



Cresswell, A.J. , Carter, J. and Sanderson, D.C.W. (2018) Dose rate conversion parameters: assessment of nuclear data. *Radiation Measurements*, 120, pp. 195-201. (doi:[10.1016/j.radmeas.2018.02.007](https://doi.org/10.1016/j.radmeas.2018.02.007)).

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# Accepted Manuscript

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PII: S1350-4487(17)30821-1

DOI: [10.1016/j.radmeas.2018.02.007](https://doi.org/10.1016/j.radmeas.2018.02.007)

Reference: RM 5877

To appear in: *Radiation Measurements*

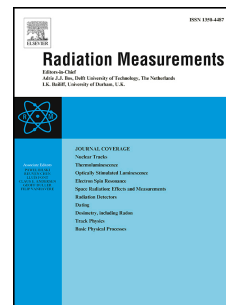
Received Date: 6 December 2017

Revised Date: 26 February 2018

Accepted Date: 26 February 2018

Please cite this article as:

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# Dose Rate Conversion Parameters: Assessment of Nuclear Data

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## Abstract

The dating of materials using stored dose methods requires accurate determination of the environmental dose rate. The calculation of dose rates from radionuclide concentrations requires conversion parameters derived from nuclear data (half life, decay energies and intensities, and branching ratios). With the substantial body of primary data, it is convenient to use data from evaluated libraries. These libraries show variations reflecting both newer data unavailable to earlier evaluations and the relative importance given to different data sets by the evaluators. Commonly used conversion parameters derive from the Evaluated Nuclear Structure Data File (ENSDF), either directly or from secondary publications, with new tabulations produced in recent years following revisions to this library. Other international evaluations of nuclear data include the NEA/OECD supported JEF2.2 and JEFF3.11 evaluations, and the Decay Data Evaluation Project (DDEP). A technique comparing different evaluations to identify data that can not be confidently used has been developed. These differences have been investigated with an evaluation of underlying nuclear data. Particular radionuclides of interest are discussed;  $^{214}\text{Bi}$  where recent evaluations depend on a single high precision data set,  $^{228}\text{Ac}$  where the decay scheme is incomplete and further measurements are required, and  $^{40}\text{K}$  where the mean beta energy has been calculated in the evaluations using an incorrect shape factor. Revised dose rate conversion factors have been

26 produced, which are largely consistent with earlier values with the exception of the  $^{40}\text{K}$  beta  
27 parameter which is 4% higher than recent values but consistent with earlier calculations.

28

29

### 30 **Keywords**

31 Dose rate conversion factors; evaluated nuclear data;  $^{214}\text{Bi}$ ;  $^{228}\text{Ac}$ ;  $^{40}\text{K}$

32

### 33 **Research Highlights**

- 34 • Innovative comparison of evaluated libraries to highlight lower confidence data
- 35 • Highlighted radionuclides with lowest confidence data -  $^{214}\text{Bi}$ ,  $^{228}\text{Ac}$ ,  $^{40}\text{K}$
- 36 •  $^{40}\text{K}$  beta spectrum incorrect in all evaluated libraries, improved mean energy given
- 37 • Revised dose rate conversion factors using best available data given

38

39

### 40 **1. Introduction**

41 In luminescence or electron-spin resonance dating the age of a mineral is determined from the  
42 ratio of the measured equivalent dose to the environmental dose rate the mineral had been  
43 exposed to, including appropriate corrections for grain size and water content. In some  
44 instances dose rates can be measured directly, using in-situ spectrometers or dosimeters, but  
45 in many cases dose rates calculated from measurements of the activity concentration ( $\text{Bq kg}^{-1}$ )  
46 or elemental concentrations (% or ppm) of natural radionuclides, or alpha and beta  
47 counting rates, in samples returned to the laboratory for analysis are needed in the absence of  
48 field measurements or to supplement other measurements. This calculation uses dose rate  
49 conversion factors derived from nuclear data. The calibration of field instruments and  
50 dosimeters often also relies on appropriate conversion factors.

51

52 These conversion factors have been calculated several times since the 1970's, following  
53 revisions to the nuclear data used, as shown in Fig. 1. The values for these parameters are  
54 tabulated in the supplementary material. These show some significant variation, but with  
55 recent estimates converging on a common value within a few % uncertainty. Nevertheless,  
56 comparisons between dose rates determined by different methods and institutions continue to  
57 show discrepancies, with the conversion factors used being one potential explanatory factor.  
58 Therefore, there is reason to examine these conversion factors again. As the nuclear data used  
59 to determine these factors is updated, it could be asked whether it is necessary to update the  
60 conversion factors? Or, has the point been reached where those updates will not lead to  
61 significant changes in the conversion factors? And, to what extent can we be confident in the  
62 nuclear data used? It would be beneficial if variations in nuclear data had been settled to  
63 values that are very unlikely to change significantly with further measurement, from which  
64 the stored dose dating community could derive an agreed set of conversion factors. It is the  
65 aim of this work to examine whether this point has been reached, and if not what is needed to  
66 move closer to that position.

67

68 The nuclear data required for these calculations are the energies and intensities of discrete  
69 radiation (alpha, gamma and x-ray) and the intensities and mean energies of beta radiation,  
70 which requires both the decay endpoint and shape of the beta spectrum. When nuclide  
71 concentrations are expressed as elemental concentrations (ppm or %) then the half lives of the  
72 decays are also required.

