

**A 14-BIT PSEUDO-DIFFERENTIAL CURRENT-SOURCE  
RESISTOR-STRING HYBRID DIGITAL-TO-ANALOGUE  
(DAC) CONVERTER WITH LOW POWER  
CONSUMPTION**

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**by**

**CHANG HUI YI**

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## LIST OF SYMBOLS AND ABBREVIATIONS

DAC	Digital-to-Analog Converter
DNL	Differential Non-Linearity
INL	Integral Non-Linearity
LSB	Least Significant Bit
MSB	Most Significant Bit
LTSpice	Linear Technology Spice IV
PTM	Predictive Technology Model
KPA	Key Performance Aspects
dB	Decibel
CMOS	Complementary Metal Oxide Semiconductor
ADC	Analog-To-Digital Converter
THD	Total Harmonic Distortion
R-2R ladder	Resistor Ladder Network
HBT	Heterojunction Bipolar Transistor
SoC	System-on-Chip
W/L	Width-to-Length Ratio
Hz	Hertz
W	Watt
VDD	Supply Voltage
GND	Ground
PMOS	Positive Channel Metal Oxide Semiconductor
SNR	Signal-to-Noise Ratio

**SEBUAH 14-BIT PSEUDO-KEBEZAAN PUNCA-ARUS  
RENTETAN-PERINTANG HIBRID PENUKAR DIGITAL KEPADA  
ANALOG DENGAN PENGGUNAAN KUASA RENDAH**

**ABSTRAK**

Sebuah 14-bit hibrid penukar digital-kepada-analog (DAC) diperbuat dengan matlamat menggunakan kuasa rendah, tetapi mengekalkan keluaran resolusi tinggi dan ketepatan. Untuk mencapai matlamat tersebut, seni bina DAC berwajaran binari digunakan untuk 10 bit kepentingan paling rendah (LSB) dan pengekodan termometer digunakan untuk 4 bit kepentingan paling tinggi (MSB) supaya memaksimumkan kelebihan daripada kedua-dua seni bina. Seni bina DAC berwajaran binari digunakan oleh kerana sifat kesederhanaan dan kelinearan tetapi kos tinggi dan tidak praktikal untuk resolusi tinggi. Oleh itu, pengekodan thermometer yang mempunyai glic yang rendah dan boleh meningkatkan monotonicity reka bentuk tersebut digunakan. Selain itu, reka bentuk projek ini menggunakan sumber arus boleh suis untuk memacu input digital. Sumber arus boleh suis tersebut digunakan untuk memanipulasi gandaan arus untuk memastikan kuasa rendah reka bentuk. Reka bentuk tersebut menggunakan model ramalan teknologi (PTM) 45nm 1.1V CMOS teknologi. Projek ini disimulasikan dengan perisian LTSpice. Keputusan simulasi menunjukkan resolusi langkah halus  $43.981\mu\text{V}$  dan keperluan arus hanya  $11.967\mu\text{A}$  menyumbang kepada penggunaan kuasa yang sangat rendah sebanyak  $23\text{mW}$ . Reka bentuk tersebut sesuai kepada semua kerja yang serupa selain daripada DAC berwajaran binari yang menggunakan  $20\text{mW}$  dan mempunyai isu glitch.

**A 14-BIT PSEUDO-DIFFERENTIAL CURRENT-SOURCE  
RESISTOR-STRING HYBRID DIGITAL-TO-ANALOGUE (DAC)  
CONVERTER WITH LOW POWER CONSUMPTION**

**ABSTRACT**

A 14-bit Hybrid DAC circuit is created with the goal of being low power yet maintaining high resolution output and high accuracy. In order to achieve this, binary weighted DAC architecture is used for the 10 LSBs and thermometer coding is used for the 4 MSBs to leverage the advantages of both architectures. Binary Weighted architecture is used due to its simplicity and high linearity but it is too expensive and impractical for higher resolutions. Thermometer coding advantage lie in having very low glitch effect thus improving the monotonicity of the design. Furthermore, this design uses a switchable current source to drive the digital input. The switchable current source is used to manipulate the current gain to ensure a low power design. The design is using predictive technology model (PTM) 45nm 1.1V CMOS technology. It is being simulated using LTSpice software. Simulation Results show a fine resolution step value of 44  $\mu\text{V}$  and a requirement of only 12  $\mu\text{A}$  current supply which results in a very low power consumption of around 23mW. This is superior to all similar works except for binary-weighted current steering DAC which consumes 20mW yet suffers from serious glitch issues.

# CHAPTER 1

## INTRODUCTION

### 1.1 Background

Digital-to-analog converter (DAC) is a device that converts discrete bit values into their matching continuously variable values [1]. The inputs are digital values of 0's and 1's with its discrete amplitude and time instants, whereas the analog outputs can be in units of voltage or current [1]. Application of DAC can be easily found in most modern electronics, such as music players, disc players, satellite digital decoders, communication transmit channel and smart phone.

DAC is a fundamental application which covered the range from communication up to the medical application. The most common example of DAC is to make the music stored inside the player, which it is stored in digital bits, to be audible to the human ear. DAC is crucial for sound amplification, as most of the audio devices, be it amplifiers or speakers, can only deal with analog waveform [2].

