

# ON THE EFFICIENCY OF STORMWATER DETENTION TANKS IN POLLUTANT REMOVAL

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## ABSTRACT

In the design of a stormwater detention tank is important to guarantee a sufficient retention time for the sedimentation of suspended solids, the biological uptake of nutrients and the die-off of bacteria carried in rainwaters. Long retention times increase the capacity of pollutant removal, but also the possibility of spills in downstream receivers and the risk of environmental pollution. In this paper, an analytical probabilistic approach, to estimate the probability distribution function of the average retention time and the efficiency in pollutant removal of stormwater tanks has been proposed. The possibility of water mixing from consecutive runoff events and storage carryover due to successive rainfall events has been considered. The method has been applied to a case study in Milano, Italy.

*Keywords:* analytical probabilistic approach, environmental pollution control, stormwater detention tanks.

## 1 INTRODUCTION

Detention tanks are often used in modern urban drainage systems to achieve both quantitative and qualitative control of stormwater runoff. The first goal is achieved by storing part of runoff to reduce overflows to receiving water bodies; the second by ensuring proper water retention times.

The two goals are in conflict with each other since the growth of retention time increases the probability of spills from the tank. A proper design should consider both these aspects, also trying to limit costs [1–4].

The key point is the definition of an optimal retention time. For simplicity, many governments suggest the use of a drawdown time (time to drain a full storage) in the range of 24–48 h. This assumption has been supported by different studies that concluded that shorter retention times could be not sufficient to allow a good sedimentation of most of suspended solids, while longer retention times are useless because most of particles contained in stormwaters sediment in few days [5]. Moreover, long retention times can cause smell problems resulting from the combination of wastewater quality, temperature and time [6]. Other studies on retention time [7, 8], observed that it also depends on the size of particles and concluded that a retention time of 24 h can remove most of particles less than 10  $\mu\text{m}$  diameter and all the particles larger than 10  $\mu\text{m}$ .

Although retention time is often regarded as a deterministic parameter [9–12], many authors have observed that it should be considered a random variable [13–15]. Therefore, also tank efficiency in pollution removal should be considered as a random variable.

In this paper, an analytical probabilistic approach is proposed, for the estimation of the probability distribution function of the average retention time to be used for the tank efficiency

estimation. The goal is, starting from a more rigorous definition of average retention time consider the possibility of spill when the volume is full and the possibility of water mixing from consecutive rainfalls due to pre-filling of the storage from previous events.

Final expressions have been applied on a case study in Milano, Italy; the series of rainfall data recorded at Milano-Monviso gauge station in the period 1991–2005 has been used. Results from the proposed method have been compared with those obtained from the continuous simulation of observed data.

## 2 TANK EFFICIENCY

Efficiency of a detention tank in terms of pollutant removal can be defined as the fraction of inflow particles that are trapped inside. A particle is trapped when its retention time, defined as the time passed inside the tank before overflow or sedimentation, is greater than or equal to the time of sedimentation, defined as the time needed to reach the tank bottom.

If sedimentation is supposed to be mainly driven by gravity and interaction among particles is neglected, the vertical component of velocity  $V_s$  for a particle of diameter  $D$  is expressed by the Stokes equation:

$$V_s(D) = \frac{g \cdot (\rho_p - \rho) \cdot D^2}{18 \cdot \mu} \quad (1)$$

Where  $\rho_p$  and  $\rho$  are the densities of particles and water and  $\mu$  is the cinematic viscosity of water.

Considering the velocity expressed by eqn (1) as a mean value of a time variant physical quantity, the time required to a particle on the water surface to settle on the tank bottom  $t_s$  is simply equal to the ratio:

$$t_s(D) = \frac{H}{V_s(D)} \quad (2)$$

where  $H$  is the water depth.

