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Published in:
Physical Chemistry Chemical Physics

Link to article, DOI:
[10.1039/c7cp05749k](https://doi.org/10.1039/c7cp05749k)

Publication date:
2018

Document Version
Peer reviewed version

[Link back to DTU Orbit](#)

Citation (APA):
Oyarzua, E., Walther, J. H., & Zambrano, H. A. (2018). Water thermophoresis in carbon nanotubes: the interplay between thermophoretic and friction forces. *Physical Chemistry Chemical Physics*, 20, 3672-3677 . DOI: 10.1039/c7cp05749k

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Water thermophoresis in Carbon Nanotubes: the interplay between thermophoretic and friction forces

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Abstract

Thermophoresis is the phenomenon wherein particles experience a net drift induced by a thermal gradient. In this work, molecular dynamics simulations are conducted to study with atomistic detail the thermophoresis of water nanodroplets inside carbon nanotubes (CNTs) and its interplay with the retarding liquid-solid friction. Different applied temperatures, thermal gradients, and droplet sizes are used to reveal the dynamics of the two kinetic regimes of the thermophoretic motion in CNTs. The results indicate that during the droplet motion, the thermophoretic force is independent of the velocity of the droplet, whereas the magnitude of the retarding friction

12 force exhibits a linear dependence. In fact, in the initial regime the magni-
13 tude of the friction force increases linearly with the droplet velocity, until
14 the thermophoretic force is balanced by the friction force as the droplet
15 reaches its terminal velocity in the final regime. In addition, an increasing
16 magnitude of the thermophoretic force is found for longer water droplets.
17 These findings provide a deeper understanding of liquid transport driven
18 by temperature gradients in nanoconfined geometries where liquid-solid in-
19 terfaces govern fluidics.

20 1 Introduction

21 Thermophoresis is a directed motion of particles caused by the presence of an externally im-
22 posed thermal gradient. In particular, thermophoretic movement of a particle suspended in
23 a molecular media is the consequence of a thermally rectified Brownian motion^{1,2}: molecules
24 in the hotter region of the media collide with the particle, transferring a greater momenta
25 as compared to the molecules in the colder regions. During more than a century, theo-
26 retical and experimental studies have been conducted to understand the factors governing
27 the termophoretic transport and elucidate its complex underlying physics³⁻⁵. One of these
28 pioneer investigations was made by Epstein in 1929⁶, who derived the first expressions for
29 the thermophoretic force and velocity. Thereafter, motivated by its important practical con-
30 sequences in the field of aerosol technology⁷, numerous investigations of thermophoresis of
31 particles in gases have been conducted⁸⁻¹². Thermophoresis of suspended particles in liquids
32 was first studied by McNab and Meisen¹³, who found thermophoretic motion of a particle to
33 be independent of the particle size. More recently, and motivated for potential applications
34 of nanofluid solutions, this phenomenon has also been studied in dispersions of nanoscale
35 particles immersed in fluids¹⁴⁻¹⁶. Thermophoresis is fundamentally related with the phe-
36 nomenon of thermodiffusion in liquid solutions^{4,17}, also called the Ludwig-Soret effect^{4,12}
37 after Carl Ludwig¹⁸ and Charles Soret¹⁹ who independently studied this phenomenon in the
38 19th century.