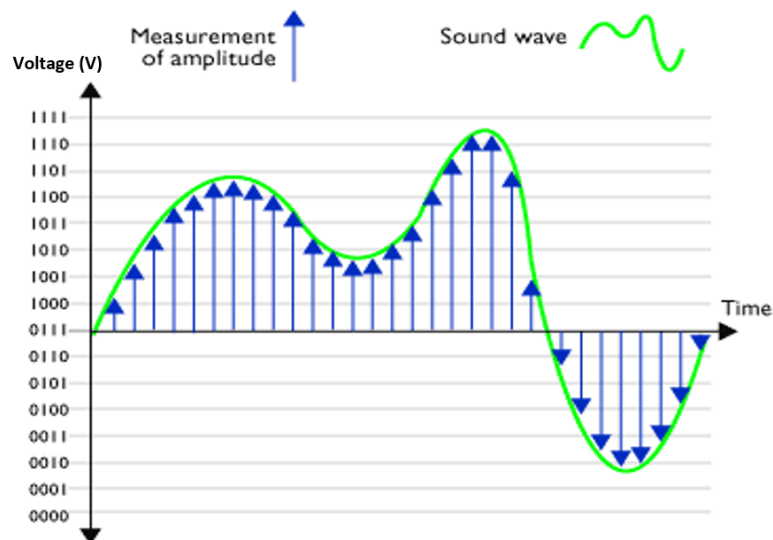


Figure 1.1: DAC transform the digital data into analog signal [3].

Figure 1.1 illustrates how a DAC transforms the digital data into analog signal. The blue arrows is the binary digital data, which has its own value in binary bits. These digital values form a sound wave, as represented by the green line, when joined together by the DAC. This explains the job of DAC, which is to reform the discrete digital values together into a continuous analog waveform. It is very crucial to have enough arrows for maximum representation of the shape, as well as having accurate dots. Horizontal X-axis represents sampling time intervals, whereas vertical Y-axis represents the amplitude of the digital value at that particular discrete time. The higher the number of dots on the X-axis, the better the DAC as it can join back more dots to represent better analog shape. Good DAC must also be able to sample accurate amplitude with minimal errors or glitch [3].

The need of a DAC comes from the necessity of storing analog voice signals, which has a history of almost 50 years ago. Back then, an analog signal is stored as a groove on a large black vinyl record. Signal inside is played on a player which has a needle which moves back and forth. This will create an electrical analog signal representing the stored sound [2]. In order to store music, the height of the analog signal is repeatedly sampled and measured over time. It is then stored in a series of discrete binary bits on memory of an audio device. These binary bits are digital audio signal. Digital music files are performed using the form of Pulse Code Modulation (PCM), and are created by sampling the amplitude of the analogue music signal at regular intervals. Digital audio data can be stored in different compression formats, sampling rates, encoding methods and word size [2].

From the above example, even gross over the years, the used of DAC still cannot be eliminate or replace with any other technology. However, a conventional DAC have its own weakness in term of resolution, accuracy, power consumption and many more when the number of bit of a DAC is increasing. As important as storing the digital audio



bits, DAC is needed to convert its binary form back to the original audio analog signal, as accurate as possible [2]. The device responsible for this conversion is none other than DAC [2]. Thus, an improvement on the conventional DAC become valuable. Hybrid DAC is the mixture creation based on the conventional DAC. The value of the hybrid DAC is it will minimize the weakness of each conventional DAC and give a desire outcomes when it is integrated into an application.

In the modern trend of the market, consumers are pampered with new technology and looking forward for a device integrated with DAC to have a high resolution and low power consumption. For the reasons given above, a hybrid DAC will definitely bring a benefit to the industry.

## **1.2 Problem Statement**

Power consumption and resolution in DAC go hand in hand as major issues focused by DAC designers. High power consumption of a circuit will leads to glitches and give the impact to the performance of a DAC in monotonicity and linearity, such as differential non-linearity (DNL) and integral non-linearity (INL). In another word, a low power consumption circuit will indirectly reduce the glitches. In order to achieve higher resolution of a DAC, number of bits  $N$  of a DAC is playing the most important role. Theoretically, when the number of bit is increasing, the voltage needed for the circuit will also increasing. In another words, low power consumption and higher resolution are opposed each other. As an answer to the arguments above, a 14-bits hybrid DAC is proposed because it leverage the both factors at a balanced point. Furthermore, 14-bits hybrid DAC is proposed because it still having market value due to some applications

such as music players, ultrasound communication transmit channel still need a 14-bits DAC, but not 13-bit nor 15-bits DAC.

A 14-bits hybrid DAC is having a bit depth of 16384 transition points. Amplitude or bit depth is simply refers to the resolution available to store the amplitude data. At this point, definitely there is an argument of using 16-bits or higher in order to achieve a better resolution. For a higher bit definitely will gives a higher resolution, but there is a limitation where the DAC with higher bit will give a higher signal-to-noise ratio (SNR) and impact the accuracy of the DAC.

Furthermore, especially in music players where it is the most common application for DAC, higher bit depth exceeded 14-bits will always sound the same to the human ears because there is a limit on the resolution that can be distinguish by human's ears. Additionally, the music players such as Apple have taken a step backwards in term of capacity because they realize that the higher bits with higher resolution with no audible improvement in quality is simply waste of resources.

After the consideration of the above factors, 14-bits hybrid DAC can give a golden balanced points that achieves the ultimate utilization of resources to produce profoundly high quality DAC in term of all aspects. Also, a hybrid type of DAC will minimize the limitations of each conventional DAC and better fixed the demands of the market. A good design is one that achieves the golden balance of utilizing the least resources to produce the highest quality of output.

### **1.3 Research Objectives**

The objectives of this project are:

1. To produce a 14-bit hybrid DAC with the architectures of binary-weighted resistor and thermometer coded in order to get the most advantages of each type of DAC.
2. To produce a low power consumption hybrid DAC.