73

## 74 **2. Nuclear Data Tables**

75

76 With the very large quantity of nuclear data available, and the specialist nature of many  
77 publications, it is often impractical to assimilate the primary data, and it is therefore  
78 convenient to refer to evaluated libraries. In this work, three such libraries are considered.

79  
80 The Evaluated Nuclear Structure Data File (ENSDF) was the first comprehensive nuclear  
81 structure data base, developed by staff at Berkeley and Oak Ridge in the late 1970s while the  
82 7<sup>th</sup> Edition of the *Table of Isotopes* was being compiled, with the first version of the data base  
83 largely mirroring the *Table of Isotopes* 7<sup>th</sup> Edition. The ENSDF consortium developed, and  
84 an international network of evaluators was established under the IAEA. The ENSDF database  
85 is maintained by the US National Nuclear Data Center at Brookhaven National Laboratory  
86 (NNDC, 2017). The database is under constant development, with updated publication of  
87 evaluated data in *Nuclear Data Sheets* at a rate of approximately every 7-11 years. The 8<sup>th</sup>  
88 Edition of the *Table of Isotopes* was produced using ENSDF data.

89  
90 The NEA and OECD coordinated evaluation projects with particular emphasis on nuclear  
91 data relevant to reactor physics, which for decay data produced two evaluated libraries, the  
92 Joint Evaluated File Version 2.2 (JEF2.2) in 1993 (NEA 2000) and Joint Evaluated Fission  
93 and Fusion File Version 3.1.1 (JEFF 3.1.1) in 2007 (Kellett et.al. 2009). Both of these data  
94 bases are fixed, without ongoing development and revision.

95  
96 It has been noted (Helmer 1999) that a significant limitation on many evaluated libraries is  
97 the lack of comments on the origin of the data and processing done, making it impossible for  
98 others to judge the quality of the evaluations, and that values for quantities differ between  
99 evaluated libraries. To address these concerns the Decay Data Evaluation Project (DDEP)  
100 was initiated in 1995 (Helmer 1999, Helmer et.al. 2002) with the intention of giving the most

101 precise values that are justified, with a methodology that includes accounting for all  
102 measurements of a quantity (either using or explicitly excluding each measurement),  
103 providing written documentation of all the data used and the decisions made, and for each  
104 evaluation to be reviewed by other members of the DDEP.

105  
106 For luminescence dating, dose rate conversion factors were calculated in the 1970s and 80s  
107 (Aitken 1974, 1983, Bell 1976, Sanderson 1987 and others) using various editions of the  
108 *Table of Isotopes* and *Nuclear Data Sheets*. Several recent re-evaluations use ENSDF data  
109 (Adamiec & Aitken 1998, Guerin et.al. 2011, Liritzis et.al. 2013), without any apparent  
110 detailed consideration of the basis for the revisions to the evaluated library. As noted, these  
111 conversion factors have converged to common values within a few percent. However, they  
112 have all been determined from different generations of the same group of evaluations, and  
113 any variations using different evaluation procedures would result in a reduction in confidence  
114 in these parameters.

115  
116 The purpose of this paper is to examine the different evaluated nuclear data libraries for the  
117 radionuclides of relevance to dosimetry from natural sources: the decay chains from  $^{238}\text{U}$ ,  
118  $^{235}\text{U}$  and  $^{232}\text{Th}$ , and the decays of  $^{40}\text{K}$  and  $^{87}\text{Rb}$ . This will identify the individual radionuclides  
119 where there is significant variability in the evaluated nuclear data, or where the uncertainties  
120 are larger, which result in the most significant uncertainty in dose rate conversion factors.  
121 From this examination, further details of existing data for those radionuclides identified as  
122 most significant are given. The influence of these variations on dose rate conversion factors  
123 for the infinite matrix condition are then described.

124

### 125 3. Examination of evaluated data for naturally occurring radionuclides

126

127 The data in the JEF2.2, JEFF3.11, ENSDF and DDEP libraries were interrogated to tabulate  
128 values for the half lives, mean decay energies and intensities, and where appropriate  
129 branching ratios, for all naturally occurring radionuclides. This data was tabulated for alpha,  
130 beta and gamma decay, x-rays and conversion electrons. These tables, with a more extensive  
131 discussion of the nuclear data, are given elsewhere (Cresswell et.al. 2018). Data were  
132 downloaded from the ENSDF and DDEP libraries in March 2017. These values have been  
133 used to calculate dose rate conversion factors for each of these evaluations, as shown in Fig. 2  
134 and tabulated in the supplementary material.

135

136 For the uranium series both ENSDF and DDEP generate significantly lower gamma  
137 conversion factors and higher beta conversion factors compared to JEF2.2/JEFF3.1.1. These  
138 are driven by data for  $^{214}\text{Bi}$ , with significant differences for both beta and gamma mean  
139 energies between the evaluated libraries (Table 1) accounting for approximately 1.5% of the  
140 total beta and 3.5% of the total gamma energies. The end-point energies, shapes and  
141 intensities of beta decays to excited levels in  $^{214}\text{Po}$  are determined from analysis of the  
142 gamma ray emission spectra. Thus differences in the evaluation of the gamma emission data  
143 will account for differences in both the gamma and beta energies.