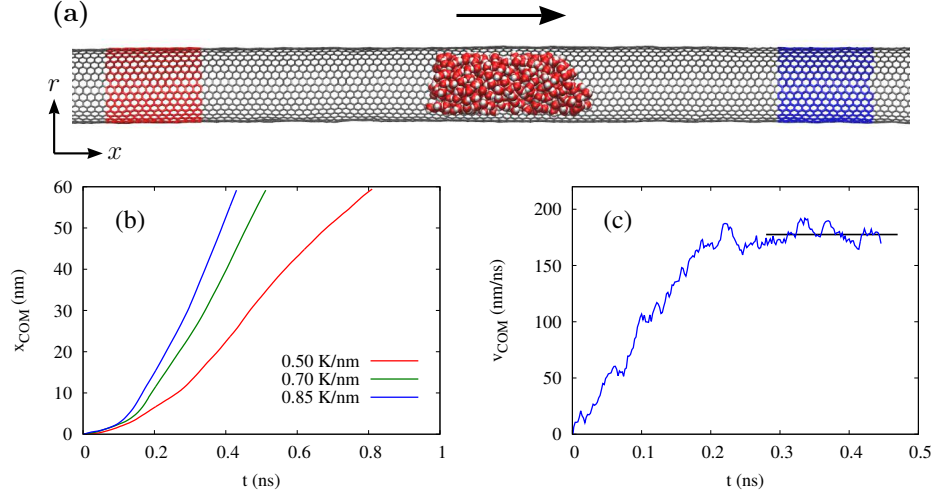


Figure 1: (a) Scheme of the studied system. The droplet inside the CNT moves from the high temperature side towards the cooler side of the CNT. The thermostat is applied directly to the carbon atoms, the red zone represents the high temperature section while the blue zone represents the low temperature section. (b) Time evolution of the center of mass position of the droplet consisting of 800 water molecules under different imposed thermal gradients. (c) History of the velocity of the center of mass of the droplet consisting of 400 water molecules under a imposed thermal gradient of 0.50 K/nm. The solid line depicts the constant velocity regime.

39 Nowadays, the advent of extremely accurate nanofabrication techniques has led to en-
 40 vision novel integrated nanofluidic devices wherein the functional stations are connected
 41 by nanoconduits^{20–22}. In this context, thermophoresis may play a critical role as an en-
 42 abling technology for achieving controlled transport of fluids in nanoscale devices. Recently,
 43 carbon nanotubes²³ (CNTs) have emerged as ideal conduits for ultra efficient water trans-
 44 port^{24–27} due to their molecularly smooth graphitic walls²⁴, well controlled diameter, spa-
 45 tial nanoconfinement and outstanding thermal and mechanical properties^{25,28}. Hence, the
 46 thermophoretic transport of fluids through the inner-core of CNTs has considerable tech-
 47 nological and scientific implications. In fact, the practical use of thermophoresis in future
 48 CNT-based nanofluidic devices requires the feasibility of achieving predictable and control-
 49 lable thermophoretic water transport inside CNTs. To date, despite the important efforts
 50 that have been devoted to investigate thermophoresis inside and outside CNTs^{29–41}, the in-
 51 terplay between applied thermal gradient, thermophoretic velocity, solid-liquid friction^{42–45}

52 and thermophoretic force^{30,33,36} in a water/CNT system, has not been studied. In this letter,
53 we present an atomistic study of the kinetics associated with thermophoresis of water nan-
54 droplets confined inside single wall carbon nanotubes and its interplay with the solid-liquid
55 friction force.

56 2 Methodology

57 To carry out this investigation, we employ both constrained and unconstrained Molecular
58 Dynamics (MD) simulations of nanodroplets confined in CNTs which are subjected to a
59 constant axial thermal gradient. The axial thermal gradient is applied by coupling two
60 Berendsen thermostats⁴⁶ at different temperatures to the carbon atoms at the respective
61 ends of the CNT cf. Fig. 1a. As demonstrated in previous studies, a Berendsen thermostat
62 is suitable for imposing proper nonequilibrium conditions in CNTs^{47,48}, and also exhibit
63 correct mechanical responses at relatively constant temperature during CNT compression⁴⁹.
64 The MD simulations were performed using the parallel MD package FASTTUBE^{29,40,50,51}.
65 The equations of motion are integrated in time using the leapfrog scheme with a time step
66 of 2 fs. Periodic boundary conditions is considered in the direction parallel to the CNT axis
67 and with free space conditions in the normal directions. The carbon-carbon intramolecular
68 interactions of the CNT are described by a Morse bond, a harmonic cosine of the bending
69 angle, and a torsion potential^{29,30,40,50}. The water is modeled using the rigid SPC/E water
70 model⁵² with the O-H bond and the H-O-H angle constrained using the SHAKE algorithm.
71 The water-CNT interactions are described by a 12-6 LJ potential calibrated to reproduce a
72 water contact angle of 81° as described by Werder et al.⁵³ and Zambrano et al.⁴⁰. The van
73 der Waals and Coulomb interactions are truncated at 1.0 nm with the Coulomb potential
74 smoothly truncated to ensure energy conservation^{40,50}. The MD package and the force
75 fields have been extensively validated in previous studies of thermophoresis^{29,30,36,40,53,54}.
76 For details of the potentials and setup of the simulations, we refer the reader to Zambrano
77 et al.⁴⁰.