Equating  $t_s(D)$  to an assumed retention time  $t_r$ , the limit diameter  $D_o$  can be calculated as:

$$D_o = \left[ \frac{18 \cdot \mu \cdot H}{g \cdot (\rho_p - \rho) \cdot t_r} \right]^{1/2} \quad (3)$$

All the particles with a diameter  $D \geq D_o$  have a sedimentation time smaller than or equal to the retention time  $t_r$  and so are trapped. The fraction of these particles can be estimated by field sieve analysis or from literature data on sediments in stormwater runoff. The others can be trapped or not according to their distance from the tank bottom.

Assuming a uniform distribution along the water depth of particle number of each diameter, the fraction of particles  $r_s$  with  $D < D_o$  that is trapped is equal to:

$$r_s(D) = \frac{h_m(D)}{H} = \frac{t_r \cdot V_s(D)}{t_r \cdot V_s(D_o)} = \frac{V_s(D)}{V_s(D_o)} = \left( \frac{D}{D_o} \right)^2 \quad (4)$$

where  $h_m$  is the distance from the tank bottom for which a particle with  $D < D_o$  has a sedimentation time equal to  $t_r$ .

Tank efficiency in particle removal can then be calculated by the following relationship:

$$E = (1 - F_o) + \frac{1}{D_o^2} \cdot \int_0^{D_o} D^2 \cdot f_D(x) \cdot dx \quad (5)$$

where  $F_o$  is the fraction of particles with a diameter smaller than  $D_o$  and  $f_D(x)$  is the slope of the tangent of the particle gradation curve.

From the combination of eqns (3) and (5) results that the tank efficiency  $E$  is a function of the retention time  $t_R$ . If inflow and outflow are equal and time invariant, as in steady flow sedimentation tanks, this time is constant and simply calculated by the relationship:

$$t_R^* = \frac{B \cdot H \cdot L}{Q} = \frac{W_o}{Q} \quad (6)$$

where  $B$  and  $L$  are the tank width and the length and  $Q$  the constant flow.

Stormwater tanks, however, are characterized by variable inflow and outflow, causing a continuous process of filling and emptying. So, retention time is also variable and often an average value is considered, depending on inflow and outflow pattern.

Due to hydrologic processes of rainfall-runoff transformation acting on the upstream urban catchment, both this average retention time and the related tank efficiency can be regarded as random variables.

It has to be highlighted that using an average retention time implies also that the tank efficiency given by eqn (5) should be considered as an 'average' too.

In the next paragraph, the probability distribution of average retention time is derived, to be used together with eqn (5) to achieve a probabilistic estimation of this 'average' tank efficiency.

### 3 PROBABILITY DISTRIBUTION FUNCTION OF AVERAGE RETENTION TIMES

In the estimation of the probability distribution function of average retention times some assumptions for the simplification of the analytical probabilistic model have been made:

- On-line stormwater detention tank;
- Inflows have been considered of constant intensity (rectangular events);
- Constant outflows rate  $Q_o(t) = q$ ;
- Runoff volume for unit of catchment surface  $v$  has been assumed equal to rainfall depth  $h$  less than an Initial Abstraction  $IA$  multiplied by the runoff coefficient  $\phi$ , that is  $v = \phi \cdot (h - IA)$ ;
- Rainfall-runoff transformation has been neglected, as typical for small catchments with short corrivation times. For highly urbanized catchment where  $IA$  tends to zero and  $\phi$  tends to one, runoff volume can be considered equal to rainfall volume,  $v = h$  and runoff duration can be assumed equal to rainfall duration;
- Use of the Inter Event Time Definition  $IETD$ , to isolate independent rainfall events from the continuous chain of storms: if the dry time between two consecutive rainfall events is smaller than  $IETD$ , the two events have been joined together into a single event, otherwise they have been considered independent;
- Exponential distribution of the hydrological variables involved in the storage process (rainfall depth  $h$  and duration  $\theta$ , interevent time  $d$ ):

$$f_h = \xi \cdot e^{-\xi \cdot h} \quad (7)$$

$$f_\theta = \lambda \cdot e^{-\lambda \cdot \theta} \quad (8)$$

$$f_d = \psi \cdot e^{-\psi \cdot (d - IETD)} \quad (9)$$

where  $\xi = 1/\mu_p$ ,  $\lambda = 1/\mu_\theta$  and  $\psi = 1/(\mu_d \cdot IETD)$ , with  $\mu_h$ : average rainfall depth,  $\mu_\theta$ : average rainfall duration,  $\mu_d$ : average interevent time.

