

1 Regularity and optimisation practice in steel structural 2 frames in real design cases

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7 Abstract

8 Large amounts of energy and carbon are embodied in the frames of buildings, making
9 efficient structural design a key aspect of reducing the carbon footprint of buildings.
10 Similarly to a previous study which analysed real structures had observed that the
11 unused mass of steel framed building could amount to nearly 46 % of the total mass
12 due to over-specification of the sections, we find a value of 36 %. We observe that this
13 value correlates with the design method, with software-aided design bringing significant
14 improvements and with the design stage, where most of the optimisation seem to occur
15 between the preliminary and tender stage.

We find that neither the regularity of the structure nor the cost, independent of the
measure used, correlate with the mean utilisation ratio (UR). Conversely, we observe an
apparent reluctance to design beams above a 0.8 capacity UR. This reluctance explains
most of the unused mass in buildings. The rest of unused mass consists in cores,
trimmers and ties (6 %), some of which bear loads not captured in this analysis but are
otherwise necessary for stability reasons, and in edge secondary beams (3 %) which
design is constrained, and should not necessarily be considered as ‘unused’ mass.

16 *Keywords:* Efficiency, Design, Steel frames, Optimisation, Design practice, Regularity

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17 **1. Introduction**

18 The efficiency of many technical systems in common use are reaching their theoretic-
19 cal efficiency limits. This is notably the case of buildings which can now be designed
20 to be operationally carbon neutral as they operate (Cotterell and Dadeby 2012). How-
21 ever, the growing needs for construction has an impact through the carbon and energy
22 embodied in the buildings, notably the frames. With the threat of global warming, new
23 objectives (Rhodes 2016) have been established for developed and developing countries
24 for carbon release. Further improvement of the operational performance aspects of new
25 buildings cannot help significantly to reach the targets. There is therefore a pressing
26 need to find new ways to reduce embodied carbon.

27 This is a particular concern as the embodied carbon in buildings can represent as
28 much as 70 % of the whole life carbon of the building (Dimoudi and Tompa 2008,
29 Nadoushani and Akbarnezhad 2015) for warehouses and sheds, and can still reach 30 %
30 in office buildings. The strategies for the reduction of this embodied carbon are different
31 depending on the material used for the frame: concrete, steel or timber. The choice of
32 material for the building frame depends amongst other considerations on the function
33 of the building and the economic constraints associated with its construction. Lowered
34 carbon footprint of concrete-framed building requires finding new supplementary ce-
35 mentitious materials, as the current production of slag and fly ash is fully exploited, or
36 of insufficient quality (Snellings 2016). In the case of steel-framed buildings, improve-
37 ments in the energy and carbon efficiency of the steel production process are unlikely as
38 they are already close to their limit (Cullen et al. 2012). In this work, we focus on the
39 design of the structural frame of steel-framed buildings.

40 A different approach to lowering the carbon footprint of buildings is to improve the
41 structural design. Strategies for efficient design of buildings depends on the choice of the
42 structural system. This is a complicated decision which depends on the capabilities of the
43 design firms, the norms and codes (including seismic), the time allotted, the budget and

44 the preferences of the client. Therefore, although it is not feasible to assess the quality of
45 a design in terms of the fundamental choices made, it is possible to measure how closely
46 the specifics of the design match an ideal, figured by an exact adherence to the code. In
47 this work, therefore, we do not assess the design itself. The codes themselves can affect
48 the absolute efficiency of the design. Modern codes such as the Eurocode define limit
49 states for elements instead of working stresses. This paradigm is much more efficient
50 than the working stress design methods used previously, for example, the change in the
51 Canadian code resulted in structures which were 15 % lighter (Kennedy 1984). The
52 Eurocode, in its latest iteration, is one of the most advanced codes, introducing provisions
53 for plastic design — which is uncommon — but also has small safety factors. Some of
54 the provisions on plastic design were already found in the British Standard. With respect
55 to the safety factors, the reliability of steel elements has been well established over a
56 century of experience and improvements (Byfield 1996). Therefore, the ideal structure
57 following the Eurocode is also quite close to a ‘optimal’ structure making maximum
58 use of the materials whilst still being extremely safe. Although the design of efficient
59 structural systems, notably using plastic provisions, is a complex topic — portal frame
60 structures are usually very efficient structures — it is possible to study how *optimised*
61 a structure is. For a given topology of beams and columns, with the loads specified, it
62 is possible to establish the lightest elements required to build the structure according
63 to the code. The choice of connexions, whether nominally pinned or moment bearing
64 affects the overall efficiency of the design, *but has no bearing on how optimised it is*.
65 Optimum design according to codes has been studied since computer modelling became
66 possible (Saka 1990).

67 Despite structures built exactly to the code being safe, the engineers seem to fre-
68 quently design well within the limits of the code. A previous study by Moynihan and
69 Allwood (Moynihan and Allwood 2014) analysed 79 steel-framed buildings, and the
70 utilisation ratios of all beams and columns were collected. They concluded that 46 %

71 of the steel mass in beams and columns is not load bearing. They have suggested a
72 number of factors which can explain this: rationalisation, *i.e.* using the same section
73 across the building frame, chosen to match the highest requirements; elements from
74 older buildings designed with pen-and-paper are not optimised because this process
75 would have been too time-consuming; UK universal beams and sections cannot satisfy
76 requirements exactly — nonetheless, many fabricated elements were found to have
77 relatively low utilisation ratios where section properties could be allocated to suit the
78 structural performance. In general, this ground-breaking study both identified a great
79 potential for savings and opened questions relating to the design process which led to
80 this performance gap.

81 As the Moynihan and Allwood study was the first of its type, we have followed a
82 similar methodology, but with a more detailed analysis of design approach. We collected
83 detailed information on the roles of elements, as well as the limiting factor of the design
84 of each beam, the floor type and the design methodology for each project. The objective
85 was to identify the design practices and goals which explain the UR but with a more
86 detailed analysis of design approach and the underlying causes of the observations.

87 **2. Materials and methods**

88 We have analysed the floor plates (excluding supporting columns) of 30 buildings,
89 27 ‘real’ at various stages of the design process and 3 ‘model’ buildings found in design
90 handbooks (Table 1). The beams represent about two-thirds of the mass of a typical steel
91 frame. These steel-framed buildings are office/commercial or educational buildings. For
92 each floor design, the details every beam for which we were able to gather sufficient
93 information for was recorded. Their type, length, mass, and connection types were
94 noted. Fabrication details such as the presence of cells in the web or the application of
95 a pre-camber were also noted. Each beam role is also noted as being either a primary,
96 secondary or a core/trimmer/tie. Edge beams are marked as such.

97 The case studies cover both traditional pen-and-paper (labelled ‘None’) and computer-

Table 1: Overview of the case studies. Sectors are Commercial (C), Education (E), and Model (M). Floor systems are Trapezoidal (T), Pre-cast Decking (P) and Re-entrant decking (D). All case studies are from the UK.