### **1.4 Scope of Research**

The aim of the project is to produce a 14-bit hybrid DAC with the combination of advantages of each algorithm and minimize the weakness of each conventional DAC. This project is essentially an attempt to propose a low power consumption hybrid DAC with higher resolution. With the combinational effect of binary weighted resistor and thermometer coded in 10-bit least significant bit (LSB) and 4-bit most significant bit (MSB) respectively, this could optimize the performance and power consumption. This hybrid architecture is expected to achieve a high resolution and low power consumption.

The aforementioned hybrid DAC was implemented by using Linear Technology Spice IV (LTSpice) software. The hybrid DAC architecture is presented with the Predictive Technology Model (PTM) 45 nm 1.1V CMOS process technology. A 45 nm technology is chosen for this project due to the maturity of the tools and the model file available best fit the project. An appropriate technology used is one of the important factor to help in reduce the power consumption where the smaller the technology, the power needed by the transistors also will be lower.

Simulations are performed and verified with the LTSpice software. For ease of study and troubleshooting, the overall circuit is divided into a few blocks of circuit, such as voltage reference, digital decoder and many more. This architecture is expected to give

an output voltage within 1.1 V – 0 V. The supply voltage is 1.1V which is fixed in current design. Besides, when migrating from different technology, the transistor width to length ratio in the architecture will need to be redesign again.

## **1.5 Outline of Report**

This report will consist of five main chapters that explain the full details and specifications from the beginning to the conclusion of this project.

**Chapter 2** is about literature reviews on previous DAC architectures and techniques. The main sources of literature are from conference proceedings, engineering journals and online reliable resources. Each DAC architecture is discussed briefly in terms of reliability, speed, power consumption and glitch. Some hybrid DAC implementations are discussed in brief in their respective concepts and methods. The methods discussed here are compared and reviewed in their theoretical aspects.

**Chapter 3** describes the development of 14-bit hybrid DAC. The process flow, designs, and methods used to achieve the desired objectives are discussed in detail. The means to carry out the simulation and collecting data are also discussed in detail. In addition, the methods to evaluate the performance of the DAC are discussed in detail in plotting the relevant values in a detailed graph.

**Chapter 4** consists of tabulated data and analysis of the results of all simulations of the project. All simulation results of the low power driver hybrid DAC is evaluated and analyzed using a set of pre-determined data. The data consists of many types of signals to be fed into the hybrid DAC. In doing so, the performances of the hybrid DAC can be tested in the simulation against all possible scenarios.

**Chapter 5** summarizes the entire project whether the objective is fulfilled. A brief conclusion based on the observations and results is discussed here. Recommendations of any future work on this field are made here.

## **CHAPTER 2**

### **LITERATURE REVIEW**

#### **2.1 Overview**

DACs are used to convert the digital data sequence to analogue signal waveforms. Over the years, many conventional DAC architectures had been developed such as pulse-width modulator DAC, over-sampling DAC, weighted current-steering, resistor ladder network (R-2R ladder DAC), thermometer-coded DAC, and binary-weighted. Each of these conventional DAC architecture has its benefits, flaws, and limitations. Each of the conventional DAC differs in limitations in static and dynamic performance, including linearity, monotonicity and glitch energy. In view of the limitations inhibited by the conventional DACs, the hybrid DAC architecture is developed. This is to synergize and leverage most of the advantages and least of the disadvantages from the conventional DAC architectures.

This chapter will begin by explaining key performance aspects that are used to evaluate various DAC architectures. It will then discuss several of the past hybrid DAC proposed by previous researchers. All mentioned hybrid DACs are evaluated and compared in terms of power consumption, glitch analysis and conversion accuracy. This serves an important point to research their respective work to gain critical insights and knowledge to achieve the project objectives. Based from their researches, a better and more efficient DAC architecture system can be developed and implemented.

From the past researches, there are few techniques have been developed to tackle the various error sources in DAC. In the era of nanometer technology, any small changes in the physical factors can give a significant impact towards the performance of the device build. Thus, the hybrid DAC architecture is developed by using PTM. The predictive

model is used for circuit characterization by giving the first eyesight of the design build. This predictive model take in count every aspects such as the process variations, the technologies used and the physical correlations among model parameters to give out an accurate predict characteristics of nanoscale of complementary metal oxide semiconductor (CMOS) [4].

## **2.2 Key Performance Aspects**

There are various aspects that are used to evaluate the quality of design of a DAC which called as Key Performance aspects (KPA). These KPAs vary from one application to another. For example, to evaluate a DAC for audio applications, having a high resolution would be of paramount importance while having low power or being able to operate at high frequency has little importance. On the other hand, if a DAC is used for communication applications being able to operate at high frequency would be of utmost importance. Here is a list of the most important DAC KPA that will be discussed in this chapter.

### **2.2.1 Resolution**

The simplest KPA is the resolution of the DAC which can be easily represented by the number of bits of the digital input to the DAC. While it is true that the higher the number of bits the higher the resolution of the DAC, this always comes at the cost of increased area, circuit complexity and power consumption. Certain applications have no use of a very fine resolution. For example, power applications do not gain any advantages from having a fine resolution. DACs used in power applications are more concerned by

low error margins (INL & DNL) as they tend to control very high voltages so accuracy is of utmost importance.