78 In the unconstrained MD simulations of thermophoresis^{29,33–37,40,41}, a constant thermal
79 gradient is applied along the axis of the CNT. The imposed thermal gradient induces a
80 thermophoretic motion of the confined nanodroplet in the opposite direction of the ther-
81 mal gradient. Moreover, in line with the results presented by Shiomi and Maruyama⁴¹,
82 two regimes in the movement of the nanodroplet are observed: first an acceleration regime
83 wherein the thermophoretic force is larger than the friction force, and then, a constant ve-
84 locity regime, wherein the thermophoretic force balances the friction force and the droplet
85 reaches its terminal velocity. Furthermore, to gain insight in the kinetics of the droplet mo-
86 tion, constrained MD simulations are conducted. This set of simulations consists of setting
87 the center of mass velocity (v_{com}) every time step to a target value, forcing the droplet to
88 move with a constrained velocity without affecting the velocity distribution of the molecules
89 in the droplet. Constrained MD simulations are performed with and without imposed ther-
90 mal gradients. The MD simulations with constrained velocity were introduced by Schoen et
91 al.²⁹ and then, in a similar context, reported by Zambrano et al.³⁶. Further details of this
92 technique are provided in the Supporting Information.

93 3 Results and discussion

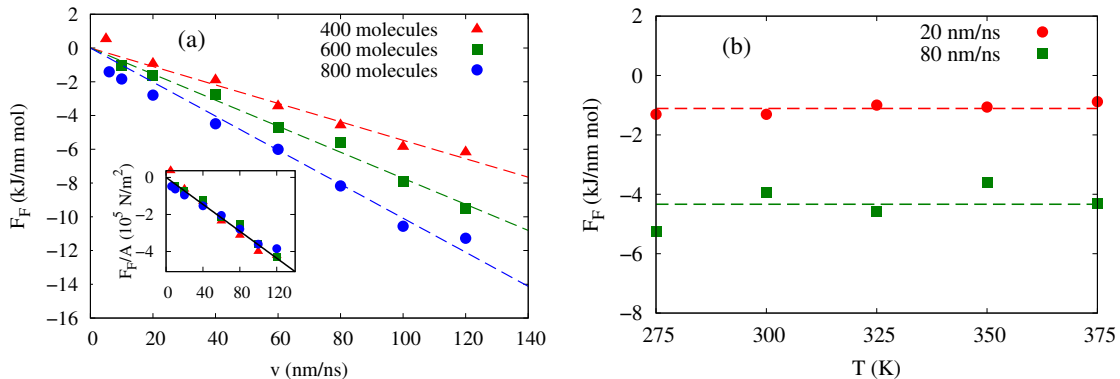


Figure 2: (a) Friction force as a function of the velocity of center of mass (v_{com}) for droplet sizes 400(\blacktriangle), 600(\blacksquare) and 800(\bullet) water molecules at 325 K. The dashed lines are fits to the data. Inset: Friction forces divided by the respective solid-liquid contact area. (b) Friction force as a function of temperature with imposed v_{com} of 20 nm/ns and 80 nm/ns with a droplet of 400 water molecules. The dashed lines are fits to the data.

