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One-dimensional steady-state thermal model for rotary kilns used in the manufacture of cement

--Manuscript Draft--

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| Abstract: | <p>Rotary kilns are used extensively in the cement industry to convert raw meal into cement clinker. In order to optimize the operation of cement kilns, computationally efficient thermal models are required. In this work, the development of a one-dimensional thermal model for kilns is explored. To simplify the model, the kiln is assumed to be well mixed in the transverse direction. A simultaneous mass and energy balance is solved based on a steady-state approximation. Existing semi-empirical models for heat transfer in the kiln are implemented and critically evaluated. The resulting one-dimensional model is capable of predicting axial temperature profiles in the rotary kiln which agree well with the available experimental data found in the literature. The model presented extends from previous models by considering a full enthalpy balance for the gas in the kiln. This allows the model to be used in a fully predictive manner, taking into account the temperature-dependent thermodynamic, transport, and radiative properties of the gas phase.</p> |

Dear editor and reviewer:

Thank you for your feedback and consideration of our work for publication. This letter contains in-line response (in red font) to your comments. The changes in the text document are also in red font as requested. Some changes to the document not relating to the reviewers comments have also been made; these are:

Pg1Ln2: The title has been changed in order to more clearly describe the content of the paper.

Table 3: Values have changed slightly due to a minor mistake found in the programming code after submission. The new values reported are based on calculations after correction.

Supplementary material 5: This material has been removed as they are superfluous. They are not needed to repeat the simulations.

Section numbers of conclusions and acknowledgement have been corrected; section number "5" was repeated in the initial submission.

Pg6Ln36: Boltzmann was spelled incorrectly and is now corrected.

For consistency throughout the paper, all subscripts "amb" in all equations have been changed to "ext"(external).

Reference numbering has been corrected.

Typographical errors have been corrected in the document "Supplementary material summary". The correction is from "degrees Celsius" to "Kelvin" x 2.

Figure 2 has been corrected. Previous submitted image was labelled degrees Celsius but was mistakenly plotted in Kelvin.

A new figure has been added to provide an example of the model works on the Tscheng kiln.

In order to better organize the supplementary material, the data in supplementary material 4 have been transposed.

Comments from the Editors and Reviewers:

Reviewer #1: This paper describes a computational model of heat transfer within a rotary kiln. The authors state that it can be developed to provide predictive performance modeling of kiln operations with a target of improving production efficiency of the cement industry. The paper is well written and provides a concise explanation of the derivation of the energy balance equation forming the basis of the model.

Thank you for your kind remarks.

Reviewer Comments

Pg5Ln1. An assumption is made of constant gas velocity for the model, but in Supplementary Material 2 of experimental data of the Barr pilot kiln experiments there are data columns for "primary" and "secondary" air flow rate. Is this impactful to the average error values reported?

No, this should not impact the average error of the values. The rate for air used in our calculations is the sum of the "primary" and "secondary". This has now also been clarified in the text in the first paragraph of section 4. Thank you.

Pg5Ln30. An inconsistency in the citation of referencing is noted. At this point in the text "...Ref. XX" is used, while later (Pg6Ln53) "...Ref. [XX]" is used. It's suggested that picking one format for the entirety of the paper will prove to be clearer.

Thank you for spotting this; we have now corrected the referencing.

Pg6Ln48. The authors state that the value of the gas film thickness has an optimum value of 0.1 for sand particles between approximately 150 microns and 1mm (which is hopefully consistent with the gradation of "Ottawa sand" referenced in the following paragraph although not stated in the text). As the targeted application of this paper is the cement industry - for which the clinkerization process may start with fine powder but develop into larger (>1mm) clinker granules, with a possible melt phase occurring along the length of the kiln - could the authors provide some context as to how the gas film thickness will vary in a cement rotary kiln?

The particle size diameter is provided in the text; for the Tscheng experiments as stated on in the second paragraph of section 4 as follows:

"In addition to the data files, the remaining information required to reproduce this work which is not provided in the supplementary material is that the solid particle diameter of all the Tscheng trials was 0.73 mm"

Also, the particle size diameter for the Barr experiments is provided in Supplementary Material 2.

Further experiments would need to be carried out to find the effect of the growing clinker nodules. i.e., the clinker particle size as a function of temperature would need to be evaluated. A new optimum can then be deduced for cement kilns or a fit produced and used to input gas film thickness as a function of particle size.

Pg8Ln49. The sentence "It is a major industrial concern and energy efficiency one of the primary focuses of current research...", may read clearer if amended to "It is a major industrial concern and energy efficiency is one of the primary focuses of current research...".

Thank you; this has now been changed.

Title:**One-dimensional steady-state thermal model for rotary kilns used in the manufacture of cement**

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Abstract

Rotary kilns are used extensively in the cement industry to convert raw meal into cement clinker. In order to optimize the operation of cement kilns, computationally efficient thermal models are required. In this work, the development of a one-dimensional thermal model for kilns is explored. To simplify the model, the kiln is assumed to be well mixed in the transverse direction. A simultaneous mass and energy balance is solved based on a steady-state approximation. Existing semi-empirical models for heat transfer in the kiln are implemented and critically evaluated. The resulting one-dimensional model is capable of predicting axial temperature profiles in the rotary kiln which agree well with the available experimental data found in the literature. The model presented here extends from previous published models by considering a full enthalpy balance for the gas in the kiln. This allows the model to be used in a fully predictive manner, taking into account the temperature-dependent thermodynamic, transport, and radiative properties of the gas phase.

Keywords: Rotary kiln, heat transfer, cement, clinker, thermal model

List of symbolsSymbols

| | | |
|----------|------------------------|---------------------------------------|
| α | (dimensionless) | Absorptivity |
| Ω | (rad s ⁻¹) | Angular velocity of kiln |
| h_b | (m) | Bed height |
| Φ | (dimensionless) | Bed solid volume fraction |
| θ | (rad) | Central angle formed by the solid bed |
| L_c | (m) | Chord length of the solid bed |

| | | | |
|----|---------------|--|-----------------------------|
| 1 | ρ | (kg m ⁻³) | Density |
| 2 | μ | (kg m ⁻¹ s ⁻¹) | Dynamic viscosity |
| 3 | ε | (dimensionless) | Emissivity |
| 4 | F | (dimensionless) | Form/view factor |
| 5 | χ | (dimensionless) | Gas film thickness |
| 6 | Gr | (dimensionless) | Grashof number |
| 7 | Q | (W m ⁻¹) | Heat flux per unit length |
| 8 | h | (W m ⁻² K ⁻¹) | Heat transfer coefficient |
| 9 | D_h | (m) | Hydraulic diameter |
| 10 | C_p | (kJ kg ⁻¹ K ⁻¹) | Isobaric heat capacity |
| 11 | D | (m) | Kiln inner diameter |
| 12 | D_o | (m) | Kiln outer diameter |
| 13 | η | (dimensionless) | Kiln solid loading fraction |
| 14 | \dot{m} | (kg s ⁻¹) | Mass flow rate |
| 15 | L_m | (m ⁻¹) | Mean beam length |
| 16 | Nu | (dimensionless) | Nusselt number |
| 17 | d_p | (m) | Particle diameter |
| 18 | P | (m) | Perimeter for heat transfer |
| 19 | Pr | (dimensionless) | Prandtl number |
| 20 | Ra | (dimensionless) | Rayleigh number |
| 21 | σ | (W m ⁻² K ⁻⁴) | Stefan Boltzmann constant |
| 22 | T | (K) | Temperature |
| 23 | k | (W m ⁻¹ K ⁻¹) | Thermal conductivity |
| 24 | R | (m ² K W ⁻¹) | Thermal resistance |
| 25 | v | (m s ⁻¹) | Velocity |

Superscripts and Subscripts

| | | |
|----|-----|---------------------------------|
| 26 | an | Angular |
| 27 | ax | Axial |
| 28 | b | Bulk bed |
| 29 | cd | Conduction |
| 30 | cv | Convection |
| 31 | cw | Covered wall |
| 32 | ext | External |
| 33 | g | Gas |
| 34 | j | j^{th} kiln wall layer |
| 35 | rd | Radiation |
| 36 | sh | Shell |
| 37 | s | Solid bed |
| 38 | w | Wall |

1. Introduction

Rotary kilns are crucial **processing units** in the chemical, metallurgical, and pharmaceutical industries. The rotary kiln is popular as it is the most advanced high-throughput and high-temperature industrial kiln technology. It is also the preferred choice in cement manufacture where production rates approach kilotons per day and many of the critical reactions take place at temperatures up to 1500°C. The world demand for cement is on the increase and at present the cement industry consumes approximately 12–15% of the global industrial energy