### **2.2.2 Integral Non-Linearity and Differential Non-Linearity**

INL and DNL are the basic parameters used to judge the accuracy of DAC. INL is defined as the difference between the output voltages at step N versus the expected ideal output value of the reference line at that point. While the DNL is the difference between the actual increment height of transition N and the ideal increment value. Both of these values are the key component of measuring the accuracy of a DAC. Vishva et al [5] demonstrates the core difference between DNL and INL by comparing two simple yet very commonly used DAC architectures. Accuracy is very crucial for critical applications like power applications or various instrumentation control systems. Li et al [6] used a combination of tricks to manage to eliminate the bottle neck created by glitches due to non-linear distortions. This enabled them to create a design that can run at a 250 MS/s. This demonstrates the design advantages of a carefully designed hybrid DAC in overcoming INL and DNL limits.

### **2.2.3 Circuit Complexity**

Circuit complexity is indeed an important aspect of a DAC. There is no value gained of over designing a DAC for a certain application when a much simpler circuit has the ability to perform equally if well designed. The more complex a circuit the more area it requires and probably the higher power it will consume. That is why in some cases sacrificing other KPAs happens to simplify the circuit.



#### **2.2.4 Sampling Rate**

Sampling rate is an important aspect of producing fine output. It is a measurement of how fast a DAC respond to changing inputs. This is very important for telecommunication and high speed applications. Nonetheless, creating a DAC that can have a high sampling rate often faces serious bottle necks in the design such as increased glitch and increased power consumption. Many creative designs have managed to achieve high sampling rate. Zhang et al [7], approach which uses a 5 plus 9 segment PMOS managed to achieve a clock frequency of 2.5 GHZ and only 40 db noise at 1 GHZ.

#### **2.2.5 Area**

Nowadays with circuits being smaller and smaller and handheld devices being more and more powerful, circuit area matters significantly for DAC for applications involving small devices like hand phones and tablets. Moreover, industrial and military applications require powerful DACs to be fitted on minute devices and yet maintain very high accuracy and performance. As mentioned above, circuit area is well connected to circuit complexity, the lower the complexity, the smaller the area. Bringas et al [8] is a great example of how a good design could create powerful DAC with small area. They made a 10-bits DAC using a hybrid of current steering for the LSB thermometer coding for the MSB which created a design with great linearity yet using simple concepts and hence smaller area.

#### **2.2.6 Power**

Power dissipation of a DAC is crucial for applications where the DAC is going to be powered by battery or solar energy. It is very important for the DAC to consume less

power to be able to serve these applications. One topology that is known to be a good balance of power is thermometer coding which saves power even as an ADC as demonstrated by Ashwini et al [9].

## **2.3 Types of DAC**

In development over the decades, there are many types of DAC have been developed to meet the requirements of the endless application. In below segment discusses most usual type of DACs which can be used in hybrid architectures.

### **2.3.1 Pulse-Width Modulator DAC**

This is the lowest cost DAC. This DAC continuously switches a constant current or voltage over a period of time. The duration of switching is determined by the binary input code to the DAC. This type of DAC is mostly used in motor to control the speed, but it is also applicable in other applications.

### **2.3.2 Over-Sampling DAC**

Over-sampling DAC is based on interpolation. It means that this DAC converts digital bits into analog signals by employing a strategy of pulse density conversion. There are many advantages in going to this strategy. The main advantage is being able to minimize the low internal resolution effect. The DAC operates using Delta-Sigma Technology that encodes analog signals into digital signal by utilizing the same methodology used by an analog-to-digital converter (ADC). Moreover, it has the ability to transfer high bit-count low frequency digital signals into a lower bit-count with higher

frequency digital signals as part of the process to convert digital signals into analog which is an important part of a DAC. These features make Oversampling DAC ideal for very high resolution designs, for instance, those greater than 16 bits because of its high linearity yet low cost. Furthermore, quantization results in a further mitigation of noise as a result of the oversampling rate performance requirement of low-pass filter at the output. With delta-sigma method sampling rate up-to 100,000 sample/s a resolution of 24 bits can be obtained [1].

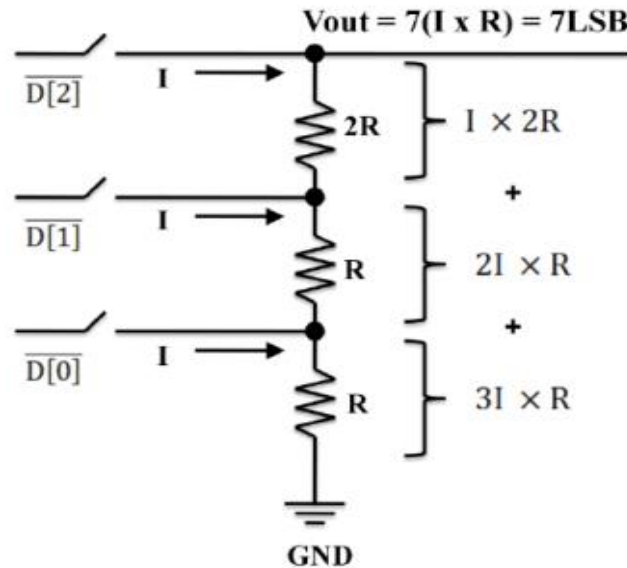
Normally, Oversampled DACs are the only solution for audio codecs, which require dynamic range in excess of 16 bit, total harmonic distortion or THD in excess of 80 dB. For this reason, audio cases are presented and studied in detail. Finally, the recent CMOS-scaled technologies perform at higher speed and thus the concepts of oversampled DACs have been recently applied to larger bandwidth devices, indicating a future increase in development of oversampled DACs [10].

