



Article

Comparison of Nonlinear Compensation Techniques for 400-Gb/s Coherent Multi-Band **OFDM Super-Channels**

Vasiliki Vgenopoulou 1,* , Mengdi Song 2, Erwan Pincemin 3, Yves Jaouën 2, Stylianos Sygletos 4 and Ioannis Roudas 5

- Department of Physics, University of Patras, Rio, 26500 Patras, Greece
- LTCI, CNRS, Telecom ParisTech, Université Paris Saclay, 75013 Paris, France; mengdi.song@telecom-paristech.fr (M.S.); yves.jaouen@telecom-paristech.fr (Y.J.)
- Orange Labs Networks, 2 Avenue Pierre Marzin, 22307 Lannion, France; erwan.pincemin@orange.com
- Aston Institute of Photonic Technologies, Aston University, Birmingham B4 7ET, UK; s.sygletos@aston.ac.uk
- Department of Electrical and Computer Engineering, Montana State University, Bozeman, MT 59717, USA; ioannis.roudas@montana.edu
- Correspondence: vvgeno@gmail.com; Tel.: +30-6972-971-284

Received: 30 January 2018; Accepted: 13 March 2018; Published: 15 March 2018

Featured Application: The results of the comparison study, between the well-known digital backpropagation nonlinear compensation method and the 3rd-order inverse Volterra series transfer function nonlinear equalizer, reveal the physical limits of the nonlinear equalizers when high bit rates are transmitted in long-haul optical communication systems, in the presence of increased nonlinear effects. In addition, the computational complexity and, by extension, the cost, introduced by each equalizer, are taken into account. The insight gained from this study could be valuable in the foreseeable future in order to indicate the nonlinear compensation method of choice for the next generation inter-data centers supporting bit rates as high as 400 Gb/s.

Abstract: The last few years, many studies have been published on the 3rd-order inverse Volterra series transfer function nonlinear equalizer (IVSTF-NLE) in long-haul optical communication systems. Nonetheless, no experimental work has been published on investigating the potential of the 3rd-order IVSTF-NLE for the compensation of Kerr nonlinearities in a long-haul wavelength division multiplexing (WDM) system consisting of high-bit rate super-channels, as high as 400 Gb/s. In this paper, we study experimentally the performance of a 3rd-order IVSTF-NLE in a coherent optical WDM system, with a central, 400-Gb/s, 4-band, dual-polarization (DP), 16-ary quadrature amplitude modulation (QAM) orthogonal frequency division multiplexing (OFDM) super-channel. We compare its performance against the performance of the digital back-propagation split-step Fourier (DBP-SSF) method for the compensation of nonlinearities after 10×100 km of ITU-T G.652 standard single mode fiber (SSMF). In the second part of this paper, we compare, via Monte Carlo simulations, the performance of the 3rd-order IVSTF-NLE and the DBP-SSF method, in terms of reach extension and computational complexity, after propagation through ITU-T G.652 SSMF and a ITU-T G.655 large effective area fiber (LEAF). By means of both experimental evaluation and simulations, we show that, in the presence of strong nonlinear effects, the 3rd-order IVSTF-NLE, which uses a single step per span, performs similarly with the two-steps-per-span DBP-SSF, whereas the eight-steps-per-span DBP-SSF is only marginally better but at the vast expense of computational complexity.

Keywords: nonlinear equalizers; volterra series transfer function; digital back-propagation

Appl. Sci. 2018, 8, 447 2 of 14

1. Introduction

Nonlinearities in long-haul fiber-optic communication systems present an obstacle to the capacity increase of optical transport networks [1]. Nonlinear compensation methods (digital or optical) have been extensively studied in recent years [2]. Digital equalization techniques can provide mitigation of both linear and nonlinear effects in coherent optical communication systems and fall into two main categories [3]: (a) pre-compensation methods that create a more resilient signal to fiber nonlinearities prior to fiber propagation [4,5]; and (b) post-compensation techniques, which are applied on the distorted signal after propagation. The latter category includes nonlinear equalizers (NLEs) based on perturbation solutions of the coupled nonlinear Schrödinger equations (CNLSE) [6–8], the digital back-propagation (DBP) based on the split-step Fourier (SSF) method [9–11], and Volterra transfer function series-based NLEs [12,13], using either 3rd-order [14–17] or 5th order-kernels [18,19].

The last few years, interesting studies have been published on the 3rd-order Volterra-based NLEs [14–17]. For this category of NLEs, the linear and nonlinear compensation is performed in parallel, rendering them more suitable for real-time implementation. One of these published works investigates the performance of a Volterra series intra-channel NLE, based on an analytical closed-form solution for the 3rd-order Volterra kernel, in the frequency domain [14]. This Volterra-NLE is tested in a single-channel optical system using a 20 Gbaud, non-return-to-zero (NRZ)-quadrature phase shift keying (QPSK) signal after 1600 km of both SSMF and non-zero dispersion shifted fiber [14]. The results reveal a ~2 dB Q²-factor improvement on the nonlinear tolerance relatively to the multistep-per-span DBP-SSF method when 2 samples per symbol (SpS) are used for the equalization process [14]. Even though the equalization performance of the 3rd-order Volterra-based NLEs can compete with the widely-used DBP-SSF method, the increasing need for reduced computational complexity has triggered more in-depth studies on this topic [15]. One of them is the numerical study of the performance of a simplified Volterra NLE, which showed reduction of the total computational complexity by a factor of ~3 compared to the full Volterra NLE [15], when tested on a long-haul 224 Gb/s dual-polarization (DP), 16-ary quadrature amplitude modulation (QAM) transmission system [15]. Then, a 3rd-order inverse Volterra series transfer function (IVSTF)-NLE was studied via simulations in [16], on a single-channel transmission system using a 256 Gb/s DP, 16QAM signal after 1024 km of an SSMF, revealing a 1 dB Q²-factor improvement and a 50% reduction in the computational complexity by lowering the processing rate. Later, the performance of a variant of the 3rd-order IVSTF-NLE was studied in a coherent orthogonal frequency division multiplexing (OFDM) single-channel system of the same total rate and transmission distance [17] showing a Q²-factor improvement of 2 dB, i.e., 1 dB higher compared to the study of [16].

Up to date and to the best of our knowledge, no experimental work has been published on investigating the potential of a 3rd-order IVSTF-NLE in a long-haul wavelength division multiplexing (WDM) system consisting of high-bit rate super-channels, as high as 400 Gb/s, which are necessary, nowadays, to meet the requirements of high-speed transmission [20]. Therefore, there is a gap in the available literature which should be covered. A very appealing version of a super-channel is based on a DP, multi-band OFDM signal offering greater spectral efficiency and increased nonlinear tolerance compared to the single-carrier case, mostly due to the splitting of high-baud-rate, single-carrier signals into multiple multiplexed low-baud-rate subcarriers [21]. Multi-band OFDM is very similar to sub-carrier multiplexing (SCM), which recently attracts much attention [22,23] due to its transmission reach improvement of about 20% compared to its high baud-rate single-carrier counterpart [22]. SCM is a transmission technique which optimally trades off intra- and inter-channel non-linear effects by an optimization of the baud-rate of its sub-bands [23].