1 demand.¹ The cement industry also emits approximately 5–8% of global CO₂ emissions
2 which arise from the decomposition of limestone and the combustion of fuels.^{2,3} It is therefore
3 vital that kilns are well understood to allow the optimization of heat-transfer in existing kiln
4 installations. In addition, it is essential that detailed models for the kiln are available so that
5 novel low-carbon cement formulations can be designed and developed. Finally, to enable
6 effective scale-up of lab based processes to pilot or industrial scales it is crucial that the
7 conditions within the kiln are well characterized.
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10 Unfortunately, the conditions within a kiln are not homogeneous and there is a complex
11 relationship between the reactions, mass transfer, heat transfer, and mechanical dynamics of
12 the processed material. Despite these difficulties, existing literature has focused on creating
13 one-dimensional models which can capture quantitatively the kiln operation while remaining
14 computationally tractable for optimization studies. A coarse-grained computational model
15 which is capable of predicting the thermal performance of the kiln within seconds is essential
16 to enable plant-wide process optimization.
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19 Li et al.⁴ were one of the first to develop a simple full-kiln heat-transfer model while
20 developing an extended penetration theory to model the wall-bed heat transfer within
21 unreactive rotary kilns. Mujumdar and Ranade⁵ also developed a one dimensional model
22 where they use a simple kinetic model to approximate reactions within the kiln. It should be
23 noted that including a detailed kinetic model is extremely difficult as not all chemical
24 reactions occurring in the cement production process are known, nor is the kinetic data
25 available. Finally, Romero Valle⁶ developed a heat transfer model which combines the two
26 aforementioned studies and the model presented here is based on that work. The models
27 introduced predict the temperatures of the solid bed, the wall, and the outer shell. The work
28 presented here improves on these previous works by also calculating the gas-phase
29 temperature and considers accurate temperature-dependent thermodynamic descriptions of the
30 solid and gas phases within the kiln. These improvements allow the model to be used in a
31 fully predictive manner without measuring the gas temperatures of the target kiln during
32 operation. There are commercial kiln models available which go beyond many of the
33 approximations within this study, e.g. KilnSimu;⁷ however, the detailed implementation of
34 these models is not yet widely available. As this study aims to validate the performance of
35 current heat-transfer models for kilns, it is tested against the full range of available
36 experimental data for inert beds from Barr⁸ and Tscheng⁹, whereas previous studies have only
37 used a limited subset of this data. The Tscheng kiln is shorter (2.44 m) than the Barr kiln
38 (5.5 m) and is operated at lower temperatures. This difference in operation allows a closer
39 evaluation of the convective and radiative transport models. The experimental data used here
40 has been carefully compiled and, where required, digitized from the original sources and the
41 resulting data files are available in the supplementary material to support further development
42 in this field.
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49 In the following two sections the kiln model is outlined and its approximations are discussed.
50 Section 4 validates the model against the available experimental data before the conclusions
51 are presented in Sec. 5.
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53 **2. Mass balance**

54 In conventional cement manufacture, the kiln is operated as a combined counter-current heat
55 exchanger and reactor. As illustrated in Fig. 1, the solid phases enter at the cold end of the
56 kiln and travel towards the burner while the gas phase flows in the opposite direction. In this
57 study, only experiments with unreactive beds are considered to allow a detailed examination
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of the thermal model. As such, there is no interchange of mass between phases and compositions can be assumed to remain constant along the length of the kiln. Pressure drop is also ignored along the kiln resulting in a constant gas velocity. In addition, the experimental studies considered here were carried out carefully to ensure a relatively constant bed height along the length of the kiln.^{8,9} This originally facilitated the development of the kiln heat transfer models and allows this study to isolate and validate the performance of these models within a more complete description of the kiln.

3. Energy balance

A one-dimensional model for inert constant-bed-height kilns can be constructed by performing a differential enthalpy balance over a transverse slice of the kiln. Within each slice, the solid and gas phases are treated as separate but homogeneous thermal bodies at a temperature T_s and T_g respectively. Assuming steady state, separate enthalpy balances for the solid and gas phases yield the following differential equations,

$$\dot{m}_s C_{p,s} \frac{\delta T_s}{\delta x} = Q_{g \rightarrow s}^{cv} + Q_{w \rightarrow s}^{cd} + Q_{g \rightarrow s}^{rd} + Q_{w \rightarrow s}^{rd} \quad (\text{Eq. 1})$$

$$\dot{m}_g C_{p,g} \frac{\delta T_g}{\delta x} = -(Q_{g \rightarrow s}^{cv} + Q_{g \rightarrow w}^{cv} + Q_{g \rightarrow s}^{rd} + Q_{g \rightarrow w}^{rd}), \quad (\text{Eq. 2})$$

where C_p is the isobaric heat capacity, \dot{m} is the mass flux, and Q is a heat flux per unit length of the kiln at the current distance, x , along the kiln. On the heat flux terms, the superscripts indicate convective (cv), radiative (rd), or conductive (cd) terms whereas the subscripts indicate the phases exchanging heat and the corresponding sign convention (see Fig. 1). As the bed composition is constant, the heat capacity is only a function of temperature. Gas heat capacity data are taken from Ref. 10 and solid heat capacity data are taken from Ref. 11.

The use of the temperatures T_g and T_s in the balance equations fixes their definition as the temperatures of homogeneous phases which have the same enthalpy as the real phase. It is not immediately apparent that temperatures homogenized in this way are appropriate to use as the driving forces for heat transfer between the phases and surroundings. Assuming constant heat transfer resistances, the linear average of the temperature at the interface of each thermal body is required for conduction and convection calculations while a fourth-order volumetric average of temperature is required for gas radiation calculations: therefore no single homogenized value of the temperature is exactly appropriate. The gas has significant variations in temperature over its volume;¹² however, the results of using first and fourth order averaging of temperature has been found to be numerically close in this case.¹³ This study, in-line with previous work,⁶ will directly use the homogeneous temperatures in the integrated heat transfer expressions and look to validate this approach as part of the study. It should also be noted that the assumption of a well-mixed solid bed is generally appropriate due to the design of a rotary kiln which promotes transverse mixing and often operates at low solid loadings.¹⁴ The effect of the temperature gradient driving axial conduction is also neglected in this work for simplicity; however, due to the large aspect ratio of kilns (and the solid bed) the error brought about by this assumption is expected to be relatively small.⁴

As part of the calculations of the heat flux, the outer shell and inner wall temperatures are required. Again, for simplicity these bodies are assumed to be homogeneous in temperature which reduces the representative temperature field to a single value and neglects internal effects such as wall to wall radiative heat transfer. At steady state, the internal wall

temperature, T_w , and external shell temperature, T_{sh} , can be solved for implicitly via an energy balance,

$$Q_{w \rightarrow ext} = Q_{g \rightarrow w}^{rd} + Q_{g \rightarrow w}^{cv} - Q_{w \rightarrow s}^{rd} - Q_{w \rightarrow s}^{cd} \quad (\text{Eq. 3})$$

$$Q_{w \rightarrow sh} = Q_{g \rightarrow w}^{rd} + Q_{g \rightarrow w}^{cv} - Q_{w \rightarrow s}^{rd} - Q_{w \rightarrow s}^{cd}. \quad (\text{Eq. 4})$$

This set of differential algebraic equations, (1) to (4), is solved simultaneously for each differential slice to calculate the temperatures of the system along the length of the kiln. The solver used here is an implicit differential algebraic solver (Implicit_Problem from Ref. 15) using 30 steps in x , with absolute and relative tolerances both set at 10^{-4} . To complete the model, expressions for the heat fluxes are required and these are described in the following subsections.

3.1. Conduction/Penetration between the solid bed and the kiln internal walls ($Q_{w \rightarrow s}^{cd}$)

Heat transfer between the underside of the solid bed and the internal wall which it covers plays an important role in the heat transferred. Although this effect is notionally denoted here as a conductive heat transfer due to the close proximity of the bed and wall, the three dominant mechanisms for heat transfer in this case are actually conduction through the gas film between the wall and the bed, direct solid-wall contact conduction, and advective heat transfer near the bed edges. Older conduction models did not take into account the presence of a gas film;^{16,17} however, Lehmberg et al.¹⁸ first included terms for a gas film and presented a complex model which cannot readily be used for design purposes due to its requirement of additional experimental parameters. Tscheng⁹ attempted to correlate experimental data¹⁶⁻¹⁸ and proposed a model that is restricted to relatively low temperatures and does not take into account the effect of particle size. Li et al.⁴ later extended penetration theory for packed beds and fluidized bed reactors developed by Schluender¹⁹ to describe the heat transfer between the bulk solids and the covered internal wall in a rotary kiln. **Their model, validated against experiments,^{18,20} presents the heat transfer coefficient as,**

$$h_{cw \rightarrow s}^{cd} = \frac{\chi d_p}{k_g} + \frac{0.5}{\sqrt{\frac{2k_b \rho_b C_{p,s} \omega}{\theta}}},$$

where χ is a dimensionless thickness of the gas film, d_p is the particle diameter, k is the thermal conductivity, ρ_b is the bulk density, ω is the angular velocity of the kiln, $\theta = 2 \sin^{-1}(L_c)/D$ is the central angle formed with the solid bed, D , is the kiln internal diameter, and L_c is the chord length of the solid bed. The gas film thickness, χ , is reported to be in the range of 0.096 – 0.198 for rotary kilns, with an optimum value of 0.1 in rotary kilns as calculated for sand with particles size in the range 0.1575–1.038mm;⁴ this value is used in all of our calculations. The temperature-dependent transport properties of the gas phase and the surroundings (discussed later on) such as thermal conductivities and viscosities are taken from Ref. 21. In our model, the effective bed thermal conductivity, k_b , is calculated using the Maxwell model based on effective medium theory as shown below,

$$k_b = \left(\frac{2k_g + k_s + 2\Phi(k_s - k_g)}{2k_g + k_s - \Phi(k_s - k_g)} \right) k_g,$$

where Φ is the bed solid volume fraction. Ottawa sand, which is the solid feed used in all experimental trials considered here, is composed of naturally rounded grains of nearly pure quartz²² and is here assumed to be 100% quartz. Temperature dependent thermal conductivity data for quartz up to 700K is readily available.²³ Above this temperature, the thermal conductivity is assumed to be constant as suggested by Yoon et al.²⁴ Solid densities and particle diameters are each taken from the sources of the individual experiments.^{8,9} Finally, the heat flux is calculated as follows,

$$Q_{w \rightarrow s}^{cd} = h_{cw-s}^{cd} P_{cw-s} (T_w - T_s),$$

where $P_{cw-s} = \theta D / 2$ is the perimeter of the wall in contact with the solid bed.