### **2.3.3 Binary Weighted Resistor DAC**

Binary-weighted resistor is the easiest and simplest form of DAC. This DAC is made from resistors connected in a series topology. All resistors have the same resistance. Hence, the only way to control the resistance value is to manipulate the number of resistors being used. This means that as the digital signal increases, the resistance increase significantly. This approach is most suitable for low-resolution designs that have a small digital input value. It is very expensive and impractical to be used for high resolution inputs. This is because a higher the resolution of the input needs a higher resistance value. This translates to more resistors needed to be used and this requires a very large area [1]. Another disadvantage of using large resistance is that it results into a mismatch between

the transistors and hence will affect the linearity of the design. All factors considered, this DAC is most suitable for building up to 8-bit input DAC.

Figure 2.1 is an example for a 3-bit binary weighted resistor string DAC structure. This DAC is connected to a current source which use to control the input. To understand the operation of the resistor, consider the scenario with inputs being of low value. In that case, the current source will be turned ON and a fixed current,  $I$  which it will be conducted through the series of resistors. As the input bits value increase, resistance value should increase significantly [11].



**Figure 2.1: 3-bit binary-weighted resistor string [12].**

Based on Figure 2.1, the simplified 3-bit equation is [12]:

$$V_{out} = (2^2 \overline{D[2]} + 2^1 \overline{D[1]} + 2^0 \overline{D[0]})(I \times R) \quad (2.1)$$

According to Equation 2.1, current,  $I$  represents fixed current flow,  $R$  represent the LSB resistance,  $D$  is the bit of input.

### 2.3.3.1 R-2R Ladder DAC

Resistor ladder network also known as R-2R ladder DAC which is another type of binary-weighted DAC. The main unique feature is the repeated cascaded connection of T-resistor R and 2R. This feature results in higher precision as the production of equivalent matched resistors or current sources is much simpler. Moreover, the simplicity of this configuration means it is much cheaper to implement. It performs using cyclic ladder like the configuration of accurate resistor networks [1].

The functionality of this DAC can be explained as follows. A string of resistor ladder implements the non-repetitive reference network. The challenges associated with the large current ratio of a binary-weighted DAC are mitigated using R-2R resistor ladder where all current sources have identical values. This results in the fact that the current switch for each bit steers the same amount of current. The issue of current source mismatch as a result of the large current ratio is avoided. A block diagram is shown in Figure 2.2. In this setting, resistors generate the binary output levels. The best way to understand the functionality of this setting is by examining the Norton equivalent circuit of each stage [13]. For this topology, only a resistor ratio of 2:1 is required, hence further reducing the impact of mismatch. If only unit-sized resistors are used, the matching can be even further improved. To achieve the desired resolution, resistor process variation is ideal for imposing the minimum resistor width needed.

While R-2R architecture does have its advantages, the fact that only a fraction of the current is passed to the following stage means that a portion of the current is wasted in the resistor ladder. As the resolution of the DAC increases, the amount of wasted current increases and the efficiency decreases.

Besides from the obvious efficiency issues, this architecture also suffers from strong glitches resulting from any mismatch between the delays of the data signals to the current switches. In fact, the timing skew between the data lanes is the main factor that limits the sampling speed of the DAC [14]. A research showed that for a 6-bit 25 GS/s R-2R DAC, a timing skew of 3 ps results in a 5.8 LSB glitch when the MSB toggles. They designed two R-2R DACs: a 6-bit 32 GS/s DAC [15] and a 6-bit 28 GS/s DAC [16]. Different methods were applied to address timing skew. The 32 GS/s DAC uses only a half rate clock and performs double sampling of the data to relax the timing constraint. The 28 GS/s DAC uses a full rate clock and relies on matching the interconnect length to minimize timing skew between the data lanes. For a more recent version of their DAC at 60 GS/s, they used the same layout technique and demonstrated a clear four-level eye diagram at 60 GS/s [17]. All three DACs used InP heterojunction bipolar transistor (HBT) technology with  $f_T$  and  $f_{MAX}$  of 175 GHz and 260 GHz [15], respectively and much less loss, semi-insulating substrate than that of the commercially available CMOS processes.

Higher sampling frequencies exposes the drawback of timing skew between data lanes. With flip-flops, the data can be retimed before reaching the current switch. However, at higher frequencies, the timing margin of the flip-flop is reduced [14]. This simply means that suppressing the timing skew of the input data becomes very challenging.

As in the binary-weighted current DAC, the R-2R topology also does not require a thermometer decoder, which simplifies circuit design. Moreover, since the output current switches have the same size, the data buffers, retimes and clock buffers driving the current switches can be identical for all the lanes as well. This simplifies the clock tree design, which is the highest frequency block in the system [18].