94 In this study, an armchair CNT with chirality (17,17) and length of 75 nm is considered
 95 for all cases. Thermal gradients of 0.2, 0.5, 0.7 and 0.85 K/nm are imposed along the axis
 96 of the CNT wherein water nanodroplets of different sizes are confined. The nanodroplets
 97 confined in the CNTs consist of 400, 600 and 800 water molecules. A schematic of the
 98 system is shown in Fig. 1a. From the atomistic trajectories, the temporal evolution of both
 99 position and velocity of the center of mass of the droplets are extracted. In line with previous
 100 studies^{29,36,40,41}, a directed displacement of the droplet is observed from the high temperature
 101 zone towards the low temperature zone. Moreover, for all cases we observe higher v_{com} as
 102 higher thermal gradients are imposed along the CNT cf. Fig. 1b. Furthermore, as shown
 103 in Fig. 1c, during the droplet displacement two dynamic regimes can be identified: first
 104 a regime with increasing velocity in time and subsequently, a constant velocity regime as
 105 depicted by the solid line. We notice that in this set of simulations, the only forces acting
 106 on the droplet are the thermophoretic force (F_T) which is the force exerted by the thermal
 107 gradient, and the retarding friction force (F_F) acting at the solid-liquid interface, hence, the
 108 resulting force is

$$F_N = m \cdot a = F_T - F_F \quad (1)$$

109 where F_N is the net force, m is the mass of the droplet and a is the instantaneous accelera-
 110 tion. Figure 1c infers that within the first regime the magnitude of the thermophoretic force
 111 acting on the droplet is higher than the magnitude of the friction force, conversely, during
 112 the constant velocity regime, the retarding friction force balances the thermophoretic force,
 113 i.e., the droplet reaches its maximum velocity at zero net force. The behavior exhibited by
 114 the droplet motion suggests that the instantaneous magnitude of the friction force and/or
 115 the thermophoretic force must be dependent on the instantaneous velocity of the droplet.
 116 In order to analyze the relationship between the droplet speed and the thermophoretic and
 117 friction forces, sets of isothermal and non-isothermal MD simulations are performed at dif-
 118 ferent constrained velocities. From the constrained simulations with an imposed thermal
 119 gradient, the instantaneous net force (F_N), i.e., the force instantaneously accelerating the

120 droplet is computed from the simulations, similar to the analysis performed by Schoen et
121 al.²⁹ and Zambrano et al.³⁶. Furthermore, the instantaneous retarding friction force (F_F) is
122 computed from the constrained simulations at constant temperature. The thermophoretic
123 force (F_T), which is the force exerted on the droplet by the imposed thermal gradient, is
124 calculated by adding the friction force (F_F) to the net force (F_N) at the respective velocity,
125 according Eq. (1).

126 We notice that the center of mass velocity (v_{com}) of the droplet is assumed to be equivalent
127 to the slip velocity considering the ultra high slippage inherent in the water-CNT interface,
128 in line with Falk et al.⁴². In fact, previous investigations^{27,55,56} reported water slip length
129 over 75 nm for a CNT of 2 nm in diameter, leading to a plug-like velocity profile for water
130 confined in CNTs^{40,45}. Furthermore, Chen et al.⁵⁷ found that water droplets spontaneously
131 slip inside CNTs owing to thermal fluctuations of water at room temperature.

132 The friction force as a function of the constrained center of mass velocity is shown in
133 Fig. 2a. In line with the previous studies^{42,43,58}, the magnitude of the friction force increases
134 for higher velocities of the droplet. Indeed, the magnitude of the friction force is linearly
135 proportional to the droplet velocity. Note that the negative values in the magnitude of the
136 friction force are due to the force direction opposite to the displacement of the nanodroplet.
137 In Fig. 2a, each point is computed from the atomic trajectories obtained from independent
138 3 ns MD simulations at constant temperature, the red, green and blue dashed lines are fits to
139 the data assuming $F_F = 0$ for $v = 0$ ⁵⁷. Moreover, the dashed lines in Fig. 2a. display differ-
140 ent slopes because each nanodroplet (400, 600 and 800 molecules) has different liquid-solid
141 contact areas. In fact, if the magnitudes of the computed friction forces presented in Fig. 2a
142 are divided by the respective contact area, all the data converge to a single slope, as shown in
143 the inset of Fig. 2a, where the magnitude of the slope corresponds to a friction coefficient of
144 3631 Ns/m^3 . Moreover, as the temperature imposed along the CNT is systematically varied
145 in each isothermal simulation, the friction force is found to be independent of the imposed
146 temperature cf. Fig. 2b. Thus, in non-isothermal simulations we assume that the magnitude

147 of the friction force does not change as different thermal gradient are imposed along the
 148 CNT.

