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# INTUMESCENT COATING MODELLING BASED ON SMALL SCALE EXPERIMENTAL TESTS 

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#### Abstract

An investigation of two different intumescent coatings used in steel fire protection has been performed to evaluate their efficiency. Among other quantities, the steel temperature and the intumescence thickness variation were measured. A mathematical model for the intumescent coating is developed. It considers the coating decomposition and models the protection by two layers, the reacted and the unreacted layer. A comparison between the experimental results and the ones obtained from the numerical model is presented.


Key-words: Fire Protection; Intumescent Coatings; Cone Calorimeter; Heat Transfer; Thermal Decomposition

## 1 Introduction

Thin film intumescent coatings are mostly used in the civil construction industry to increase the fire resistance requirements prescribed by the structural fire design codes. They are applied essentially to structural elements with inadequate fire behaviour, like the case of steel and aluminium structures. An intumescent coating when submitted to fire starts to bubble and swells to form a carbonaceous, porous, low-density char, reducing the heat transfer to underlying virgin material layer and therefore to the substrate.
The performance of two commercial water-based intumescent paint were assessed by a set of experimental tests, conducted in a cone calorimeter, which enables the mass loss rate calculation, the substrate temperature and the intumescence thickness variation with time, [1].
A numerical model is established with the conservation equation of energy for the substrate, virgin and char layers, the conservation of mass of gas and solids and the transport of gas through the char is modelled using the empirical Darcy's law approximation. The model allows knowing the moving boundary and the free boundary locations and therefore the overall intumescence thickness with time.
The paper presents the model development, the numeric treatment of the differential equations and, based on the intumescence thickness variation, the steel temperature comparison between the numeric and the experimental results.

## 2 Results from the cone calorimeter tests

To assess the performance of two commercial water-based intumescent paints a set of experimental tests was performed in a cone calorimeter as prescribed by the standard ISO5660, [2]. The steel plates were coated in one side with different dry film thicknesses ( $0.5,1.5,2.5[\mathrm{~mm}]$ ) and tested with two radiant heat fluxes: $35[\mathrm{~kW} / \mathrm{m} 2]$ and $75[\mathrm{~kW} / \mathrm{m} 2]$. During tests, among other quantities, steel temperature, intumescence mass loss and thickness variation were measured. Additional results and a detailed presentation of the experimental work can be found in [1].
The steel temperature profiles are registered in Fig. 1 to Fig. 4. The measured values from the thermocouples welded on the bottom of the plate are very close to the temperatures measured at the top. For the same heat flux, the time to reach the same temperature increases with the increase of the dry film thickness.


Fig. 1. Steel plate temperatures for $4[\mathrm{~mm}]$ specimens, with coating A, tested with heat a flux of $35\left[\mathrm{kwm}^{-2}\right]$.


Fig. 2. Steel plate temperatures for 4 [ mm ] specimens, with coating B, tested with heat a flux of $35\left[\mathrm{kwm}^{-2}\right]$.


Fig. 3. Steel plate temperatures for $4[\mathrm{~mm}]$ specimens, with coating A, tested with heat a flux of $75\left[\mathrm{kwm}^{-2}\right]$.


Fig. 4. Steel plate temperatures for $4[\mathrm{~mm}]$ specimens, with coating $B$, tested with heat a flux of $75\left[\mathrm{kwm}^{-2}\right]$.

The intumescent development (free boundary $\mathrm{L}(\mathrm{t})$ ) is represented in Fig. 5 to Fig. 8 for specimens with paint A and B, with different thicknesses and radiant heat fluxes. The presented values are mean values of four central measurements in the distance between the thermocouples. The figures show that for the lower heat flux the intumescence becomes stable but for the highest it continues to increase. The coating A have a higher expansion at the initial stage compared to the coating B. For longer periods of exposure coating B continues to expand.


Fig. 5. Coating A intumescence development for 4 $[\mathrm{mm}]$ specimens tested with a heat flux of $35\left[\mathrm{kwm}^{-2}\right]$.

ig. 6. Coating $B$ intumescence development for 4 $[\mathrm{mm}]$ specimens tested with a heat flux of $35\left[\mathrm{kwm}^{-2}\right]$.


## 3 Intumescent coating modelling

The model is based on the assumption that the coating decomposes in a single step reaction, at a specified temperature and in a very thin front, which separates the reacted zone from the virgin material, to volatiles and residual char. The decomposition gases are assumed to behave ideally and are not reactive. As an additional simplifying assumption the char and the gases are considered as being in thermal equilibrium. It is considered a generalized Stefan problem, in which the moving boundary and the free boundary locations are determined as part of the problem.