In this paper, we experimentally investigate the performance of the 3rd-order IVSTF-NLE in a WDM experimental using a 400 Gb/s, DP, 16QAM, OFDM super-channel at the center of a WDM comb, after propagating through 10×100 km of an SSMF [16]. In addition, its performance is compared with the conventional DBP-SSF method with multiple steps per span [9]. Then, we extend the comparison study, via Monte Carlo simulations, by replacing the SSMF with a large effective area

Appl. Sci. 2018, 8, 447 3 of 14

fiber (LEAF) to test the robustness of the 3rd-order IVSTF-NLE against the multi-span DBP-SSF NLE in the presence of stronger nonlinear effects. We observe that, in the presence of strong nonlinear effects, the 3rd-order IVSTF-NLE performs similarly to the almost twice more complex DBP-SSF with two-steps-per-span, whereas the eight steps-per-span DBP-SSFR is only slightly better. Nonetheless, the later algorithm is very demanding, in terms of real multiplications, as we estimate in the present study.

The rest of the paper is organized as follows: In Sections 2 and 3, the experimental and the simulation setups are described, respectively. In Section 4, we present and discuss the experimental and simulation results. In addition, we estimate the computational complexity of the NLEs in terms of the number of real multiplications. Finally, the conclusions are summarized in Section 5.

2. Experimental Section

The 3rd-order IVSTF-NLE used in this experimental study is based on the algorithm published in [16]. For completeness and for the reader's convenience, we summarize below the major schematics highlighting its operating principle, whereas the theoretical model is summarized in the Appendix A.

The block diagram of the 3rd-order IVSTF-NLE is shown in Figure 1a. The equalization is performed in parallel. In the block diagram of Figure 1a, the linear compensation is represented by the two upper arms and the nonlinear compensation by the N nonlinear branches. The linear compensation comprises a single branch per polarization, accounting for the chromatic dispersion (CD) introduced by all the N fiber spans, in the frequency domain. Each polarization tributary passes through a filter with transfer function $K_1(\omega)$ (see Expression (A5) in the Appendix A). On the other hand, the nonlinear compensation is implemented in a span-by-span basis through N separate branches, as described in (A6).

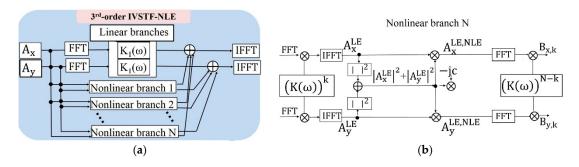


Figure 1. (a) Block diagram of the 3rd-order IVSTF-NLE; (b) Operating principle of the kth nonlinear compensation branch of the 3rd-order IVSTF-NLE [16]. (Symbols: Inverse Fast Fourier Transform (IFFT), Linearly Equalized (LE), Non-Linearly Equalized (NLE), Fast Fourier Transform (FFT)).

Figure 1b illustrates the operating principle of the kth nonlinear branch, which is divided into three stages. The first stage performs CD compensation in the frequency domain, and it is realized through the filter $(K(\omega))^k$ (see Expression (A7) in the Appendix A). The second stage is the compensation of the intra-channel nonlinearities, in the time domain, implemented as described in (A8). The third and the last stage of each nonlinear branch is the compensation of the residual dispersion, in the frequency domain, through a filter with transfer function $(K(\omega))^{N-k}$ (see Expression (A9) in the Appendix A). More specifically, first, the received x and y polarization tributaries (i.e., A_x and A_y) are linearly compensated in the frequency domain. Then, the linearly-compensated polarization tributaries are switched back in the time domain (i.e., A_x^{LE} and A_y^{LE}) for the intra-channel nonlinearity equalization where each one of them is multiplied with the instantaneous power of x and y polarization (i.e., $|A_x^{LE}|^2 + |A_y^{LE}|^2$) scaled by the adjustable parameter C_{IVSTF} . The optimization of the latter is achieved by sweeping a range of values in the vicinity of its nominal value $C_{nominal} = (8/9)\gamma L_{eff}$,

Appl. Sci. 2018, 8, 447 4 of 14

where $L_{eff} = (1 - e^{-\alpha L})/\alpha$ is the effective span length. Finally, the polarization tributaries $A_x^{LE,NLE}$ and $A_y^{LE,NLE}$ are switched again to the frequency domain, where the residual CD is compensated through a filter with transfer function $(K(\omega))^{N-k}$.

The experimental setup is depicted in Figure 2. The configuration consists of a coherent, DP 16QAM OFDM super-channel in a 10×100 km transmission line carrying a net bit rate of 400 Gb/s. The OFDM super-channel consists of 4 bands. Thus, the net bit rate per band is equal to 100 Gb/s. By adding 20% soft-decision forward error correction (SD-FEC) overhead and 20% OFDM overhead, including the cyclic prefix (CP), as well as the training sequence (TS) and the pilot tones, then, the raw bit rate per band is 144 Gb/s. Each band occupies 18 GHz (Figure 3d). A guard-band of 2 GHz is introduced to limit the crosstalk between adjacent bands. The total bandwidth of the super-channel is 78 GHz, corresponding to a net spectral efficiency of 5.13 b/s/Hz. The OFDM frame is generated by Matlab® using a 1024-point fast Fourier transform (FFT)/inverse FFT (IFFT). There are 576 subcarriers, each carrying 16QAM. They are generated by a 15-GHz bandwidth Keysight[®] arbitrary waveform generator (AWG) operating at 64 Gsamples/s. The in-phase and quadrature components of the coherent OFDM signal are electrically amplified using two linear RF driver amplifiers (SHF807), which feed a quadrature modulator (CMZM). The first CMZM generates the odd channels while the second generates the even channels, in order to totally decorrelate the data carried by adjacent channels. The odd and even combs are combined together using a 3-dB polarization maintaining (PM) coupler. The polarization multiplexing is realized by dividing the signal into two paths, putting a delay of one-OFDM-symbol-duration on one of the paths, switching it to the perpendicular polarization, and combining them together, as shown in Figure 2. The one-OFDM-symbol-duration delay corresponds to 1152 samples (1024 FFT size samples and 128 CP samples). Then, the OFDM super-channel is combined with 58 wavelengths modulated at 100 Gb/s using DP-QPSK and spaced 50-GHz apart from each other. The transmission line is composed of 10 spans of 100 km of SSMF. A single-stage erbium doped fiber amplifiers (EDFAs), with 20 dB gain and ~4.5 dB noise figure, is applied at the end of each span and for all the 10 spans. At this point, we note that the linear and non-linear equalization schemes that are presented in this paper are not adaptive but feed forward schemes. Although they may require exact knowledge of the system's parameters to operate, their operation is not affected by the amount of accumulated noise at the receiving end. On the other hand, their effectiveness in improving the system performance is affected by the noise added by the EDFA elements along the link and the nonlinear mixing between signal and noise. This additional non-linear noise effect cannot be treated by any equalization scheme at the receiver, but only with the use of distributed compensation methods, such as all optical regenerators or cascaded optical phase conjugation (OPC) elements [24].