#	Year	Stage	Storeys & Height	Model	System		
1	C	2005	As Built	13	50.0	None	T
2	C	2009	Tender	17	66.0	None	R
3	C	2006	Construction	5	17.5	None	P
4	C	2013	Construction	3	12.0	None	R
5	C	2010	Construction	6	21.8	None	R
6	C	2008	Construction	3	11.0	None	R
7	C	2016	Preliminary	10	45.0	Unknown	T
8	C	2006	Construction	5	23.3	None	T
9	C	2001	Construction	3	11.4	None	T
10	E	2016	As Built	3	11.8	Full Frame	P
11	E	2017	Preliminary	2	8.0	Full Frame	P
12	E	2017	Tender	2	9.0	Full Frame	P
13	E	2012	Construction	3	11.6	Full Frame	T
14	E	2016	Construction	2	7.7	Full Frame	R
15	E	2006	Construction	3	9.3	None	P
16	E	2013	Construction	2	7.6	Full Frame	T
17	E	2005	Construction	3	11.2	None	R
18	E	2013	Tender	5	11.2	None	R
19	E	2016	Construction	2	6.3	Full Frame	T
20	E	2014	Construction	3	12.6	Full Frame	T
21	E	2013	Construction	3	11.6	Full Frame	T
22	E	2014	Construction	2	8.7	None	P
23	E	2016	Tender	3	11.4	Full Frame	T
24	C	2014	Construction	1	5.9	Unknown	T
25	C	2016	Tender	13	54.9	Unknown	R
26	E	2018	Tender	4	17.2	Full Frame	T
27	C	2016	Construction	2	5.7	None	P
28	M	—	—	8	26.8	Floor Plate	T
29	M	—	—	8	26.8	Floor Plate	T
30	M	—	—	8	26.8	Floor Plate	T

⁹⁸ aided optimisation (marked 'Full Frame') design methods, and different slab forms of
⁹⁹ construction: pre-cast, and composite metal deck both trapezoidal and re-entrant.

100 *2.1. Evaluation of the UR in the case studies*

101 Each floor beam has been recalculated using the CSC Fastrak software(CSC ????)
102 according to the known design loads of the structures. The original digital plans were
103 used when available, otherwise, they were redrawn. The software gives the utilisation
104 ratios according to the bending moment, the deflection, the natural frequency, and the
105 shear forces. The dominating UR of the beam is the largest of these four, which is
106 deemed limiting. Based on this information, it is possible to measure the approximate
107 over-design of each beam and the corresponding mass. It is also possible to relate the
108 dominating UR to geometric and functional information. The role of parameters such
109 as type of decking, design method (computer modelling or pen-and-paper) can then be
110 related to the overall design.

111 The plans for all the case studies were entered in the software manually. The beams
112 were re-calculated according to the standard which was used at the time, either the
113 British Standard BS-5950 or the Eurocode EC3. However, as most of the design is
114 dominated by bending, deflection or natural frequency, the results presented here are
115 independent of the standard chosen as the formulas used in the British standard and
116 Eurocode for these criteria are identical.

117 To ensure consistency, the following starting assumptions and restrictions apply:

- 118 1. The modelling was restricted to a single floor plate of each building, as opposed
119 to a full frame analysis. Modelling a full frame would require many more assump-
120 tions to be made involving wind loading and stability systems, and would take
121 significantly longer. By analysing a single plate only the vertical loads need to be
122 established, which can generally be easily extracted from the design information.
123 Any members determined to be part of the lateral stability system (such as in
124 braced bays) have been omitted from the data collection, as have any members
125 that form part of a portal frame. This decision also enables us to directly compare
126 efficiencies between buildings with different numbers of stories.

- 127 2. Whilst gravity loads for the general floor finishes (Super-Imposed Dead/SDL) and
128 the imposed loads were generally easily available, loads for cladding were a lot
129 more difficult to determine in some cases. Where specific loads have been given
130 these have been applied, and for retained façade projects cladding loads have
131 been ignored. In all other cases beams have either been omitted from the data
132 collection, or beams were marked as edge beams.
- 133 3. Similarly, any beams that only take load from stairs and lifts have been omitted,
134 or if included marked as core members.
- 135 4. Any ‘unusual’ beams were also omitted from the study. This included any curved
136 members, angle sections or tapered beams. PFC sections were generally omitted if
137 they formed trimmers only, but included where they formed load bearing beams.
138 Hollow sections were only included if it was known that they weren’t designed to
139 resist torsion — generally torsion resisting beams were omitted.
- 140 5. Transfer beams with incoming point loads were omitted, unless coming from an
141 existing model. This is due to the difficulty in accurately determining the loads
142 imparted onto the beam.

143 Care was taken to account as much as possible for the constrains which come from
144 the construction stage.

- 145 1. Overall frame stability — steel frames are often inherently unstable during
146 construction, until all vertical and horizontal bracing and any diaphragm floors are
147 in place. However this is standard in the UK across all (normal) jobs, and the
148 practice is for the fabricator/erector to provide additional temporary bracing based
149 on their construction sequence. This rarely affects final steel sizes and hence was
150 not considered.
- 151 2. Composite beams — Composite beams are unable to achieve their full increased
152 capacity until the concrete has adequately cured. Because of this, they need to be
153 checked for a construction load case, where they are expected to take the weight of

154 the wet concrete plus a nominal construction live load under their ‘plain’ section
155 condition. This is a feature built into the Tekla/Fastrak software, and therefore
156 has been taken into account in the analysis.

157 3. Precast planks — The stability of the beams can be affected depending on the
158 plank installation sequence. Where a beam supports two sets of planks, the centre
159 of mass of each will be offset from the centroid — therefore if the planks are
160 installed entirely along one side before the other you end up with a torsion in the
161 beam that needs to be accounted for. It is impossible to know without having
162 worked on these projects whether this was an issue. However any redesign of
163 beams for the temporary condition would generally be the responsibility of the
164 contractor, and would thus not appear in our analysis.

165 A key question to evaluate the design is the regularity of design: small buildings
166 with simple shapes can have a very high mean utilisation ratio: in the data set the case
167 study 1 has an mean UR close to 1 with almost no dispersion. It is however an outlier in a
168 number of respects: it is both very small and very simple. Therefore, the optimal design
169 for that building offers no scope for rationalisation trade-offs. In general, a measure of
170 the regularity of each design should be related to its mean UR.

171 2.2. *Regularity measure*

172 A hypothesis for the underutilisation of the elements is that rationalisation induces
173 a mismatch between the constraints and the range of available section profiles. Ra-
174 tionalisation is the use of a reduced set of profiles dimensioned to match the stricter
175 design constraints rather than a more extensive set of profiles, tuned to the full range of
176 constraints. Under this hypothesis, the more regular a building is, the lower the effect of
177 rationalisation: the constraints being effectively similar, the same profile can be optimal
178 for a larger number of beams. The converse, which is that a wide spread of constraints
179 in the structure satisfied by a reduced set of sections results in low UR is obvious.

180 Therefore, to show that rationalisation could be occurring in the case studies, more

181 complex buildings should be have lower UR, *independently* of the number of sections
182 they use for their section size.