Different methodologies can be found in the literature to model the thermal decomposition of a polymer or polymer based materials. One way is to state that the pyrolysis occur only at the material surface, $x=s(t)$, being necessary to specify the pyrolysis temperature and its heat of vaporisation. In this case the temperature inside the virgin layer does not exceed $T_{p}$. It is possible to say that the thermal pyrolysis can take place also in the surface, but following one-step reaction approximated by the Arrhenius equation, depending on the instantaneous surface temperature. The methodology followed in this work was to consider that the decomposition occurs not only at the surface but also inside, for temperatures above the pyrolysis temperature. In this case the moving boundary regression rate must be determined considering the motion of all domain. This strategy implies that a mass diffusion term needs to appear in the energy equation due its motion, but it was disregarded due to the small thickness of the virgin layer.
Considering a first order reaction, the mass loss is given by

$$
\dot{m}(T(x, t))=\frac{\partial \rho_{v}}{\partial t}= \begin{cases}0 & \text { for } T<T_{p}  \tag{1}\\ -\rho_{v} A_{0} e^{-\frac{E_{0}}{R T(x, t)}} & \text { for } T \geq T_{p}\end{cases}
$$

where $\dot{m}$ are the local mass losses, $\mathrm{T}(\mathrm{x}, \mathrm{t})$ is the temperature at point x at instant $\mathrm{t}, \mathrm{A}_{0}$ is the pre exponential factor, $\mathrm{E}_{0}$ the activation energy and R the universal gas constant. The position of the moving boundary is obtained by summing all the mass losses and dividing by the specific mass.
The energy equation is for the steel and virgin layers are:

$$
\begin{align*}
& \left(\rho_{s} C p_{s}\right) \frac{\partial T}{\partial t}=\frac{\partial}{\partial x}\left(k_{s} \frac{\partial T}{\partial x}\right)  \tag{2}\\
& \left(\rho_{v} C p_{v}\right) \frac{\partial T}{\partial t}=\frac{\partial}{\partial x}\left(k_{v} \frac{\partial T}{\partial x}\right) \tag{3}
\end{align*}
$$

The conservation equation for the solid virgin material phase is given by

$$
\begin{equation*}
\frac{\partial \rho_{v} V_{v}}{\partial t}=-\dot{w}_{v}^{\prime " d} V_{v} \tag{4}
\end{equation*}
$$

Where $\dot{w}_{v}^{\prime " d}$ represents the destruction rate of virgin material per unit volume, originated by the thermal decomposition. The virgin material decomposition produces a fraction of gas, equal to the porosity, $\varphi$, and a solid char fraction equal to $(1-\varphi)$.

$$
\begin{equation*}
1 \mathrm{~kg} \text { virgin coationg } \rightarrow v_{g} \text { gases }+v_{c} \text { char } \tag{5}
\end{equation*}
$$

$v$ are the stoichiometric coefficients and are related to the gas and solid fractions

$$
\begin{equation*}
v_{g} \equiv G F \equiv \varphi \quad v_{c} \equiv S F \equiv(1-\varphi) \tag{6}
\end{equation*}
$$

The gas fraction is given by:

$$
\begin{equation*}
\varphi=\left(1-\frac{\rho_{c}}{\rho_{v}}\right) \chi \tag{7}
\end{equation*}
$$

$\chi$ represents the fraction of the bulk density difference between the virgin and char materials that is converted to gas. In this study the value used was $\chi=0.66$, [3].
The formation rate of char and gas masses is:

$$
\begin{gather*}
\dot{w}_{g a s}^{p}=-\left(1-\frac{\rho_{c}}{\rho_{v}}\right) \chi \rho_{v} A \frac{d s(t)}{d t}  \tag{8}\\
\dot{w}_{c h a r}^{p}=-\left[1-\left(1-\frac{\rho_{c}}{\rho_{v}}\right) \chi\right] \rho_{v} A \frac{d s(t)}{d t} \tag{9}
\end{gather*}
$$

The conservation of gas mass equation is:

$$
\begin{equation*}
\frac{\partial\left(\rho_{g} \varphi\right)}{\partial t}+\frac{\rho_{g} \varphi}{V} \frac{\partial V}{\partial t}+\frac{\partial \dot{m}_{g}^{\prime \prime}}{\partial x}=0 \tag{10}
\end{equation*}
$$

In the previous equation $\partial V / \partial t$ represents the intumescence rate. The gas mass flux, $\dot{m}_{g}^{\prime \prime}$, is calculated accordingly to Darcy's law:

$$
\begin{equation*}
\dot{m}_{g}^{\prime \prime}=-\frac{\rho_{g} K}{\varphi \mu} \frac{\partial P}{\partial x} \tag{11}
\end{equation*}
$$

It is assumed that the gases present in the intumescent material behave as a perfect gas. The thermodynamic properties are related by the ideal gas law, assuming that the gas is a mixture of $50 \mathrm{wt} \% \mathrm{CO}_{2}$ and $50 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ :

$$
\begin{equation*}
\rho_{g}=\frac{M_{g}}{R} \frac{P(x, t)}{T_{g}(x, t)} \tag{12}
\end{equation*}
$$