3.2. Radiation ($Q_{g \rightarrow w}^{rd}$, $Q_{w \rightarrow s}^{rd}$, $Q_{g \rightarrow s}^{rd}$)

The cement kiln enclosure contains a mixture of gases generated from the combustion of fuels and chemical reactions occurring within the kiln. In our simulations, the gas is assumed to be either dry air (see Table 1) or the result of complete combustion of the natural gas in dry air. To achieve an accurate description of radiative heat transfer within the kiln, evaluation of the emissive and absorptive properties of these gas mixtures is required. The procedure of Hottel and Sarofim²⁵ is followed here using temperature dependent total gas mixture absorptivity and emissivity correlations with linear extrapolation.²⁶ The emissivity of the surfaces of the bed, wall, and shell are assumed to be standard values reported in literature:⁶ 0.9, 0.85, and 0.8 respectively. Due to the complexity involved in accounting for a large series of emissivity relations due to partial and second incidence absorption, reflection and transmission, the radiative heat transfer between the gas and bed or wall are calculated using a simplified radiation model,²⁵

$$Q_{g \rightarrow s/w}^{rd} = \sigma (\varepsilon_{s/w} + 1) P_{g-s/w} \frac{\varepsilon_g T_g^4 - \alpha_g T_{s/w}^4}{2}, \quad (\text{Eq. 5})$$

where σ is the Stefan Boltzmann constant, ε is an emissivity, and α is an absorptivity which are both a function of the mean beam length (L_m). The correlation of Gorog et al.²⁷ is used to calculate the average mean beam length which includes reflection effects:

$L_m = 0.95D(1 - h_b/D)$ where h_b is the height of the bed. Depending on whether this equation is for the solid or the wall (s/w), the perimeter is either $P_{g-s} = L_c$ (exposed bed) or

$P_{g-w} = \pi D - \theta D / 2$ (exposed wall). Equation (5) is derived from the expression for the radiative heat transfer rate from a gas to a black surface multiplied by a low-order correction factor, $(\varepsilon_{s/w} + 1)/2$, for the emissivity of the surface. Hottel and Sarofim have shown that if the emissivity of the surface is high ($\varepsilon_{s/w} \geq 0.8$), the error introduced by use of this truncated expression does not exceed 10%.²⁵ Radiative heat transfer between the internal wall and the solid bed is calculated using the following expression,²⁵

$$Q_{w \rightarrow s}^{rd} = \frac{\sigma (T_w^4 - T_s^4)}{(1 - \varepsilon_w) / \varepsilon_w P_{s-w} + 1 / F_{s \rightarrow w} P_{w-s} + (1 - \varepsilon_s) / \varepsilon_s P_{w-s}},$$

where $F_{s \rightarrow w}$ is the bed to wall form/view factor ($F_{s \rightarrow w} = 1$ for flat beds) and P_{w-s} is the perimeter of the exposed bed, and P_{s-w} is the perimeter of the exposed wall as defined earlier.

1 It should be noted that both radiative expressions ignore axial radiation for simplicity and
 2 computational efficiency. The gas-solid/wall and solid-wall radiation effects are decoupled for
 3 simplicity as well. A more detailed model which includes these effects would require
 4 additional computational cost which appears not to be justified here.
 5

7 **3.3. Convection ($Q_{g \rightarrow s}^{cv}$, $Q_{g \rightarrow w}^{cv}$)**

9 Convective heat transfer in rotary kilns was studied by Tscheng as a function of kiln operating
 10 parameters including gas and solid throughput, rotational speed, solid loading, inclination,
 11 particle-size, and temperature.⁹ The resulting convective heat transfer coefficients are given
 12 below,
 13

$$14 \quad h_{g-s} = 0.46 \frac{k_g}{D_h} \text{Re}_{ax}^{0.535} \text{Re}_{an}^{0.104} \eta^{-0.341}$$

$$15 \quad h_{g-w} = 1.54 \frac{k_g}{D_h} \text{Re}_{ax}^{0.575} \text{Re}_{an}^{-0.292},$$

16 where η is the solid loading (fraction of solid fill) and D_h is the hydraulic diameter which is
 17 given below,
 18

$$19 \quad D_h = \frac{0.5D(2\pi - \theta + \sin \theta)}{\left(\pi - \frac{\theta}{2} + \sin \frac{\theta}{2}\right)}.$$

20 Two Reynolds numbers are used to characterize the gas flow within the kiln and are
 21 calculated using the following expressions,
 22

$$23 \quad \text{Re}_{ax} = \frac{\rho_g v_g D_h}{\mu_g} \qquad \text{Re}_{an} = \frac{\rho_g \omega D_h^2}{\mu_g},$$

24 where μ_g is the gas dynamic viscosity and $v_g = 4\dot{m}_g \rho_g^{-1} (D^2(\pi - \theta) + L_c(D - 2h_b))^{-1}$ is the gas
 25 velocity based on subtracting the area of the bulk bed from the area of the kiln tube. The gas
 26 density is calculated from the ideal gas equation. The overall heat flux is then given by
 27 $Q_{g \rightarrow s}^{cv} = h_{g-s/w} P_{g-s/w} (T_g - T_{s/w})$, where P_{g-s} is the perimeter of the exposed bed and P_{g-w} is the
 28 perimeter of the exposed wall as defined earlier.
 29

30 **3.4. Heat loss from the kiln ($Q_{w \rightarrow ext}$, $Q_{w \rightarrow sh}$)**

31 Rotary kilns are relatively inefficient unit operations with modern industrial kiln thermal
 32 efficiencies reported to be as low as 40%.²⁸ Heat losses from the kiln therefore play an
 33 important role in the overall energy balance in the kiln. It is a major industrial concern and
 34 energy efficiency is one of the primary focuses of current research in cement manufacture.
 35 The heat loss from the kiln internal wall to the surroundings is derived from the total
 36 resistance, R_{Total} ,
 37

$$38 \quad R_{Total} = \sum_j R_{wall,j}^{cd} + \left((R_{sh-ext}^{cv})^{-1} + (R_{sh-ext}^{rd})^{-1} \right)^{-1},$$

39 where resistance arises from conduction through the layers of the kiln wall. These resistances
 40 are in series with the external resistances of convection (R_{sh-amb}^{cv}) and radiation (R_{sh-amb}^{rd}) from
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the outer shell of the kiln to the surroundings. These resistances are calculated using standard expressions as shown in the equations below,

$$R_{wall,j}^{cd} = \frac{\ln(D_{outer,j} / D_{inner,j})}{2\pi k_j}$$

$$R_{sh-ext}^{rd} = \left(P_{sh} \sigma \varepsilon_{sh} (T_{sh}^2 + T_{ext}^2) (T_{sh} + T_{ext}) \right)^{-1}$$

$$R_{sh-ext}^{cv} = \frac{D_o}{P_{sh} \text{Nu}_{ext} k_{ext}},$$

where D_o is the outer diameter of kiln, $D_{inner/outer,j}$ are the inner/outer diameters of the wall layer j , the subscript ext is used to indicate the environment external to the kiln, $P_{sh} = \pi D$ is the perimeter of the outer shell, and Nu_{ext} is the Nusselt number for natural convection. Standard semi-empirical expressions for natural convection on the outside of horizontal cylinders were taken from Ref. 29; $\text{Nu}_{ext} = n(\text{Gr Pr})^m$, where Gr is the Grashof number, Pr is the Prandtl number, and the coefficients n and m vary with the Rayleigh number (Gr Pr) as: 0.85 and 0.188 when $10^2 \leq \text{Ra} \leq 10^4$, 0.48 and 0.25 when $10^4 \leq \text{Ra} \leq 10^7$, and 0.125 and 1/3 when $10^7 \leq \text{Ra} \leq 10^{12}$ respectively. Thermal conductivities of the kiln layers in the Barr kiln are taken from the original source, while those of the Tscheng kiln are assumed to be standard values reported in literature: $0.294 \text{ Wm}^{-1}\text{K}^{-1}$ for the refractory, $45.2 \text{ Wm}^{-1}\text{K}^{-1}$ for the steel shell, $0.08 \text{ Wm}^{-1}\text{K}^{-1}$ for the ceramic paper insulation, and $0.04 \text{ Wm}^{-1}\text{K}^{-1}$ for the fibre glass insulation. The heat loss from the kiln to the surroundings is then solved using $Q_{w \rightarrow ext} = (T_w - T_{ext}) / R_{Total}$ and $Q_{w \rightarrow sh} = (T_w - T_{sh}) / \sum_j R_{wall,j}^{cd}$. These equations allow T_w and T_{sh} to be solved for implicitly in each transverse slice using equations (3) and (4).

4. Model Validation

The thermal model described above is validated against experiments which were carried out in two kilns whose physical properties are shown in Table 2. Due to unquantifiable disturbances near the ends of the kilns, only selected regions of the axial length of the kiln are used for validation and these are between 0.8–5.0 m for the Barr kiln⁸ and 1.25–1.78 m for the Tscheng kiln.⁹ The Tscheng kiln experimental data is extracted from Ref. 9 while the original Barr kiln experimental data is collected via graphical digitization from Ref. 8. The kiln atmosphere in the Tscheng kiln was composed of preheated air while that of the Barr kiln is calculated from the combustion of natural gas in air as described in Ref. 8; for simplicity, the natural gas is assumed to be 100% CH₄. **For the Barr kiln calculations; the air flowrate is the sum of the primary and secondary air reported in Ref. 8.**

Barr collected two sets of gas temperature measurements, the first set is 2.5 cm above the solid bed surface and the second set is 10 cm away from the kiln wall surface. The latter gas temperatures are used for validation as they appear to be the best available representation of the enthalpy-averaged gas temperature used in the simulation model. The operating conditions of the Tscheng (Supplementary Material 1) and Barr (Supplementary Material 2) kiln trials are provided here. The compiled experimental data for temperature versus kiln length of the Tscheng⁸ (Supplementary Material 3) and Barr⁸ (Supplementary Material 4) trials are also provided as supplementary data. In addition to the data files, the remaining information required to reproduce this work which is not provided in the supplementary material is that