A dynamic gain equalizer (DGE) is introduced in the middle of the link to flatten the multiplex power after 10×100 km. At the end of the link, an optical bandpass filter (BPF) selects the OFDM band under measurement. This one is detected by a polarization- and phase-diversity coherent receiver using an external cavity laser (ECL) with 100 kHz linewidth as local oscillator (LO). The effective number of bits (ENoB) in the digital-to-analog converters (DACs) and in the analog-to-digital converters (ADCs) is approximately 5. We use 10^6 bits to evaluate the bit error rate (BER) by error counting.

We consider three scenarios to explore the physical limits of the NLEs performance: (a) a single-channel transmission of a single-band DP, 16QAM OFDM signal (Figure 3a); (b) WDM transmission with a 2-band DP, 16QAM OFDM signal (Figure 3b), and, finally (c) WDM transmission with a 4-band, DP, 16QAM OFDM super-channel at the center of the WDM comb (Figure 3c).

Appl. Sci. 2018, 8, 447 5 of 14

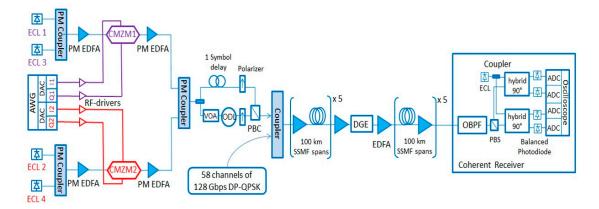


Figure 2. Experimental setup. (Symbols: external cavity laser (ECL), polarization-maintaining (PM) coupler, polarization-maintaining erbium-doped fiber amplifier (PM EDFA), quadrature modulator (CMZM), arbitrary waveform generator (AWG), digital-to-analog converter (DAC), RF driver amplifier, variable optical attenuator (VOA), optical delay line (ODL), polarization beam combiner (PBC), dynamic gain equalizer (DGE), optical bandpass filter (OBPF), polarization beam splitter (PBS), analog-to-digital converter (ADC)).

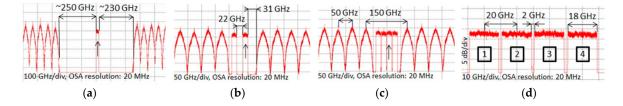


Figure 3. Spectra of: (a) a single-channel transmission of a single-band DP, 16-ary quadrature amplitude modulation (QAM) orthogonal frequency division multiplexing (OFDM) signal, (b) Wavelength division multiplexing (WDM) transmission with a 2-band DP, 16QAM OFDM signal, (c) WDM transmission with a 4-band, DP, 16QAM OFDM super-channel at the center of the WDM comb and (d) the multi-band (MB) OFDM super-channel. The black arrow, in each case, indicates the band under measurement.

The power spectra are recorded by a high-spectral-resolution (20 MHz) optical spectrum analyzer (OSA). The first scenario corresponds to a to a pseudo-single-channel transmission scenario in which the cross-phase modulation (XPM) and the four wave mixing (FWM) are considered practically negligible (Figure 3a). In the second scenario, the inter-channel nonlinearities are increased (Figure 3b). Finally, the third study case exacerbates the intra- and inter-channel nonlinearities (Figure 3c). The guard-band spacing between the third OFDM band and its immediate left/right neighbors are 250/230 GHz, 22/31 GHz and 2/2 GHz for the study cases (a), (b) and (c), respectively.

For the detection of the OFDM band under study, we used a 50 GSa/s sampling rate real-time oscilloscope, followed by resampling at 32 GSa/s. The latter is the sampling frequency used by the NLEs. The off-line OFDM signal processing is thoroughly described in [25]. In the coherent receiver, IVSTF-NLE and DBP-SSF equalizers are placed at the initial stages of the digital signal processing (DSP), where CD compensation is usually performed [26]. The detected OFDM band has an aggregate symbol rate of 18 Gbaud. Thus, the NLEs operate with 1.8 SpS. In order to achieve this, we have applied down-sampling, in the frequency domain, right before the NLEs. After the NLEs, we apply one more down-sampling, again in the frequency domain, in order to achieve 1 SpS. Through trial and error, it was observed that further increase of the number of SpS provides just a marginal performance improvement adding unnecessarily computational load.

Appl. Sci. 2018, 8, 447 6 of 14

3. Simulation Setup

In addition to the experimental comparison between the 3rd-order IVSTF-NLE and the DBP-SSF method, we extend this comparison study, in terms of reach extension, after propagation in an SSMF and in a LEAF. Due to lack of a LEAF link in the lab, we decided to model a transmission system similar to the experimental case depicted in Figure 3c, in which the nonlinearities are exacerbated. In this way, we complete the experimental comparison with Monte Carlo simulations and measure what the reach extension is when employing the different nonlinear compensation methods. The replacement of the SSMF with a LEAF is only an extension of our study in order to gain a better insight on the robustness of the NLEs in extreme nonlinear effects and it is not suggested for practical use.

The simulated transmission model is shown in Figure 4 and consists of three coherent, 4-band DP, OFDM super-channels. Quantizations are carried out in the simulation in order to take into account the ENoB, which is set equal to 5, in the DAC and ADC. The laser phase noise is neglected. The SSMF is modeled with attenuation coefficient equal to $\alpha = 0.2$ dB/km, CD of D = 17 ps/nm/km and Kerr coefficient $\gamma = 1.3$ W⁻¹km⁻¹ [27]. Considering the parameters of LEAF, we have $\alpha = 0.19$ dB/km, D = 4 ps/nm/km, and $\gamma = 1.5$ W⁻¹km⁻¹ [27]. The BER is calculated by error counting. A total number of 436,224 bits per band are used.