183 Regularity is a difficult thing to measure. To have a more robust analysis, we have
184 used a number of measures for regularity. The first one (top five measure) was used
185 in the original study by Moynihan and Allwood: the fraction of the total mass taken
186 by the five most common elements. The second (Pseudo-Gini) is an extension of this
187 idea, inspired by the Gini coefficient (Milanovic 1997). Third is the Shannon index
188 which is a measure of diversity rather than regularity: a more diverse profile selection
189 could indicate a less regular building. Finally, we have used a measure of Kolmogorov
190 complexity (Kolmogorov 1968) on simplified descriptions of the design. All these
191 measures describe the relative roles of frequent and rare sections in the structure. They
192 are not direct regularity measures of structure geometry, but rather assume that the
193 distribution of section types reflects the regularity of the design. The Kolmogorov
194 measure comes closest to a real measure of the complexity of the assembly.

195 There may not be a completely satisfactory measure of the regularity of a design.
196 Nonetheless, if none of the proposed measures correlates with the UR, we can conclude
197 that in all likelihood, regularity and thus rationalisation is not a significant factor in the
198 efficiency of a design.

199 2.2.1. Top five measure

This measure has the benefit of being simple: it is the fraction of the total mass of a given case study taken by the five most common sections. The disadvantage is that it favours considerably smaller structures built with fewer section types. n is the number of section types:

$$I_5 = \frac{\sum_{i=1}^5 m_i}{\sum_i m_i} \quad (1)$$

200 This method also implies that the fabrication process is cheaper when the number

201 of sections is reduced. In turn, this assumes that retooling is expensive. In reality, the
202 operations of large fabricators are heavily automatised and the time needed to produce
203 any section reflects more the complexity of the links and cells which may require human
204 intervention. Retooling operations represent negligible amounts of time: The machines
205 are multi-tool, and beams spend most of their time moving on the floor of the workshop
206 going from post to post, and not being machined. Nonetheless, small savings are possible
207 when purchasing stock steel in bulk, and smaller fabricators are less well equipped. This
208 approach can be extended to be independent of the total number of sections used in a
209 construction.

210 2.2.2. *Pseudo-Gini*

211 The following approach extends the top five measure by replacing the arbitrary
212 cut-off of 5 with a measure of the distribution of mass. A real Gini index measure would
213 use the covariance of the section mass with respect to its rank. The measure proposed
214 here is an approximation of the Gini coefficient: they are both measures of the skewness
215 of cumulative curves related to a linear model.

A perfectly irregular design would have its mass equally distributed among all the
beam section it uses, whereas a regular design would have nearly all its mass in only a
few sections. Therefore comparing the cumulative mass of the sections with the uniform
solution is a measure of the regularity of the design. using m_i the total mass of section
type i , and n the number of different sections. This index is computed as:

$$I_G = \sum_i^n \frac{i}{n} - \frac{m_i}{\sum_i^n m_i} \quad (2)$$

216 This measure is not as biased against heavier structures, but it gives a regularity of 0
217 rather than one for a structure built with a single element type, which is an unexpected
218 behaviour. Indeed, a structure built with a single element type may be either perfectly
219 regular or perfectly irregular depending on how its elements are assembled.

220 2.2.3. *Shannon index*

The Shannon index is an information-theoretic measure of diversity. It is used commonly to measure the richness of ecosystems, in this case, it measures the richness of the section selection. Small number of sections representing a large fraction of the total mass of steel may indicate a more rationalised construction. The total mass fraction for each section type i is $\frac{m_i}{\sum m_i}$. The Shannon index of a case study I_S is

$$I_S = - \sum_i^n \frac{m_i}{\sum_i^n m_i} \log(m_i) \quad (3)$$

This is a measure of diversity rather than regularity, and thus is in general larger when the number of section types grows. To use it as a regularity measure, we have renormalised the results:

$$I_S^{\text{renorm}} = 1 - \frac{I_S - \min I_S}{\max I_S - \min I_S} \quad (4)$$

221 2.2.4. *Kolmogorov complexity*

222 The Kolmogorov complexity was introduced as a measure of regularity. It is defined
223 as the size of the smallest programme which can reproduce a dataset, typically encoded
224 in binary. For example, a very simple dataset, containing only '0' repeated a given
225 number of time can be produced by a very small programme, while a very complex
226 dataset requires a much larger programme to generate.

227 The Kolmogorov complexity was measured by compressing text files containing:

- 228 • the case study number
- 229 • the type of floor
- 230 • their mass
- 231 • the steel grade
- 232 • the type of section (if UK universal beam or column), else n/a

29 → Steel Braced → 60.9 → S355 → 457 x 191 x 82 → n/a → 7.5 → Edge
Primary → Pin/Pin → No → No

Figure 1: typical line of the file describing the sections. → mark tabulations separating the columns.

- 233 • the type of section (if fabricated), else n/a
- 234 • their length
- 235 • their function
- 236 • their boundary conditions
- 237 • whether they are pre-cambered
- 238 • whether they have cells in their web

239 Taken together, these form a ‘bill of materials’ which describes the case studies. The
240 files were UTF-8 encoded, and the programme bzip2 version 1.0.6 was used for the
241 compression. An example line of such a file is given as figure 1. The compressed file
242 sizes were reported in 8 bit bytes using the command ‘ls -l’. This value was used as
243 the Kolmogorov complexity I_K .

The encoding is not perfect, and a binary representation may have been preferable.
However, the initial size of the file is small, and a binary encoding may not have left
significant possibilities for further compression, reducing the sensitivity of the approach.
To use as a regularity measure, we have renormalised the results:

$$I_K^{\text{renorm}} = 1 - \frac{I_K - \min I_K}{\max I_K - \min I_K} \quad (5)$$

244 3. Results

245 3.1. Utilisation ratio overview

246 A representation of all beams analysed per project and per role is seen on Figure 2.
247 This figure shows the large spread both between and within projects. The distribution of
248 primary and secondary beams depends on the specific layout of each floor. Groups of

249 points extending horizontally usually indicate a single section type used repeatedly in
250 the same configuration.

251 The secondary beams make up the largest fraction of beams. Assuming a typical
252 rectilinear floor plate this makes sense, as they will be the beam most often used to span
253 over the typical bay width. These beams will often also be the ones designed first by the
254 engineer, as not only do they make up the greatest number of beams by % but they often
255 dictate the typical structural depth of floors. It is reasonable to say that more care will be
256 taken in the design of these beams, and this is reflected by the correlation in the graph.

257 Conversely, the core/trimmer/tie beams (in grey) will often be the ones least thought
258 about. They are often required to ‘fill in the gaps’ within the structure, used to tie
259 columns together and frame out slab edges and lift cores, *etc.* It is generally the case that
260 a typical size might be taken for these beams, often a 203 Universal Beam section, as
261 this represents the lowest section size preferred by fabricators. The chart also indicates
262 a correlation between increasing ratios of these member types and a reduced average
263 utilisation ratio. Primary beams generally appear to have little impact on the average
264 utilisation ratio. The lower percentage of these is likely to be a factor, however as they
265 are often the deepest beams within a floor plate it is likely that more detail will have
266 been put into their design.