To estimate the probability distribution function of average retention times, care must be taken to the definition of retention time. If the hypothesis of plug flow (flow parcels leave the basin in the same order they entered) and completely mixed flow are considered, the average retention time  $\bar{t}_R$  can be calculated as the difference between the average release time  $\bar{t}_O$  and the average input time  $\bar{t}_I$  that is the horizontal distance between centroids of inflow and outflow hydrographs:

$$\bar{t}_R = \bar{t}_O - \bar{t}_I \tag{10}$$

On the assumption of independence of inflow and outflow hydrograph, eqn (10) can be simplified as follow:

$$\begin{aligned} \bar{t}_R &= \bar{t}_O - \bar{t}_I = \int_0^{t_o} \tau_o \cdot f_{\tau_o}(\tau_o) \cdot d\tau_o - \int_0^{t_i} \tau_i \cdot f_{\tau_i}(\tau_i) \cdot d\tau_i = \\ &= \frac{1}{V_o} \cdot \int_0^{t_o} \tau \cdot Q_o(\tau) \cdot d\tau - \frac{1}{V_i} \cdot \int_0^{t_i} \tau \cdot Q_i(\tau) \cdot d\tau \end{aligned} \tag{11}$$

$t_o$ : release time, that coincides with emptying time;

$t_i$ : input time;

$V_o$ : outflow volume;

$V_i$ : inflow volume;

$Q_o$ : outflow rate;

$Q_i$ : inflow rate.

For constant outflow rate,  $Q_o(\tau) = q = \text{const.}$ , the average release time results:

$$\bar{t}_O = \frac{1}{V_o} \cdot \int_0^{t_o} \tau \cdot Q_o(\tau) \cdot d\tau = \frac{1}{t_o \cdot q} \cdot \frac{1}{2} \cdot t_o^2 \cdot q = \frac{1}{2} \cdot t_o \tag{12}$$

If even inflow rate is constant during the event,  $Q_i(\tau) = q_i = \text{const.}$ , the average inflow time results:

$$\bar{t}_I = \frac{1}{V_i} \cdot \int_0^{t_i} \tau \cdot Q_i(\tau) \cdot d\tau = \frac{1}{t_i \cdot q_i} \cdot \frac{1}{2} \cdot t_i^2 \cdot q_i = \frac{1}{2} \cdot t_i \tag{13}$$

Considering the simplifying hypothesis of eqns (11)–(13) becomes:

$$\bar{t}_R = \frac{1}{2} \cdot (t_o - t_i) = \frac{1}{2} \cdot t_o \cdot \left( 1 - \frac{t_i}{t_o} \right) = \frac{1}{2} \cdot t_o \cdot \left( 1 - \frac{q}{q_i} \right) \tag{14}$$

Sometimes, the tank is not completely empty when a new runoff event occurs, that is there is a carryover from previous runoffs. Obviously, the probability of pre-filling increases when outflow rate is low, as in the case of tanks for the enhancement of water quality (e.g. first flush tanks). For this reason, in the estimation of the probability distribution function of average

retention times the possibility of water mixing from two consecutive runoffs has been considered.

In the following, specific variable (for unit of area) have been used. For a couple of consecutive runoffs  $i$  and  $i+1$ , if  $w$  is the storage volume and  $q$  the constant outflow rate, two different conditions can occur:

- $w/q \leq IETD$ : the possibility of pre-filling of the storage volume from the event  $i$  at the beginning of the event  $i+1$  is excluded;
- $w/q > IETD$ : the storage volume could be not completely empty from the event  $i$  at the beginning of the event  $i+1$  and pre-filling could occur.