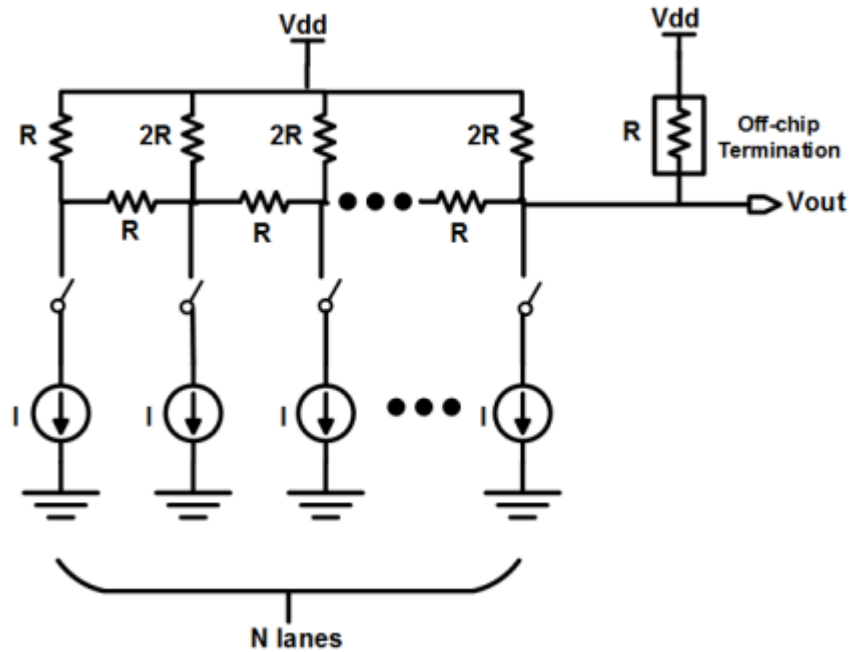


Figure 2.2: R-2R ladder DAC [18].

### 2.3.4 Current Steering DAC

The current-steering DAC is implemented by manipulate the current value which has a significant advantage on high speed design. Normally, the input bits of the DAC is connected to switchable current-sources. The main advantage of the current-steering possess is that it is significantly faster that then voltage switches approach. This is explained by the fact that referenced current is not interrupted and significant voltage will be visible only at the output but not across the switches [12]. Another benefit of this approach is that a decoder is not required and hence it has a much lower circuit complexity with faster operating speed [19]. However, the negative aspects of this approach are mainly having a limitation on static and dynamic performance. This can be accounted to current mismatch, process variation and glitch energy.

### 2.3.4.1 Binary Weighted Current DAC

This DAC is formed by using weighted current sources which are joined to a switch that is manipulated by the digital inputs [19]. There are many advantages of using this approach. Firstly, it is power efficient and it takes up small area. Secondly, no decoder is required which reduces circuit complexity significantly and allows it to operate at higher speeds [20]. Therefore, the current-steering switching method performs much faster than the voltage-switching mechanism. Nonetheless, this setting suffers from poor performance in the special case of all switches transit the state simultaneously [12]. In addition to that, the current-steering DAC also has limitations in dynamic performance, such as glitch energies and current mismatch due to process variation.

A simplified circuit diagram of a binary-weighted DAC is shown in Figure 2.3. Input binary codes switch the binary-weighted current sources to a 50  $\Omega$  on-chip load resistor and a 50  $\Omega$  off-chip termination resistor to generate the analog voltage output. For high speed DACs, a 50  $\Omega$  output impedance is necessary to match with the input termination of the measurement equipment, such as an oscilloscope or spectrum analyzer. It is important to have proper termination for high speed DACs to avoid signal degradation. From the diagram, the obvious advantage of this architecture is that it only requires N current sources for an N-bit DAC. This can result in area and power savings by having fewer data lanes, which reduces the number of buffers necessary to drive them. This is very important for high speed DACs, because smaller area means smaller footprint and less layout parasitic capacitance to drive. As the conversion rate of the DAC increases, the bandwidth of the DAC becomes increasingly limited by the interconnect capacitance. Example of DACs using binary-weighted current sources include a 6-bit, 20 GS/s DAC [21].

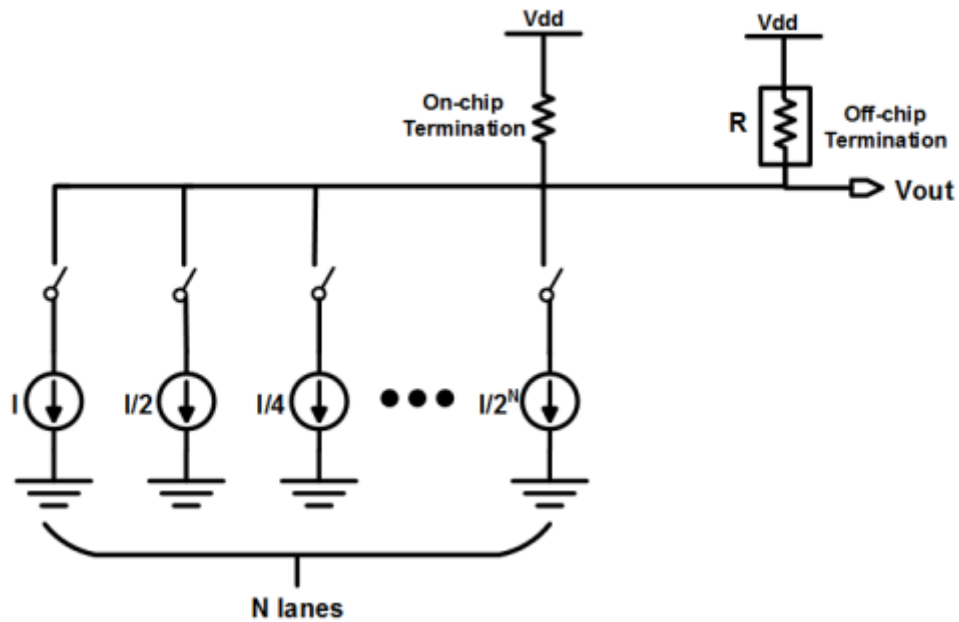


When it comes to area and power savings, they are somewhat limited because the current switches need to be scaled with the current to ensure the transistors are biased at peak  $f_T$  current density. As a result, all the buffers driving the current switches also need to be scaled appropriately. This architecture is demanding in terms of device matching to achieve high resolution. Sometimes, in order to reduce mismatch of the current sources caused by the large ratio, it is desirable to use unit-sized current sources. This results in an increase of the area of the DAC.