267 Edge secondary beams appear to follow a similar pattern to the core/trimmer/tie
268 beams. This is likely down to the fact that the Engineer will utilise identical sections to
269 the general internal secondary beams, which will render these members inefficient due
270 to the reduced loading. It must be noted that often the analysis of these members may
271 not include an accurate assessment of the cladding loading, so the data is slightly less
272 reliable.

273 The large variation observed is unsurprising as every project is unique, but also
274 highlights the challenges in distinguishing any particular design trend. The 3 model
275 buildings are very different and have been excluded in the following analyses (see for

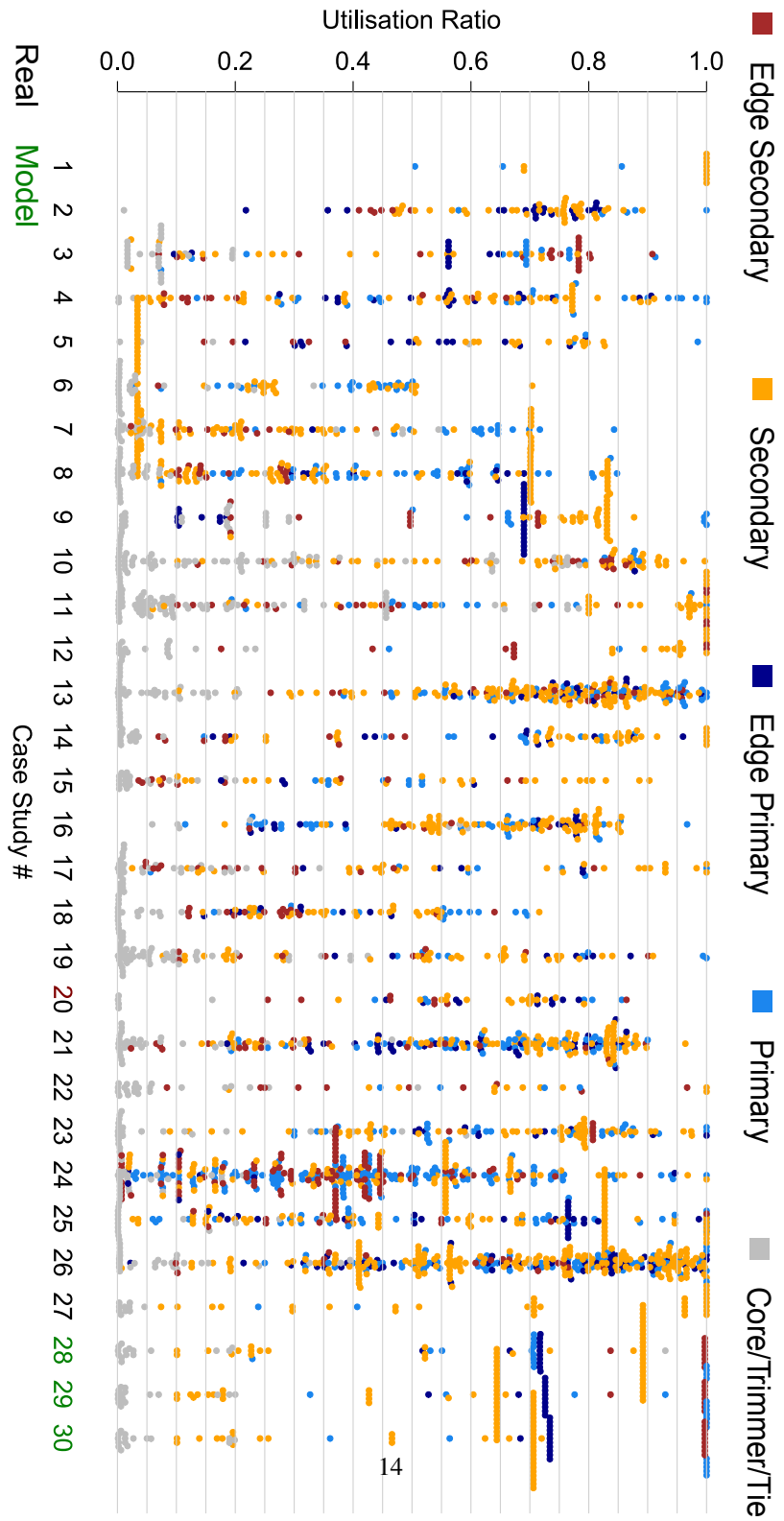


Figure 2: Overview of the projects analysed in the study. Every dot is a beam, and the colours reflect their roles in the designs. This plot illustrates the considerable differences between designs.

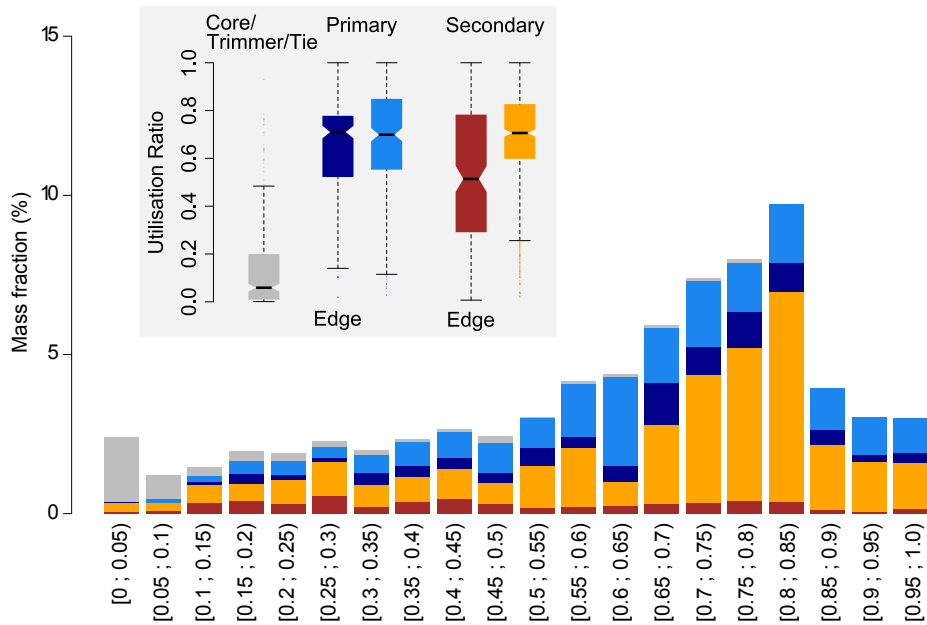


Figure 3: Utilisation ratio as a function of beam type in the studied projects (excluding models). The colours mark the beam types, with the overall distribution of UR as a function of beam type represented as box-plots in the insert. the notch on the box-plots indicates the standard error of the medians. Non-overlapping notches indicate statistically significantly different medians.

276 example Figure 9: the distribution of UR and beam types is clearly different from real
 277 structures).

