between rifampicin and ethambutol on stimulation of the death slow-multiplying bacteria	-0.15	57.7
$\sigma^2$	Additive residual variability on log scale (variance)	1.23	16.7

E, ethambutol; F, fast-multiplying bacteria; H, isoniazid; N, non-multiplying bacteria; R, rifampicin; RSE, relative standard error reported on the approximate standard deviation scale; S, slow-multiplying bacteria.

<sup>a</sup>Fixed to estimates from application of the MTP model *in vitro* by Clewe *et al.*<sup>4</sup> 2016.





**Figure 4** Visual Predictive Check of the final Multistate Tuberculosis Pharmacometric model linked to the General Pharmacodynamic Interaction model applied to colony forming unit (CFU) data from a tuberculosis-infected experimental mouse model without treatment (natural growth) and with different drug treatments. Data above the lower limit of quantification (LLOQ) are shown in plots in the first and third rows, and the horizontal lines represent the LLOQ in plots in the first and third rows. The solid lines are the medians of the observations and open circles are the observations. Light gray shaded areas represent 95% confidence intervals for the medians. Data below the LLOQ are shown in plots in the second and fourth rows where the solid lines are the medians of the LLOQ data. Light gray shaded areas represent 95% confidence intervals for the medians of the LLOQ data. R<sub>5</sub>, R<sub>10</sub>, and R<sub>20</sub> represent 5, 10, and 20 mg/kg of rifampicin monotherapy. H<sub>12.5</sub>, H<sub>25</sub>, and H<sub>50</sub> represent 12.5, 25, and 50 mg/kg of isoniazid monotherapy. R<sub>10</sub>H<sub>25</sub>, R<sub>10</sub>H<sub>25</sub>Z<sub>150</sub>, and R<sub>10</sub>H<sub>25</sub>E<sub>100</sub>Z<sub>150</sub> are different combinations using 10 mg/kg of rifampicin, 25 mg/kg of isoniazid, 150 mg/kg of pyrazinamide, and 100 mg/kg of ethambutol.

study). The PD interactions on the death rate of S ( $INT_{RH}^S$ ) and N ( $INT_{RH}^N$ ) between rifampicin and isoniazid were identified and presented in **Figure 2** in solid and dashed red lines, illustrating prediction from the final MTP-GPDI model with quantified, observed interaction and model-predicted expected additivity based on the monotherapies. In R<sub>10</sub>H<sub>25</sub>Z<sub>150</sub>, isoniazid was shown to stimulate the death rate of N as well, which was not identified in monotherapy. There are some implications to consider when interpreting isoniazid effect on the N bacterial state. Due to the different length of the exposure-response experiments (i.e., 4-week mono drug treatments vs. 24-week combination treatments),

the composition of the bacterial burden was quite different, with a much higher number of N bacteria in the 24-week experiment compared to the 4-week experiment. However, isoniazid effect on the N bacterial state was not identified in R<sub>10</sub>H<sub>25</sub> either, but solely in the presence of pyrazinamide in the triple combination, even though there was no pyrazinamide effect identified from monotherapy. Still, because of the lack of data on isoniazid mono effects at later time points, we could not clearly distinguish whether pyrazinamide triggered the isoniazid effect on N bacterial state or if this effect was an effect of isoniazid alone. This aspect of our work underscores the importance of defining the same setting of

experiments for drug efficacy evaluation in monotherapy and in assessing PD interactions in combinations. In the report from Grosset *et al.*,<sup>27</sup> the combination of isoniazid and rifampin was bactericidal to a similar magnitude as the combination of isoniazid, rifampicin, and pyrazinamide, but both of those two combinations were less effective than the one combining rifampin and pyrazinamide. They concluded that there was antagonism between isoniazid and the combination of rifampicin and pyrazinamide in mice. Later studies by Almeida *et al.*<sup>28</sup> reported that the antagonism between isoniazid and the combination of rifampin and pyrazinamide was dependent on the dose of isoniazid. Increasing the dose of isoniazid alone resulted in a better antimicrobial effect. Conversely, increasing the dose of isoniazid in the combination of rifampicin and pyrazinamide resulted in a lower antimicrobial effect. Our model-based approach matches these observations, but surpasses these results by providing quantitative measures to describe PD interactions (i.e., our model predicted a 0.86 log<sub>10</sub> CFU/lungs higher bacterial load, compared to an expected additivity in R<sub>10</sub>H<sub>25</sub>). An antagonistic interaction (less effect than expected additivity) between isoniazid and rifampicin was found in this work (**Figure 2a** and **Figure 3**) which is an agreement with clinical early bacterial activity data from day 0–14, as reported by Jindani *et al.*<sup>29</sup> A synergistic interaction on N state bacteria was identified between rifampicin and ethambutol in this work. This interaction was only quantifiable by using the GPDI approach, which can capture interactions between active and inactive drugs, as interactions are quantified as shift of a PD parameter and not on the effect level. However, mono effects and interactions arising from ethambutol could not formally be differentiated using the data, because there was no longitudinal CFU data from mice receiving ethambutol alone, as these mice became moribund due to a lack of early ethambutol mono effects. This implies that, in future studies, higher doses of ethambutol should be studied to establish a complete exposure-response relationship also in monotherapy. This would allow evaluating longer monotherapy time-courses to clearly distinguish between mono and combination effects of ethambutol at later time points of therapy.

Using the MTP model together with the GPDI model, this study provides estimates of single drug effects together with a quantitative model-based evaluation framework for PD interactions among antitubercular drugs in TB drug development.

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