1 the solid particle diameter of all the Tscheng trials was 0.73 mm,⁹ and in the Barr trials, solid
2 loading was always at 12%, and the kiln RPM at 1.5.⁸ In our calculations, the only remaining
3 free parameters are the initial conditions for the solid and gas temperatures. In this case, the
4 temperatures of the solid and gas at the solid inlet end of the kiln then are calculated via least-
5 squares regression of the model results to the kiln data. This is performed as there is
6 insufficient data to determine these values directly from the experiments due to the
7 disturbances at the kiln entry and exit.
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10 The model is compared against 53 sets of kiln trial data and a summary of the simulation
11 predictions is given in Table 3. A representative example of one Barr trial is given in Fig. 2
12 and a representative example of one Tscheng trial is given in Fig. 3. For the simulation of the
13 Tscheng trial shown in Fig. 3, as the physical properties between 1.02 – 1.22m are not known.
14 Due to the unknown properties of the equipment installed in this region, the initial conditions
15 on both sides of this zone are calculated separately. Table 3 and Figs. 2 and 3 demonstrate
16 that the model gives an excellent agreement between the experimental and simulated
17 temperatures with an average error of ± 15.5 K in the Barr kiln and ± 6.5 K in the Tscheng kiln.
18 The average absolute error in the Tscheng kiln is significantly lower than that of the Barr kiln;
19 however, the relative errors are comparable due to the lower operating temperatures of the
20 Tscheng experiments. Overall it appears that this model is sufficiently accurate to capture the
21 performance of these two trial kilns. Due to the relatively large difference in operating
22 conditions between the two kiln trial data sets, the strong agreement indicates that this model
23 is quite general and may be capable of predictively capturing the performance of a wide range
24 of kiln geometries and operating conditions.
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29 Figure 4 displays the simulated heat fluxes of the various heat transfer paths for the same
30 selected Barr trial as presented in Fig. 2. It is apparent that the radiative heat flux between the
31 solid bed and the kiln wall is negligible compared to other heat fluxes. A temperature cross-
32 over between the solid and wall implies that the wall heats the solid feed up until around 2 m
33 into the kiln. Figure 5 presents a comparison between the total calculated radiative and
34 convective heat transfer from the gas phase in Barr trial T4. As is expected, convection is
35 dominant at lower temperatures ($< 950^{\circ}\text{C}$ or 2 m into the kiln in this case) and radiation is the
36 dominant at higher temperatures.
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39 The model can also be used to validate the assumptions made by Tscheng⁹ in deriving the
40 convective heat transfer coefficients. The radiative contribution calculated from this model is
41 less than 1.5% of the convective contribution in the Tscheng experiments. This approaches
42 the experimental error and validates their assumption to neglect radiation while developing
43 convective heat transfer models for rotary kilns under their conditions.
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45

46 5. Conclusions

47 A one dimensional rotary kiln thermal model is presented which considers a full mass and
48 energy balance for all the species of gas and solid in the kiln. The model considers solid and
49 gas temperature-dependent thermodynamic, transport, and radiative properties. The model is
50 demonstrated to predict axial temperature in the rotary kiln to within experimental error,
51 hence validating the key approximations used, such as the homogenization of the temperature.
52 This also appears to confirm that neglecting axial effects is not unreasonable, although these
53 effects may have been partially included during the fitting of the empirical expressions used
54 for heat transfer. By including a thermodynamic description of the gas phase, the model is
55 complete and may be used to predict the performance of new kiln designs (with inert beds). In
56 this case, estimates for the two initial conditions (which are the only free parameters in the
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1 model) may be obtained from an adiabatic flame temperature calculation for the gas inlet and
2 ambient temperature used for the solid inlet. The current model does not include the effects of
3 a burner within the kiln; thus further work will be required to determine the additional
4 radiation effects and progression of combustion along the length of the kiln.
5

6 **In order to expedite the development of novel clinker compositions and kiln processes such as**
7 **that in Ref. 30**, work is currently underway to couple the thermal model presented here with a
8 thermodynamic database for combustion and cements which we recently compiled.³¹ This
9 development will allow the enthalpy of solid and gas reactions to be included in the heat
10 balance and extend the model to reactive systems. There is limited data for the solid phase
11 reaction kinetics; however, our initial results indicate that a simple equilibrium
12 thermodynamic model is capable of predicting the final output of industrial and pilot cement
13 kilns to a reasonable degree of accuracy. Finally, variations in bed height and solid mass flux
14 arising from changes in the solid phase will require a predictive model for the motion of the
15 solid bed; however, there are a number of models available in the literature. The resulting
16 coupled heat transfer, thermodynamics, and solid dynamics model will allow the broad
17 optimization of the kiln design, fuel, and raw feed composition for a wide range of industries.
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22 **6. Acknowledgements**

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24 for Research and Development (GORD), Qatar through research grant number
25 ENG016RGG11757.
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33 **Figure and Table Captions**

34
35 Figure 1. An illustration of the heat transfer fluxes per length, Q , considered in the kiln model.
36 Arrows indicate the positive direction of heat flux. The superscripts indicate convective (cv),
37 radiative (rd), or conductive (cd) terms whereas the subscripts indicate the phases in question:
38 e.g., solid bed (s), gas (g), kiln internal wall (w), and external environment (ext).
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41 Figure 2. The temperature profile along the length of the kiln as obtained from simulation
42 (lines) and Barr trial T4 experiments (symbols). Black solid vertical lines represent the region
43 used for validation of the model.
44

45 Figure 3. The temperature profile along the length of the kiln as obtained from simulation
46 (lines) and Tscheng trial A11 experiments (symbols). Black solid vertical lines represent the
47 region used for validation of the model. The region between 1.02m and 1.22m is uninsulated
48 and as the physical properties of the kiln in this region are not known, due to the unknown
49 properties of the equipment installed in that section of the kiln, the initial conditions to
50 perform the integration on either side of this region are calculated separately.
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54 Figure 4. Comparison of the heat fluxes of the various heat transfer paths of Barr trial T4, as
55 predicted by the computational model.
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57 Figure 5. Comparison between the total calculated radiative and convective heat transfer from
58 the gas to both the solid and wall within the kiln enclosure of Barr trial T4.
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2 Table 1. Gaseous composition of dry air used in simulations in this work.
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4 Table 2. Properties of the Tscheng and Barr experimental kilns.
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6 Table 3. A summary of model error for all available experimental data.
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9 **Tables**

10
11 **Table 1. Gaseous composition of dry air used.**
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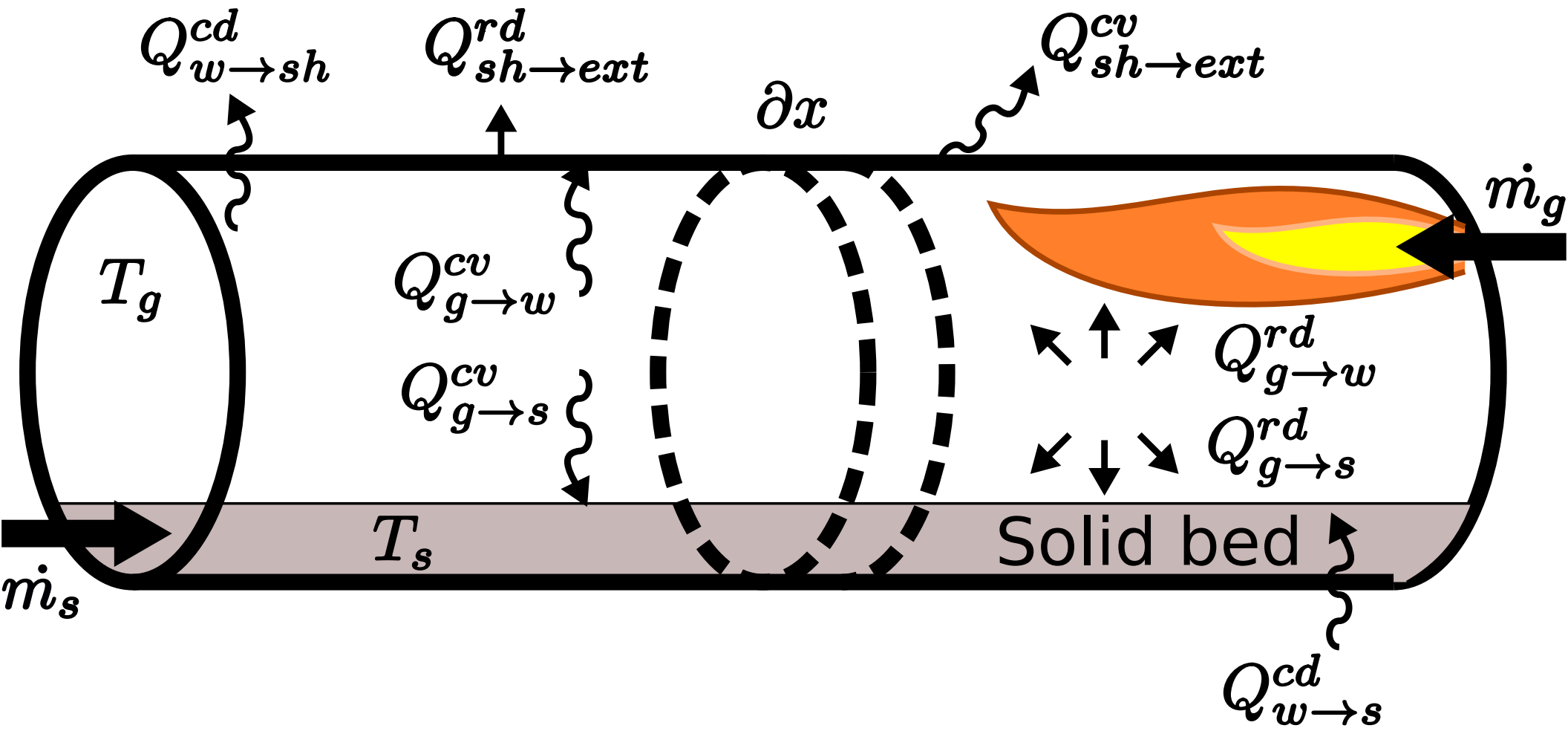
| Component | N ₂ | O ₂ | Ar | CO ₂ | Ne | He | CH ₄ | Kr |
|-----------|----------------|----------------|-------|-----------------------|-------------------------|-----------------------|-----------------------|-----------------------|
| mol-% | 78.084 | 20.946 | 0.934 | 3.97x10 ⁻² | 1.818 x10 ⁻³ | 5.24x10 ⁻⁴ | 1.79x10 ⁻⁴ | 1.14x10 ⁻⁴ |