In case there is no water carryover from event  $i$  storage volume is completely empty at the beginning of event  $i+1$  ( $t_0 < \theta_i + d_i$ ), as shown in Fig. 1.

If the active volume is partially filled at the beginning of event  $i+1$  (Fig. 2), water mixing from two consecutive events has to be considered in the derivation of the probability distribution function of average retention times.

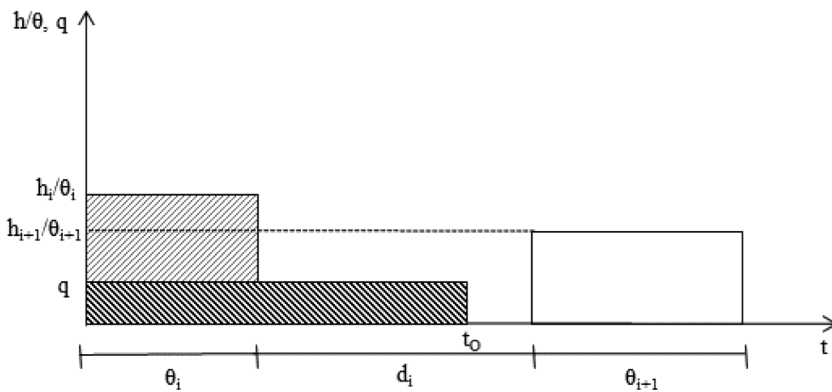


Figure 1: Couple of runoffs without pre-filling.

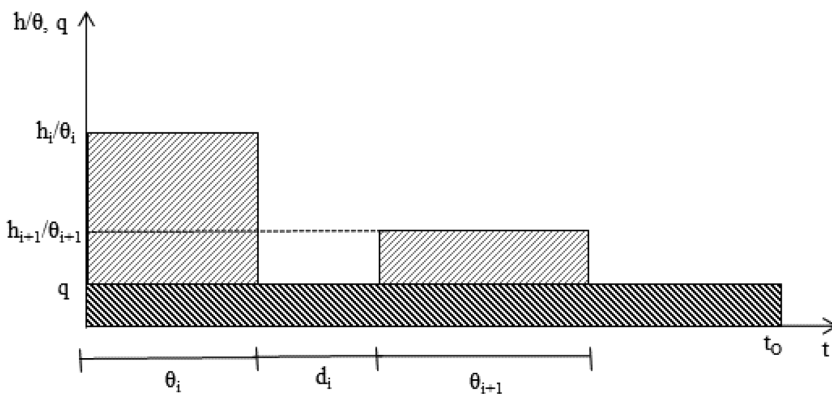


Figure 2: Couple of runoffs with pre-filling.

Generally inflow rates can be higher or lower than outflow rates; in the first case, the possibility of spills if storage volume is full at the end of each event has been considered.

### 3.1 Condition $w/q \leq \text{IETD}$ : pre-filling is excluded

In this case, inter-event time is always enough to have no prefilling and events are independent. The inflow time  $t_i$  coincides with the runoff duration  $\theta$ , so that eqn (14) becomes:

$$\bar{t}_R = \frac{1}{2} \cdot (t_o - \theta) \tag{15}$$

The emptying time  $t_o$  can be expressed by:

$$t_o = \begin{cases} 0 & h_i - q \cdot \theta_i \leq 0 \\ h_i / q & 0 < h_i - q \cdot \theta_i < w \\ \theta_i + w / q & h_i - q \cdot \theta_i \geq w \end{cases} \tag{16}$$