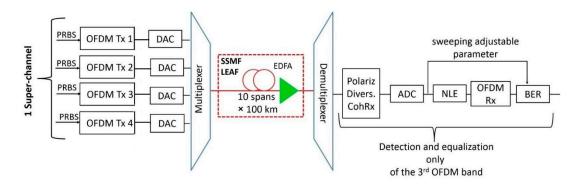


Figure 4. Simulation setup of a 4-band, single-polarization, OFDM super-channel using as a transmission link either an SSMF or a LEAF. (Abbreviations: pseudo-random bit sequence (PRBS), OFDM transmitter (OFDM Tx), digital-to-analog converter (DAC), standard single-mode fiber (SSMF), large effective area fiber (LEAF), erbium-doped fiber amplifier (EDFA), polarization-diversity coherent receiver (Polariz. Divers. CohRx), analog-to-digital converter (ADC), nonlinear equalizer (NLE), OFDM receiver (OFDM Rx), and bit-error-rate (BER).

4. Results and Discussion

In the following, we present experimental and numerical results for the performance of the 3rd-order IVSTF-NLE and the DBP-SSF method, varying the number of steps per span. For brevity, we denote the different versions of the DBP-SSF NLEs as DBP-SSF_{Nsteps}, where N_{steps} is the number of steps per span. In both, experimental and simulation, studies we have only detected the 3rd-band of the central OFDM super-channel, since inner bands are more affected by inter-channel nonlinear impairments compared to the outer bands. To compare the performance of different NLEs, we use the Q^2 -factor as a figure of merit, which is related to BER by Q^2 (dB) = $20\log_{10}\left[\sqrt{2} \operatorname{erfc}^{-1}(2\operatorname{BER})\right]$ [16]. We estimated the net Q^2 -factor improvement (ΔQ^2) in dB which is obtained as follows: First, we estimated the maximum Q^2 -factor value when only linear equalization is applied (max. $Q^2_{w. LE}$). Second, we applied both, linear and nonlinear, equalization and we evaluated the corresponding maximum Q^2 -factor value (max. $Q^2_{w. NLE}$). We define as $\Delta Q^2 = Q^2_{w. NLE} - Q^2_{w. LE}$ the net Q^2 -factor improvement, thus, the higher the ΔQ^2 , the better the performance of the NLE. For both, experimental and simulation, results four trials were conducted and then the average was calculated and recorded as the final value.

Appl. Sci. 2018, 8, 447 7 of 14

4.1. Experimental Results

Figure 5a shows the maximum Q^2 -factor as a function of the launch power after 10×100 km of SSMF for single-channel transmission with linear compensation only, as well as with IVSTF or DBP-SSF_{1,2,8} NLEs (scenario described in Figure 3a). The Q^2 -factor improvement is ~1 dB (i.e., BER = 3.2×10^{-3} with linear equalization only (wo. NLE) and BER = 9.9×10^{-4} with linear and nonlinear equalization (w. NLE)) for all NLEs, which agrees with the published results for the single-channel, single-carrier system in [16].

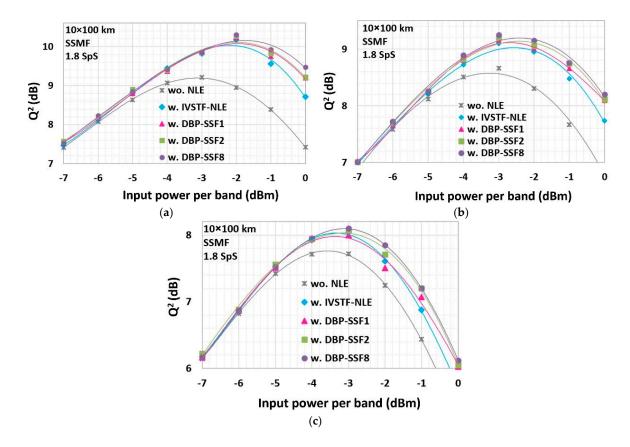


Figure 5. Experimental results on Q^2 -factor vs. input power per band without/with IVSTF-NLE and DBP-SSF_{1,2,8} in (a) single-channel with a single OFDM band; (b) a single-OFDM-band super-channel surrounded by WDM DP-QPSK channels; and (c) a WDM, 4-band OFDM super-channel surrounded by WDM DP-QPSK channels after transmission through 10×100 km SSMF.

Figure 5b corresponds to a WDM coherent optical system with two OFDM bands at its center (scenario described in Figure 3b). In this case, the Q^2 -factor improvements are ~0.44 dB (i.e., BER = 5.3×10^{-3} wo. NLE and BER = 3.6×10^{-3} w. NLE) for the 3rd-order IVSTF-NLE, ~0.5 dB for the DBP-SSF₁ NLE, and ~0.6 dB (i.e., BER = 5.3×10^{-3} wo. NLE and BER = 3.2×10^{-3} w. NLE) for the DBP-SSF_{2,8} NLEs. We observe that, in this scenario, the performance of the DBP-SSF method saturates at two steps per span.

Figure 5c shows representative plots of the Q^2 -factor vs. input power per band for a central 4-band OFDM super-channel surrounded by WDM DP QPSK channels (scenario described in Figure 3c). The measured Q^2 -factor improvements are ~0.33 dB (i.e., BER = 7.5×10^{-3} wo. NLE and BER = 5.8×10^{-3} w. NLE) for the 3rd-order IVSTF-NLE, ~0.28 dB for the DBP-SSF₁ NLE, ~0.35 dB (i.e., BER = 7.5×10^{-3} wo. NLE and BER = 5.7×10^{-3} w. NLE) by the DBP-SSF₂ NLE and ~0.4 dB (i.e., BER = 7.5×10^{-3} wo. NLE and BER = 5.5×10^{-3} w. NLE) by DBP-SSF₈ NLE.

Appl. Sci. 2018, 8, 447 8 of 14

Summing up our observations from the experimental results, we note that all NLEs mitigate equally well the intra-channel nonlinear effects (Figure 5a) but their performances degrade when the inter-channel nonlinear crosstalk is also considered (Figure 5c). This modest performance improvement is mainly due to the detection and compensation of each OFDM band separately, leaving inter-channel nonlinearities uncompensated. We observe that the IVSTF-NLE is worse compared to DBP-SSF method for input powers per band higher than the optimum because as the input power per band increases, the nonlinear effects become stronger requiring more computational steps to achieve their compensation. In addition, we observe that the DBP-SSF method reaches its optimum performance at 8 steps per span. Nevertheless, the latter is only marginally more powerful compared to the DBP-SSF₂ NLE. Therefore, as the nonlinear phenomena become stronger, larger number of steps per span are required for the DBP-SSF method to reach its performance limit. On the contrary, the 3rd-order IVSTF-NLE, which operates with a single step per span, performs almost as good as the DBP-SSF₂ NLE, with the latter being twice more complex than the former. Finally, we emphasize that the primary focus of the experimental results is to compare and gain a better insight about the potential of each NLE in the presence of very strong nonlinear effects. Although the performance results of all NLEs is modest, especially in the worst-case scenario (see Figure 5c), they are indicative of the fact that the 3rd-order IVSTF-NLE can compete with significantly lower computational effort the heavily iterative DBP-SSF with multi-steps per span.