Having a large current ratio negatively impacts the dynamic performance of the DAC. One of the researcher's design [21], scaled buffers were used to drive the weighted current sources. However, in order to save power, scaling was done such that there was still a fan-out difference of 4:1 between the MSB and LSB. As a result, MSB lanes driving a large load will have more delay, which will cause glitches at the DAC output. The researcher[21] compensated for this delay by retiming the MSB earlier than the LSB. Also, to further reduce the current ratio, they applied the LSB current to a  $25 \Omega$  load, whereas the rest of the binary currents go to a  $50 \Omega$  load.

There are two disadvantages of a binary-weighted DAC that plague all DACs not using thermometer decoding. The DAC may not be monotonic. A monotonic DAC is the one where the output always increases with increasing input code [22]. The other disadvantage is that the DAC may suffer from large glitch energy when the MSB toggles, for example, when the code changes from 1000 to 0111 for a 4-bit DAC. This problem is especially pronounced for high speed DACs, because the duration of the bit period can be too short for the glitch to settle within one bit period. Hence, it is important to align the digital bits to reduce the glitch energy as much as possible.

The main advantage of the binary-weighted DAC is its simplicity. It does not require thermometer decoder, which can be challenging to design at very high speed with low power. Some designs have taken advantage of this fact while minimizing the impact of the glitches by using binary-weighted currents for the LSBs only [23].



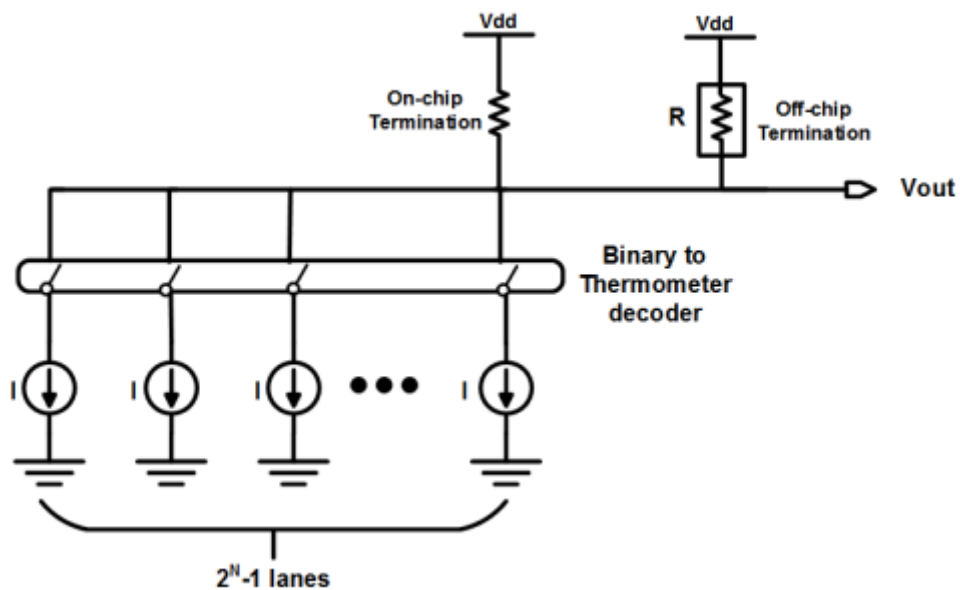
**Figure 2.3: Binary-weighted current DAC [18].**

### 2.3.4.2 Thermometer Coding DAC

This DAC consists of a decoding circuit of binary to thermometer codes. For N-bit of DAC needs  $2^N - 1$  current source. As the digital code increases by one, the thermometer decoded bits switch one more current source to the output. All the current sources have the same current, so the current switches and the circuit driving the current switches are also identical [18]. Each of the current source is used in controlling the current flow through the DAC. The digital signal must be translated into the corresponding thermometer code, which is consisting  $2^N - 1$  bits in thermometer code

for N-bit of the digital inputs. This decoder will convert into  $2^N - 1$  bits in thermometer code for any N-bit of binary inputs. For example, for a 4 bits DAC, it will have 15 segments.

Figure 2.4 shows the thermometer coded DAC. This kind of DAC architecture has the minimum glitch effect. Hence, it has significantly better DNL, and glitch and monotonicity performances as compared to other DAC architectures. However, this high precision DAC architecture needs a high cost to build due to its encoding circuits needed. It is more preferable in low resolution cases since the encoding circuit in high resolution cases could be very large as the binary input bits is increasing [24].



**Figure 2.4: Thermometer code based current DAC [18].**

## **2.4 Hybrid DAC Architecture System**

Hybrid DAC architecture is composed by integrating two or more type of conventional DAC architectures as mentioned at section 2.2. In most integrated devices where DACs are used, hybrid DAC is more preferred. This is because to provide a balance among cost, speed and precision. To achieve this balance, using only any one of the techniques mentioned above is very challenging.