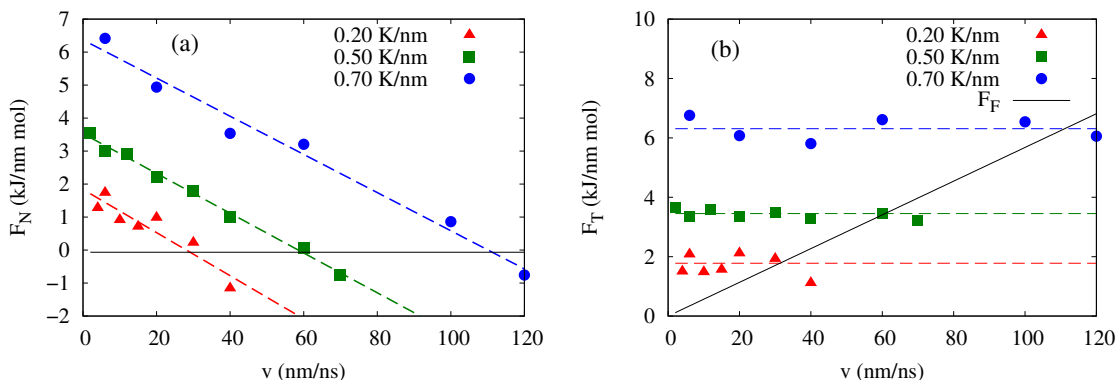


Figure 3: Net force and thermophoretic force of the 400 water molecules case under thermal gradients of 0.20 K/nm (\blacktriangle) 0.50 K/nm (\blacksquare) and 0.70 K/nm(\bullet). (a) Net force as a function of the velocity of center of mass. The solid black line is a guide for $F_N = 0$. (b) Thermophoretic force as a function of the velocity of center of mass. The dashed lines are fits to the data. The solid black line is the absolute value of the friction force for the 400 water molecules case (Fig 2.a).

149 The net force (F_N) acting on the nanodroplets is computed from constrained MD sim-
 150 ulations with imposed thermal gradients. Constant velocities (v_{com}) ranging from 3 m/s to
 151 120 m/s are imposed to the center of mass of the droplet while thermal gradients of 0.20,
 152 0.50 and 0.70 K/nm are applied along the axis of the CNT. For the case of a water droplet
 153 of 400 molecules, the net force as a function of the imposed velocity (v_{com}) is depicted in
 154 Fig. 3a. For all the imposed thermal gradients, we observe that the instantaneous net force
 155 decreases linearly with the imposed velocity (v_{com}), starting from a positive value at zero
 156 velocity and decreasing until it vanishes when the droplet achieves its terminal velocity.
 157 Moreover, it should be noted in Fig. 3a that the slope of the blue, green and red dashed
 158 lines is equivalent to the slope for the corresponding dashed red line in Fig. 2a, which is the
 159 friction coefficient times the solid-liquid contact area. The dashed red line in Fig. 2a shows
 160 the friction force versus velocity for the same droplet consisting of 400 water molecules,
 161 therefore, the decrease in the net force is due to the growth of the friction force with higher
 162 velocities. Since $F_N = m \cdot a$, the thermophoretic motion of the droplet is associated with

163 a decreasing acceleration during the first regime (see Support Info. Figure S4), before the
 164 terminal velocity is reached, showing no evidence of a constant acceleration regime during
 165 the thermophoretic motion as inferred by previous authors^{41,59}.