4.2. Simulation Results

The first step in the simulation study was to validate the model that we implemented. For this matter, we performed Q^2 -factor evaluation as a function of the input power per band after propagation through 10×100 km of an SSMF, using 1.8 SpS for the equalization process. All NLEs were optimized, as we did for the experimental study, through their adjustable parameters [9,16]. The simulation results are shown in Figure 6. The measured Q^2 -factor improvements, compared to linear equalization, are ~0.32 dB (i.e., BER = 5.9×10^{-3} wo. NLE and BER = 4.6×10^{-3} w. NLE) for the 3rd-order IVSTF-NLE, ~0.3 dB (i.e., BER = 5.9×10^{-3} wo. NLE and BER = 4.6×10^{-3} w. NLE) for the DBP-SSF₁ NLE, and ~0.35 dB (i.e., BER = 5.9×10^{-3} wo. NLE and BER = 4.5×10^{-3} w. NLE) for the DBP-SSF_{2,8} NLEs. There is a very good agreement with the experimental results represented in Figure 5c. Thus, our model is a fair representation of the experimental setup.

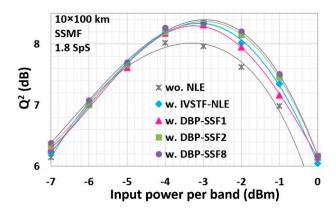


Figure 6. Simulation results on Q^2 -factor vs. input power per band without/with IVSTF-NLE and DBP-SSF_{1,2,8} NLEs for the 3rd-band of the central OFDM in a WDM system with three wavelengths, 4-band DP-16QAM OFDM super-channels after 10×100 km of SSMF.

Next, we compare the maximum reach versus input power per band, with and without the NLEs, after signal transmission through an SSMF and a LEAF. Figure 7a shows that the maximum reach is achieved for input power per band equal to -3 dBm in SSMF, in all cases. At the FEC limit (i.e.,

Appl. Sci. 2018, 8, 447 9 of 14

BER = 2×10^{-2} or Q^2 = 6.25 dB), the maximum reach is 1400 km with linear equalization only. After nonlinear compensation, the maximum reach was extended ~3% for the 3rd-order IVSTF-NLE, ~3% for the DBP-SSF₁ NLE, ~4.6% for the DBP-SSF₂ NLE and ~7% for the DBP-SSF₈ NLE, with respect to linear equalization. We observe that the DBP-SSF method slightly outperforms the 3rd-order IVSTF-NLE, especially if the number of steps per span increases.

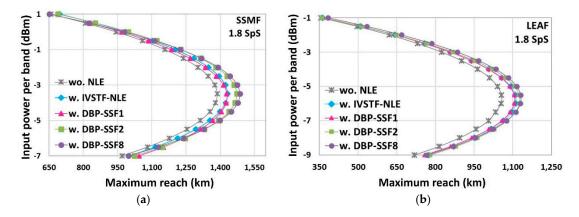


Figure 7. Maximum transmission reach at the FEC limit vs. launch power using IVSTF-NLE and DBP-SSF_{1,2,8} NLEs for the 3rd band of the center OFDM super-channel in the simulation case, after signal transmission through (a) SSMF and (b) LEAF.

Then, we replace the SSMF with LEAF to investigate how the maximum reach is affected when the nonlinear impairments become stronger. In Figure 7b, the maximum reach without NLE is 1100 km in LEAF, which is 300 km shorter compared to SSMF. The maximum reach is extended by \sim 6.3% for the 3rd-order IVSTF-NLE, \sim 5.4% for the DBP-SSF $_1$ NLE, \sim 6.3% for the DBP-SSF $_2$ NLE, and \sim 7.3% for the DBP-SSF $_8$ NLE compared to linear case. The DBP-SSF method with eight steps per span is once more the NLE with the best performance, compared to all the aforementioned NLEs, but at the vast expense of computational complexity, as shown in the following sub-section.

The modest reach extensions provided by the NLEs provide valuable information about their physical limits while the nonlinearities increase gradually. Especially from Figure 7b, it is observed that even though the nonlinear effects have been further increased, due to the replacement of the SSMF with a LEAF, the performance of the single-step-step-span 3rd-order IVSTF-NLE has been improved (i.e., from \sim 3% in SSMF increased to \sim 6.3% in LEAF). On the contrary, the DBP-SSF method needs eight-steps-per-span in order to provide the maximum reach extension (i.e., \sim 7% in both, SSMF and LEAF, cases). Thus, in LEAF case, the performance of the 3rd-order IVSTF-NLE differs only slightly compared to the performance of DBP-SSF₈ NLE while the former is almost eight times less complex.

4.3. Evaluation of Computational Complexity

The computational complexity is one of the criteria used to decide whether a specific NLE is suitable for real-time implementation. Therefore, in this subsection, we evaluate the computational complexity of the various nonlinear compensation methods, in terms of the number of real multiplications per sample per polarization. In addition, we compute the maximum Q^2 -factor provided by the various NLEs as a function of complexity, after transmission through SSMF and LEAF.

First, we estimate the computational complexity of the 3rd-order IVSTF-NLE in terms of real multiplications per sample per polarization following the method of [16]. However, in our calculations, and modeling, we used the same FFT block size (N_{FFT}) for both the linear and the nonlinear branches, while in [16] each of the nonlinear branches operate with $N_{FFT}/2$. We decided to use the same N_{FFT} in both, the linear and the nonlinear, branches because it was observed, through trial and error, that only then the 3rd-order IVSTF-NLE exhibits its best performance in the worst case scenario (see Figure 3c)

and after 1000 km of SSMF using only 1.8 SpS. We consider a radix-2 implementation of FFT. In this case, the number of real multiplications for every FFT/IFFT is equal to $2\log_2 N_{FFT}$ [16]. Therefore, the FFT and the IFFT at the input and at the output of the IVSTF-NLE, respectively, are realized with $4\log_2 N_{FFT}$ real multiplications [16]. The linear branch of the IVSTF-NLE, as depicted in Figure 1a, operates with 4 real multiplications.

At each nonlinear branch (Figure 1b), CD compensation is performed with 4 real multiplications per sample, in the frequency domain. Next, an IFFT requires $2\log_2N_{FFT}$ real multiplications in the time domain. Then, 5 real multiplications per sample per polarization are required for multiplying the total power of x and y polarizations with jc (i.e., C_{IVSTF}). The latter multiplication is common between the two polarizations, thus, only 2.5 multiplications are required per sample per polarization. An FFT follows, with $2\log_2N_{FFT}$ real multiplications, for the compensation of the residual CD in the frequency domain, adding 4 more real multiplications. Totally, $4 + 4\log_2N_{FFT} + N_{spans} \times (4\log_2N_{FFT} + 10.5)$ real multiplications per sample per polarization are needed for the operation of the 3rd-order IVSTF-NLE. For the DBP-SSF method, the required number of real multiplications per polarization per sample is $N_{steps} \times N_{spans} \times (4\log_2N_{FFT} + 10.5)$ [16].