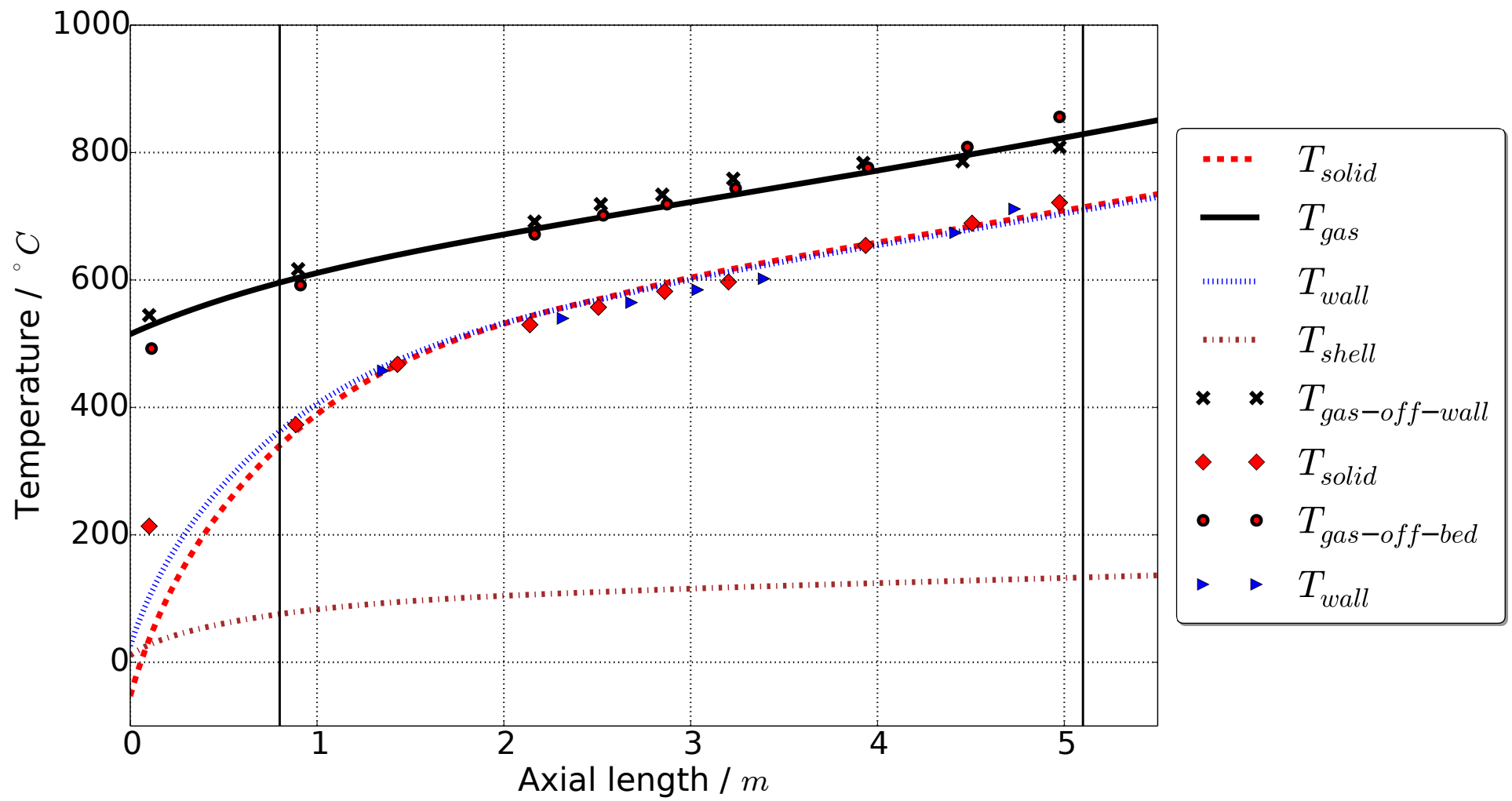
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17 **Table 2. Properties of the Tscheng and Barr experimental kilns.**
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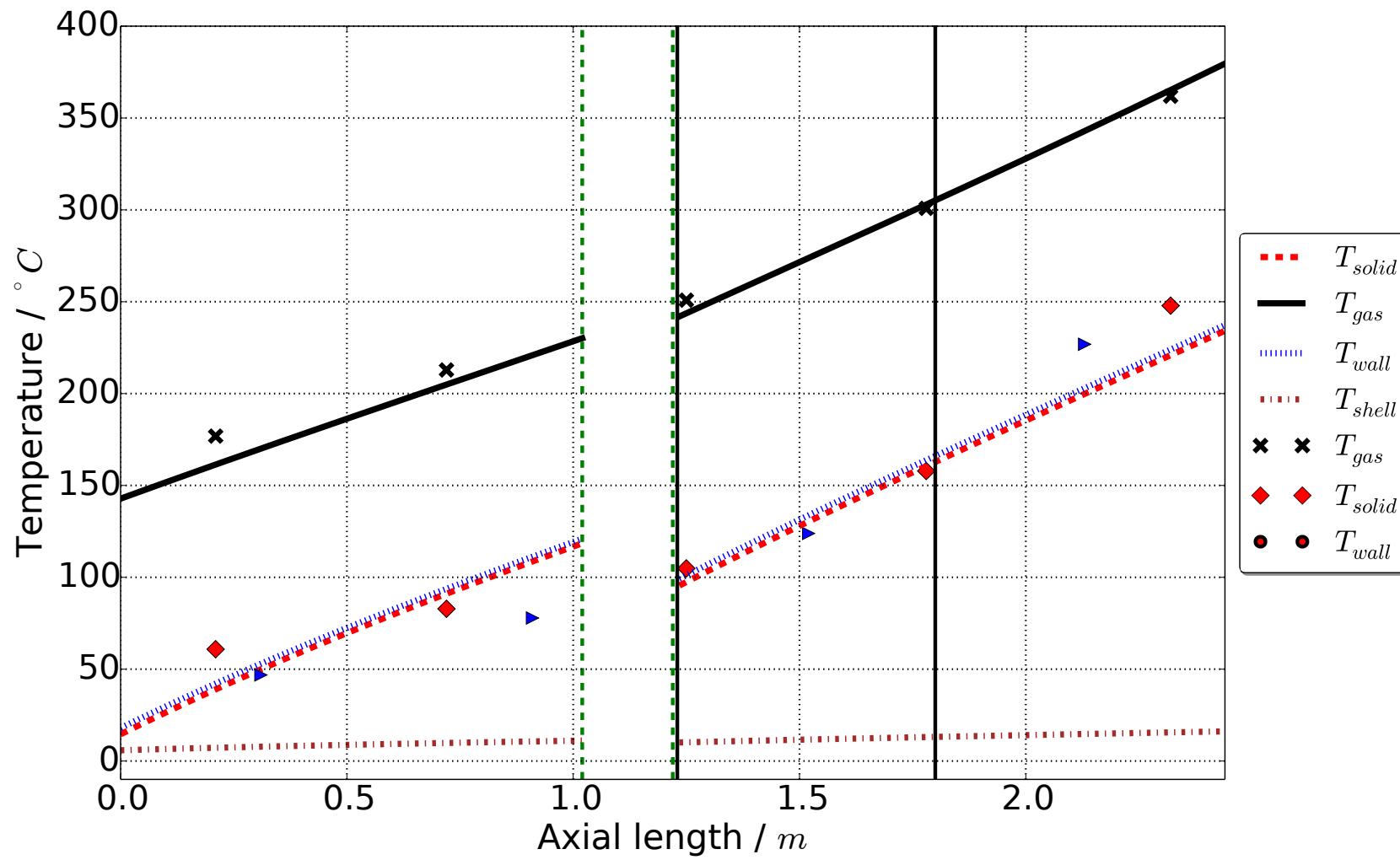
| Property | Barr kiln [8] | Tscheng kiln [9] |
|------------------------------|---------------|------------------|
| Length (m) | 5.5 | 2.44 |
| Inner radius (mm) | 205.5 | 94.25 |
| Refractory thickness (mm) | 93.0 | 1.0 |
| Steel thickness (mm) | 6.0 | 6.35 |
| Ceramic paper thickness (mm) | ... | 6.4 |
| Fibre glass thickness (mm) | ... | 76 |
| Outer radius (mm) | 304.5 | 184.0 |
| Experiment IDs | T1—T9 | A11—A54 |