166 From the computed friction and the instantaneous net forces, the thermophoretic force is
 167 calculated. In Fig. 3b the thermophoretic force for the 400 water molecules case is presented,
 168 wherein each point is obtained from the sum of the net force (F_N) computed from the
 169 constrained simulations (Fig. 3a) and the friction force (F_F) (Fig. 2a) at the corresponding
 170 velocity, according to Eq. (1). As depicted in Fig. 3b, the thermophoretic force displays not
 171 dependency on the droplet velocity, i.e., the droplet is subjected to a constant thermophoretic
 172 force during the motion. Moreover, Fig. 3b shows that for higher imposed thermal gradients,
 173 the thermophoretic force increases as observed in previous studies^{29,33,36,41}. We note that the
 174 relation between velocity and thermophoretic force has been studied for systems consisting of
 175 motile coaxial CNTs³⁶ wherein a decreasing thermophoretic force has been observed for higher
 176 velocities of the inner CNT. Conversely, in the present study for a solid-liquid interface, we
 177 find that the thermophoretic force is not velocity dependent while the friction force increases
 178 linearly with the droplet speed.

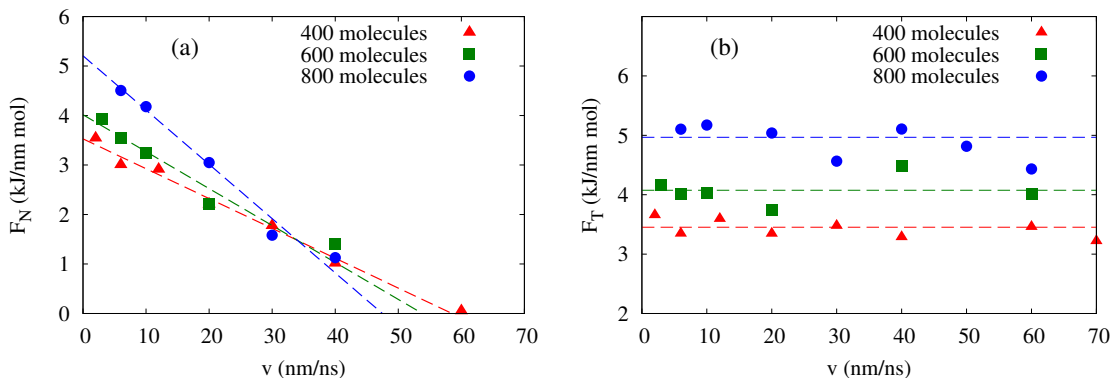


Figure 4: Net force and thermophoretic force for droplet sizes of 400(▲), 600(■) and 800(●) water molecules under an applied thermal gradient of 0.50 K/nm. (a) Computed Net force as a function of the velocity of the center of mass. The dashed lines are fits to the data. (b) Thermophoretic force as a function of the velocity of center of mass. The dashed lines are fits to the data.

179 It is also interesting to evaluate the effect of the size of the droplets on the thermophoretic

180 and net force. The net force as a function of the constrained center of mass velocity is
181 shown in Fig. 4a for droplets consisting of 400 (red triangles), 600 (green squares) and
182 800 (blue circles) molecules under an imposed thermal gradient of 0.50 K/nm. The dashed
183 lines in Fig. 4a are linear fits for each case, with the slopes depicting the friction coefficient
184 times the respective solid-liquid contact area. Note that the solid-liquid contact area is
185 larger for droplets with higher number of water molecules. Therefore, Fig. 4a indicates
186 that all the nanodroplets move with a decelerated motion, slowed down with a rate that
187 is directly proportional to the size of the particular nanodroplet (See Fig. 2a), i.e., at the
188 same instantaneous speed, droplets with a larger solid-liquid contact area experience a higher
189 retarding friction. Indeed, as shown in Fig. 4a for an imposed thermal gradient of 0.50 K/nm,
190 the magnitude of the terminal velocity is higher for droplets with smaller number of water
191 molecules. The same behavior is observed for different imposed thermal gradients as shown in
192 Supporting Info. Figure S5. Furthermore, the thermophoretic force is computed from the net
193 force values presented in Fig. 4a. In Fig. 4b, for an imposed thermal gradient of 0.50 K/nm,
194 higher thermophoretic forces are computed for longer water droplets, which shows that the
195 magnitude of the thermophoretic force is directly related to the droplet size (or the droplet
196 length due to the constant CNT cross-section). It should be noted that there is no consensus
197 about the relation between the thermophoretic force and the size of the motile particle.
198 For example, the thermophoretic force has been found to be dependent of particle size for
199 distributions of particles in gas media^{60,61} and for particles inside CNTs⁶². On the other
200 hand, a non size dependence of the thermophoretic force has been found for solid particles
201 in liquid media¹³, oil droplets in liquid mixtures⁶³ and double-walled CNTs³³. Here, to
202 gain insight into the relationship between the thermophoretic force and the particular size of
203 the water nanodroplet, Fig. 5 depicts the thermophoretic force as a function of the thermal
204 gradient for droplets consisting of 400, 600 and 800 water molecules. The results indicate
205 that the magnitude of the thermophoretic force acting on the droplet is directly related to
206 both the magnitude of the imposed thermal gradient and the particular length of the droplet.