From the computational complexity analysis, it is obvious that the lower the N_{FFT} , the lower the computational complexity per block. At this point, the key question is if there is an optimum N_{FFT} , at which the performance limit of each NLE can be reached with a minimum computational complexity per block. To answer this question, we applied, right before each NLE, the method of overlap and save (OS) to divide the received, uncompensated signal into small FFT blocks. After the full compensation of each block (i.e., linear and nonlinear), we aggregated them back together, at the output of each NLE, to form the output signal. Then, we measured the Q^2 -factor as a function of the N_{FFT} , after 14×100 km of SSMF, at the optimum input power per band (i.e., -3 dBm). We chose this transmission reach because it corresponds to the FEC limit without nonlinear compensation (i.e., $Q^2 = 6.25$ dB). Following a similar rationale, we repeated the simulation runs after 11×100 km of LEAF, at optimum input power per band equal to -6 dBm.

Figure 8a,b show the results for the SSMF and LEAF study, respectively. In both cases, all NLEs reach their performance limit, at a certain N_{FFT} . Tables 1 and 2 show the Q^2 -factor improvement, with respect to the FEC limit, provided by each NLE, at the optimum N_{FFT} as well as the number of real multiplications required per sample per polarization for these improvements. After SSMF transmission (Table 1), we observe that the 3rd-order IVSTF-NLE is as good as the DBP-SSF₈ NLE but with the latter being almost eight times more complex. After LEAF transmission (Table 2), we observe that, in the presence of stronger nonlinear effects, the 3rd-order IVSTF-NLE is as good as the DBP-SSF₂ NLE with the latter requiring ~2 times more real multiplications, compared to the former. Finally, the DBP-SSF₈ NLE is only marginally better compared to the IVSTF-NLE.

The estimations, summarized in Tables 1 and 2, validate what it was already observed in the experimental and the simulation results, and this is the fact that the performance of the DBP-SSF method saturates with eight-steps-per-span, whereas the improvement it provides is comparable to the improvement provided by the significantly less complex 3rd-order IVSTF-NLE. Although we understand that the differences from the performances of DBP-SSF_{1,2} NLEs might sound modest, we still draw useful conclusions considering the physical limits of the NLEs in the presence of increased nonlinearities.

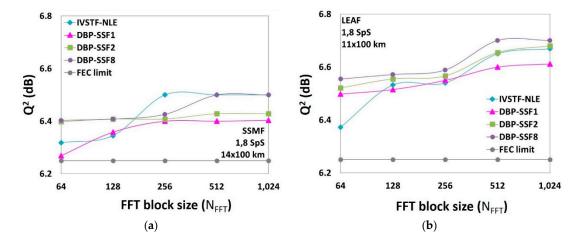


Figure 8. Q^2 -factor as a function of the N_{FFT} , at the optimum input power per band, after (a) 14×100 km of SSMF and (b) 11×100 km of LEAF.

Table 1. Maximum Q^2 -factor and the corresponding number of real multiplications per sample per polarization required at the optimum N_{FFT} , after 14×100 km of SSMF at optimum input power equal to -3 dBm.

NLE	Optimum N_{FFT}	Maximum Q ² (dB)	Maximum BER	Number of Real Multiplications
3rd-order IVSTF	256	6.5	1.7×10^{-2}	631
DBP-SSF ₁	256	6.4	1.8×10^{-2}	595
DBP-SSF ₂	512	6.43	1.8×10^{-2}	1302
DBP-SSF ₈	512	6.5	$1.7 imes 10^{-2}$	5208

Nonlinear equalizer (NLE), FFT block size (N_{FFT}), Inverse Volterra series transfer function (IVSTF), Digital backpropagation (DBP) based on split-step Fourier (DBP-SSF).

Table 2. Maximum Q^2 -factor and the corresponding number of real multiplications per sample per polarization required at the optimum N_{FFT} , after 11×100 km of LEAF at optimum input power equal to -6 dBm.

NLE	Optimum N_{FFT}	Maximum Q ² (dB)	Maximum BER	Number of Real Multiplications
3rd-order IVSTF	512	6.65	1.6×10^{-2}	552
DBP-SSF ₁	512	6.6	1.6×10^{-2}	512
DBP-SSF ₂	512	6.65	1.6×10^{-2}	1023
DBP-SSF ₈	512	6.7	1.5×10^{-2}	4092

5. Conclusions

We compare, experimentally, the performance of a 3rd-order IVSTF-NLE and the DBP-SSF method, with various numbers of steps per span, in a coherent optical WDM system, with a central 400 Gb/s 4-band, DP-16QAM OFDM super-channel exacerbating the intra- and inter-channel nonlinearities. Then, we extend the study numerically by estimating the maximum transmission reach, provided by the NLEs under study, with respect to the FEC limit after transmission in a LEAF. Both, the experimental and the simulation, results reveal that the performance of the single-step-per-span 3rd-order IVSTF-NLE can compete the well-known DBP-SSF method. The latter requires eight-steps-per-span in order to reach its optimum performance which, however, is comparable with the performance with the almost eight times less complex 3rd-order IVSTF-NLE. Although the differences in the performance of the DBP-SSF_{1,2} NLEs, compared to the DBP-SSF₈ NLE and the 3rd-order IVSTF-NLE, are only marginal,

they are still indicative of the robustness of each and every NLE in the presence of exacerbated nonlinear effects. Thus, the 3rd-order IVSTF-NLE could be a reasonable choice for compensating nonlinear impairments with lower computational complexity and, by extension, lower cost.

More generally, our study confirms that digital nonlinear equalization is especially efficient to mitigate intra-channel nonlinear effects and less convenient when also inter-channel nonlinearities are involved. However, with the increase of data rate carried by the sub-channels constituting the super-channel (supported by the improvement of bandwidth/resolution of DACs/ADCs), digital nonlinear equalization could know a renewed interest because, at high bit/symbol rate per sub-channel, intra-channel nonlinearities are predominant.