Substituting eqn (11) in eqn (10), the average retention time results:

$$\bar{t}_R = \frac{1}{2} \cdot \begin{cases} 0 & h_i - q \cdot \theta_i \leq 0 \\ h_i / q - \theta_i & 0 < h_i - q \cdot \theta_i < w \\ w / q & h_i - q \cdot \theta_i \geq w \end{cases} \tag{17}$$

It has to be observed that the average retention time has an upper limit, equal to  $(w/q)/2$ , and its probability distribution function is truncated in the upper tail. From eqns (17), the probability that the average retention time is greater than a fixed value  $t_x$  is then expressed as:

$$\begin{aligned} F_{\bar{t}_R} &= P(t_x < \bar{t}_R) = P\left(t_x < \bar{t}_R < \frac{w}{2 \cdot q}\right) + P\left(\bar{t}_R = \frac{w}{2 \cdot q}\right) \\ &= \int_{\theta=0}^{\infty} f_{\theta} \cdot d\theta \cdot \int_{h=q(\theta+2 \cdot t_x)}^{w+q\theta} f_h \cdot dh + \int_{\theta=0}^{\infty} f_{\theta} \cdot d\theta \cdot \int_{h=w+q\theta}^{\infty} f_h \cdot dh = \frac{e^{-2\xi q t_x}}{1+q^*} \end{aligned} \tag{18}$$

and  $q^* = \xi \cdot q / \lambda$ .

### 3.2 Condition $w/q > \text{IETD}$ : possibility of pre-filling

In case of pre-filling from event  $i$  at the beginning of event  $i+1$ , the average input time  $\bar{t}_i$  can be expressed by:

$$\begin{aligned} \bar{t}_i &= \frac{1}{V_i} \cdot \int_0^{\tau_i} \tau \cdot Q_i(\tau) \cdot d\tau = \frac{1}{V_i} \cdot \left[ Q_{i,i} \int_0^{\theta_i} \tau \cdot d\tau + Q_{i,i+1} \int_{\theta_i+d_i}^{\theta_i+d_i+\theta_{i+1}} \tau \cdot d\tau \right] = \\ &= \frac{h_i \cdot \theta_i / 2 + h_{i+1} \cdot (\theta_i + d_i + \theta_{i+1} / 2)}{h_i + h_{i+1}} \end{aligned} \tag{19}$$

Equation (11) in this case results:

$$\bar{t}_R = \bar{t}_0 - \bar{t}_I = \frac{1}{2} \cdot \left[ t_0 - \frac{h_i \cdot \theta_i + h_{i+1} \cdot (2 \cdot \theta_i + 2 \cdot d_i + \theta_{i+1})}{h_i + h_{i+1}} \right] \quad (20)$$

The emptying time  $t_0$  can be expressed by:

$$t_0 = \begin{cases} 0 & \text{case I} \\ h_i / q & \text{cases II - III - IV} \\ w / q + \theta_i & \text{cases V - VII} \\ w / q + \theta_{i+1} & \text{case VI} \\ (h_i + h_{i+1}) / q & \text{case VIII} \\ \theta_i + d_i + \theta_{i+1} + w / q & \text{cases IX - X} \\ \theta_i + (w + h_{i+1}) / q & \text{case XI} \end{cases} \quad (21)$$

*case I* – Rainfall intensity lower than outflow rate:

$$h_i - q \cdot \theta_i \leq 0; h_{i+1} - q \cdot \theta_{i+1} \leq 0$$

*case II* – No pre-filling, event  $i$  without spills:

$$0 < h_i - q \cdot \theta_i \leq w; h_i - q \cdot \theta_i - q \cdot d_i \leq 0;$$

*case III* – Intensity of event  $i$  lower than outflow rate, event  $i+1$  without spills:

$$h_i - q \cdot \theta_i \leq 0; 0 < h_{i+1} - q \cdot \theta_{i+1} \leq w;$$

*case IV* – Pre-filling, event  $i$  without spills, event  $i+1$  with intensity lower than outflow rate:

$$0 < h_i - q \cdot \theta_i \leq w; h_i - q \cdot \theta_i - q \cdot d_i > 0; h_i - q \cdot \theta_i - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} \leq 0;$$