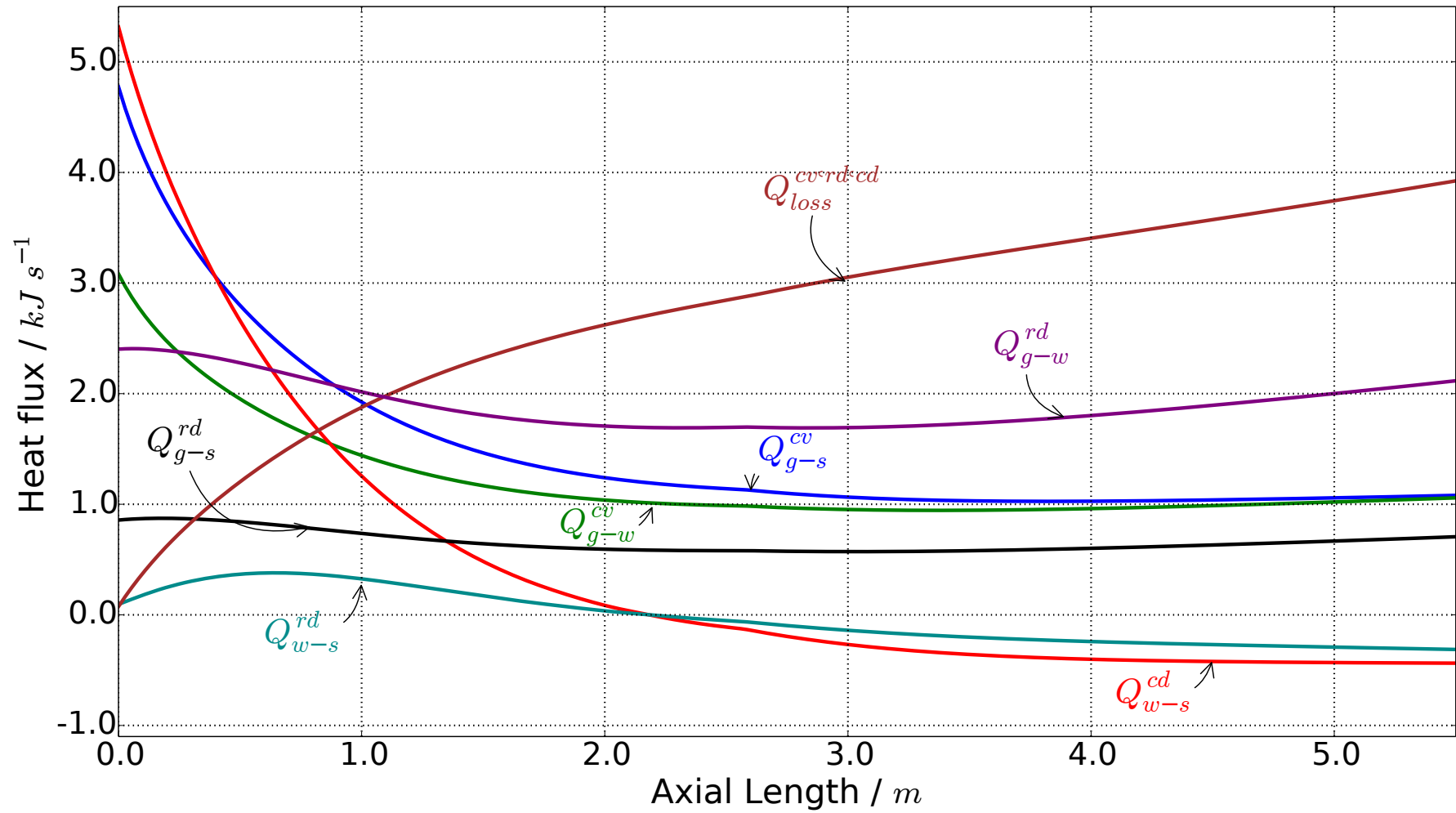
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30 **Table 3. Statistics on the deviation from the experimental results of the model temperature**
31 **predictions for all trial data sets.**
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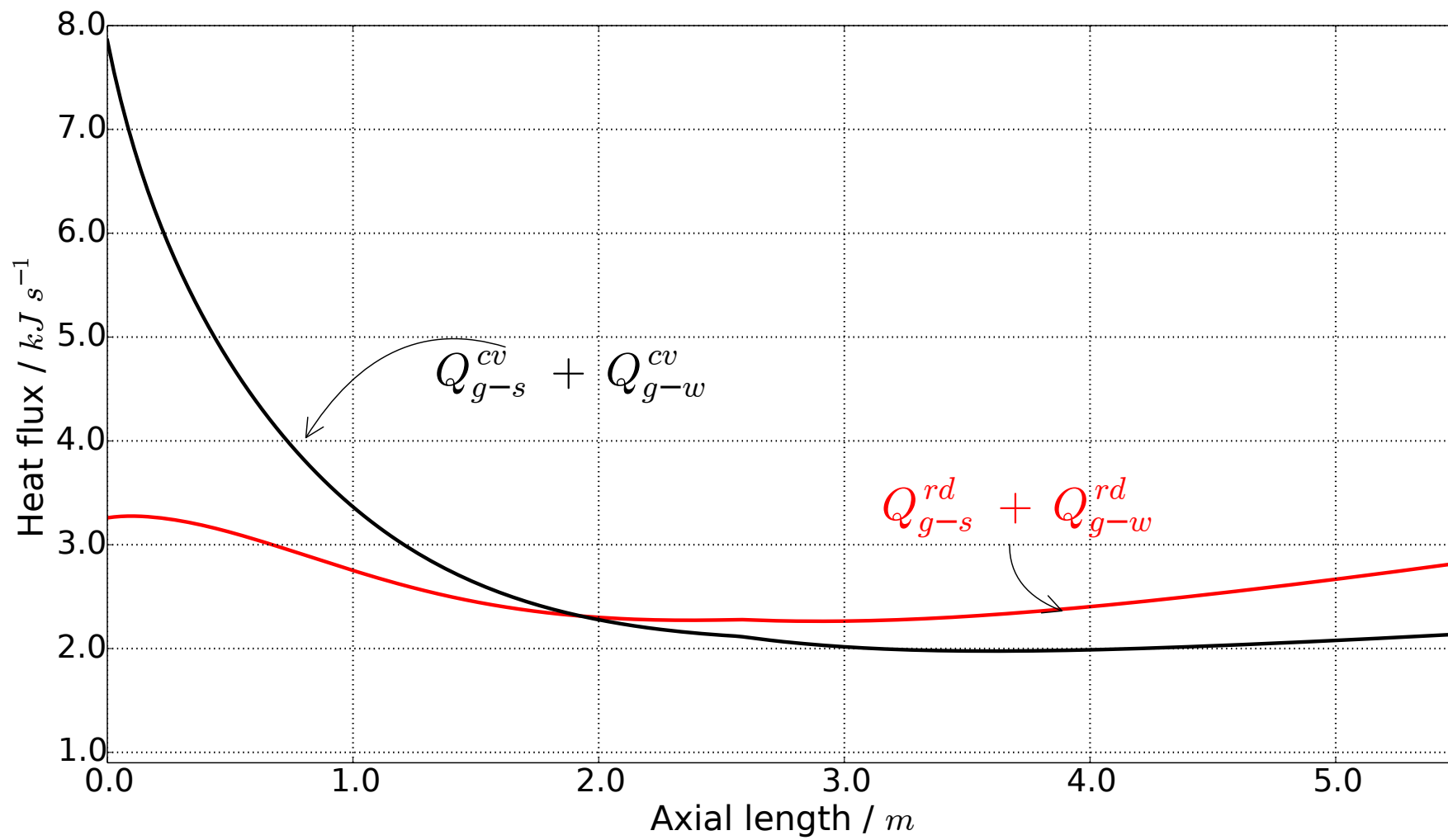
| Kiln | Trials | Total measurements | | | Maximum error (K) | | | Mean error (K) | | |
|---------|--------|--------------------|-------|------|-------------------|-------|-------|----------------|-------|-------|
| | | Gas | Solid | Wall | Gas | Solid | Wall | Gas | Solid | Wall |
| Barr | 9 | 68 | 73 | 69 | +54.1 | +37.8 | +39.6 | +15.5 | +13.9 | +13.5 |
| Tscheng | 44 | 88 | 88 | 44 | +8.6 | +17.0 | +23.1 | +2.2 | +3.8 | +6.5 |











This document provides a description of the supplementary data files provided with the title paper (“1D thermal model of rotary kilns used in cement production”).

Supplementary Material 1: Operating conditions of the Tscheng pilot kiln experiments.

Provided in this file are the operating conditions for the 44 Tscheng experiments (A11 – A54) including the air flow-rates, kiln RPM, kiln incline, solid loading, and solid flow-rates. The column labels are in the first row and the units are provided in brackets. The solid particle diameters in all the Tscheng experiments are 0.73 mm.

Supplementary Material 2: Operating conditions of the Barr pilot kiln experiments.

Provided in this file are the operating conditions for the 9 Barr experiments (T1 – T9) including the natural gas flow-rates, primary and secondary air flow-rates, solid flow-rates, and solid particle diameter. The columns labels are in the first row and the units provided in brackets. In all 9 experiments, the solid loading is set at 12% and the kiln RPM set at 1.5.

Supplementary Material 3: Experimental temperature vs kiln length data of the Tscheng pilot kiln experiments.

Provided in this file are the experimental thermocouple temperature measurements for the 44 Tscheng experiments (A11 – A54) taken from the original source. The experiments IDs are given in the first column. The remaining columns contain the thermocouple temperature measurements in **Kelvin**; these are labelled T-A-B where A denotes the material in question (g for gas, s for solid bed, and w for wall) and B denotes the thermocouple number. The locations of the gas and bed thermocouples are: (1) 0.21, (2) 0.72, (3) 1.25, (4) 1.78, and (5) 2.32 meters along the kiln. The locations of the wall thermocouples are: (1) 0.31, (2) 0.91, (3) 1.52, and (4) 2.13 meters along the kiln. For the thermocouple locations, 0 meters corresponds to the solid feed end of the kiln.

Supplementary Material 4: Experimental temperature vs kiln length data of the Barr pilot kiln experiments.

Provided in this file are the digitized experimental thermocouple temperature measurements (in **Kelvin**) and locations on the kiln length in meters of the thermocouples for the 9 Barr experiments (T1 – T9). Two sets of gas temperature measurements were collected, one 10 cm off the kiln wall, labelled Tg_off_wall, and the second, 2.5 cm off the kiln solid bed labelled Tg_off_bed, both from the same thermocouple measured as the kiln rotates. The solid bed and wall temperature measurements are labelled Ts and Tw respectively. The thermocouples are fixed therefore their locations are assumed to be the average of the digitized measurements. The numbers following column headers denote the thermocouple numbers. The gas thermocouple locations are: (1) 0.11, (2) 0.89, (3) 2.15, (4) 2.51, (5) 2.85, (6) 3.20, (7) 3.91, (8) 4.44, and (9) 4.95. The solid bed thermocouple locations are: (1) 0.11, (2) 0.87, (3) 1.44, (4) 2.14, (5) 2.50, (6)

2.85, (7) 3.20, (8) 3.91, (9) 4.48, (10) 4.95, (11) 5.25, and (12) 5.50 meters. The wall thermocouple locations are: (1) 1.33, (2) 2.32, (3) 2.67, (4) 3.03, (5) 3.38, (6) 3.83, (7) 4.40, and (8) 4.78. For the thermocouple locations, 0 meters represents the solid feed end of the kiln. Data shown as "NA" in this file implies that data are not available for that thermocouple.