207 Therefore, in line with previous studies^{30,31}, we infer that the thermophoretic force acting
 208 on the droplet is generated by the net current of phonons induced by the imposed thermal
 209 gradient, i.e., the rectified thermal vibrations of the carbon atoms provide the effective force
 210 to drive the water droplet through the CNT. Nevertheless, we notice further investigation is
 211 required to find the precise relationship between the interfacial phonon scattering dynamics
 212 and the thermophoretic force acting on nanodroplets confined in CNTs. We believe that
 213 this investigation provides deeper understanding of liquid transport driven by temperature
 214 gradients in nanodevices and will be useful for the development of nanofluidic applications.

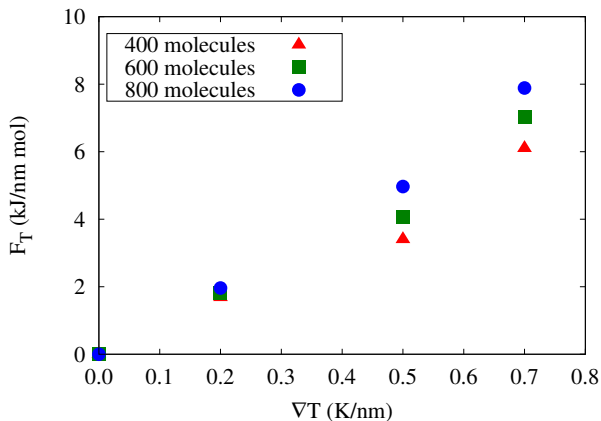


Figure 5: Thermophoretic force as a function of the thermal gradient for droplet sizes of 400 (▲), 600 (■) and 800 (●) water molecules.

215 4 Conclusions

216 In summary, by using molecular dynamics we studied in detail the interplay between ther-
 217 mophoretic and friction forces which govern the thermophoretic transport of water nan-
 218 odroplets through CNTs. The results indicate that the thermophoretic force is not velocity
 219 dependent while the friction force increases linearly with the droplet speed. Moreover, we
 220 find that the magnitude of the thermophoretic force is determined by the imposed thermal
 221 gradient and the particular length of the droplet. In general, the thermophoretic motion of a
 222 nanodroplet exhibits two kinetic regimes: (i) a initial regime wherein the droplet moves with
 223 decreasing acceleration, i.e., the friction force is linearly proportional to the droplet velocity

224 whereas the thermophoretic force has a constant value defined by the thermal gradient and
225 the droplet length, and (ii) a subsequent regime wherein the droplet moves at constant ve-
226 locity due to balance between the thermophoretic force and the retarding friction force. The
227 results presented in this letter contribute to gain insight in the transport of liquids driven by
228 thermal gradients and have practical implications for the design of CNT-based nanofluidic
229 devices.

230 Acknowledgement

231 E. Oyarzua thanks financial support from CONICYT scholarship no. 21140427. This re-
232 search was partially funded by CONICYT under FONDECYT project No 11130559. We also
233 thank the partial financial support from the University of Concepcion under VRID project
234 no. 21496651. The authors received computational support from the Department of Physics
235 at the Technical University of Denmark. Furthermore, the authors wish to acknowledge
236 professor Constantine M. Megaridis for valuable scientific discussions.

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379 **Graphical TOC Entry**

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