*case V* – No pre-filling, event  $i$  with spills:

$$h_i - q \cdot \theta_i > w; w - q \cdot d_i \leq 0;$$

*case VI* – Event  $i$  with intensity lower than outflow rate, event  $i+1$  with spills:

$$h_i - q \cdot \theta_i \leq 0; h_{i+1} - q \cdot \theta_{i+1} > w;$$

*case VII* – Pre-filling, event  $i$  with spills, event  $i+1$  with intensity lower than outflow rate:

$$h_i - q \cdot \theta_i > w; w - q \cdot d_i > 0; w - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} \leq 0;$$

*case VIII* – Pre-filling, both event  $i$  and event  $i+1$  without spills:

$$0 < h_i - q \cdot \theta_i \leq w; h_i - q \cdot \theta_i - q \cdot d_i > 0; 0 < h_i - q \cdot \theta_i - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} \leq w;$$

*case IX* – Pre-filling, both and event  $i$  and event  $i+1$  with spills:

$$h_i - q \cdot \theta_i > w; w - q \cdot d_i > 0; w - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} > w;$$

*case X* – Pre-filling, event  $i$  without spills, event  $i+1$  with spills:

$$0 < h_i - q \cdot \theta_i \leq w; h_i - q \cdot \theta_i - q \cdot d_i > 0; h_i - q \cdot \theta_i - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} > w;$$

case XI – Pre-filling, event *i* with spills and event *i+1* without spills:

$$h_i - q \cdot \theta_i > w; w - q \cdot d_i > 0; 0 < w - q \cdot d_i + h_{i+1} - q \cdot \theta_{i+1} \leq w.$$

For the same assumption on the probability distribution functions of rainfall depth, duration and interevent time considered above, that is  $f_{h,i} = f_{h,i+1} = f_h, f_{\theta,i} = f_{\theta,i+1} = f_\theta$  and  $f_d = f_{d,i} = f_{d,i+1}$ , case III, case IV, case VI, case VII and case XI cannot occur and eqn (20) becomes:

$$\bar{t}_R = \bar{t}_0 - \bar{t}_1 = \frac{1}{2} \cdot [t_0 - 2 \cdot \theta - d] \tag{22}$$

Substituting eqn (21) in eqns (15) and (22), respectively, if a single event or a couple of chained events is considered, the average retention time results:

$$\bar{t}_R = \begin{cases} 0 & \text{case I} \\ 0.5 \cdot (h/q - \theta) & \text{case II} \\ h/q - \theta - d/2 & \text{case VIII} \\ w/(2 \cdot q) & \text{cases V - IX - X} \end{cases} \tag{23}$$

Equation (23) is valid for  $w/q > IETD$  and for  $t_x < w/(2 \cdot q)$ .

The probability distribution function of average retention times results:

$$\begin{aligned} F_{\bar{t}_R} &= P(t_x < \bar{t}_R) = P\left(t_x < \bar{t}_R < \frac{w}{2 \cdot q}\right) + P\left(\bar{t}_R = \frac{w}{2 \cdot q}\right) \\ &= \int_{\theta_1}^{\theta_2} f_\theta \cdot d\theta \cdot \int_{d_1}^{d_2} f_d \cdot dd \cdot \int_{h_1}^{h_2} f_h \cdot dh + \int_{\theta_3}^{\theta_4} f_\theta \cdot d\theta \cdot \int_{d_3}^{d_4} f_d \cdot dd \cdot \int_{h_3}^{h_4} f_h \cdot dh \\ &\quad + \int_{\theta_5}^{\theta_6} f_\theta \cdot d\theta \cdot \int_{d_5}^{d_6} f_d \cdot dd \cdot \int_{h_5}^{h_6} f_h \cdot dh + \int_{\theta_7}^{\theta_8} f_\theta \cdot d\theta \cdot \int_{d_7}^{d_8} f_d \cdot dd \cdot \int_{h_7}^{h_8} f_h \cdot dh \\ &\quad \theta_1 = \theta_3 = \theta_5 = \theta_7 = 0; \theta_2 = \theta_4 = \theta_6 = \theta_8 = \infty; \\ &\quad d_1 = d_8 = 2 \cdot t_x; d_2 = d_4 = d_5 = w/q; d_3 = d_7 = IETD; d_6 = \infty; \end{aligned} \tag{24}$$