144

145 The evaluation of the gamma decay scheme involves normalising available gamma  
146 spectrometry data to the 609 keV (1<sup>st</sup> excited state to ground state) transition, to allow the  
147 generation of a relative intensity level scheme. This is then normalised to an evaluated  
148 absolute intensity for the 609 keV transition. The absolute intensities for the 609 keV  
149 emission in the ENSDF and DDEP libraries are identical ( $45.49 \pm 0.19\%$ ), whereas the



150 intensity in the JEF2.2/JEFF3.11 library is higher ( $46.9 \pm 4.0\%$ ). The JEF2.2 evaluation for  
151  $^{214}\text{Bi}$  was not revised in the JEFF3.11 evaluation, and the ENSDF and DDEP libraries include  
152 two measurements not available to the JEF2.2 evaluators. In particular, a high precision data  
153 set reported by Morel et.al. (2004) using  $^{226}\text{Ra}$  sources certified to 0.2% precision, and 4  
154 different HPGe detectors and 2 or 3 source geometries for each detector to check cascade  
155 summing correction, with an absolute intensity for the 609 keV gamma ray of  $45.57 \pm 0.18\%$ .  
156 To date, this dataset is the most precise measurement of the critical 609 keV absolute  
157 intensity, and the relative intensities of the other emissions from  $^{214}\text{Bi}$  decay. To tie down this  
158 critical intensity more conclusively there would be value in independent measurements with  
159 similar attention to detail to rule out potential bias in the source activity certification, detector  
160 efficiencies and cascade summing corrections.

161  
162 For the thorium series, the ENSDF and DDEP libraries produce lower gamma dose rate  
163 conversion factors, with significantly improved precision, compared to JEF2.2 and JEFF  
164 3.11. This is largely explained by differences in the  $^{228}\text{Ac}$  decay data (Table 2). Even with  
165 more recent data improving the precision of the evaluation, the DDEP evaluation (Pearce  
166 2010) notes that this decay scheme is incomplete. The effective Q-value<sup>1</sup> calculated from  
167 individual decay rates and intensities ( $2010 \pm 100$  keV) is low compared to the Q-value from  
168 mass differences ( $2123.8 \pm 2.7$  keV). There is a ~7% discrepancy between beta and gamma  
169 emissions, suggesting missing gammas. “Further measurements of the gamma data,  
170 particularly at low energy, would be of benefit, as would coincidence studies to validate the  
171 placement of gammas in the level scheme” (Pearce 2010). Absolute gamma emissions were  
172 normalised to the 463 keV emission, however it is noted that “this value is not consistent with  
173 expected beta decay characteristics” (Pearce 2010). If the discrepancies in the decay scheme

---

<sup>1</sup> The Q-value is the difference in rest mass energy of the parent and daughter nuclides. This should equal the total energy released in the decay (the sum of all radiation and nuclear recoil).

174 are the result of unobserved gamma rays, with associated beta transitions, then it is expected  
 175 that total gamma and beta energies per decay would be larger than determined from the  
 176 ENSDF/DDEP libraries by a few percent.

177

178 For  $^{40}\text{K}$  the half lives given in the evaluated libraries (Table 3) considered here carry  
 179 relatively large uncertainties, of 1.0-1.5% for the JEF2.2 and JEFF3.11 libraries, and 0.2% for  
 180 the ENSDF and DDEP libraries. In addition, the half lives vary significantly with the JEF2.2  
 181 value approximately 2.5% larger than that given in the ENSDF and DDEP libraries. This  
 182 difference in half life is significant when  $^{40}\text{K}$  activity is given in terms of elemental  
 183 composition (%K). In geochronology based on the decay of  $^{40}\text{K}$  it is desirable to know the  
 184  $^{40}\text{K}$  to the greatest possible precision. Given the importance of the  $^{40}\text{K}$  decay constants in  
 185 these communities, independent evaluations of the half life and branching ratios have been  
 186 conducted combining experimental nuclear physics data with Ar-Ar ages from independently  
 187 dated minerals. Half lives calculated by Min et.al. (2000) and Renne et.al. (2010) using these  
 188 approaches are also given in Table 3.

189

190 There is also considerable variation in the mean beta energies reported in each library,  
 191 ranging from ~450 keV to ~520 keV, corresponding to 5-10% variation in dose rate  
 192 conversion factors. The major difference to the mean energy is the shape of the beta-  
 193 spectrum assumed. To determine the mean beta decay energy, it is necessary to know the  
 194 shape and end-point energy of the beta spectrum. The end-point energy is well defined from  
 195 the atomic mass difference between  $^{40}\text{K}$  and  $^{40}\text{Ca}$ , at  $1311.07 \pm 0.12$  keV. The shape of the  
 196 beta spectrum is proportional to a factor  $pWq^2$  for sharing momentum between the leptons,  
 197 the Fermi function  $F(Z,W)$  and a shape factor  $C(W)$ .

$$\frac{dN}{dW} \propto pWq^2 F(Z,W) C(W)$$

198 where  $W$  is the total beta energy,  $Z$  is the atomic number of the daughter,  $p$  is the momentum  
 199 of the beta particle and  $q$  the momentum of the neutrino. Theoretical shape factors for  
 200 allowed or forbidden unique transitions are given by:

$$C(W) = (2L - 1)! \sum_{k=1}^L \lambda_k \frac{p^{2(k-1)} q^{2(L-k)}}{(2k - 1)! [2(L - k) + 1]!}$$

201 where  $L = \Delta J$ , and  $L = I$  for  $\Delta J = 0$ . The parameter  $\lambda_k$  cannot be calculated in a straightforward  
 202 manner, and typically an assumption that  $\lambda_k = 1$  is used.

203

204 The decay from  $^{40}\text{K}$  (ground state  $4^-$ ) to  $^{40}\text{Ca}$  (ground state  $0^+$ ) is a third unique forbidden  
 205 (3U) transition. The commonly used LOGFT program for calculating the shape of the  
 206 spectrum only calculates allowed and first and second unique forbidden (1U, 2U) transitions,  
 207 and when presented with any other transition defaults to an allowed transition shape.