278 3.2. Overall design

279 The overall dataset exhibits a striking distribution of the UR: a peak at very low UR
 280 corresponding to the core, trimmers and ties, a main peak at 0.8 with a long tail towards
 281 lower UR and a sharp drop-off beyond that point (Figure 3). This profile holds for both
 282 primary and secondary beams. However, the peak for primary beams is less sharp.
 283 Edge secondary beams have significantly lower utilisation ratio. This is likely because
 284 their sizes, notably their depths are prescribed by the links to the façade and therefore
 285 they cannot be optimised. Further, as cladding details were not consistently known no
 286 allowance for their loads has been applied in this analysis, artificially lowering the UR.

Figure 4 shows the amount of steel m_{unused} which is underused in the structure. This

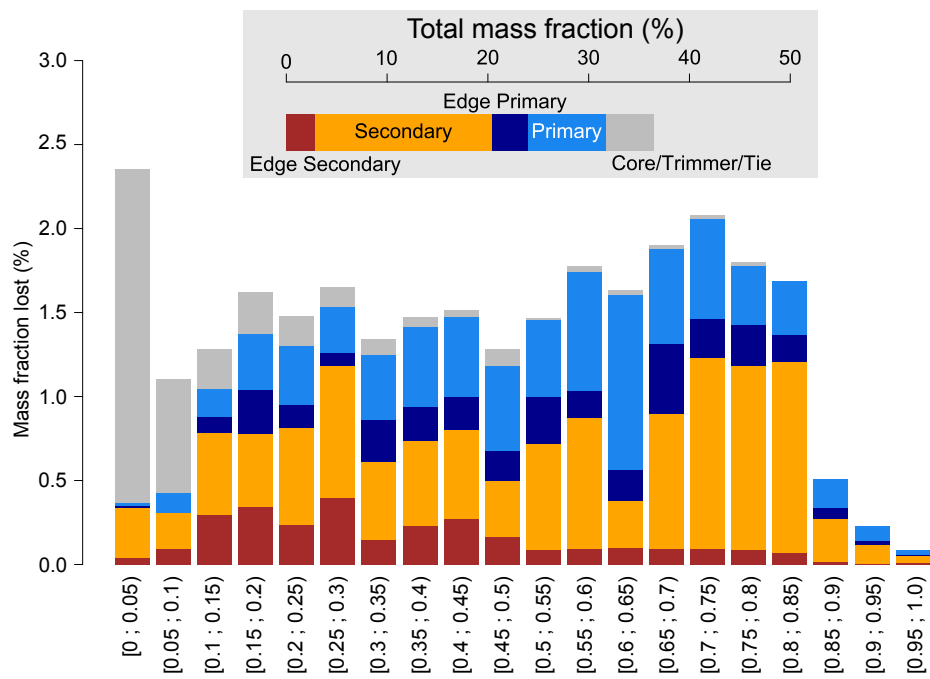


Figure 4: Under-utilisation of the steel mass in the elements analysed in this study. This figure describes how the unused mass is distributed as a function of the role and u_r of the elements.

value is obtained for each element of mass m_{element} as:

$$m_{\text{unused}} = m_{\text{element}}(1 - \text{UR}) \quad (6)$$

287 The graph indicates that the steel mass, aside from the cores/trimmer/ties is underutilised
288 fairly uniformly: there are no obvious patterns in underutilisation. Importantly, the large
289 drop after 0.8 is not due to beams in the 0.8-1.0 being very very light, or all very close
290 to $\text{UR} = 1$, but is rather due to the fact that very few beams have $\text{UR} > 0.8$.

291 3.3. Reproducibility of the results

292 The key observation is the characteristic distribution of UR across projects.

To verify that this observation was statistically significant, a convergence analysis was performed. All permutations — or when this number was too large, at least 20000 permutations — of all subset sizes of case studies have been analysed for their average UR distribution. This is reported on Figure 5 with, for reference, the theoretical convergence for samples with random UR distribution. If the UR of case studies were randomly distributed, this study should have identified the real mean distribution of UR within 9.6 % using the usual expression for the standard error ϵ_{std} .

$$\epsilon_{\text{std}} = \frac{E}{\sqrt{n}} = \frac{50}{\sqrt{27}} \approx 9.6\% \quad (7)$$

293 With E the expected value for the difference between two uniformly distributed numbers
294 between 0 and 100 % (50 %) and n the number of samples. In this case, the calculated
295 values are all under the theoretical curve, which indicates that the distribution of UR in
296 all case studies is related to the average UR distribution we report. If this were not the
297 case, we would expect the calculated points to lie on or close to the theoretical line.

298 The average difference between the weight of any 0.1-wide UR bin in any case study
299 and the average from all case studies is 2.0 % in relative terms. By comparison, the
300 theoretical value would be $\frac{1}{\sqrt{27}} = 9.6\%$ if the UR of beams were uniformly distributed.
301 This indicates that UR distributions from case studies are always more similar to the

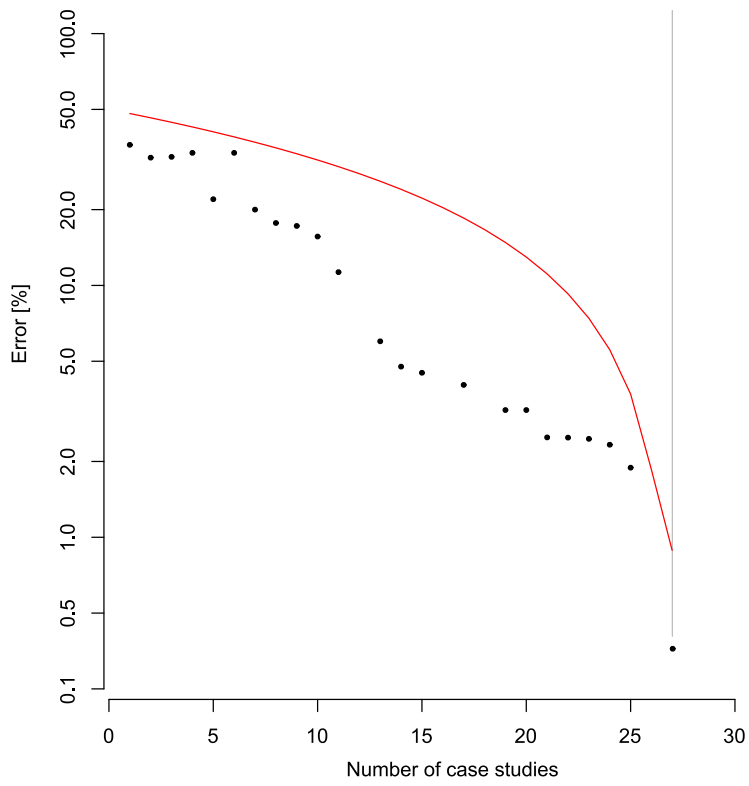


Figure 5: Average norm of the difference between the average UR distribution of a subset of n case studies and the UR distribution of all studies. The red line is the theoretical convergence for random distributions of UR.