$$h_1 = h_5 = q \cdot (\theta + 2 \cdot t_x); h_2 = h_3 = h_8 = q \cdot \theta + (q \cdot d + w)/2; h_4 = h_6 = \infty; h_7 = q \cdot (t_x + d/2 + \theta);$$

which solution is:

$$F_{\bar{t}_R}(t_x) = \frac{1}{1 + q^*} \cdot \left[ (1 - \beta) \cdot e^{-\psi \cdot IETD - 2 \cdot t_x \cdot (\psi + \xi \cdot q)} + \beta \cdot e^{-\xi \cdot q \cdot \left(\frac{IETD}{2} + t_x\right)} \right] \tag{24*}$$

with:  $\beta = 2 \cdot \psi / (q \cdot \xi + 2 \cdot \psi)$  and  $q^* = q \cdot \xi / \lambda$ .

#### 4 CASE STUDY

To test the reliability of derived expressions for the estimation of the probability distributions of average retention times, a case study in Milano, Italy, has been analyzed. The series of rainfall data recorded at Milano-Monviso gauge station in the period 1991–2005 has been used and IETD=10 hours has been assumed.



Table 1: Main characteristics of rainfall variables.

$\mu_h$ [mm]	18.49	$V_h$ [-]	1.15	$\rho_{h,\theta}$ [-]	0.62
$\mu_\theta$ [h]	14.37	$V_\theta$ [-]	1.03	$\rho_{\theta,d}$ [-]	0.11
$\mu_d$ [h]	172.81	$V_d$ [-]	1.30	$\rho_{d,h}$ [-]	0.11

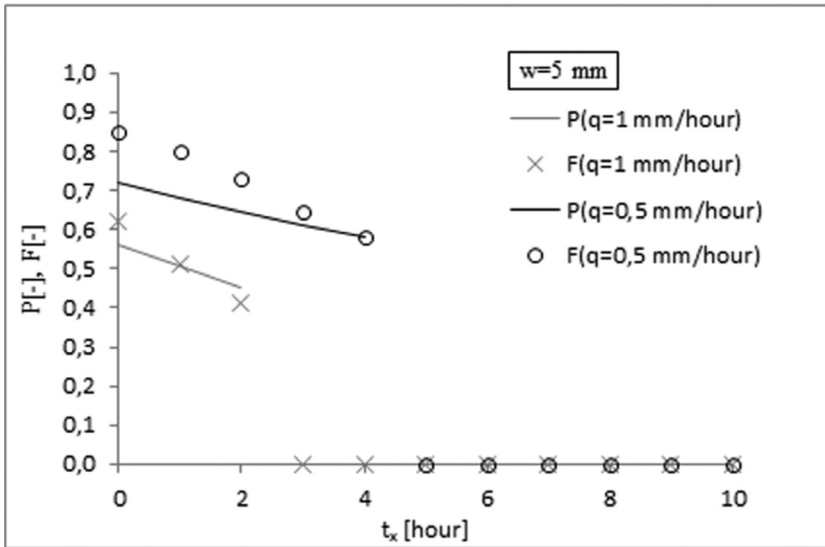


Figure 3: Probability and frequency distributions of average retention times ( $w = 5$  mm;  $q = 1$  mm/h;  $q = 0.5$  mm/h).