Author Contributions: Yves Jaouën and Erwan Pincemin conceived the experiment. Mengdi Song and Erwan Pincemin designed and performed the experiment; Vasiliki Vgenopoulou analyzed the experimental data, conducted the theoretical study and wrote the paper. Mengdi Song contributed to the authorship of the experimental setup. Stylianos Sygletos provided valuable advice considering the writing of the paper. Yves Jaouën and Ioannis Roudas supervised the whole work.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

In the absence of polarization mode dispersion (PMD) and polarization-dependent loss (PDL), the fiber propagation of the complex envelope of a DP optical signal is described by the following equations, as given by [16]:

$$\frac{\partial A_x}{\partial z} - j \frac{\beta_2}{2} \frac{\partial^2 A_x}{\partial t^2} + \frac{\alpha}{2} A_x = -j \gamma' \left(|A_x|^2 + |A_y|^2 \right) A_x \tag{A1}$$

$$\frac{\partial A_y}{\partial z} - j \frac{\beta_2}{2} \frac{\partial^2 A_y}{\partial t^2} + \frac{\alpha}{2} A_y = -j \gamma' \Big(|A_x|^2 + |A_y|^2 \Big) A_y \tag{A2}$$

where A_x and A_y denote the signal components in the two polarization states, while the sum $(|A_x|^2 + |A_y|^2)$ is the total signal power. The variables t and z denote the time and distance axes, respectively, α is the attenuation coefficient, β_2 is the group velocity dispersion parameter, $\gamma' = (8/9)\gamma$ is the effective nonlinear coefficient, and γ is the nonlinear coefficient [28]. According to [16], the solution of (A1) and (A2) can be expended into Volterra series transfer function (VSTF) kernels up to the 3rd-order as follows:

$$A_{x}(\omega, z) = H_{1}(\omega, z) A_{x}(\omega) + \int \int_{-\infty}^{\infty} H_{3}(\omega_{1}, \omega_{2}, \omega - \omega_{1} + \omega_{2}, z)$$

$$\times \left[A_{x}(\omega_{1}) A_{x}^{*}(\omega_{2}) + A_{y}(\omega_{1}) A_{y}^{*}(\omega_{2}) \right]$$

$$\times A_{x}(\omega - \omega_{1} + \omega_{2}) d\omega_{1} d\omega_{2}$$
(A3)

$$A_{y}(\omega, z) = H_{1}(\omega, z) A_{y}(\omega) + \int \int_{-\infty}^{\infty} H_{3}(\omega_{1}, \omega_{2}, \omega - \omega_{1} + \omega_{2}, z)$$

$$\times \left[A_{x}(\omega_{1}) A_{x}^{*}(\omega_{2}) + A_{y}(\omega_{1}) A_{y}^{*}(\omega_{2}) \right]$$

$$\times A_{y}(\omega - \omega_{1} + \omega_{2}) d\omega_{1} d\omega_{2}$$
(A4)

where ω is the angular frequency, $A_x(\omega,z)$ and $A_y(\omega,z)$ are the Fourier transforms of the signal components in the x and y polarization after distance z, while $A_x(\omega) = A_x(\omega,0)$ and $A_y(\omega) = A_y(\omega,0)$ are the optical signal spectra at the input of the fiber (i.e., z=0). In addition, $H_1(\omega,z)$ and $H_3(\omega_1,\omega_2,\omega-\omega_1+\omega_2)$ are the first- and third-order VSTF kernels, respectively. For an optically amplified transmission link with N spans, the mathematical expressions for the corresponding first- and third-order inverse VSTF (IVSTF) kernels are as follows [16]

$$K_1(\omega) = H_1^{-1}(\omega) = e^{\frac{j\omega^2 \beta_2 NL}{2}}$$
 (A5)

$$K_3(\omega_1, \omega_2, \omega - \omega_1 + \omega_2) \approx \frac{j\gamma'}{4\pi^2} \times \frac{1 - e^{-\alpha L}}{\alpha} K_1(\omega) \sum_{k=1}^N e^{jk\beta_2 L\Delta\Omega}$$
 (A6)

where $\Delta\Omega = (\omega_1 - \omega) \times (\omega_1 - \omega_2)$ is the spacing between the discrete frequencies in the sampled spectrum, L denotes the span length, and N is the total number of fiber spans. The last two equations (i.e., (A5) and (A6)) can be realized by the scheme shown in Figure 1a,b, respectively.

The operating principle of each nonlinear branch is divided into three stages and each polarization tributary passes through them (as described in Figure 1b). The first stage is the CD compensation through a filter with transfer function [16]

$$(K(\omega))^k = e^{\frac{j\omega^2\beta_2kL}{2}} \tag{A7}$$

where k = 1, ..., N indicates the number of the fiber span and $K(\omega) = e^{j\omega^2\beta_2kL}$ compensates the dispersion of each span. The second stage is the nonlinear compensation realized through the filter $K_{3,k}(\omega_1,\omega_2,\omega-\omega_1+\omega_2)$ with transfer function [16]

$$K_{3,k}(\omega_1,\omega_2,\omega-\omega_1+\omega_2) \approx \frac{j\gamma'}{4\pi^2} \times \frac{1-e^{-\alpha L}}{\alpha} K_1(\omega) e^{j\omega^2 \beta_2 L\Delta\Omega}$$
 (A8)

Finally, the third stage is used for the compensation of the residual dispersion through the filter $K(\omega)^{N-k}$ with transfer function [16]

$$(K(\omega))^{N-k} = e^{\frac{j\omega^2 \beta_2 (N-k)L}{2}} \tag{A9}$$

References

- 1. Essiambre, R.-J.; Kramer, G.; Winzer, P.J.; Foschini, G.J.; Goebel, B. Capacity limits of optical fiber networks. *J. Lightware Technol.* **2010**, *28*, 667–701. [CrossRef]
- 2. Temprana, E.; Myslivets, E.; Kuo, P.-P.; Liu, L.; Ataie, V.; Alic, N.; Radic, S. Overcoming Kerr-induced capacity limit in optical fiber transmission. *Science* **2015**, *384*, 1445–1448. [CrossRef] [PubMed]
- 3. Cartledge, J.C.; Ellis, A.D.; Shiner, A.I.; Abd EL-Raman, A.I.; McCarthy, M.E.; Reimer, M.; Borowie, A.; Kashi, A. Signal processing techniques for reducing the impact of fiber nonlinearities on system performance. In Proceedings of the Optical Fiber Communication Conference and Exhibition (OFC), Anaheim, CA, USA, 20–24 March 2016.
- 4. Liu, X.; Chaplyvy, R.; Winzer, P.J.; Tkach, R.W.; Chandrasekhar, S. Phase-conjugated twin waves for communication beyond the Kerr nonlinearity limit. *Nat. Photonics* **2013**, *7*, 560–568. [CrossRef]
- 5. Shiner, A.; Reimer, A.; Borowiec, A.; Oveis Gharan, S.; Gaubette, J.; Mehta, P.; Charlton, D.; Roberts, K.; O'Sullivan, M. Demonstration of an 8-dimensional format with reduced inter-channel nonlinearities in polarization multiplexed coherent systems. *Opt. Express* **2014**, 22, 20366–20374. [CrossRef] [PubMed]
- 6. Tao, Z.; Dou, L.; Yan, W.; Li, L.; Hoshida, T.; Rasmussen, J.C. Multiplier-free intrachannel nonlinearity compensation algorithm operating at symbol rate. *J. Lightware Technol.* **2011**, 29, 20366–20374. [CrossRef]
- 7. Liang, X.; Kumar, S. Multi-stage perturbation theory for compensating intra-channel nonlinear impairments in fiber-optic links. *Opt. Express* **2014**, 22, 29733–29745. [CrossRef] [PubMed]
- 8. Gao, Y.; Cartledge, J.C.; Karar, A.S.; Yam, S.S.-H.; O'Sullivan, M.; Laperle, C.; Borowiec, A.; Roberts, K. Reducing the complexity of perturbation based nonlinearity pre-compensation using symmetric EDC and pulse shaping. *Opt. Express* **2014**, *22*, 1209–1219. [CrossRef] [PubMed]
- 9. Ip, E.; Kahn, J.M. Compensation of dispersion and nonlinear impairments using digital backpropagation. *J. Lightware Technol.* **2008**, *26*, 3416–3425. [CrossRef]
- 10. Napoli, A.; Maalej, Z.; Kuschnerov, M.; Rafique, D.; Timmers, E.; Spinnler, B.; Rahman, T.; Coelho, L.D.; Hanik, N. Reduced complexity digital back-propagation methods for optical communication systems. *J. Lightware Technol.* **2014**, *32*, 3416–3425. [CrossRef]