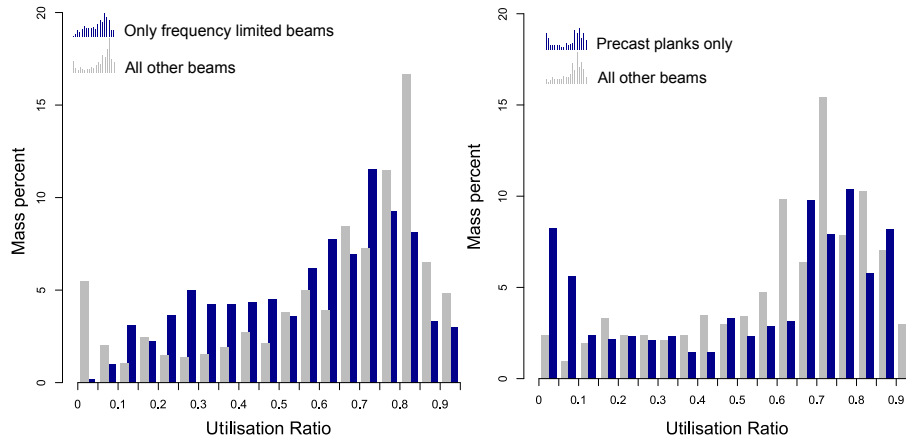


Figure 6: Distribution of the UR where the beams where the limiting factor is natural frequency have been separated (left) and where the precast planks have been separated (right). No significant difference in the distribution of UR is found.

302 average UR distribution than to a random one.

303 From this analysis, we can conclude that the global UR distribution we observed is
 304 likely representative of the real UR distribution of all steel-framed buildings of similar
 305 size and age in the UK. Further, we conclude that the UR distribution in buildings is
 306 significantly related to the UR distribution of all buildings¹.

307 3.4. Limitations of the analysis

308 The analysis had to make assumptions, as not all the design parameters were known
 309 in all cases. This in particular could affect the reliability of the analysis of composite
 310 floor plates. A complete natural frequency analysis needs to take into account the
 311 connections to the columns, which was not possible in this work. To verify that the
 312 results were independent of the floor type – precast or composite – and that the possible
 313 errors in frequency analysis do not affect the overall distribution of UR, we present
 314 the distributions where beams possibly affected by these issues have been removed
 315 (Figure 6).

¹This result is not trivial: completely uncorrelated random distributions will still converge to an average.

316 No significant difference in the distribution of UR is found when those possibly
 317 confounding factors, floor technology and possibly erroneous calculation of the natural
 318 frequency, are controlled for. The higher noise of the distribution is explained by the
 319 smaller sample sizes.

320 *3.5. Role of design methods*

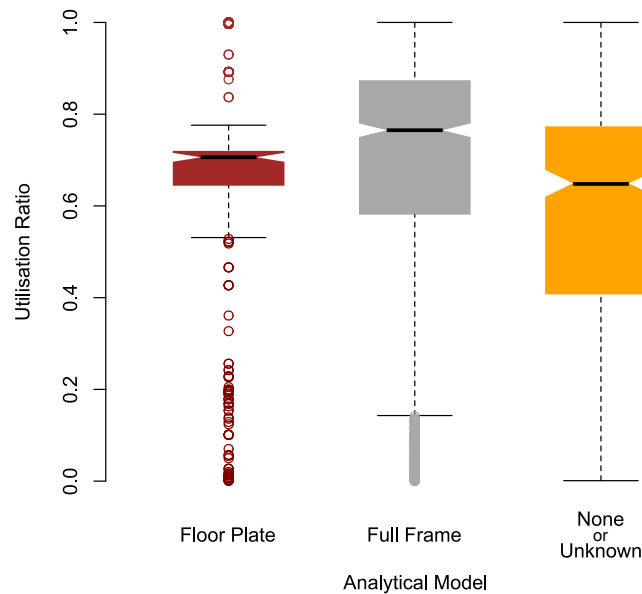


Figure 7: Box-plot of the utilisation ratios of the beams analysed for this paper as a function of the choice of model. The 'Floor Plate' only cover model structures. The beams with 'Unknown' analytical model are likely to have model 'None' but this could not be ascertained. The notches mark the standard error of the median: non-overlapping notches indicate statistically significantly different medians.

321 The analytical models used to choose the beams in each of the case studies were
 322 (Figure 7):

323 **Floor plate** models were only used for the model buildings. They treat all the beams in
 324 the modelled floor as a single unit.

325 **Full frame** models take into account the behaviour of the complete frame of the build-
 326 ing. They can be used to select the optimal beams.

327 **None** is the label describing the beams calculated using pen-and paper models. Without
328 an automated calculation method, it is more labour intensive to choose the optimal
329 beam amongst the choice of UK universal sections.

330 **Unknown** describes the beams where we could not be certain which analytical method
331 was used. However, due to the age of the designs, it is very likely that they should
332 be counted in the ‘None’ category. We found that the average utilisation ratios
333 was the same in the none and unknown cases.

334 The beam designed without analytical models (‘None’ and ‘Unknown’) have a mean UR
335 of 0.64 *versus* 0.76 for the cases studied designed using full frame computer models.

336 *3.6. No relationship between cost and UR*

337 Structures can be very differently priced, and this could be expected to have an
338 impact on the UR, as rationalisation of the section sizes would seem a more attractive
339 proposition when the budget is tight. However, we found no correlation between the
340 price per square metre in the sample and the median UR of the beams. This suggests that
341 the budget does not affect the overall optimisation of the structures (Fig. 8).

342 The cost of the buildings has not been corrected for their age as we also could find
343 almost no correlation between age and price: the projects are too different and too
344 geographically spread.

345 *3.7. Optimisation process during the design*

346 The case studies cover structures at different stages of the design process. These
347 are ‘Preliminary’, which are quite rough beam layouts, ‘Tender’ which are optimised
348 designs produced to gain contracts and ‘Construction’ which reflects the utilisation
349 ratios of projects sent for fabrication and erection (Figure 9).

350 The density plots from Figure 9 reflect the distribution of the mass of steel in the
351 floors as a function of their utilisation ratios. These density plots have been generated
352 using the R software using identical smoothing kernels. The model structures have been

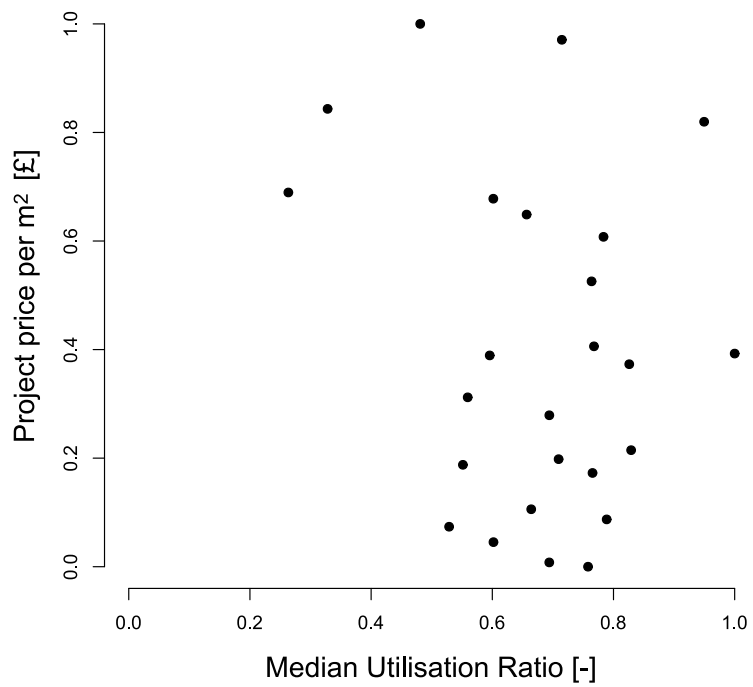


Figure 8: No correlation is found between the price per square metres (normalised between 0 and 1) of the analysed buildings and the UR.