$M_{g}$ is the mean molecular weight of the gases, $M_{g}=50 \% M_{C O_{2}}+50 \% M_{H_{2} O}$. Therefore, the generated gas molar mass used in the model is $31[\mathrm{~g} / \mathrm{mol}]$.
The last three equations combined can be used to give a differential equation for the pressure inside the intumescence. In the numeric calculations, the intumescence rate is assumed to be known, provided by the experimental results, so the pressure calculation is disregarded being assumed that the internal pressure is constant and equal to the atmospheric pressure.
An energy equation for the overall conservation of energy within the intumescence zone can be obtained by combining the energy equation for the gases with that of the solid char material. The equation for the conservation of energy per unit bulk volume can be written as:

$$
\begin{equation*}
(\rho C p)_{e f f} \frac{\partial T}{\partial t}+\frac{\partial}{\partial x}\left(\dot{m}_{g}^{\prime \prime} T_{g} C p_{g}\right)=\frac{\partial}{\partial x}\left(k_{e f f} \frac{\partial T}{\partial x}\right)-C p T \frac{\partial \rho}{\partial t}-(\rho C p)_{e f f} \frac{T}{V} \frac{\partial V}{\partial t} \tag{13}
\end{equation*}
$$

where

$$
\begin{align*}
& (\rho C p)_{e f f}=\varphi \rho_{g} C p_{g}+(1-\varphi) \rho_{c} C p_{c} \\
& k_{e f f}=\varphi k_{g}+(1-\varphi) k_{c} \tag{14}
\end{align*}
$$

The effective thermal conductivity for the intumescence bulk material, including gas and char, is equal to the thermal conductivity of the gas per unit bulk volume, plus that of the solid material. The same applies to the effective heat capacity.
In the steel plate back surface it is assumed an adiabatic boundary condition and at the boundary steel/virgin layers it is assumed a perfect thermal contact. At the moving front, the boundary conditions are:

$$
\begin{align*}
& k_{v} \frac{\partial T}{\partial x}=\varepsilon \dot{q}_{r}^{\prime \prime}-\varepsilon \sigma\left(T^{4}-T_{a}^{4}\right)-h_{c}\left(T-T_{a}\right) \quad \text { for } \\
& k_{v} \frac{\partial T}{\partial x}-k_{c} \frac{\partial T}{\partial x}=Q_{H} \quad \text { for } \quad T(s(t), t)<T_{P}  \tag{15}\\
&
\end{align*}
$$

In which $Q_{H}$ is the heat flux due to the endothermic decomposition of the virgin material, given by $-h_{p} \rho_{v} \dot{s}(t)$, where $h_{p}$ represents the decomposition enthalpy. A wide range of values are reported in the literature for the heat of pyrolysis and ranges from a few units to units of millions. The value used in the calculations was 50 [ $\mathrm{J} / \mathrm{kg}$ ].
Generally the emissivity is temperature dependent and varies as a function state of the material. For intumescent materials values between 0.7 and 0.95 can be found in the literature, where the lower value is normally used for the virgin material state, [4], and values of $0.8,0.9$ and 0.95 are used for the intumescence char surface, see [4,5, 6]. In this work an emissivity value of 0.92 and a constant convective heat transfer coefficient equal to 20 $\left[\mathrm{W} /\left(\mathrm{m}^{2} \mathrm{~K}\right)\right]$ are considered.
The intumescent coating specific mass was measured by the pycnometer method given a value of 1360 and 1250 $\left[\mathrm{kg} / \mathrm{m}^{3}\right]$ for the virgin coating and a value of 692.4 and $450\left[\mathrm{~kg} / \mathrm{m}^{3}\right]$ for the char material, for paints A and B, respectively. Steel properties are assumed constant, with a specific heat value of $600[\mathrm{~J} / \mathrm{kgK}]$ and a specific mass equal to $7850\left[\mathrm{~kg} / \mathrm{m}^{3}\right]$.
The mathematical model is based on the following major simplifying assumptions: there is no heat between gas and char, the thermophysical properties and the pressure at both layers are constant.
The solution method was implemented in a Matlab routine using the Method Of Lines (MOL), [7], and the integrator ode15s to solve the set of ordinary differential equations. The temperature field is determined by the steel and virgin energy equations. When the front reaches the pyrolysis temperature, equal to 250 [ ${ }^{\circ} \mathrm{c}$ ], starts to decompose and to move. Then the moving front rate is determined and the intumescence forms. The position the free boundary is set equal to the experimental results and the intumescence temperature field is determined. In each time step the virgin and char layers are remeshed.


Fig. 11. Comparison of measured and computed steel temperatures and position of the moving front,

$$
E_{0}=125 \mathrm{KJmol}^{-1} .
$$

The numerical results follow reasonably well the experimental values, as presented in Fig. 11. The results show that both the determined steel temperatures and the moving front are strongly dependent on the activation energy
that defines the amount of mass loss of virgin paint. The value used in the simulations was obtained from the literature, but the correct values of both paints are needed. Currently a set of thermogravimetric tests are being conducted to determine reaction kinetics parameters, the activation energy and the exponential factor.

## 4 Conclusions

A numerical model is applied to determine the steel temperature considering the intumescence measured in the cone calorimeter experimental tests. The model considers the intumescent heat sink and swelling based in the mass transfer, swelling and the kinetic decomposition. The results show that temperature variation is strongly dependent on the kinetic parameters.

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