208 Recalculations of the beta spectral shapes to evaluate the reliability of the  $\lambda_k = 1$   
 209 approximation (Mougeot 2015) have included the  $^{40}\text{K}$  beta spectrum using an experimental  
 210 shape factor from Leutz et.al. (1965). The program BetaShape (Mougeot 2015, 2016) has  
 211 been used to generate spectra for different shape factors theoretically with the  $\lambda_k = 1$   
 212 assumption and for experimental shape factors reported in the literature. These spectra are  
 213 plotted in Fig.3, with the data included in the supplementary material. The mean beta  
 214 energies have been calculated for these, and given in Table 4 with corresponding mean  
 215 energies from the LOGFT program for the allowed and first and second unique forbidden  
 216 transitions. The mean energy for the Leutz et.al. (1965) shape factor is identical to that  
 217 reported by Mougeot (2015). Recent high precision measurements of beta spectra have been  
 218 conducted (Carles & Kossert 2007), proposing a shape factor of the form  $C(W) = \lambda_1 p^6 +$   
 219  $\lambda_2 q^6 + 7p^2 q^2 (p^2 + q^2)$  for  $^{40}\text{K}$ , with  $\lambda_1 = 1.8$  and  $\lambda_2 = 1.23$ , to resolve discrepancies between  
 220 cutoff energy yield and maximum point energy. However, the authors note that this form of

221 shape factor fails Cherenkov counting tests, and in correspondence stated that they consider  
222 the spectrum generated by BetaShape using the Leutz et.al. (1965) shape factor is “the best  
223 choice for K-40 at this moment” (Kossert pers. comm.)  
224

225 Comparing the mean energy per decay in the different evaluations (Table 3) with the  
226 calculated mean energies for different shape factors (Table 4) it appears that the JEFF 3.11  
227 and DDEP evaluators have used the LOGFT program, letting the program default to an  
228 allowed transition shape. The DDEP evaluators (Mougeot & Helmer 2009) state that the  
229 mean energy is given by the LOGFT program without further elaboration. The mean energy  
230 reported by the ENSDF evaluation is consistent with forcing the LOGFT program to use a 2U  
231 shape factor, which would be closer to the 3U value. And, the JEF2.2 evaluators have a value  
232 consistent with the Leutz et.al. (1965) shape factor, with a marginally larger endpoint energy.  
233 It is noted that Lederer & Shirley (1978) also give a mean energy for  $^{40}\text{K}$  beta decay of  
234 583 keV, and this value is explicitly stated in the calculations of dose rate conversion factors  
235 of Aitken (1983, 1985), Bell (1976), Nambi & Aitken (1986) and Sanderson (1987).  
236 Subsequent calculations use the lower mean energy in the ENSDF library, Adamiec & Aitken  
237 (1998) note that this leads to a 4% reduction in the  $^{40}\text{K}$  beta conversion factor.  
238

239 The beta spectrum is also required to calculate absorbed dose fractions. Mejdahl (1979)  
240 recognised that this is a third unique forbidden transition, and used a spectrum transformed  
241 from a corresponding allowed shape using the method of Wu & Moszkowski (1966). Nathan  
242 et.al (2003) used a Fermi model spectrum with spectral factors from Behrens & Szybisz  
243 (1976), with the spectrum given in the supplementary information of Guérin et.al. (2012)  
244 having a mean energy of 508 keV, consistent with the use of an allowed spectral shape  
245 despite statements that spectral factors had been used.

246

247 **4. Discussion and Conclusions**

248 The estimation of dose rate from radionuclide concentrations requires accurate nuclear data  
249 covering half lives, branching ratios, emission energies and intensities. The use of evaluated  
250 libraries provides a convenient means of accessing this data to calculate conversion ratios.  
251 The evolution of the evaluated library reported in *Nuclear Data Sheets* and *Table of Isotopes*,  
252 and more recently formalised in the Evaluated Nuclear Structure Data File (ENSDF), has  
253 resulted in a variety of dose rate conversion factors being determined. However, with two  
254 additional sets of evaluations; the NEA/OECD JEF2.2 and JEFF3.11 libraries tailored for  
255 nuclear reactor and nuclear medicine applications, and the Decay Data Evaluation Project  
256 (DDEP); an assessment of the variations in relevant nuclear data across current versions of  
257 these different libraries has been conducted with the intention of identifying if the different  
258 evaluation processes significantly bias the resulting evaluated data and to identify which  
259 radionuclides might carry significant variations, and thus be needing further measurements to  
260 refine the nuclear data.

261

262 In the uranium series, combining both  $^{235}\text{U}$  and  $^{238}\text{U}$ , the JEF2.2/JEFF3.11 gamma conversion  
263 factors are 0.7% higher than the corresponding ENSDF/DDEP values, and conversely the  
264 beta conversion parameters are 1.5% lower. It has been shown that these differences are  
265 mostly due to differences in the data for  $^{214}\text{Bi}$ . These differences are due to the inclusion of a  
266 single high precision data set (Morel et.al. 2004) in the more recent ENSDF/DDEP  
267 evaluations. Although the absolute intensity of the 609 keV gamma ray from this is consistent  
268 with other measurements since the 1980s, within a 1-2  $\sigma$  limit, the ENSDF/DDEP evaluations  
269 are heavily biased to this single data set. It would be of benefit if an independent high  
270 precision data set confirmed the measurements of Morel et.al. (2004). It is considered that the

271 ENSDF and DDEP evaluations, incorporating the Morel et.al. (2004) data, are the best  
272 available, with the differences between them insignificant. For the purpose of calculating  
273 dose conversion factors, the mean of these is used with an uncertainty assigned that  
274 encompasses the  $1\sigma$  range of both values.