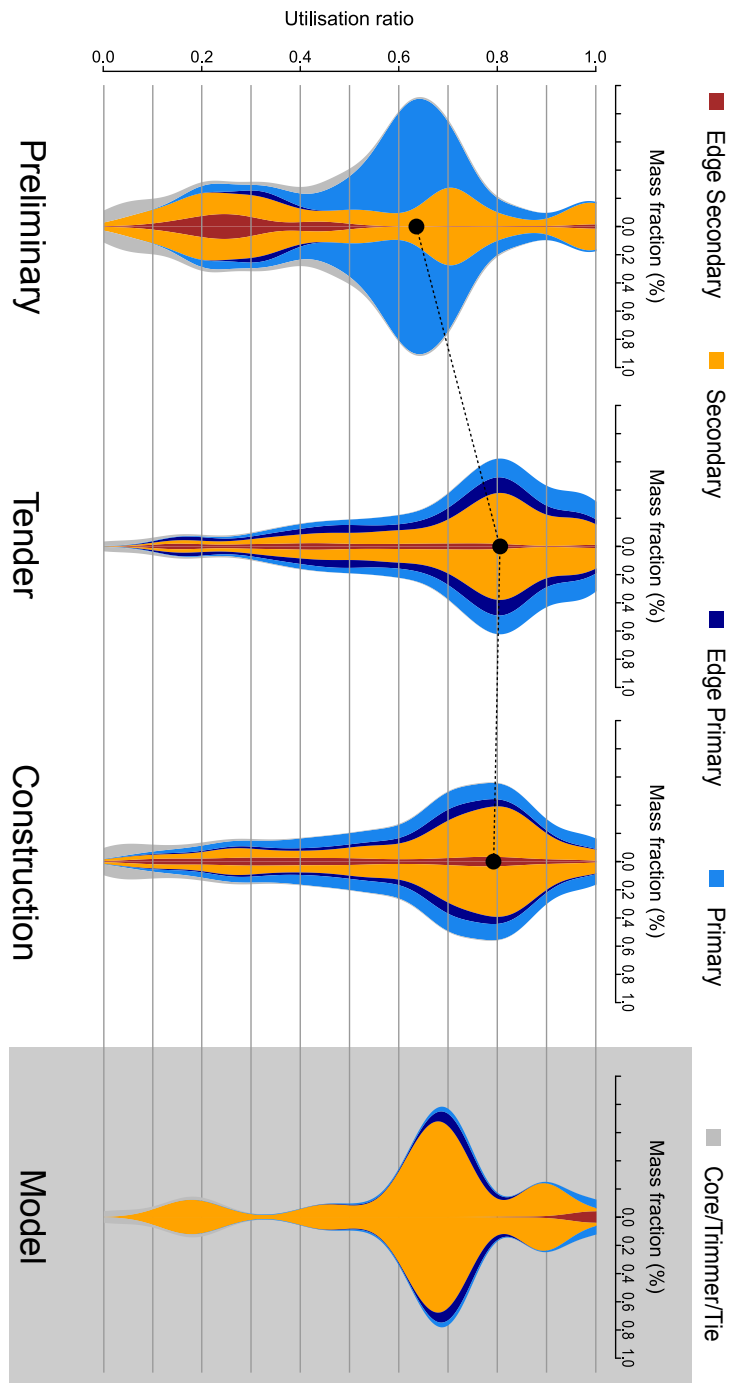


Figure 9: Density plot of the utilisation ratios of the analysed beams as a function of the project stage. The black dots indicate the mode UR .

353 excluded as they do not reflect real design practice; interestingly, they recall preliminary
354 designs. Cores, trimmers and ties are found at the tail at the low end of the UR distribution,
355 and a peak at $UR = 0.8$ is observed. In preliminary designs, a large number of low UR
356 load-bearing elements are present, and the mode UR is only 0.64.

357 *3.8. Regularity and efficiency*

358 A key hypothesis put forward to explain the unused mass of frames in the previous
359 study was that designers ‘rationalise’ their designs, optimising the section which bears
360 the largest loads and using it everywhere else. If this were the case, we should observe
361 that more regular designs where the effect of rationalisation is small to be more efficient.

362 Such an effect is not visible for any of the regularity measures used (Figure 10).
363 Rather, it would seem that the efficiency of the design (measured by the mean utilisation
364 ratio) is independent of the shape and mass of the building frame.

365 **4. Discussion**

366 The distribution of frame mass according to its utilisation ratio follows a charac-
367 teristic pattern first observed in (Moynihan and Allwood 2014), with a similar mean
368 UR of 65 % *versus* 55 % in the earlier study. We observe the same pattern in this study,
369 indicating that the selection of case studies is consistent with the previous findings, and
370 that the pattern is a fundamental characteristic of the current design practice (Figure 3).
371 The pattern is independent of whether the beam elements have UK universal beam or
372 column sections, or are fabricated. Therefore, the under-utilisation of the steel cannot
373 be attributed to the usage of less-than-perfect universal sections. Further, the large range
374 of available sections allows UR to be as high as 0.95 in many cases.

375 Although the the change of a single beam could change the overall behaviour of the
376 structure, this is not a factor which was considered in this analysis: The most important
377 effects concern stability, which would depend on the columns – which were not analysed
378 – and vibration – which was computed on a beam-per-beam basis as discussed above. In

