## Approximating the singular integrals of Cauchy type with weight function on the interval.

## ABSTRACT

It is known that the solutions of characteristic singular integral equations (SIEs) are expressed in terms of singular integrals of Cauchy type with weight functions w (x) =  $(1 + x)v(1 - x)\mu$ , where  $v = \pm \text{frac}(1, 2)$ ,  $\mu = \pm \text{frac}(1, 2)$ . New quadrature formulas (QFs) are presented to approximate the singular integrals (SIs) of Cauchy type for all solutions of characteristic SIE on the interval [- 1, 1]. Linear spline interpolation, modified discrete vortex method and product quadrature rule are utilized to construct the QFs. Estimation of errors are obtained in the classes of functions H $\alpha$  ([- 1, 1], A) and C1 ([- 1, 1]). It is found that the numerical results are very stable even for the cases of semi-bounded and unbounded solutions of singular integral equation of the first kind.

**Keyword:** Singular integral; Singular integral equations; Quadrature formula; Discrete vortex method; Approximation; spline.