275

276 In the thorium series, the gamma conversion factors from the ENSDF/DDEP libraries are  
277 ~3.5% lower than for the JEF2.2/JEFF3.11 libraries. It has been shown that these differences  
278 are largely derived from differences in the  $^{228}\text{Ac}$  nuclear data. Although this has not been  
279 examined in detail here, the DDEP evaluator (Pearce 2009) noted that the decay data for this  
280 radionuclide is incomplete with an ~7% discrepancy between beta and gamma intensity data,  
281 and recommended that further experimental gamma data be collected with particular  
282 emphasis on low energy gammas and coincidence measurements to confirm the level scheme.  
283 It is considered that the ENSDF/DDEP evaluations are the likely to underestimate total  
284 gamma and beta energies per decay by 2-4%, and for this work it has been assumed that the  
285 ENSDF/DDEP values should be used with an additional 3% added to them, with the  
286 uncertainty increased by 10%.

287

288 For  $^{40}\text{K}$  and  $^{87}\text{Rb}$ , there is considerable variation in both beta and gamma dose conversion  
289 factors between the four contemporary evaluated libraries and the literature values from  
290 different versions of the ENSDF library, with 3-12% variation in the beta conversion  
291 parameters and 1-4% variation for the gamma conversion parameters. These variations reflect  
292 differences in  $^{40}\text{K}$  nuclear data in different evaluations; with 2-5% variation in half life  
293 values, upto 15% variation in mean beta energy, and small variations in branching ratios.

294

295 The  $^{40}\text{K}$  half life is also critical to geochronology, and independent evaluations of nuclear  
296 data and Ar-Ar measurements of known age minerals by the geochronology community has  
297 produced half-life values consistent with the latest ENSDF and DDEP evaluations with  
298 similar precision of  $\sim 0.2\%$ . The mean of the ENSDF & DDEP values for the half life has  
299 therefore been taken as the best value currently available, with uncertainties to encompass the  
300  $1\sigma$  range of both values. The dominant difference between evaluated libraries is the mean  
301 beta decay energy, which reflects the shape of the decay spectrum used. The LOGFT  
302 program most commonly used to calculate mean energies and branching ratios does not  
303 include the 3U transition needed to model the  $^{40}\text{K}$  decays to  $^{40}\text{Ca}$  and the  $^{40}\text{Ar}$  ground state.  
304 Thus, approximations are made in the calculations of mean energy and branching ratio, the  
305 difference in mean energy reflects the difference between using a 2U or an allowed transition  
306 as an approximation to the 3U transition. The use of an alternative program, BetaShape, that  
307 does allow for 3U shape factors results in an increase in the calculated mean energy. At  
308 present, experimental shape factors for the  $^{40}\text{K}$  decay are poorly measured, especially in the  
309 low energy ( $<100$  keV) region, and additional precision measurements of the  $^{40}\text{K}$  beta  
310 spectrum would be of considerable benefit in more accurately determining experimental  
311 shape factors. However, it would be surprising if future experimental data results in a mean  
312 energy significantly different from  $585 \pm 5$  keV, with the best current measurement giving a  
313 mean energy of  $583.98 \pm 0.10$  keV (Leutz et.al. 1965, Mougeot 2015) which includes an  
314 uncertainty twice that given by this shape factor.

315

316 Based on our assessment of what are currently the best nuclear data as reviewed here, dose  
317 rate conversion factors can be calculated (Table 5). In most cases, these are consistent with  
318 values currently regularly used (Adamiec & Aitken 1998, Guérin et.al. 2011, Liritzis et.al.  
319 2013). The exception is the K+Rb beta parameter which is approximately 4% larger, in line

320 with earlier calculations using the 583 keV mean energy of Lederer & Shirley (1978),  
321 including the calculations of Aitken (1983) which had been widely used prior to adoption of  
322 the newer values. It should be noted that although these conversion factors are determined  
323 using our assessment of the best available data, there are still serious doubts regarding that  
324 data. As such, these factors are provisional subject to clarification of the inconsistencies in  
325 the nuclear data.

326

327 These conversion factors have been used to calculate dose rates for a standard mineral  
328 composition following the assumptions of Adamiec & Aitken (1998) for alpha efficiency,  
329 beta attenuation and cosmic contributions. These are given in Table 6 with values given by  
330 Adamiec & Aitken (1998) for comparison. In all instances, the total dose rates are slightly  
331 larger than those calculated by Adamiec & Aitken (1998), and generally in agreement with  
332 those of Nambi & Aitken (1986) except for  $^{40}\text{K}$  (where the current work predicts higher dose  
333 rates) and Th gamma.

334

335 It is clear that the choice of dose rate conversion factors to be used is still to be fully resolved.  
336 The values suggested here may be used, but without resolution of significant doubts in the  
337 nuclear data it may be preferable to maintain continuity with prior work by not changing the  
338 values used with each new revision. Whatever values are used, it should be recognised that  
339 propagating uncertainties in the evaluated libraries would underestimate the true  
340 uncertainties. In this work, uncertainties in the parameters are in the range of 1-3%, previous  
341 studies (Aitken 1985, following Bell 1979) have noted that 5% is the maximum error likely to  
342 occur. In addition, the values used should be clearly stated when reporting dose rates.