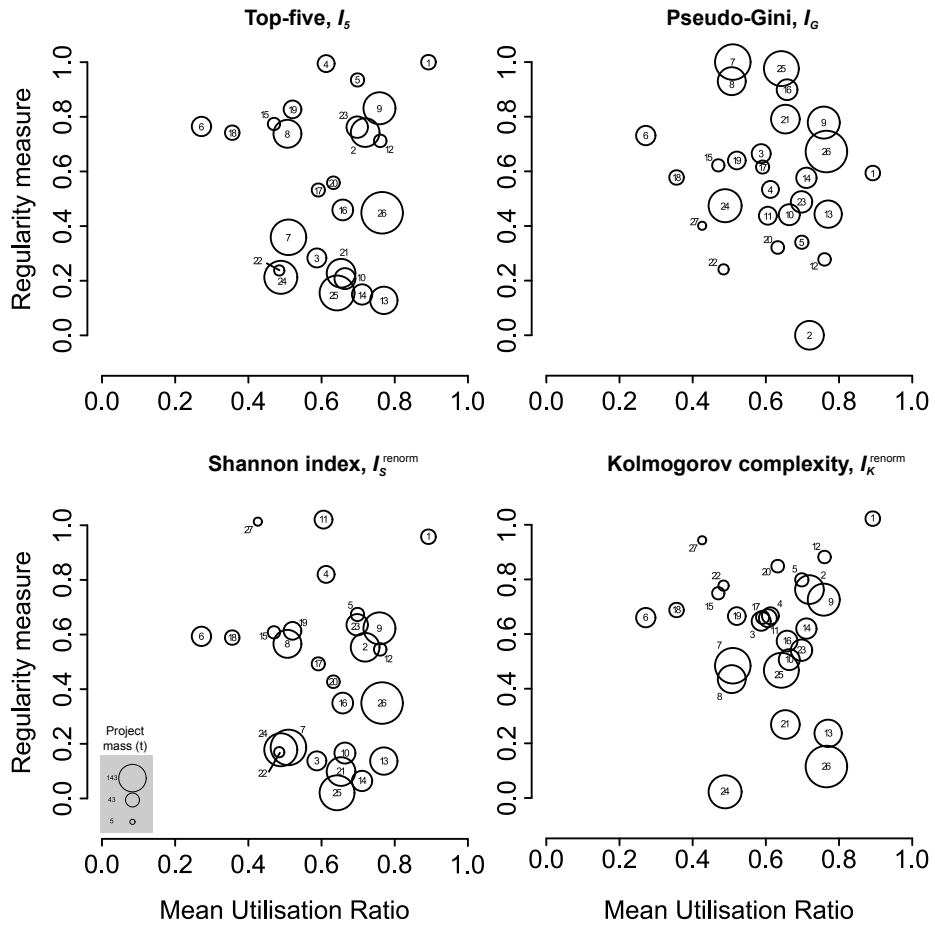


Figure 10: Overview of the regularity of all real projects analysed in the study. Projects are labelled according to their numbers. The area of the circles is proportional to the mass of steel in each case study. The model projects have been excluded. A large commonality is observed between the measures, but none correlate with the utilisation ratio.

379 practice, real designs are never optimised to the level that changing a single beam could
380 significantly affect the spread of the load on the structure as this would be unsafe.

381 Not all beams offer the same opportunity for optimisation. Core/trimmer/ties beams
382 have a very low utilisation ratio as they are either not load-bearing elements, but are
383 required for the stability of the structure, or in the case of cores, bear loads not captured
384 in this analysis. They therefore do not represent lost mass in this analysis. Primary beams
385 are less aggressively optimised in general. Primary beams tend to be less optimised
386 because their dimensions can be dictated by the ceiling heights and they sometimes need
387 to accommodate cells to allow for the passage of services. Secondary beams represent
388 the largest potential for improving the optimisation of designs (Figure 4). Whereas, any
389 change in primary beams later in the design process can trigger many further changes,
390 however it is not clear why *secondary* beams could not be more optimised.

391 Although finding efficient algorithms for optimising the structure itself, *i.e.* the
392 topology of the beams, is still an open question (Kaveh et al. 2012), the optimal choice
393 of beams for a given structure is a solved problem. Indeed, we find that structures
394 designed with modern computer tools have significantly better mean UR (Figure 7) than
395 those designed traditionally. Nonetheless, these remain well below 1. In particular, the
396 ‘Full Frame’ and ‘Floor Plate’ models shows that the computer-aided choice of section
397 effectively improves the median UR of the beams to 0.76 from 0.64. As the design time
398 needed to change the beam selection in a computer model of the frame is very small, the
399 UR is also likely a reflection of the goals of the designer and of the optimisation process.

400 The optimisation process seems to occur predominantly between the preliminary
401 and tender stage (Figure 9) of design. The result of this process is reducing the number
402 of load bearing low UR elements, and in general refining the selection of beams. After the
403 tender stage, most of the design work consists of integrating the services and detailing.
404 It is possible that the utilisation ratio reached at the tender stage are too conservative as
405 the beams do not see their UR further rise as the project goes from tender to construction.

406 Once a project reaches the ‘construction’ stage, it can still undergo further changes, but
407 these are not the direct responsibility of structural engineers. Fabricators will design
408 the connections, and in certain cases optimise the design further, selecting different
409 sections than the ones specified by the structural engineers. None of the projects studied
410 has a sufficient scale for this to have been an economically viable option. Therefore,
411 the designs of the projects analysed in this paper were finalised with the sections as
412 designed by the structural engineers.

413 The regularity analysis did not show any correlation between the complexity of the
414 building, its mass, its cost, the floor technology, and the utilisation ratio of its elements
415 (Figure 10). This indicates that the design strategy leading to the observed utilisation
416 ratio does not depend significantly on the specific building, and must reflect general
417 industry design practices. The hypothesis underlying the notion that rationalisation
418 occurs is that bulk discounts can be had if fewer section types are used. Interviews
419 with fabricators indicated that the bulk discount for using similar sections is small, as
420 operations are highly automatised and fabricators have in general little difficulty to cope
421 with complex orders (private communication).

422 Collectively, these observations indicate that the underutilisation of steel in the
423 frame does not come from difficulties in the design or rationalisation, but rather reflect
424 defensive design practices by engineers. The strong incentive to design safe buildings is
425 compounded by the need to design defensively to guard against changes in requirements
426 during the design process.

427 **5. Conclusion**

428 Following the study by [Moynihan and Allwood](#), we could confirm the principal
429 finding that about 35-45 % of the steel by mass of the load-bearing frame is not required
430 in terms of structural efficiency. However, only part of this is over-design, as the cores,
431 trimmers, and ties representing 6 % of the total mass are necessary for the stability of
432 structures and are mandated by the codes, and a further 3 % of the mass is underused in

433 secondary edge beams whose design is frequently constrained by the available space.
434 Nonetheless, these beams are still oversized in many cases: in general, the smallest
435 available section should be used. The original study had suggested that rationalisation,
436 was a likely culprit for the overdesign. We could show that this was likely not the case.

437 The remainder of the underutilisation can be explained by the design practice of
438 the engineers. To guard against changes during the project, the engineers seem very
439 reluctant to design beams with u_R beyond 0.8. In effect, this results in *at least* 20 %
440 of the mass of steel frames which is not necessary for the purpose of safety or service.
441 Small changes in the design target could create important material savings at no cost. For
442 this to be practical, one should assess how often the defensive design practice prevented
443 re-designs.

444 We could establish that computer-aided design improves significantly the u_R of
445 structures. pushing the mean value from 0.7 to 0.8, a 15 % improvement. General use of
446 automated design tools in the industry will yield substantial savings in embodied carbon
447 and energy. We also found that secondary beams could in general be more optimised
448 than they are currently.

449 There is probably an opportunity, before sending the plans to the fabricator, to
450 perform a round of optimisation. If the model structure is already coded in a computer
451 aided design tool, this operation should not be onerous. Nonetheless, there may be little
452 incentive to do this after the tender depending on the form of the tender. Thus, design
453 and build contracts may offer more scope for optimising designs.

454 Importantly, this study shows that further improvement in the design of steel frames
455 should come from more elaborate strategies, in particular taking into account the design
456 of connections when choosing the sections or designing composite deckings. Such a
457 strategy would allow the selection of thinner sections without otherwise changing the
458 design practice.

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