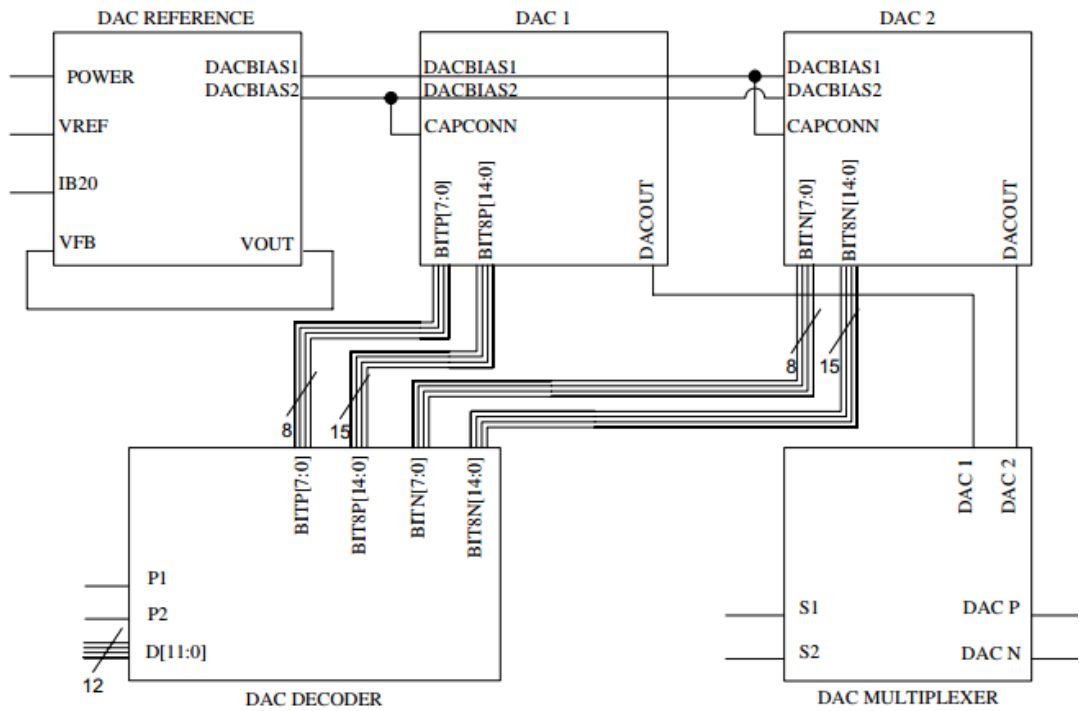
It has to be pointed that the segmented DACs is special kind of hybrid DAC which combines two principles. While for the most significant bits it employs the thermometer-coded principle, and for the least significant bits, it utilizes the binary-weighted principle. Via this hybrid methodology, a tradeoff is achieved in between the precision of the DAC and the number of current sources required by the DAC.

### **2.4.1 12-Bit Pseudo-Differential Hybrid DAC**

Figure 2.5 shows the overall block diagram of a 12-bit pseudo-differential hybrid DAC. Referring to a researcher [12], this hybrid DAC consists of three conventional DACs, which are thermometer coding DAC, binary-weighted resistor DAC, and weighted current-steering DAC.

This hybrid DAC utilized the advantages of these three DAC. To start, the binary weighted resistor DAC is used to represent 8 LSBs. On the other hand, the thermometer coding scheme is used to represent 4 MSBs. Other than that, to provide current to follow through the resistors topology layout, this configuration uses current-steering as a switchable current source. As essential cell in the hybrid DAC architecture, this is used to generate current to the resistors. Based on all of that, the 12-bit pseudo-differential hybrid DAC has compelling advantages across different segments. For example, it has

better DNL and INL, along with a reduced overall area and lower circuit complexity [12]. The hybrid DAC configuration is quite compact. It is possible to be utilized at numerous mixed signal designs or system on chip (SoC) implementation.



**Figure 2.5: 12-bit pseudo-differential hybrid DAC architecture [12].**

Referring to Figure 2.5, it is clearly shows that DAC reference block is the core to the overall design as it provides constant bias voltages to two DAC blocks. The DAC Decoder decodes the 12-bit binary input into an appropriate code for both DACs simultaneously. It then splits 8-bit binary-weighted resistor string in LSB section and 4-bit to 15-bit of thermometer coding decoder in MSB section. A DAC blocks are composed by switchable current sources and resistor string circuit as the essential cell in DAC block, three PMOS transistors are used to create the switchable current source with different width-to-length ratio (W/L). It is used to supply the resistor string with a fixed current

when it is switched on. Each of the block or elements used in this hybrid DAC will have more discussion in section below.

### 2.4.1.1 Switchable Current Source

Figure 2.6 clearly shows the structure of the switchable current source that is created using three PMOS transistors. Its operation is dependent on the voltage level of the input at gate of M3. High voltage at M3 turns the transistor off, which in return switch on the current source. This will make a fixed value of current flows to IOU<sub>T</sub> through transistor M2. If a low voltage be applied at M3, the current source is switched off. In this case, M3 will be supplied by a fixed current from the transistor M1 to the ground, instead of IOU<sub>T</sub>. The fourth terminal of the PMOS transistors is tied to VDD is connected to the fourth terminal of the PMOS transistors [12].

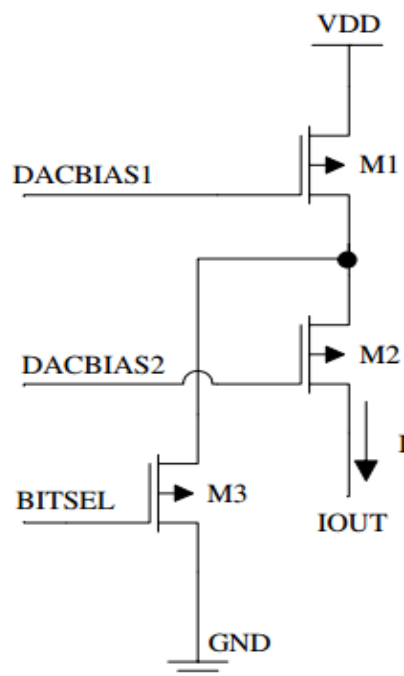


Figure 2.6: Switchable current source [12].