343

344



345

346 **Acknowledgements**

347 The authors acknowledge with thanks the constructive discussions with Dr Ryan Ickert  
348 (SUERC) regarding  $^{40}\text{K}$  half life evaluations used in Ar-Ar dating.

349

350

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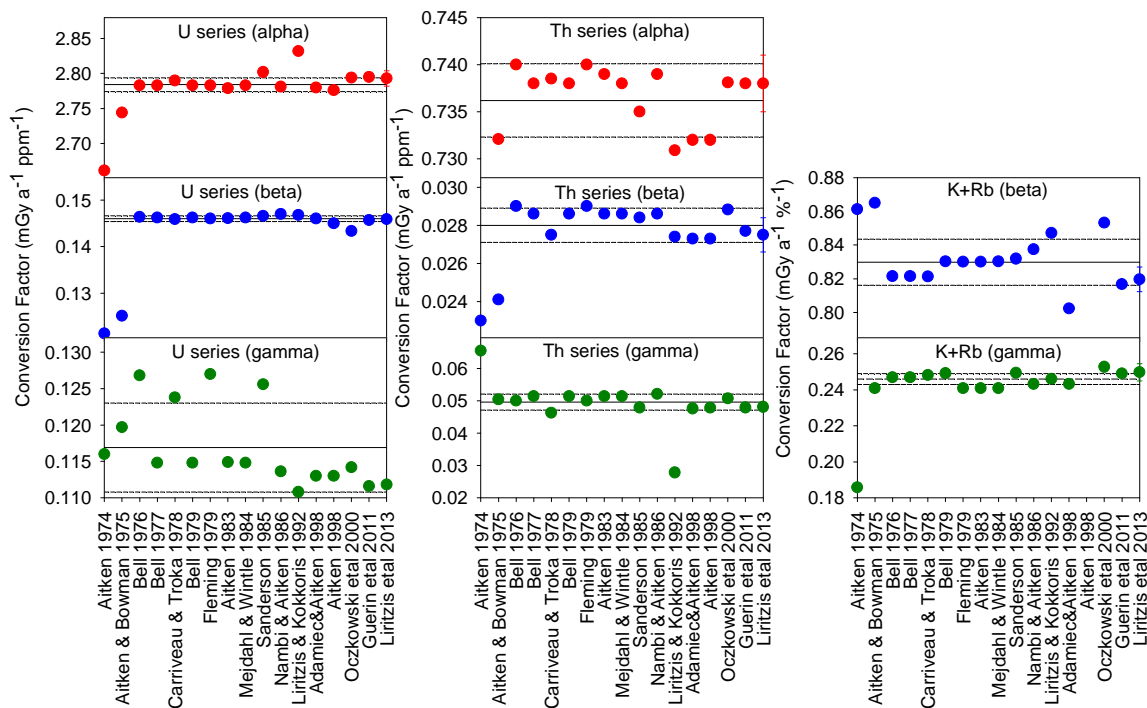
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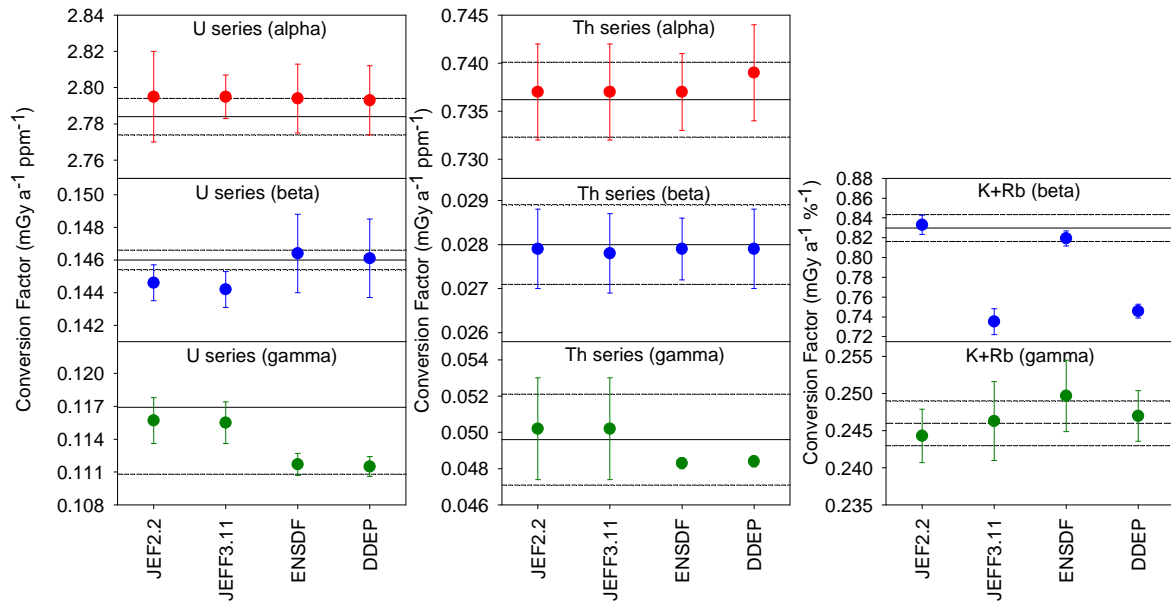
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474 Figure 1: Dose rate conversion factors for the uranium series ( $^{235}\text{U} + ^{238}\text{U}$ ), Th series ( $^{232}\text{Th}$ )  
 475 and  $^{40}\text{K}$  taken from the literature. The control lines show the robust mean  $\pm 1$  standard  
 476 deviation.