11. Maher, R.; Lavery, D.; Millar, A.; Alvarado, A.; Parsons, K.; Killey, R.; Bayvel, P. Reach enhancement of 100% for a DP-64QAM super-channel using MC-DBP. In Proceedings of the Optical Fiber Communication Conference and Exhibition (OFC), Los Angeles, CA, USA, 22–26 March 2015.

- 12. Peddanarappagari, K.V.; Brandt-Pearce, M. Volterra series transfer function of single-mode fibers. *J. Lightware Technol.* **1997**, *15*, 2232–2241. [CrossRef]
- 13. Vannucci, A.; Serena, P.; Bononni, A. The RP method: A new tool for the iterative solution of the nonlinear Schrödinger equation. *J. Lightware Technol.* **2002**, 20, 1102–1112. [CrossRef]
- 14. Guiomar, F.P.; Reis, J.D.; Teixeira, A.L.; Pinto, A.N. Mitigation on intra-channel nonlinearities using a frequency-domain Volterra series equalizer. *Opt. Express* **2012**, *20*, 1360–1369. [CrossRef] [PubMed]
- 15. Guiomar, F.P.; Pinto, A.N. Simplified Volterra series nonlinear equalizer for polarization multiplexed coherent optical systems. *J. Lightware Technol.* **2013**, *31*, 3879–3891. [CrossRef]
- 16. Liu, L.; Li, L.; Huang, Y.; Cui, K.; Xiong, Q.; Hauske, F.N.; Xie, C.; Cai, Y. Intrachannel nonlinearity compensation by inverse Volterra series transfer function. *J. Lightware Technol.* **2012**, 21, 310–316. [CrossRef]
- 17. Giacoumidis, E.; Aldaya, I.; Jarajreh, M.A.; Tsokanos, A.; Le, S.T.; Farjady, F.; Jaouën, Y.; Ellis, A.D.; Doran, N.J. Volterra-based reconfigurable nonlinear equalizer for coherent OFDM. *IEEE Photonics Technol. Lett.* **2014**, 26, 1383–1386. [CrossRef]
- 18. Gagni, M.; Guiomar, F.P.; Wabnitz, S.; Pinto, A.N. Simplified high-order Volterra series transfer function for optical transmission links. *Opt. Express* **2017**, *25*, 2446–2459. [CrossRef] [PubMed]
- 19. Amari, A.; Dobre, O.A.; Venkatesan, R. Fifth-order Volterra based equalizer for fiber nonlinearity compensation in Nyquist WDM superchannel system. In Proceedings of the International Conference on Transparent Optical Networks (ICTON), Girona, Spain, 2–6 July 2017.
- 20. Klekamp, A.; Dischler, R.; Buchali, F. Transmission reach of optical OFDM superchannels with 10-600 Gb/s for transparent bit-rate adaptive networks. In Proceedings of the 37th European Conference and Exhibition on Optical Communication (ECOC), Geneva, Italy, 18–22 September 2011.
- 21. Qiu, M.; Zhuge, Q.; Changon, M.; Gao, Y.; Xu, X.; Morsy-Osman, M.; Plant, D.V. Digital subcarrier multiplexing for fiber nonlinearity mitigation in coherent optical communication system. *Opt. Express* **2014**, 22, 18770–18777. [CrossRef] [PubMed]
- Zhuge, Q.; Chatelain, B.; Plant, D.V. Comparison of Intra-Channel Nonlinearity Tolerance between Reduced-Guard-Interval CO-OFDM Systems and Nyquist Single Carrier Systems. In Proceedings of the Optical Fiber Communication Conference and Exposition (OFC/NFOEC), Los Angeles, CA, USA, 4–8 March 2012.
- 23. Bosco, G.; Carena, A.; Curri, V.; Poggiolini, P.; Forghieri, F. Performance Limits of Nyquist-WDM and CO-OFDM in High-Speed PM-QPSK Systems. *IEEE Photonics Technol. Lett.* **2010**, 22, 1129–1131. [CrossRef]
- 24. Ellis, A.D.; Al Khateeb, M.A.Z.; McCarthy, M.E. Impact of optical phase conjugation on the nonlinear Shannon limit. *J. Lightware Technol.* **2017**, *35*, 792–798. [CrossRef]
- 25. Pincemin, E.; Song, M.; Karaki, J.; Zia-Chahabi, O.; Guillosou, T.; Grot, D.; Thouenon, G.; Betoule, C.; Clavier, R.; Poudoulec, A.; et al. Multi-channel OFDM transmission at 100 Gbps with sub-channel optical switching. *J. Lightware Technol.* **2014**, *32*, 2202–2219. [CrossRef]
- 26. Savory, S.J. Digital filters for coherent optical receivers. Opt. Express 2008, 16, 804–817. [CrossRef] [PubMed]
- Wood, W.A.; Ten, S.; Roudas, I.; Sterlingov, P.M.; Kaliteevskiy, N.A.; Downie, J.D.; Rukosueva, M. Relative importance of optical fiber effective area and attenuation in span length optimization of ultra-long 100 Gbps PM-QPSK systems. In Proceedings of the SubOptic Conference, Paris, France, 22–25 April 2013.
- 28. Agrawal, G.P. *Fiber-Optic Communication System*, 3rd ed.; Wiley-Interscience: New York, NY, USA, 2002; pp. 64–65, ISBN 0471215716.



© 2018 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).