Supplementary Material 1

| Experiment ID | Air flow (kg/hr) | RPM | Incline (degree) | Solid loading (%) | Solid flow (kg/hr) |
|---------------|------------------|------|------------------|-------------------|--------------------|
| A11 | 24.6 | 3 | 1.2 | 17 | 25 |
| A12 | 24.6 | 3 | 1.2 | 17 | 25 |
| A13 | 24.6 | 3 | 1.2 | 17 | 25 |
| A14 | 24.6 | 3 | 1.2 | 17 | 25 |
| A15 | 24.6 | 1.5 | 1.2 | 17 | 14.2 |
| A16 | 24.6 | 1.5 | 1.2 | 17 | 14.2 |
| A17 | 24.6 | 1.5 | 1.2 | 17 | 14.2 |
| A18 | 18.6 | 3 | 1.2 | 15 | 21 |
| A19 | 18.6 | 1.6 | 2.2 | 17 | 29.1 |
| A20 | 18.6 | 1.6 | 1.2 | 17 | 15 |
| A21 | 34 | 1.5 | 1.2 | 17 | 15 |
| A22 | 34 | 3 | 1.2 | 17 | 34 |
| A23 | 34 | 1.5 | 1.2 | 17 | 15 |
| A24 | 34 | 6 | 1.2 | 17 | 50.5 |
| A25 | 34 | 1.5 | 3.4 | 17 | 39 |
| A26 | 34 | 3.2 | 2.2 | 11 | 34.6 |
| A27 | 50.5 | 3.2 | 2.2 | 11 | 34 |
| A28 | 50.5 | 3.1 | 3 | 11 | 52.7 |
| A29 | 50 | 3.1 | 1.2 | 11 | 19.4 |
| A30 | 50 | 1.6 | 2.2 | 11 | 18.2 |
| A31 | 50.5 | 6 | 2.2 | 11 | 66.3 |
| A32 | 81 | 3 | 2 | 11 | 36 |
| A33 | 65.5 | 3 | 2 | 11 | 36 |
| A34 | 73 | 3 | 2 | 11 | 36 |
| A35 | 81 | 3 | 2 | 11 | 36 |
| A36 | 34 | 3 | 2 | 11 | 36 |
| A37 | 34 | 3 | 2 | 11 | 36 |
| A38 | 34 | 3 | 2 | 11 | 36 |
| A39 | 34 | 3 | 2 | 11 | 36 |
| A40 | 18.6 | 3 | 2 | 11 | 36 |
| A41 | 18.6 | 3 | 2 | 11 | 36 |
| A42 | 18.6 | 3 | 2 | 11 | 36 |
| A43 | 18.6 | 3 | 2 | 11 | 36 |
| A44 | 50 | 3 | 2 | 11 | 36 |
| A45 | 65.5 | 0.9 | 2 | 6.5 | 12 |
| A46 | 34 | 1 | 2 | 6.5 | 13.3 |
| A47 | 34 | 3 | 2 | 6.5 | 35.8 |
| A48 | 65.5 | 3 | 2 | 6.5 | 35.8 |
| A49 | 65 | 0.9 | 2 | 6.5 | 11.7 |
| A50 | 95.5 | 3 | 2 | 6.5 | 35.8 |
| A51 | 95.5 | 1 | 2 | 6.5 | 15.8 |
| A52 | 34 | 1 | 2 | 6.5 | 11.3 |
| A53 | 95.5 | 1 | 2 | 6.5 | 16.1 |
| A54 | 81 | 0.95 | 2 | 6.5 | 12 |

| Experiment ID | Fuel flow rate (L/s) | Primary air flow rate (L/s) | Secondary air flow rate (L/s) |
|---------------|----------------------|-----------------------------|-------------------------------|
| T1 | 0.83 | 9.4 | 18.8 |
| T2 | 1.02 | 16.5 | 40.6 |
| T3 | 1.42 | 17.4 | 40.6 |
| T4 | 1.97 | 17.4 | 43 |
| T5 | 0.68 | 9.4 | 19.8 |
| T6 | 0.9 | 14.2 | 29.3 |
| T7 | 1.04 | 18.4 | 43 |
| T8 | 2 | 18.8 | 40.1 |
| T9 | 2.53 | 18.8 | 43 |

| Solid mass flow rate (kg/hr) | Sand Particle Diameter (mm) |
|------------------------------|-----------------------------|
| 62 | 2.5 |
| 62 | 2.5 |
| 62 | 2.5 |
| 62 | 2.5 |
| 58 | 0.58 |
| 62 | 0.58 |
| 63 | 0.58 |
| 64 | 0.58 |
| 65 | 0.58 |

| Experiment ID | T-g-1 | T-g-2 | T-g-3 | T-g-4 | T-g-5 | T-s-1 | T-s-2 | T-s-3 |
|---------------|-------|-------|-------|-------|-------|-------|-------|-------|
| A11 | 450 | 486 | 524 | 574 | 635 | 334 | 356 | 378 |
| A12 | 425 | 460 | 489 | 535 | 592 | 323 | 339 | 356 |
| A13 | 402 | 423 | 457 | 493 | 538 | 321 | 337 | 354 |
| A14 | 372 | 392 | 411 | 436 | 457 | 314 | 327 | 341 |
| A15 | 330.6 | 340 | 348.3 | 358.8 | 372 | 306.7 | 308.9 | 312.8 |
| A16 | 414 | 438 | 462 | 494 | 535 | 341 | 356 | 374 |
| A17 | 470 | 505 | 543 | 594 | 652 | 364 | 383 | 410 |
| A18 | 351.5 | 378.9 | 412.2 | 445 | 488 | 313.9 | 325.6 | 338.9 |
| A19 | 350 | 375.1 | 405 | 448 | 497 | 312.2 | 322.2 | 332.2 |
| A20 | 365 | 392.8 | 427.2 | 464 | 507 | 330.5 | 340 | 352.8 |
| A21 | 380 | 398 | 418 | 436 | 455 | 335 | 346.1 | 360.3 |
| A22 | 368 | 388 | 407 | 428 | 455.8 | 320.6 | 331.1 | 341.7 |
| A23 | 383 | 400.8 | 418 | 437 | 456 | 337.8 | 348.9 | 365 |
| A24 | 357 | 374 | 390.6 | 407 | 430 | 308.3 | 315 | 322.2 |
| A25 | 361 | 377.2 | 391.5 | 410 | 430 | 305.6 | 313.6 | 322.2 |
| A26 | 370 | 385 | 398.9 | 414 | 437 | 313.8 | 323.3 | 333.3 |
| A27 | 369 | 380 | 388.9 | 401 | 413 | 316.7 | 326.1 | 334.4 |
| A28 | 361 | 371 | 381.1 | 395 | 410 | 312.8 | 318.9 | 327.9 |
| A29 | 376 | 386 | 396 | 406 | 417 | 328.9 | 339.4 | 353.9 |
| A30 | 378 | 388 | 399 | 410 | 420.5 | 329.4 | 341.1 | 357.2 |
| A31 | 353 | 365 | 375.6 | 387.5 | 404.5 | 308.3 | 313.9 | 321.5 |
| A32 | 407 | 417.8 | 425.1 | 437.5 | 450 | 333.3 | 350.6 | 366.7 |
| A33 | 393 | 407 | 418.3 | 431 | 445 | 326.1 | 341.7 | 358.3 |
| A34 | 396.2 | 412.2 | 423.3 | 436 | 448.9 | 331.7 | 347.2 | 362.7 |
| A35 | 396.8 | 411.1 | 422.2 | 433 | 444.4 | 326.7 | 348.9 | 366.7 |
| A36 | 366.7 | 380.6 | 395.6 | 415 | 441 | 311.1 | 322.2 | 334.4 |
| A37 | 420 | 445.4 | 476.7 | 513 | 560 | 322.8 | 343.3 | 369.4 |
| A38 | 395 | 417 | 440.6 | 471 | 505 | 318.9 | 334.4 | 355 |
| A39 | 420.6 | 446.5 | 475 | 512 | 559 | 323.9 | 343.3 | 369.4 |
| A40 | 385.6 | 417 | 461.1 | 510 | 560 | 318.3 | 331.7 | 352 |
| A41 | 358.3 | 376 | 410.6 | 447 | 505 | 308.9 | 317.8 | 332.2 |
| A42 | 351.7 | 360 | 384.4 | 413.5 | 460 | 306.1 | 312.2 | 321.7 |
| A43 | 375.6 | 400 | 440 | 478 | 535 | 313.3 | 325 | 345 |
| A44 | 398 | 416.7 | 433.9 | 452.5 | 475 | 323.9 | 338.9 | 360 |
| A45 | 412 | 425 | 434.4 | 441.1 | 448 | 361.1 | 373.9 | 391.7 |
| A46 | 382.1 | 397.2 | 413.3 | 427.3 | 444 | 333.3 | 345.6 | 361.7 |
| A47 | 367.8 | 382.2 | 398.9 | 416 | 441 | 312.8 | 322.8 | 336.1 |
| A48 | 400 | 408 | 420.6 | 432 | 447 | 327.8 | 341.1 | 360 |
| A49 | 419 | 427 | 435 | 442.3 | 448 | 368.9 | 378.3 | 397.8 |
| A50 | 404 | 410.2 | 417.2 | 424 | 431 | 375 | 377.8 | 391.7 |
| A51 | 406.6 | 412.2 | 417.6 | 422 | 427 | 370.6 | 377.2 | 390.6 |
| A52 | 384 | 398.1 | 416.7 | 428 | 443 | 335.5 | 348.9 | 368.3 |
| A53 | 403.3 | 409.5 | 414.4 | 413.5 | 422.8 | 374.4 | 375.6 | 388.9 |
| A54 | 419 | 427 | 434.4 | 442 | 450 | 373.3 | 381.7 | 397.2 |