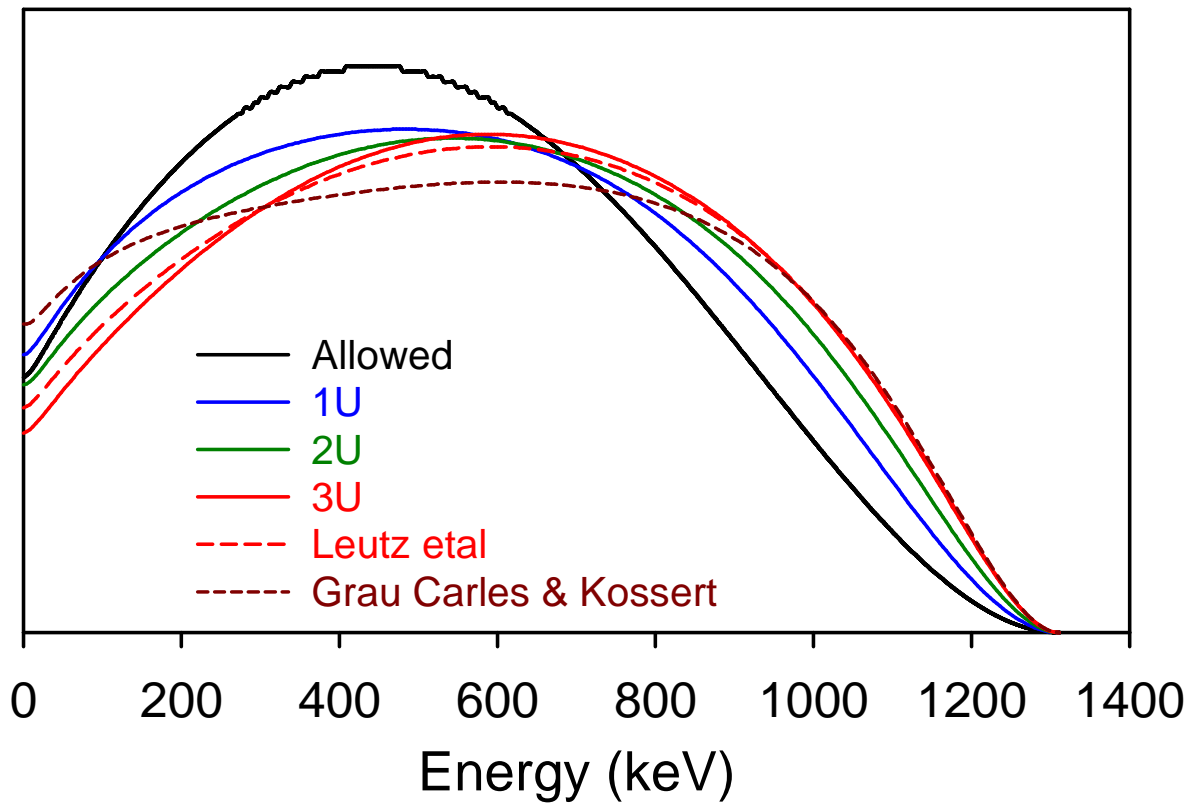
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478 Figure 2: Dose rate conversion factors for the uranium series ( $^{235}\text{U} + ^{238}\text{U}$ ), Th series ( $^{232}\text{Th}$ )  
 479 and  $^{40}\text{K}$  calculated from four evaluations. The control lines show the robust mean  $\pm 1$   
 480 standard deviation from previous literature values (Fig. 1).

481





482 Figure 3: Beta spectra calculated by the BetaShape program (Mougeot 2015, 2016) using  
 483 theoretical shape factors, with the  $\lambda_k=1$  assumption, for allowed and first, second and third  
 484 unique forbidden transitions, and for experimentally derived shape factors reported by Leutz  
 485 et.al. (1965) and Carles & Kossert (2007). All spectra are calculated using an endpoint energy  
 486 of 1311.07 keV.

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489

490 Table 1: Mean gamma and beta energies per decay of  $^{214}\text{Bi}$  calculated from different  
491 evaluated libraries

	Mean energy per decay (keV)	
	Gamma	Beta
JEF 2.2/JEFF 3.11	$1536.9 \pm 30.3$	$613.7 \pm 15.5$
ENSDF	$1474.1 \pm 1.6$	$640.0 \pm 3.3$
DDEP	$1467.8 \pm 1.9$	$645.8 \pm 3.7$

492

493

494 Table 2: Mean gamma energies per decay of  $^{228}\text{Ac}$  calculated from different evaluated  
495 libraries

	Mean energy per decay (keV)
JEFF 3.11	$955.6 \pm 133.8$
ENSDF	$864 \pm 10$
DDEP	$864 \pm 10$

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499 Table 3:  $^{40}\text{K}$  half lives, beta- branching ratios and energies from different evaluations

	Half life ( $\times 10^9$ a)	End point (keV)	Mean energy / beta decay (keV)	Branching %	Mean energy / $^{40}\text{K}$ decay (keV)
JEF2.2	$1.280 \pm 0.010$	$1311.6 \pm 0.5$	$584.9 \pm 0.6$	$0.893 \pm 0.001$	$521.48 \pm 0.62$
JEFF 3.11	$1.265 \pm 0.020$	$1311.04 \pm 0.12$	$508.29 \pm 0.05$	$89.15 \pm 0.13$	$453.16 \pm 0.66$
ENSDF	$1.248 \pm 0.003$	$1311.07 \pm 0.12$	$560.18 \pm 0.05$	$89.14 \pm 0.18$	$499.3 \pm 1.0$
DDEP	$1.2504 \pm 0.0030$	$1311.07 \pm 0.12$	$508.32 \pm 0.05$	$89.25 \pm 0.17$	$453.68 \pm 0.87$
Min etal (2000)	$1.269 \pm 0.025$				
Renne etal (2010)	$1.2479 \pm 0.0024$				