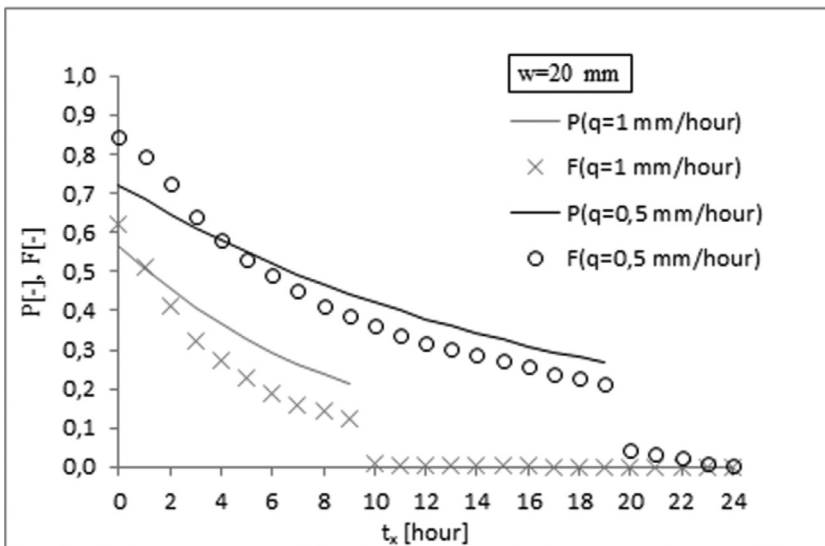


Figure 4: Probability and frequency distributions of average retention times ( $w = 20$  mm;  $q = 1$  mm/h;  $q = 0.5$  mm/h).

The main characteristics (mean, variation coefficient and correlation index) of rainfall variables involved in storage process (rainfall depth  $h$ , rainfall duration  $\theta$  and interevent time  $d$ ) have been shown in Table 1.

Outflow rates of  $q = 0.5$  mm/h and  $q = 1.0$  mm/h and a storage volume  $w = 5$  mm and  $w = 20$  mm have been considered.

Figures 3 and 4 compare the probability distribution functions of the average retention time, calculated by eqns (18) and (24\*) with the frequency distribution of simulated data, respectively, for  $w = 5$  mm and  $w = 20$  mm (continuous black line and circles for  $q = 0.1$  mm/h and continuous grey line and crosses for  $q = 1.0$  mm/h).

Differences in results can be due to:

- The simplifying assumption on the independence of input rainfall variables  $h$ ,  $\theta$ ,  $d$  while in particular the correlation index between rainfall depth and rainfall duration is not negligible (Table 1);
- The simplifying assumption on exponential distribution of input rainfall variables  $h$ ,  $\theta$ ,  $d$ ; as it can be deduced from Table 1, only the frequency distribution of rainfall durations perfectly fits an exponential probability distribution function ( $V_{\theta} \approx 1$ );
- The simplifying assumption of considering only a couple of consecutive event at time; if the outflow rate tends to zero, the number of chained events increases;
- The simplifying assumption of considering the probability distribution functions of rainfall characteristics of event  $i$  equal to those of event  $i+1$  ( $f_{h,i} = f_{h,i+1} = f_h$ ,  $f_{\theta,i} = f_{\theta,i+1} = f_{\theta}$  and  $f_{d,i} = f_{d,i+1}$ ), that excludes cases III-IV-VI-VII-XI of eqn (21) in the resulting formula (24\*);

## 5 CONCLUSIONS

Proposed approach relates the efficiency of a stormwater detention tanks in pollutant removal with the retention time. In particular, the probability distribution function of the average retention time has been estimated. Derived formulas are easy to implement and can be a valid aid to engineer, when there are no long-term registration of records data and only the mean values of rainfall characteristics are available. Moreover, they can be used to size stormwater detention tanks because allow to analyze the influence of outflow rates and storage volumes on the probability distribution of the average retention time, that is on probability distribution of the efficiency of the storage in pollutant removal.

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