| T-s-4 | T-s-5 | T-w-1 | T-w-2 | T-w-3 | T-w-4 |
|-------|-------|-------|-------|-------|-------|
| 431 | 521 | 320 | 351 | 397 | 500 |
| 397 | 473 | 314 | 338 | 372 | 445 |
| 392 | 447 | 313 | 333 | 368 | 429 |
| 368 | 405 | 308 | 326 | 352 | 395 |
| 326.7 | 348.3 | 301 | 306 | 316 | 333 |
| 417 | 473 | 324 | 347 | 387.5 | 447 |
| 473 | 554 | 341 | 370 | 425 | 520 |
| 363.9 | 402.8 | 308 | 323 | 349 | 385 |
| 355.5 | 391.7 | 304 | 317 | 341 | 377 |
| 383.3 | 424.4 | 315.5 | 331 | 363 | 407 |
| 384.4 | 411.1 | 319.4 | 336 | 365.8 | 401 |
| 363.3 | 390 | 311 | 326.6 | 349.6 | 378 |
| 385.6 | 412.8 | 321 | 338 | 365 | 400 |
| 336.7 | 360 | 302 | 311.6 | 330 | 355 |
| 338.9 | 362.1 | 300 | 313.4 | 331 | 360 |
| 350 | 376.1 | 306 | 321.6 | 340 | 364.8 |
| 351.7 | 373.9 | 306.8 | 323 | 341.6 | 366 |
| 341.7 | 358.9 | 304 | 315.5 | 333 | 353 |
| 370.6 | 391.1 | 320 | 338.8 | 350 | 380 |
| 373.9 | 394.4 | 320 | 339 | 360 | 387 |
| 331.7 | 350 | 302.3 | 313.6 | 326 | 345.6 |
| 391.1 | 417.3 | 321.1 | 347.4 | 375.5 | 407 |
| 380.6 | 407.2 | 313 | 338.4 | 367.4 | 395 |
| 385.8 | 412.2 | 315.8 | 344 | 370 | 402 |
| 388.9 | 414.2 | 315.8 | 345 | 375.5 | 404 |
| 352.2 | 378.1 | 304.5 | 321.7 | 339 | 368 |
| 399.7 | 443 | 312.6 | 341.1 | 380.4 | 425.5 |
| 380 | 415.3 | 312.4 | 335.4 | 361 | 401 |
| 400 | 445.4 | 312 | 344 | 380 | 425.5 |
| 377.8 | 428 | 311 | 333 | 364 | 413 |
| 348.3 | 387.2 | 300.4 | 317.6 | 335 | 372.8 |
| 336.1 | 366.7 | 299 | 312.6 | 327 | 356.8 |
| 365 | 412.2 | 306 | 325 | 352 | 397.5 |
| 384.2 | 419.4 | 312 | 338 | 371 | 407 |
| 416.7 | 434.4 | 339.8 | 365 | 400 | 428 |
| 386.7 | 411.1 | 314 | 338.4 | 369.4 | 400 |
| 352.8 | 380 | 306 | 323.6 | 344.2 | 370.5 |
| 382 | 409.4 | 318 | 340.2 | 369 | 395 |
| 419.4 | 438.3 | 349.6 | 374.4 | 402.5 | 430 |
| 407.2 | 418.9 | 355 | 374 | 395 | 415 |
| 402.7 | 418.3 | 351.4 | 372.2 | 393.3 | 413 |
| 391.7 | 418.9 | 319 | 341.5 | 373 | 405 |
| 404.4 | 415.6 | 347 | 369 | 395 | 410 |
| 418.9 | 435 | 351 | 364.4 | 400 | 430 |

| Experiment ID | T1 | T2 | T3 | T4 | T5 |
|---------------|---------|---------|---------|---------|---------|
| Tg_off_wall 1 | 592.996 | 612.5 | 701.567 | 817.842 | 585.573 |
| Tg_off_wall 2 | 661.964 | 660.714 | 765.204 | 890.041 | 640.609 |
| Tg_off_wall 3 | 749.991 | 707.143 | 824.451 | 964.73 | 714.213 |
| Tg_off_wall 4 | 769.207 | 726.786 | 837.618 | 992.116 | 735.246 |
| Tg_off_wall 5 | 803.748 | 726.786 | 848.589 | 1007.05 | 749.782 |
| Tg_off_wall 6 | 818.617 | 744.643 | 855.172 | 1031.95 | 770.839 |
| Tg_off_wall 7 | 872.36 | 757.143 | 890.282 | 1056.85 | 808.566 |
| Tg_off_wall 8 | NA | 771.429 | NA | 1059.34 | 818.314 |
| Tg_off_wall 9 | 943.188 | 787.5 | 907.837 | 1081.74 | 836.834 |
| Tg_off_bed 1 | 564.547 | 589.286 | 673.041 | 765.56 | 557.191 |
| Tg_off_bed 2 | 576.646 | 619.643 | 730.094 | 865.145 | 570.781 |
| Tg_off_bed 3 | 629.676 | 687.5 | 795.925 | 944.813 | 613.845 |
| Tg_off_bed 4 | 662.016 | 707.143 | 815.674 | 974.689 | 643.628 |
| Tg_off_bed 5 | 692.196 | 716.071 | 833.229 | 992.116 | 675.591 |
| Tg_off_bed 6 | 744.25 | NA | 848.589 | 1017.01 | 727.188 |
| Tg_off_bed 7 | 848.3 | 757.143 | NA | 1049.38 | 778.003 |
| Tg_off_bed 8 | 891.362 | 764.286 | 894.671 | 1081.74 | 800.863 |
| Tg_off_bed 9 | 927.877 | 783.929 | NA | 1129.05 | 808.476 |
| Ts1 | 400.487 | 371.429 | 464.577 | 486.722 | 400.107 |
| Ts2 | 454.172 | NA | 574.295 | 646.058 | 453.009 |
| Ts3 | 514.676 | 528.571 | 642.32 | 740.664 | NA |
| Ts4 | 555.323 | NA | 688.401 | 802.905 | 509.162 |
| Ts5 | NA | 591.071 | 712.539 | 830.29 | 538.921 |
| Ts6 | 606.878 | NA | 725.705 | 855.187 | 553.41 |
| Ts7 | NA | NA | 749.843 | 870.124 | 587.555 |
| Ts8 | NA | 650 | 778.37 | 927.386 | 640.552 |
| Ts9 | 751.305 | 673.214 | 806.897 | 962.241 | 685.131 |
| Ts10 | 809.75 | 700 | 857.367 | 994.606 | 701.588 |
| Ts11 | NA | NA | 815.674 | NA | 735.828 |
| Ts12 | 854.971 | 730.357 | 852.978 | NA | 768.005 |
| Tw1 | 530.129 | 535.714 | 626.959 | 730.705 | 504.345 |
| Tw2 | 587.89 | 583.929 | 694.984 | 812.863 | 563.319 |
| Tw3 | 609.293 | 601.786 | 714.734 | 837.759 | 584.375 |
| Tw4 | 635.099 | 616.071 | 732.288 | 857.676 | 603.227 |
| Tw5 | 652.128 | 628.571 | 749.843 | 875.104 | 624.284 |
| Tw6 | 704.025 | 651.786 | 789.342 | NA | 662.579 |
| Tw7 | 764.543 | 687.5 | 822.257 | 947.303 | 694.069 |
| Tw8 | 812.15 | 712.5 | 850.784 | 984.647 | 732.483 |

| T6 | T7 | T8 | T9 |
|---------|---------|---------|---------|
| 673.041 | 651.066 | 834.648 | 874.748 |
| 690.596 | 659.607 | 876.944 | 966.177 |
| 747.649 | 703.487 | 959.68 | 1072.98 |
| 756.426 | 709.999 | 974.382 | 1090.49 |
| 776.176 | 716.512 | 1010.67 | 1116.66 |
| 780.564 | 725.246 | 1031.86 | 1136.34 |
| 813.48 | 742.71 | 1059.12 | 1173.51 |
| 802.508 | 742.469 | NA | NA |
| 802.508 | 755.581 | 1105.45 | 1219.5 |
| 585.266 | 582.173 | 741.92 | 805.349 |
| 642.32 | 628.497 | 838.121 | 924.972 |
| 727.9 | 690.144 | 935.95 | 1044.8 |
| 747.649 | 701.106 | 963.601 | 1070.97 |
| 760.815 | 705.43 | 989.108 | NA |
| NA | NA | NA | NA |
| 795.925 | 729.372 | 1046.18 | 1173.51 |
| 787.147 | NA | NA | 1178.08 |
| 787.147 | 744.47 | 1120.55 | 1252.04 |
| 365.831 | 428.843 | 450.82 | 503.907 |
| 484.326 | 504.06 | 618.199 | 701.579 |
| 541.379 | 530.475 | 712.463 | 797.252 |
| 585.266 | 550.161 | 780.714 | 882.137 |
| 605.016 | 572.224 | 810.51 | 921.324 |
| 618.182 | 587.62 | 823.068 | 951.841 |
| 640.125 | 605.248 | 857.199 | 978.025 |
| 668.652 | 629.374 | 903.877 | 1023.87 |
| 694.984 | 660.229 | 950.693 | 1076.17 |
| 727.9 | 662.244 | 995.478 | 1126.25 |
| NA | NA | NA | NA |
| NA | 684.235 | NA | NA |
| 565.517 | 534.963 | 710.422 | 803.711 |
| 620.376 | 581.195 | 791.3 | 901.731 |
| 637.931 | 598.813 | 818.951 | 938.754 |
| 653.292 | 609.765 | 837.977 | 962.765 |
| 662.069 | 618.5 | 865.629 | 995.45 |
| 694.984 | 644.968 | 912.582 | 1041.19 |
| 714.734 | NA | NA | 1071.79 |
| 738.871 | 684.538 | 987.026 | 1113.17 |