500

501

502 Table 4: Mean beta energies calculated for an endpoint energy of 1311.07 keV using the  
 503 BetaShape program (Mougeot 2015, 2016) for theoretical shape factors, assuming  $\lambda_k=1$ , and  
 504 experimentally measured shape factors. With mean energies from the LOGFT program for  
 505 comparison.

	C(W)	Mean beta energy (keV)	
		BetaShape	LOGFT
Allowed	1	$507.83 \pm 0.05$	$508.31 \pm 0.05$
1U	$p^2 + q^2$	$536.08 \pm 0.05$	$534.04 \pm 0.05$
2U	$p^4 + q^4 + \frac{10}{3}p^2q^2$	$563.01 \pm 0.05$	$560.18 \pm 0.05$
3U	$p^6 + q^6 + 7p^2q^2(p^2 + q^2)$	$587.89 \pm 0.05$	
Leutz et.al. 1965	$0.95p^6 + 1.05q^6 + 6.3p^2q^4 + 6.25q^2p^4$	$583.98 \pm 0.05$	
Carles & Kossert 2007	$1.8p^6 + 1.23q^6 + 7p^2q^4 + 7q^2p^4$	$569.26 \pm 0.05$	

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509 Table 5: Dose rate conversion factors based on current best nuclear data. The data used are  
 510 from the DDEP library with the exception of  $^{214}\text{Bi}$  (mean of ENSDF and DDEP),  $^{228}\text{Ac}$  (the  
 511 ENSDF and DDEP values increased by 3%) and  $^{40}\text{K}$  mean beta energy (from the Leutz et.al.  
 512 1965 shape factor), and  $^{87}\text{Rb}$ ,  $^{230}\text{Th}$ ,  $^{228}\text{Ra}$  and  $^{227}\text{Th}$  which are not currently included in the  
 513 DDEP library (ENSDF data used for these).

	$^{238}\text{U} + ^{235}\text{U}$ mGy a <sup>-1</sup> ppm <sup>-1</sup>		$^{232}\text{Th}$ mGy a <sup>-1</sup> ppm <sup>-1</sup>		$^{40}\text{K} + ^{87}\text{Rb}$ mGy a <sup>-1</sup> % <sup>-1</sup>
	Total	Pre-Rn <sup>1</sup>	Total	Pre-Rn <sup>1</sup>	
Alpha	2.79 ± 0.02	1.27 ± 0.01	0.738 ± 0.004	0.309 ± 0.002	
Beta	0.142 ± 0.002	0.056 ± 0.001	0.028 ± 0.001	0.0096 ± 0.0007	0.854 ± 0.008
Gamma	0.112 ± 0.001	0.0037 ± 0.0001	0.0489 ± 0.0003	0.0188 ± 0.0002	0.248 ± 0.003

514 <sup>1</sup> The columns labelled 'Pre-Rn' give values for 100% escape of radon for  $^{238}\text{U}$  and  $^{232}\text{Th}$ , but  
 515 include the full  $^{235}\text{U}$  decay series due to the short half life of  $^{219}\text{Rn}$ , following the approach of  
 516 Adamiec & Aitken 1998.

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518

519 Table 6: Dose rates (mGy a<sup>-1</sup>) for a standard concentration from Nambi & Aitken, 1986  
 520 (N&A 86), Adamiec & Aitken 1998 (A&A 98) and the current work, assuming zero moisture  
 521 content.

		1% K	50 ppm Rb	3 ppm Th	1 ppm U	Total
Effective alpha <sup>1</sup>	N&A 86			0.190	0.222	0.413
	A&A 98			0.183	0.218	0.401
	This work			0.190	0.223	0.413
Beta	N&A 86	0.814	0.023	0.086	0.147	1.071
	A&A 98	0.782	0.019	0.082	0.146	1.029
	This work	0.835	0.019	0.084	0.142	1.080
Gamma <sup>2</sup>	N&A 86	0.243		0.156	0.114	0.693
	A&A 98	0.243		0.143	0.113	0.679
	This work	0.247		0.147	0.112	0.686
Fine- grain total	N&A 86	1.058	0.023	0.433	0.489	2.18
	A&A 98	1.025	0.019	0.408	0.477	2.11
	This work	1.082	0.019	0.421	0.477	2.18
Coarse grain total <sup>3</sup>	N&A 86	0.976	0.018	0.234	0.246	1.65
	A&A 98	0.947	0.014	0.217	0.244	1.60
	This work	0.999	0.014	0.223	0.240	1.66

522 <sup>1</sup> Effective alpha dose rates are derived using  $k=0.1$  and  $k_{eff} = 0.86$  (Th) and 0.80 (U),

523 following Adamiec & Aitken (1998).

524 <sup>2</sup> Total gamma includes 0.180 mGy a<sup>-1</sup> as a cosmic component, following Adamiec & Aitken  
 525 (1998).

526 <sup>3</sup> Beta attenuation factors for coarse grains taken as 0.90, except for Rb which is taken as  
 527 0.75, following Adamiec & Aitken (1998).

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